



NTNU | Norwegian University of  
Science and Technology

# TPG4230 – Field development and operations

Spring Semester 2024

# Information

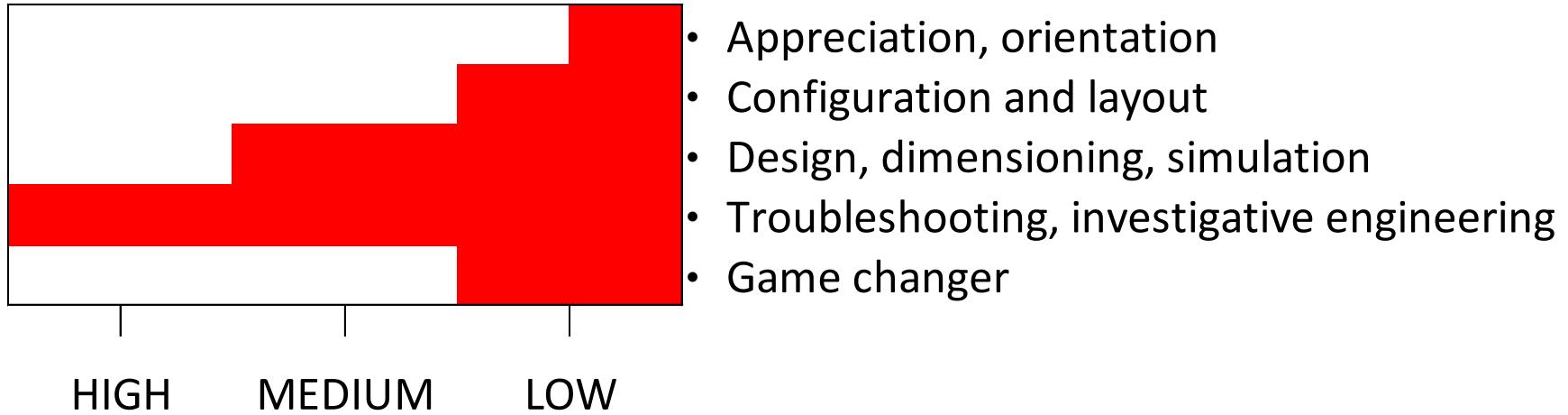
- Lecturer: Assoc. Prof. Milan Stanko (Production Tech) ([milan.stanko@ntnu.no](mailto:milan.stanko@ntnu.no)). Office 510.
- Teaching assistant: Ali Hamdan  
[ali.hamdan@ntnu.no](mailto:ali.hamdan@ntnu.no)
- Lecture schedule
  - Thursdays, 08:15-10:00, P1 (theory and exercises)
  - Fridays, 10:15-11:00, P12 (session with TA)
  - Fridays, 12:15-14:00, P11 (theory and exercises)
- Course [description](#)



# Course content

- Field development workflow
  - Lifecycle, production modes, bottlenecking, onshore vs. offshore.
- Field production performance
  - Computation of production profile, production scheduling, extending plateau, production potential, boosting, networks
- Value chain model, cost estimation and NPV calculations
- Dealing with uncertain parameters in Field Development
  - Monte Carlo, Decision and probability trees
- Offshore structures
  - Layout of production systems, Marine loads
- Flow assurance considerations in field development

# Goals of the course



Basic Engineering Skills required

# Course scope

- A selection of topics and petroleum engineering skills needed for the planning, development and operation of oil and gas fields and to understand, model and analyze their production performance
- Topics typically covered in the course (with varying degrees of detail) are: life cycle of a hydrocarbon field, field development workflow, probabilistic reserve estimation, project economic evaluation, offshore field architectures and production systems, reservoir depletion and field performance, production scheduling, flow assurance, flow design of boosting, field processing facilities, export product control and integrated asset modeling

# Goals of the course

At the end of the course, the student should be able to:

- Understand the process of planning and developing offshore oil and gas fields and some petroleum engineering aspects that govern the operation of such fields.
- Describe the lifecycle of oil and gas fields, the most common offshore field architectures, describe, understand and explain the functionality of the main components of a production system
- Understand and recognize the decision variables, objectives and constraints involved in field planning
- Perform engineering calculations such as probabilistic estimation of reserves, NPV calculations, flow equilibrium in production systems, flow equilibrium in surface networks, compute production profiles using models of the reservoir and production system, and to analyze applications of subsea boosting

# Course scope

- The course will focus on developing digital competences and will include some aspects on energy efficiency, emissions to air and sea, and skill transfer for the energy transition.

## Examples

- Emissions to sea
- CO2 emissions to air
- Field development of CO2 storage fields
- CO2 injection networks

# Course scope

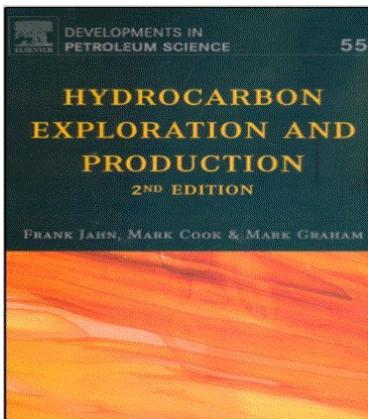
- Practical SI units only (bar, m<sup>3</sup>), not field units.
- Little focus on exploration and subsurface characterization (geology, geophysics, petrophysics, generation of reservoir realizations)

# Information

- Lectures until 26 April (breaking for Easter)
- Consultation time: preferably after class. Try to make an email appointment.
- Reference group – any volunteers?
- **Use Blackboard and the course progress file to navigate the course**
  - Use the forum for Q&A
  - For group deliveries: Join a group before delivering the exercise (even if one person only!!)

# Reference material

- Compendium
- Recommended
- Supplementary
- Hydrocarbon exploration and production (Jahn, Cook and Graham)



# Evaluation

- 100% «written» school exam
  - Digital exam in Inspera, most likely using Excel. No written/handwritten material allowed (equations will be provided in the exam papers)
  - Previous years [exams](#)
  - Examples [2018](#), [2020](#), [2021](#), [2022](#), [2023](#)
  - Make it nice, easy to understand and follow. When provided, use the Excel template

# Evaluation

- Mandatory assignments
  - All assignments must be **approved** to get access to the exam
  - All assignments must be delivered in Blackboard by the deadline
  - Some assignments will be discussed (or solved) in class
  - Individual delivery. Groups of up to 3 people may be allowed for some assignments
  - Nr. of assignments is not yet known, but it is usually 3-4.
  - **Let me know early if there is a deadline conflict with other courses**
  - Those students that took the course last year and **delivered and approved** the homework, do not have to deliver the obligatory exercises this year. They will be approved. All others must deliver the obligatory exercises.

# Teaching

- Flipped classroom
  - Participants watch by themselves pre-recorded videos (ca 45 min) (on [Youtube](#))
  - Live classes every week
    - Discussing further theory, exercises, group work, tutorials on software, Q&A, advanced topics, guest presentations, industry visits?
    - Classes will be recorded, and the recording will be shared on Blackboard

# How to watch the pre-recorded videos

- Watching pre-recorded videos (on Youtube):
  - Watch at higher playback speed (1.5x -2x, Milan speaks slow) 😊
  - At certain time stamps (**or at the end of the video**), the videos have embedded links to: other relevant videos, material and quizzes. Example [link1](#) [link2](#)
  - It is recommended to go through the complete video and click on the links along the way
  - Pause when needed. Try to summarize what was presented with your own words. Take notes. (with pen and paper or on the pdf)

# Quizzes

- Supposed to help you summarize the learnings and consolidate knowledge
- Embedded on videos [link2](#)
- No solution key will be given.
- Some quizzes might be given as mandatory assignment

# Quizzes

- Known bugs
  - When there is a multiple-choice question, if you want to clear your selection, you have to refresh the page 
  - In some browsers one must scroll down sometimes to see the rest of the quiz and the result code
  - Be patient, give it time to load and process information

# Tools

- Excel (+VBA)
- Python (Jupyter Notebook) –using Google Colab
- Hysys (Aspentech, run on ntnu farm) or DWSIM
- IPM (Petex): Prosper, GAP and MBAL

# Questions?

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Outline:

- (cont) Additional comments to course introductory information
- Class activity: oil content in discharged water

Useful links:

<https://www.miljodirektoratet.no/ansvarsområder/forurensning/petroleum/regulering-petroleum/>

<https://www.miljodirektoratet.no/regelverk/konvensjoner/oslo-paris-konvensjonen/>

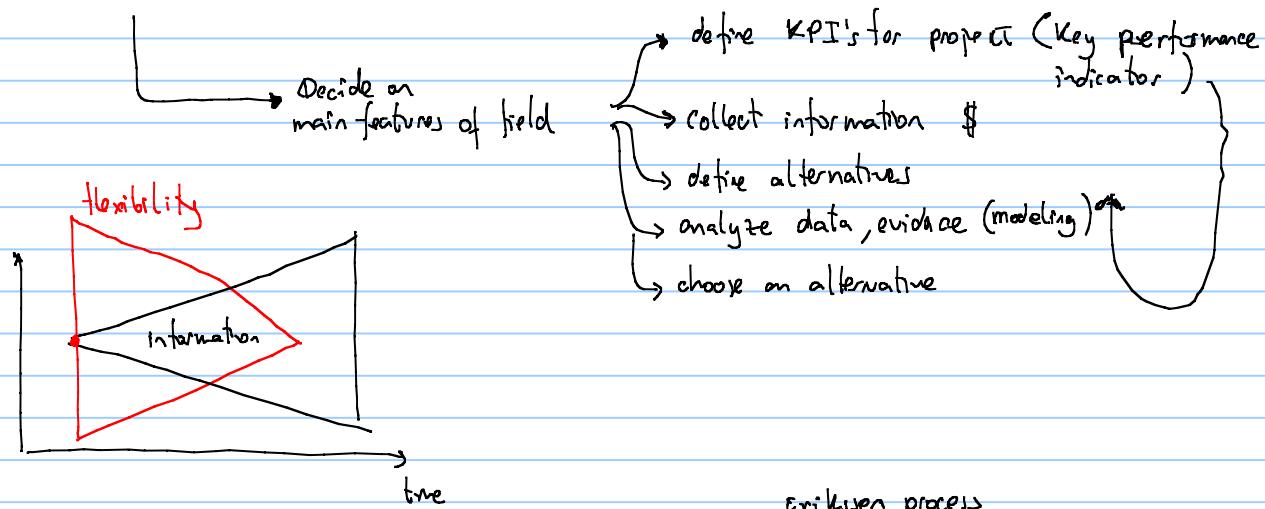
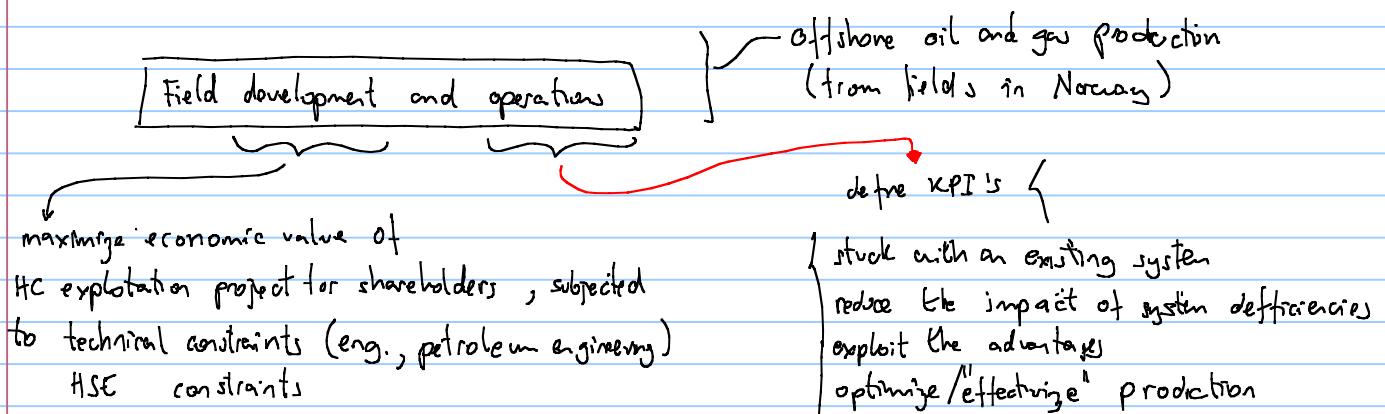
<https://www.ospar.org/convention/text>

## Class activity: Maximum allowable concentration of oil in water for discharge to sea

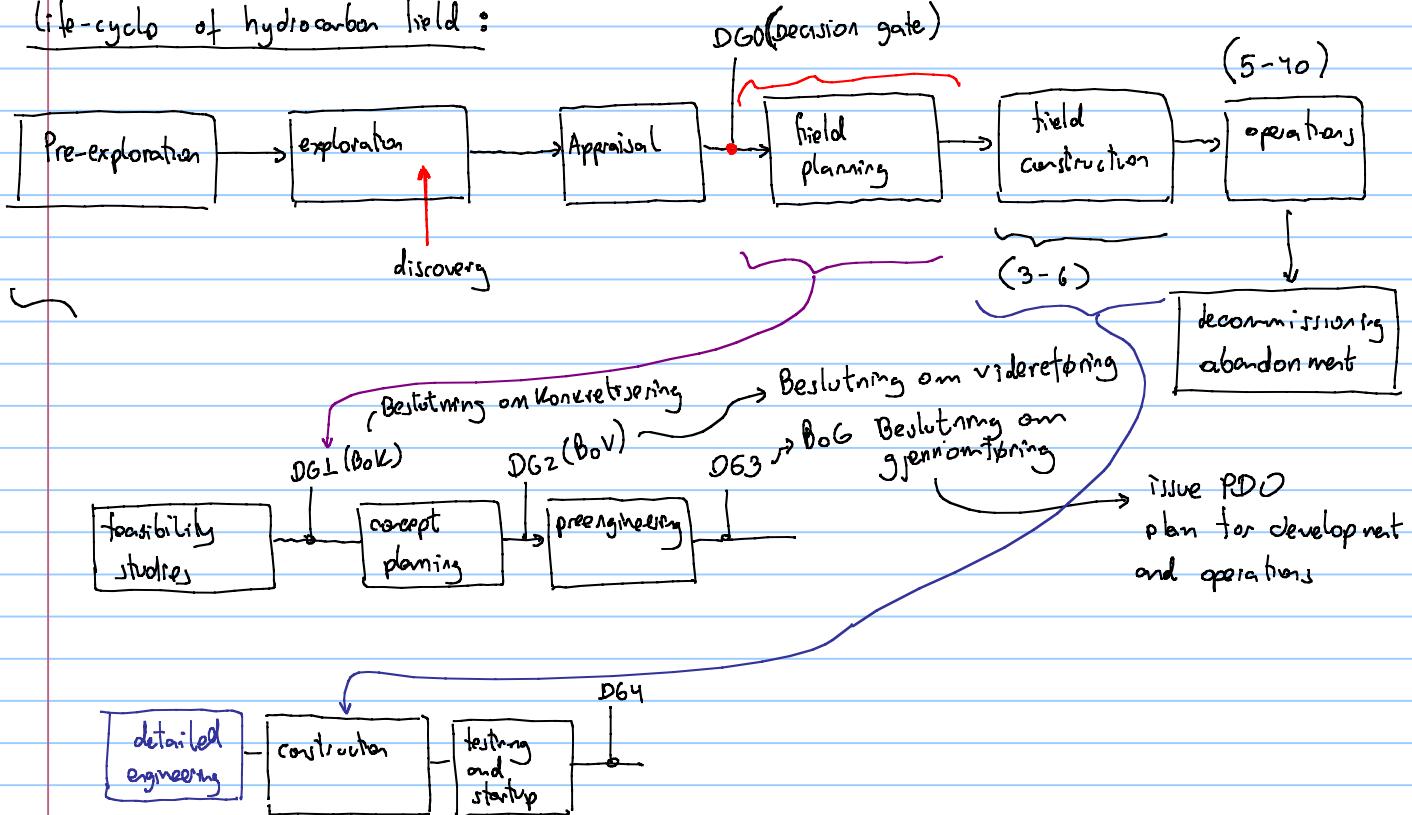
Offshore oil and gas facilities worldwide must keep the hydrocarbon content of discharges to sea below acceptable levels set by authorities. In the North Sea, for instance, the required average concentration of hydrocarbons discharged in effluents, such as produced water, must be below 30 mg/l (monthly average concentration).

Work in groups to conduct the following activities and answer the following questions

1. Read and understand the definition of ppm [https://en.wikipedia.org/wiki/Parts-per\\_notation](https://en.wikipedia.org/wiki/Parts-per_notation)
2. Who is setting the limit of 30 mg/l in the Norwegian Continental shelf? (tip: do an internet search).
3. What is the average concentration of oil in produced water in the Norwegian Continental Shelf? (tip: do an internet search)
4. How is this requirement monitored and enforced? What are the reporting requirements the companies must comply with and to whom must they report? What happens if this is not achieved in a month? (tip: do an internet search)
5. Assume that an oil platform has been discharging produced water (around 500 000 stb/d) with an oil concentration of 10 ppm for 15 days in a month. If the water processing train suddenly has an emulsification problem, that causes the concentration of oil in produced water to increase to 60 ppm, for how many days will the platform be able to produce before shutting down to comply with the 30 ppm-in-a-month requirement?
6. As a follow-up to question 5, how many barrels of oil are released in a month by the oil platform discharging produced water (around 500 000 stb/d) with an oil concentration of 10 ppm.
7. Set a person in your group to be the controller. Ask this person to close their eyes or leave the room while preparations. Using the colorant and the syringe provided, and tap water, prepare two containers, one with a 30 ppm solution of colorant in water, and one with water only. Ask the controller to open their eyes. See if they can identify which one is the one with the colorant.
8. Find out what is the lethal concentration of oil in water for fish (tip: do an internet search)
9. Using the colorant and the syringe provided, and tap water, prepare a container, with the concentration found in task 8. Discuss the differences with the one prepared in 7.

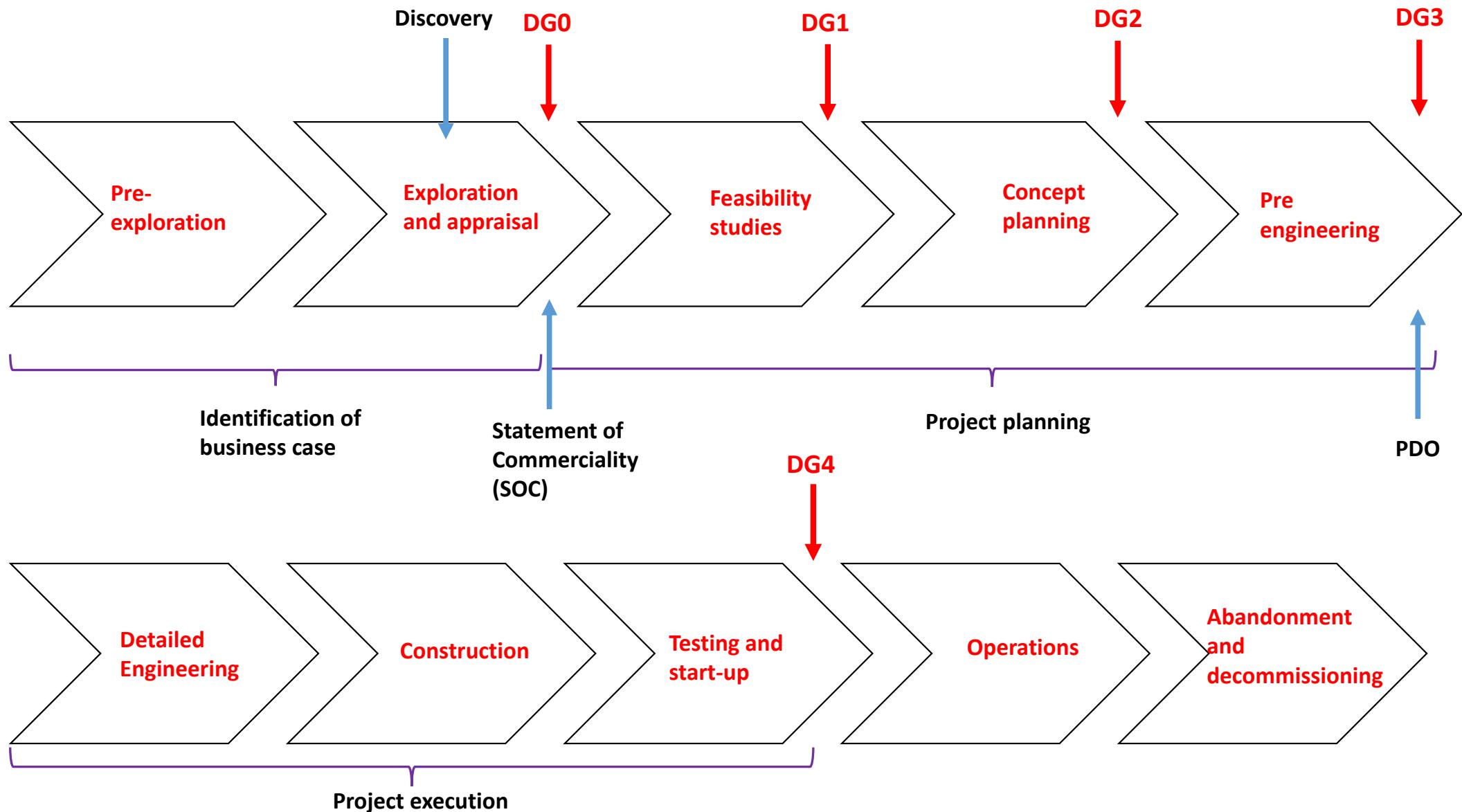


### Life-cycle of hydrocarbon field :

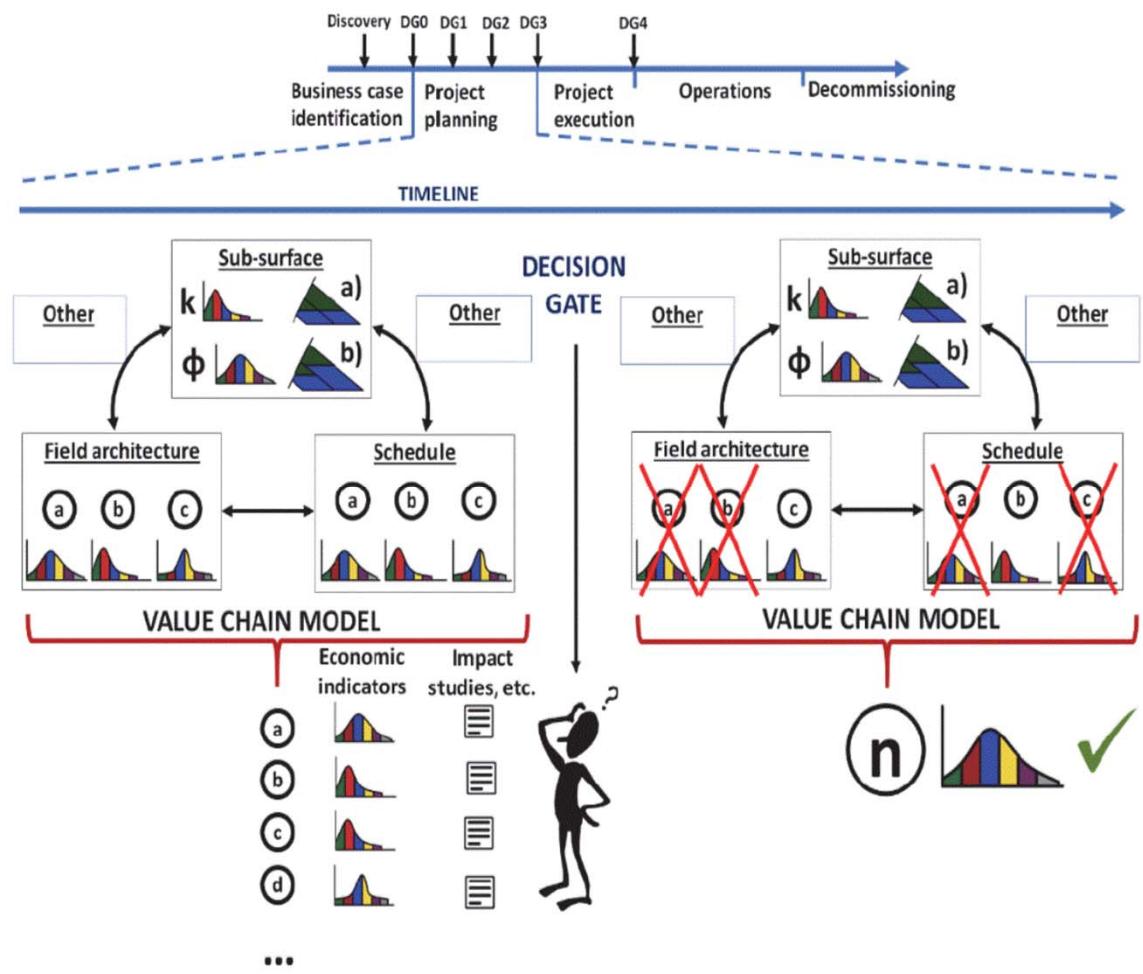


# THE FIELD DEVELOPMENT PROCESS

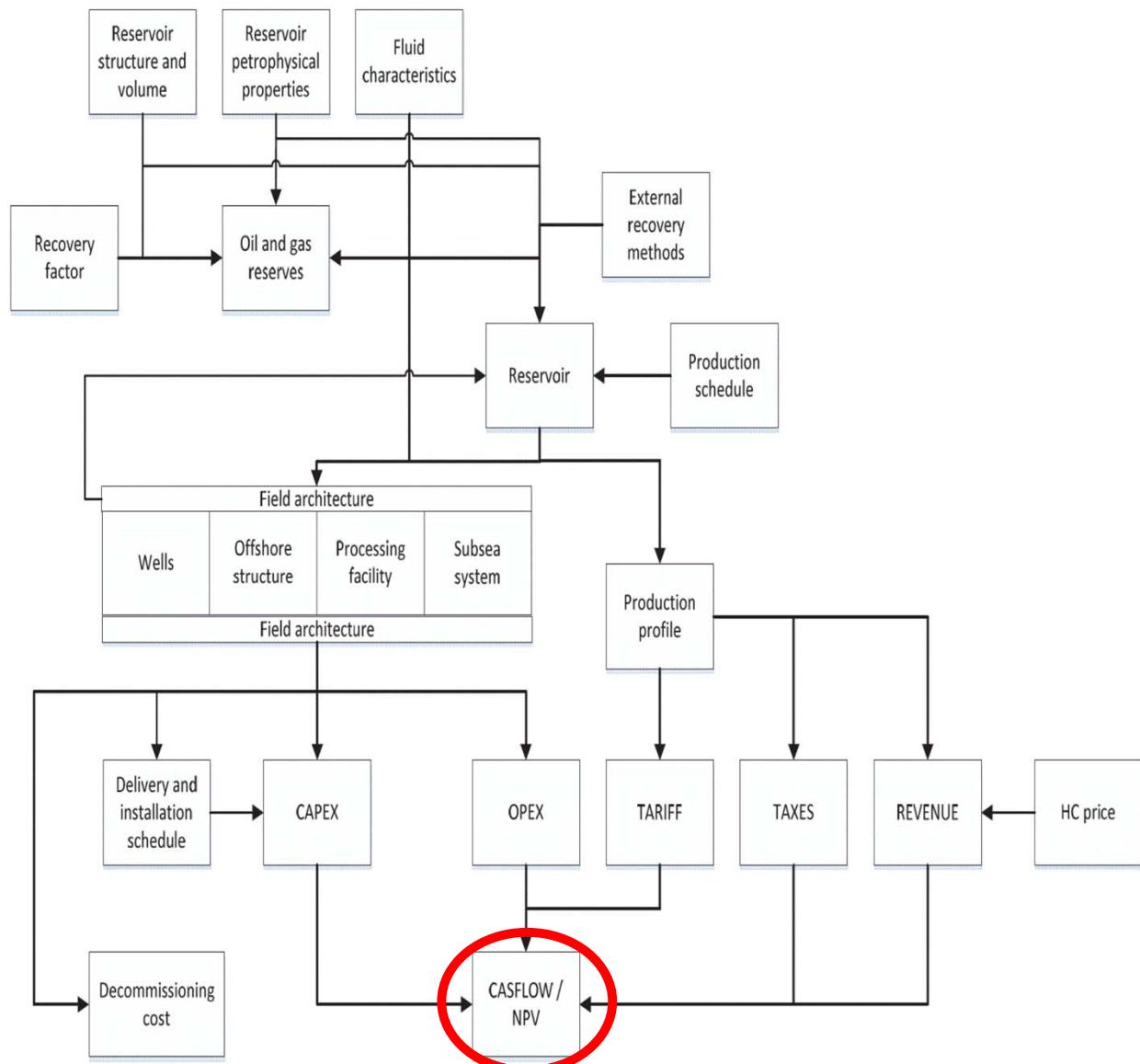
Prof. Milan Stanko (NTNU)

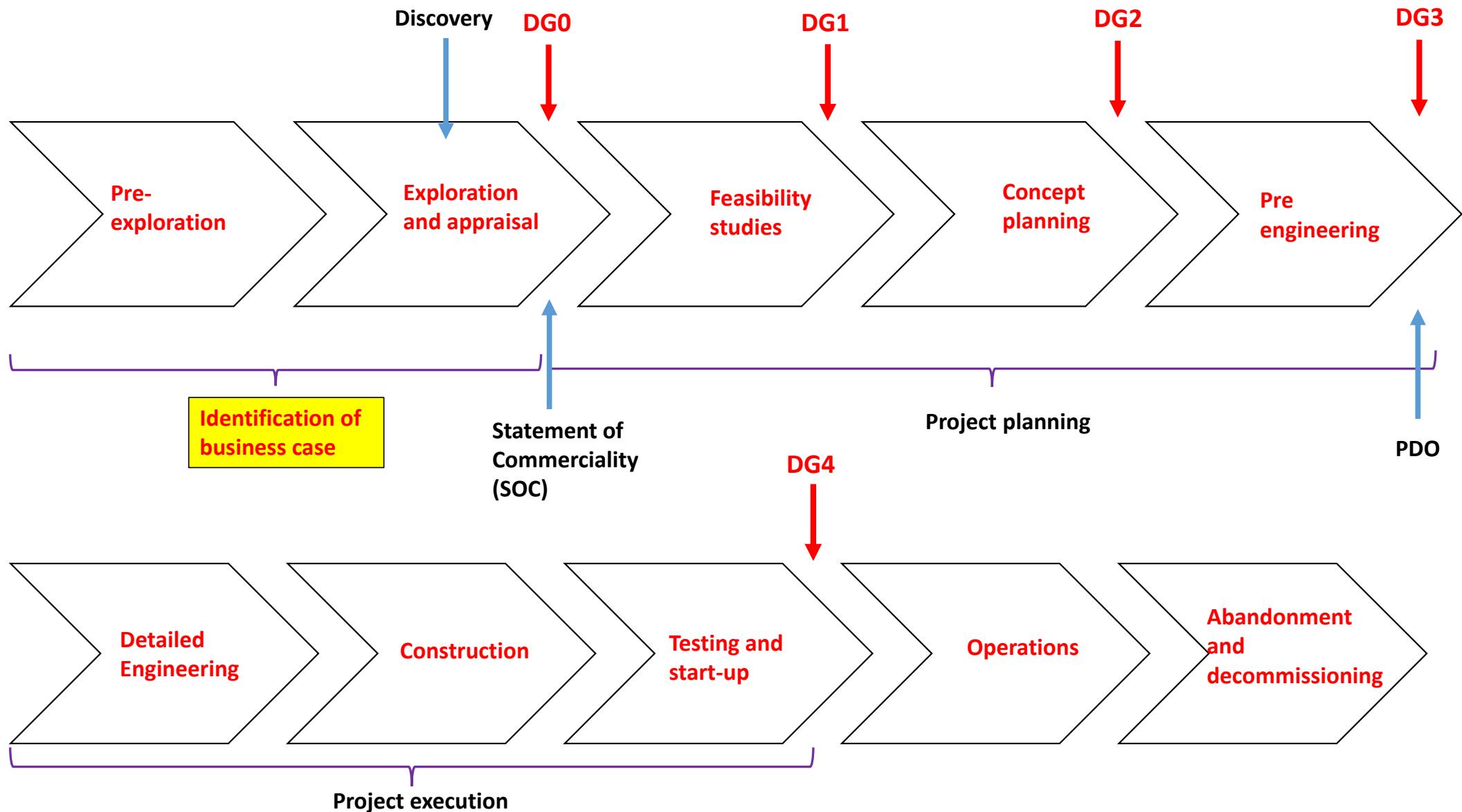


During the field development process a model of the value chain is made based on the disciplines involved and populated with information. Initially there are many alternatives and little information. As time progresses and decisions are taken, the model is expanded, there is more information but less flexibility.



Key performance indicators are computed with the value chain model and are used to take decisions in the decision gate process.





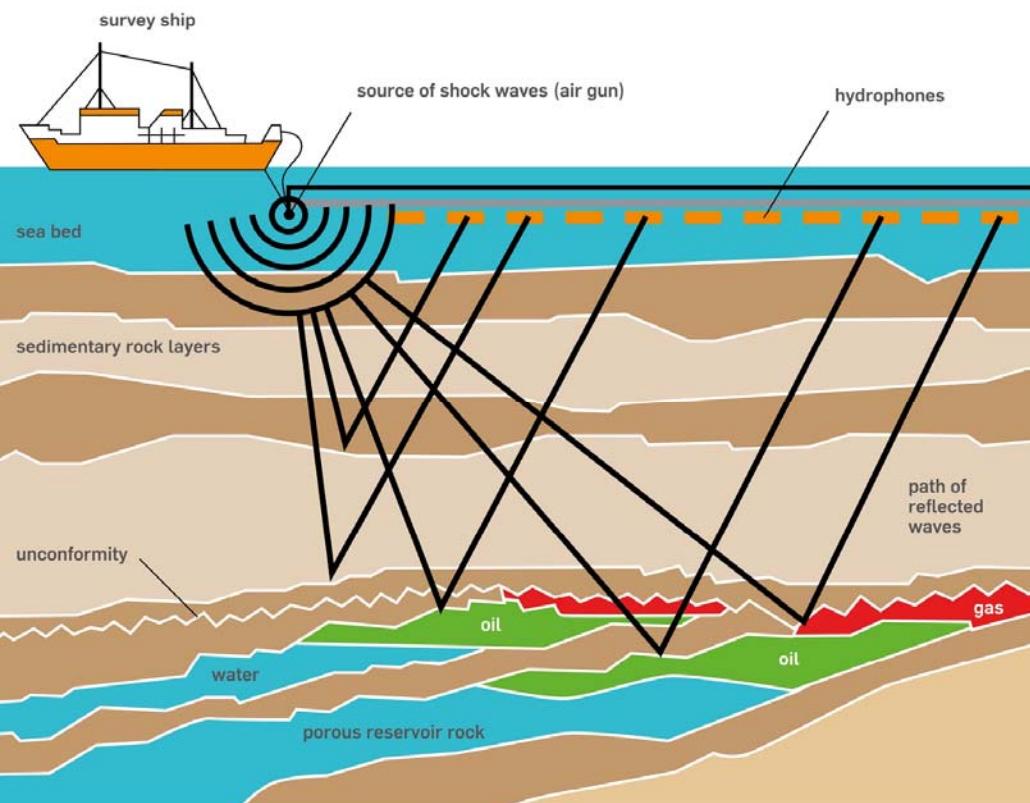
# IDENTIFICATION OF BUSINESS CASE

The main goal of this stage is to prove economic potential of the discovery and quantify and reduce the uncertainty in the estimation of reserves.

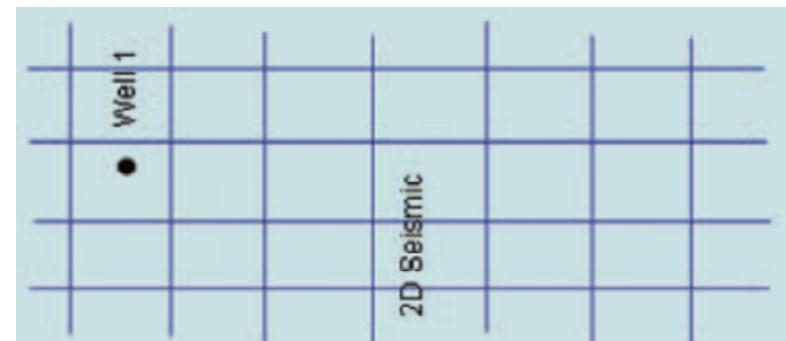
# IDENTIFICATION OF BUSINESS CASE - TASKS

- Pre-exploration – scouting: collecting information on areas of interests. Technical, political, geological, geographical, social, environmental considerations are taken into account. E.g. expected size of reserves, political regime, government stability, technical challenges of the area, taxation regime, personnel security, environmental sensitivity, previous experience in the region, etc.
- Getting pre-exploration access – The exploration license (usually non-exclusive). In the NCS only seismic and shallow wells are allowed. This is usually done by specialized companies selling data to oil companies.  
Area: 500 Km<sup>2</sup>
- Identify prospects.

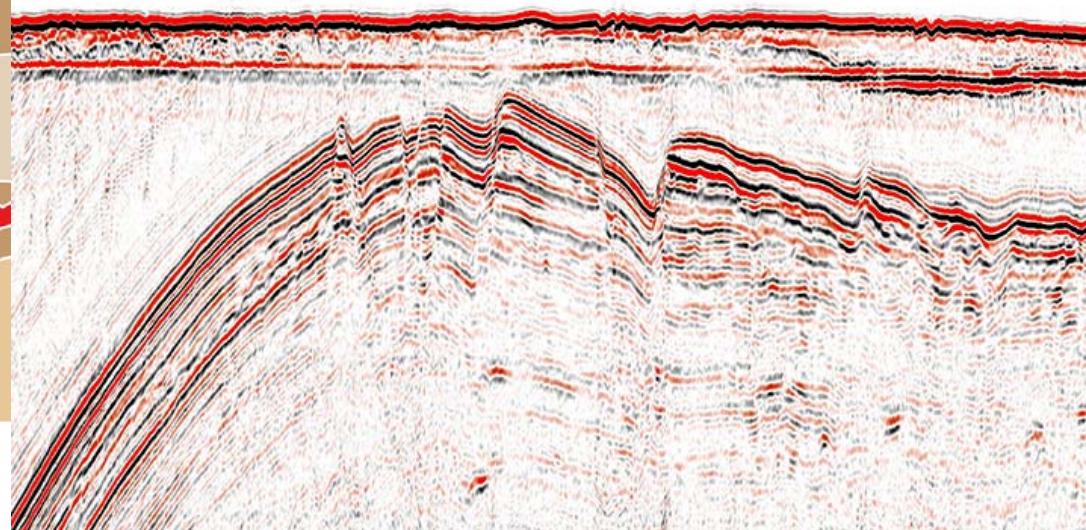
# IDENTIFICATION OF BUSINESS CASE - TASKS



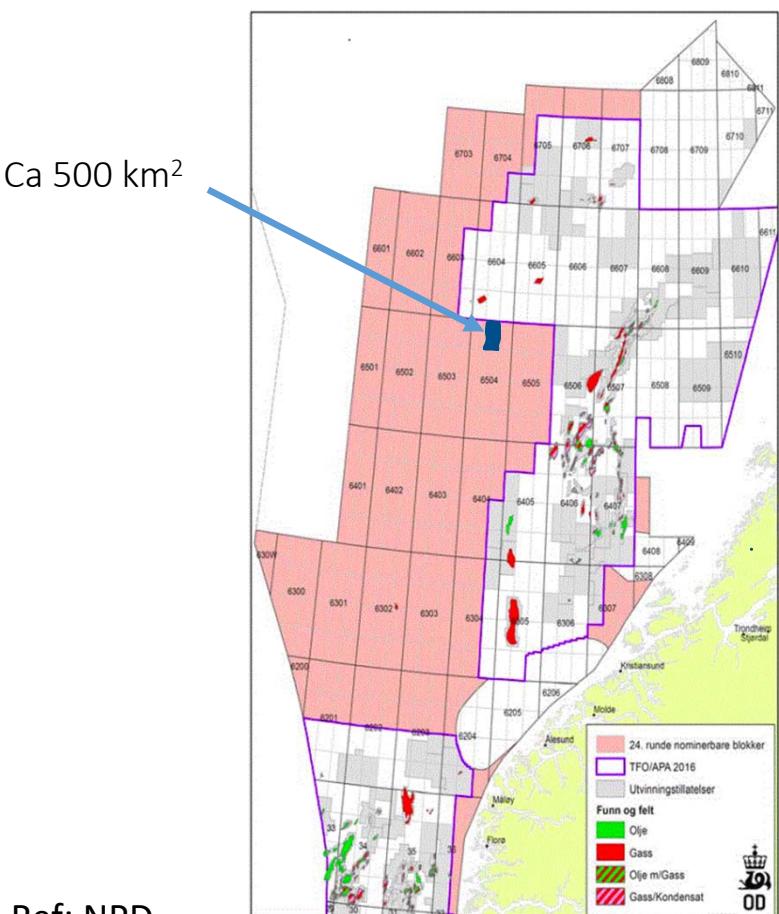
Ref: <https://krisenergy.com/company/about-oil-and-gas/exploration/>



Seismic exploration



# IDENTIFICATION OF BUSINESS CASE - TASKS

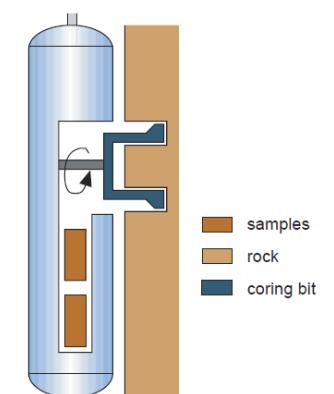
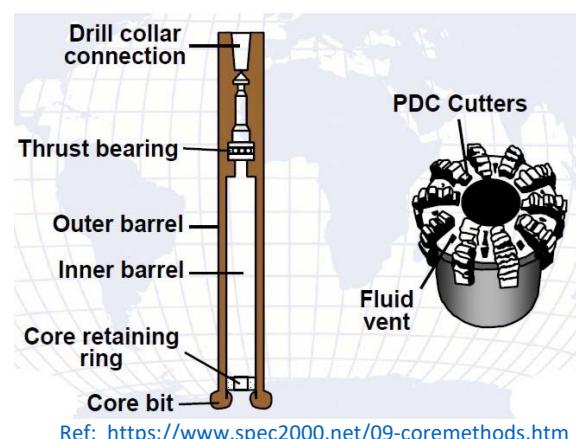


- Apply and obtain exclusive production license (6 years, possible to extend for 30 years). In the NCS: Licensing rounds (frontier areas) or Awards in predefined areas (APA). The current fees (if inactive) are 34 000 NOK/km<sup>2</sup> for the first year, 68 000 NOK/km<sup>2</sup> for the second year and 137 000 NOK/km<sup>2</sup> per year thereafter.

Ref: NPD

# IDENTIFICATION OF BUSINESS CASE - TASKS

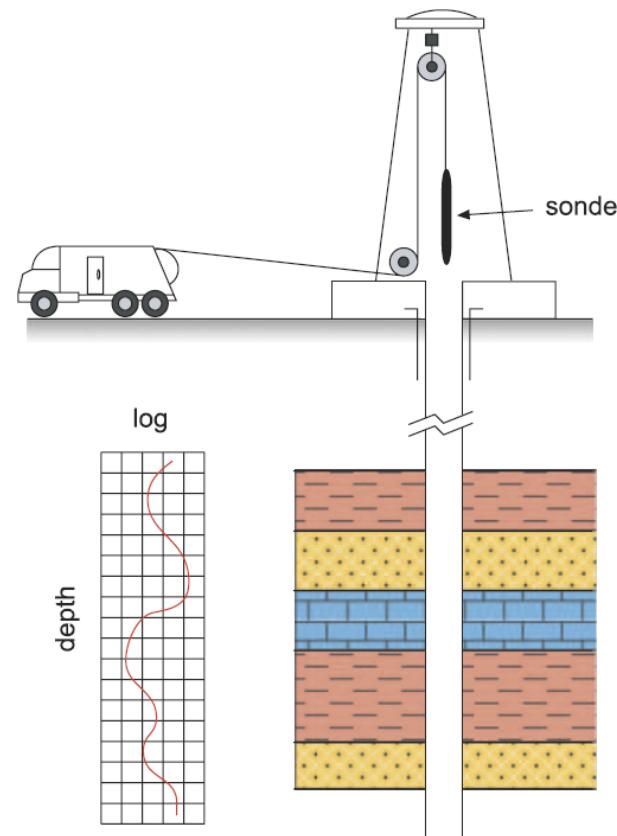
- Exploration. Perform geological studies, geophysical surveys, seismic, exploration drilling (Well cores, wall cores, cuttings samples, fluid samples, wireline logs, productivity test).
- Discovery!



Ref: Hydrocarbon exploration and production, Jahn et al.

# IDENTIFICATION OF BUSINESS CASE - TASKS

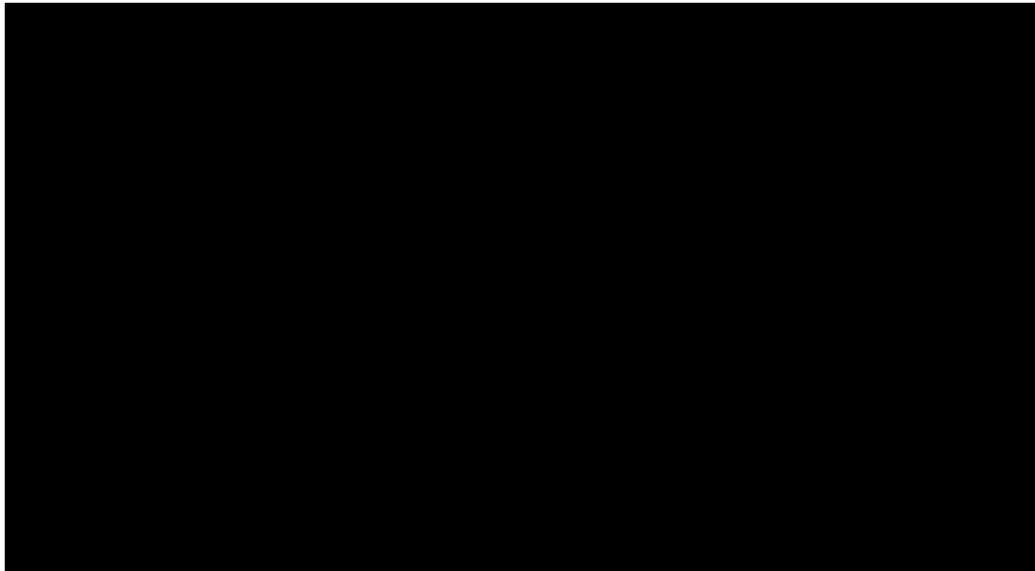
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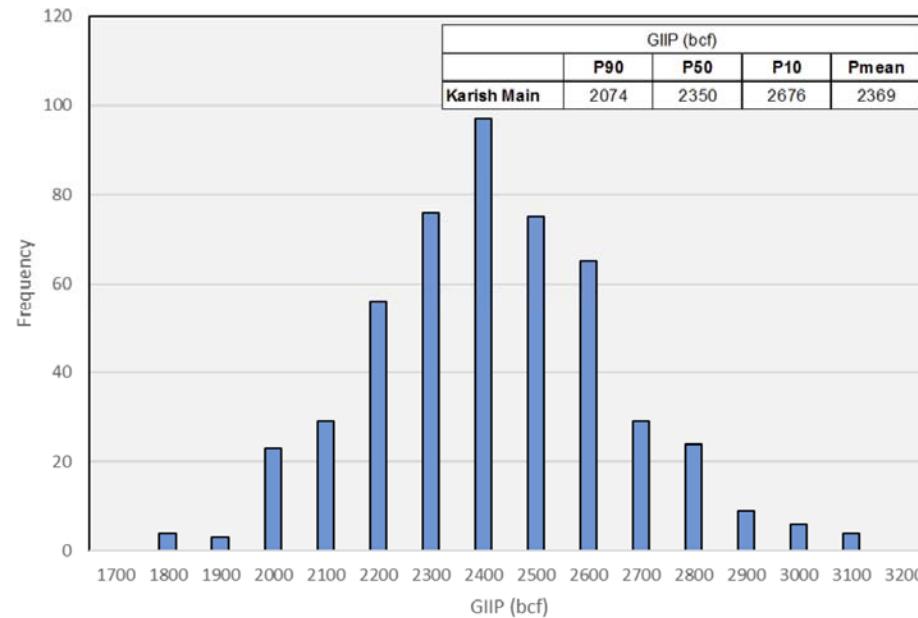
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- Discovery!



<https://www.youtube.com/watch?v=Qd7F8T0IVXU>

# IDENTIFICATION OF BUSINESS CASE - TASKS

- Assessment of the discovery and the associated uncertainty. Risk management:
  - Probabilistic reserve estimation. Identify and assess additional segments.



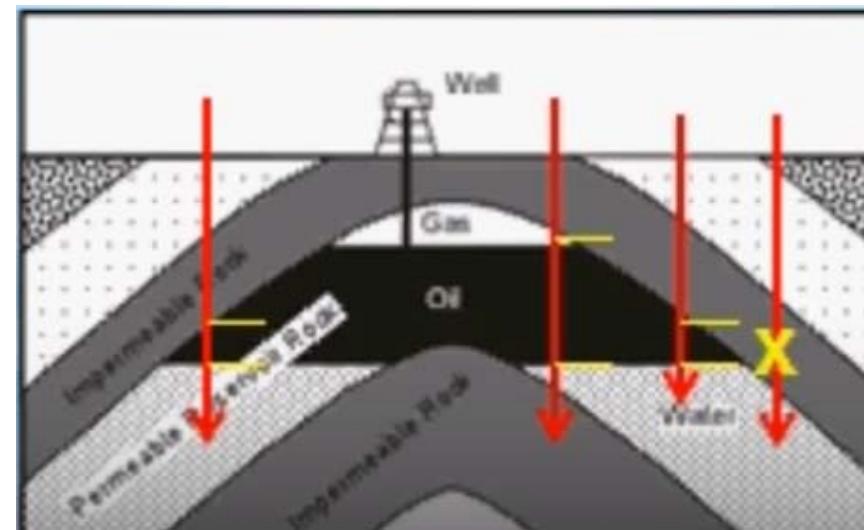
Ref: PDO Karish and Tanin.  
Energean

# IDENTIFICATION OF BUSINESS CASE - TASKS

- Assessment of the discovery and the associated uncertainty. Risk management:
  - Probabilistic reserve estimation. Identify and assess additional segments.
  - Perform simplified economic valuation of the resources.
  - Field appraisal to reduce uncertainty: more exploration wells and seismic to determine for example: fault communication, reservoir extent, aquifer behavior, location of water oil contact or gas oil contact.

# IDENTIFICATION OF BUSINESS CASE - TASKS

- Appraisal

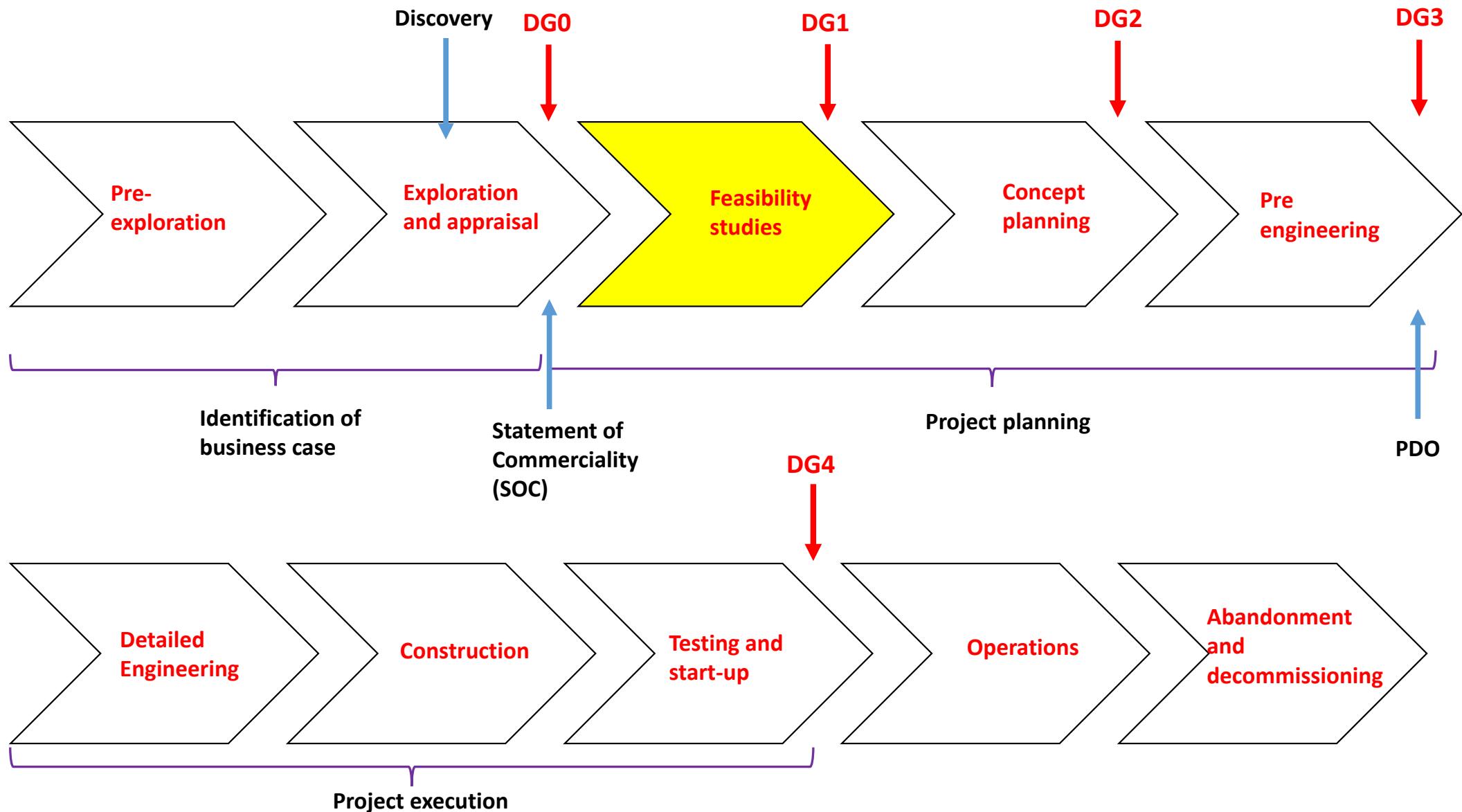


Ref: <https://www.youtube.com/watch?v=-e9jjnsquGI>

# IDENTIFICATION OF BUSINESS CASE - TASKS

DG0:

- Issue a SOC (Statement of Commerciality) and proceed with development.
- Continue with more appraisal
- Sell the discovery.
- Do nothing (wait)
- Relinquish to the government

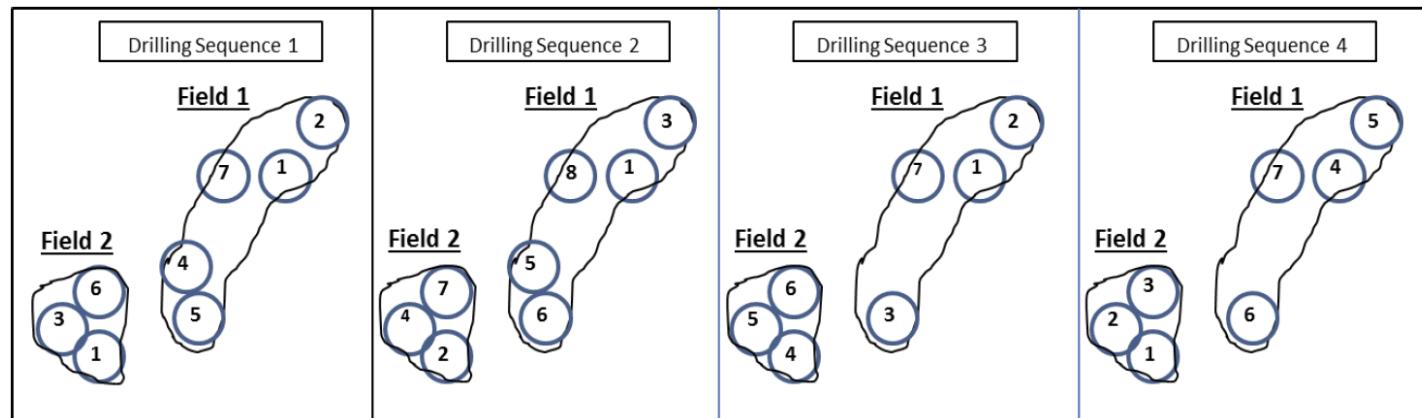


# FEASIBILITY STUDIES - TASKS

**OBJECTIVE:** Justify further development of the project, finding one or more concepts that are technically, commercially and organizationally feasible

- Define objectives of the development in line with the corporate strategy.
- Establish feasible development scenarios.
- Create a project timeline and a workplan.

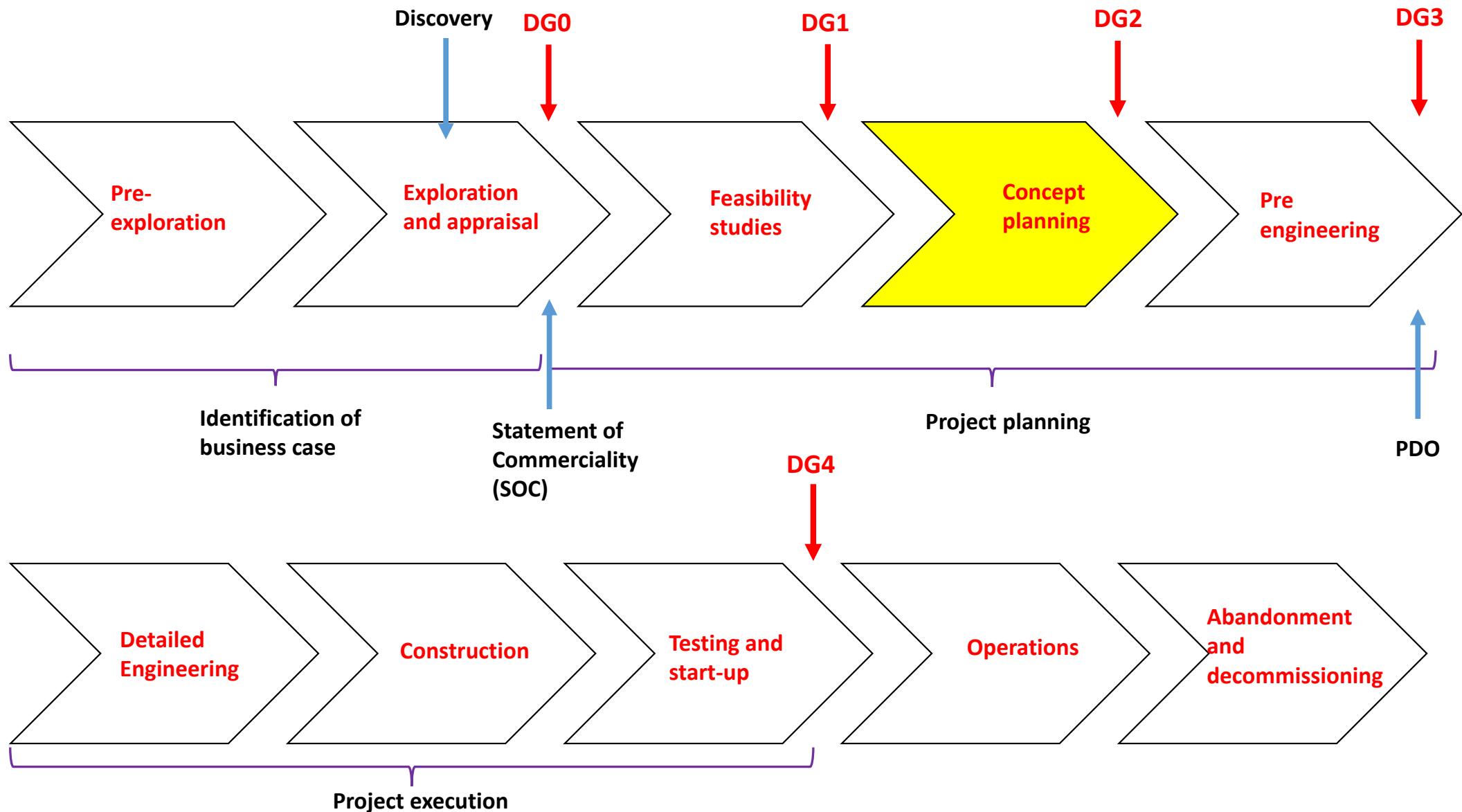
# FEASIBILITY STUDIES - TASKS



Ref: UTC 2017, Strategies, methods and tools for development of subsea fields, Skogvang and Løken.

# FEASIBILITY STUDIES - TASKS

- Identify possible technology gaps and blockers.
- Identify the needs for new technology.
- Identify added value opportunities.
- Cost evaluation for all options (at this stage, cost figures are  $\pm 40\%$  uncertain)



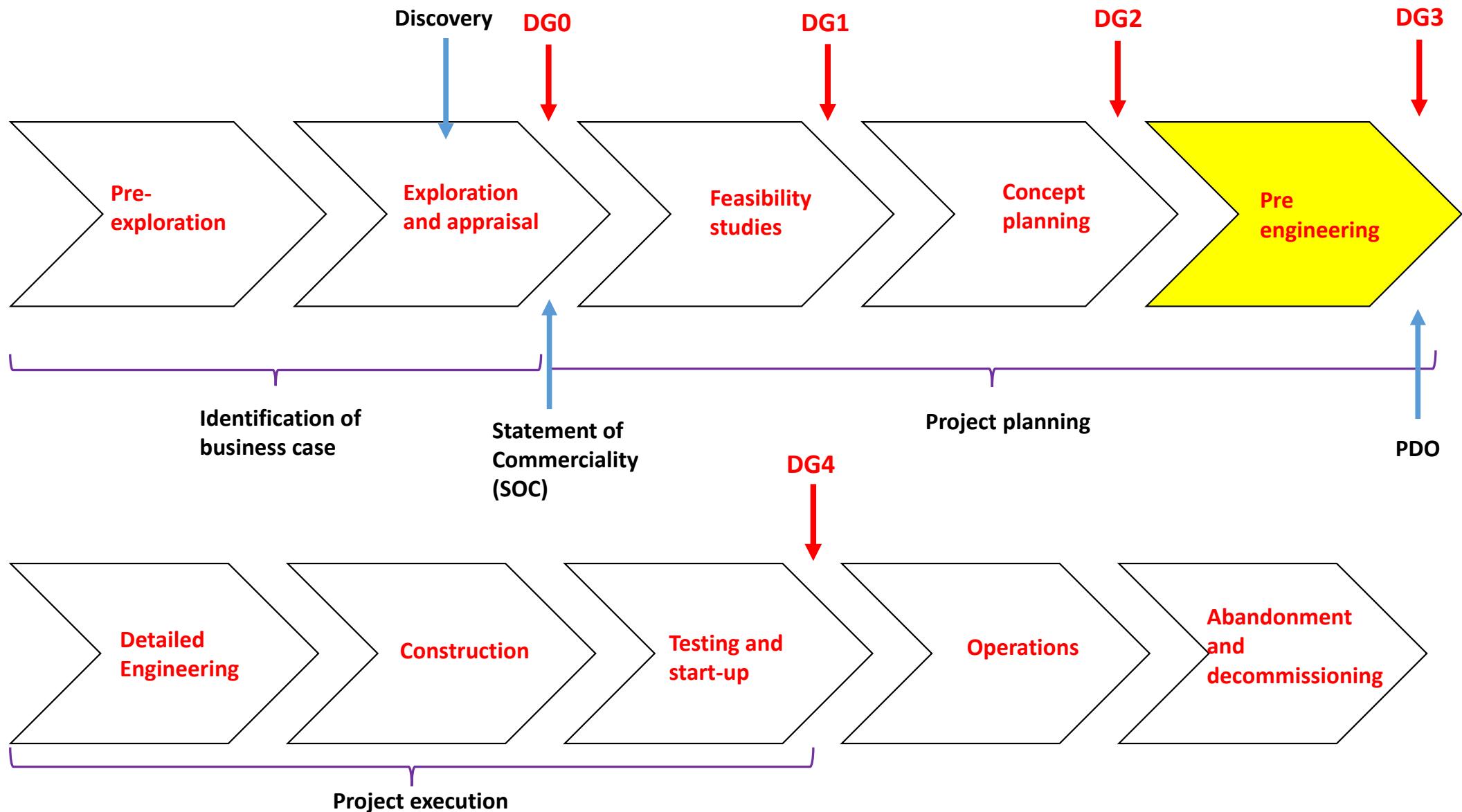
# CONCEPT PLANNING - TASKS

**OBJECTIVE:** Identify development concepts, rank them and select and document a viable concept (Base Case Scenario).

- Evaluate and compare alternatives for development and screen out non-viable options.
- Elaborate a Project Execution Plan (PEP) which describes the project and management system.
- Define the commercial aspects, legislation, agreements, licensing, financing, marketing and supply, taxes.

# CONCEPT PLANNING - TASKS

- Create and refine a static and a dynamic model of reservoir.  
**Define the depletion and production strategy.**
- Define an HSE program
- **Flow assurance evaluation.** Identification of challenges related with fluid properties, multiphase handling and driving pressure.
- Drilling and well planning
- Pre-design of facilities
- Planning of operations, start-up and maintenance
- Cost and manpower estimates of the best viable concept.



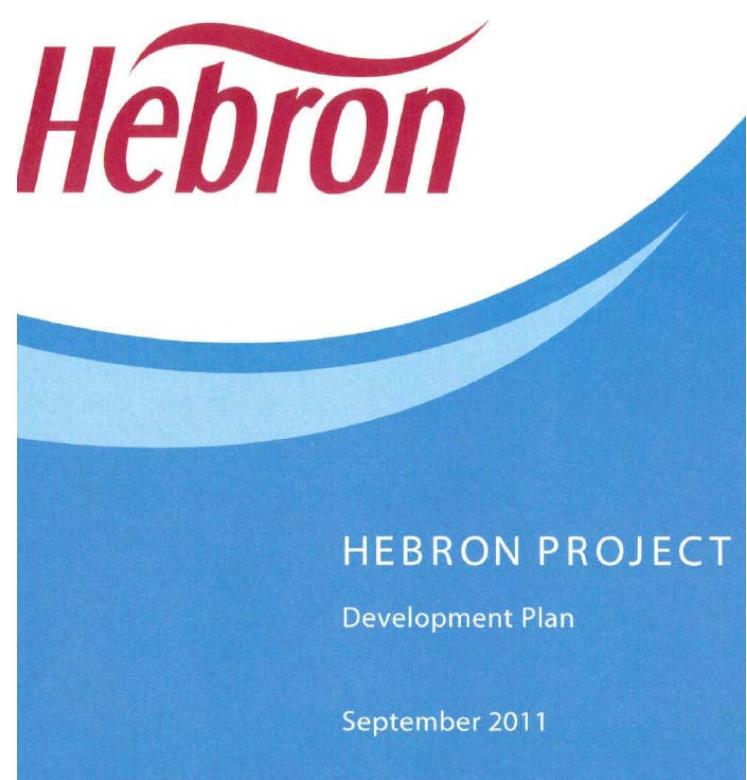
# PRE-ENGINEERING - TASKS

**OBJECTIVE:** Further mature, define and document the development solution based on the selected concept.

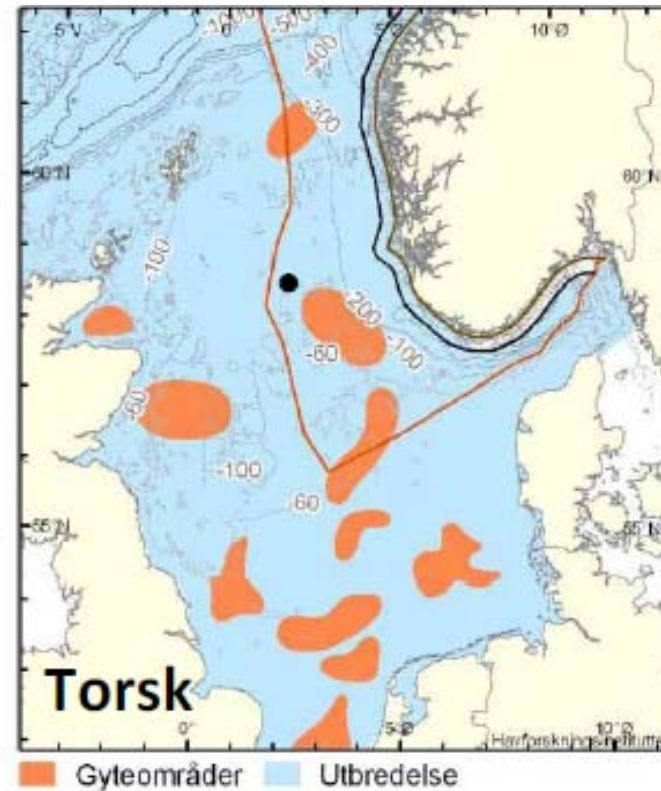
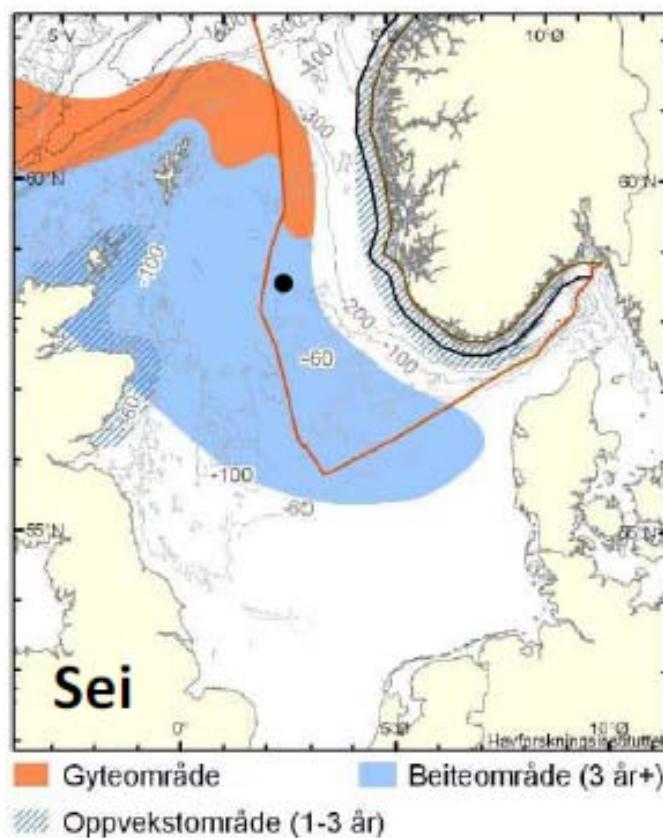
- Selection of the final technical solution. Decide and define all remaining critical technical alternatives.
- Execute Front End Engineering Design (FEED) Studies: determine technical requirements (arranged in packages) for the project based on the final solution chosen. Estimate cost of each package.
- Plan and prepare the execution phase.

# PRE-ENGINEERING - TASKS

- Prepare for submission of the application to the authorities.
- Perform the Environmental impact assessment.
- Establish the basis for awarding contracts.
- Issue:
  - Plan for development and operations
  - Plan for installation and operations of facilities for transport and utilization of petroleum (PIO)
  - Impact assessment report

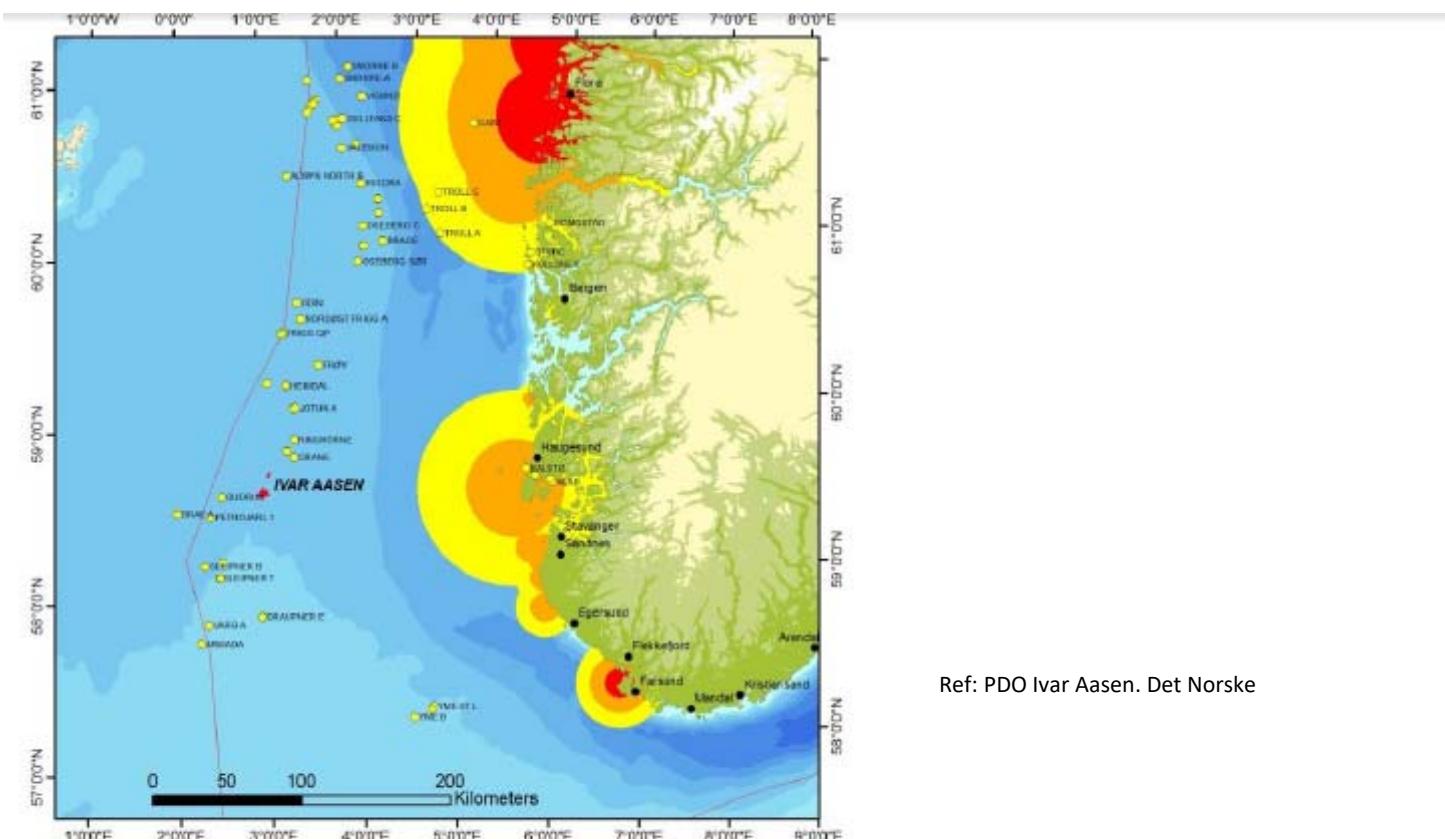


# PRE-ENGINEERING - TASKS



Ref: PDO Ivar Aasen, Det Norske

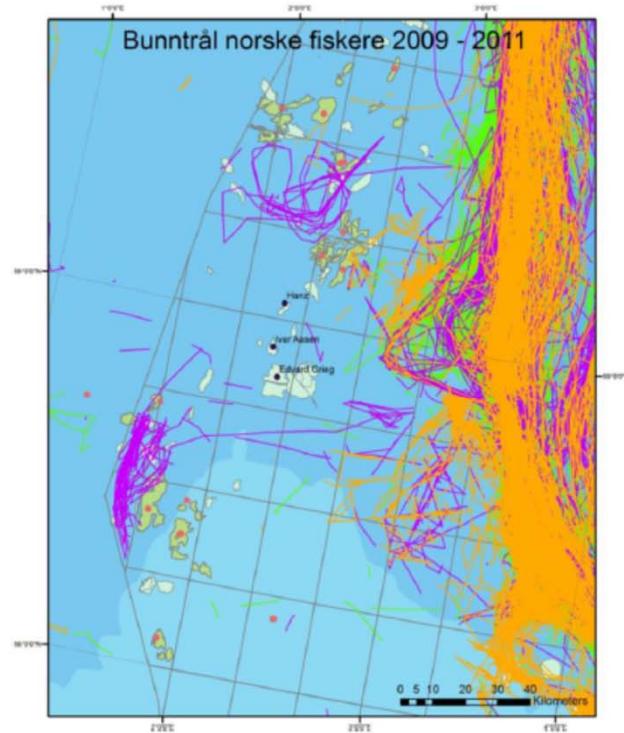
# PRE-ENGINEERING - TASKS



Ref: PDO Ivar Aasen. Det Norske

Figur 18. Svært viktige (rød), viktige (oransje) og nokså viktige (gule) leveområder for sjøfugl langs kysten av Nordsjøen i hekketiden. Kartet markerer buffersoner rundt de viktige hekkelokalitetene (NINA)

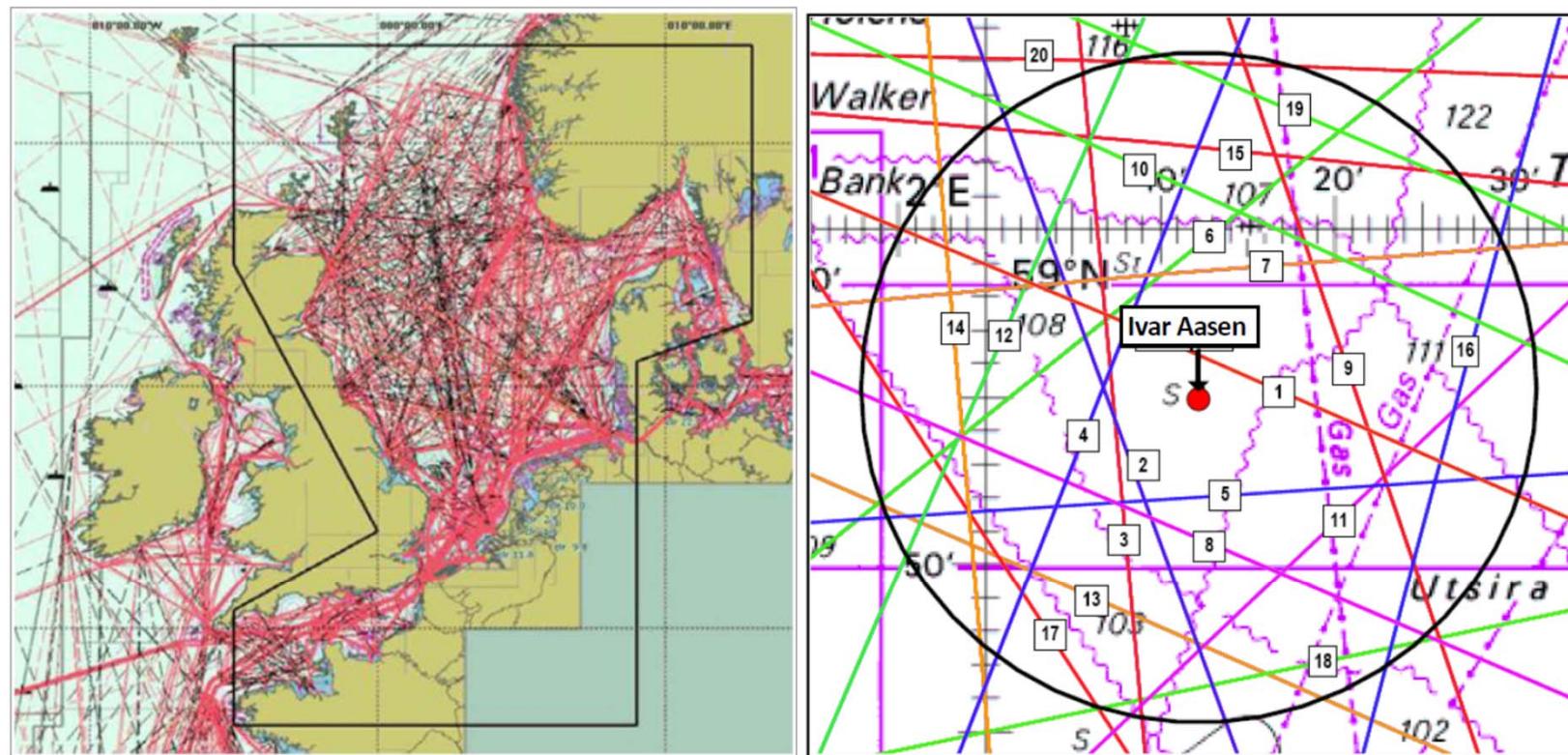
# PRE-ENGINEERING - TASKS



Ref: PDO Ivar Aasen. Det Norske

Figur 23. Registrert norsk fiskeriaktivitet med bunentrål i området omkring Aasen i 2009 (grønn), 2010 (fiolett) og 2011 (orange). Figur utarbeidet på grunnlag av data fra Fiskeridirektoratets satellittsporing av større fiskefartøyer

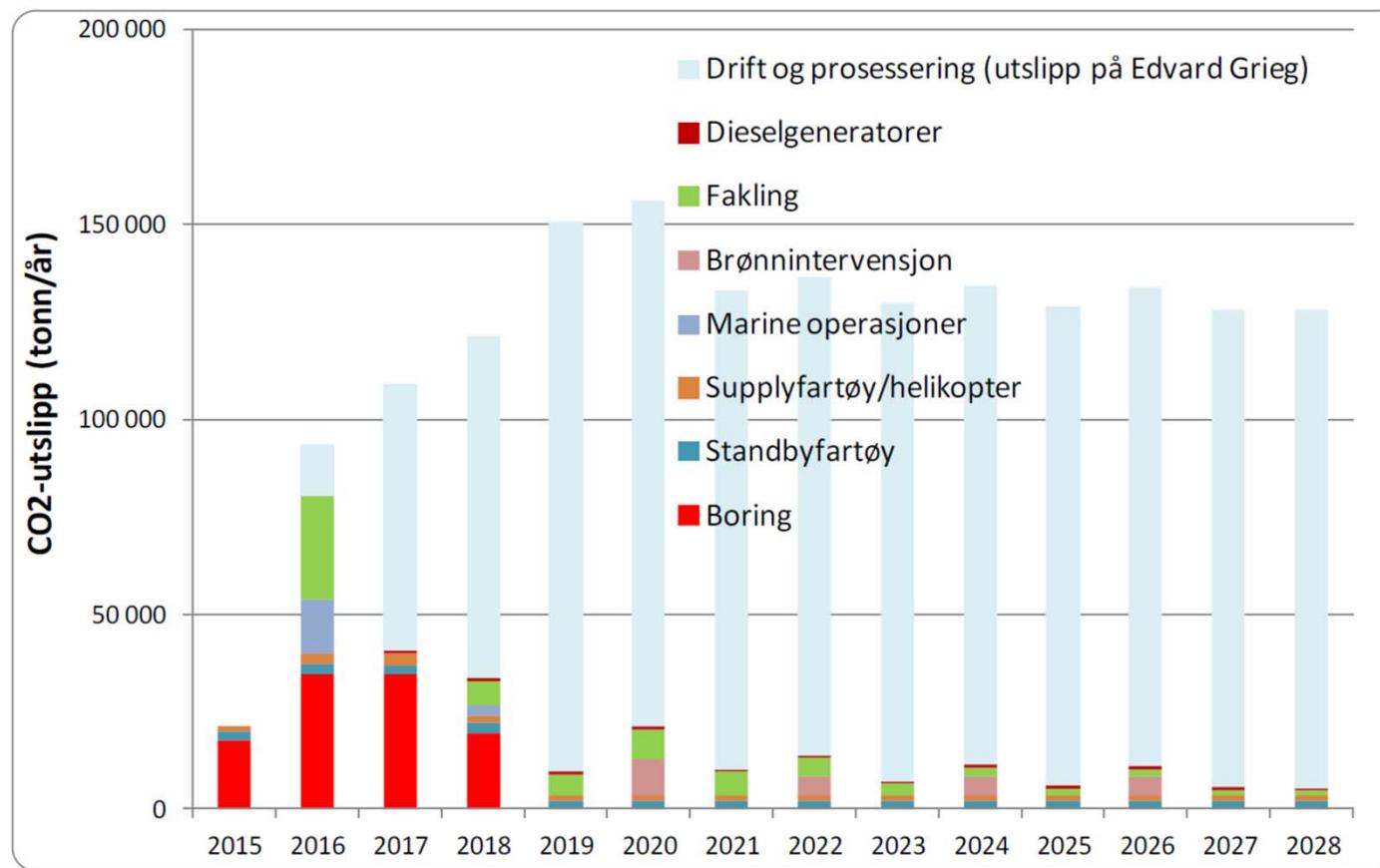
# PRE-ENGINEERING - TASKS



Figur 24. Trafikkompleksitet i Nordsjøen (venstre) og skipsleder for handels- og offshorefartøy innenfor en radius på 10 nautiske mil fra Aasen (høyre)

Ref: PDO Ivar Aasen. Det Norske

# PRE-ENGINEERING - TASKS



**Figur 25. Samlede utslipp av CO<sub>2</sub> fra Aasenfeltet i perioden 2015 – 2028**

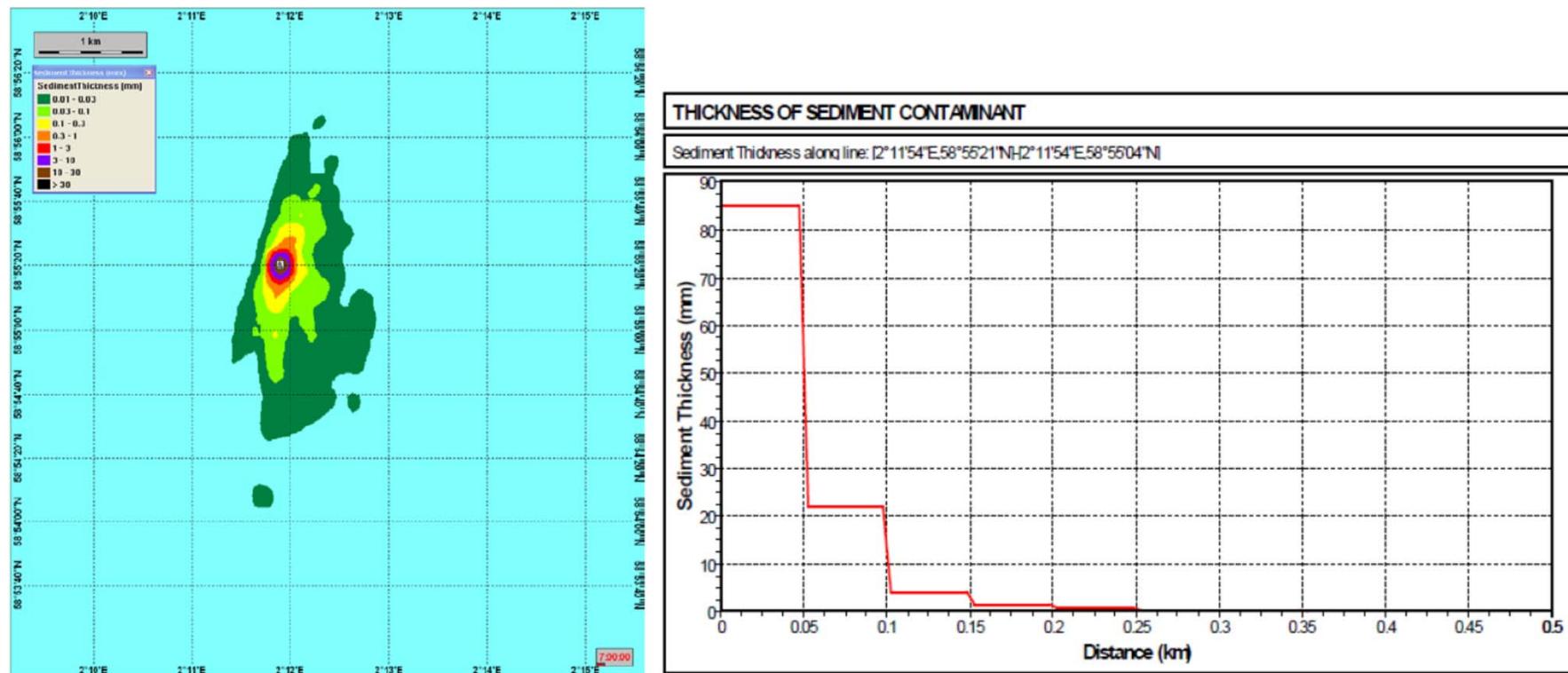
Ref: PDO Ivar Aasen. Det Norske

# PRE-ENGINEERING - TASKS

**Tabell 5-1. Foreløpig oversikt over estimerte mengder kaks for typiske produksjonsbrønner på Aasen, West Cable og Hanz**

Seksjon	Borevæske	Boret lengde (m)			Mengde borekaks (tonn)		
		Aasen	West Cable	Hanz	Aasen	West Cable	Hanz
36"	WBM	88	88	86	70	70	70
26"	WBM	370	370	400	150	150	160
17 ½"	OBM	1 550	1 020	990	310	205	200
12 ¼"	OBM	860	3 890	1 700	90	390	170
8 ½"	OBM	1 390	1 530	90	70	80	5
<b>SUM (avrundet)</b>		<b>4 300</b>	<b>6 900</b>	<b>3 300</b>	<b>690</b>	<b>895</b>	<b>605</b>
<b>SUM WBM kaks</b>					<b>220</b>	<b>220</b>	<b>230</b>
<b>SUM OBM kaks</b>					<b>470</b>	<b>675</b>	<b>375</b>

# PRE-ENGINEERING - TASKS

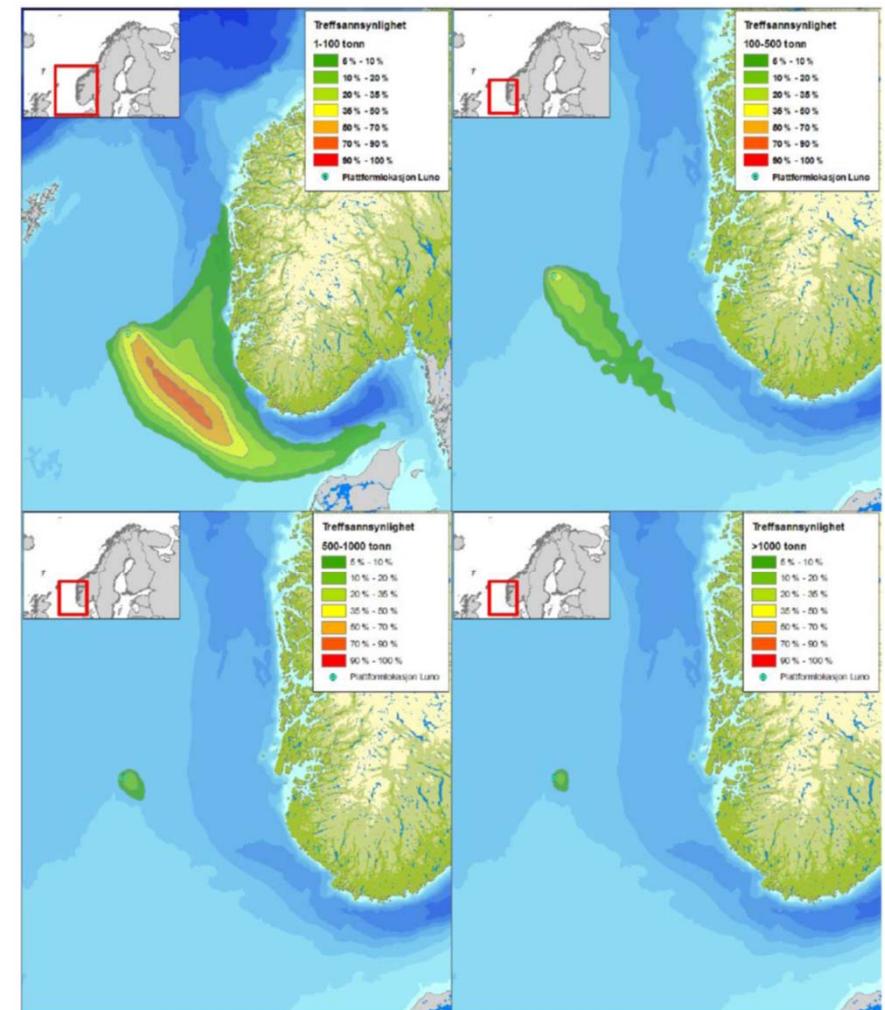


Figur 29. Sedimentering ved utslipp av vannbasert kaks ved havbunnen (sommersituasjon)

Ref: PDO Ivar Aasen. Det Norske

# PRE-ENGINEERING - TASKS

Ref: PDO Ivar Aasen. Det Norske

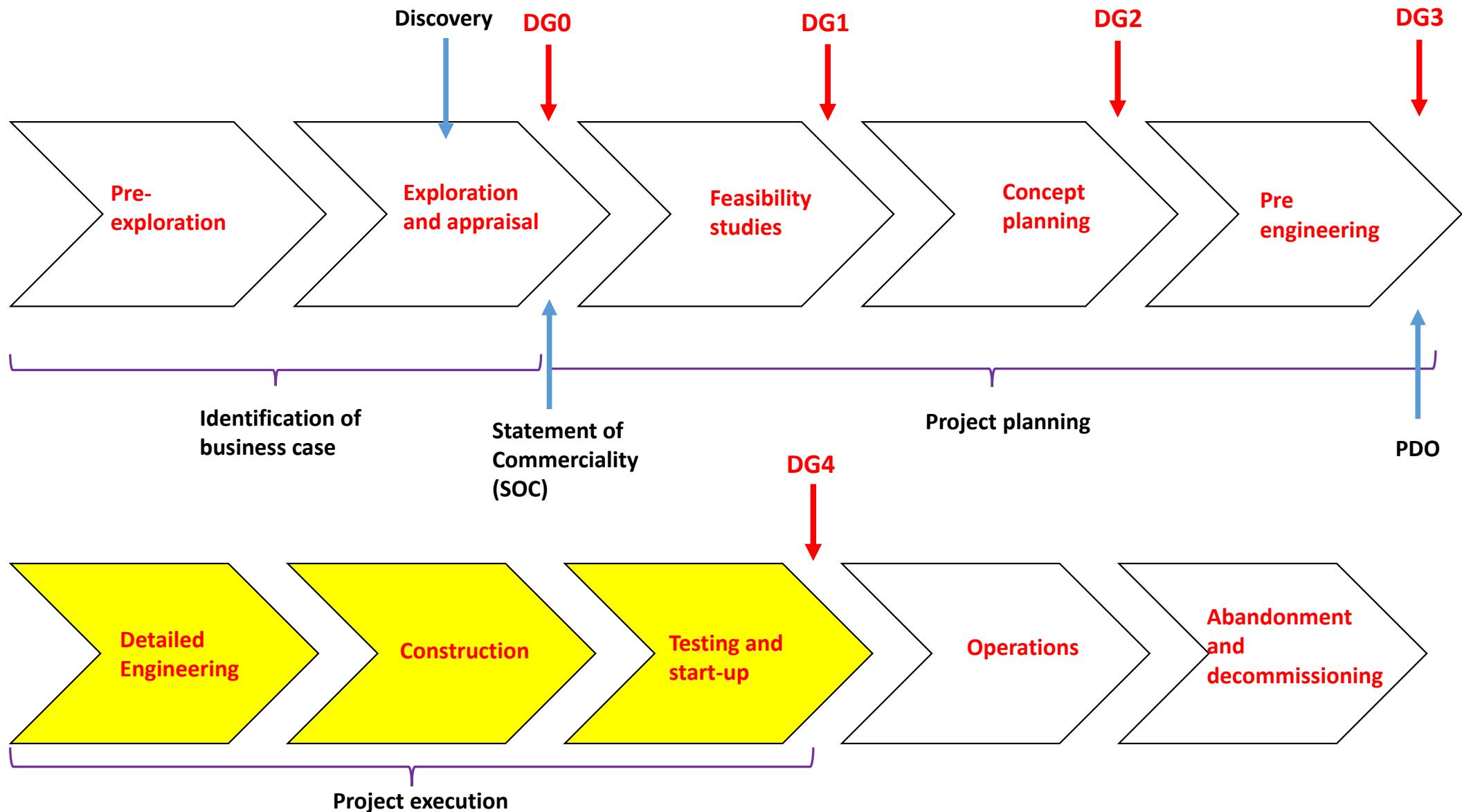


Figur 37. Sannsynligheten for treff av ulike mengdekategorier av olje i  $10 \times 10$  km ruter gitt en sjøbunnsutblåsing fra Aasen/Grieg (helårsstatistikk). Influensområdet er basert på alle utslippsrater og varigheter og deres individuelle sannsynligheter. Merk at det markerte området ikke viser omfanget av et enkelt oljeutsipp, men er det området som berøres i mer enn 5 % av enkeltsimuleringene av oljens drift og spredning (Lundin 2011).

# PRE-ENGINEERING - TASKS

- Wait for the government to study  
the proposal





# DETAILED ENGINEERING, CONSTRUCTION, TESTING AND STARTUP

**OBJECTIVE:** Detailed design, procurement of the construction materials, construction, installation and commissioning of the agreed facilities.

## **Individual contracts**

Detailed engineering

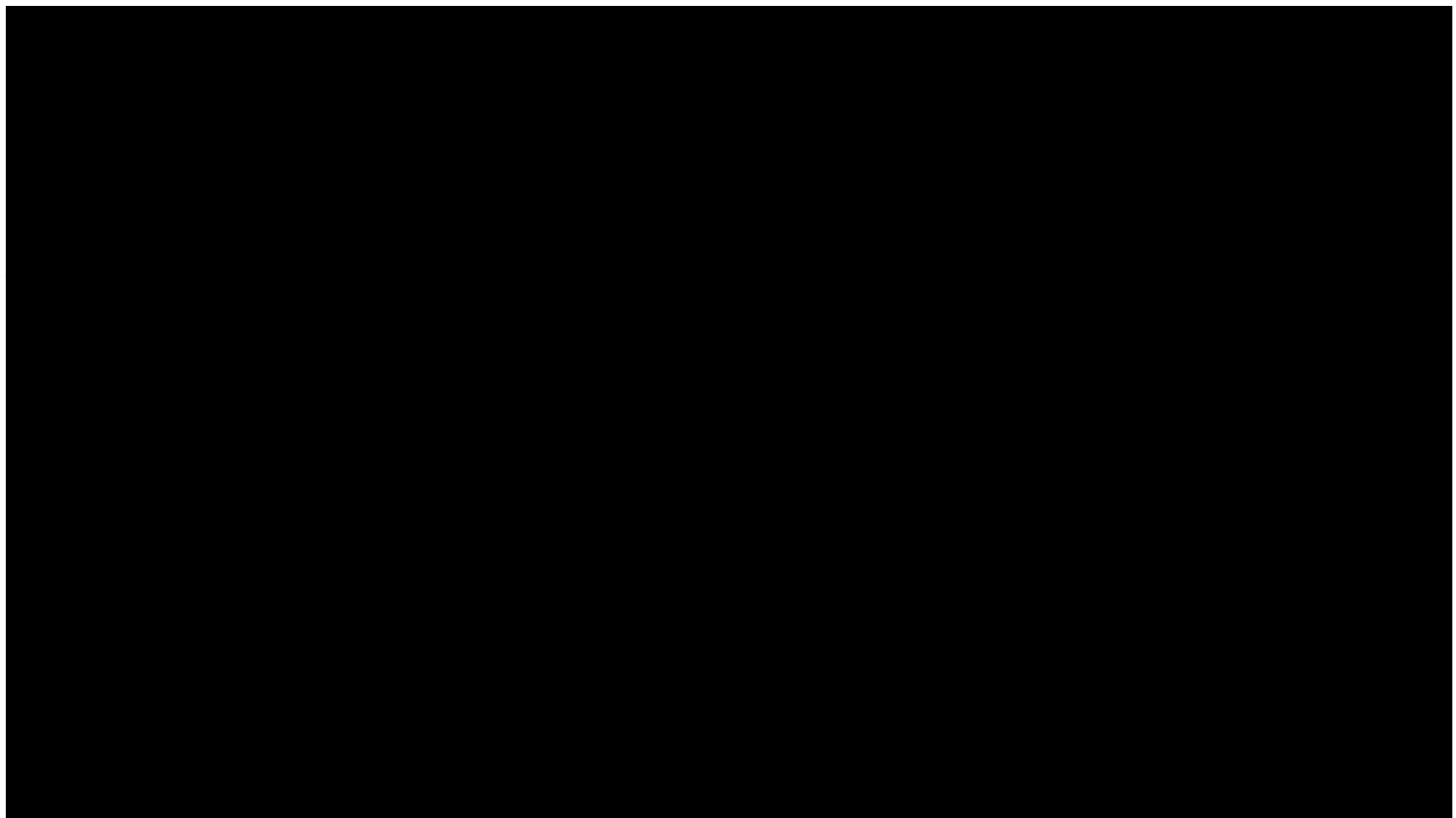
Bids, contracts

Construction, fabrication

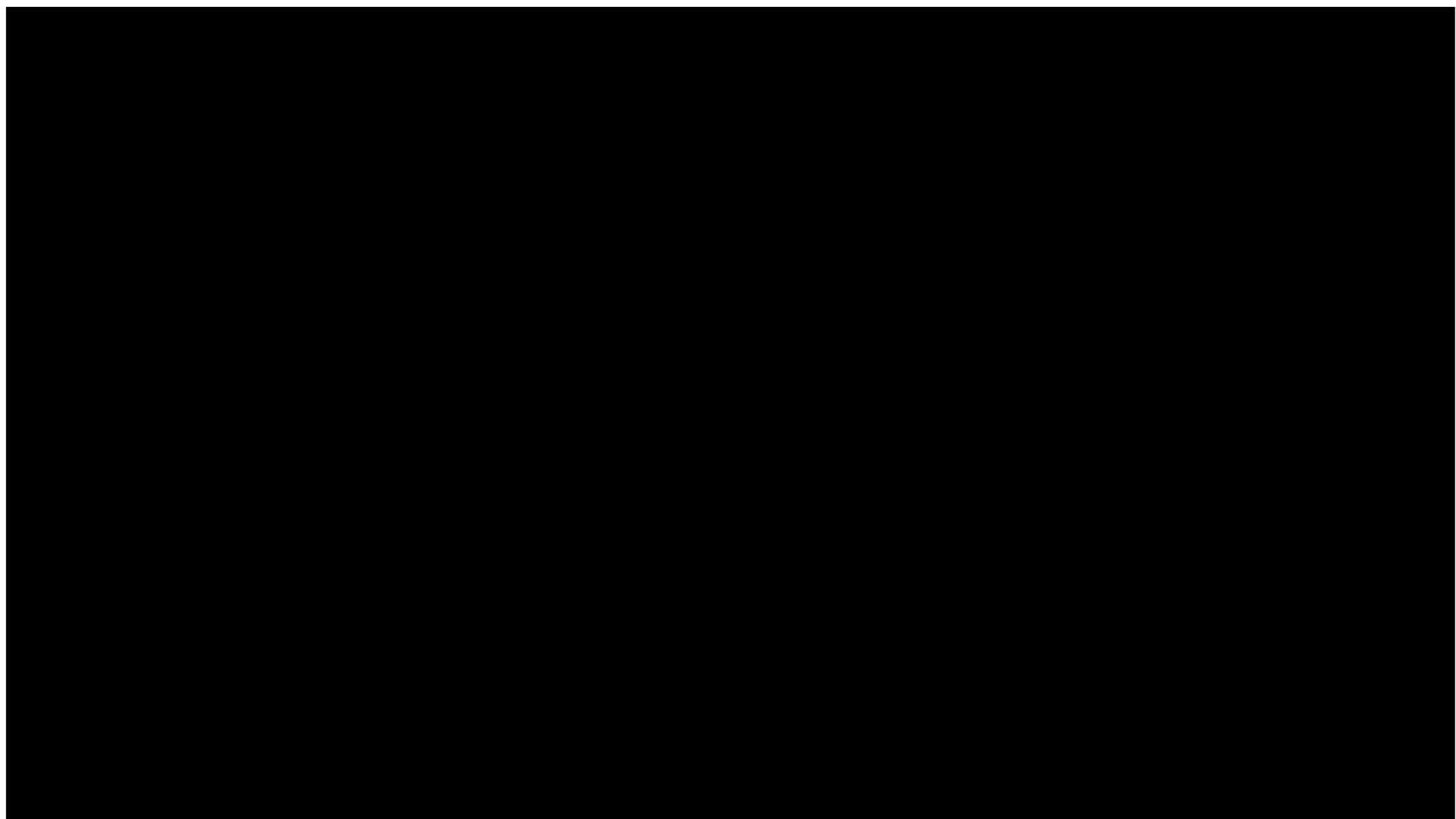
Installation

Commissioning (Cold or Hot)

**EPCM** (Engineering, procurement, construction, and management contract) with one main contractor.



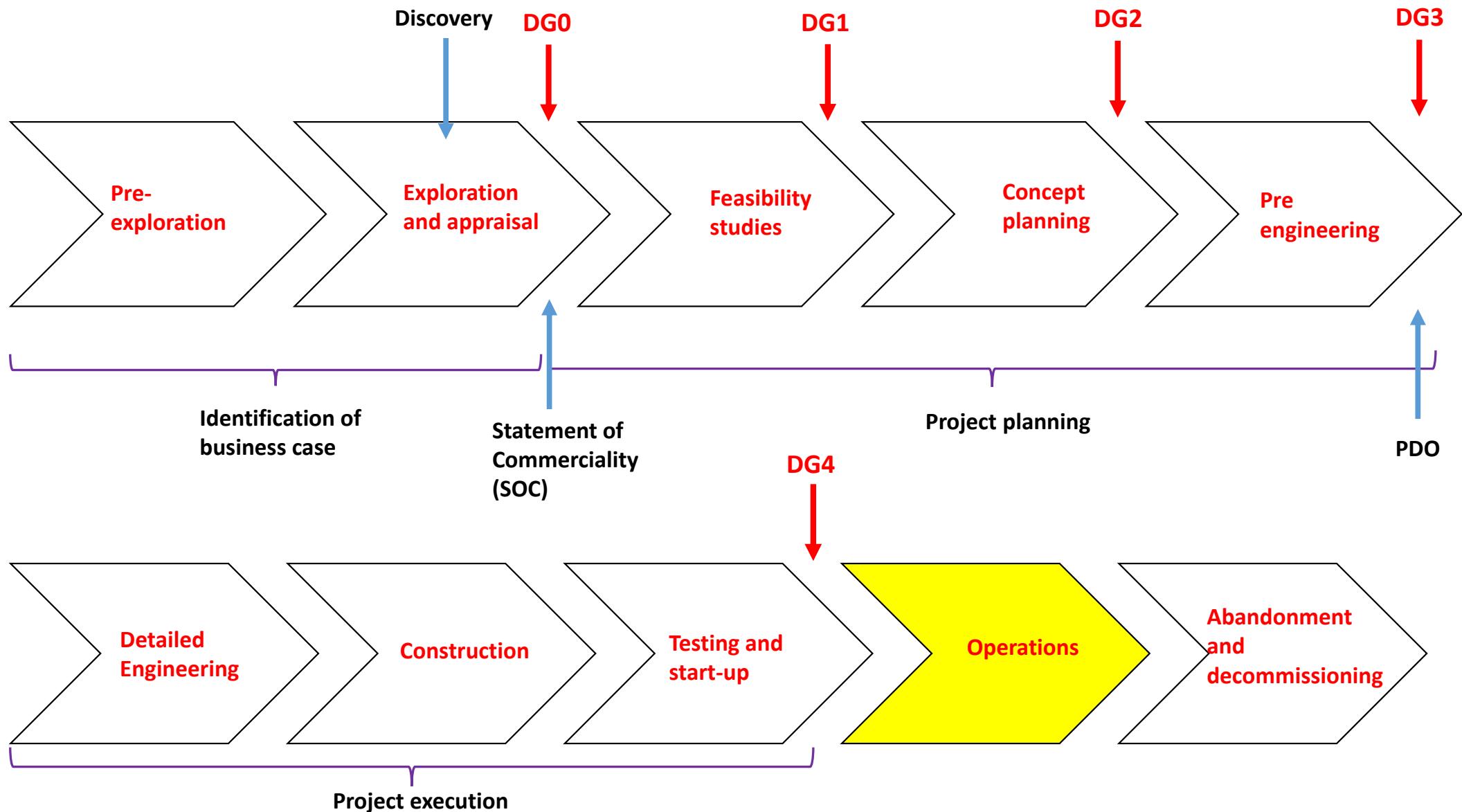
<https://www.youtube.com/watch?v=TzLAfzhqVHc>



<https://www.youtube.com/watch?v=TiWOgTq0YD4>

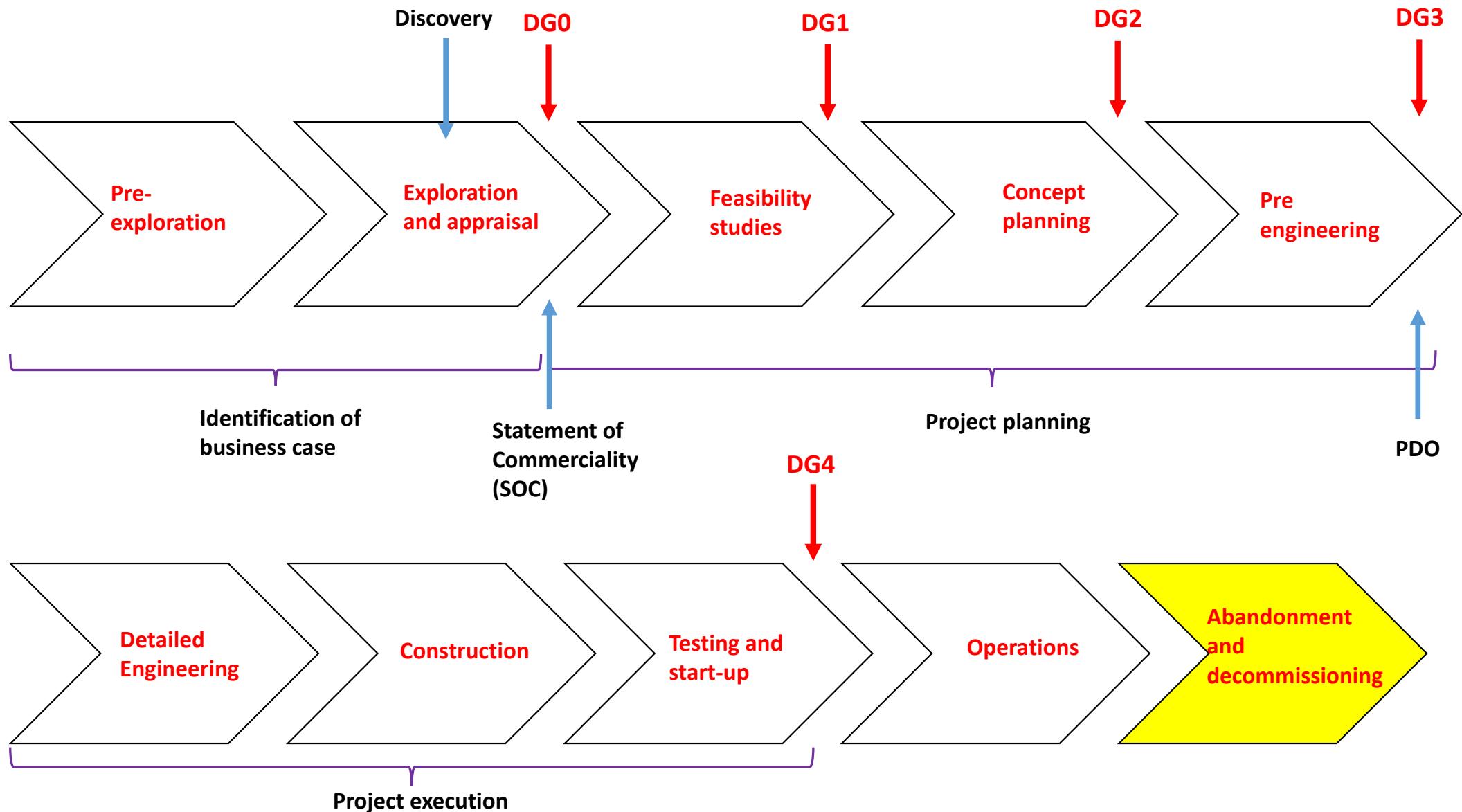
# DETAILED ENGINEERING, CONSTRUCTION, TESTING AND STARTUP

- Constructing wells.
- Perform hand over to asset, operations
- Prepare for start-up, operation and maintenance



# OPERATIONS

- Production startup, Build-up phase, Plateau phase, Decline phase, Tail production, Field shutdown.
- Maintenance.
- Planning Improved Oil recovery methods.
- Allocation and metering.
- De-bottlenecking.
- Troubleshooting.



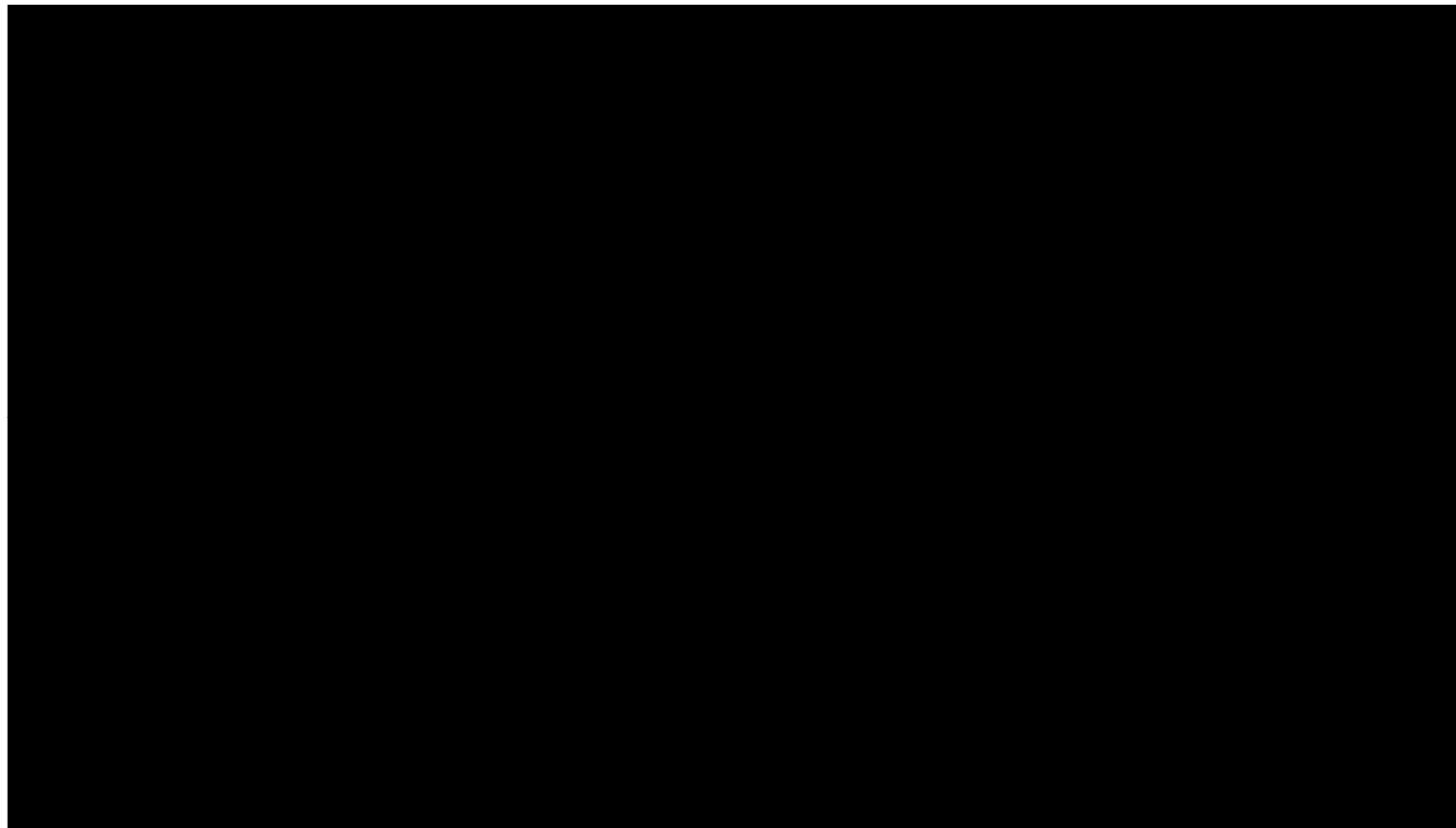
# DECOMMISSIONING AND ABANDONMENT

- Engineering “down and clean”: flushing and cleaning tanks, processing equipment, piping.
- Coordinate with relevant environmental and governmental authorities.
- Well plugging and abandonment (P&A)
- Cut and remove well conductor and casing.
- Remove topside equipment.

# DECOMMISSIONING AND ABANDONMENT

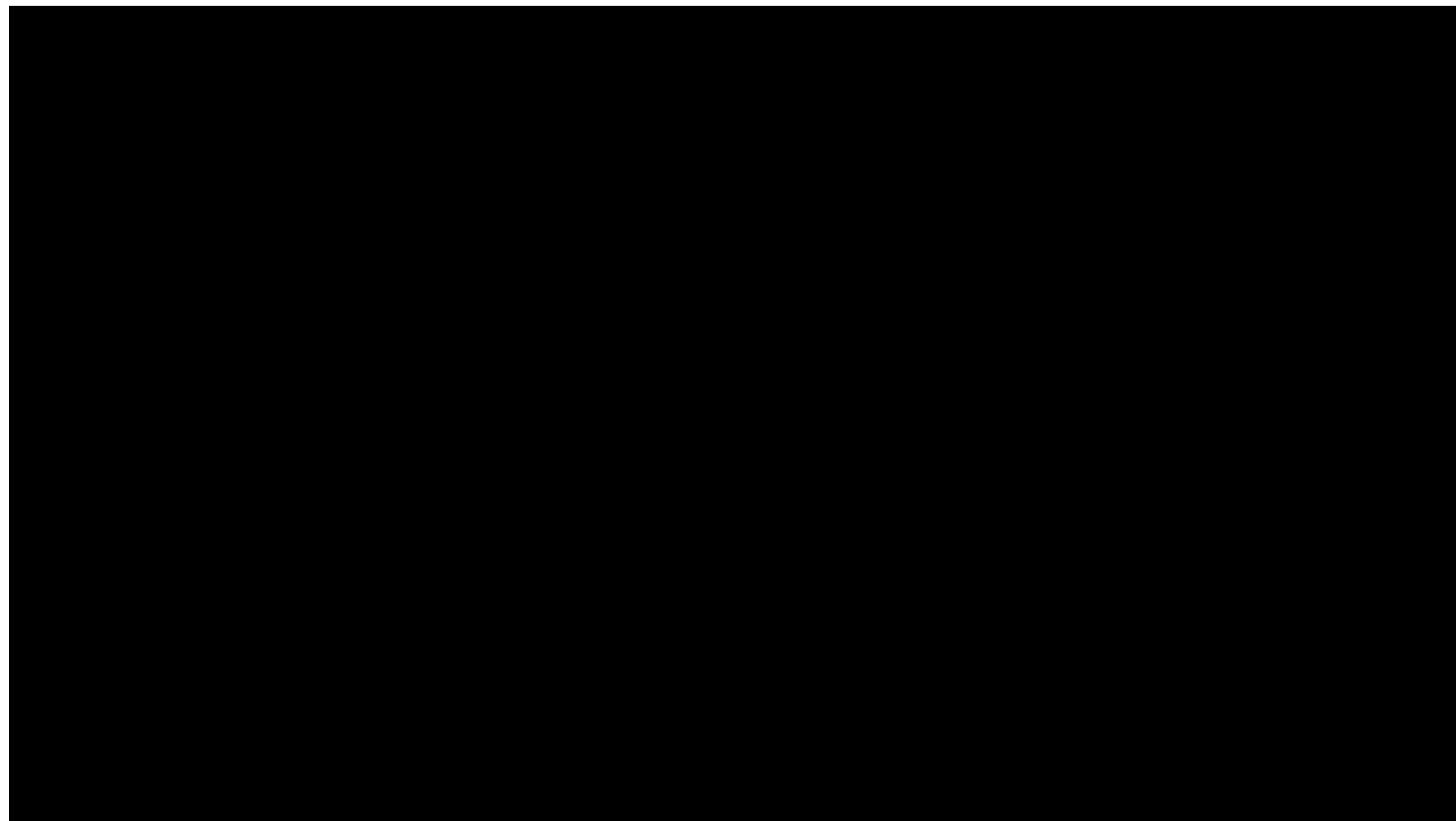
- Removal of the offshore structure: Lifting operations and transport
- Remove or bury subsea pipelines
- Mark and register leftover installations on marine maps
- Monitoring
- Recovery of material: Scrap (steel) and recycling equipment (Gas turbines, separators, heat exchangers, pumps, processing equipment)
- Disposal of residues

# DECOMMISSIONING AND ABANDONMENT



[https://www.youtube.com/watch?v=SLO9uD5Ub\\_Y](https://www.youtube.com/watch?v=SLO9uD5Ub_Y)

# DECOMMISSIONING AND ABANDONMENT



<https://www.youtube.com/watch?v=1GA3Elu81rw>

## Class 20240119 - OUTLINE

- Members of reference group
- Clarification about ppm
- Field mechanical analog
- Bottlenecking
  - Interactive app
  - Heidrun Example

3 E06  
(! ! !)

1 mt us → ? 1E06 kg

$$\text{ppmw} = \frac{m_a}{m_t} \xrightarrow{\text{component}} \frac{1 \text{ kg}}{1000000 \text{ kg}}$$

$m_t / (1E6)$  I divide the denominator by 1E06 to find out how many million kg are in the amount

$$\text{ppmw} = \left( \frac{m_a}{m_t} \cdot 1E06 \right) \quad m_a \text{ and } m_t \text{ are in the same units}$$

I can also use different units for  $m_a$  and  $m_t$  such that the 1E06 factor disappears

$$m_a [\text{kg}] \xrightarrow{\text{1E06 (ns)}} \cdot (1 \text{ kg})$$

$$1000 \text{ s} \rightarrow 1 \text{ kg}$$

$$1000000 \text{ ms} \rightarrow 1 \text{ kg}$$

$$\text{ppmw} = \frac{m_a}{m_t} \xrightarrow{[\text{ns}]} \frac{m_a}{m_t} \xrightarrow{[\text{kg}]}$$

$$\text{ppmV} = \frac{V_a}{V_t}$$

to convert from pure mass units to mixed mass-volume units, the density of the mixture is required

$$\text{ppm} = 30 \left[ \text{mg/L} \right] \xrightarrow{[\text{M}]} \left[ \frac{\text{mg}}{\text{L}} \right] = \frac{m_a}{\left( m_t / \rho_e \right)} \xrightarrow{[\text{kg/L}]} \left[ \frac{\text{kg}}{\text{L}} \right]$$

Often it is possible to neglect the mass of the component in the denominator and simply use the mass of the "rest"

$$30 \text{ ppm} \quad \frac{(m_a)}{m_a + m_{\text{rest}}} = \frac{m_a \cdot 1000}{m_{\text{rest}}} \quad \text{rns/L}$$

$$m_t \approx m_a + m_{\text{rest}} \approx m_{\text{rest}}$$

$$\frac{m_a}{m_{\text{rest}}} \xrightarrow{\text{not}} \frac{m_a}{m_{\text{rest}} / \rho_w} \xrightarrow{1 \text{ kg/L}}$$



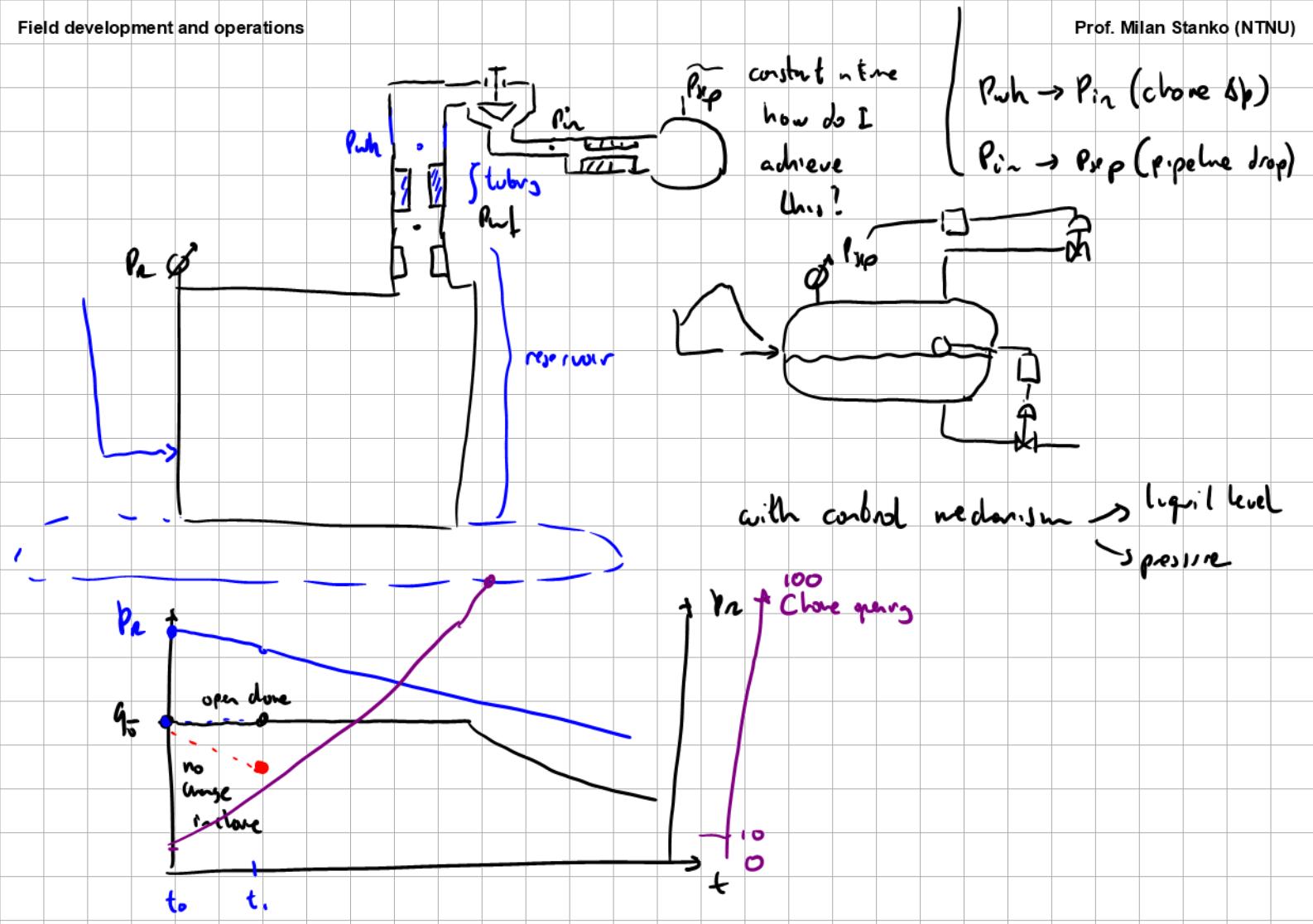
$$q_s = \int \begin{cases} P_n \\ P_{wh} \\ P_{in} \end{cases}$$

$\Delta P$  losses along way

$(P_n \rightarrow P_{wh})$  (drawdown)

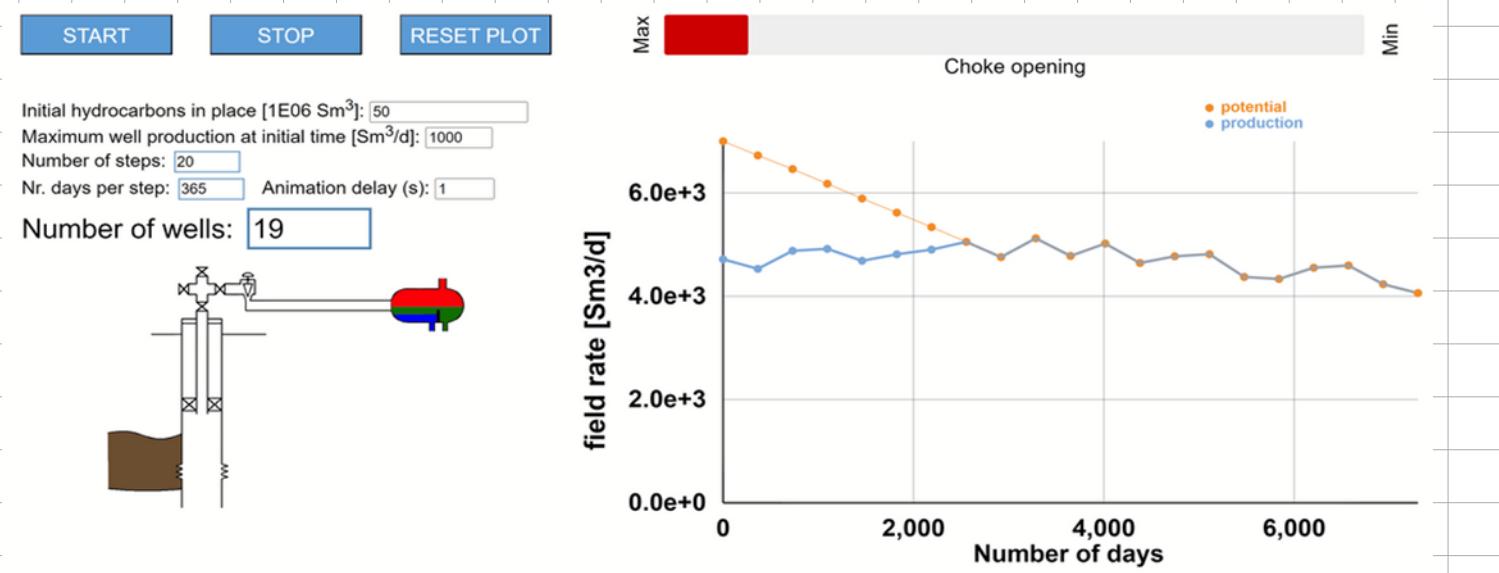
$(P_{wh} \rightarrow P_{in})$  (tubing drop)

Bottom hole flowing bottom-hole pressure



### Demonstration using the field simulator

<http://www.ipt.ntnu.no/~stanko/files/Courses/TPG4230/2022/Quizzes/Quiz%20Field%20Simulator%202.html>



## Main takeaways.

-Many things can be done to avoid rate dropping in time. Easiest and cheapest is to open the choke. Other solutions that are cumbersome, expensive and not practical for frequent adjustment are to avoid pR to drop (injection), reduce well drawdown (e.g. reservoir stimulation), reduce tubing drop (e.g. increase diameter), reduce pipeline drop (e.g. increase diameter)

-when reservoir pressure drops, Choke must be opened in time to keep constant rate

-There will be a time at which the choke is fully open. at that time, we "lose" control of the field and decline starts.

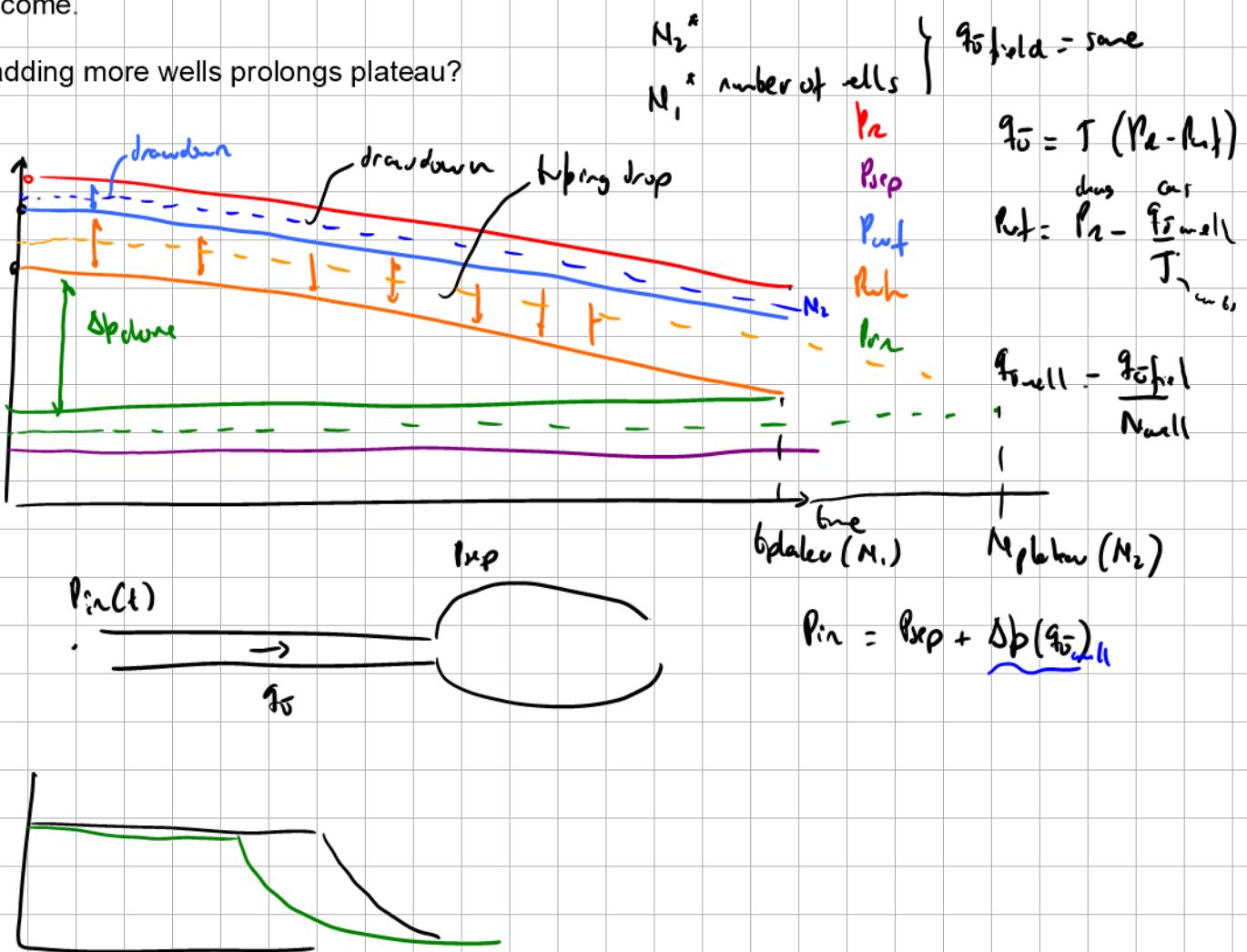
-higher plateau gives shorter plateau, Lower plateau gives longer plateau

-Plateau can be prolonged by adding more wells (but is expensive)

-Isn't it better to always produce as much as possible?

-In terms of just revenue, yes (money today as more value than money in the future). But: when considering cost, processing higher amounts will require more costly installations. A Net present value analysis is required, to evaluate expenses and income.

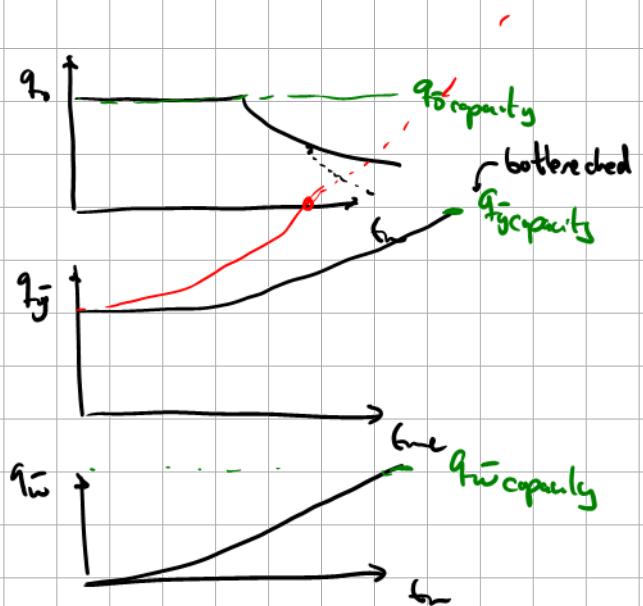
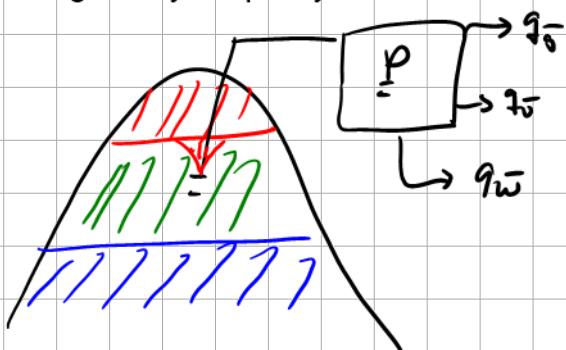
Why adding more wells prolongs plateau?



## Bottlenecking

-when we reached capacity of some process in the field --> that prevents from producing more oil and gas.

Processing facility «capacity» is reached



Processing facilities typically have  $q_{o\text{max}}$ , design  $q_{\bar{o}\text{max}}$ ,  $q_{w\text{max}}$

<http://www.ipt.ntnu.no/~stanko/files/Courses/TPG4230/Tools/>

[http://www.ipt.ntnu.no/~stanko/files/Courses/TPG4230/Tools/Oilfield bottlenecking showcase v1.exe](http://www.ipt.ntnu.no/~stanko/files/Courses/TPG4230/Tools/Oilfield_bottlenecking_showcase_v1.exe)

water cut WC

$$WC = \frac{q_w}{q_o} = \frac{\bar{q}_w}{q_o + \bar{q}_w} [-]$$

$$\frac{\bar{q}_w}{q_o + \bar{q}_w} \cdot (100) [\%]$$

$$q_o = 1000 \text{ m}^3/d$$

$$q_o = 1000 \text{ m}^3/d$$

$$WC = 50\%$$

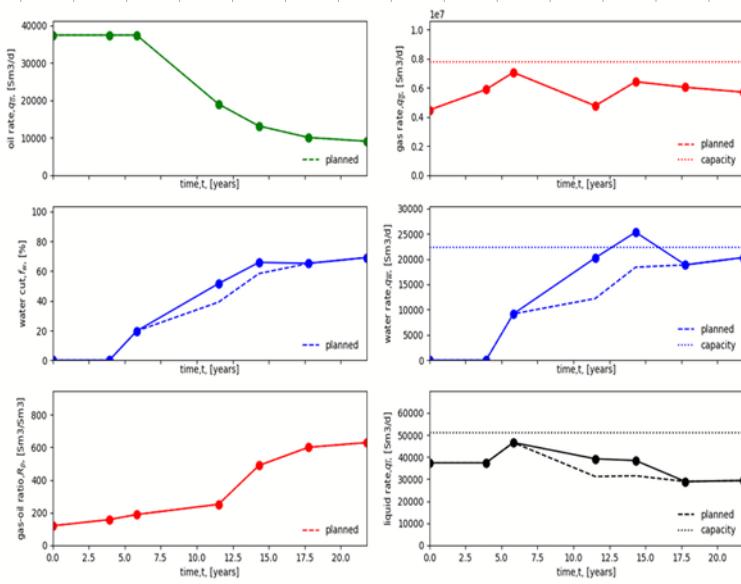
$$WC = 50\%$$

$$\bar{q}_w = 1000 \text{ m}^3/d$$

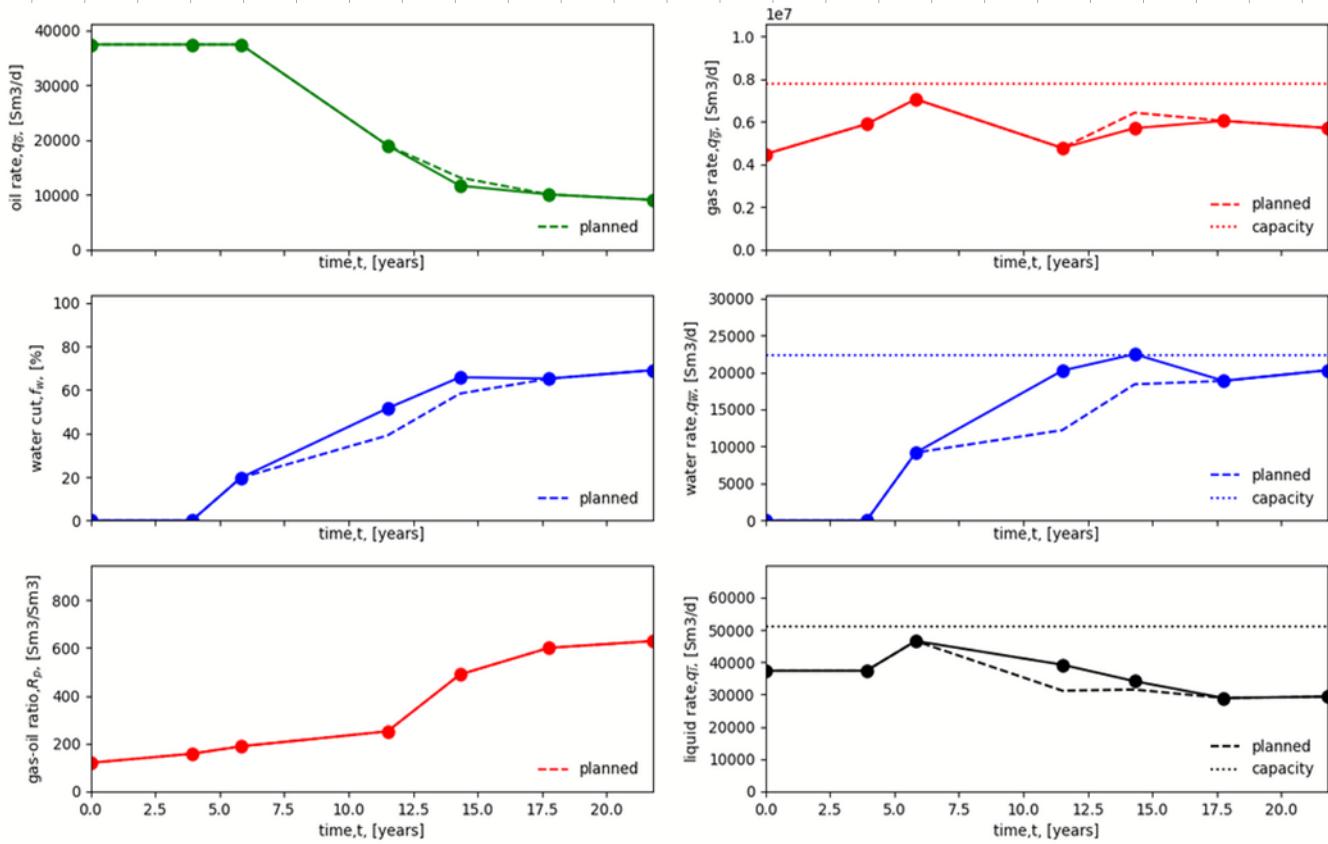
$$\bar{q}_w = ?$$

$$0.3 = \frac{\bar{q}_w}{1000 + \bar{q}_w}$$

$$GOR(R_p) = \frac{q_o}{q_w} \quad q_f = q_o \cdot R_p$$



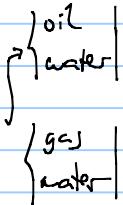
\*Adjusted



- Field production performance

- production model (production scheduling)
  - plateau height vs. plateau length
  - deciding plateau height

production scheduling : deciding / forecasting rates of oil and associated products



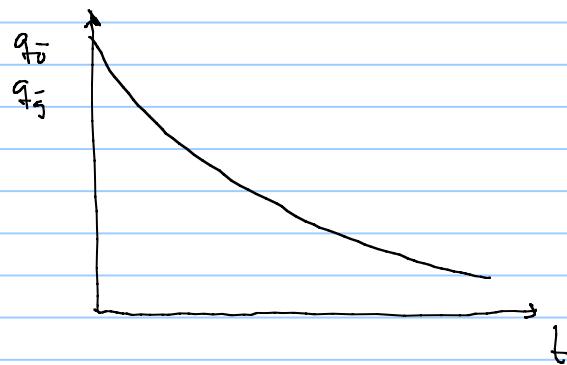
during the life of field

two ways to produce a field

Production mode A  
"plateau production"



Production mode "B"  
"deactive production"



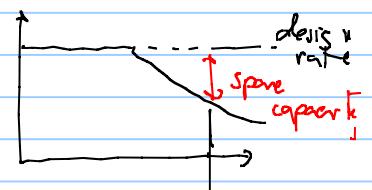
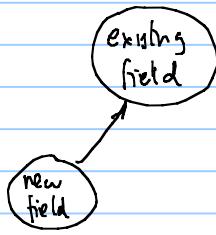
- typically used for gas fields with a contract

- big-medium reservoir

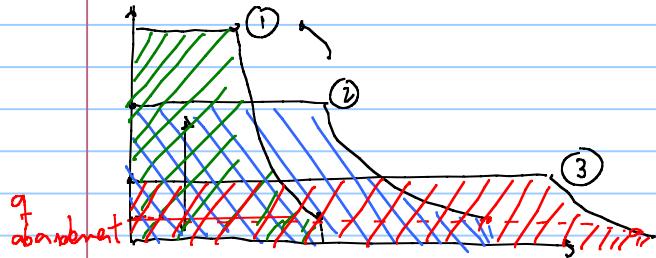
- standalone development  $\rightarrow$  requires its own facilities, offshore structure etc.

- produce as much as possible as early as possible

- satellite developments to existing fields that use existing infrastructure



in mode "A" there is a relationship between plateau height and duration

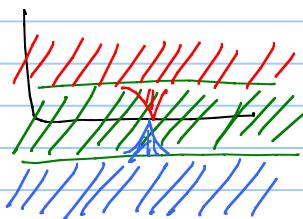


$$N_p = \int_0^t q(t) dt$$

↳ cumulative production until abandonment  $N_{pu}$



- for gas, plateau height/length is given by contract
- for oil/gas → there is a requirement by authorities to reach certain RF



higher rates can cause  
high GOR  
high WC  
sand production

to define plateau rate an economic analysis must be made

higher plateau → higher revenue

$$NPV \rightsquigarrow \text{net present value} \quad NPV = \sum_{i=1}^N \frac{CF_i}{(1+C)^i}$$

cash flow = revenue - expenses

$\Delta Q_p \cdot p_a^i$  production of oil/gas in year  $i$

discounting rate ( $5\% \rightarrow 15\%$ )  
 $0.05 - 0.15$

$$NPV = \text{Expenses} + \frac{\Delta Q_p \cdot p_o^5 - OPEX^5}{(1+0.07)^5} + \frac{\Delta Q_p \cdot p_o^6 - OPEX^6}{(1+0.07)^6} + \dots$$

well processing facilities platform start production

due to discounting, it makes sense to produce as much as possible, as early as possible

year	$CF_i = \frac{1}{(1+C)^i}$
1	0.93457944
2	0.87343873
3	0.81629788
4	0.76289521
5	0.71298618
6	0.66634222
7	0.62274974
8	0.5820091
9	0.54393374
10	0.50834929
11	0.4750928
12	0.44401196
13	0.41496445
14	0.38781724
15	0.36244602

if plateau rate is higher → bigger processing facilities  
→ bigger offshore structure  
→ more wells

expenses become very negative  
but also revenues become bigger

for HC fields, plateau rate is usually decided by doing an economic evaluation and sensitivity analyses  
excepters / blending of crude.

Rules of thumb for first iteration on plateau rate

for oil: 10% of  $N_{pu}$  per year

$\sim$  ultimate cumulative production (at abandonment)

TRR  $\rightarrow$  total recoverable reserves

Example 180 E06 stb  $\rightarrow$  N initial oil in place (OoIP)

$$N_{pu} = R_{Fu} \cdot N$$

$\sim$   
(0.3-0.5)

$$N_{pu} = 0.4 \cdot 180 \text{ E}06 \text{ stb}$$

$$N_{pu} = 72 \text{ E}06 \text{ stb}$$

$$q_{plateau} = \frac{N_{pu} \cdot 0.1}{\begin{matrix} \text{No producing day} \\ [\text{stb}/\text{d}] \end{matrix}} = \frac{72 \text{ E}06 \cdot 0.1}{0.9 \cdot 365} \approx 21900 \text{ stb/d}$$

$\hookrightarrow$  95% uptime (0.95, 365)

for gas (2-5)% of  $G_{pu}$

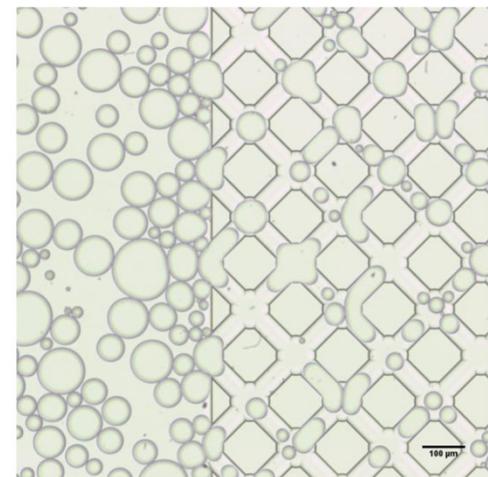
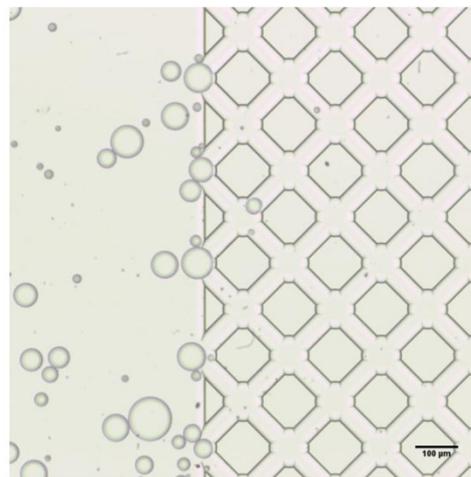
$Q$  is either oil or gas  
 $N$  is for oil  
 $G$  is for gas

## **Class 20240125 - OUTLINE**

- Additional comments about Bottlenecking
- quick go-through the previous video lectures' content
- Introduction to field processing

# Bottlenecking - reasons

- Processing facility «capacity» is reached
  - Separation capacity (residence times)
  - Capacity of rotating equipment (pumps/compressors)
  - Water Treatment capacity
  - Water injection – Plugging of injectors
  - Sand production/wellbore stability



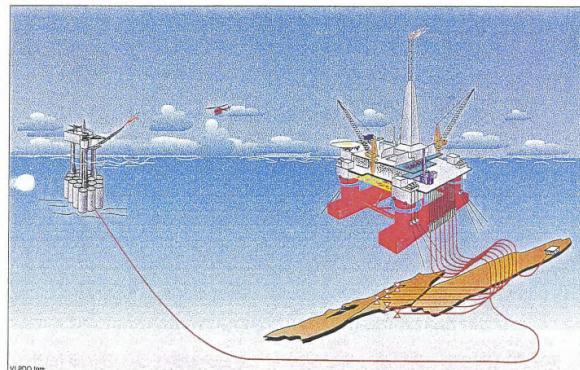
# Processing capacity in PDO

VISUND

Plan for Development  
and Operation

PL 120

September 1995



VI PDO bms.

Partners:



STATOIL

conoco

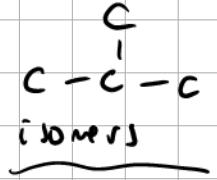
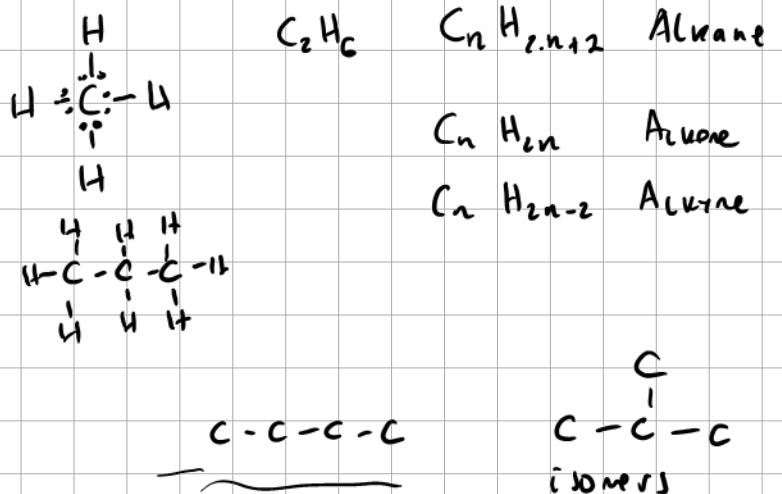
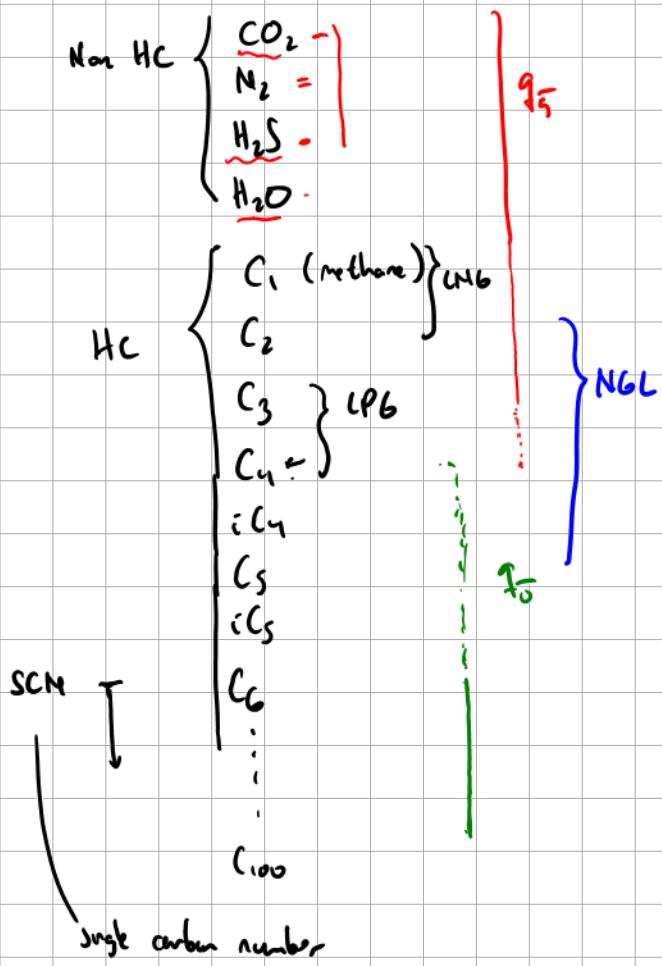
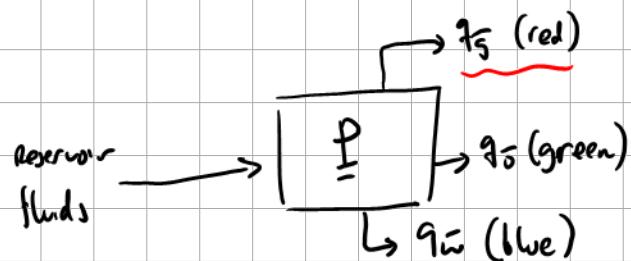
saga

elf

Process Categories	Capacities
Oil production	16,000 Sm <sup>3</sup> /sd
Liquid production	28,000 Sm <sup>3</sup> /sd
Water production	15,000 Sm <sup>3</sup> /sd
Water injection	18,000 Sm <sup>3</sup> /sd
Utsira water production	15,000 Sm <sup>3</sup> /sd
Gas production initially (excl. fuel gas)	10 MSm <sup>3</sup> /sd
Gas injection	10 MSm <sup>3</sup> /sd
Export gas production	13 MSm <sup>3</sup> /sd

Table 1-2 Process Capacities

20240125



LNG ... liquefied natural gas

LPG ... liquefied petroleum gas

NGL ... Natural gas liquids



NTNU | Norwegian University of  
Science and Technology

# Introduction to oilfield processing

Assoc. Prof. Milan Stanko

**Well  
stream** →

**Well  
stream**

Oil, Gas and  
Water  
separation &  
stabilization

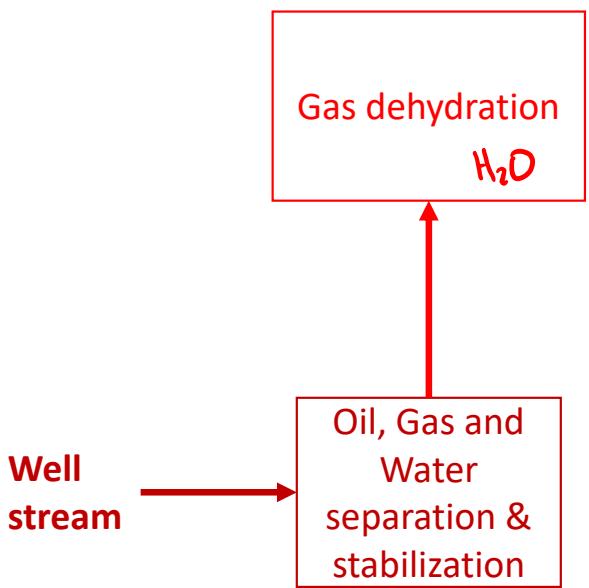


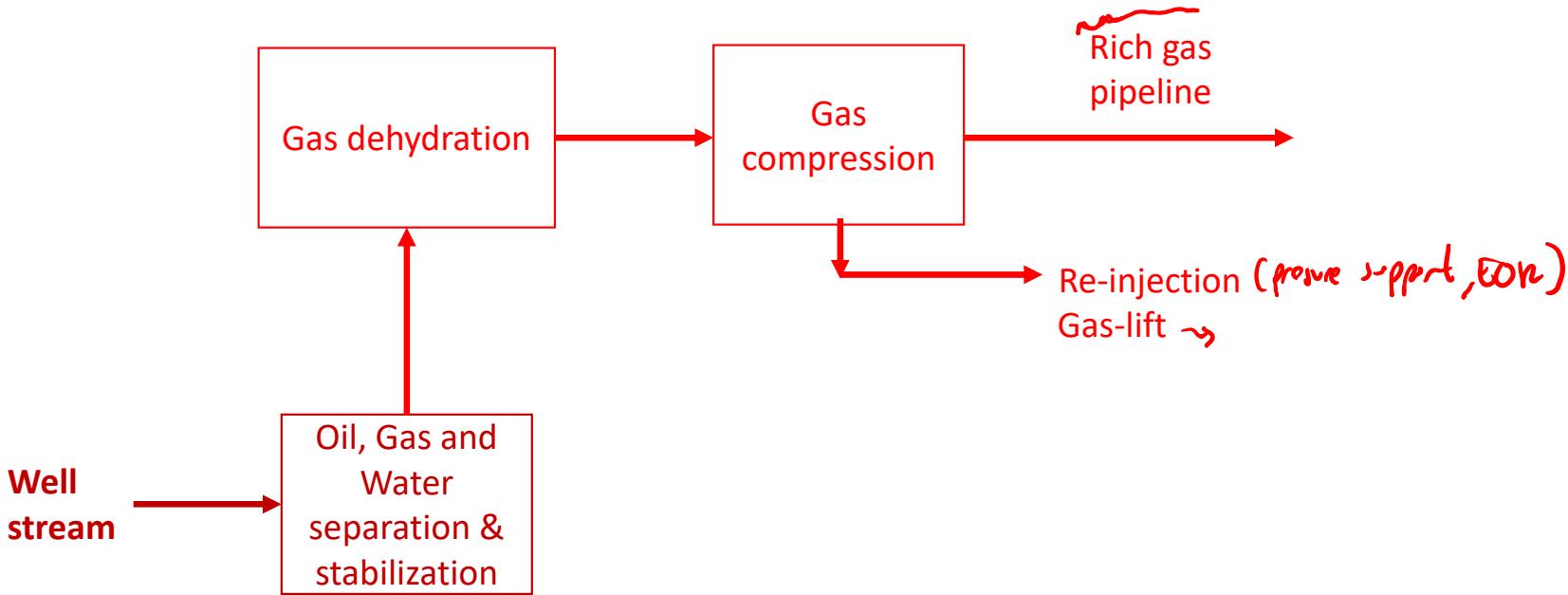
Color convention

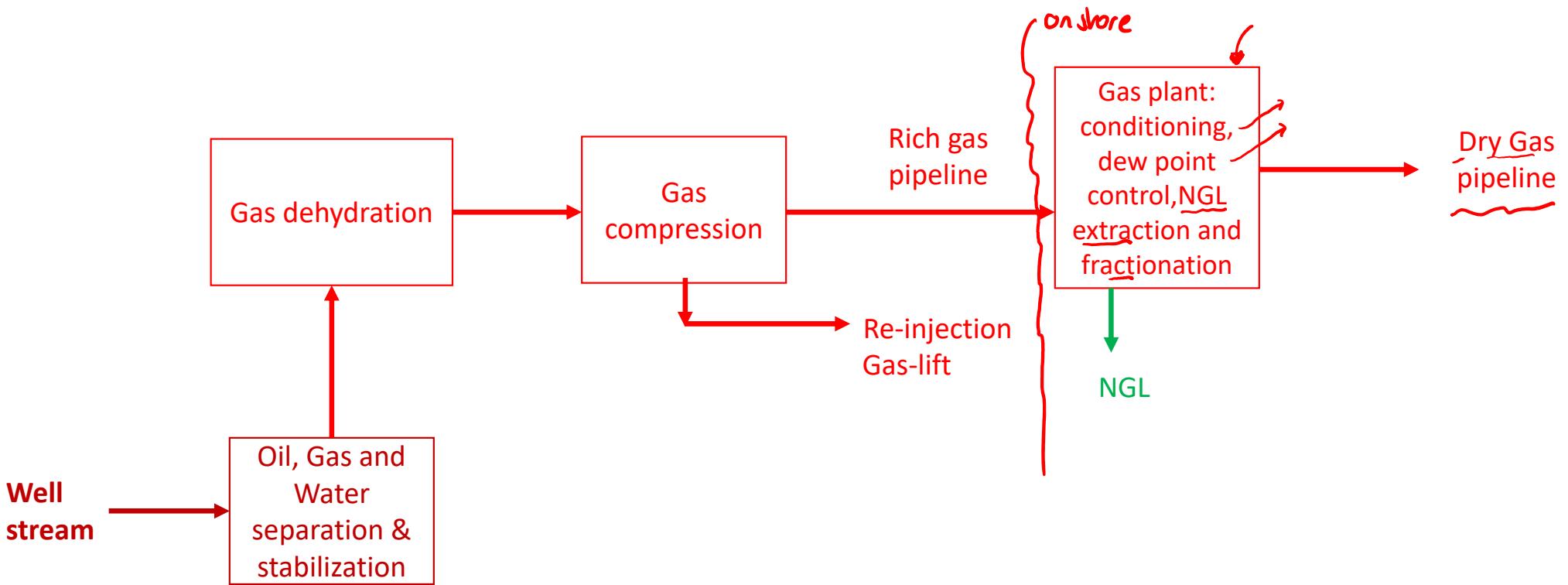


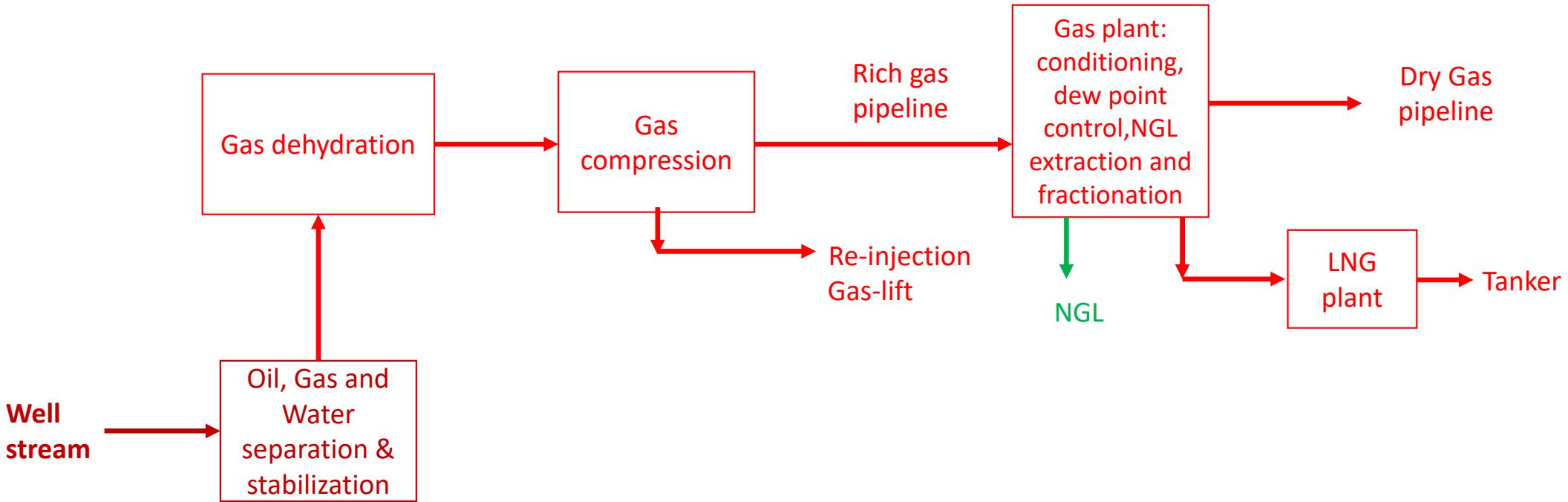
Well  
stream

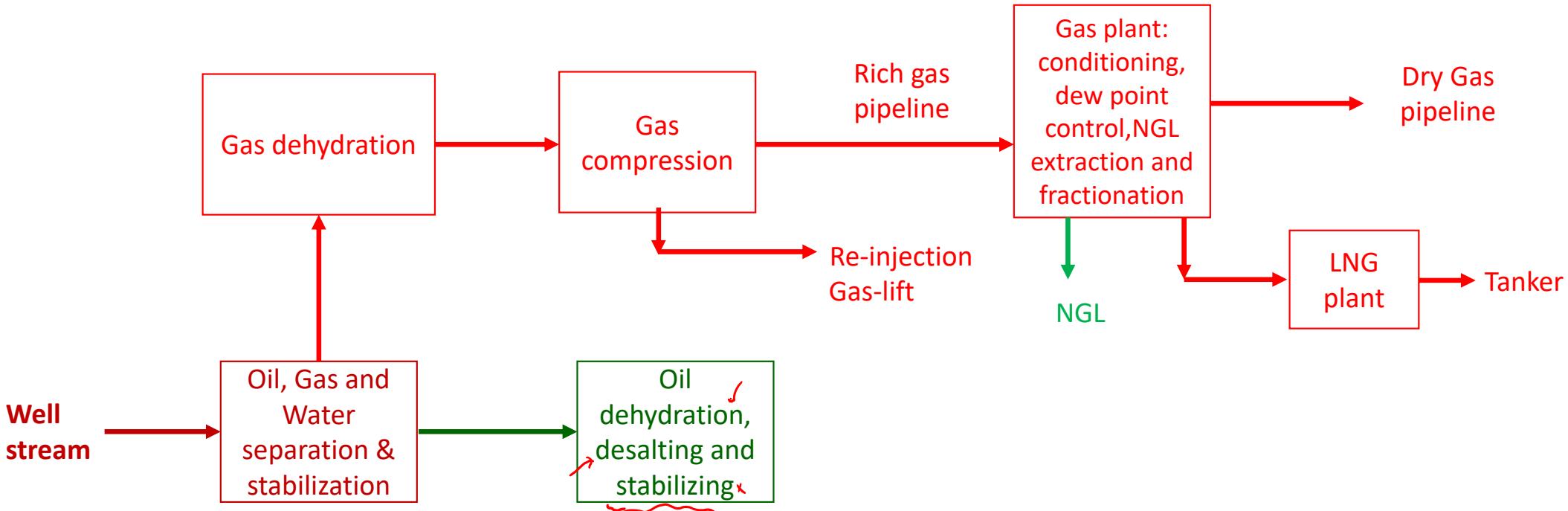


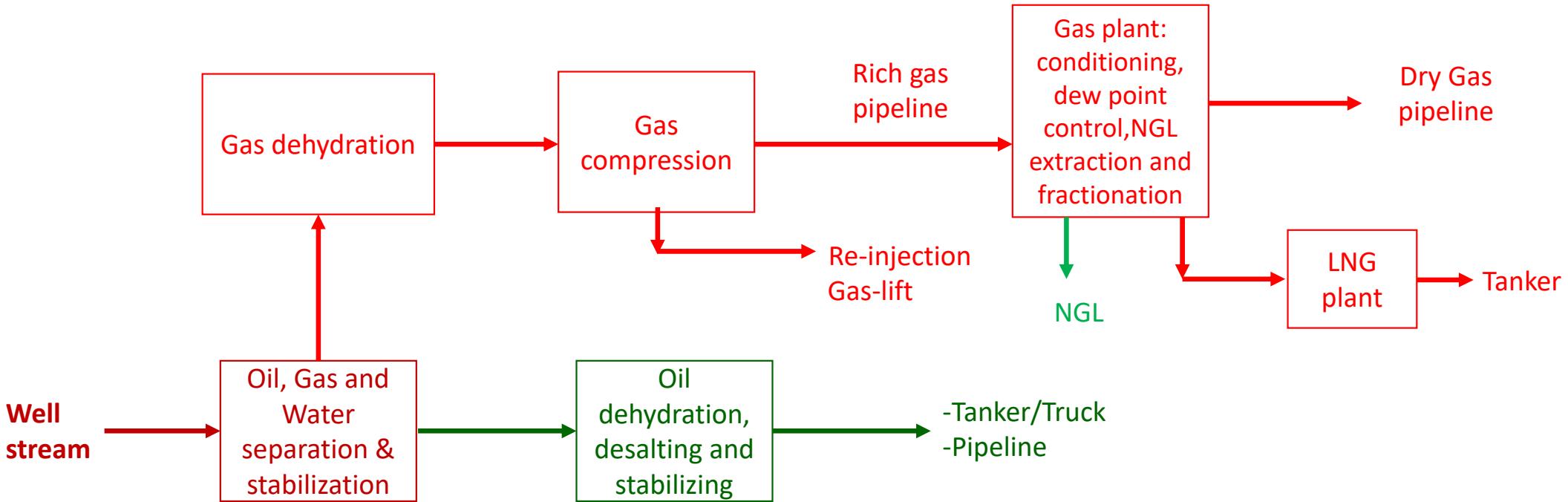


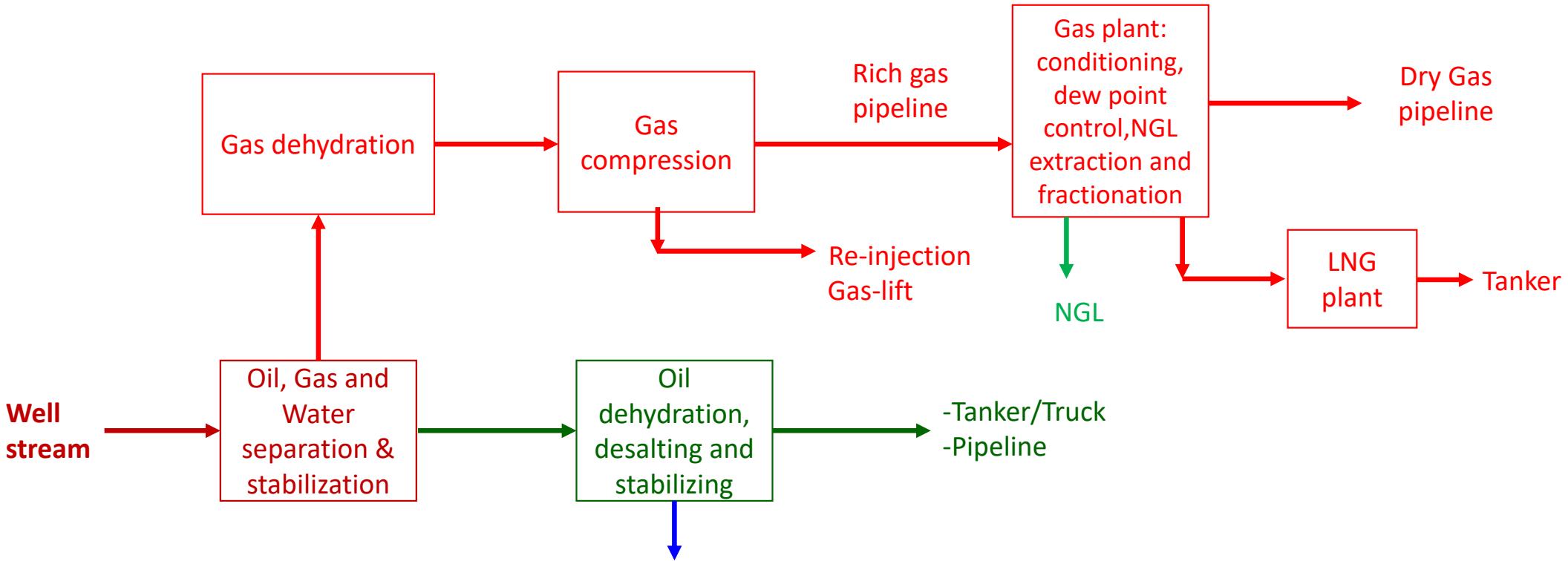


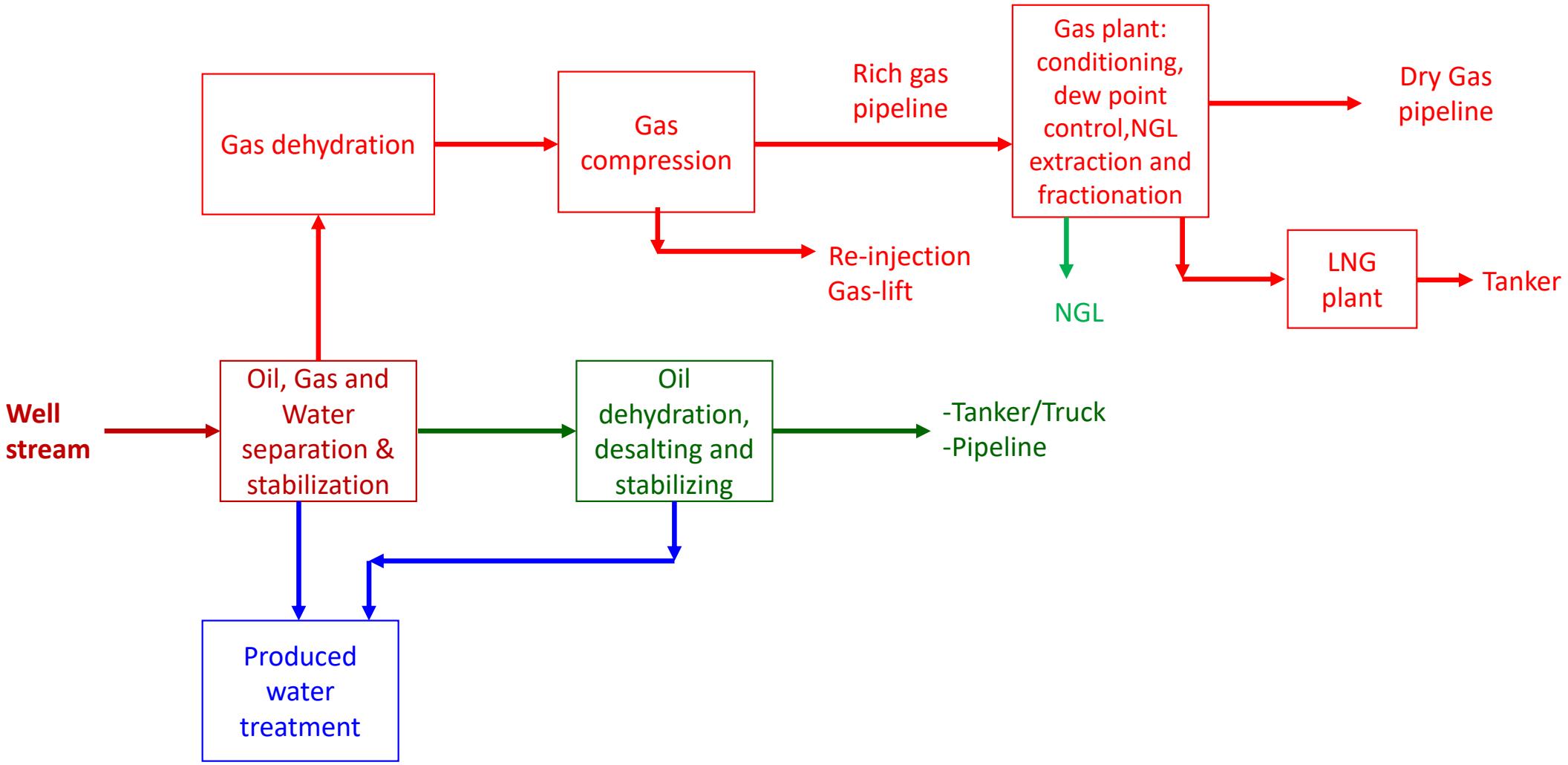


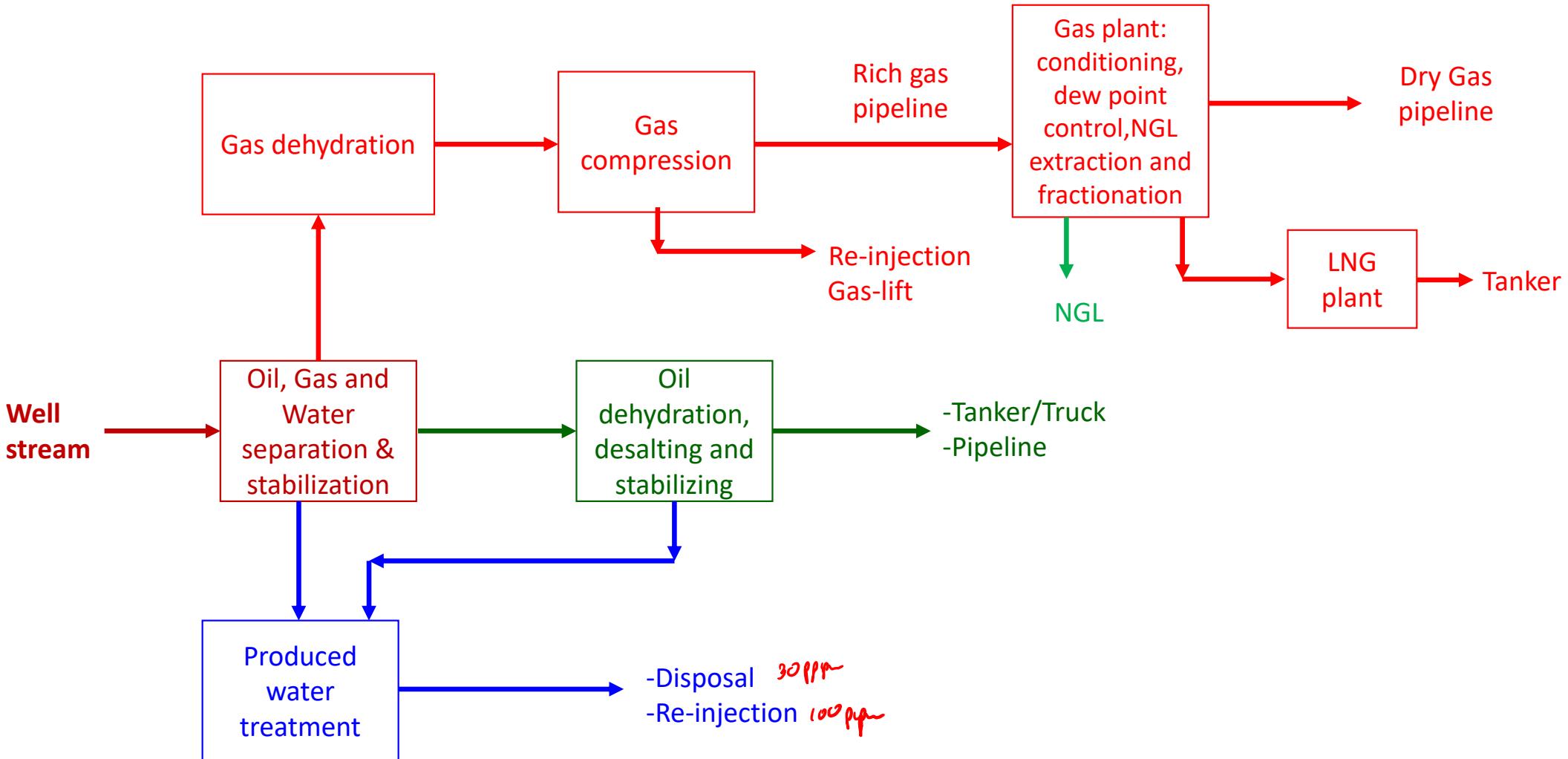


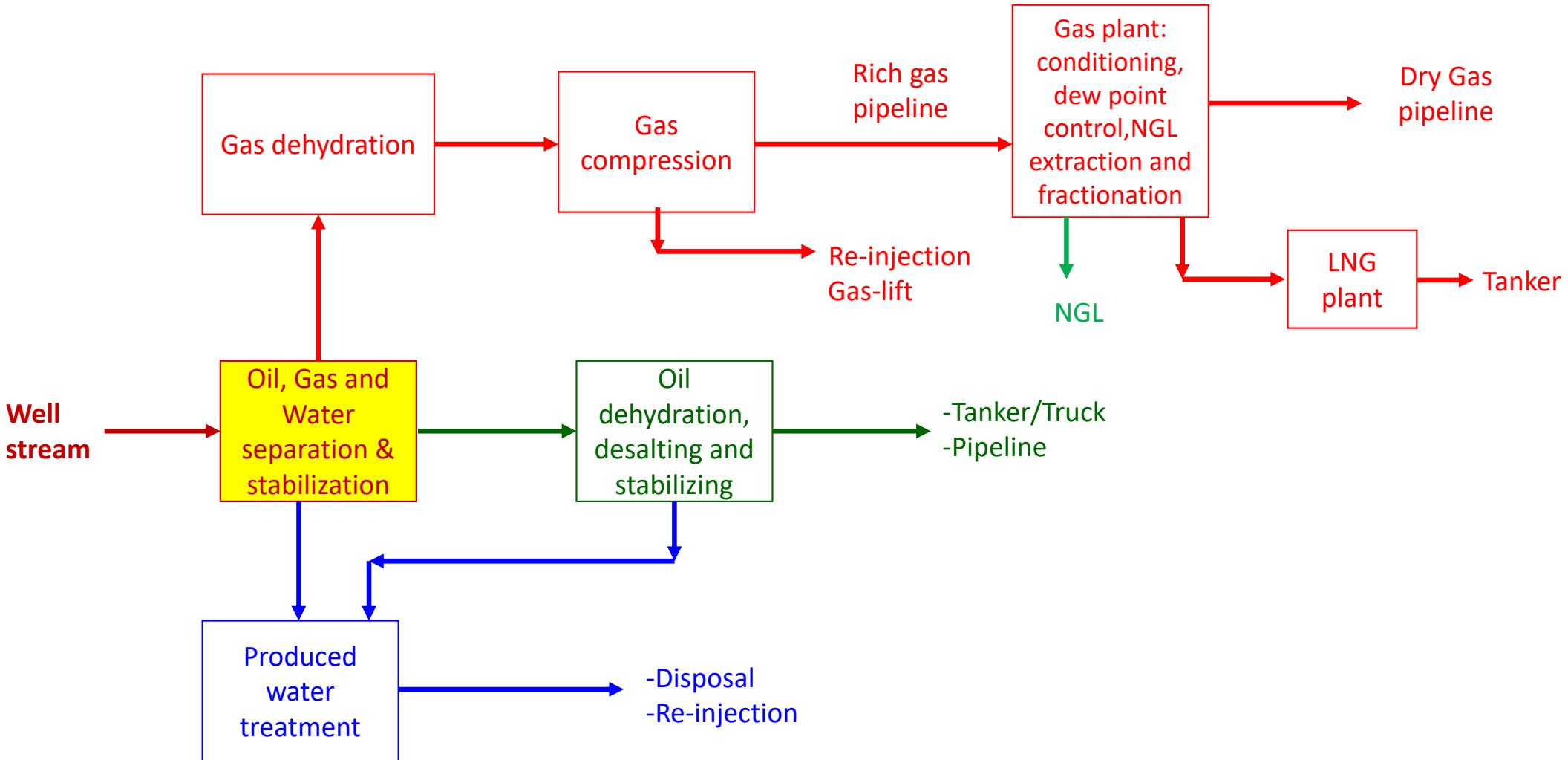


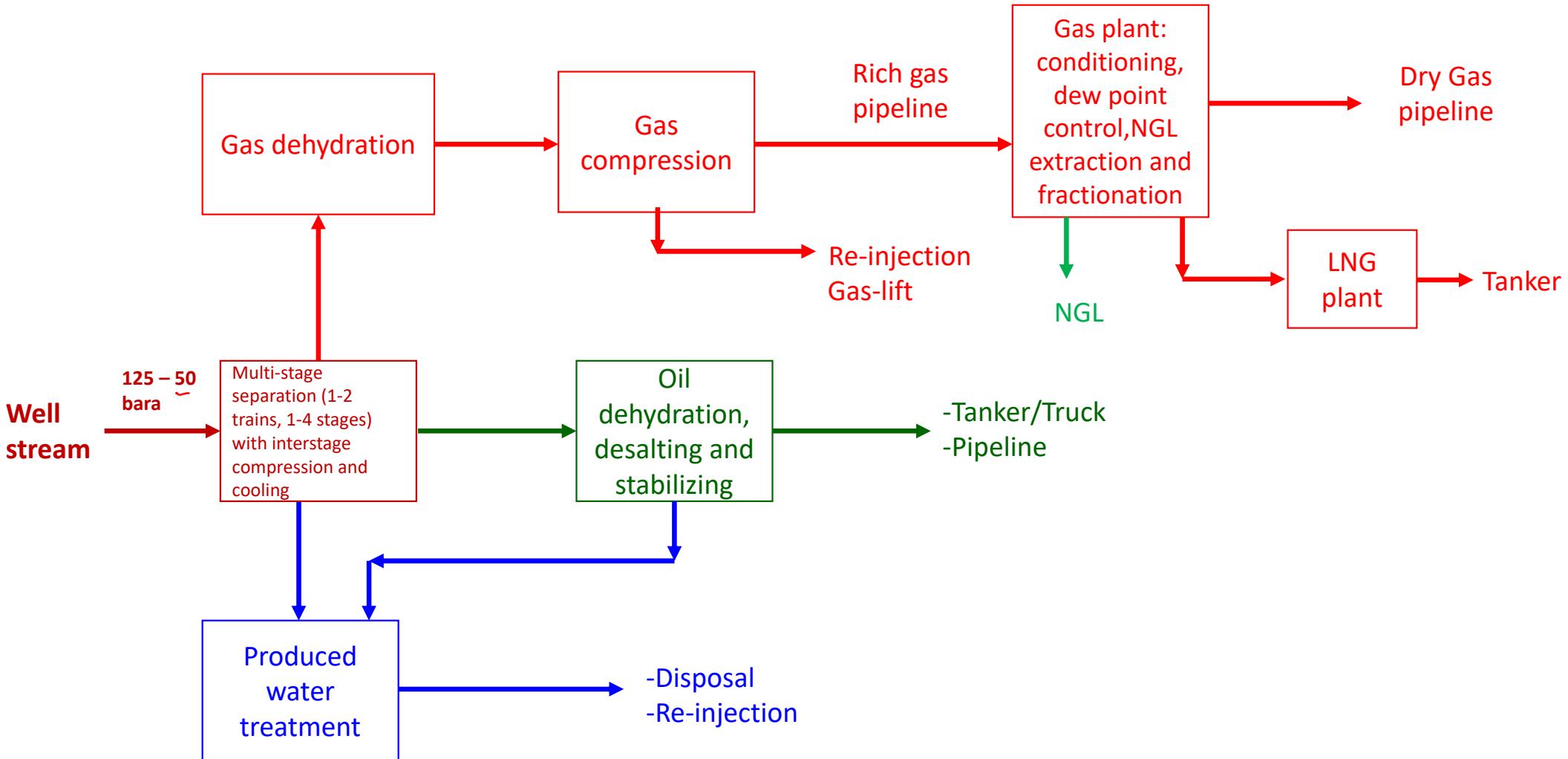


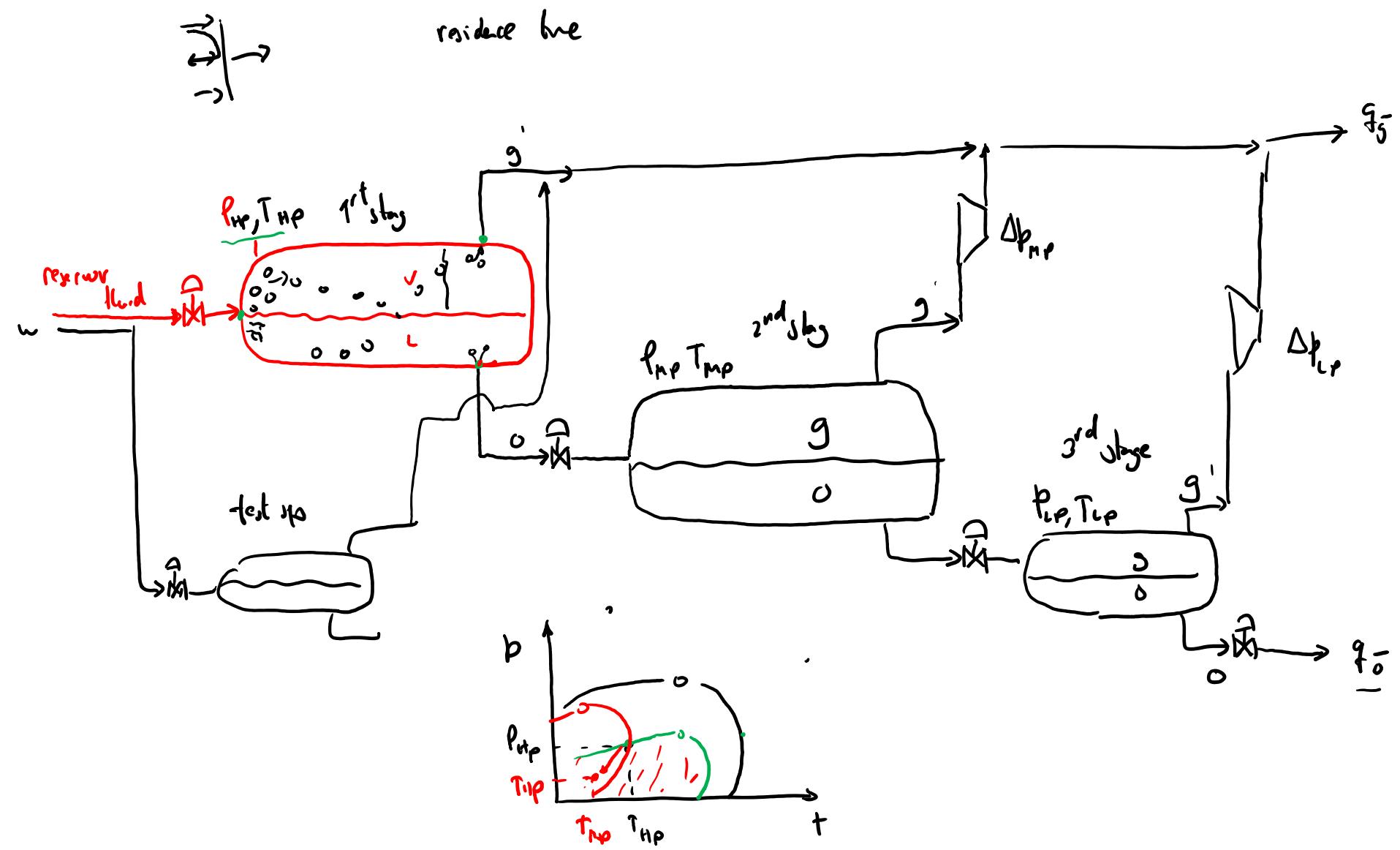






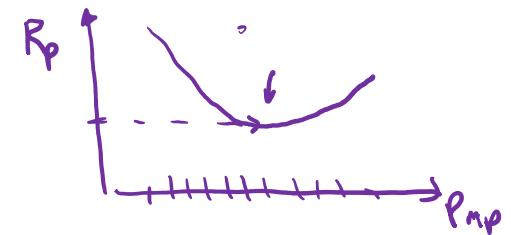
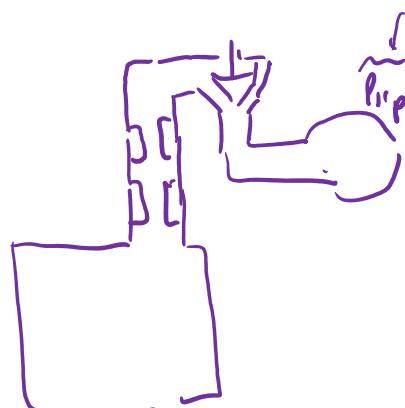
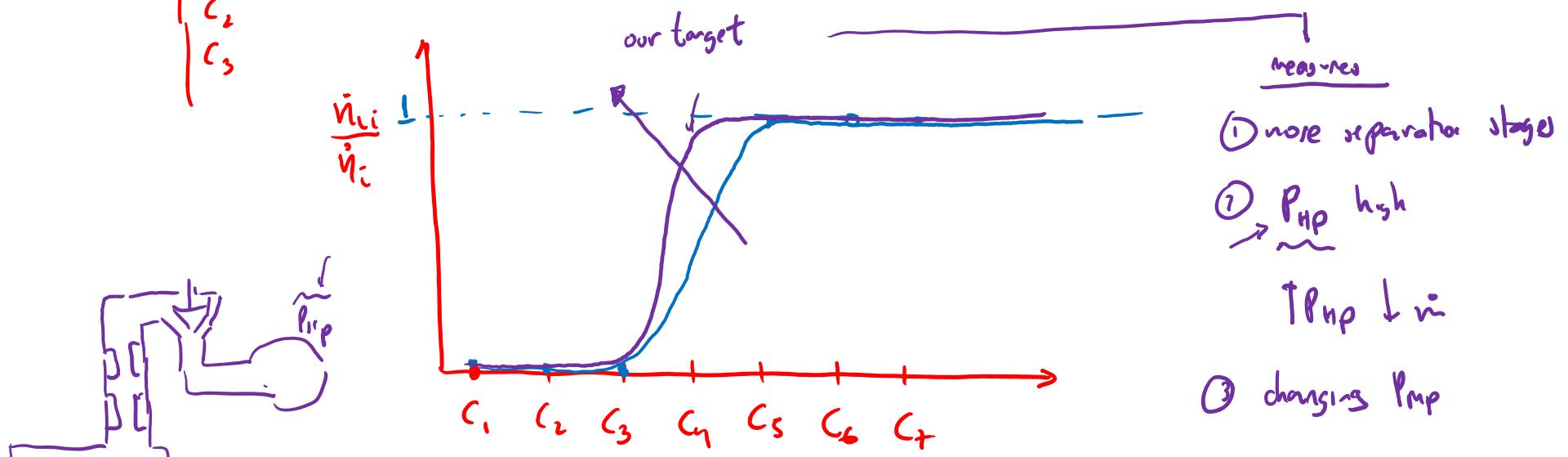
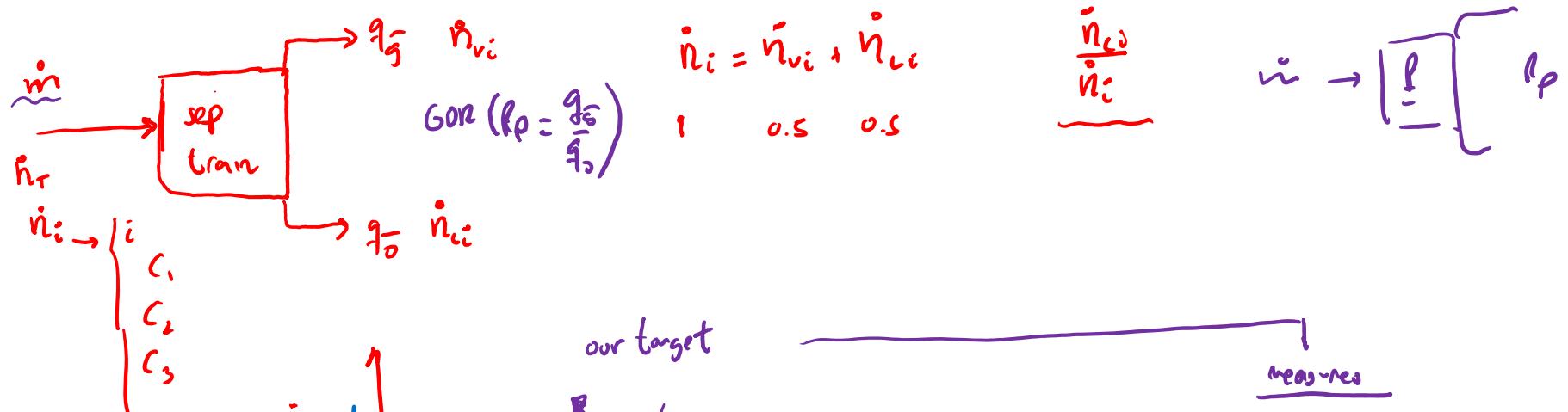






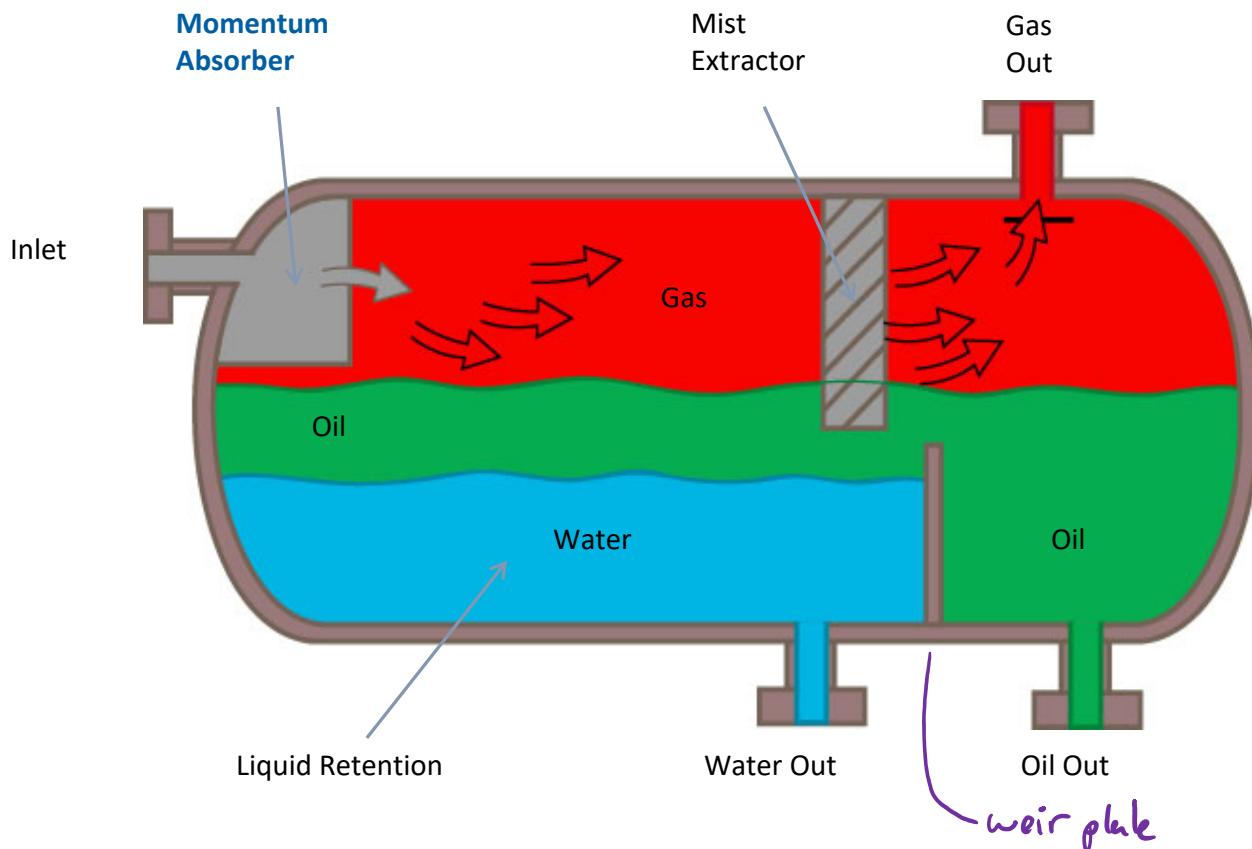
## **Class 20240126 - OUTLINE**

- Missing reference group member
- Upcoming reference group meeting
- Exercise set 1 published –Deadline 11.02
- cont. multi-stage separation
- How do a horizontal and vertical separator look like?
- Class exercise, Hysys simulation

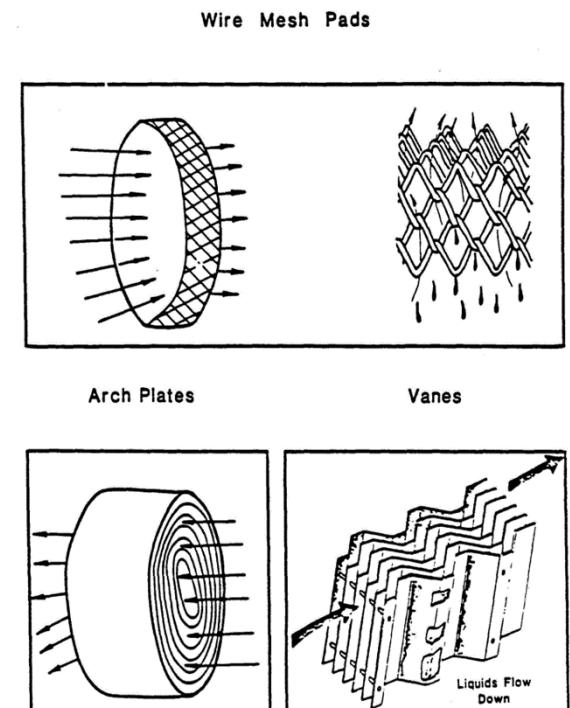


# Horizontal separator

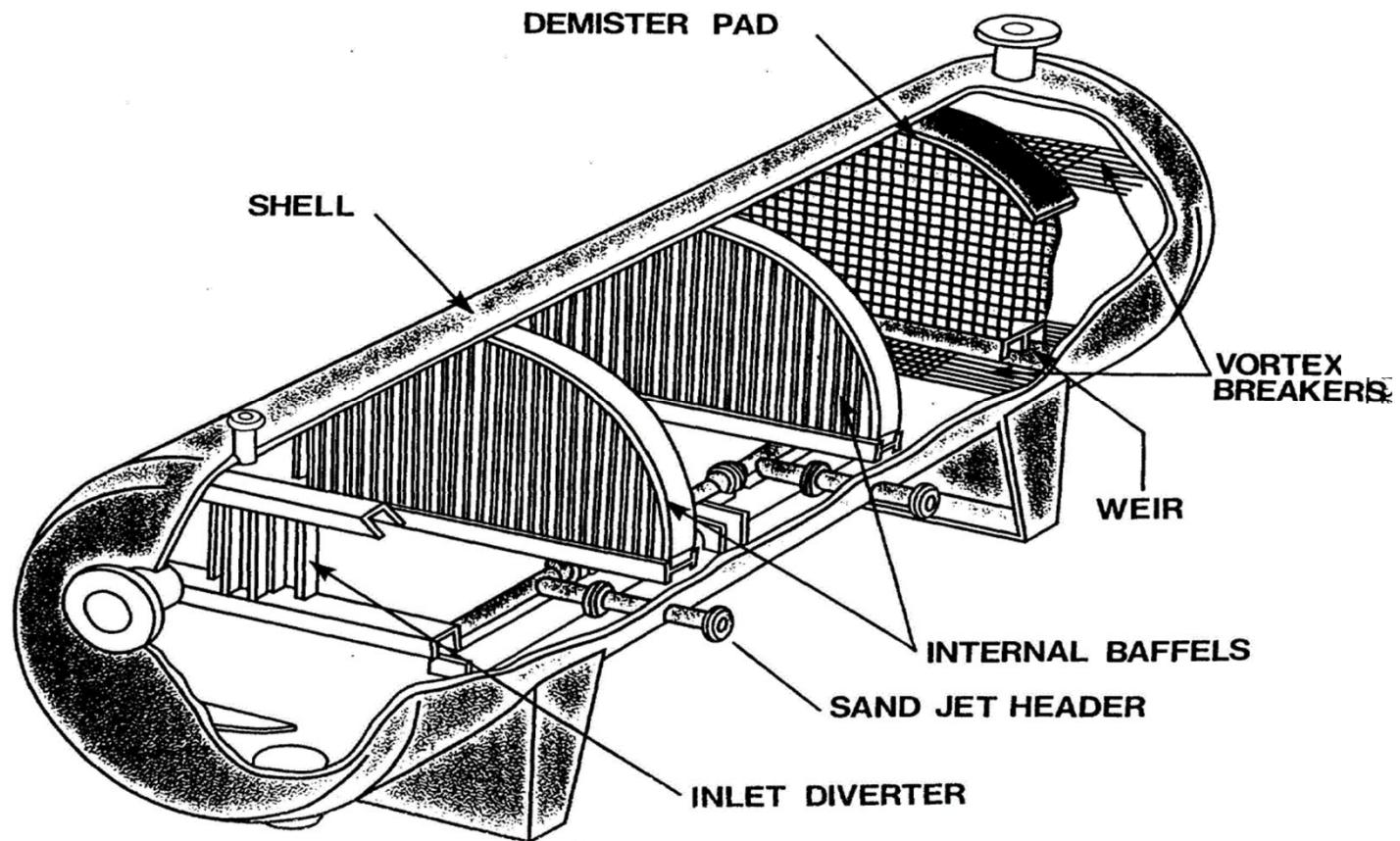
Horizontal Separator



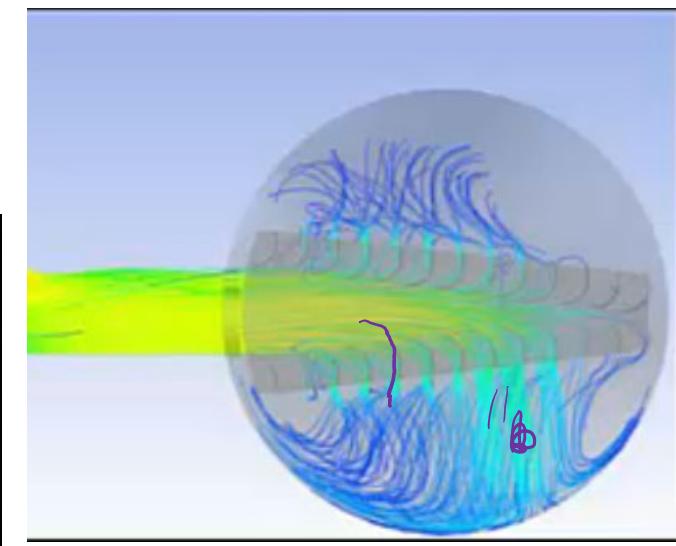
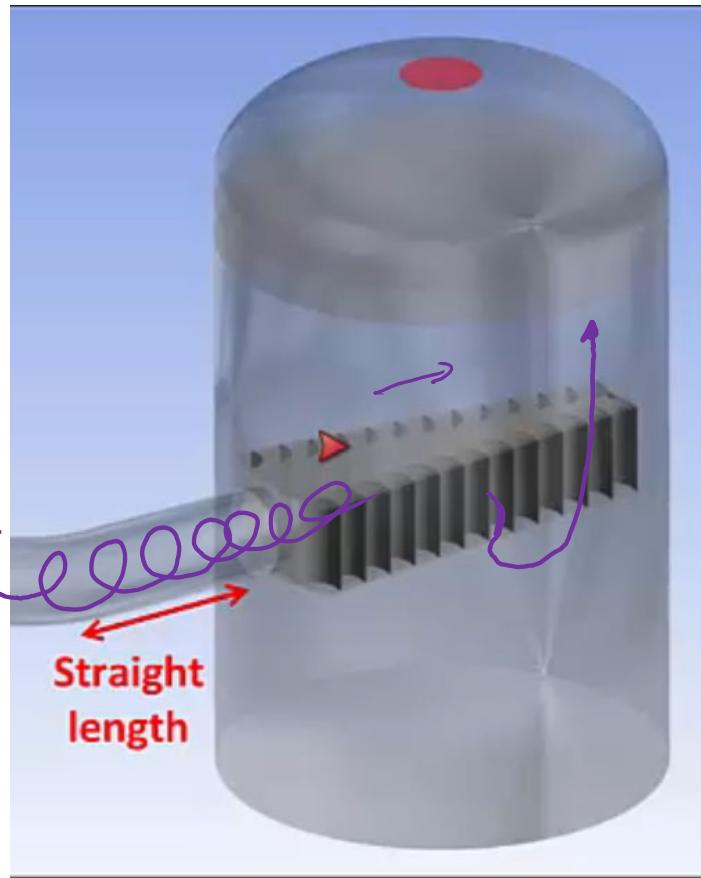
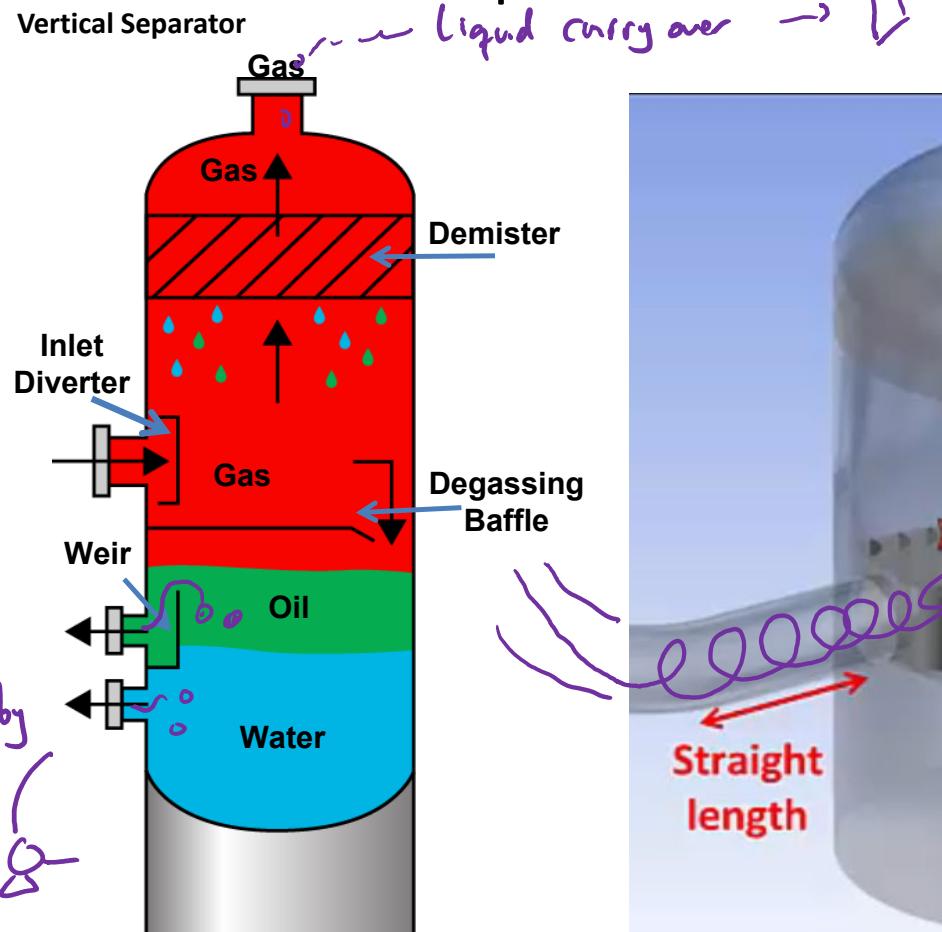
TYPICAL MIST EXTRACTOR



# Horizontal separator



# Vertical separator



{ $l_0$ }

# HYSYS Example

### Problem 3<sup>1</sup>

$\dot{Q}_0$

**Task 1.** Using Hysys<sup>2</sup> simulate a separation train with three stages (details given below). The total mass flow of hydrocarbons is: 27 000 kg/h. The composition of the stream is given below.

$$\dot{m} = \rho \cdot g \quad \text{kg/m}^3 \quad [\text{kg}_s] \quad \dot{m}$$

$$[\text{V}] \rightarrow [\text{M}]$$

$$\dot{q}_0 = [J \cdot \text{m}^3/\text{d}]$$

$$\dot{q}_g = [J \cdot \text{m}^3/\text{d}]$$

$$\text{API}, \dot{q}_w = \frac{\dot{q}_0}{\dot{q}_w(100)} \quad \dot{q}_w = [J \cdot \text{m}^3/\text{d}]$$

$$\dot{m} = \underbrace{\dot{q}_0 \cdot f_0}_{\dot{m}_0} + \underbrace{\dot{q}_g \cdot f_g}_{\dot{m}_g} + \dot{q}_w \cdot f_w \quad \downarrow 1000 \rightarrow 1200 \text{ m}^3/\text{d} (\text{brine})$$

$$\dot{q}_g = R_p \cdot \dot{q}_0 \quad f_g \quad \dot{f}_0 \rightarrow \dot{f}_g$$

$$R_p = \frac{M_w g}{M_w \text{air}}$$

$$P_{sc} V = n R_p T_{sc}^{1/2} t^{1/2}$$

$$n = \frac{m}{M_w}$$

$$\frac{t}{P} = \frac{1}{M_w} R_p (C_{air})$$

# Data

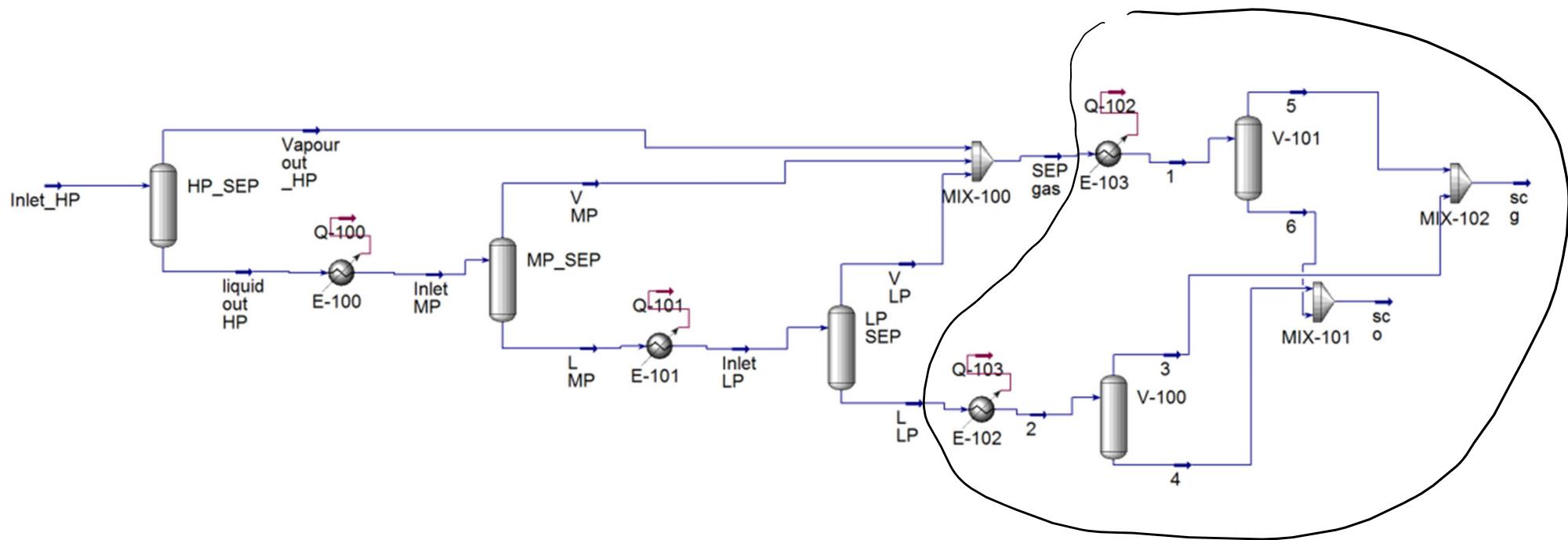
Component	Mole Fraction
Nitrogen	0.003672
CO <sub>2</sub>	0.001092
Methane	0.429256
Ethane	0.046897
Propane	0.029618
i-butane	0.014919
n-butane	0.009325
i-pentane	0.008446
n-pentane	0.005030
Hexanes	0.018433
Heptanes	0.041418
Octanes	0.049891
Nonanes	0.038403
Decanes	0.303600

Total mass flow: 27 000 kg/h

Separation Stage	Pressure (bara)	Temperature (C)
Stage 1	65	75
Stage 2	20	65
Stage 3	2	60
Standard Conditions	1.01325	15.66

## Tasks:

- Simulate the system in Hysys
- Perform a sensitivity study on the 2nd stage separation pressure to maximize oil production

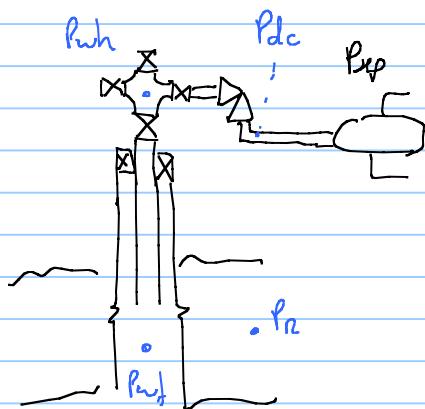


Taking to Standard conditions.  
This is an imaginary process.

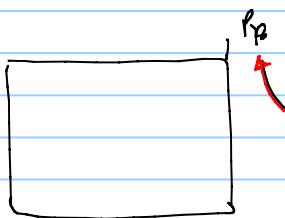
Youtube video: Intro to Excel VBA functions and sub

There were no notes for this video

Simplified dry gas production system



Reservoir model



Dry gas material balance

$$P_R = P_{Ri} \frac{z_R}{z_i} \left( 1 - \frac{G_p}{G} \right) f(g_j)$$

$g_j = f(t)$

$f$  uncertain value

$R_f$  recovery factor

gas deviation factor

$$\frac{T_R}{T_c} \frac{p_R}{p_c} \sim f(\text{gas composition})$$

MB dry gas equation is implicit

- Given  $R_f$ , assume  $P_R$
- with  $P_R$  compute  $z_R$
- verify that  $\epsilon = P_R - P_{Ri} \frac{z_R}{z_i} \left( 1 - R_f \right) = 0 \leq \text{TOLerance}$
- if not,

**3.3.2 Z-Factor Correlations.** Standing and Katz<sup>4</sup> present a generalized Z-factor chart (**Fig. 3.6**), which has become an industry standard for predicting the volumetric behavior of natural gases. Many empirical equations and EOS's have been fit to the original Standing-Katz chart. For example, Hall and Yarborough<sup>21,22</sup> present an

accurate representation of the Standing-Katz chart using a Carnahan-Starling hard-sphere EOS,

$$Z = ap_{pr}/y, \dots \quad (3.42)$$

where  $a = 0.06125t \exp[-1.2(1-t)^2]$ , where  $t = 1/T_{pr}$ .

The reduced-density parameter,  $y$  (the product of a van der Waals covolume and density), is obtained by solving

$$\begin{aligned} f(y) = 0 = & -ap_{pr} + \frac{y + y^2 + y^3 - y^4}{(1-y)^3} \\ & - (14.76t - 9.76t^2 + 4.58t^3)y^2 \\ & + (90.7t - 242.2t^2 + 42.4t^3)y^{2.18+2.82t}, \dots \quad (3.43) \end{aligned}$$

$$\begin{aligned} \text{with } \frac{df(y)}{dy} = & \frac{1 + 4y + 4y^2 - 4y^3 + y^4}{(1-y)^4} \\ & - (29.52t - 19.52t^2 + 9.16t^3)y \\ & + (2.18 + 2.82t)(90.7t - 242.2t^2 + 42.4t^3) \\ & \times y^{1.18+2.82t}. \dots \quad (3.44) \end{aligned}$$

The derivative  $\partial Z/\partial p$  used in the definition of  $c_g$  is given by

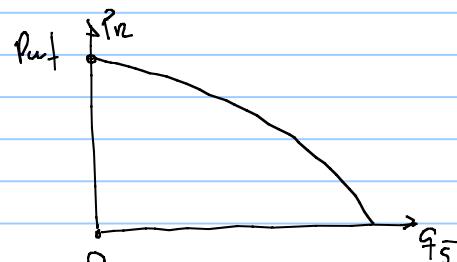
$$\left(\frac{\partial Z}{\partial p}\right)_T = \frac{a}{p_{pc}} \left[ \frac{1}{y} - \frac{ap_{pr}/y^2}{df(y)/dy} \right]. \dots \quad (3.45)$$

$$P_n \rightarrow P_{nf}$$

IPL equation

$$q_g = C_R (P_n^2 - P_{nf}^2)^n \quad \begin{matrix} \text{low pressure dry gas equation} \\ \text{back pressure exponent} \end{matrix}$$

inflow coefficient  $\{ T_R, K, h, s \}$  (skin factor)



- pseud-steady state regime  
(boundary dominated flow)  
page 37 of compendium

Equation approximation to Z chart

to predict  $T_c, p_c$  we will use  
Sutton correlations

Sutton<sup>7</sup> suggests the following correlations for hydrocarbon gas mixtures.

$$T_{pcHC} = 169.2 + 349.5\gamma_{gHC} - 74.0\gamma_{gHC}^2 \dots \quad (3.47a)$$

$$\text{and } p_{pcHC} = 756.8 - 131\gamma_{gHC} - 3.6\gamma_{gHC}^2. \dots \quad (3.47b)$$

$$\gamma_g = \frac{M_{wgas}}{M_{wair}} (28.97)$$

$$M_{wgas} = \sum_{i=1}^N z_i M_{wi}$$

- $P_{wf} \rightarrow P_{wh}$

Dry gas tubing equation

$$q_g = C_T \left( \frac{P_{wf}^2}{e^S} - P_{wh}^2 \right)^{0.5}$$

↑ elevation coefficient  
tubing coefficient (friction loss)

$$q_g = 0$$

$$P_{wf} = P_{wh} e^{S/2}$$

(hydrostatic losses)

Page 156, Appendix A of compendium

$$q_{sc} = \left( \frac{\pi}{4} \right) \cdot \left( \frac{R}{M_{air}} \right)^{0.5} \cdot \left( \frac{T_{sc}}{p_{sc}} \right) \cdot \left( \frac{D^5}{f_M \cdot L \cdot \gamma_g \cdot Z_{av} \cdot T_{av}} \right)^{0.5} \cdot \left[ \left( p_{wf}^2 - p_t^2 \cdot e^S \right) \cdot \left( \frac{S}{e^S - 1} \right) \right]^{0.5}$$

$$C_T = \left( \frac{\pi}{4} \right) \cdot \left( \frac{R}{M_{air}} \right)^{0.5} \cdot \left( \frac{T_{sc}}{p_{sc}} \right) \cdot \left( \frac{D^5}{f_M \cdot L \cdot \gamma_g \cdot Z_{av} \cdot T_{av}} \right)^{0.5} \cdot \left( \frac{S \cdot e^S}{e^S - 1} \right)^{0.5}$$

$$S = 2 \cdot L \cdot C_a = 2 \cdot \frac{M_g}{Z_{av} \cdot R \cdot T_{av}} \cdot L \cdot g \cdot \cos(\alpha)$$

Comments about Darcy equation

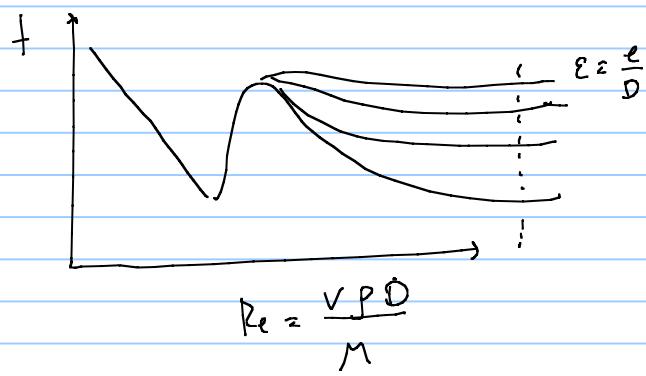
to compute  $G$

$$\tau_{av} \rightarrow \frac{\tau_{wf} + \tau_{wh}}{2}$$

An estimate of  $\tau_{wh}$  is needed

$$\tau_{av} \sim \frac{\tau_{wf} + \tau_{wh}}{2}$$

for friction factor



$M_2$  is  $\ll M_1$

$R_e \gg$

always in fully turbulent regime

$$V \approx f(q_{local}) \quad \text{for gas } V \uparrow \uparrow \quad \rho \text{ is low compared to liquid}$$

$$q_{local} + (g) \quad \text{liquid } V = [0.5 - 4] \frac{V_f}{g}$$

$$\text{gas } V = [5 - 4] \frac{V_f}{g}$$

$$f_m = f(\epsilon) \quad \text{however } \epsilon \neq (D) \\ \text{due to manufacturing}$$

bore equation for dry gas: (page 166)

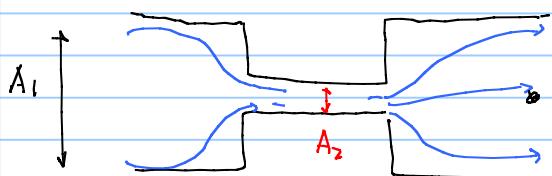
"opening" tuning factor  $\frac{R_0}{M_W}$

$$q_{\bar{g}} = \frac{p_1 \cdot T_{sc} \cdot A_2 \cdot C_d}{p_{sc}} \cdot \sqrt{2 \cdot \frac{R}{Z_1 \cdot T_1 \cdot M_W} \cdot \frac{k}{k-1} \cdot \left( y^{\frac{2}{k}} - y^{\frac{k+1}{k}} \right)}$$

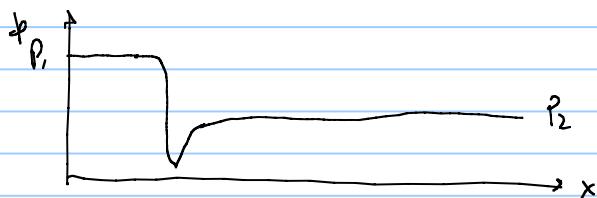
$p_{sc} = 1.01325 \text{ bar}$

$T_{sc} = 15.56^\circ\text{C}$

$y = \frac{P_2}{P_1}$  (downstream)  
(upstream)



if  $y > y_c \approx 0.6$ , there is untraced flow at the throat



if  $y > y_c$   $q_{\bar{g}} = q_{\bar{s}_c} =$

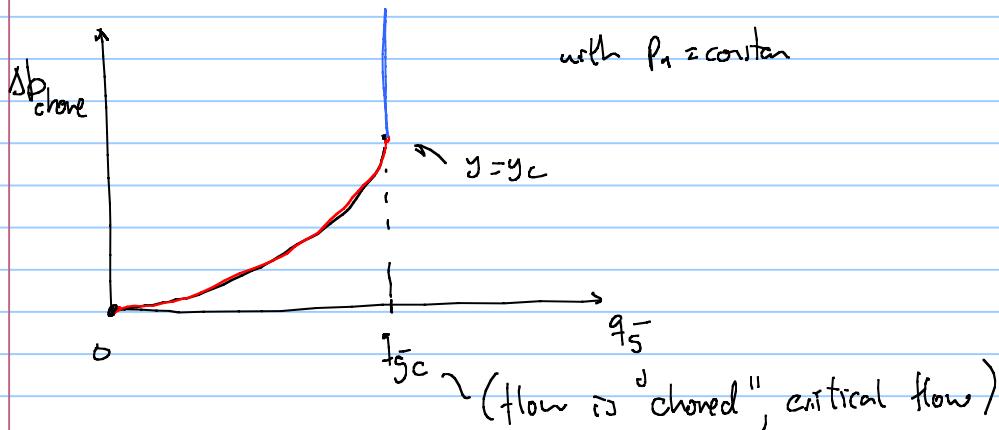
$$q_{\bar{g}} = \frac{p_1 \cdot T_{sc} \cdot A_2 \cdot C_d}{p_{sc}} \cdot \sqrt{2 \cdot \frac{R}{Z_1 \cdot T_1 \cdot M_W} \cdot \frac{k}{k-1} \cdot \left( y^{\frac{2}{k}} - y^{\frac{k+1}{k}} \right)}$$

in blue  $y_c$   $y_c$

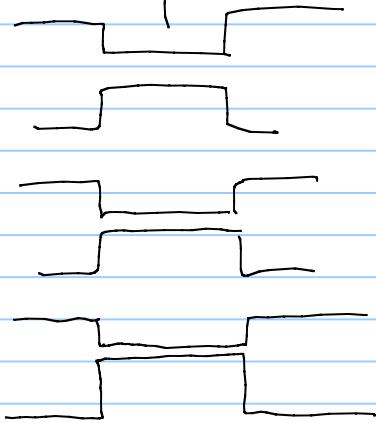
if  $y < y_c$

$$q_{\bar{g}} = \frac{p_1 \cdot T_{sc} \cdot A_2 \cdot C_d}{p_{sc}} \cdot \sqrt{2 \cdot \frac{R}{Z_1 \cdot T_1 \cdot M_W} \cdot \frac{k}{k-1} \cdot \left( y^{\frac{2}{k}} - y^{\frac{k+1}{k}} \right)}$$

in red  $y_c$



in onshore fields, bean chokes are often used  
given in  $\frac{1}{64}$ "



offshore often adjustable  
chokes are used  
needle choke



adjustable throat area

$\rightarrow P_{sep}$  flowline  $\rightarrow$  tubing equation can be used for flowline

horizontal flowline, the tubing equation simplifies to

$$\dot{q}_S = C_{FL} \left( \frac{P_{dc}^2 - P_{sep}^2}{\rho g} \right)^{0.5}$$

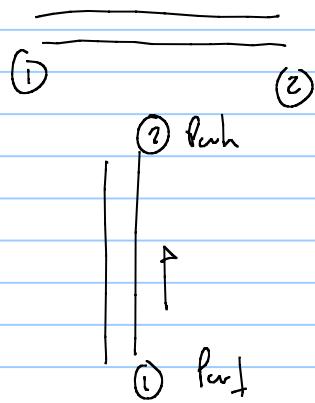
$S=0$  (L'Hopital)

### VBA Visual basic for applications

for pipe equations in VBA (1) is upstream

$\xrightarrow{q}$

(2) is downstream



## **Class 20240201 - OUTLINE**

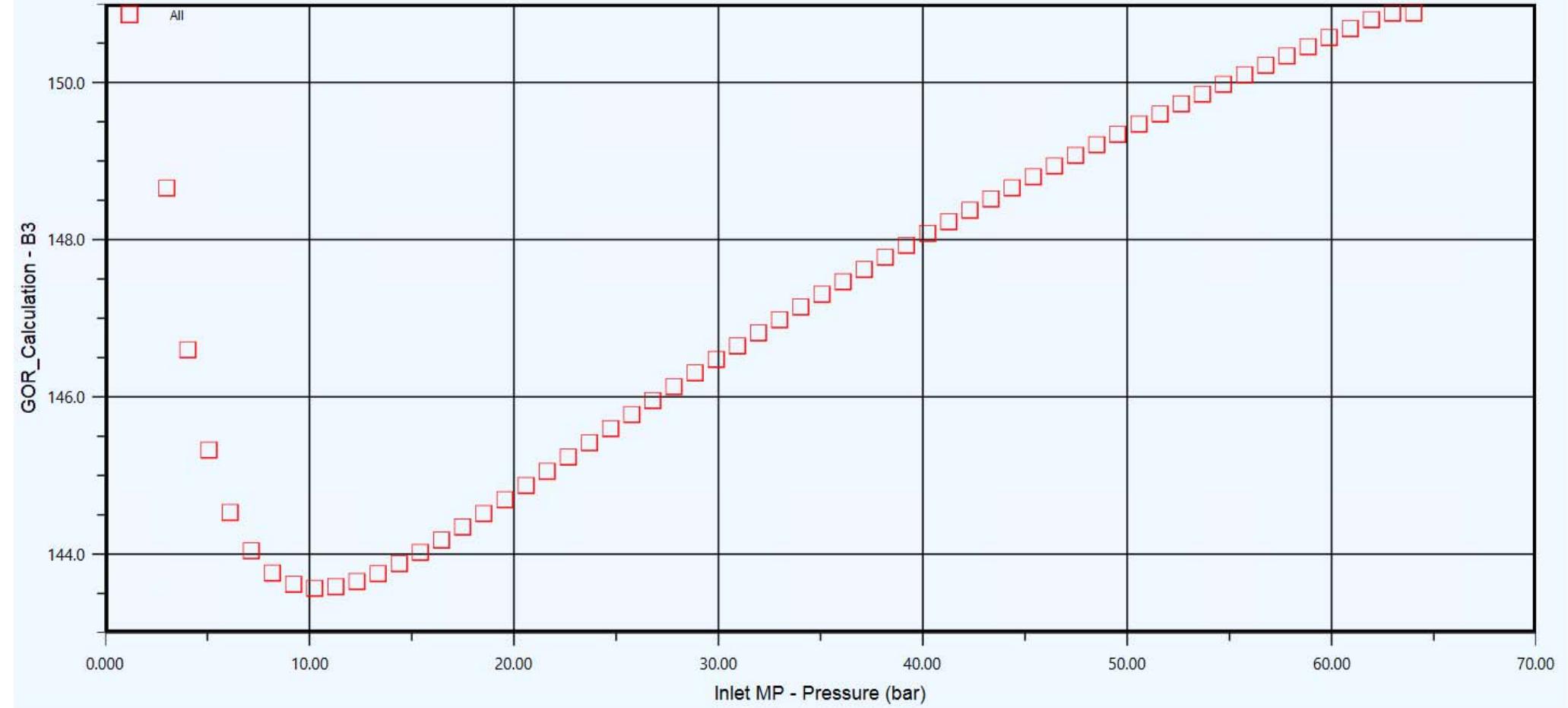
- cont Class exercise (mandatory exercise 1), Hysys simulation
- How a real separation process looks like in reality
- Simple sizing of horizontal gas-oil separator

## Tasks:

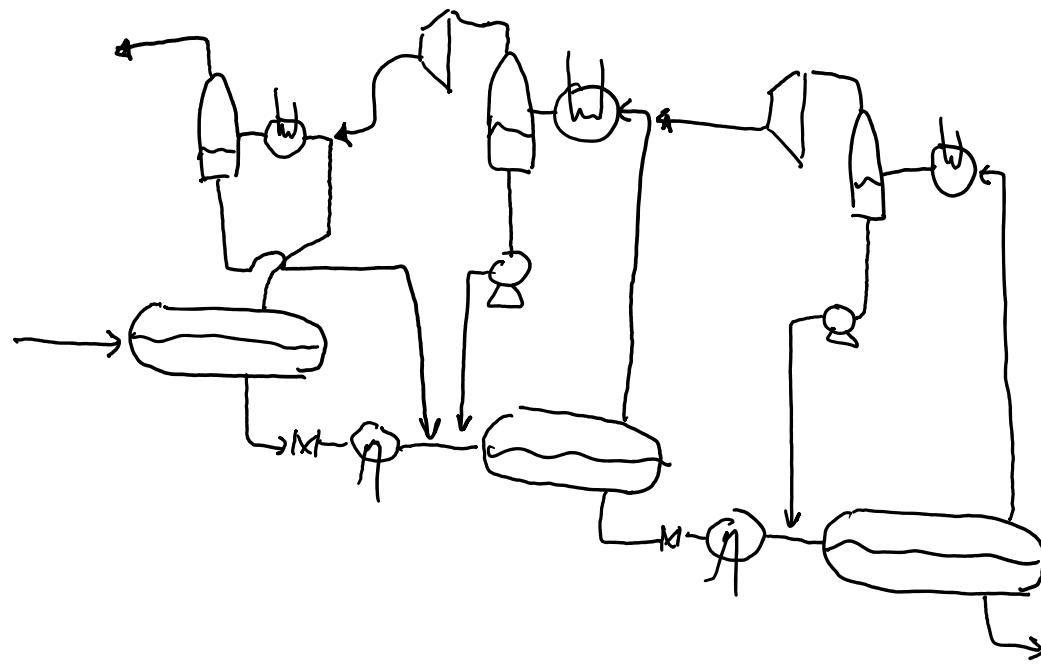
cont Class exercise (mandatory exercise 1), Hysys simulation

- Simulate the system in Hysys
- Perform a sensitivity study on the 2nd stage separation pressure to maximize oil production

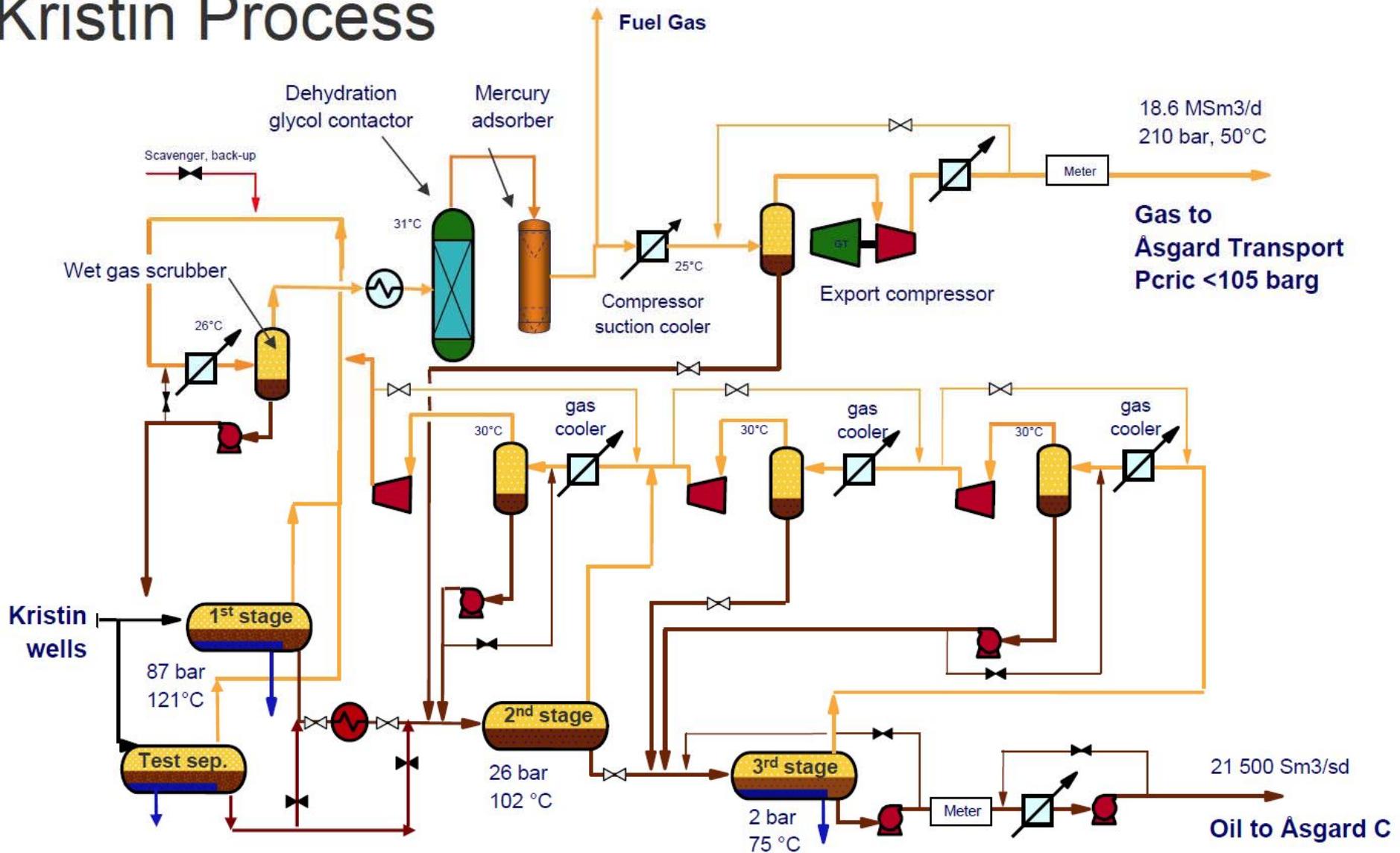
## Case Study 1

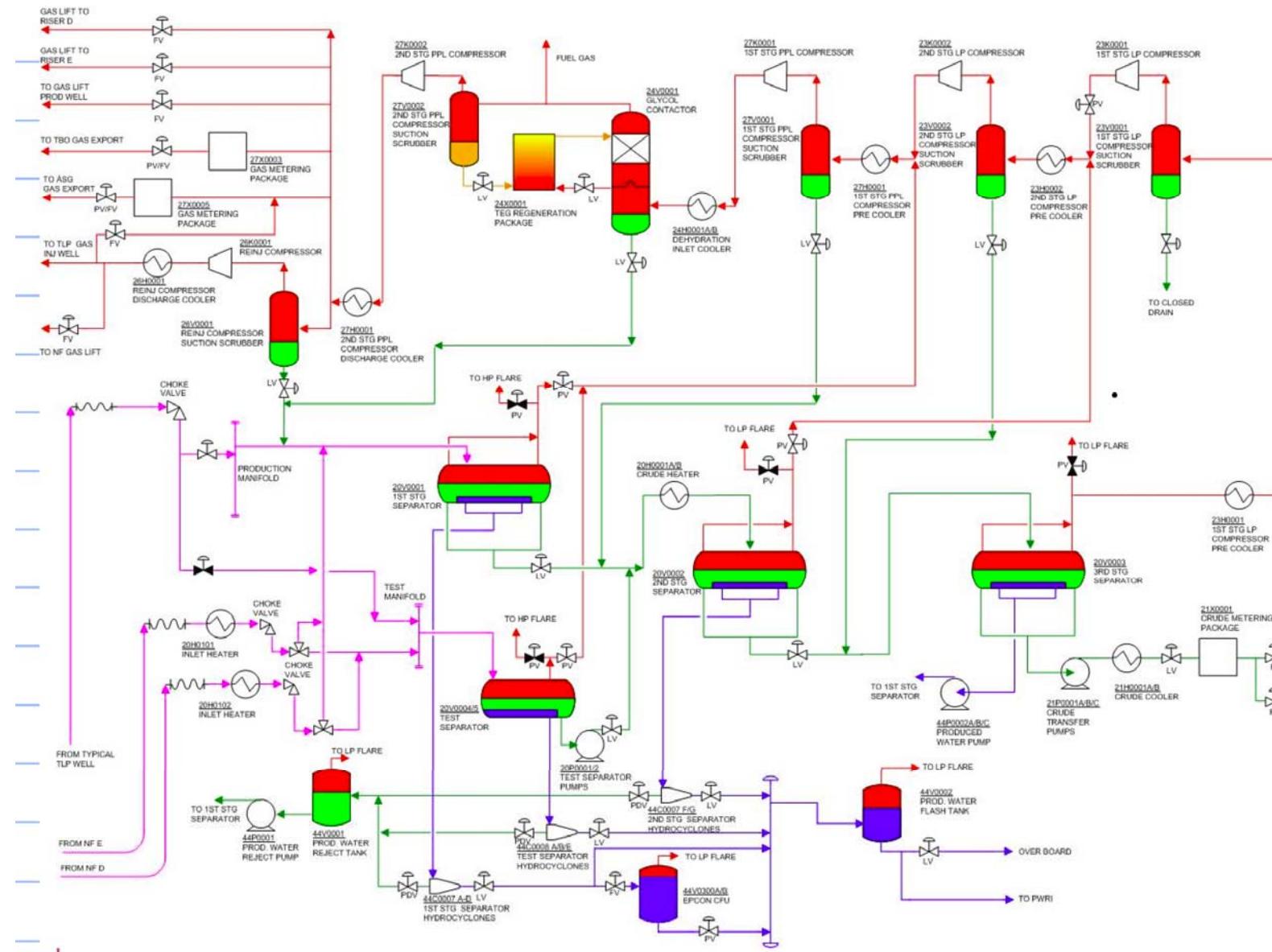


How does the separation process looks like in reality:



# Kristin Process





- Example of (simple) sizing horizontal gas-oil separator

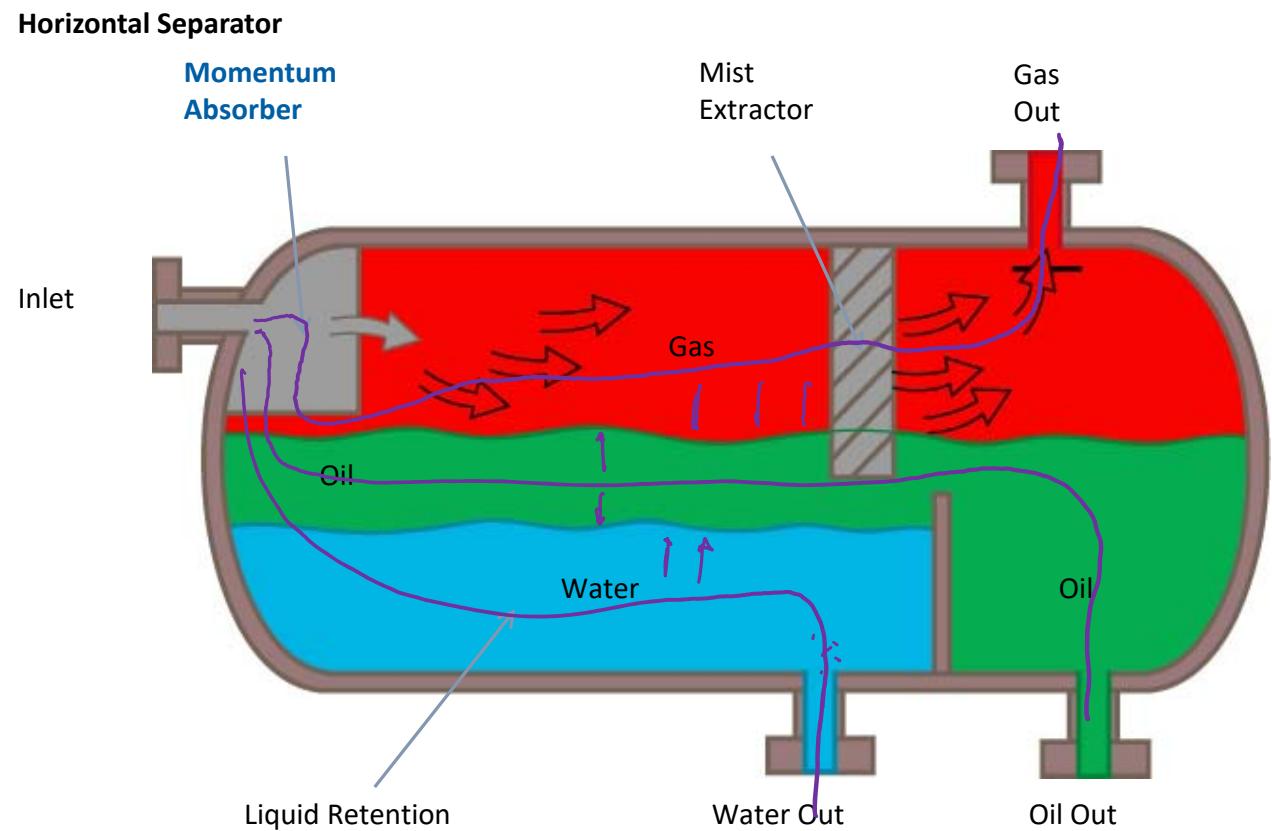
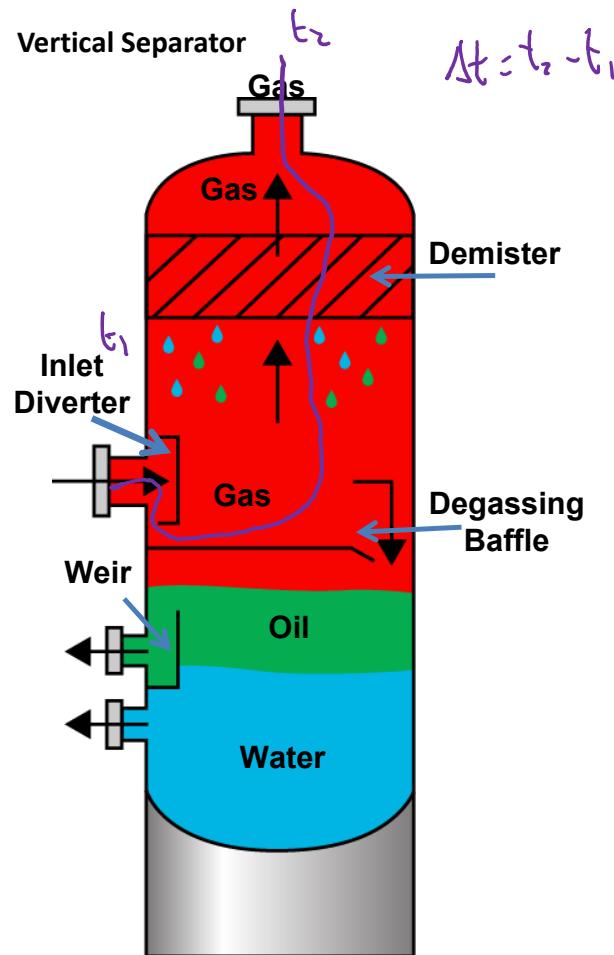
# Separation design theory

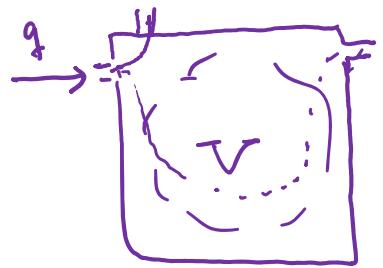
Find separator dimensions such as:

$$\begin{cases} L \\ ID, L \end{cases}$$

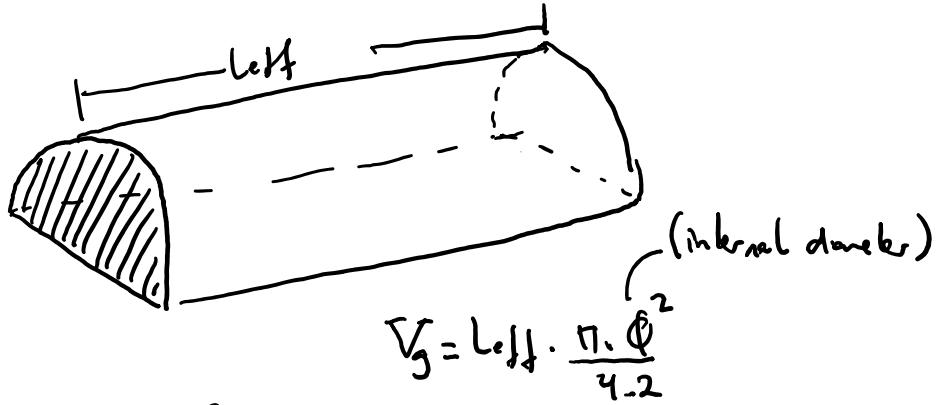
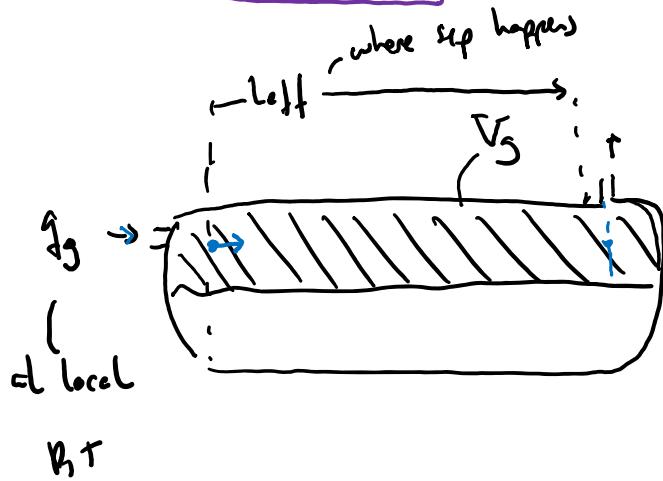
Residence time > separation time

# Residence time





$$t_{res} = \frac{V}{q} \quad \begin{bmatrix} V \\ \frac{V}{q} \end{bmatrix}$$



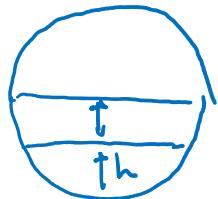
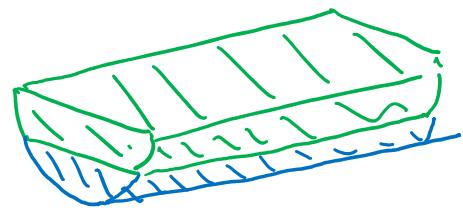
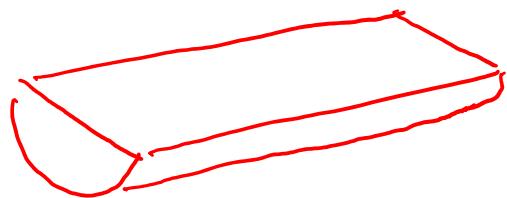
$$t_{res} = \frac{V_g}{g_s} = L_{eff} \cdot \frac{\pi \cdot \varrho^2}{8 \cdot g_s}$$

$$V_g = \frac{g_s}{A} = \frac{g_s}{\frac{\pi \cdot \varrho^2}{4}}$$

$$t_{res} = \frac{L_{eff}}{V_g} = \frac{L_{eff} \cdot \pi \cdot \varrho^2}{7_s \cdot \delta}$$

30 s  $\rightarrow$  2,3 min

residue tree of oil

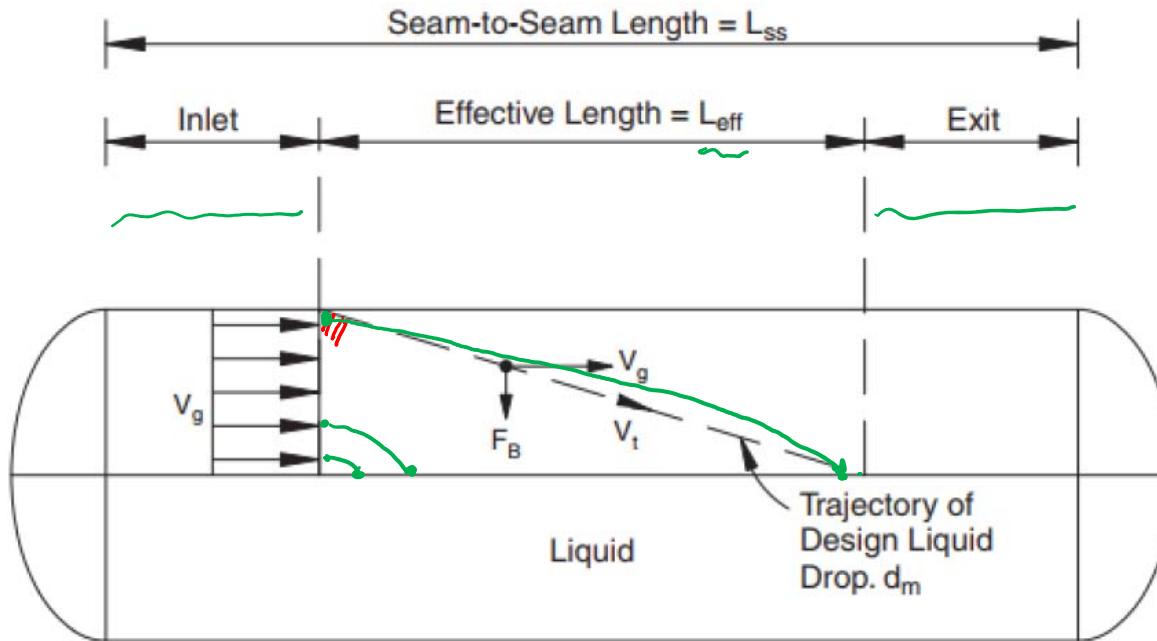


# Separation time - gas

time that it takes for an oil droplet to travel from top to liquid level

$$t_{sep} = \frac{h}{v_s}$$

settling  
velocity



Legend:

$$V_g = \text{Average Gas Velocity} = \frac{Q}{A}$$

$V_t$  = Terminal or Setting Velocity Relative to Gas

$F_B$  = Buoyant Force

# Separation time = settling time

how to estimate  $v_s$

$$F_{\text{drag}} \uparrow \quad \rho_f V_d \cdot g \text{ (buoyancy)} \uparrow \quad m \cdot g \text{ (weight)} \downarrow$$

$$\rightarrow (\rho_p - \rho_f) V_d g$$

$$F_{\text{drag}} = \frac{1}{2} \rho_f \cdot A_d \cdot C_d \frac{V_s^2}{4}$$

$\underbrace{\qquad \qquad \qquad}_{\text{drag coefficient}}$

$$\Sigma F = 0$$

assumed  $V$  (smallest possible, more conservative)

$$V_d = V_s = \sqrt{\frac{4 \rho_d g}{3 C_d} \frac{(\rho_d - \rho_f)}{\rho_f}}$$

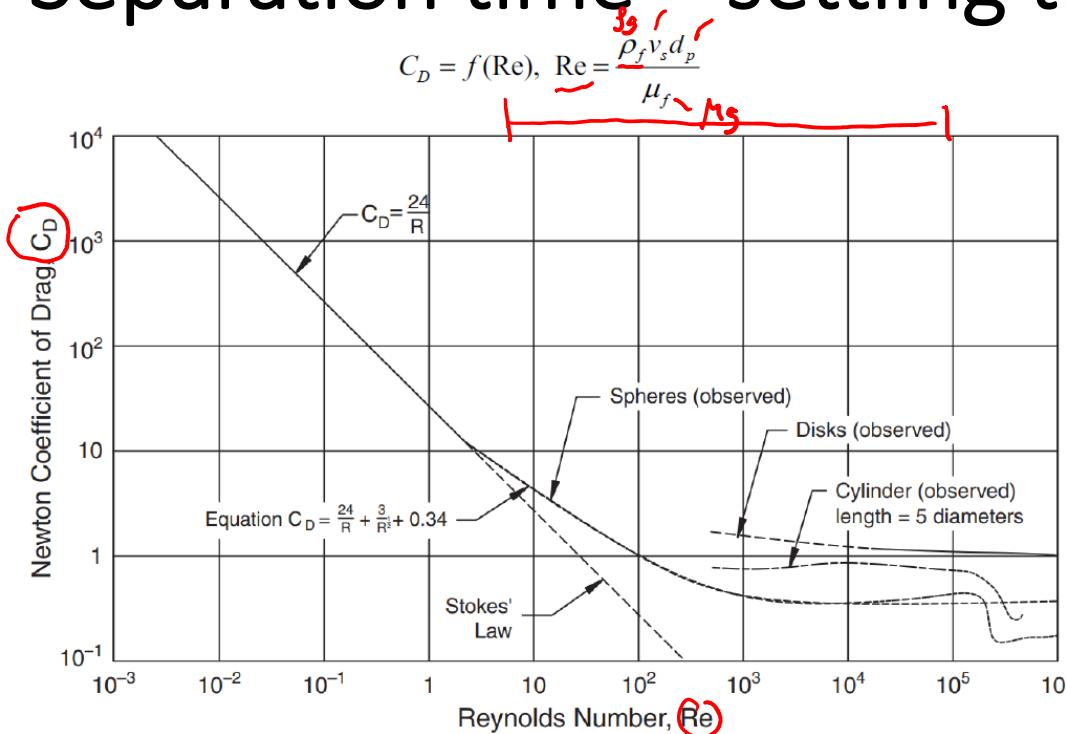
?

?

$\rho_{\text{oil}}$        $\rho_{\text{gas}}$

If it is a bubble of gas in oil, the direction of drag is opposite,  
Then it should be (denf-dend)

# Separation time = settling time



Laminar Flow	$\text{Re} < 2$	$C_D = \frac{24}{\text{Re}}$
Transition Flow	$2 \leq \text{Re} < 2 \cdot 10^5$	$C_D = \frac{24}{\text{Re}} + \frac{3}{\sqrt{\text{Re}}} + 0.34$
Turbulent	$2 \cdot 10^5 < \text{Re}$	0.2

case ① oil droplet in gas

$M_g \downarrow$

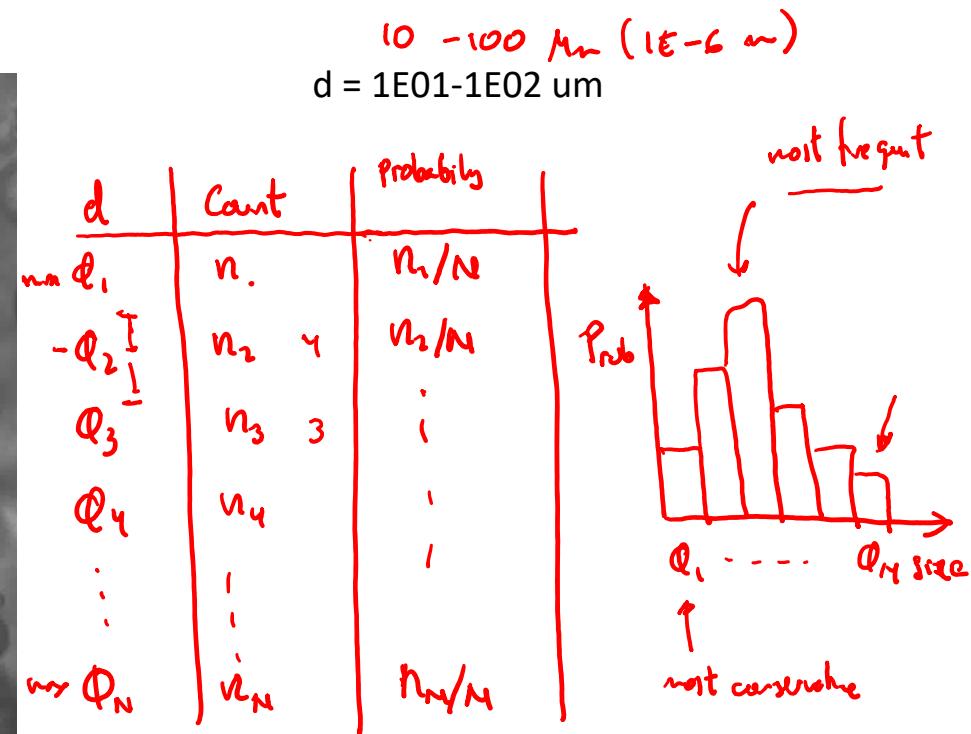
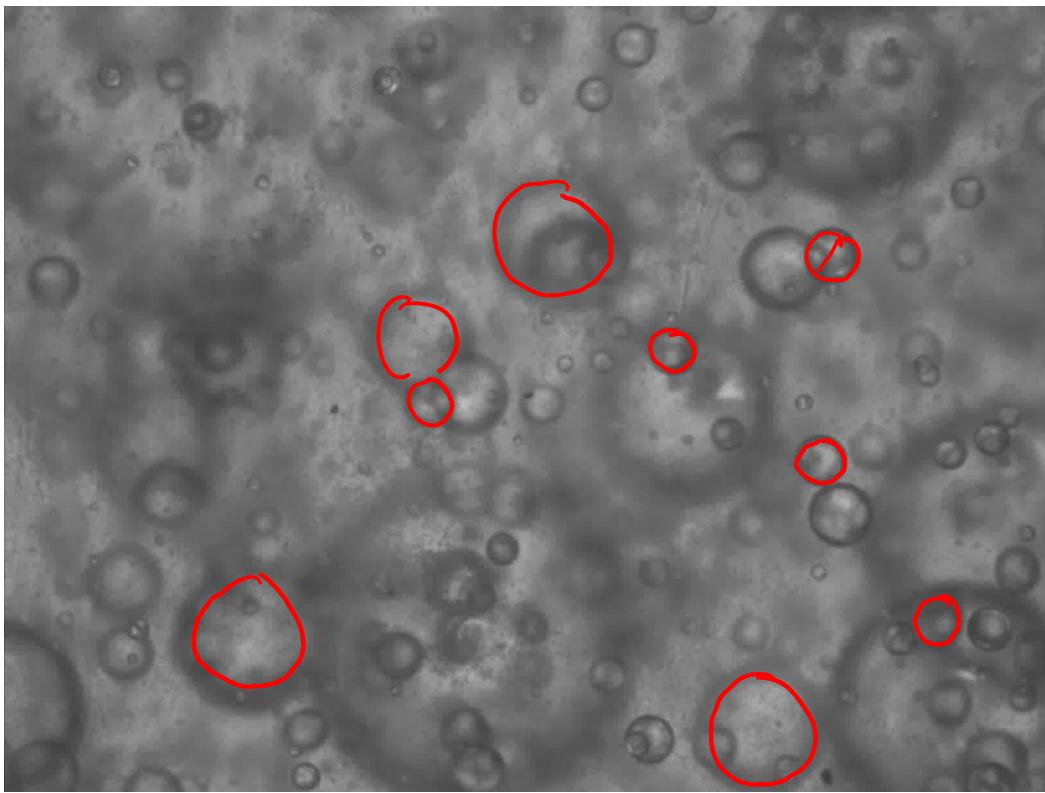
$\text{Re}_d \uparrow$

case ② oil in water  
water droplet in oil

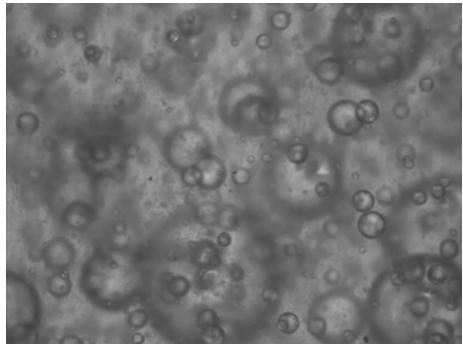
$M_o \uparrow$

$\text{Re} \downarrow$

# Separation time – droplet size distribution



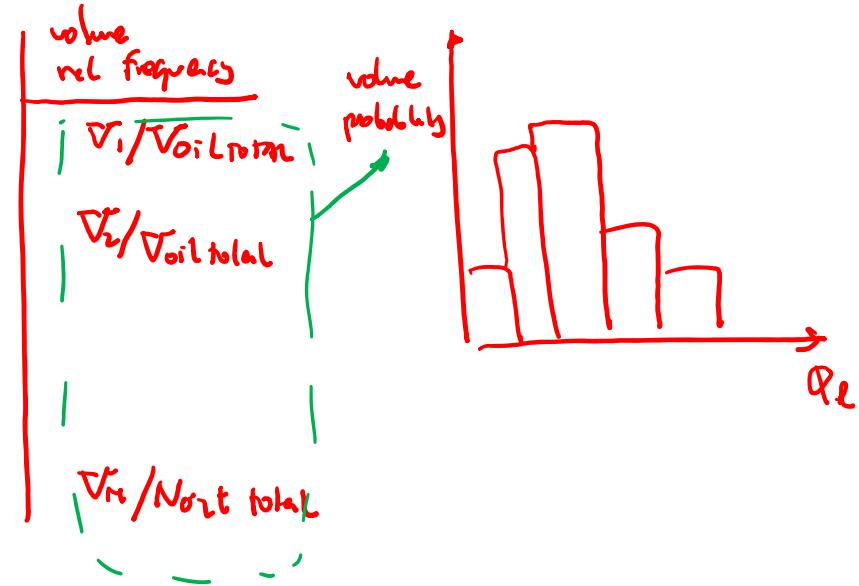
# Separation time – droplet size distribution



$d = 1E01-1E02 \text{ um}$

(volume based)

$d$	cat	volume
$\phi_1$	$n_1$	$n_1 \cdot \frac{4}{3} \pi (\frac{\phi_1}{\delta})^3 = V_1$
$\phi_2$	$n_2$	$n_2 \cdot \frac{4}{3} \pi (\frac{\phi_2}{\delta})^3 = V_2$
:	:	:
:	:	:
$\phi_N$	$n_N$	$= V_N$



the calculation of  $V_s$  is important! (because  $C_0 = f(V_s)$ )

$$V_s = \sqrt{\frac{4 \rho_d g}{3 C_0} - \frac{(\rho_d - \rho_f)}{\rho_f}}$$

$$Re = \frac{\rho_f \cdot \rho_d \cdot V_s}{\eta_f}$$

The same equation can be used for

- Bubbles of gas in liquid
- droplets of liquid in liquid

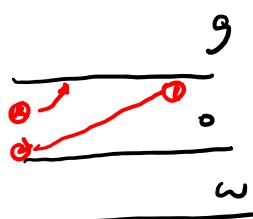
BUT if the droplet/bubble is going up, the order of the density difference must be changed.

- ① assume  $V_s$
  - ② calculate  $Re$
  - ③ calculate  $C_0$
  - ④ calculate  $V_s$
  - ⑤ check if  $V_{s\text{ calc}} = V_{s\text{ assumed}}$
- yes ↓ solution
- not

# Oil separation time

API

Crude API	Retention Time (min)
>30	1
20 - 30	1 - 2
10 - 20	2 - 4



$$I \frac{h}{\sqrt{g}} = t_{sep}$$

too optimistic

So, experience-based values are often used instead (see table above)

$t_{exp} > t_{sep,cal} = t_{retention}$

# Separation time = settling time

for droplet of oil in gas :

$t_{residence}$  ), settling

$$\frac{\text{Lefl } \rho_{\text{sep}}^2 \pi}{\sigma \cdot g_{\text{sg}}} > \frac{\rho_{\text{sep}}/2}{v_s} \quad \text{assuming liquid level is at half separator}$$

$$\boxed{\frac{\text{Lefl } \rho_{\text{sep}}}{\sigma \cdot g_{\text{sg}}} > \frac{4 \cdot g_{\text{sg}}}{v_s \cdot \pi}}$$

# **Class 20240202 - OUTLINE**

- Simple sizing of horizontal gas-oil separator – Exercise
- Other topside processing equipment

# Simple Calculation example

- Design an oil-gas horizontal separator (Leff and ID) for the first stage of the Hysys problem provided earlier
- oil droplet size: 150 um
- Slenderness ratio (Lss/D): 3-4 (assume Lss=Leff+D)
- Max ID: 4.5 m
- Max Leff: 20 m

Crude API	Retention Time (min)
>30	1
20 - 30	1 - 2
10 - 20	2 - 4

API spec 12J

# Simple Calculation example

[http://www.ipt.ntnu.no/~stanko/files/Courses/TPG4230/2023/Class\\_files/Simple\\_Separator\\_sizing\\_exercise.xls](http://www.ipt.ntnu.no/~stanko/files/Courses/TPG4230/2023/Class_files/Simple_Separator_sizing_exercise.xls)

Use hysys to get properties and rates of oil and gas

$$\text{Left. } \Phi_{\text{sep}} > \frac{q_{\text{gas}}}{v_s \cdot \pi} \quad ?$$

t?

$$v_d = v_s = \sqrt{\frac{4 q_d g}{3 G} \left( \frac{f_d - f_t}{f_t} \right)}$$

$$R_e = \frac{f_g \rho_d v_s}{M_g \mu}$$

$$q_{\text{gas}} = 48.54 \text{ m}^3/\text{h} \quad \checkmark$$

$$\begin{aligned} \Phi_d &= 150 \text{ E-6 m} \\ f_o &= 631.7 \text{ kg/m}^3 \\ f_g &= 46.81 \text{ kg/m}^3 \\ M_g &= 1.44 \text{ E-2 kg} \end{aligned} \quad \left. \begin{array}{l} \\ \\ \end{array} \right\} v_s$$

$$v_s = 0.16 \text{ m/s}$$

$$\text{left. } \Phi_{\text{sep}} > 4 \cdot \left( \frac{48.54}{3600} \right) \frac{1}{0.16 \cdot 3.1415} \text{ m}^3/\text{s} \quad \left( \frac{1}{\text{m}^3/\text{s}} \right)$$

$$\text{left. } \Phi_{\text{sep}} > 0.11 \text{ m}^3/\text{s}$$

Convention: red is input, blue is calculated

# Simple Calculation example

slenderness ratio condition

$$l_{ss} = l_{eff} + \phi \quad \text{not always true!}$$

$$3 \leq \frac{l_{ss}}{\phi_{sep}} \leq 4$$

$$3 \leq \frac{l_{eff}}{\phi_{sep}} + 1 \leq 4$$

$$2 \leq \frac{l_{eff}}{\phi_{sep}} \leq 3$$

$$2\phi_{sep} \leq l_{eff} \leq 3\phi_{sep}$$

# Simple Calculation example

oil separation time

$t_{\text{sep}} > \overbrace{t_{\text{sep oil}}}^{\rightarrow \text{separation of gas bubbles from oil to gas}}$

$$\frac{\text{left. } \phi_{\text{sep}}^2 \cdot \pi}{8} > t_{\text{sep oil}}$$



$\frac{q_o}{\text{from bable API 12 T}}$

{ from Hysys 39.18 m³/h  $\rightarrow 0.0108 \text{ m}^3/\text{s}$

$$\text{API gravity} = \frac{141.5}{\text{SG}} - 131.5$$

$$\text{API} = \frac{141.5}{\frac{631.2}{1000}} - 131.5 = 92$$

API > 30

Crude API	Retention Time (min)
>30	1
20 - 30	1 - 2
10 - 20	2 - 4

$$\frac{\text{left } \Phi_{\text{sep}}^2 \pi}{8 q_0} \geq 60 \text{ s}$$

$$n \%$$

$$\text{left } \Phi_{\text{sep}}^2 \geq \frac{60}{\pi} \cdot \frac{q_0}{8} = \frac{60 \cdot 1}{\pi} \cdot 0.0108 = 1.65 \text{ m}^3 \rightarrow$$

$$\text{left. } \Phi_{\text{sep}}^2 \geq 1.65$$

$l_{eff} \cdot \phi_{sep} > 0.11 \text{ m}^2$  ① separation of oil from gas

$$2\phi_{sep} \leq l_{eff} \leq 3\phi_{sep}$$

② slenderness ratio

$$l_{eff} \cdot \phi_{sep}^2 > 1.65 \text{ m}^3$$

③ separation of gas from oil

decide  $l_{eff}$ ,  $\phi_{sep}$ , as small as possible

$\downarrow$  cost  $\downarrow$  transport

### Attempt 1

$$\varnothing_{\text{rep}} = 0.5 \text{ m}$$

$$l_{\text{eff}} = 1.5 \text{ m}$$

$$0.5 \cdot 1.5 = 0.75 > 0.11 \quad \textcircled{1} \quad \checkmark$$

$$(l_{\text{eff}}/\varnothing_{\text{g}}) = 3 \leq 3 \quad \textcircled{2} \quad \checkmark$$

$$1.5 \cdot (0.5)^2 > 1.65 \quad \textcircled{3}$$

$0.375 > 1.65 \quad \times \quad \text{don't work}$

### Attempt 2

$$\begin{aligned} \varnothing_{\text{rep}} &= 0.9 \text{ m} \\ l_{\text{eff}} &= 2.1 \text{ m} \end{aligned} \quad \left. \right\}$$

$$\textcircled{1} \quad 0.9 \cdot 2.1 = 1.89 > 0.11 \quad \checkmark$$

$$\textcircled{2} \quad \frac{l_{\text{eff}}}{\varnothing_{\text{rep}}} = 2.33 \quad 2 \leq 2.33 \leq 3 \quad \checkmark$$

$$\textcircled{3} \quad l_{\text{eff}} \cdot \varnothing_{\text{rep}}^2 = 1.7 > 1.65 \quad \checkmark$$

limiting constraint !

### **Problem 1 (20 points)**

You are part of the field development team for a recently discovered reservoir. You are considering to re-use equipment from an existing platform that will be dismantled soon.

Consider a horizontal gas oil separator with an effective length of 5 m and an inner diameter of 1.7 m. consider the required residence time for gas is 20 s, and the required retention time for oil is of 60 s. During normal operating conditions, half of the separator is filled with liquid.

**Task 1 (5 points).** Calculate what are the maximum volumetric rates of oil and gas (at local pressure and temperature,  $q_o$  and  $q_g$ ), in  $\text{m}^3/\text{d}$ , than can flow through the separator.

**Task 2 (5 points).** From the values calculated in task 1, compute the maximum allowed standard conditions rates of oil and gas (in  $\text{Sm}^3/\text{d}$ ). Use the following expressions:

$$q_{\bar{g}} = \frac{q_g}{B_g} + \frac{R_s}{B_o} q_o$$

$$q_{\bar{o}} = \frac{q_o}{B_o}$$

Use the following values for the black oil properties:

$$B_g = 0.01 [\text{m}^3/\text{Sm}^3]$$

$$R_s = 50 [\text{Sm}^3/\text{Sm}^3]$$

$$B_o = 1.2 [\text{m}^3/\text{Sm}^3]$$

**Task 3 (5 points).** Consider that a field starts producing in plateau mode with a producing gas-oil ratio (GOR or  $R_p$ ) equal to  $150 \text{ Sm}^3/\text{Sm}^3$ . What is the maximum oil production (in standard conditions, in  $\text{Sm}^3/\text{d}$ ) that can be processed by the horizontal separator.

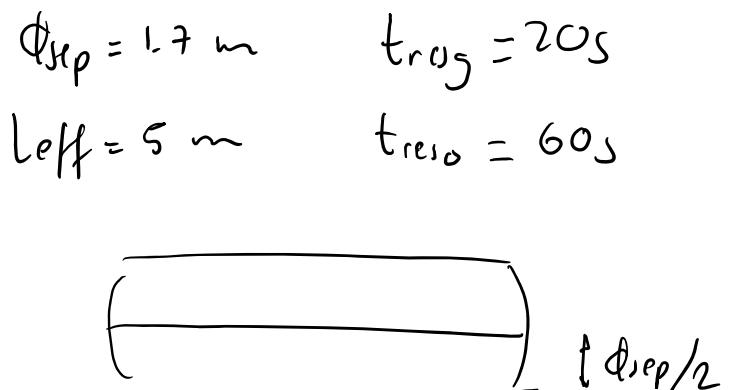
**Task 4 (5 points).** The value of producing gas-oil ratio used in Task 3 was calculated using a reservoir model assuming that vertical permeability is low and there is no coning from the gas cap. There is high uncertainty in this assumption. If a higher value of vertical permeability is used, the producing gas-oil ratio reaches  $400 \text{ Sm}^3/\text{Sm}^3$  during the plateau period. For this situation, estimate what is the maximum oil production (in standard conditions, in  $\text{Sm}^3/\text{d}$ ) that can be processed by the horizontal separator.

**Additional information:**

- You can use the Excel sheet provided to perform your calculations.
- Add text explaining your procedure

# metry, calculate max oil and gas

[http://www.ipt.ntnu.no/~stanko/files/Courses/TPG4230/Old\\_Exams/2023/TPG4230\\_2023\\_Exam\\_solution.pdf](http://www.ipt.ntnu.no/~stanko/files/Courses/TPG4230/Old_Exams/2023/TPG4230_2023_Exam_solution.pdf)



**Task 1 (5 points).** Calculate what are the maximum volumetric rates of oil and gas (at local pressure and temperature,  $q_o$  and  $q_g$ ), in  $\text{m}^3/\text{d}$ , than can flow through the separator.

$$\frac{t_{\text{req}}}{20 \text{ s}} = \frac{\left( \frac{V_g}{q_g} \right)}{q_g ?} \rightarrow \frac{1 + \frac{S}{2}}{8} \cdot Q_{\text{sep}} \cdot \pi$$

$$t_{\text{req}} > t_{\text{sep}} \\ t_{\text{req}} = t_{\text{sep}}$$

$$q_{g\max} = \frac{Q_{\text{sep}}^2 \pi}{8 t_{\text{req}}} = 0.283 \text{ m}^3/\text{s} = \underline{24501 \text{ m}^3/\text{d}} \rightarrow \frac{\text{m}^3/\text{d}}{\text{at local P,T 1st stage sep}}$$

$$\frac{t_{\text{req},o}}{60 \text{ s}} = \frac{V_o}{q_o} \rightarrow \frac{Q_{\text{sep}}^2 \pi}{8} \cdot \frac{1}{t_{\text{req},o}} \\ q_{o\max} = 1167 \text{ m}^3/\text{d} \rightarrow \frac{\text{m}^3/\text{d}}{}$$

$$q_o @ p, T \xrightarrow{BO \text{ prop}} q_{\bar{o}} @ p_{sc}, t_{sc}$$

**Task 2 (5 points).** From the values calculated in task 1, compute the maximum allowed standard conditions rates of oil and gas (in  $\text{Sm}^3/\text{d}$ ). Use the following expressions:

$$q_{\bar{g}} = \frac{q_g}{B_g} + \frac{R_s}{B_o} q_o$$

$$q_{\bar{o}} = \frac{q_o}{B_o}$$

Use the following values for the black oil properties:

$$B_g = 0.01 [\text{m}^3/\text{Sm}^3]$$

$$R_s = 50 [\text{Sm}^3/\text{Sm}^3]$$

$$B_o = 1.2 [\text{m}^3/\text{Sm}^3]$$

$$q_{\bar{g}} = \frac{q_g}{B_g} + \frac{R_s}{B_o} q_o = 2790391 \text{ Sm}^3/\text{d}$$

↗ 24501      ↗ SO      ↗ 8167  
 ↘ 0.01      ↘ 1.2

$$q_{\bar{o}} = \frac{q_o}{B_o} = 6805 \text{ Sm}^3/\text{d}$$

↘ 1.2

To refresh about Boproperties check chapter 4 of the compendium (ca 100 ish page)

**Task 3 (5 points).** Consider that a field starts producing in plateau mode with a producing gas-oil ratio (GOR or  $R_p$ ) equal to  $150 \text{ Sm}^3/\text{Sm}^3$ . What is the maximum oil production (in standard conditions, in  $\text{Sm}^3/\text{d}$ ) that can be processed by the horizontal separator.

$$q_0 = ?$$

$$q_g = ?$$

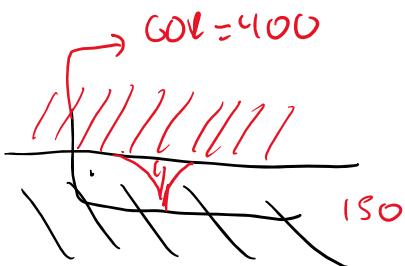
① the field operates at maximum oil rate ( $6805 \text{ Sm}^3/\text{d}$ )

$$q_{\bar{g}_{\text{plateau}}} = 150 \cdot 6805 = 1.020750 \cdot 10^6 \text{ Sm}^3/\text{d} < 2.8E6 \text{ Sm}^3/\text{d}$$

② the field operates at maximum gas rate ( $2.8E6 \text{ Sm}^3/\text{d}$ )

$$q_{\bar{o}_{\text{plateau}}} = \frac{2.8E6}{150} = 18666 \text{ Sm}^3/\text{d}$$

**Task 4 (5 points).** The value of producing gas-oil ratio used in Task 3 was calculated using a reservoir model assuming that vertical permeability is low and there is no coning from the gas cap. There is high uncertainty in this assumption. If a higher value of vertical permeability is used, the producing gas-oil ratio reaches 400 Sm<sup>3</sup>/Sm<sup>3</sup> during the plateau period. For this situation, estimate what is the maximum oil production (in standard conditions, in Sm<sup>3</sup>/d) that can be processed by the horizontal separator.



① Case ①  $q_{\text{g,plateau}} = 6805 \text{ Sm}^3/\text{d}$  (at capacity)

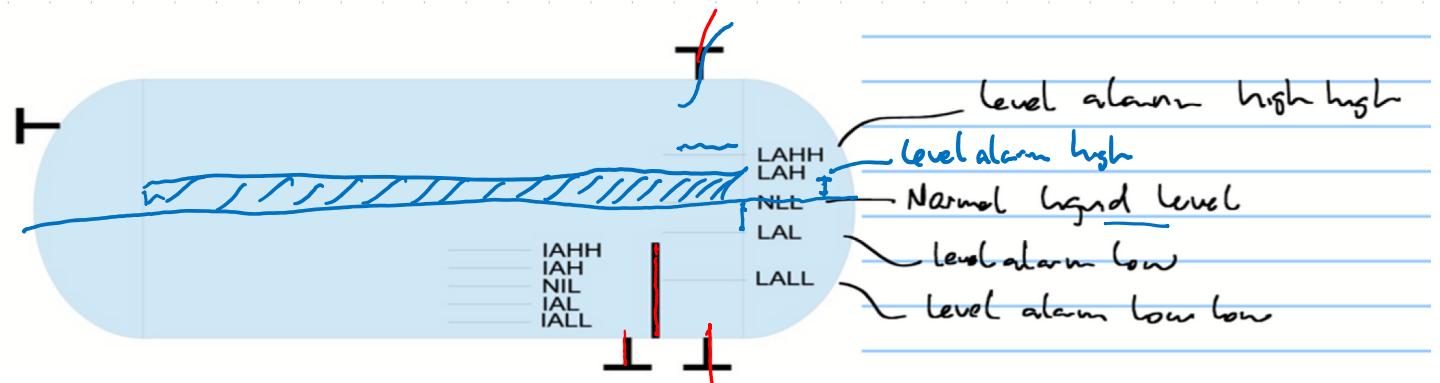
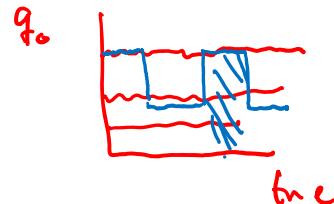
$$q_{\text{g,plateau}} = 400 \cdot 6805 = 2722000 \text{ Sm}^3/\text{d} < 2.8 \times 10^6$$

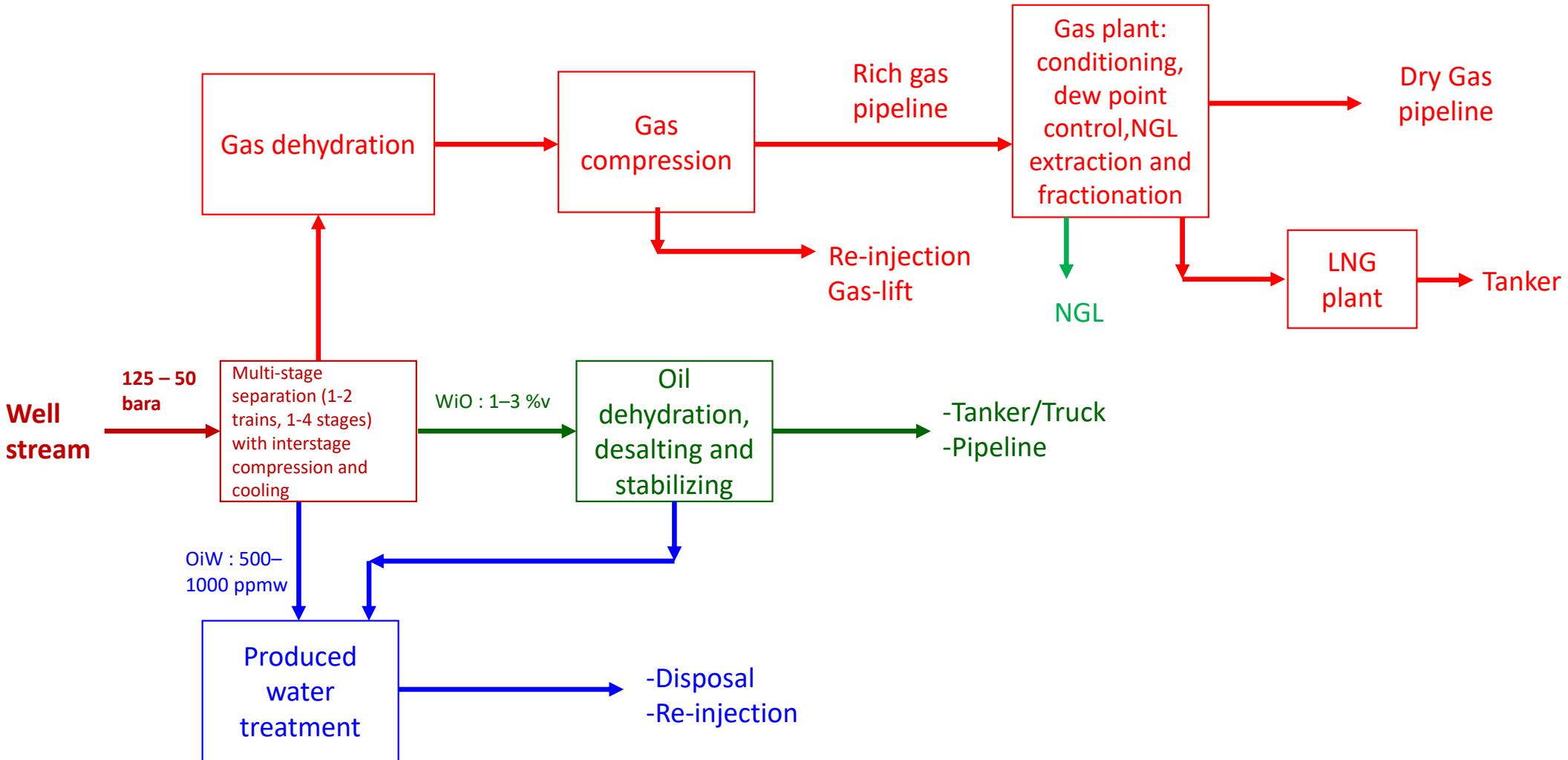
② Case ②  $q_{\text{g,plateau}} = 2.8 \times 10^6 \text{ Sm}^3/\text{d}$  (at capacity)

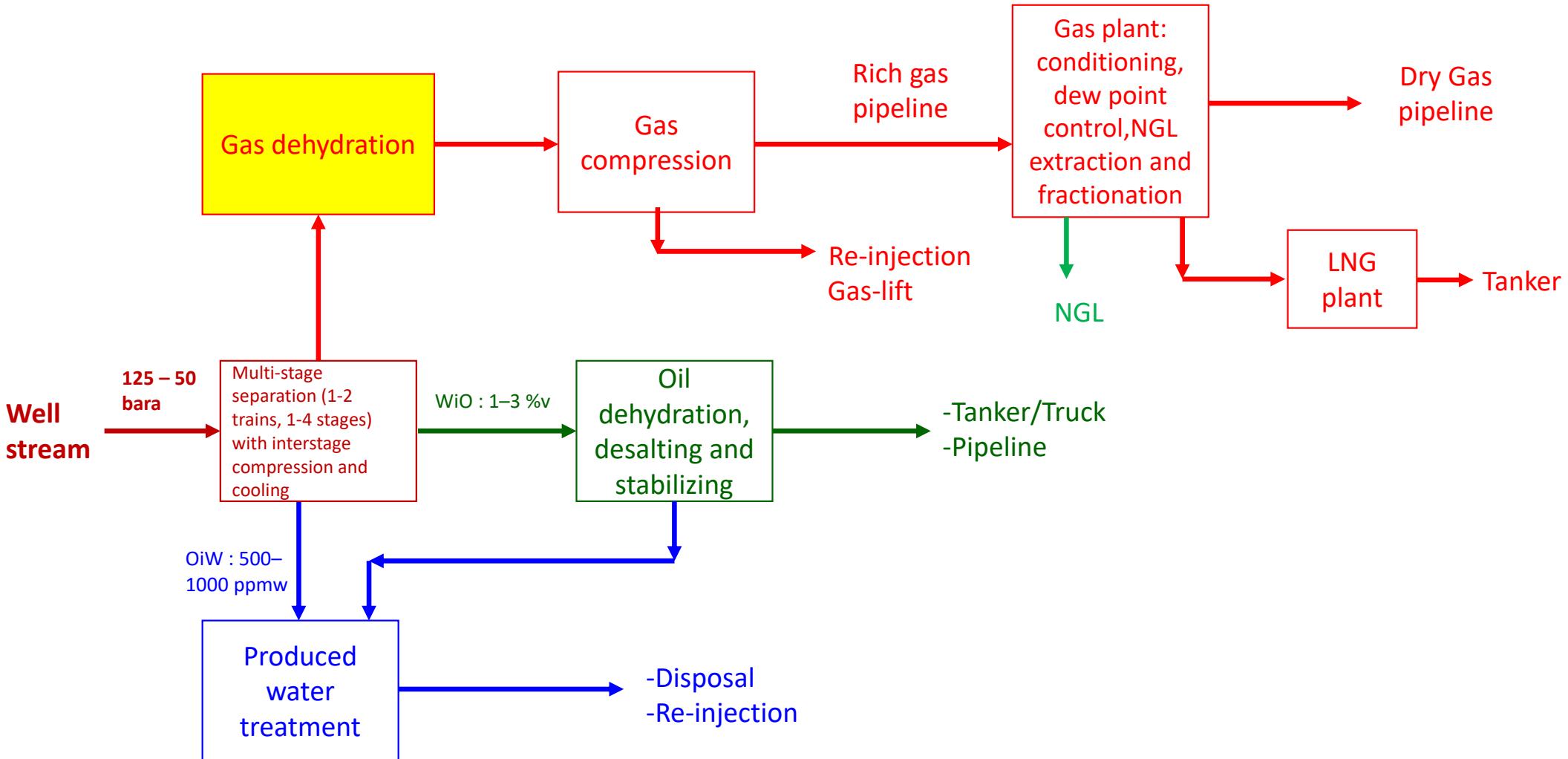
$$q_{\text{o,plateau}} = \frac{2.8 \times 10^6}{400} = 7000 \text{ Sm}^3/\text{d}$$

# Other design considerations

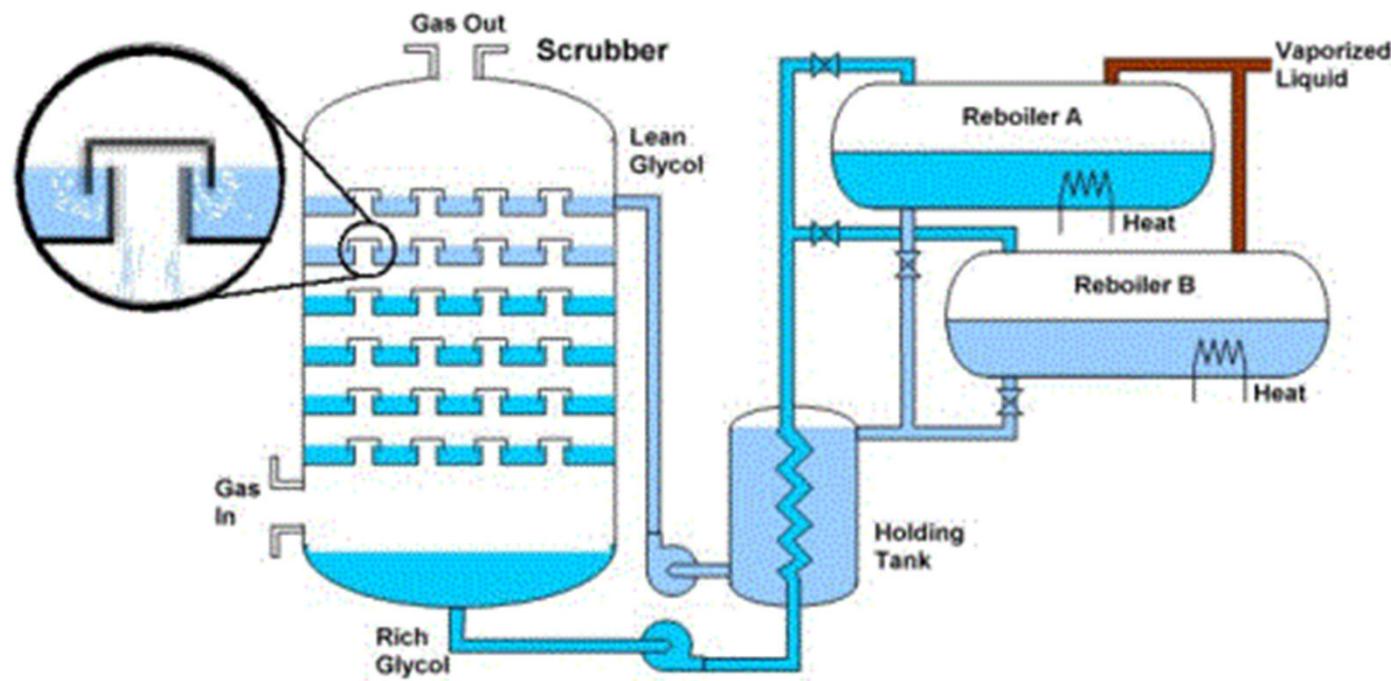
- 3 phases (gas, oil and water)
- Internals
- Inlet and outlet section
- Structural design
- Additional space for transient flow (slugs)
- ++







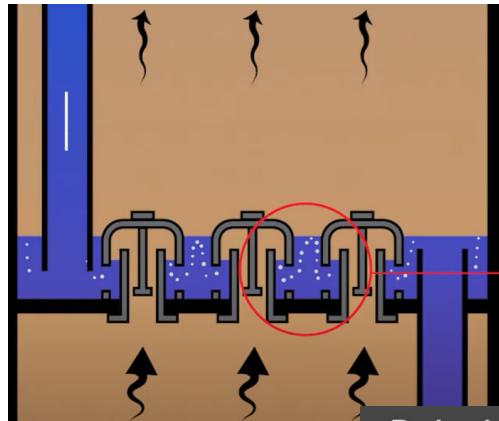
# TEG dehydration



# Youtube links for TEG dehydration

- Inside a gas dehydration tower: <https://www.youtube.com/watch?v=f7q8gWf8fg>
- Gas dehydration unit: <https://www.youtube.com/watch?v=kTtiqTeTZ0I>



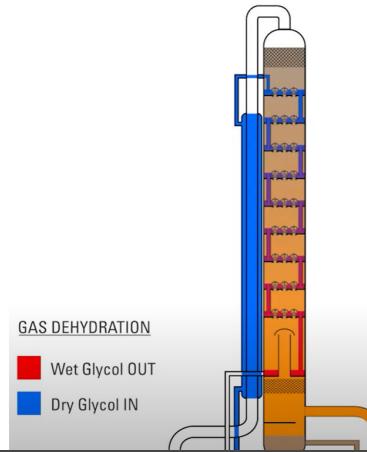


## Dehydration Unit Sizes

Dehydration units vary in size depending on **gas flow**.

In a unit this size, flow rates can be **a few million cubic feet per day (MMCFD)**.

Play 46



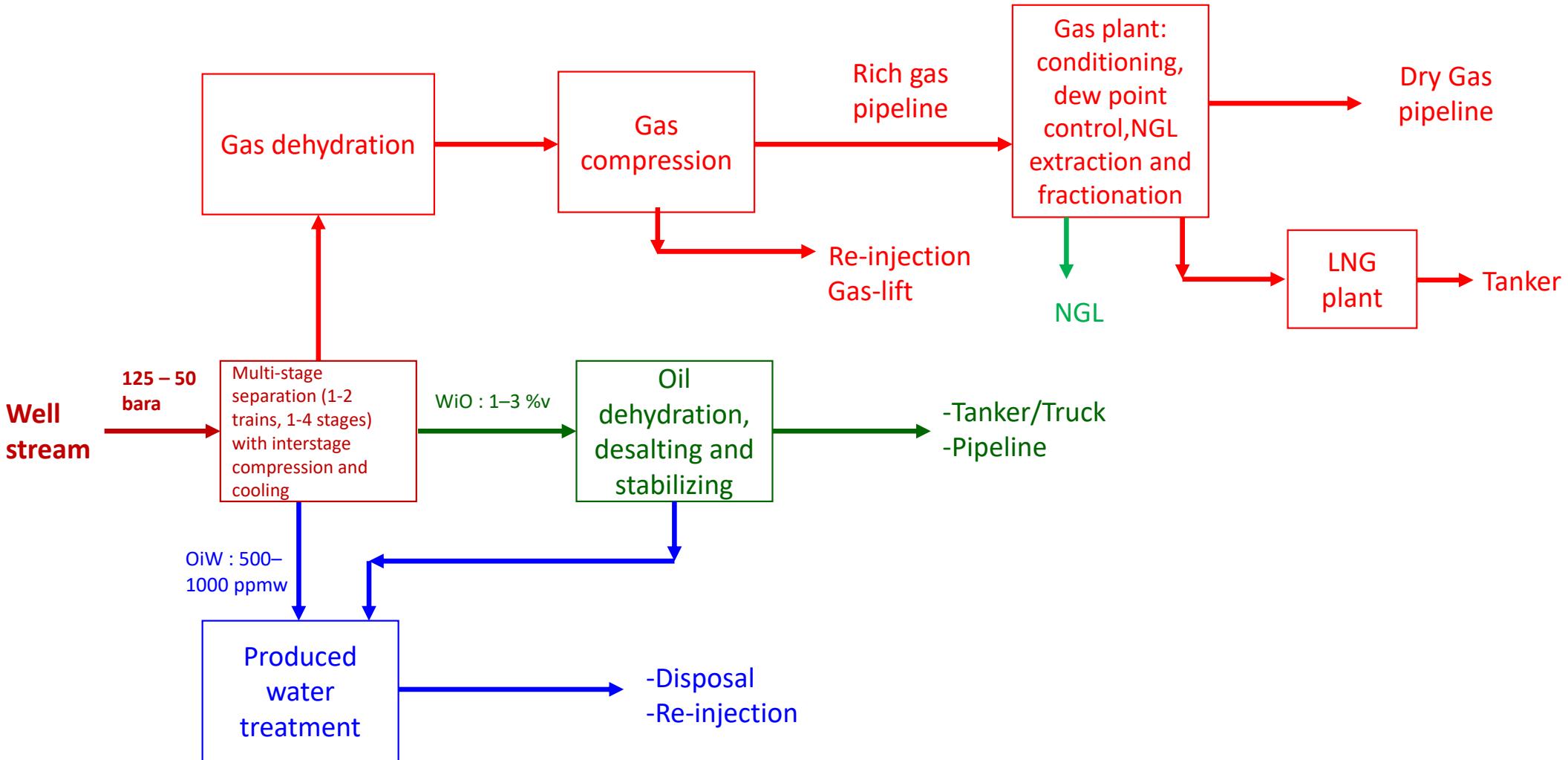
1. Glycol moves through **contactor tower**, absorbing the moisture from the natural gas becoming **WET GLYCOL**.

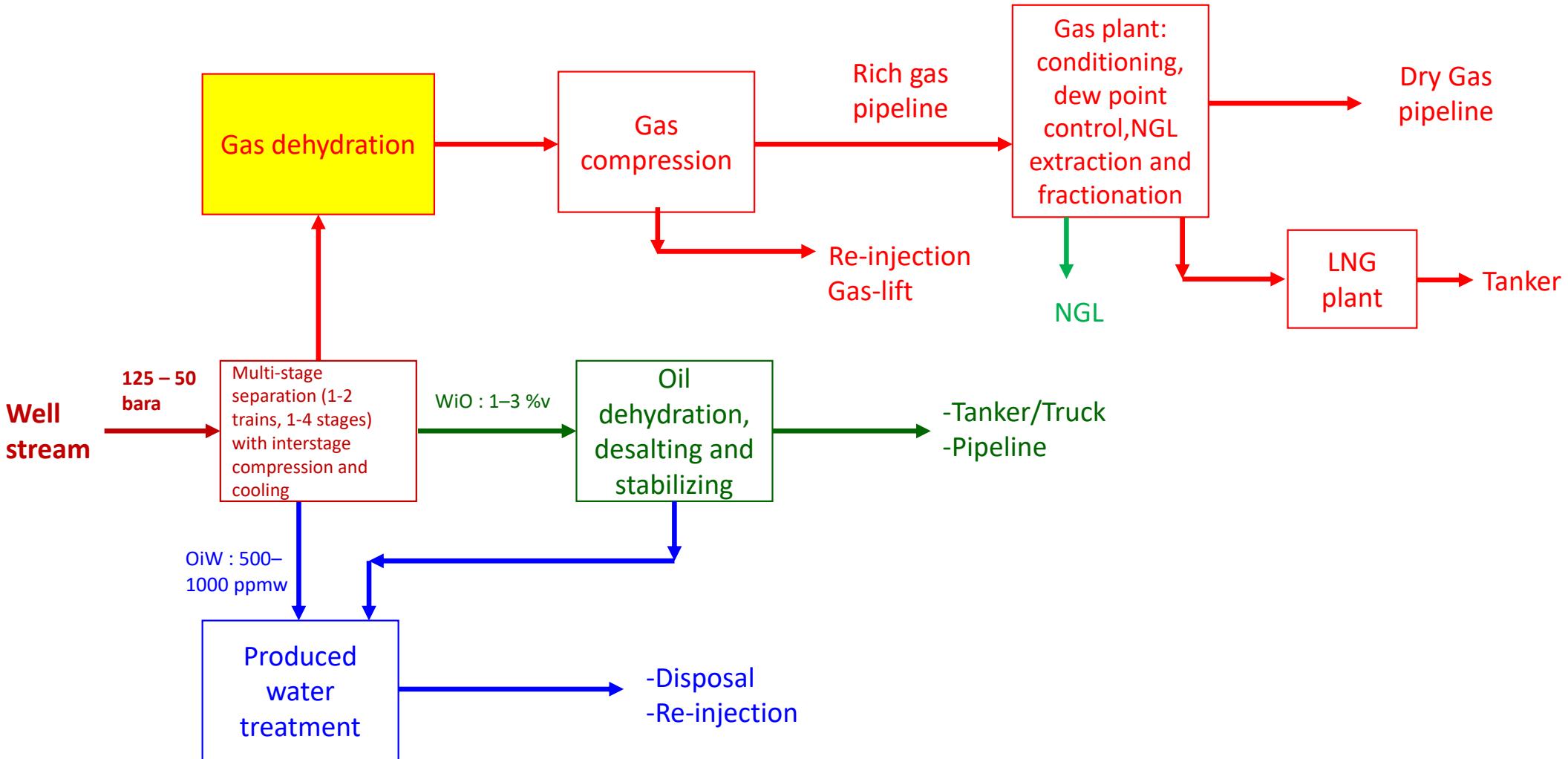
**Wet Glycol = "Rich" Glycol**  
Glycol entrained with water



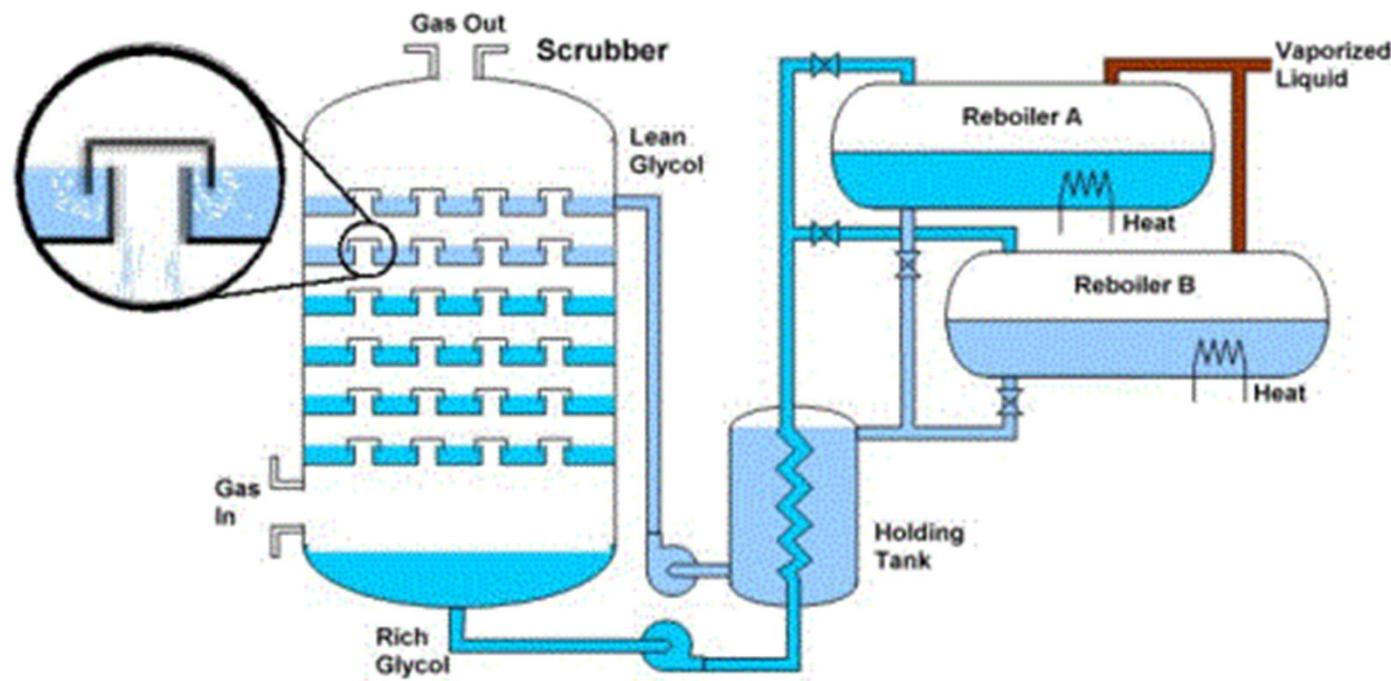
# **Class 20240208 - OUTLINE**

- Other topside processing equipment
- Intro – Production scheduling for the Snowwhite field





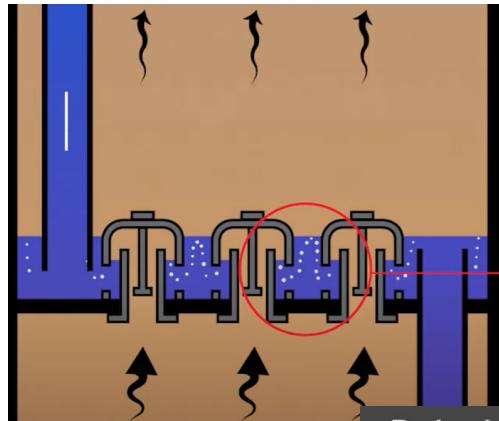
# TEG dehydration



# Youtube links for TEG dehydration

- Inside a gas dehydration tower: <https://www.youtube.com/watch?v=f7q8gWf8fg>
- Gas dehydration unit: <https://www.youtube.com/watch?v=kTtiqTeTZ0I>



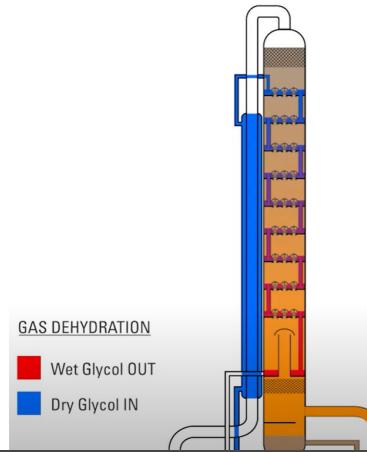


## Dehydration Unit Sizes

Dehydration units vary in size depending on **gas flow**.

In a unit this size, flow rates can be **a few million cubic feet per day (MMCFD)**.

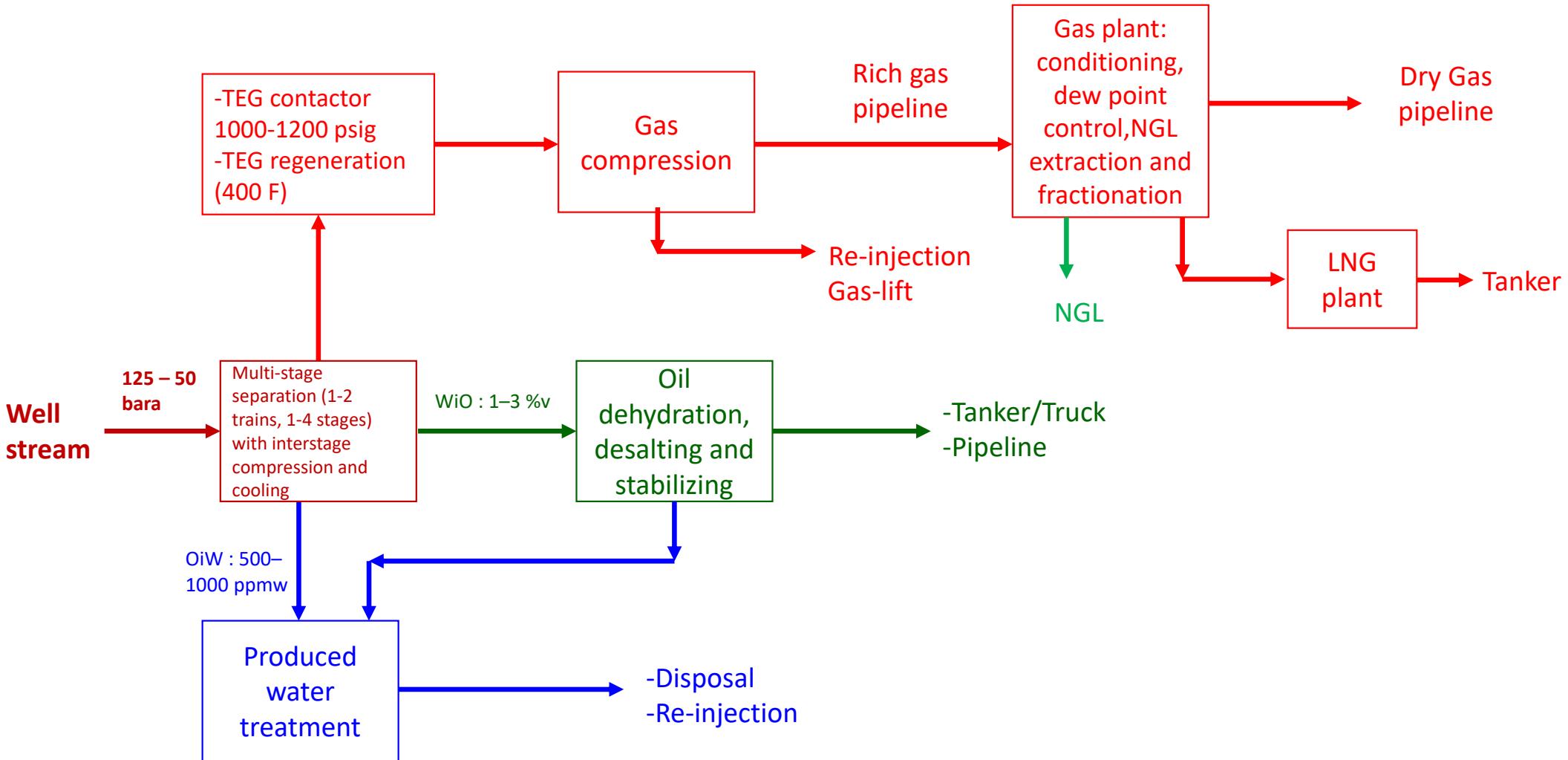
Play 46

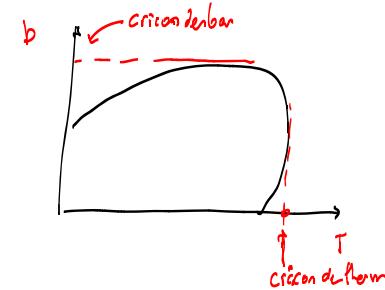
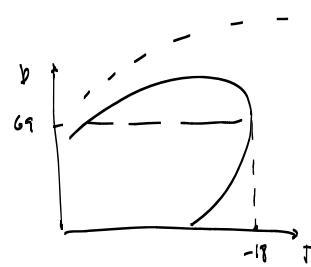
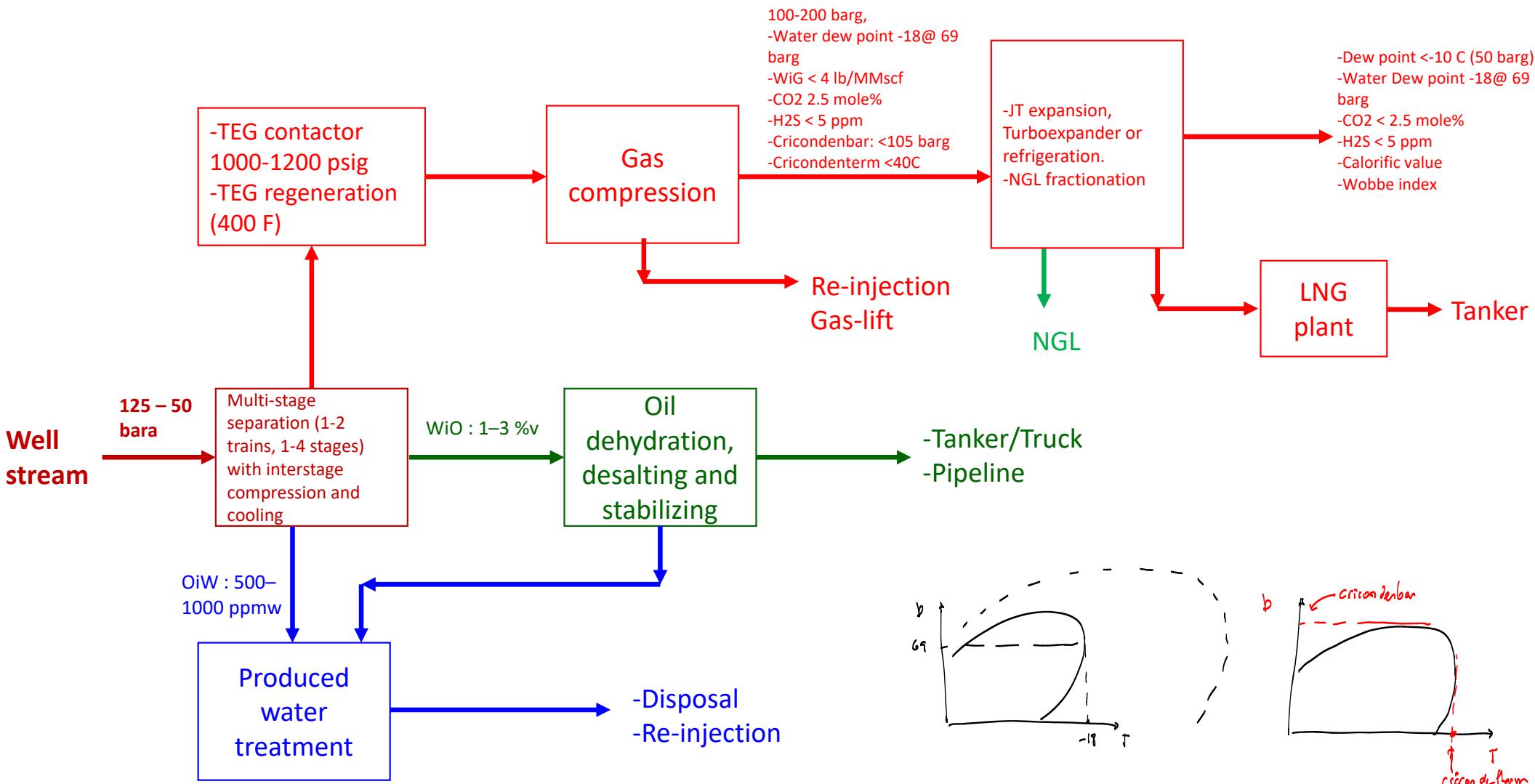


1. Glycol moves through **contactor tower**, absorbing the moisture from the natural gas becoming **WET GLYCOL**.

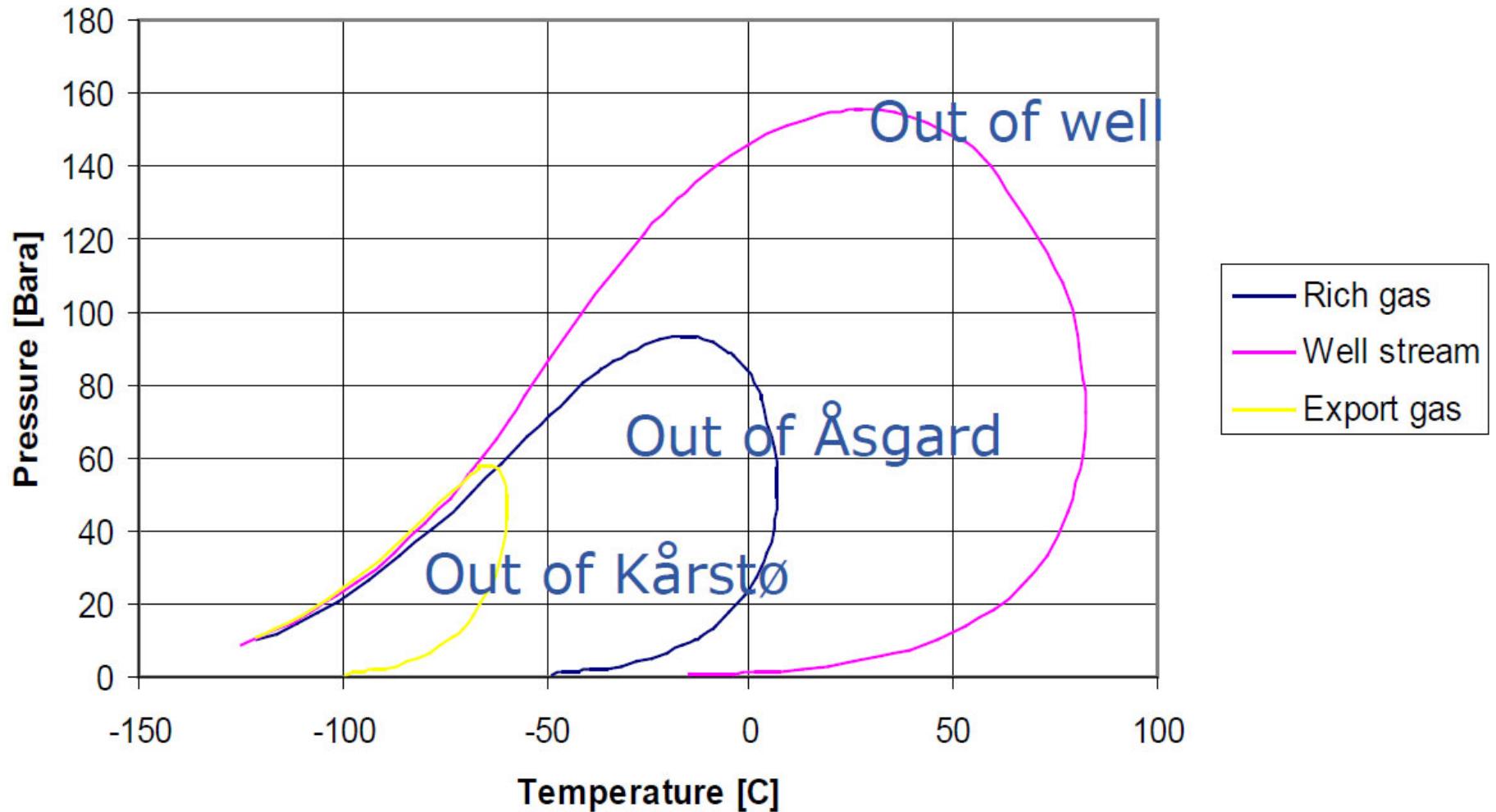
**Wet Glycol = "Rich" Glycol**  
Glycol entrained with water

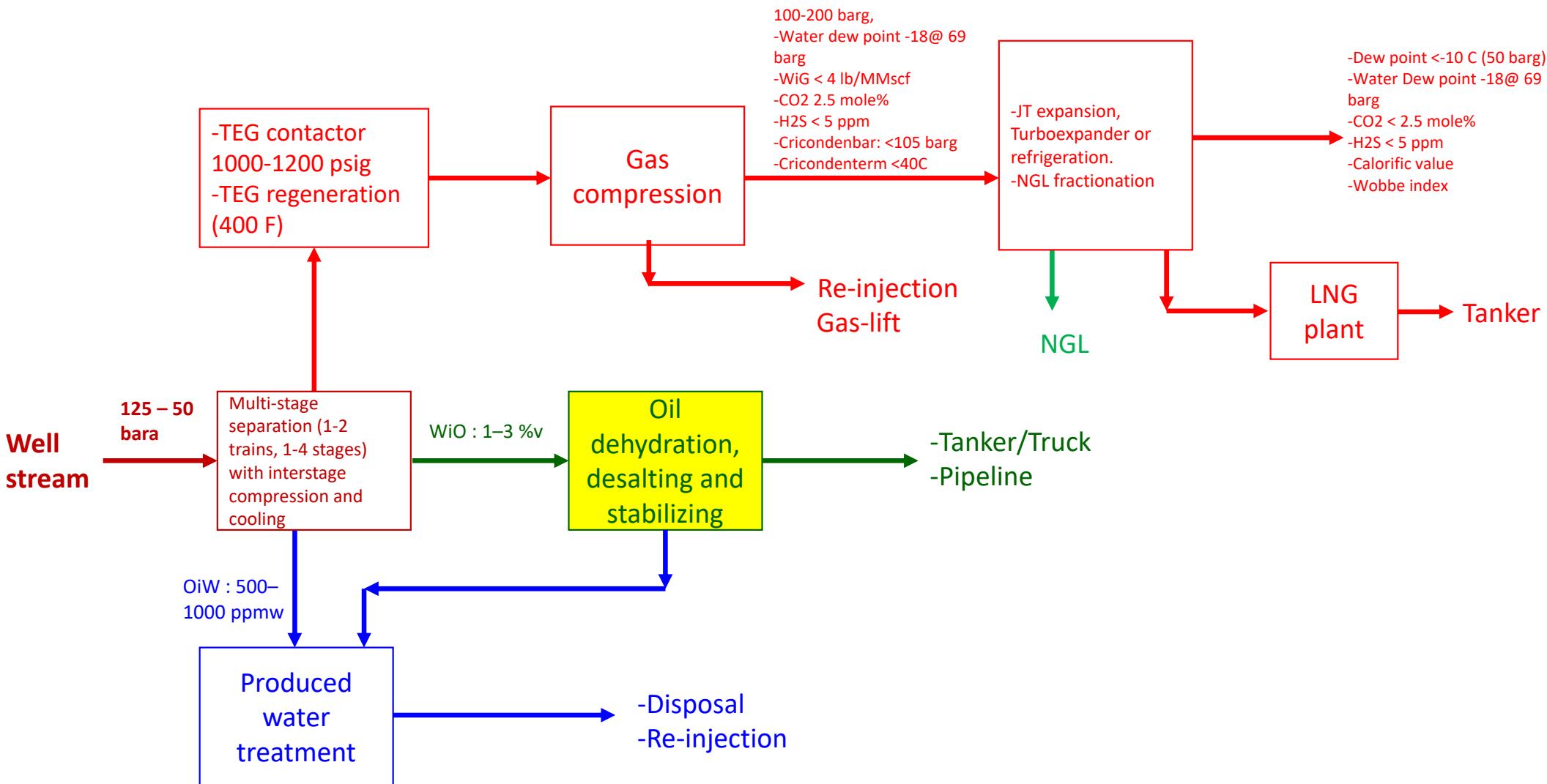




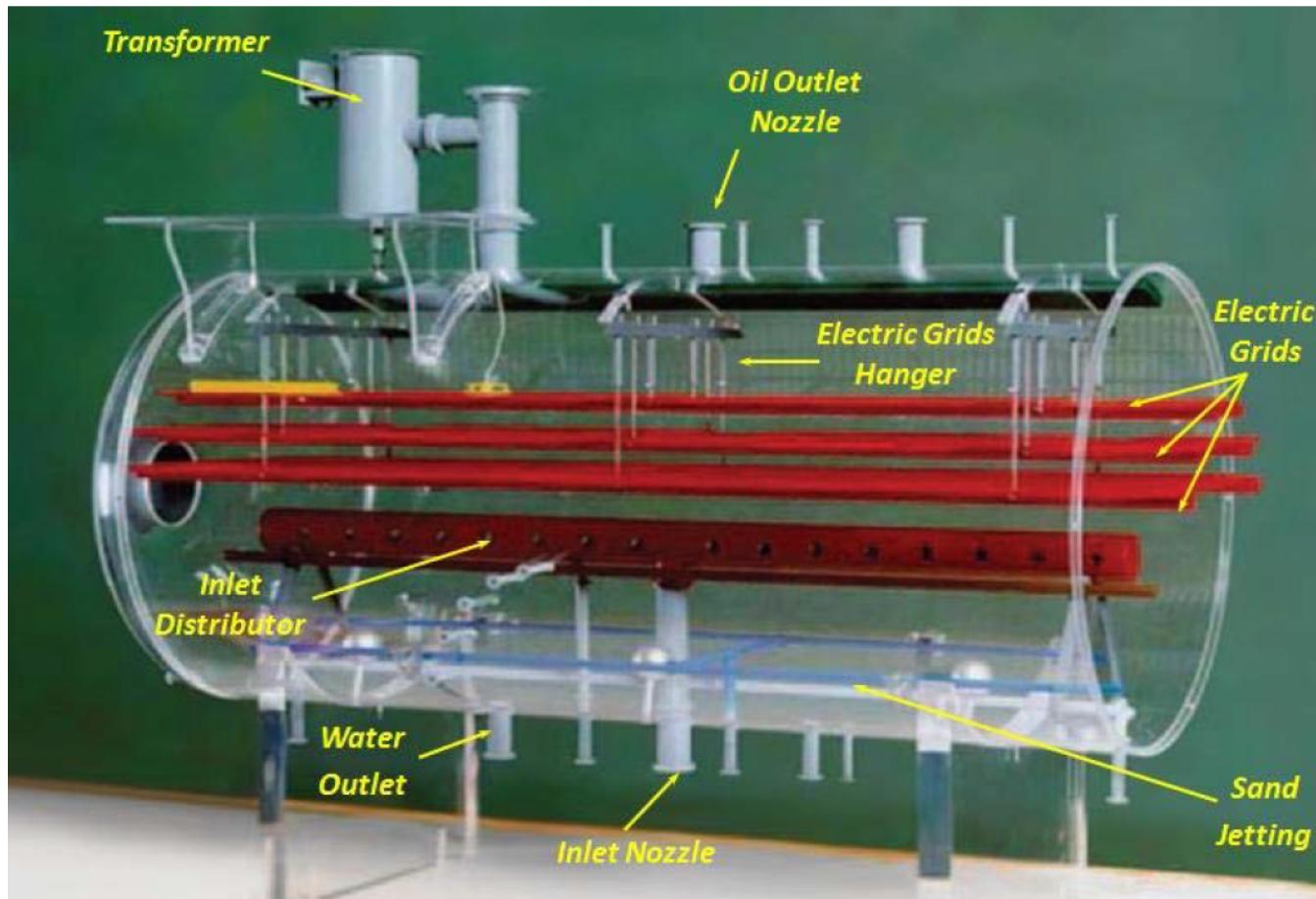


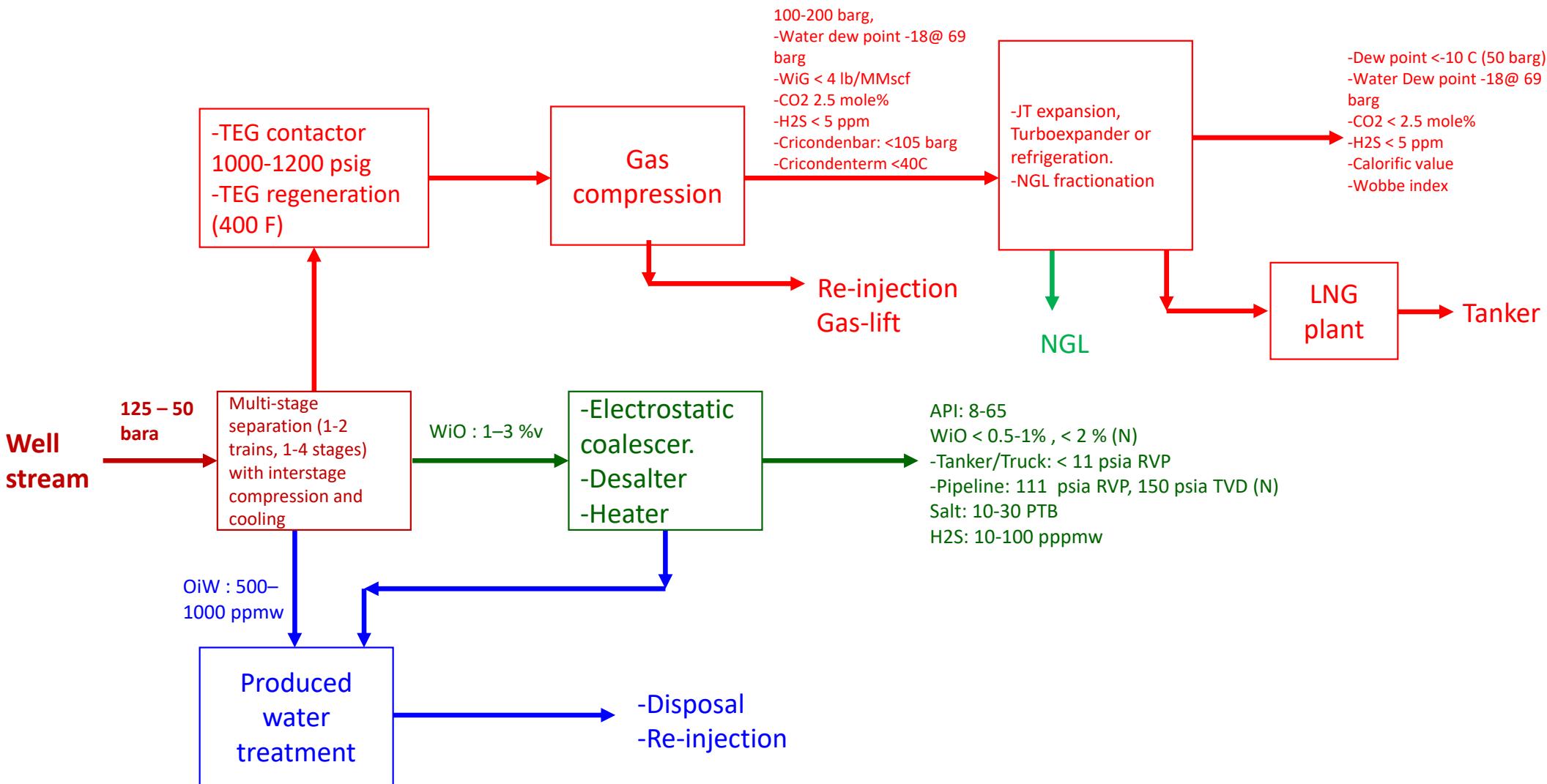
## Hydrocarbon phase behaviour





# Electrostatic coalescer





API: 8-65

Wi0 < 0.5-1%, < 2 % (N)

-Tanker/Truck: < 11 psia RVP

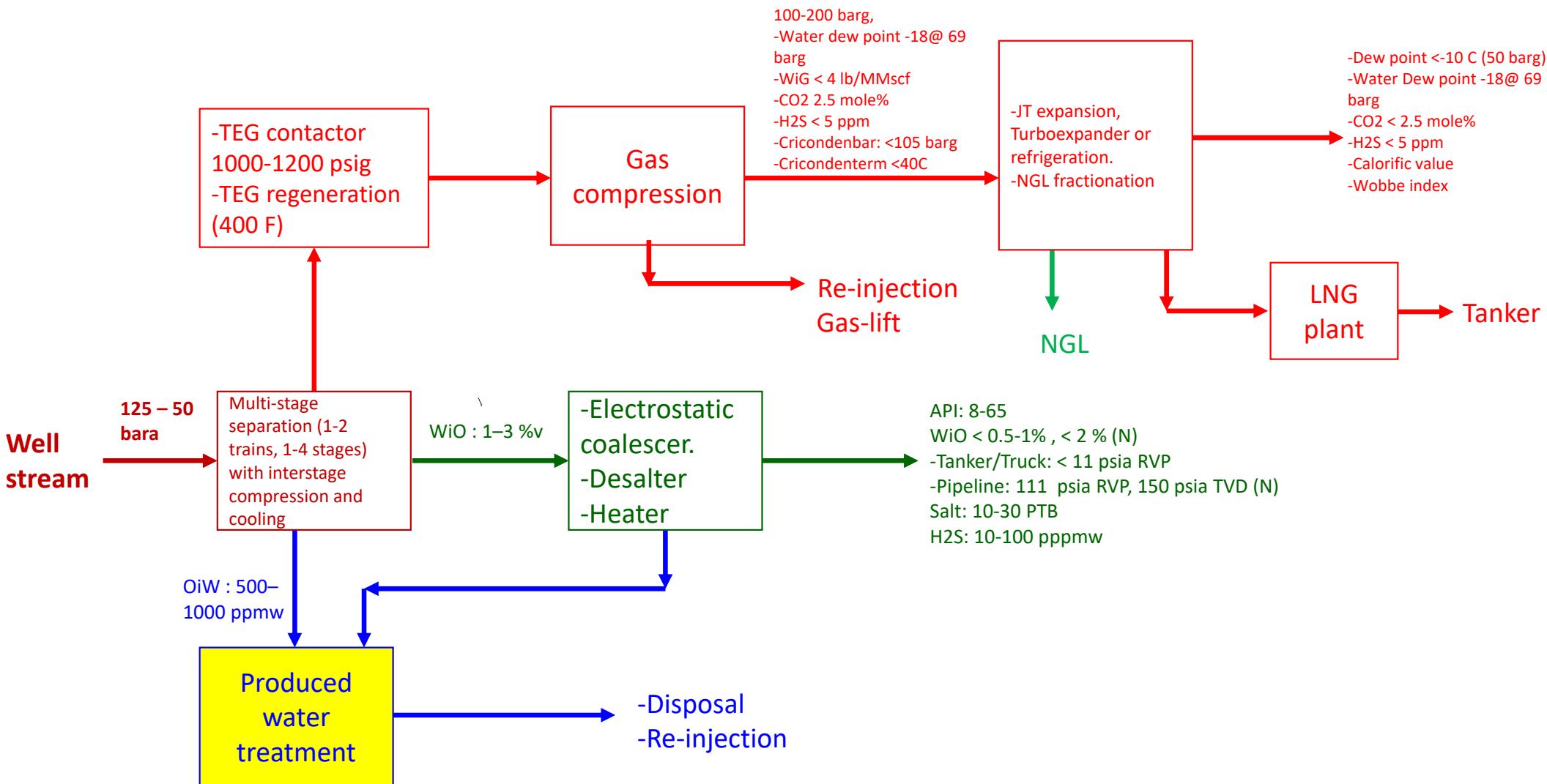
-Pipeline: 111 psia RVP, 150 psia TVD (N)

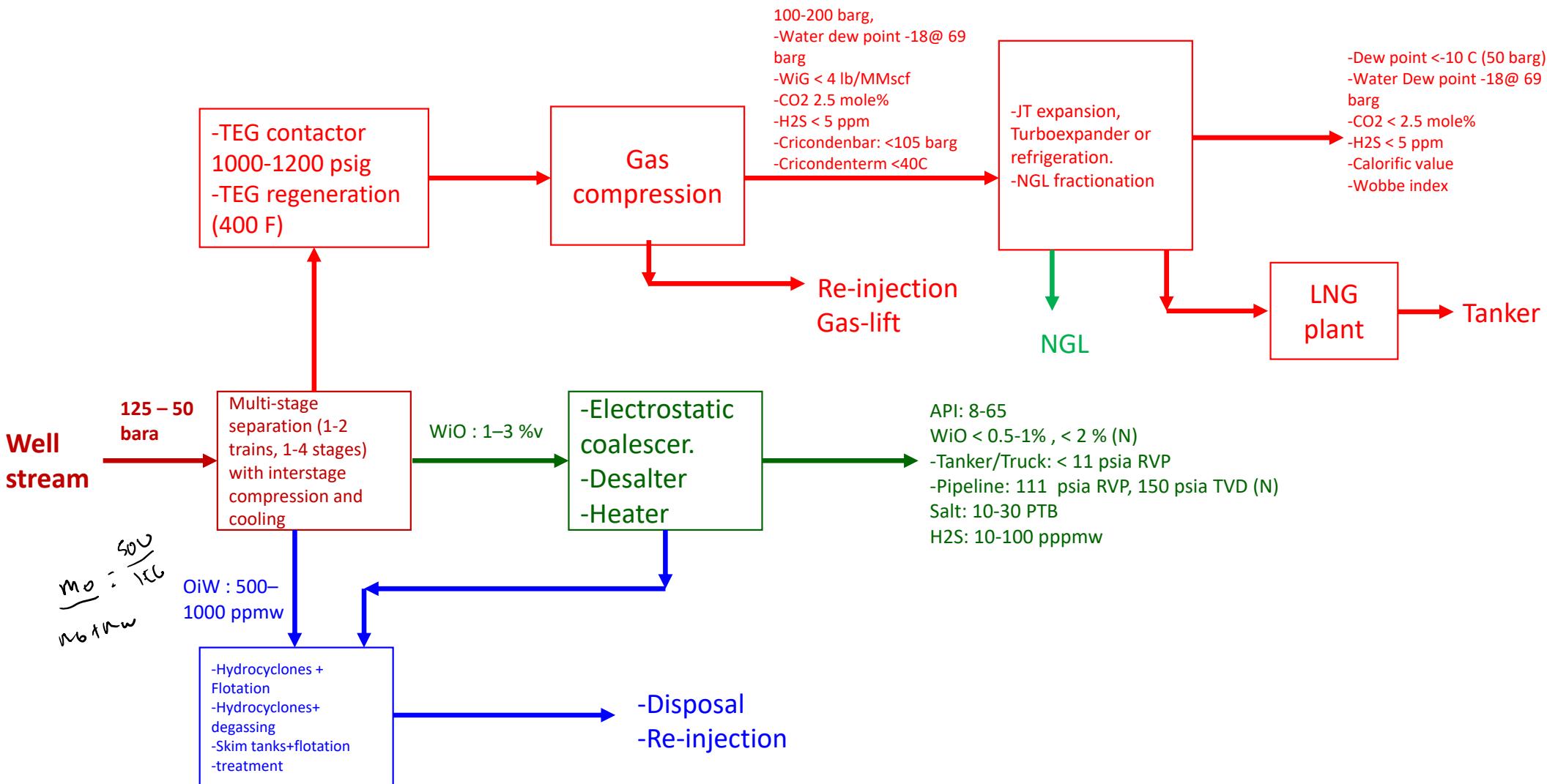
Salt: 10-30 PTB

H2S: 10-100 pppmw

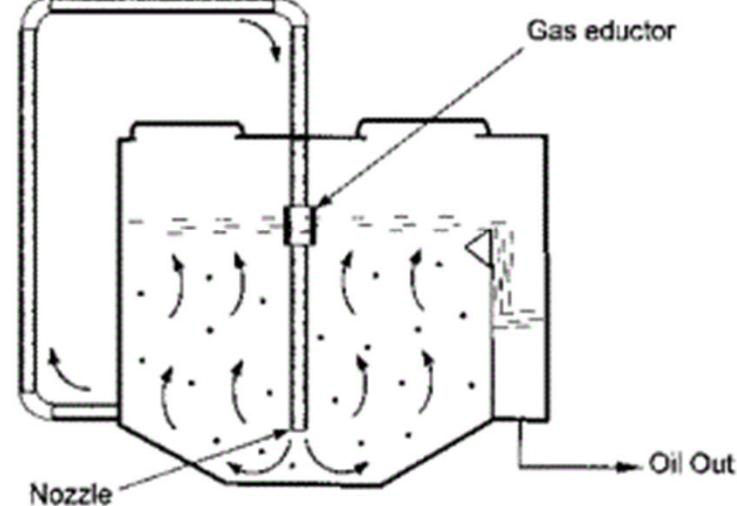
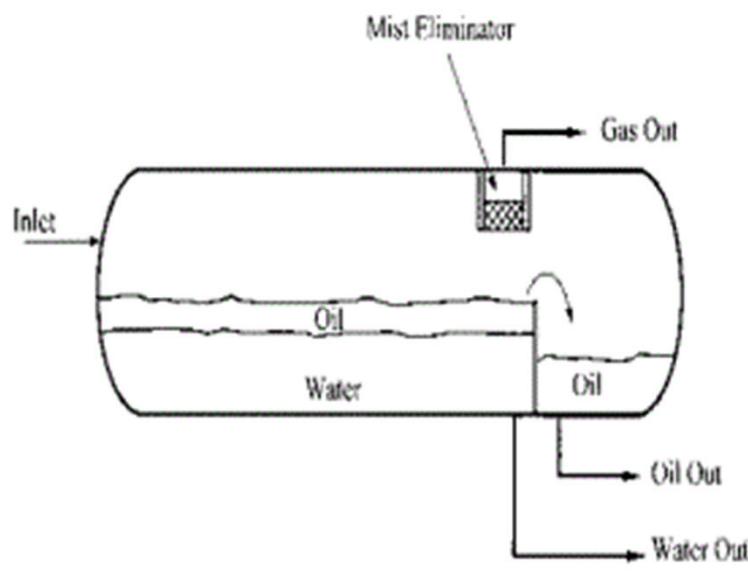
Main Reid vapor pressure  
True vapor pressure

pounds per thousand barrels

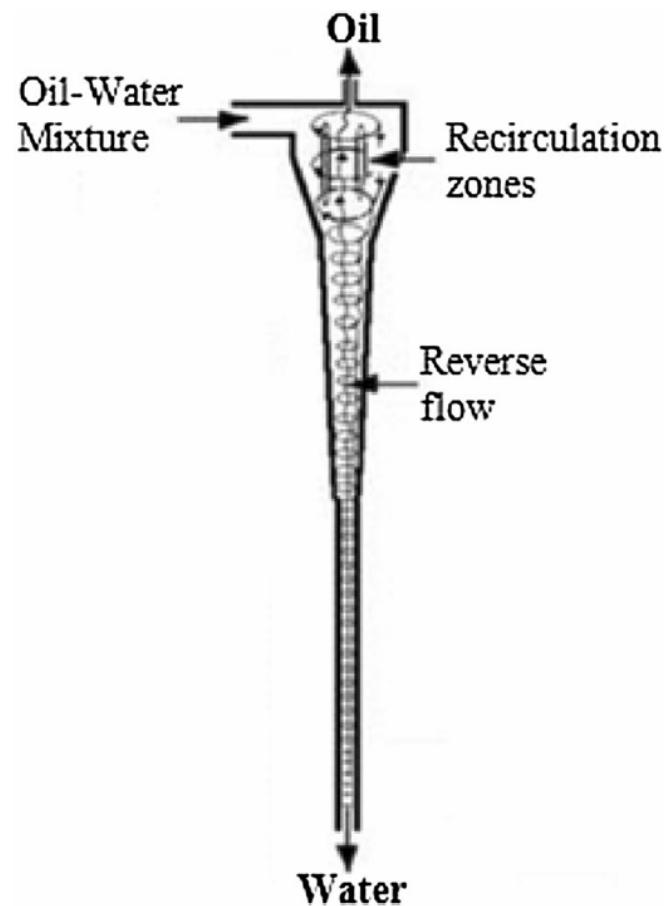


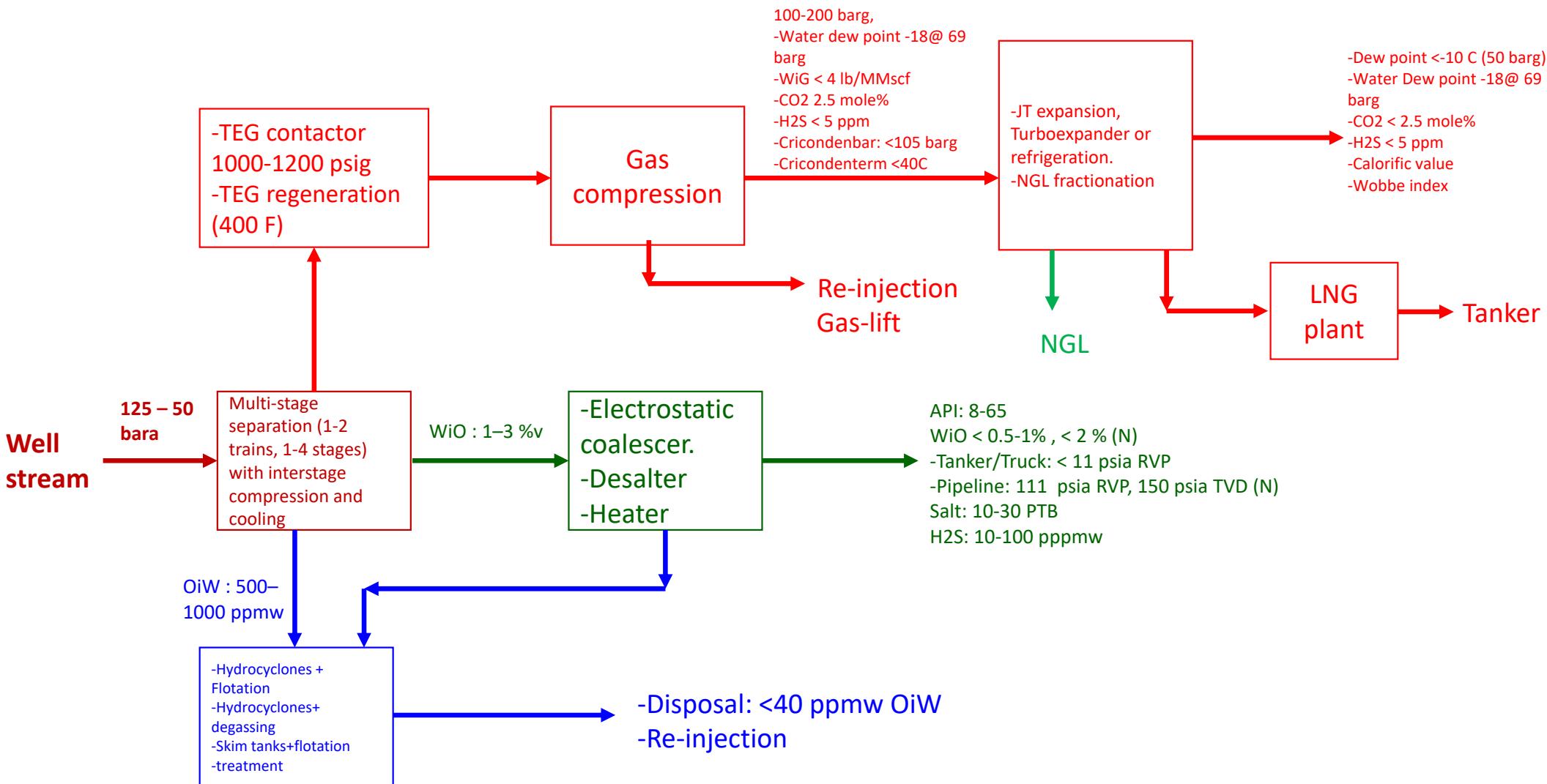


# Skim tank + flotation unit



# Hydrocyclone

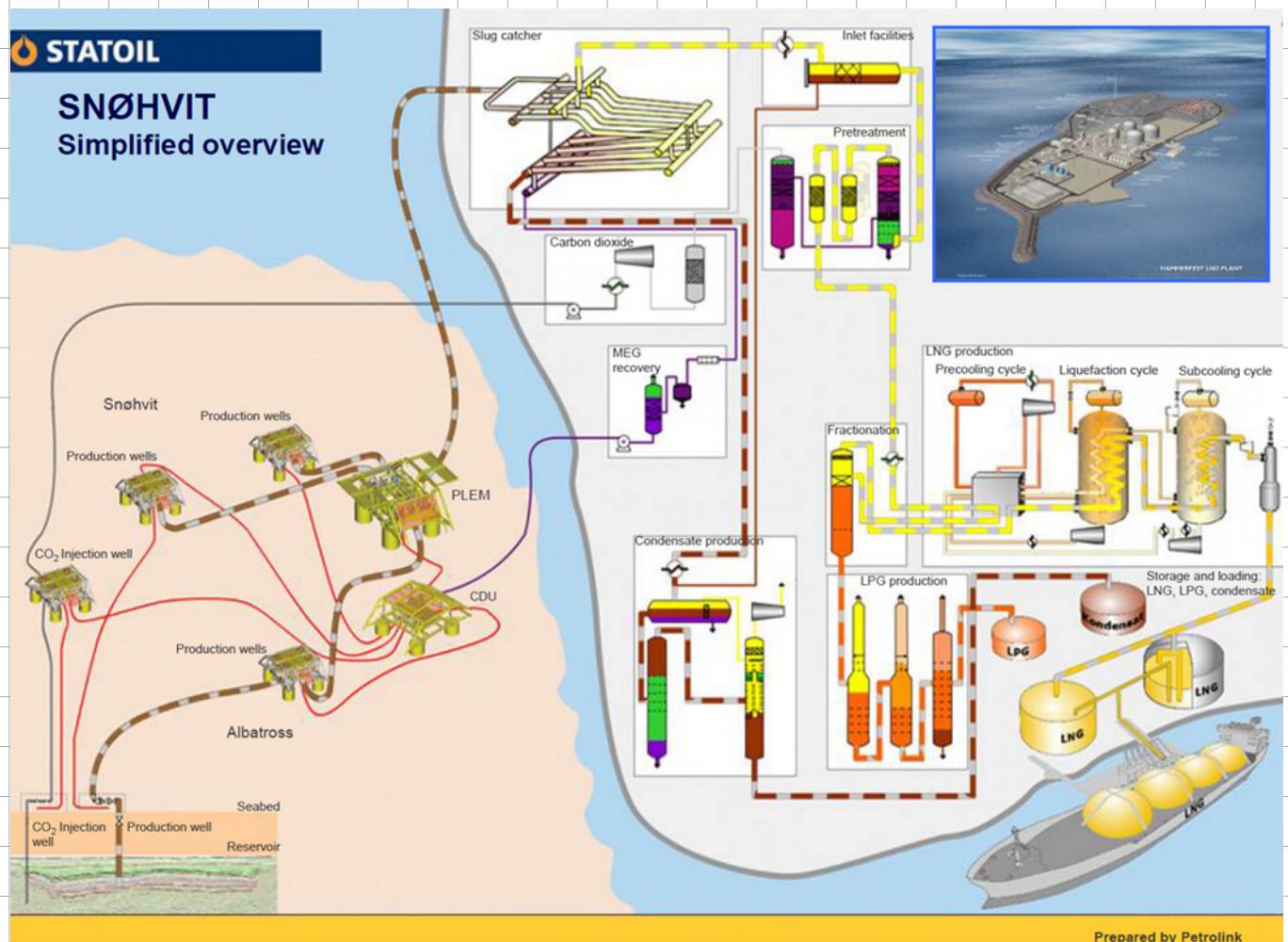
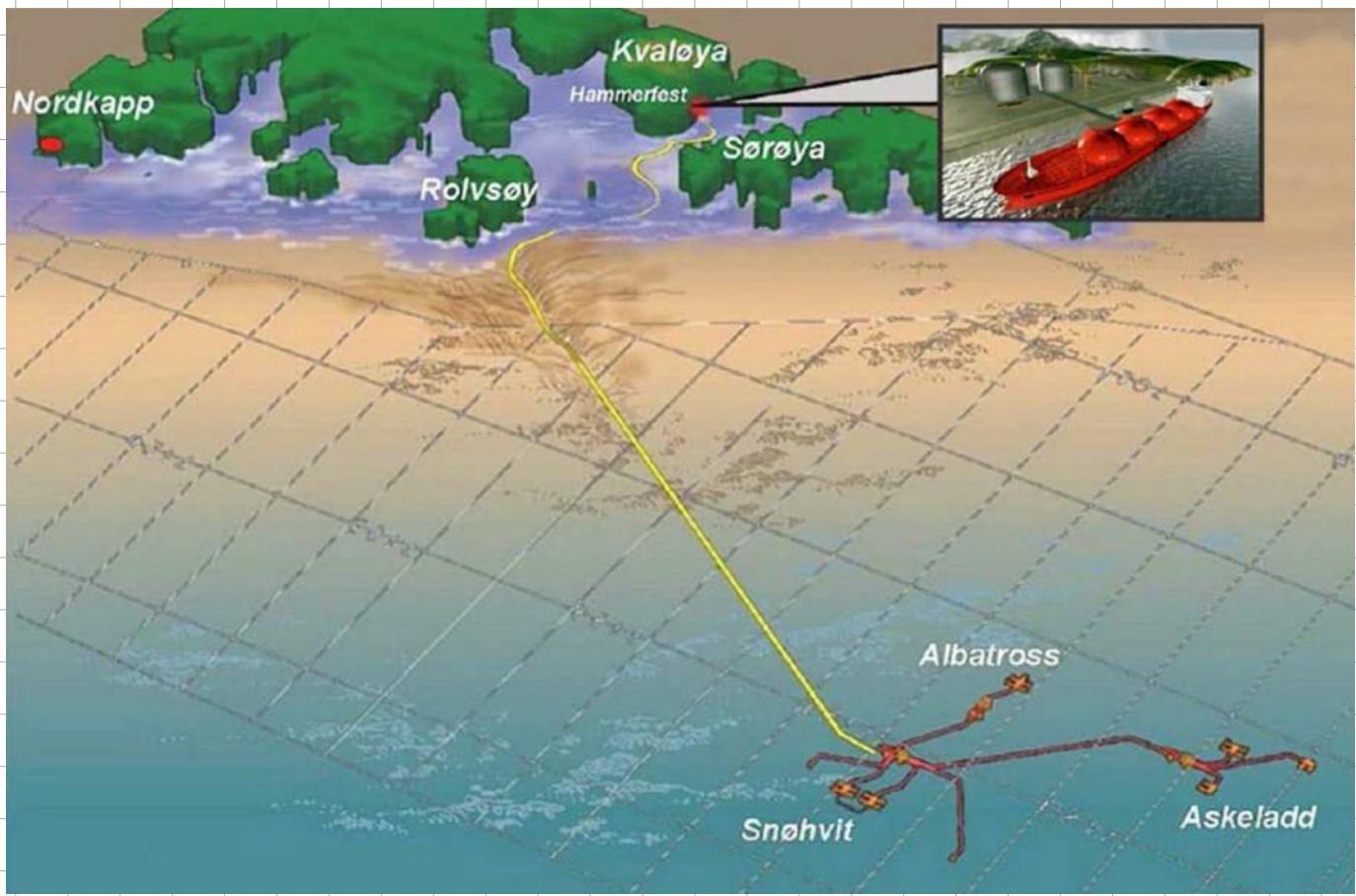




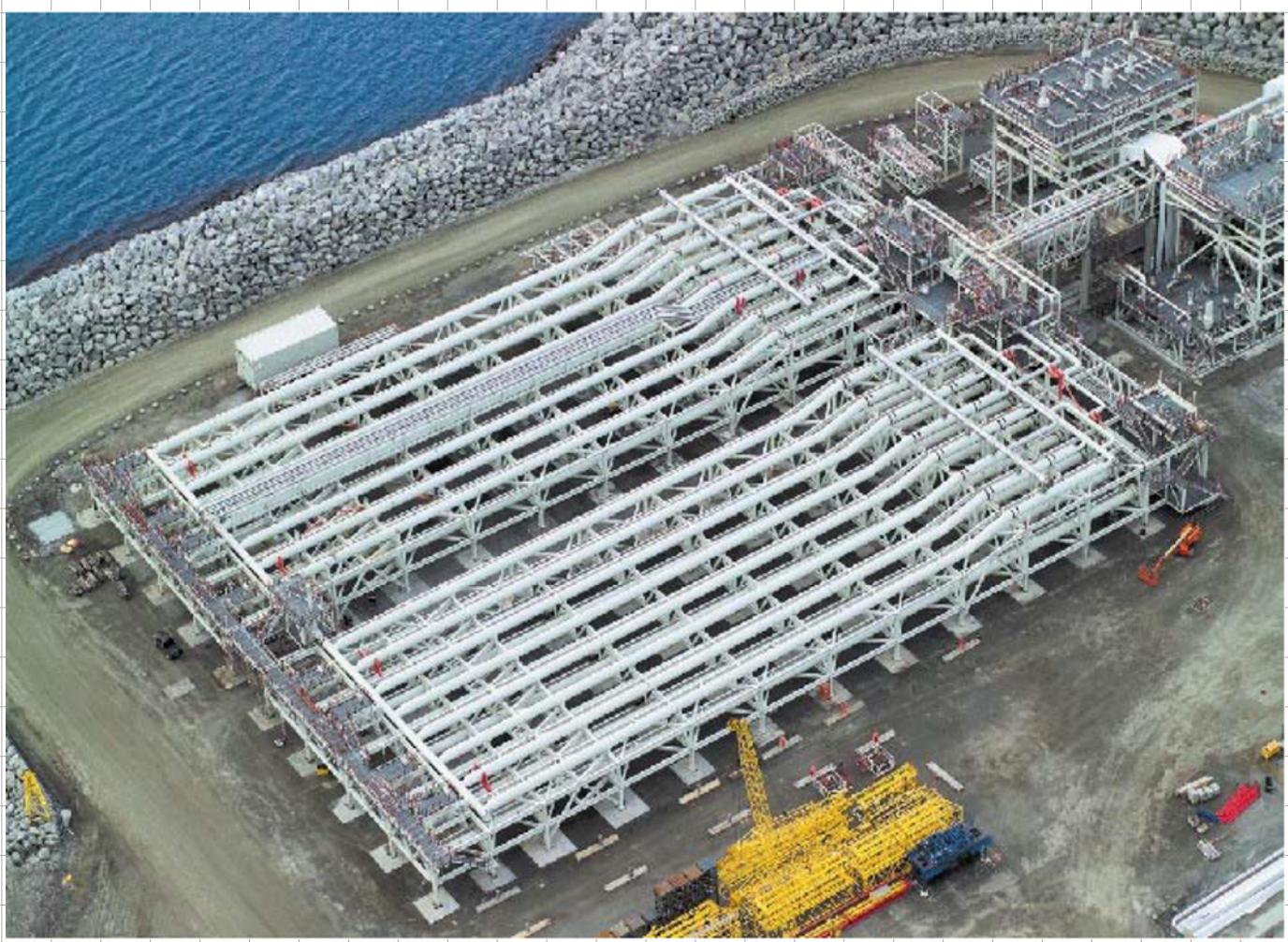
# Other links

Water knockout : <https://www.youtube.com/watch?v=wQ1A8w9Ouy4>

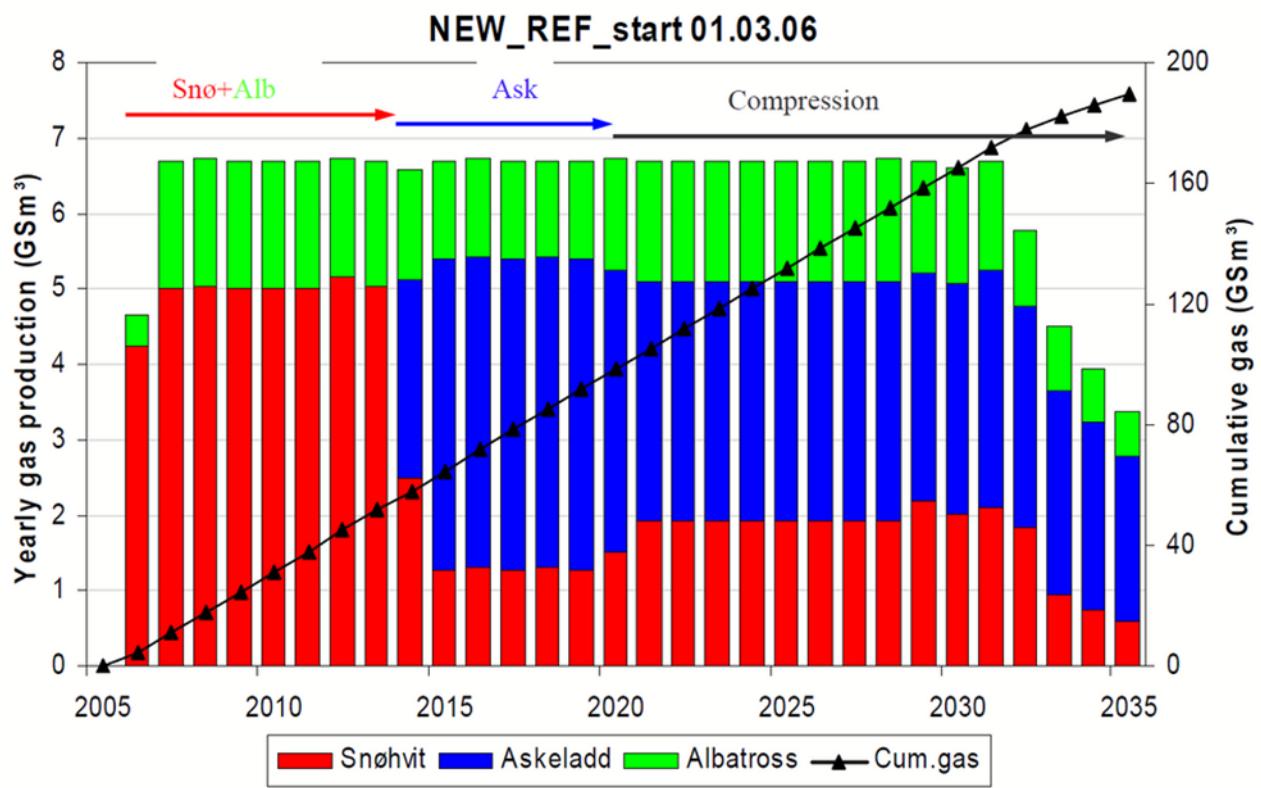
Walkthrough an oil and gas platform in the UK . <https://www.youtube.com/watch?v=UrWTMCgHr6s>



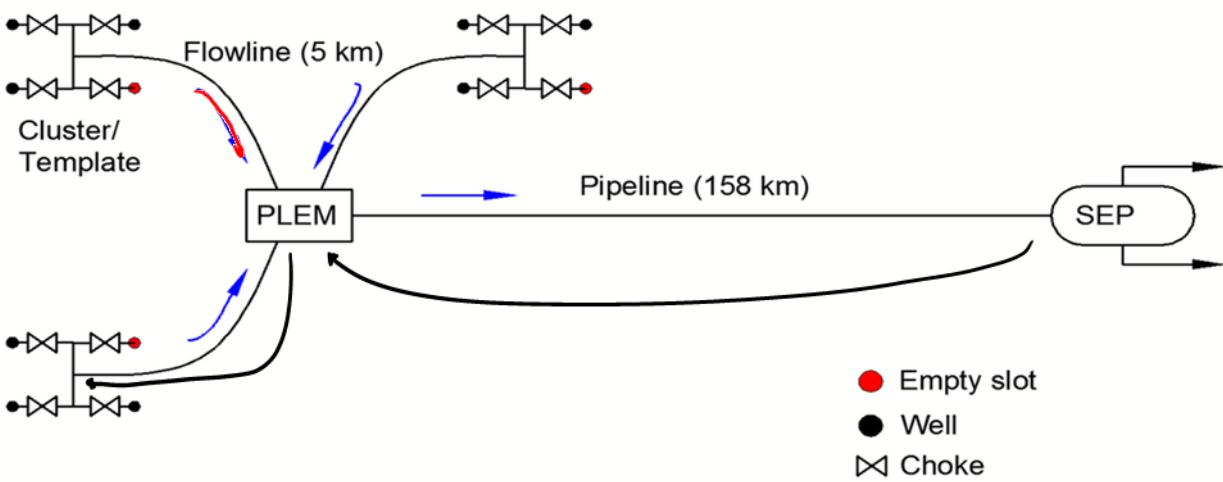
Slugcatcher: [https://www.youtube.com/watch?v=xY4WdJLai\\_0](https://www.youtube.com/watch?v=xY4WdJLai_0)



## Production profile (20,8 mill. Sm<sup>3</sup>/sd – 6,7 GSm<sup>3</sup>/år)



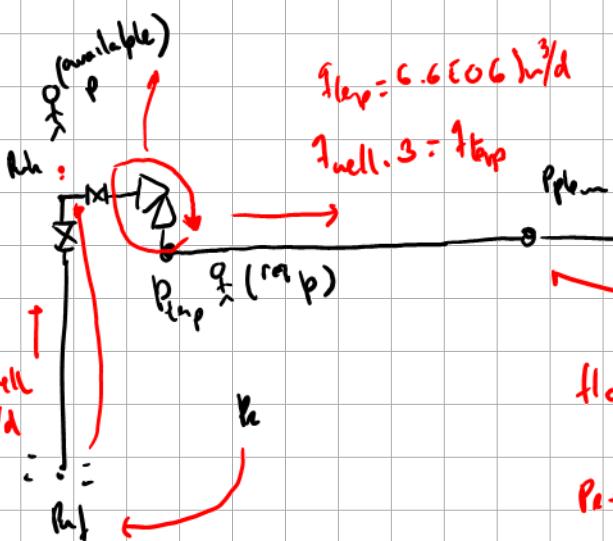
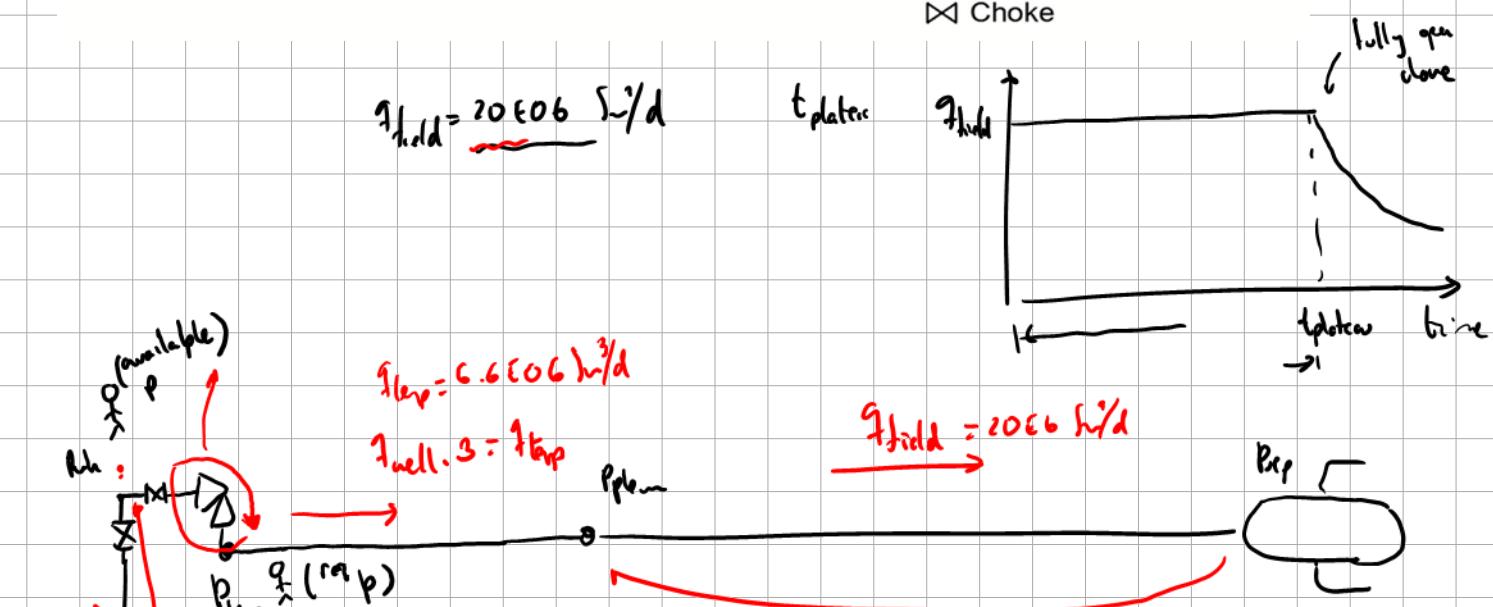
Goal: perform production scheduling calculations for the Snøhvit field, i.e. 1) determine plateau duration, 2) determine post-plateau production



$$q_{\text{field}} = 20 \times 0.6 \text{ Sm}^3/\text{d}$$

$t_{\text{plateau}}$

- Empty slot
- Well
- ▷ Choke



flow equilibrium (energy accounting)

$$P_t \rightarrow P_{wh} \rightarrow \text{TPR}$$

inflow performance relationship

$$P_{wh} \rightarrow P_{t, \text{pump}} \rightarrow \text{TPR}$$

tubing performance relationship

counter-current

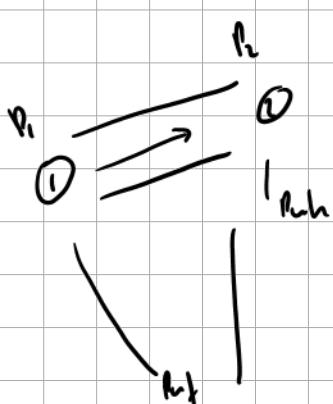
$$P_{t, \text{pump}} \rightarrow P_{t, \text{pump}} \rightarrow \text{Pipeline performance relationship}$$

$$q_{\text{well}} = C_R (P_t - P_{wh})^{n/2}$$

$$q_{\text{tubing}} = C_T \left( \frac{P_t}{P_{wh}} - 1 \right)^{0.5}$$

$$q_{\text{field}} = C_P (P_{t, \text{pump}}^2 - P_{wh}^2)^{0.5}$$

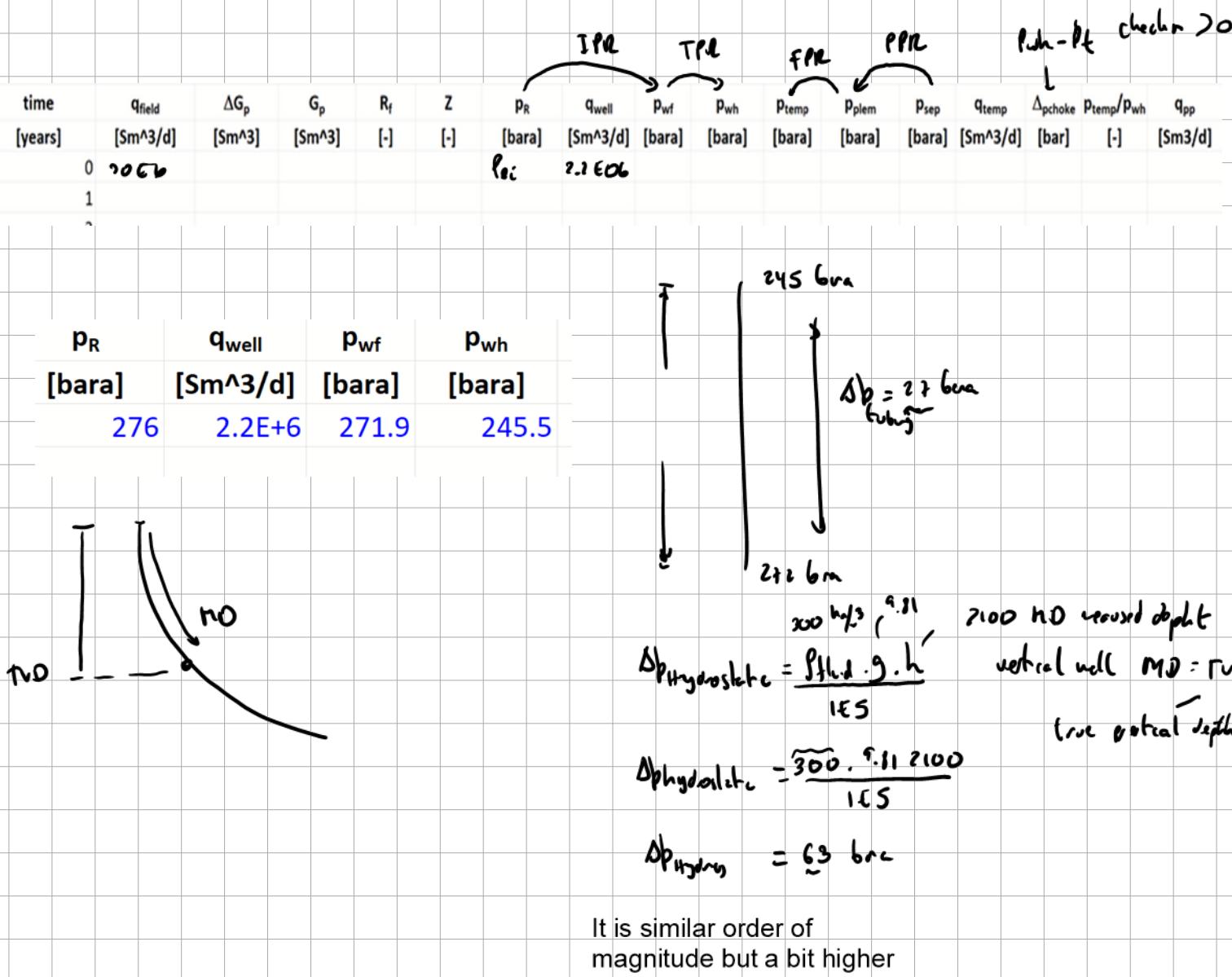
$$q_{\text{t, pump}} = C_{P_t} \left( \frac{P_t^2}{P_{t, \text{pump}}} - \frac{P_{wh}^2}{P_{t, \text{pump}}} \right)^{0.5}$$



$$\text{when } \Delta p_{\text{t, tube}} = 0 \quad P_{wh} = P_t$$

$$\Delta p_{\text{t, tube}} = P_{wh} - P_t > 0 \quad \text{Means 1) enough energy to deliver the flow}$$

2) there is not enough energy to deliver



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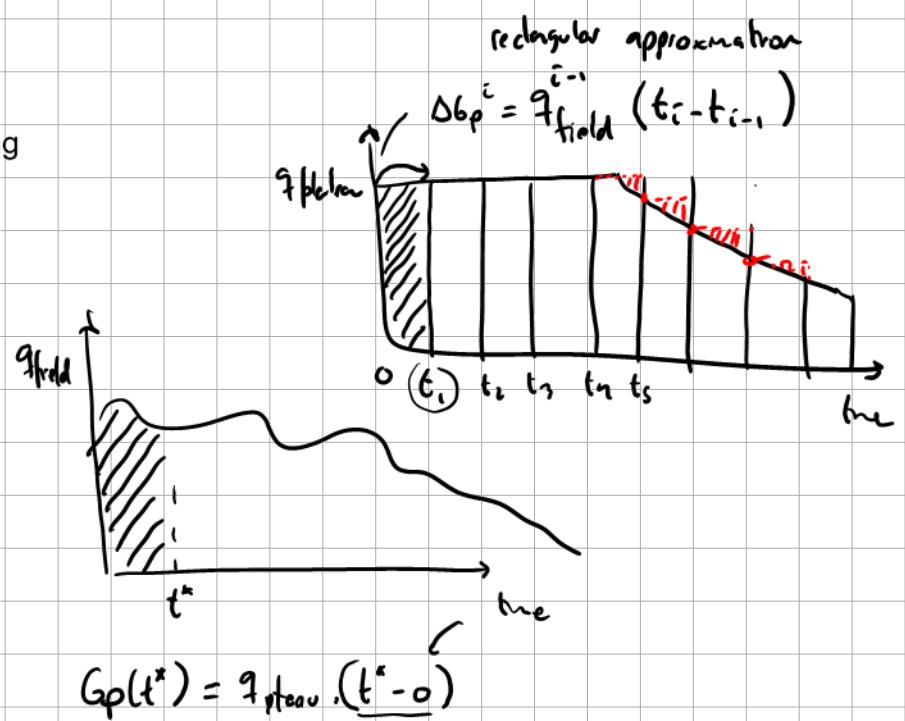
## Outline:

- (cont) Snowwhite production scheduling exercise

## Additional information:

- Outcome of ref group meeting nr 1
- Mandatory exercise nr. 2 published

$$G_p = \int_0^{t^*} q_{\text{field}} dt$$



## trapezoidal approximation

$$\Delta t_i^i = \frac{(q_{\text{field}}^{i-1} + q_{\text{field}}^i)(t^i - t^{i-1})}{2}$$

Excel value error for Pwh

$$q_{\text{fuel}} = C_r \left( \frac{P_w f}{e^j} - P_{wh}^2 \right)^{0.5}$$

$$P_{wh} = \sqrt{\frac{P_w f}{e^j} - \left( \frac{q_{\text{fuel}}}{C_r} \right)^2}$$

Check the video recording for the step-by-step solution!

Check the video recording for the step-by-step solution!

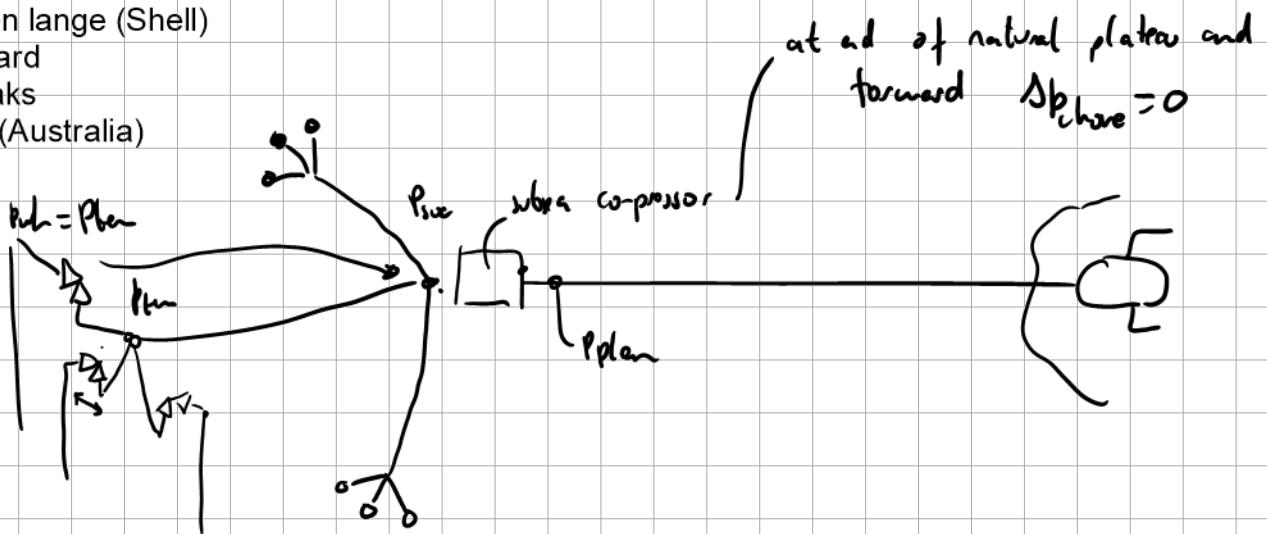
Boosting available energy < required energy provides energy to the fluid to bridge the gap!

-Ormen lange (Shell)

-Asgard

-Gullfaks

-Janz (Australia)



$$q_{temp} = C_{fl} \left( P_{tue} - P_{suc} \right)^{0.5}$$

$$P_{tue} = \sqrt{P_{tue}^2 - \left( \frac{q_{temp}}{C_{fl}} \right)^2}$$

- Installing a compressor at the PLEM. Consider the minimum allowable suction pressure is 15 bara and maximum two compressors of 11 MW each.

When considering boosting equipment, there are a few factors to take into account:

-Minimum allowed suction pressure (compressors, pump-cavitation, gas liberation which is bad for pump performance)

-Required boosting power

-Liquid pumps 0.5-5 MW Max)

-Compressor (11 MW max)

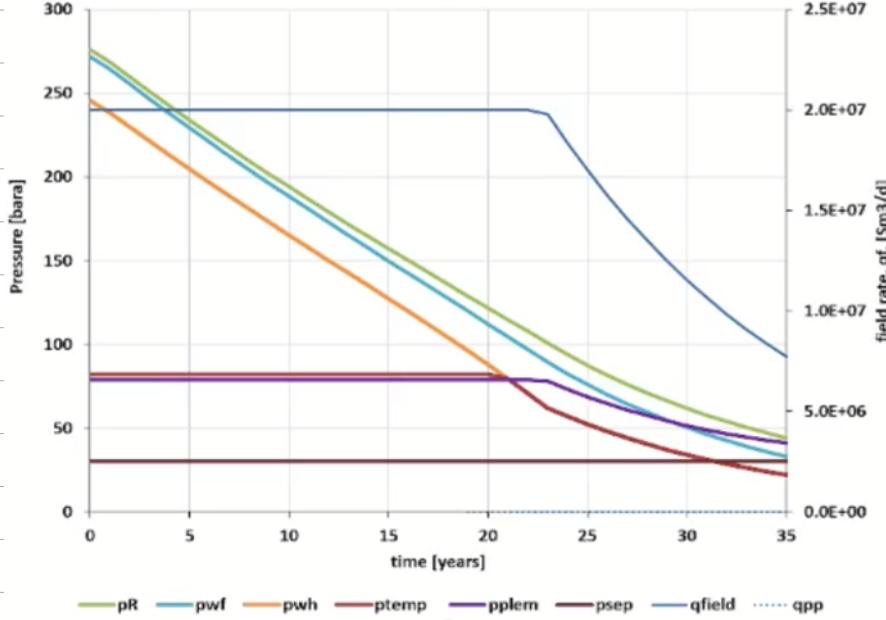
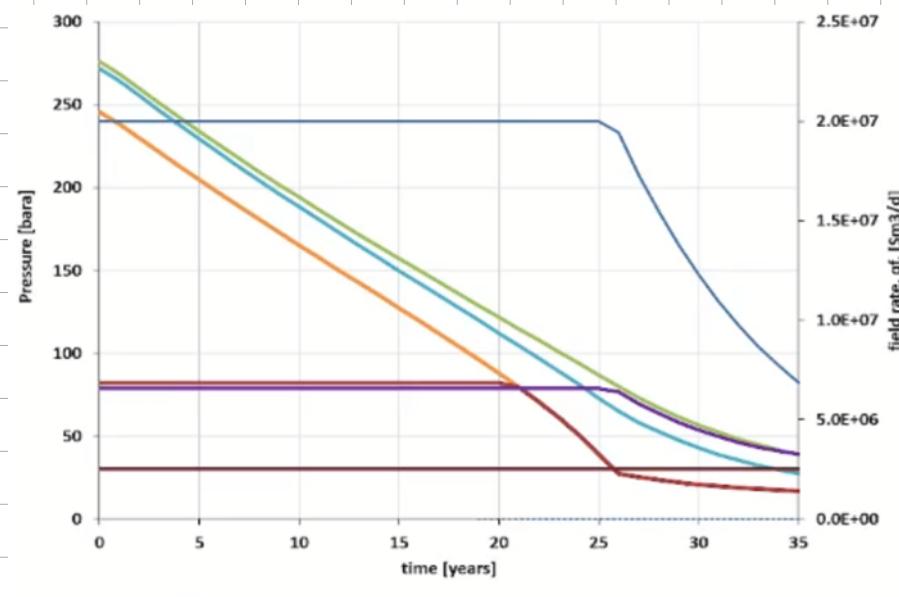
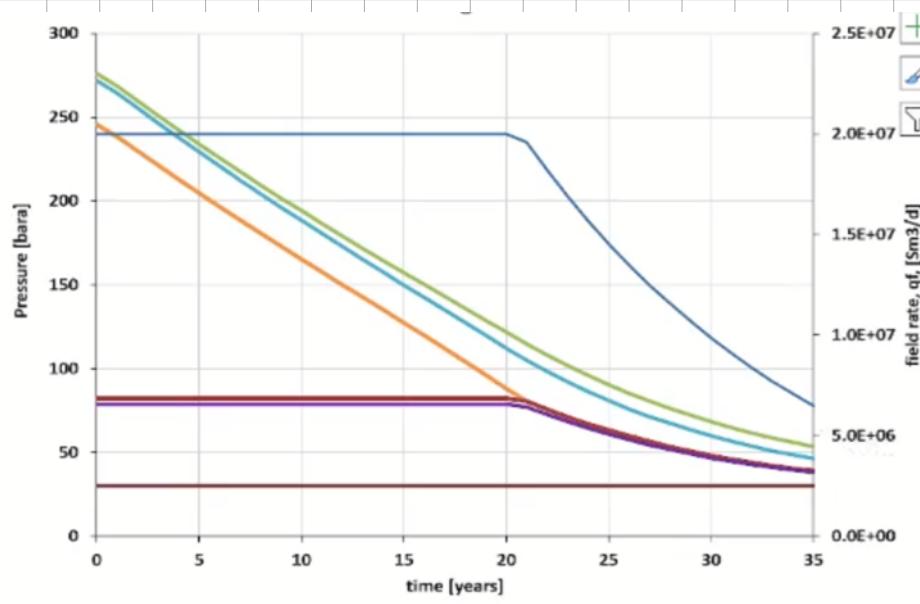
-Multiphase pump (0.5-5 MW max)

1 car --> 80 hp -->  $80 \times 700 \text{ W} = 56000 \text{ W} \rightarrow 56 \text{ kW}$

$1 \text{ MW} = 1000 \text{ kW}/56 \text{ kW} \rightarrow 19 \text{ cars}$

house consumption per year (Robin) --> 15 000 kWh (15 MWh) --> power = energy/time -->  $15 \text{ MWh}/(24 \times 365) = 1.7 \text{ kW} \rightarrow 588 \text{ houses}$

## Results:



20240215

## Outline:

- Boosting
- Economic indicators of petroleum projects

for liquid pumps

$$\dot{Q}_H = \frac{\rho g \Delta P}{2g_f}$$

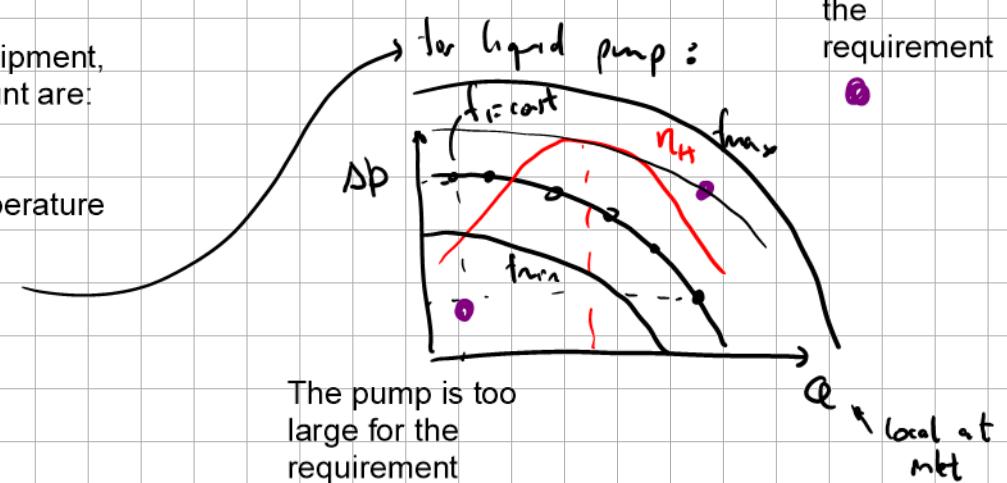
volume rate at inlet

hydraulic power

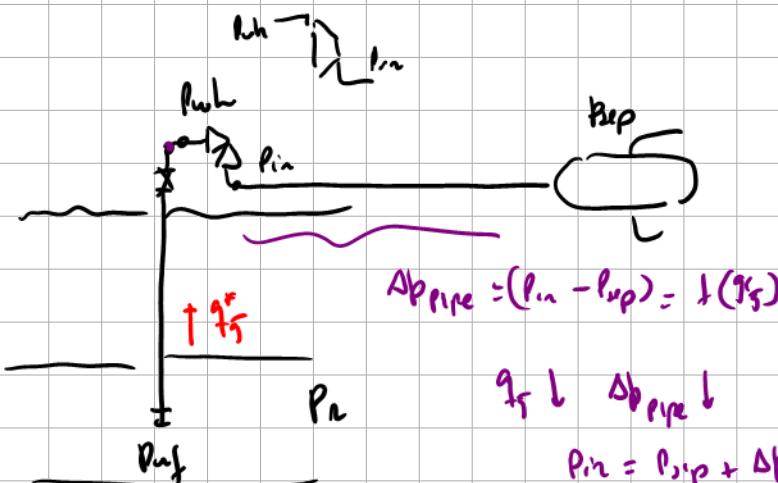
When evaluating boosting equipment, some things to take into account are:

- Minimum suction pressure
- Maximum Available power
- Maximum allowed outlet temperature (compressors)
- Operational map (envelope)

The pump is too small for the requirement



### flow equilibrium (accounting of available and required energy in the system)



$$\Delta P_{available} = (P_{in} - P_{out}) = f(q_f)$$

$$q_f \downarrow \Delta P_{available} \downarrow$$

$$P_{in} = P_a + \Delta P_{available}$$

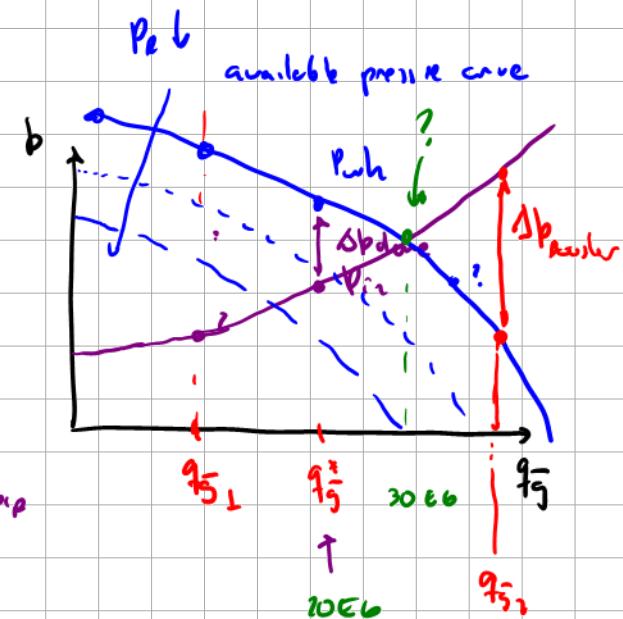
$$\Delta P_{available} = (P_a - P_{out}) = f(q_f)$$

$$q_f \downarrow \Delta P_{available} \downarrow$$

$$\Delta P_{available} = (P_{out} - P_{wh}) = f(q_f) (\Delta P_{available})$$

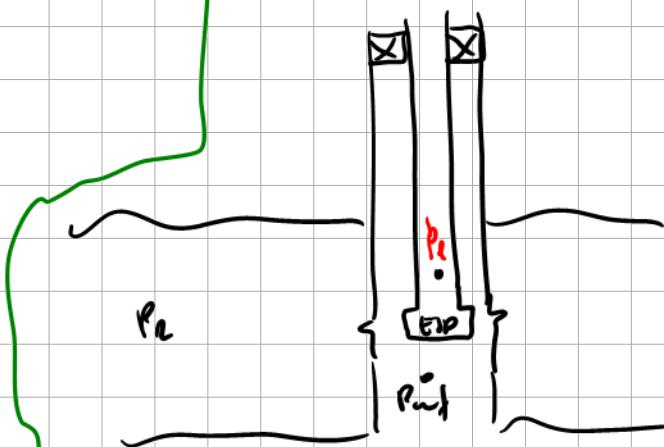
$$q_f \downarrow \Delta P_f \downarrow$$

$$P_{wh} = P_a - \Delta P_{available} - \Delta P_f$$



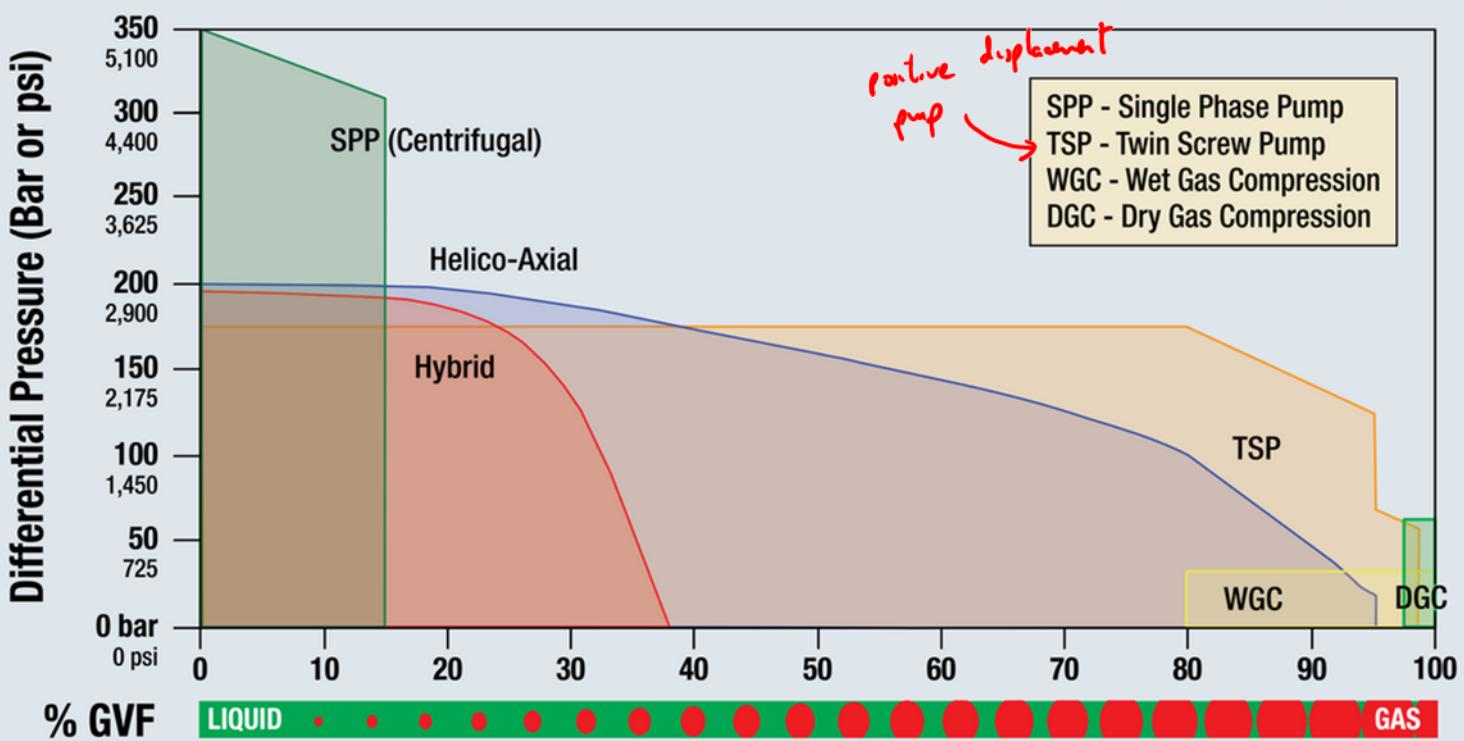
types of boosters for subsea applications  
for groups of wells  
"subsea boosting"

Artificial lift  
in well (ESP electric  
submersible pump)



<https://www.offshore-mag.com/resources/maps-posters/document/14185956/2020-worldwide-survey-of-subsea-processing>

### GRAPH 1 – GVF vs. DIFFERENTIAL PRESSURE - OPERATIONAL AND CONCEPTUAL CAPABILITIES



Notes: 1. For pump applications, the term differential pressure is used. However, for compressor applications the term pressure ratio is used. 2. Curves are approximate and assume a specific liquid throughput, identical for each pump type.

COURTESY OF **Intecsea**  
Working Group

gas volume fraction at inlet  $GVF = \frac{Q_g}{Q_g + Q_l} \times 100$



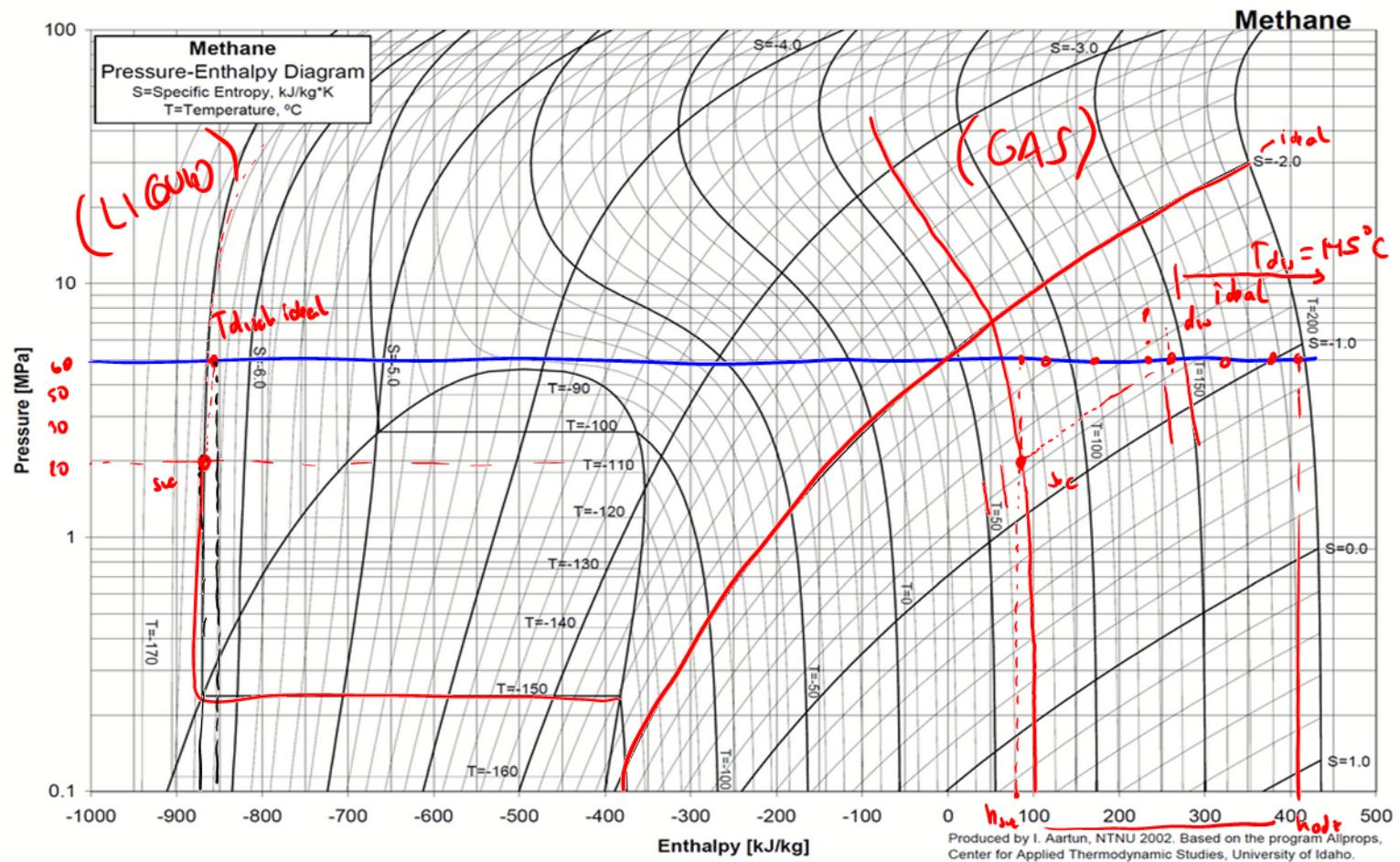
$T_b L_v$   
 $L_v L_p$

helico-axial pump arrangement

## Video of a twin screw pump operating

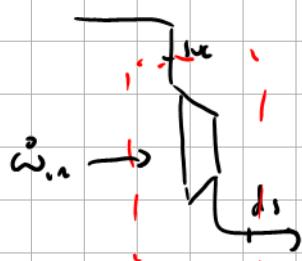
<https://www.youtube.com/watch?v=fcpTchOS81g>

A short comment about boosters and temperature change:



$$\dot{\omega}_{\text{comp}} = m(h_{dw} - h_{su})$$

$$hd_{sc} = \left( h_{sc} + \frac{\omega_{can}}{m} \right)$$



Key performance indicators

Net present value: KPI typically used to evaluate and decide on projects and to compare development alternatives

$$NPV = \sum_{t=1}^n \frac{CF_t}{(1+i)^t} = \sum_{t=1}^n \frac{\text{Revenue}_t - \text{Expenses}_t}{(1+i)^t}$$

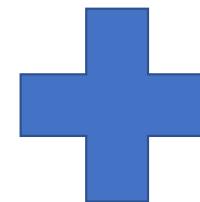
↑  
discount rate

Discounted cash flow (DCF) method

- Calculated on a yearly basis:
  - Typically end of year OR mid-year

Net present value: KPI typically used to evaluate and decide on projects and to compare development alternatives

$$NPV = \sum_{t=1}^n \frac{CF_t}{(1+i)^t} = \sum_{t=1}^n \frac{Revenue_t - Expenses_t}{(1+i)^t}$$



Discounted cash flow (DCF) method

- Calculated on a yearly basis:
  - Typically end of year OR mid-year



## Net present value

$$NPV = \sum_{t=1}^n \frac{CF_t}{(1+i)^t} = \sum_{t=1}^n \frac{\text{Revenue}_t - \text{Expenses}_t}{(1+i)^t}$$

In currency of year «t»

## Net present value

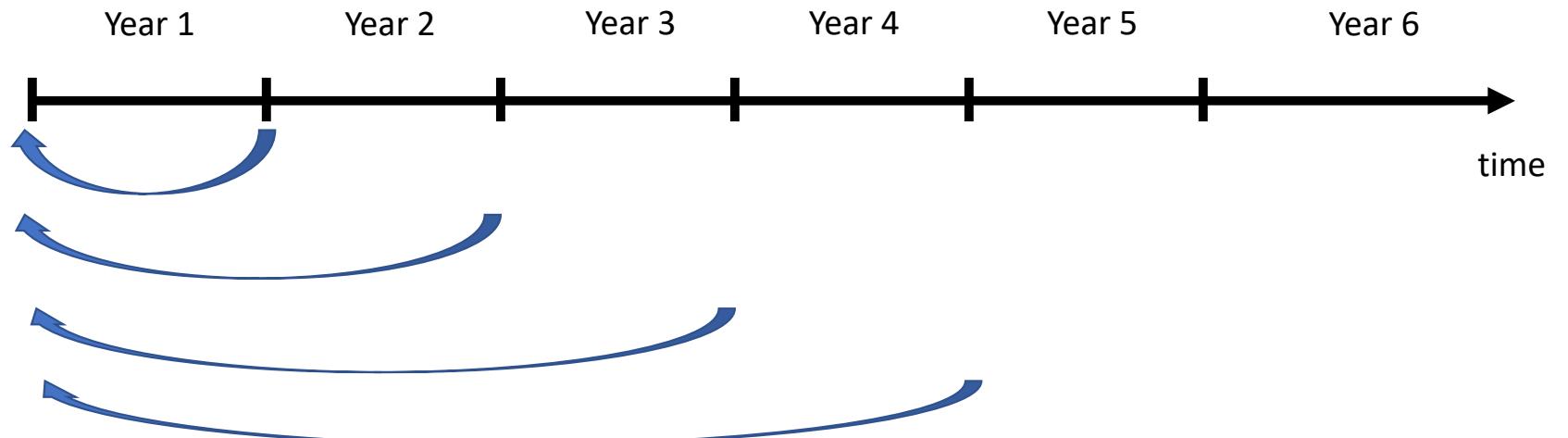
$$NPV = \sum_{t=1}^n \frac{CF_t}{(1+i)^t} = \sum_{t=1}^n \frac{\text{Revenue}_t - \text{Expenses}_t}{(1+i)^t}$$

To convert currency in year  
«t» to currency of year 0  
(reference year)

## Net present value

$$NPV = \sum_{t=1}^n \frac{CF_t}{(1+i)^t} = \sum_{t=1}^n \frac{\text{Revenue}_t - \text{Expenses}_t}{(1+i)^t}$$

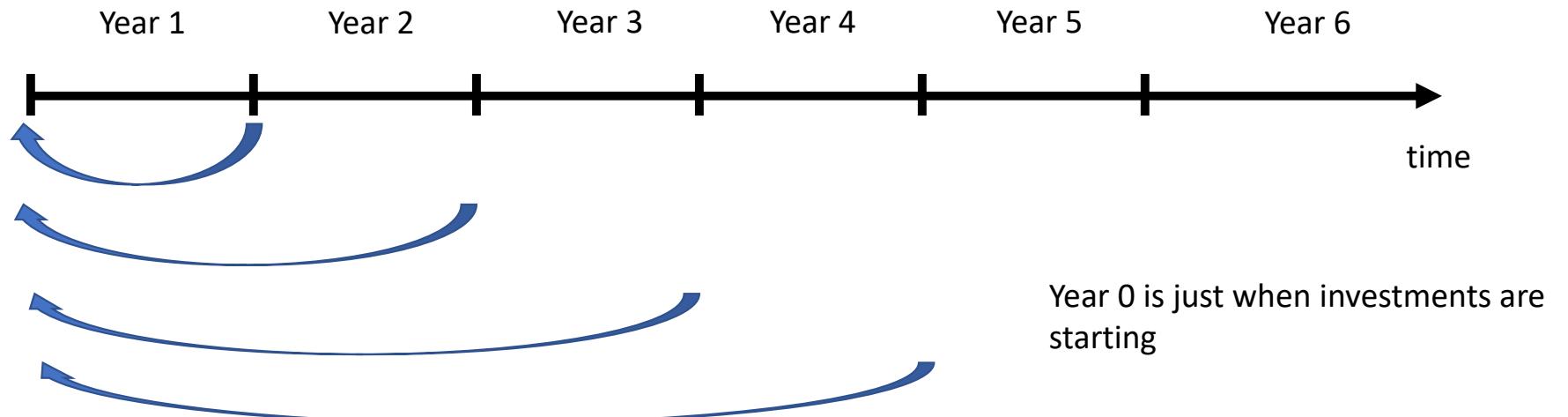
To convert currency in year «t» to year 0 (reference year)



## Net present value

$$NPV = \sum_{t=1}^n \frac{CF_t}{(1+i)^t} = \sum_{t=1}^n \frac{\text{Revenue}_t - \text{Expenses}_t}{(1+i)^t}$$

To convert currency in year «t» to year 0 (reference year)



## Net present value

$$NPV = \sum_{t=1}^n \frac{CF_t}{(1+i)^t} = \sum_{t=1}^n \frac{Revenue_t - Expenses_t}{(1+i)^t}$$



- Typically: 7-12%, based on operator's past experience
- Should be better than investing the capital on other financial instruments

# Net present value

$$NPV = \sum_{t=1}^n \frac{CF_t}{(1+i)^t} = \sum_{t=1}^n \frac{Revenue_t - Expenses_t}{(1+i)^t}$$

$Revenue_t$ :

- Sales of oil and gas (yearly production \* price per volume)
- Tariffs to other companies for using your infrastructure (e.g. processing fluids for tie-backs)

# Net present value

$$NPV = \sum_{t=1}^n \frac{CF_t}{(1+i)^t} = \sum_{t=1}^n \frac{Revenue_t - Expenses_t}{(1+i)^t}$$

$Revenue_t$ :

- Sales of oil and gas (yearly production \* price per volume)
- Tariffs to other companies for using your infrastructure (e.g. processing fluids for tie-backs)



- Assuming 50 USD/bbl, a field with 150 kstbd, for a year this gives 7.5 E09 USD (20E06 USD per day)

# Net present value

$$NPV = \sum_{t=1}^n \frac{CF_t}{(1+i)^t} = \sum_{t=1}^n \frac{Revenue_t - Expenses_t}{(1+i)^t}$$

$Revenue_t$ :

- Sales of oil and gas (yearly production \* price per volume)
- Tariffs to other companies for using your infrastructure (e.g. processing fluids for tie-backs)



- Assuming 50 USD/bbl, a field with 150 kstbd, for a year this gives 7.5 E09 USD (20E06 USD per day)
- Assuming a gas price of 0.66 USD/m<sup>3</sup> (Feb 2023), and a production of 20E06 Sm<sup>3</sup>/d, this gives for a year 4.8 E09 USD (13 E06 USD per day)

# Net present value

$$NPV = \sum_{t=1}^n \frac{CF_t}{(1+i)^t} = \sum_{t=1}^n \frac{Revenue_t - Expenses_t}{(1+i)^t}$$

$Revenue_t$ :

- Sales of oil and gas (yearly production \*  
*price per volume*)
- Tariffs to other companies for using your infrastructure (e.g. processing fluids for tie-backs)

- Usually assumed constant
- If gas, it is usually negotiated as part of a delivery contract

# Net present value

$$NPV = \sum_{t=1}^n \frac{CF_t}{(1+i)^t} = \sum_{t=1}^n \frac{Revenue_t - Expenses_t}{(1+i)^t}$$

$Revenue_t$ :

- Sales of oil and gas (yearly production \* price per volume)
- Tariffs to other companies for using your infrastructure (e.g. processing fluids for tie-backs)

During early years (4-8) there is no revenue!! (field doesn't exist)

## Net present value

$$NPV = \sum_{t=1}^n \frac{CF_t}{(1+i)^t} = \sum_{t=1}^n \frac{Revenue_t - Expenses_t}{(1+i)^t}$$

$$Expenses_t = \underbrace{DRILLEX_t + CAPEX_t}_{\text{Drilling expenditure}} + Depreciation_t + OPEX_t + TAX_t + ABEX_t$$

## Net present value

$$NPV = \sum_{t=1}^n \frac{CF_t}{(1+i)^t} = \sum_{t=1}^n \frac{Revenue_t - Expenses_t}{(1+i)^t}$$

$$Expenses_t = DRILLEX_t + CAPEX_t + Depreciation_t + OPEX_t + TAX_t + ABEX_t$$

The biggest expenses occur at the beginning, when there is a lot of construction and drilling

# Net present value

$$NPV = \sum_{t=1}^n \frac{CF_t}{(1+i)^t} = \sum_{t=1}^n \frac{Revenue_t - Expenses_t}{(1+i)^t}$$

$$Expenses_t = DRILLEX_t + CAPEX_t + Depreciation_t + OPEX_t + TAX_t + ABEX_t$$

## Exploration costs

All exploration costs are, as a starting point, deductible and may be off-set against profits from production.

Moreover, companies may claim an annual cash refund of the tax value of direct and indirect exploration costs under ordinary petroleum tax and special tax (this amounts to 78% of such costs), with the exception of finance costs, with the amount of the refund limited to the tax value of the net tax losses. This is an alternative to carrying the losses forward.

Source: oil and gas taxation in Norway. Deloitte

# Net present value

$$NPV = \sum_{t=1}^n \frac{CF_t}{(1+i)^t} = \sum_{t=1}^n \frac{Revenue_t - Expenses_t}{(1+i)^t}$$

$$Expenses_t = DRILLEX_t + CAPEX_t + Depreciation_t + OPEX_t + TAX_t + ABEX_t$$

A deductible for taxes is **an expense that a taxpayer or business can subtract from adjusted gross income**, which reduces their income, thereby reducing the overall tax they need to pay.

<https://www.investopedia.com> › ... › Tax Deductions

Deductible Definition, Common Tax and Business Deductibles

## Net present value

$$NPV = \sum_{t=1}^n \frac{CF_t}{(1+i)^t} = \sum_{t=1}^n \underbrace{\frac{Revenue_t - Expenses_t}{(1+i)^t}}_{\text{often neglected}}$$

*↓*

$$Expenses_t = DRILLEX_t + CAPEX_t + Depreciation_t + OPEX_t + TAX_t + ABEX_t$$

### Examples:

- Well plugging
- Removal of flowlines, pipelines, offshore structure
- Cleaning
- monitoring

## Net present value

$$NPV = \sum_{t=1}^n \frac{CF_t}{(1+i)^t} = \sum_{t=1}^n \frac{Revenue_t - Expenses_t}{(1+i)^t}$$

$$Expenses_t = DRILLEX_t + CAPEX_t + Depreciation_t + OPEX_t + TAX_t + ABEX_t$$

Are often neglected as they are deductible and they occur late in the life of the field (heavily discounted)

### Abandonment costs

Abandonment costs are deductible when the costs are actually incurred. Accounting provisions made in order to meet future abandonment costs are not deductible.

Source: oil and gas taxation in Norway. Deloitte

## Net present value

$$NPV = \sum_{t=1}^n \frac{CF_t}{(1+i)^t} = \sum_{t=1}^n \frac{Revenue_t - Expenses_t}{(1+i)^t}$$

$$Expenses_t = DRILLEX_t + CAPEX_t + \textcircled{Depreciation}_t + OPEX_t + TAX_t + ABEX_t$$

Capital allowances for investments made in production facilities and pipelines and installations which are part of such production facilities and pipelines are calculated on a straight line basis over six years at a rate of 16.66% per year from the date the capital expenditure was incurred. The capital allowances are granted both when calculating the basis for ordinary petroleum tax and special tax.

Source: oil and gas taxation in Norway. Deloitte

## Net present value

$$NPV = \sum_{t=1}^n \frac{CF_t}{(1+i)^t} = \sum_{t=1}^n \frac{Revenue_t - Expenses_t}{(1+i)^t}$$

$$Expenses_t = DRILLEX_t + CAPEX_t + Depreciation_t + OPEX_t + TAX_t + ABEX_t$$

### Examples:

- Drilling vessel renting (daily rate)
- Drilling materials (tubulars, cement, mud, completion, wellhead)
- Test during drilling (DST, logging, pressure tests, sampling)
- X-mas tree
- Drilling tools
- Salaries, insurance

## Net present value

$$NPV = \sum_{t=1}^n \frac{CF_t}{(1+i)^t} = \sum_{t=1}^n \frac{Revenue_t - Expenses_t}{(1+i)^t}$$

$$Expenses_t = DRILLEX_t + CAPEX_t + Depreciation_t + OPEX_t + TAX_t + ABEX_t$$

### Examples:

- Drilling vessel renting (daily rate)
  - Drilling materials (tubulars, cement, mud, completion, wellhead)
  - Test during drilling (DST, logging, pressure tests, sampling)
  - X-mas tree
  - Drilling tools
  - Salaries, insurance
- ] • Cost per well:  
30-180 E06 USD (offshore)  
10-15 E06 (onshore)

# Example

Source: Karish-Tanin PDO

Table 8-4: Drilling tangibles cost estimate

Item	Source	Cost (US\$)
<b>Wellhead</b>	TechnipFMC quotation 7/4/17	362,500
<b>Conductor</b>	LR data based on planned 2017 well	320,000
<b>20" Casing</b>	Tenaris quotation 31/3/17	722.56/m
<b>13-5/8" Casing</b>	Tenaris quotation 31/3/17	342.76/m
<b>9-5/8" Casing</b>	Tenaris quotation 31/3/17	204.80/m
<b>9-5/8" 13 Cr Casing</b>	Tenaris quotation 31/3/17	956.00/m
<b>Float equipment, etc. (full set)</b>	LR data based on planned 2017 well	366,000
<b>Total</b>		<b>6,617,464.00</b>

Table 8-5: Completion tangibles cost estimate

Item	Source	Cost (US\$)
<b>Well test equipment</b>	LR data based on planned 2017 well	1,015,000
<b>SSTT</b>	Expro quotation 10/4/17	750,000
<b>OHGP</b>	LR data based on planned 2017 well	925,000
<b>Upper completion</b>	LR data based on planned 2017 well	625,000
<b>Xmas Tree</b>	TechnipFMC quotation 7/4/17	4,738,682
<b>FMC Installation costs</b>	TechnipFMC quotation 7/4/17	1,300,000

# Example

Source: Karish-Tanin PDO

Table 8-6: Total calculated drilling costs – 3 Karish Main development wells

Certainty level	Total days	Total Services Spread rate (US\$ mln)	Total Rig rate (US\$ mln)	Drilling tangibles (US\$ mln)	Completion tangibles (US\$ mln)	Total Drillex (US\$ mln)
P90	379	95.22	94.75	24.82	35.07	248.86
P50	277	55.68	55.40	19.86	28.06	159.00
P10	241	36.33	36.15	14.89	21.04	108.41

# Net present value

$$NPV = \sum_{t=1}^n \frac{CF_t}{(1+i)^t} = \sum_{t=1}^n \frac{Revenue_t - Expenses_t}{(1+i)^t}$$

$$Expenses_t = DRILLEX_t + CAPEX_t + Depreciation_t + OPEX_t + TAX_t + ABEX_t$$

## Examples:

- Engineering studies
- Processing facilities (separators, pumps, compressors, heat exchangers, control system, injection, oil, water and gas treatment)
- Offshore structure (cost of platform or vessel, living quarters, power source, helideck)
- Subsea system (template, flowlines, pipelines, risers, umbilicals, metering)
- Export system
- Salaries, insurance

# Net present value

$$NPV = \sum_{t=1}^n \frac{CF_t}{(1+i)^t} = \sum_{t=1}^n \frac{Revenue_t - Expenses_t}{(1+i)^t}$$

$$Expenses_t = DRILLEX_t + \text{CAPEX}_t + \text{Depreciation}_t + OPEX_t + TAX_t + ABEX_t$$

## Examples:

- Engineering studies
- Processing facilities (separators, pumps, compressors, heat exchangers, control system, injection, oil, water and gas treatment)
- Offshore structure (cost of platform or vessel, living quarters, power source, helideck)
- Subsea system (template, flowlines, pipelines, risers, umbilicals, metering)
- Export system
- Salaries, insurance

There is usually a payment schedule for CAPEX over a few years for big items (FPSO, subsea equipment etc)

# Net present value

$$NPV = \sum_{t=1}^n \frac{CF_t}{(1+i)^t} = \sum_{t=1}^n \frac{Revenue_t - Expenses_t}{(1+i)^t}$$

$$Expenses_t = DRILLEX_t + CAPEX_t + Depreciation_t + OPEX_t + TAX_t + ABEX_t$$

## Examples:

- Engineering studies
- Processing facilities (separators, pumps, compressors, heat exchangers, control system, injection, oil, water and gas treatment)
- Offshore structure (cost of platform or vessel, living quarters, power source, helideck)
- Subsea system (template, flowlines, pipelines, risers, umbilicals, metering)
- Export system
- Salaries, insurance

## Total cost:

-O (1E09) USD

## Examples:

- O( 1E06) USD per km of subsea pipeline
- FPSO 200 – 3000 1E06 USD

# Examples

**Table 6-6 CAPEX Estimation Example (2007 Data)**  
**1. Subsea Equipment Cost**

	Subsea Trees	Unit	Cost
<b>Subsea Tree Assembly</b>		<b>3</b>	<b>\$4,518,302</b>
(each) 5-inch × 2-inch 10-ksi vertical tree assembly	1	included	
Retrievable choke assembly	1	included	
Tubing hanger 5-in. 10 ksi	1	included	
High-pressure tree cap	1	included	
5-in. tubing head spool assembly	1	included	
Insulation	1	included	
<hr/>			
<b>Subsea Hardware</b>			
<b>Subsea Manifold</b>			
(EE trim)	1		\$5,760,826
<b>Suction Pile</b>			
Suction pile for manifold	1		\$1,000,000
<b>Production PLET</b>	2		\$3,468,368
<b>Production Tree Jumpers</b>	3		\$975,174
<b>Pigging Loop</b>	1		\$431,555
<b>Production PLET Jumpers</b>	2		\$1,796,872
<b>Flying Leads</b>			\$1,247,031
Hydraulic flying lead SUTA to tree			
Electrical flying lead SUTA to tree			
Hydraulic flying lead SCM to manifold			
Electrical flying lead SUTA to manifold			
<hr/>			
<b>Other Subsea Hardware</b>			
<b>Multiphase Flow Meter</b>	1		\$924,250

Source: Yong Bai, Qiang Bai, Subsea engineering Handbook.

# Examples

**Table 6-6** CAPEX Estimation Example (2007 Data)—cont'd

**1. Subsea Equipment Cost**

Subsea Trees	Unit	Cost
<b>Umbilicals</b>		
<b>Umbilical</b> 25,000ft Length		\$11,606,659
<b>Risers</b>		
<b>Riser</b> Prod. 8.625-in. × 0.906-in. × 65 SCR, 2 × 7500 ft		\$6,987,752
<b>Flowlines</b>		
<b>Flowline</b> Dual 10-in. SMLS API 5L X-65, flowline, 52,026 ft		\$4,743,849
	<b>Total Procurement Cost</b>	<b>\$54,264,324</b>
<b>2. Testing Cost</b>		
<b>Subsea Hardware FAT,EFAT</b>		\$27,132,162
<b>Tree SIT &amp; Commissioning</b>		\$875,000
<b>Manifold &amp; PLET SIT</b>		\$565,499
<b>Control System SIT</b>		\$237,786
	<b>Total Testing Cost</b>	<b>\$28,810,447</b>
<b>3. Installation Cost</b>		
<b>Tree</b> 3 days × \$1000k per day		\$3,000,000
<b>Manifold &amp; Other hardware</b>		\$48,153
<b>Jumpers</b> (1 day per jumper + downtime)		\$32,102
<b>ROV Vessel Support</b>		\$1,518,000
<b>Other Installation Cost</b>		\$862,000
<b>Pipe-lay</b> 52,0260ft		\$43,139,000

Source: Yong Bai, Qiang Bai, Subsea engineering Handbook.

# Net present value

$$NPV = \sum_{t=1}^n \frac{CF_t}{(1+i)^t} = \sum_{t=1}^n \frac{Revenue_t - Expenses_t}{(1+i)^t}$$

$$Expenses_t = DRILLEX_t + CAPEX_t + Depreciation_t + OPEX_t + TAX_t + ABEX_t$$

## Examples:

- Salaries
- Insurance
- Maintenance
- Equipment
- Well intervention
- Power consumption
- Production chemicals (MEG, inhibitors)
- Pigging
- Transportation and export

- Heavily depends on the size and type of facility
- It often dictates when to abandon (CF becomes negative)

# Net present value

$$NPV = \sum_{t=1}^n \frac{CF_t}{(1+i)^t} = \sum_{t=1}^n \frac{Revenue_t - Expenses_t}{(1+i)^t}$$

$$Expenses_t = DRILLEX_t + CAPEX_t + Depreciation_t + OPEX_t + TAX_t + ABEX_t$$

## Examples:

- Salaries
- Insurance
- Maintenance
- Equipment
- Well intervention
- Power consumption
- Production chemicals (MEG, inhibitors)
- Pigging
- Transportation and export

- }
- Heavily depends on the size and type of facility
  - It often dictates when to abandon (CF becomes negative)

$$\text{Annual OPEX} = [A(\%) \times \text{cumulative CAPEX}(\$)] + \left[ B\left(\frac{\$}{bbl}\right) \times \text{production}\left(\frac{bbl}{year}\right) \right]$$

## Net present value

$$NPV = \sum_{t=1}^n \frac{CF_t}{(1+i)^t} = \sum_{t=1}^n \frac{Revenue_t - Expenses_t}{(1+i)^t}$$

$$Expenses_t = DRILLEX_t + CAPEX_t + Depreciation_t + OPEX_t + TAX_t + ABEX_t$$

Should be adjusted by inflation

$DRILLEX_t$  $CAPEX_t$  $OPEX_t$ 

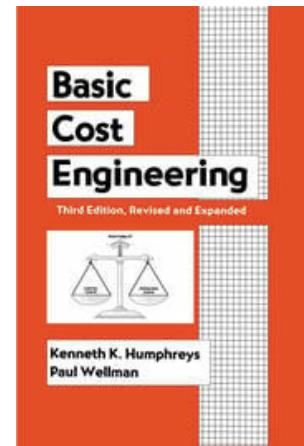
Function of number of wells, maximum production rates of oil, gas and water, development concept, type of fluids etc.

## Cost estimation – expected accuracy

- For DG1, +-40%
- For DG2, +-30%
- For DG3, +-20%

# Costing

- It is a profession and a discipline
- Internal company databases  
(based on previous projects)
- Provided by contractors and suppliers
- Commercial software
- Depending on the desired accuracy, can take significant time



$$C_2 = C_1 \left( \frac{S_2}{S_1} \right)^n$$

$C_1$  = cost of equipment of capacity  $S_1$

$C_2$  = cost of equipment of capacity  $S_2$

# Class outline 20240216

-(cont). Economic indicators for oil and gas projects

## Net present value

$$NPV = \sum_{t=1}^n \frac{CF_t}{(1+i)^t} = \sum_{t=1}^n \frac{Revenue_t - Expenses_t}{(1+i)^t}$$

$$Expenses_t = DRILLEX_t + CAPEX_t + Depreciation_t + OPEX_t - TAX_t + ABEX_t$$

- Petroleum tax
- CO2 tax (in 2022 NOK 1.65 NOK/Sm3 gas)

The Norwegian petroleum tax system is based on the taxation of the entity rather than taxation of specific petroleum assets.

### **Neutral tax system**

The petroleum taxation system is intended to be neutral, so that an investment project that is profitable for an investor before tax is also profitable after tax. This ensures substantial revenues for the Norwegian society and at the same time encourages companies to carry out all profitable projects.

To ensure a neutral tax system, only the company's net profit is taxable, and losses may be carried forward in the company tax. Special tax value of losses is reimbursed at the tax settlement, the year after it accrued. Neutral properties in the tax system are also important when defining investment based tax deductions.

Sources:

oil and gas taxation in Norway. Deloitte

<https://www.norskpetroleum.no/en/economy/petroleum-tax>

<b>Ordinary corporate tax</b>	<b>Special tax</b>
Operating income (norm prices for oil)	Operating income (norm prices for oil)
- Operating expenses	- Operating expenses
- Linear depreciation for investments (6 years)	- Depreciation for investments (100 %)
- Exploration expenses, R&D and decom.	- Exploration expenses, R&D and decom.
- Environmental taxes and area fees	- Environmental taxes and area fees
- Net financial costs	- Calculated ordinary tax
- (Loss carry forward)	
<b>= Corporation tax base (22 %)</b>	<b>= Special tax base (71,8 %)</b>

The Petroleum Price Council is responsible for setting norm prices, which it does after collecting information from the companies and holding meetings with them. The norm price system applies to various types and qualities of petroleum. For gas, the actual sales prices are used.

Source: <https://www.norskpetroleum.no/en/economy/petroleum-tax>

## Net present value

$$NPV = \sum_{t=1}^n \frac{CF_t}{(1+i)^t} = \sum_{t=1}^n \frac{Revenue_t - Expenses_t}{(1+i)^t}$$

$Expenses_t = DRILLEX_t + CAPEX_t + Depreciation_t + OPEX_t - TAX_t + ABEX_t$

- CO2 tax (in 2022 NOK 1.65 NOK/Sm3 gas)

## Net present value

$$NPV = \sum_{t=1}^n \frac{CF_t}{(1+i)^t} = \sum_{t=1}^n \frac{Revenue_t - Expenses_t}{(1+i)^t}$$

$$Expenses_t = DRILLEX_t + CAPEX_t + Depreciation_t + OPEX_t - TAX_t + ABEX_t$$

*(30 MW)*

262100 MWh (30 MW)  
1 MWh  
257 Sm3 gas

- CO2 tax (in 2022 NOK 1.65 NOK/Sm3 gas)

Example:

- Considering gas turbine efficiency 1 MWh/257 Sm3 gas (TPG4245 – 2022).
- For a field with 30 MW, in a year this represents 262 800 MWh, which represents 67 E06 Sm3 of gas.
- This will be taxed with ca 111 E06 USD.

## Net present value - Royalties

$$NPV = \sum_{t=1}^n \frac{CF_t}{(1+i)^t} = \sum_{t=1}^n \frac{Revenue_t - Expenses_t}{(1+i)^t}$$

$$Expenses_t = DRILLEX_t + CAPEX_t + Depreciation_t + OPEX_t + TAX_t + ABEX_t$$

- Used in some countries
- % from the production, not the profit!!

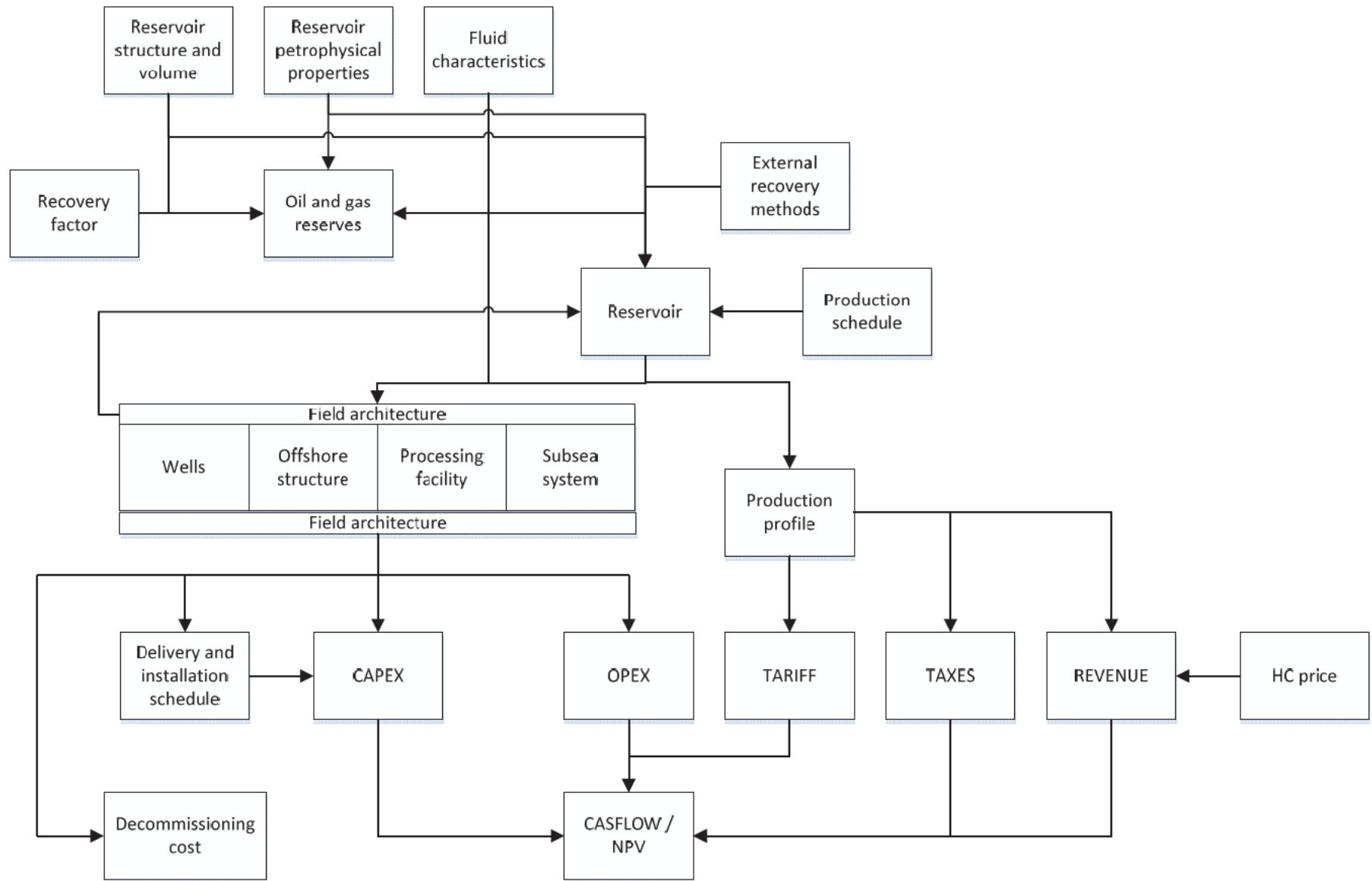
## Net present value calculation- Who does what:

- Production profiles of oil, gas and condensate: petroleum engineers
- CAPEX: cost engineers (or suppliers) with input from facilities engineers, marine engineers
- DRILLEX: cost engineers (or suppliers) with input from drilling engineers
- Gas and oil prices: Market analyst
- Tax, Inflation, Exchange rate, discount rate: Finance department

## Net present value calculation- Who does what:

- Production profiles of oil, gas and condensate: petroleum engineers
- CAPEX: cost engineers (or suppliers) with input from facilities engineers, marine engineers
- DRILLEX: cost engineers (or suppliers) with input from drilling engineers
- Gas and oil prices: Market analyst
- Tax, Inflation, Exchange rate, discount rate: Finance department

- Highly affected by the development strategy
- All are interconnected!!
- Take time to generate. If there are changes, it takes time to get new values



Example:

Higher production rates →

bigger separators and compressors →

more weight →

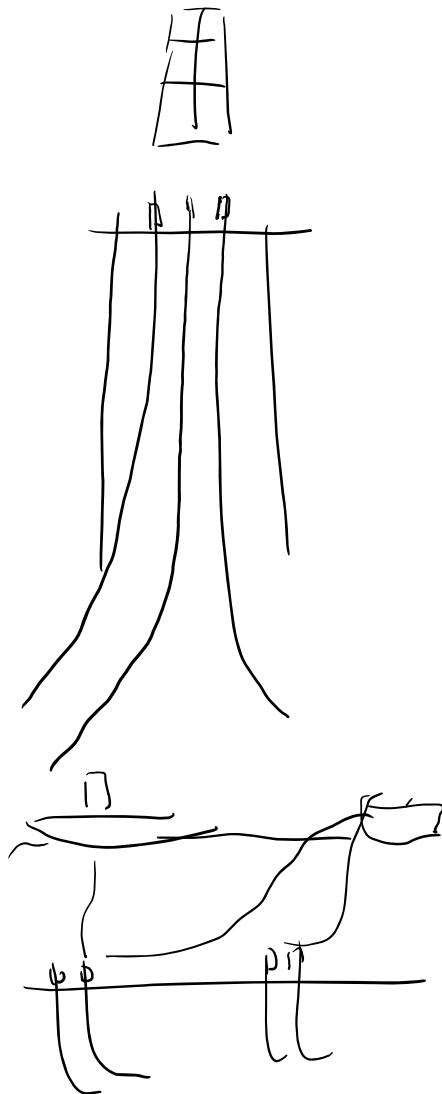
bigger offshore structure

# NPV estimation

Source: Hebron field  
PDO

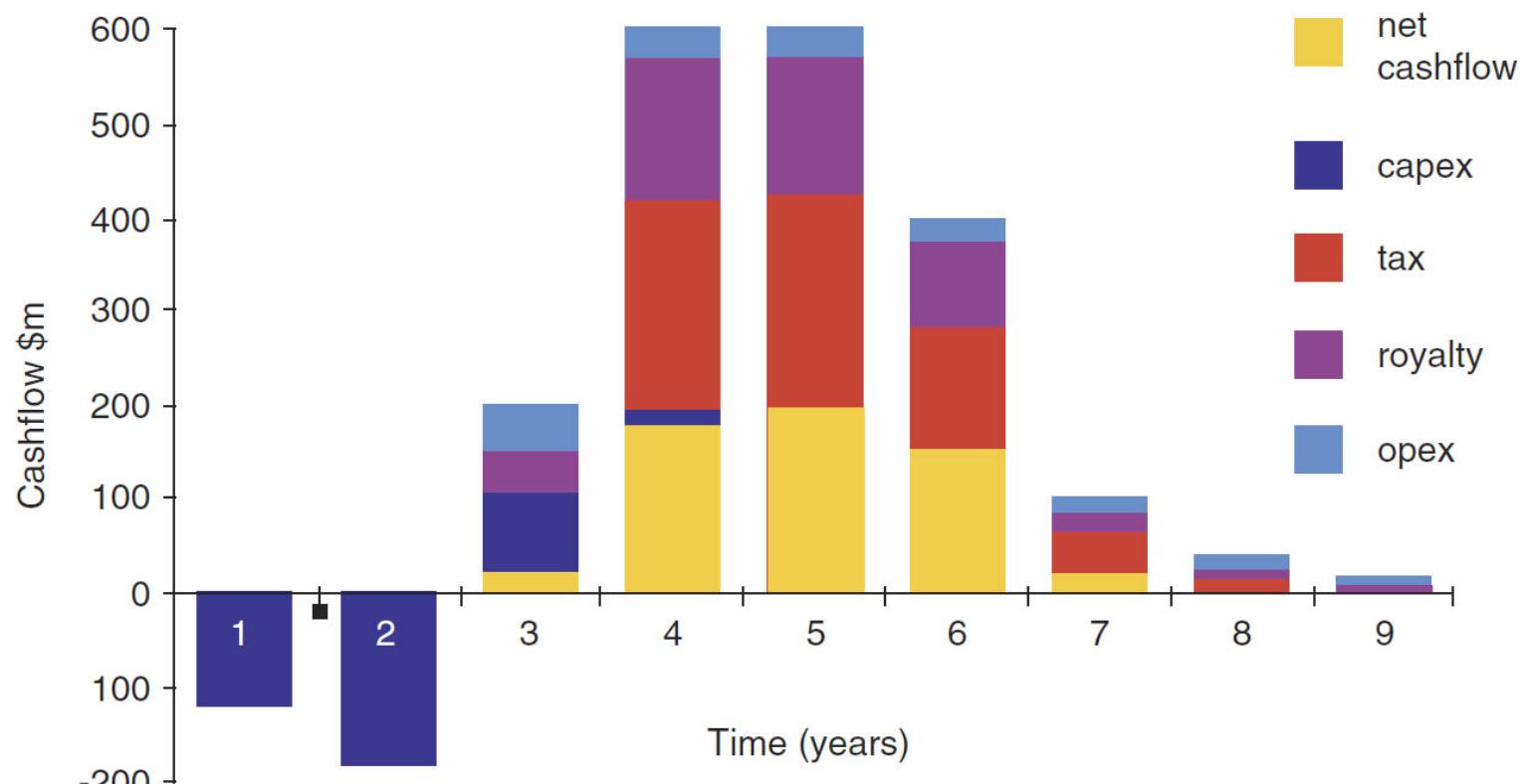
Table 13.4-1: Hebron Platform Development Capital and Operating Estimates

Year	Capital Costs (\$M CAD))				Drilling	Total	Operating Costs (\$MCAD)			
	Pre-Production			OLS						
	Proj.	Admin.	Topside							
2010	68		12	13	0	93	1			
2011	174		394	240	0	807	9			
2012	244		704	291	12	1252	11			
2013	216		698	391	36	1340	14			
2014	290		643	444	107	1484	20			
2015	327		409	234	69	1039	36			
2016	256			175	0	513	65			
2017					222	222	157			
2018					236	236	147			
2019					242	242	148			
2020					242	242	174			
2021					242	242	159			
2022					218	218	159			
2023					189	189	159			
2024					215	215	179			
2025							159			
2026							161			
2027							164			
2028							187			
2029							176			
2030							196			
2031							194			
2032							210			
2033							190			
2034							188			
2035							186			
2036							202			
2037							182			
2038							181			
2039							179			
2040							197			
2041							180			
2042							180			
2043							180			
2044							187			
2045							176			
2046							592			
<b>TOTAL</b>	\$ 1,575	\$ 2,861	\$ 1,788	\$ 224	\$ 1,887	\$ 8,334	\$ 5,883			



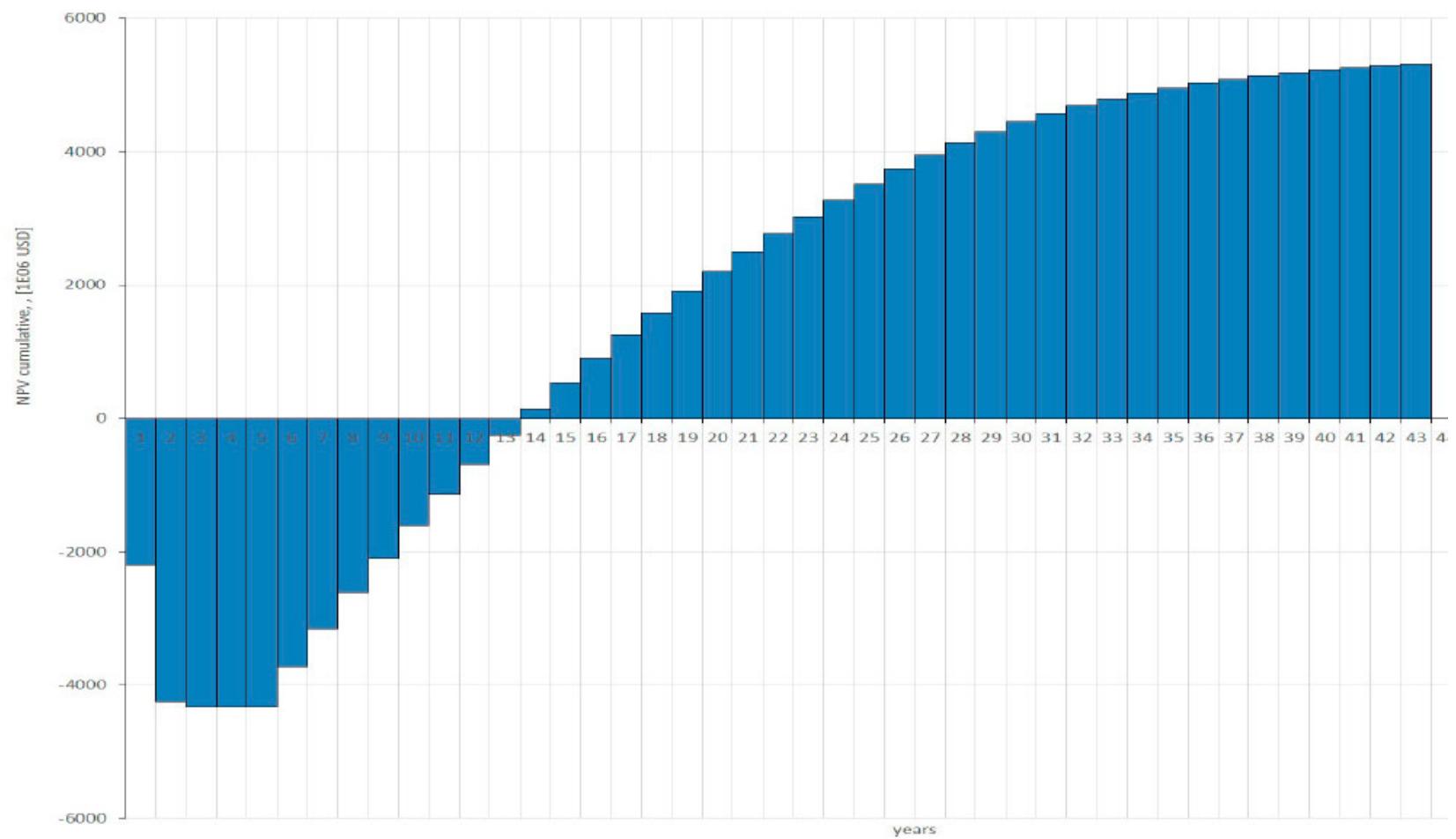
## CF versus time

Source: Frank Jahn,  
Mark Cook, Mark  
Graham. Hydrocarbon  
Exploration and  
Production



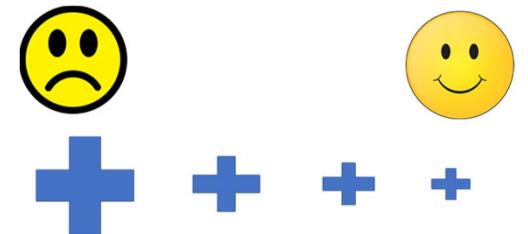
**Figure 14.5** Components of a project cashflow.

## NPV versus time



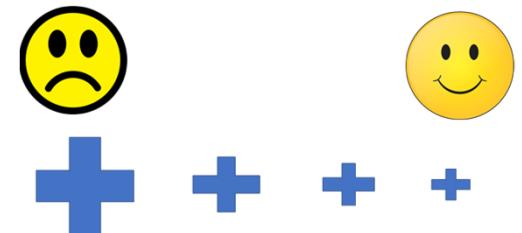
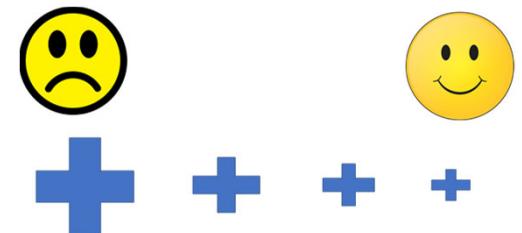
## Other KPIs used

- Break-even price → oil price that give  $NPV = 0$



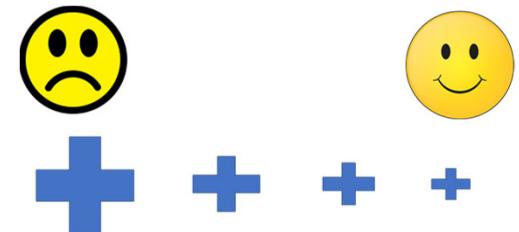
## Other KPIs used

- Break-even price → oil price that give  $NPV = 0$
- NPV break-even → time when  $NPV = 0$

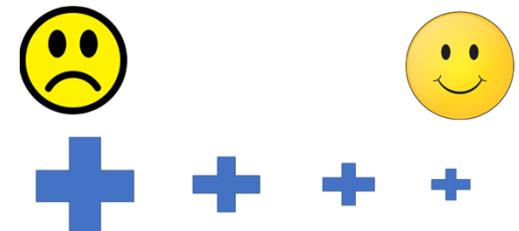


## Other KPIs used

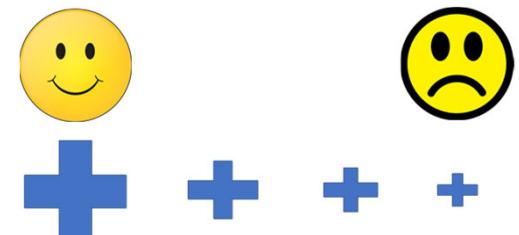
- Break-even price → oil price that give  $NPV = 0$



- NPV break-even → time when  $NPV = 0$

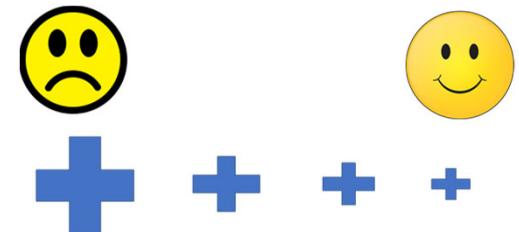


- Internal rate of return (IRR) → discount rate for which  $NPV = 0$

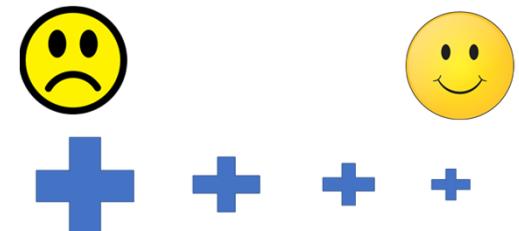


## Other KPIs used

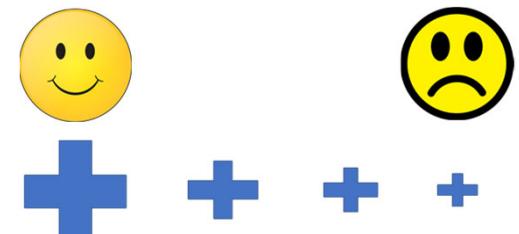
- Break-even price → oil price that give  $NPV = 0$



- NPV break-even → time when  $NPV = 0$



- Internal rate of return (IRR) → discount rate for which  $NPV = 0$



- OTHERS...

# Standards

INTERNATIONAL  
STANDARD                    ISO  
                                  15663

First edition  
2021-02

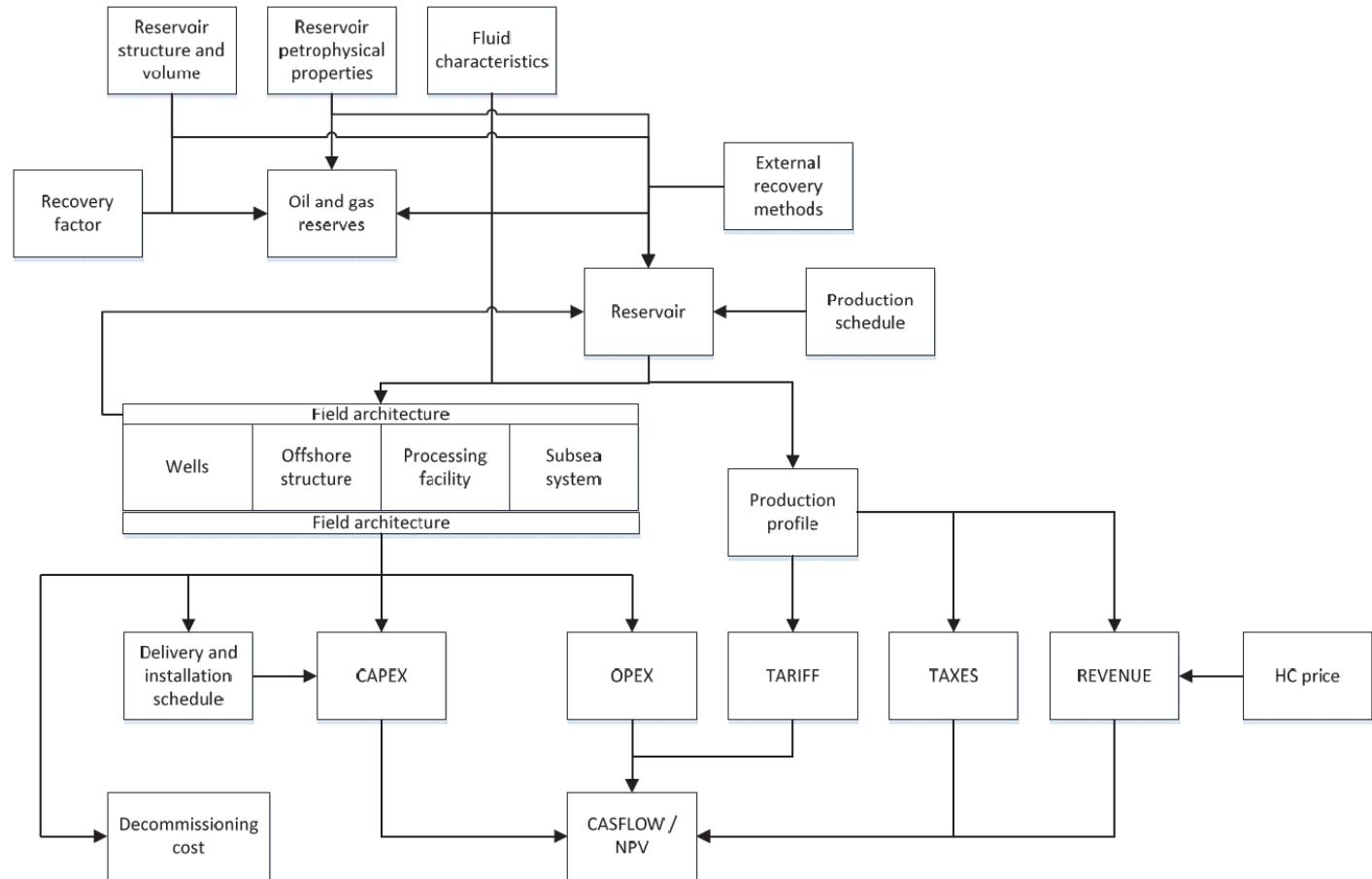
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**Petroleum, petrochemical and natural  
gas industries — Life cycle costing**

*Industries du pétrole et du gaz naturel — Estimation des coûts  
globaux de production et de traitement*

# Handling uncertainty



# Handling uncertainty – from the standard

## Industry practices:

- Typical sensitivity analysis is performed changing inputs for CAPEX (e.g. +-15% and +-30%), product price (e.g. +-10% and +-20%), production start delay (e.g. 1 year). Results are calculated for NPV and IRR
- For production impact, worst and best production cases are performed
- Probabilistic approach with quantitative analysis very complex to be performed and very seldom used (for giant project only in case).
  - The results is a probabilistic curve for NPV and IRR using risked CAPEX and schedule, production, prices and discount rate as input
  - Deterministic NPV with P< P50 indicates good probability to achieve the deterministic result
- Sensitivity for CO2 tax scenarios is also performed

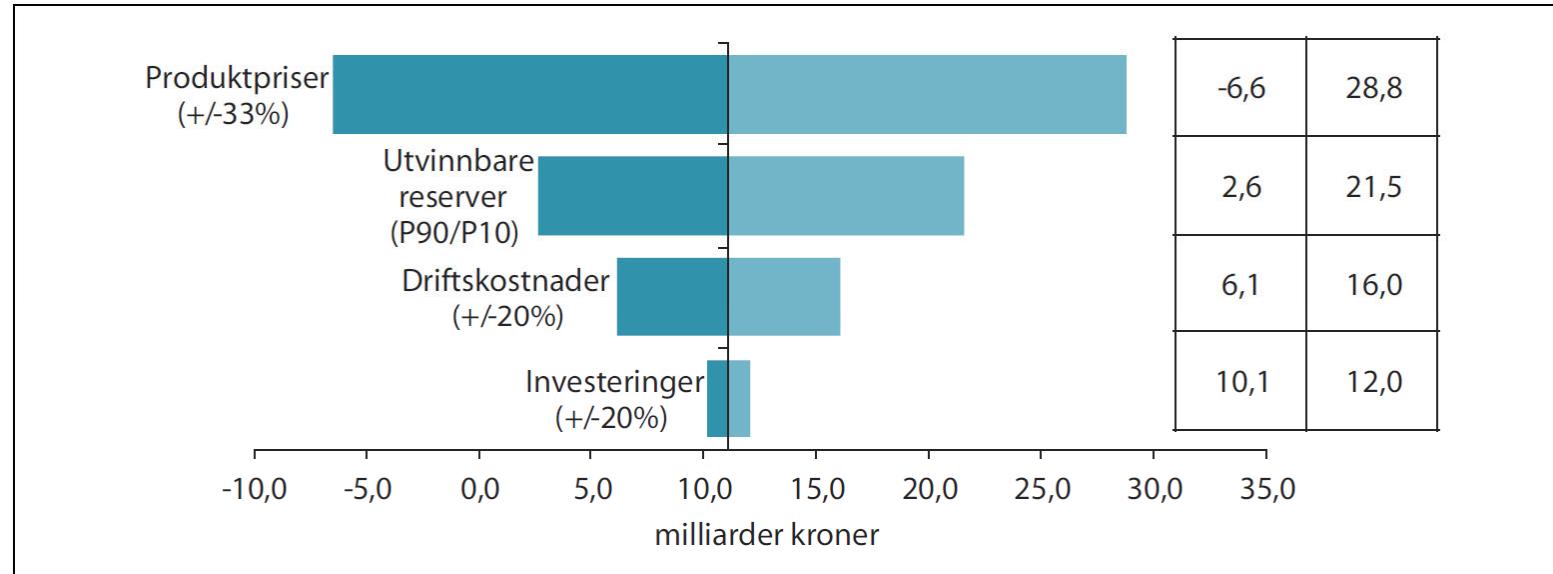
Source: ISO 15663:2021 course, 9 June 2021

# Sensitivity analysis

Varying one at a time: «Ceteris paribus» principle

# Sensitivity analysis

## Tornado chart



Source: Proposisjon til  
Stortinget: Utbygging  
og drift av Aasta  
Hansteen-feltet

Figur 2.3 Sensitivitetsanalyser

# Sensitivity analysis

## Spider plots

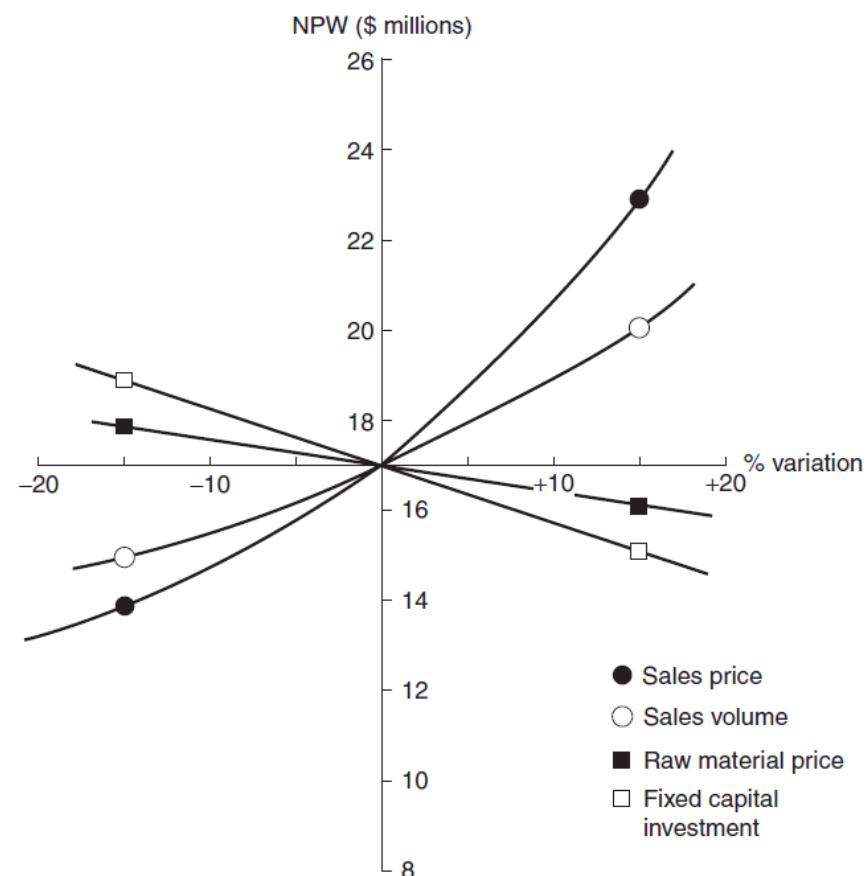


FIG. 9-14 Strauss plot.

## Sensitivity analysis - deficiencies

- There could be uncertainties that occur simultaneously
- Probability of occurrence?

# Field development goal

Find field design to maximize NPV

# Field development goal

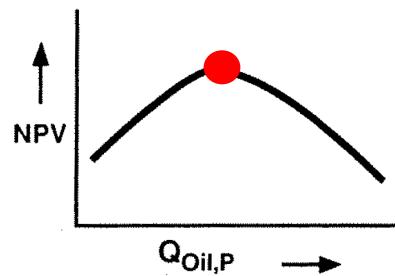
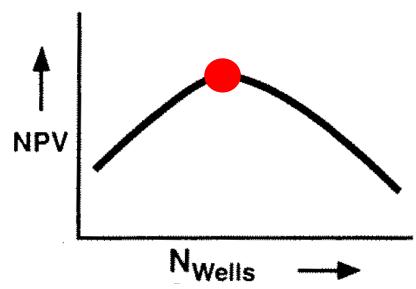
Find field design to maximize NPV

There is an optimal production scheduling and drilling schedule that maximize NPV

Action	Advantages	Disadvantages
Higher HC rates during early times	Gives higher revenue	Gives higher cost (CAPEX, OPEX)
Drill more wells	Allows for higher rates, extends field life	Gives higher cost (DRILLEX, CAPEX, OPEX)

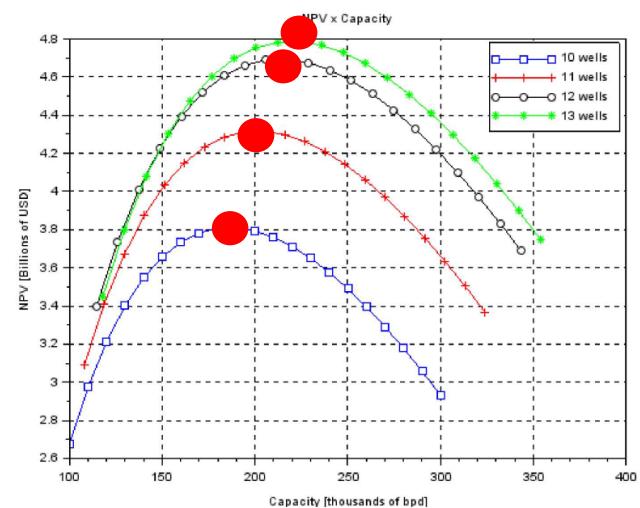


## Variation of NPV with plateau rate and number of wells:



**Choosing between rocks, hard places and a lot more: the economic interface**

Helge Hove Haldorsen

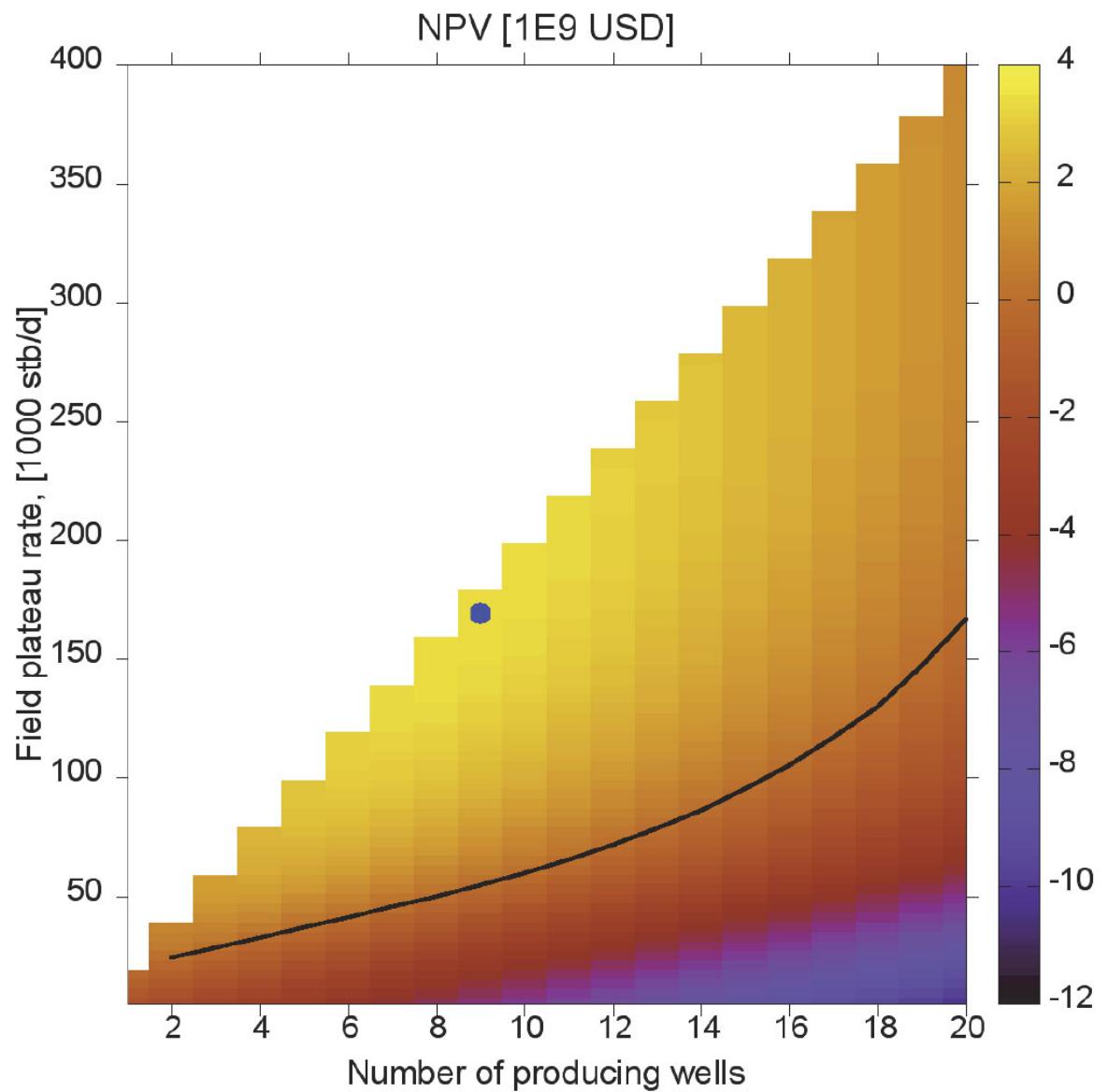


OTC-28898-MS

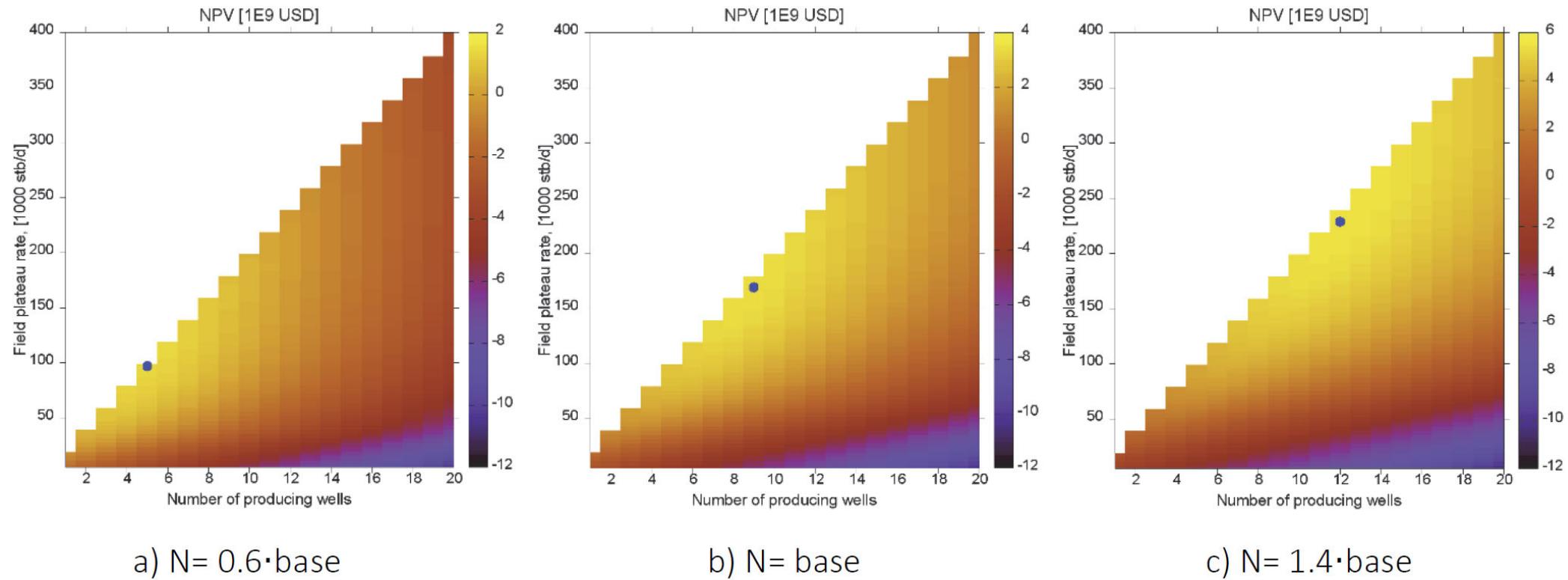
**A Cost Reduction Methodology for Offshore Projects**

G. C. Nunes, Rio Petroleo Consulting Group; A. H. da Silva and L. G. Esch, Universidade do Estado do Rio de Janeiro

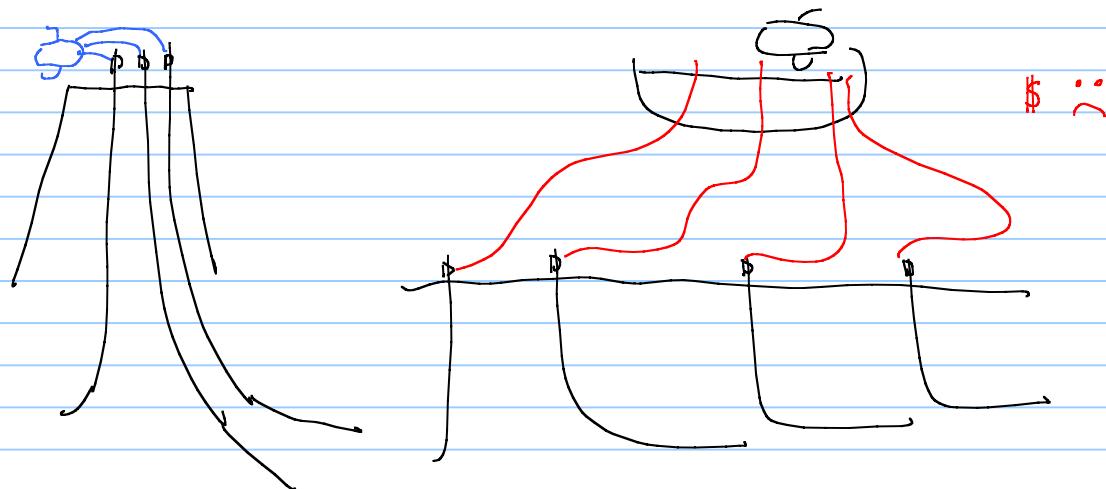
Example from Milan's  
Compendium section 5.2.3.

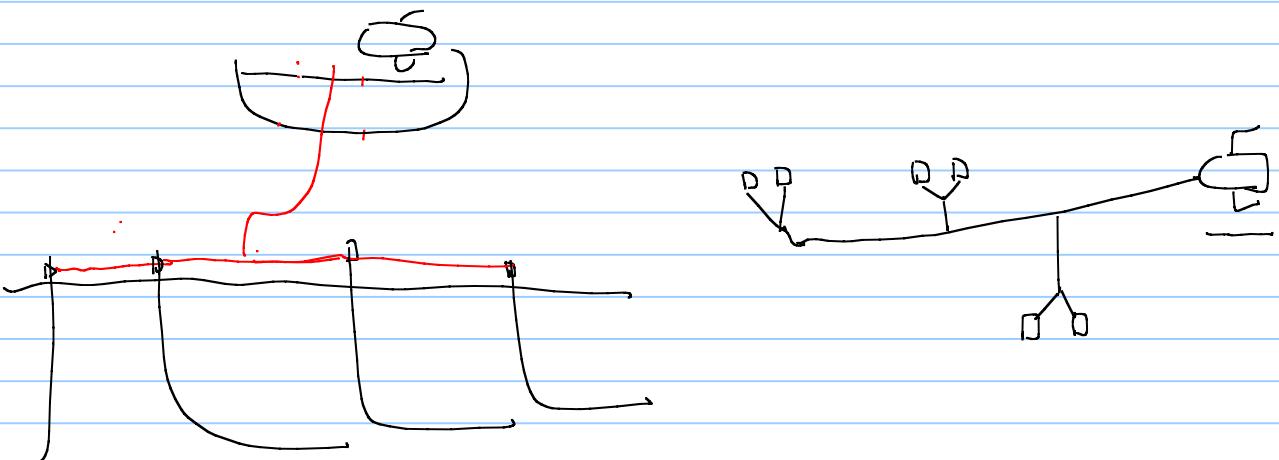


# Effect of uncertainties

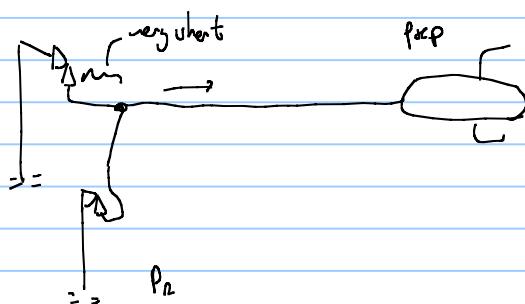


- Networks collection of pipes, flowline, pipeline, valves, pumps, take the fluids from wells to the processing facilities.





Example: 2 Oil gas well

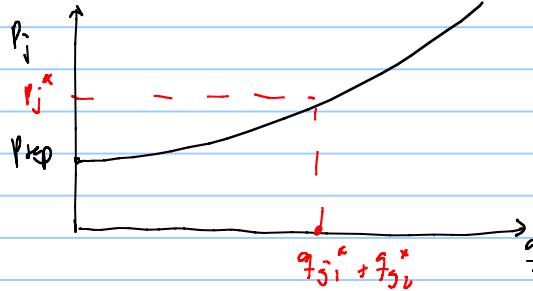
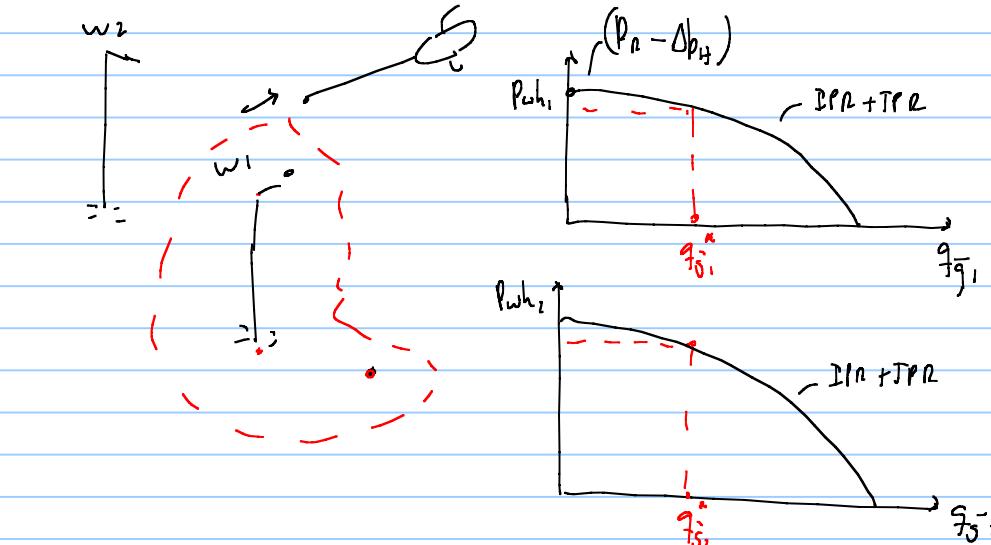
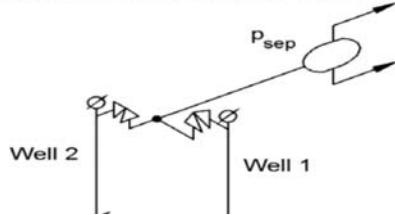


$$\text{open above} \quad \Delta p_{c_1} = 0 \quad \Delta p_{c_2} = 0$$

Equations	Nr equations	Nr unknowns
$\text{DP}, q_{\bar{j}_1} = C_{R_1} (P_{a_1}^2 - P_{w_{f_1}}^2)^{n_1}$ $q_{\bar{j}_2} = C_{R_2} (P_{a_2}^2 - P_{w_{f_2}}^2)^{n_2}$	2	4
$\text{TPR}, \bar{q}_{\bar{j}_1} = C_{T_1} \left( \frac{P_{w_{f_1}}}{e^{j_1}} - P_{w_{h_1}} \right)^{0.5}$ $\bar{q}_{\bar{j}_2} = C_{T_2} \left( \frac{P_{w_{f_2}}}{e^{j_2}} - P_{w_{h_2}} \right)^{0.5}$	2 [4]	2 [6]
$\text{PPR}, \bar{q}_{\bar{j}_1} + \bar{q}_{\bar{j}_2} = C_{P_1} (P_j^2 - P_{sep}^2)^{0.5}$	1 [5]	1 [7]
$\Delta p_{c_1} = 0 \quad P_{w_{h_1}} = P_j$	1 [6]	0 [7]
$\Delta p_{c_2} = 0 \quad P_{w_{h_2}} = P_j$	1 [7]	0 [7]

**PROBLEM 4 (18 POINTS). Network solving. (2017) exam**

Consider the gas field with two wells, a manifold a pipeline and a separator shown in the figure below. The wellhead of the wells are very close to the junction so it can be safely assumed that the wellhead pressure and junction pressure are equal when the choke is open.



approach nr. 1

1: assume  $q_{j1}^*, q_{j2}^*$

2: Read  $p_{wh_1}^*, p_{wh_2}^*, p_j^*$   
 $(wPR_1), (wPR_2), (PPR)$

3: Verify  $p_{wh_1}^* = p_{wh_2}^* = p_j^*$

not

$q_{j1}^*, q_{j2}^*$  are solution

approach nr. 2

1. assume  $p_j^* = p_{wh_1}^* = p_{wh_2}^*$

2. Read  $q_{j1}^* (wPR_1), q_{j2}^* (wPR_2),$   
 $q_{ppr}^* (PPR)$

3. Verify

$$q_{j1}^* + q_{j2}^* = q_{\text{pipeline}}^*$$

yes  
solution

not

1<sup>st</sup> iteration  $p_j = 50 \text{ bma}$

$$q_{j1}^* = 1.2 \times 10^6 \text{ Sm}^3/\text{d}$$

$$q_{j2}^* = 1.52 \times 10^6 \text{ Sm}^3/\text{d} + 2.37 \times 10^6 \text{ Sm}^3/\text{d} \quad \varepsilon = 0.92 \times 10^6 \text{ Sm}^3/\text{d}$$

$$q_{\text{pipeline}}^* = 1.8 \times 10^6 \text{ Sm}^3/\text{d} \quad 1.8 \times 10^6 \text{ Sm}^3/\text{d}$$

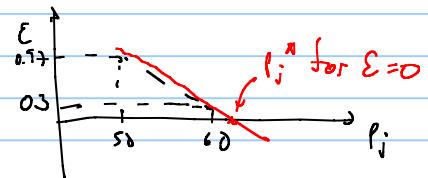
2<sup>nd</sup>

$$p_j = 60 \text{ bma}$$

$$q_{\text{pipeline}}^* = 2.3 \times 10^6 \text{ Sm}^3/\text{d} \quad 2.3 \times 10^6 \text{ Sm}^3/\text{d} \quad \varepsilon = 0.3 \times 10^6 \text{ Sm}^3/\text{d}$$

$$q_{j2}^* = 1.45 \times 10^6 \text{ Sm}^3/\text{d} + 2.60 \times 10^6 \text{ Sm}^3/\text{d}$$

$$q_{j1}^* = 1.15 \times 10^6 \text{ Sm}^3/\text{d}$$



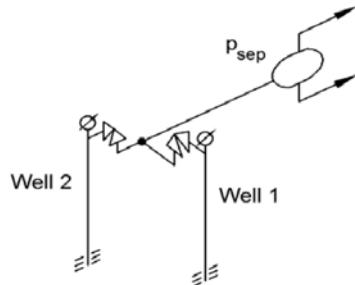
$$\frac{\varepsilon_1 - \varepsilon_2}{p_{j1} - p_{j2}} = \frac{\varepsilon_1 - 0}{l_{j1} - l_{j2}}$$

$$p_j^* = \sim$$

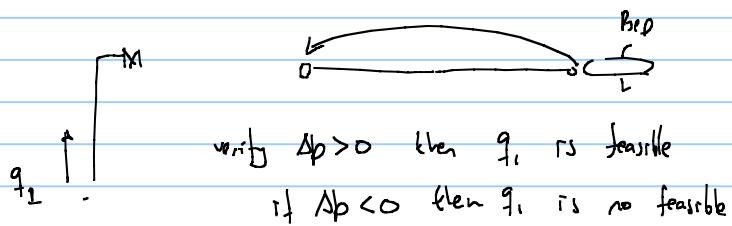
Exercise: using data from Problem 4 of the Exam 2017:

**PROBLEM 4 (18 POINTS). Network solving.**

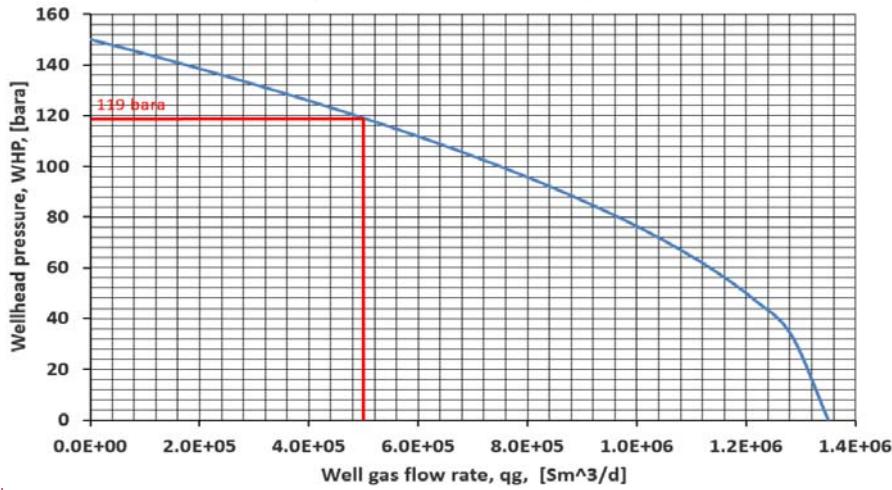
Consider the gas field with two wells, a manifold and a pipeline and a separator shown in the figure below. The wellhead of the wells are very close to the junction so it can be safely assumed that the wellhead pressure and junction pressure are equal when the choke is open.



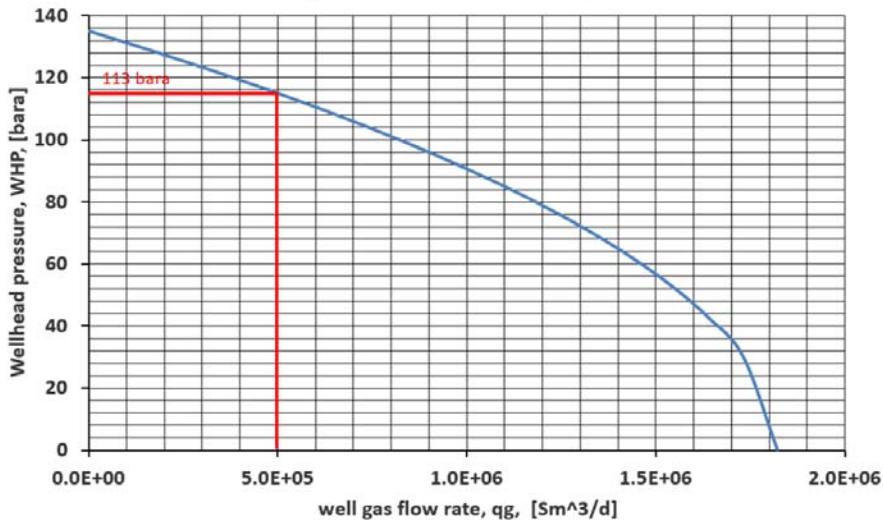
Will it be possible to produce  $0.5 \times 10^6 \text{ Sm}^3/\text{d}$  from each well? If so, what is the choke  $\Delta p$  required in each well?

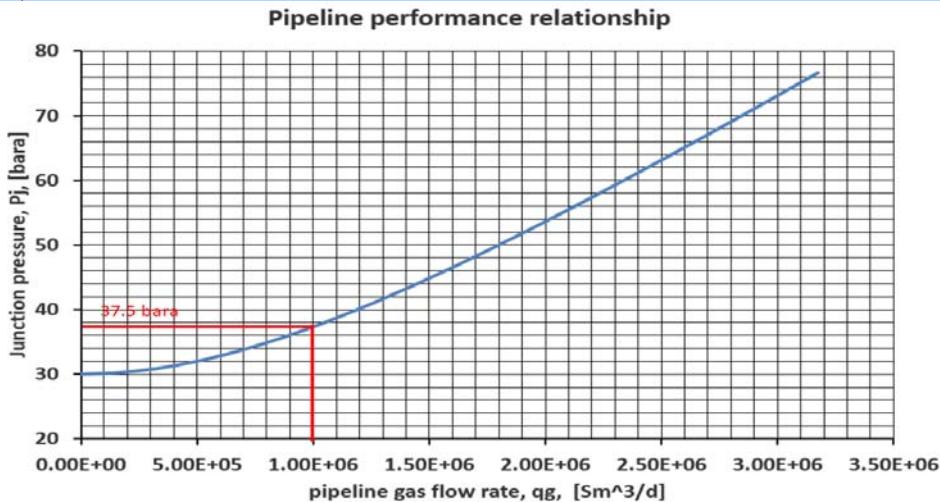


wellhead performance relationship - Well 1



wellhead performance relationship - Well 2

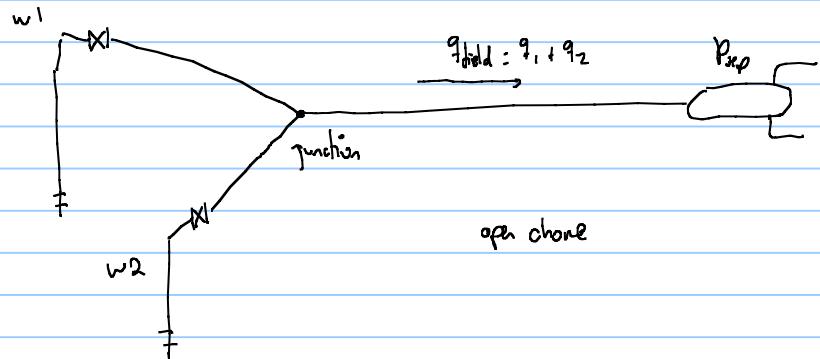




$$\Delta p_{\text{choke}1} = 119 - 37.5 = 81.5 \text{ bara}$$
$$\Delta p_{\text{choke}2} = 113 - 37.5 = 75.5 \text{ bara}$$

Yes, it is possible to produce  $0.5 \times 10^6 \text{ Sm}^3/\text{d}$  from well 1 and 2.

Exercise on Dry gas network using Excel



we have to assume either  $\bar{q}_1, \bar{q}_2$

$$\dot{q} = C_d (\bar{P}_f^2 - \bar{P}_{w_f}^2)^n$$

OR:  $P_{w1}, P_{w2} \leftarrow P_{w_f} < P_f$

↳ we prefer to assume  
P<sub>wf</sub> because I know the  
upper bound

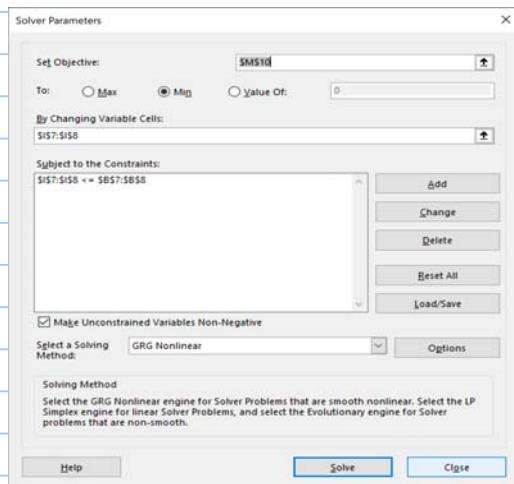
$$\bar{P}_{w_f} = \sqrt{\bar{P}_f^2 - \left(\frac{\dot{q}}{C_d}\right)^{\frac{1}{n}}}$$

i don't know  $P_{max}$ , and  
can give problems to eq.

objective variable:

$$(\bar{P}_{j_{av}} - \bar{P}_{j_1})^2 + (\bar{P}_{j_{av}} - \bar{P}_{j_2})^2 + (\bar{P}_{j_{av}} - \bar{P}_{j_{exp}})^2$$

Component Name	IPR			Tubing		Flowline			psep	pwf	qwell	pwh	pjunc	error
	p <sub>R</sub> [bara]	C [Sm <sup>3</sup> /bar <sup>2</sup> n]	n	S	C <sub>t</sub> [Sm <sup>3</sup> /bar <sup>2</sup> ]	C <sub>f1</sub> [Sm <sup>3</sup> /bar <sup>2</sup> ]	[bara]	[bara]						
W_1	120		52	0.8	0.13	7680	8673	38	1.02E+05	33	31	1E-01		
W_2	120		40	0.75	0.11	8600	7563	34	4.95E+04	31	31	9E-1		
Pipeline						14080	28.6		1.51E+05				31	2E-01
								Average=		31		4E-01		



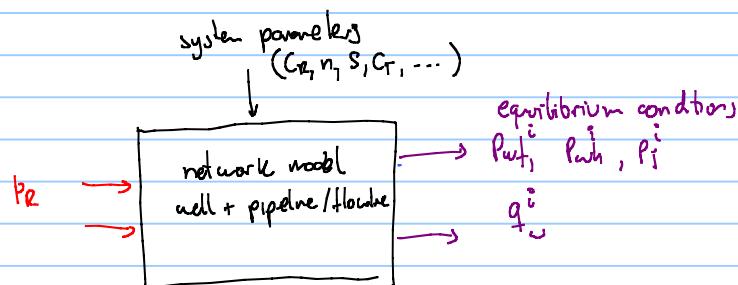
If solver is not available

Activate solver → excel menu → options

↓  
Add-in

↓  
go

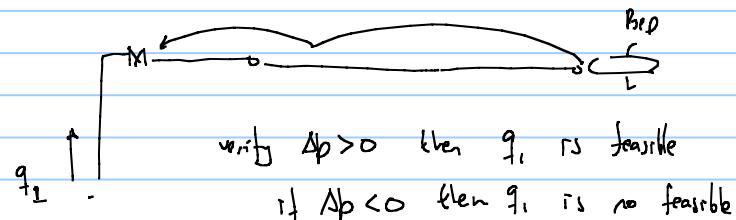
↓  
tick on "solver"  
or "problem solver"



solving the network  
with above

- Option 1, fixing rates

(option usually not available in  
commercial software)



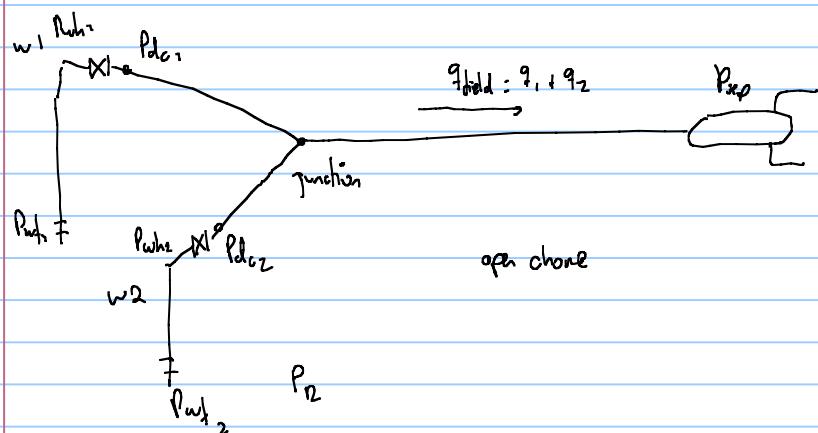
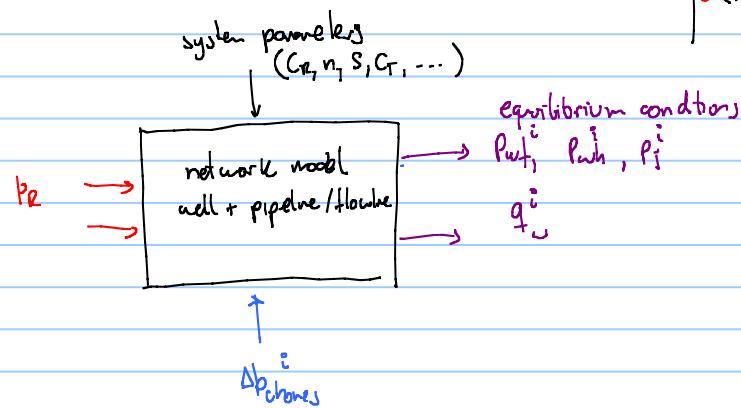
for example, it is desirable to

$$\left\{ \begin{array}{l} q_1 = 80000 \text{ Sm}^3/\text{d} \\ q_2 = 40000 \text{ Sm}^3/\text{d} \end{array} \right.$$

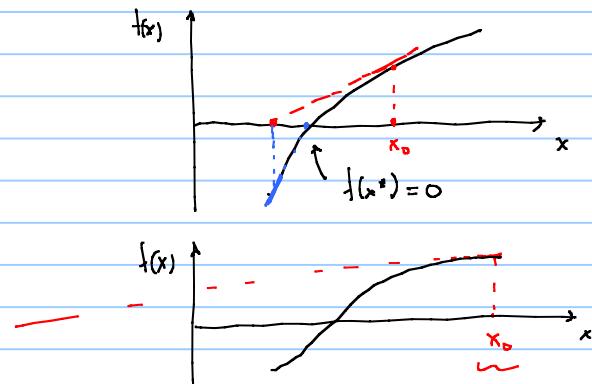
Component Name	IPR		Tubing		Flowline		psep	pwf	qwell	pwh	dpchoke	pdc	pjunc	
	p <sub>r</sub> [bara]	C [Sm <sup>3</sup> /bar <sup>2</sup> n]	n	S	C <sub>t</sub> [Sm <sup>3</sup> /bar <sup>2</sup> ]	Cfl [Sm <sup>3</sup> /bar <sup>2</sup> ]								
W_1	120		52	0.8	0.13	7680	8673		69	8.00E+04	64	33	31	30
W_2	120		40	0.75	0.11	8600	7563		66	4.00E+04	63	32	30	30
Pipeline						14080	28.6			1.20E+05				

- Option 2 : include the choke "model"  $\rightarrow$  2 options

$\bullet \Delta p_{\text{choke}}$  this option will be discussed next  
 $\bullet \text{choke opening}$   $\Delta p_{\text{choke}} = f(q_3, \text{Opening}) - p_1$



IPR			Tubing			Flowline			psep	pwf	qwell	pwh	dpchoke	pdc	pjunc	error
p <sub>R</sub>	C	n	S	C <sub>t</sub>	C <sub>f</sub>	[bara]	[bara]	[bara]	[bar]	[bar]	[bar]	[bar]	[bar]	[bar]	(bara <sup>2</sup> )	
120	52	0.8	0.13	7680	8673		42	9.92E+04	38	5	33	30	3E-10			
120	40	0.75	0.11	8600	7563		39	4.84E+04	36	5	31	30	1E-09			
				14080	28.6			1.48E+05				30	3E-09			
						Average=						30	4E-09			

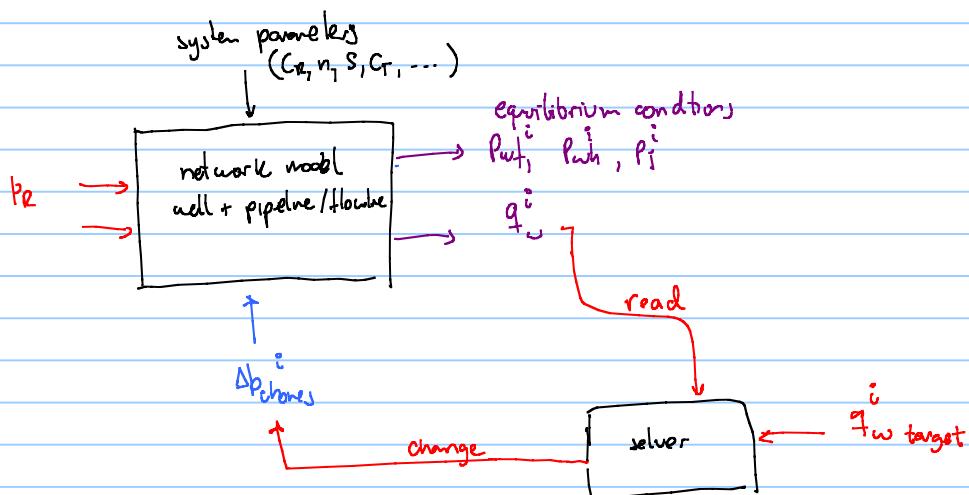


-- step 1  
--- step 2

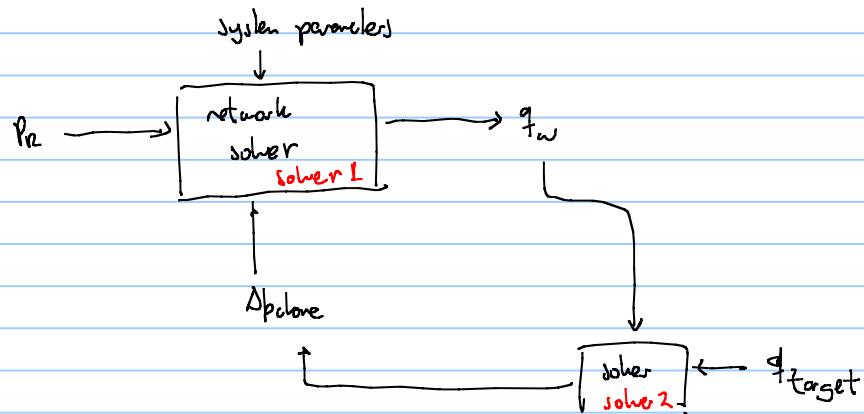
for derivative-based solver  
it is necessary to give a good  
initial seed

IPR			Tubing			Flowline			psep	pwf	qwell	pwh	dpchoke	pdc	pjunc	error
p <sub>R</sub>	C	n	S	C <sub>t</sub>	C <sub>f</sub>	[bara]	[bara]	[bara]	[bar]	[bar]	[bar]	[bar]	[bar]	[bar]	(bara <sup>2</sup> )	
120	52	0.8	0.13	7680	8673		57	9.01E+04	52	20	32	30	1E-09			
120	40	0.75	0.11	8600	7563		54	4.44E+04	51	20	31	30	8E-10			
				14080	28.6			1.35E+05				30	4E-09			
						Average=						30	6E-09			

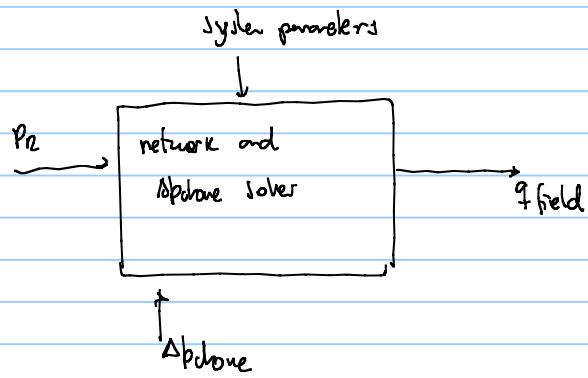
- How to use this model to find  $\Delta p_{\text{above}}$  such that  $q_1 = 80000 \text{ m}^3/\text{d}$   
 $q_2 = 90000 \text{ m}^3/\text{d}$



in excel it is not possible to have two levels of solver



"Merging the two solvers"



objective variable :

$$(P_{j\text{av}} - P_{j_1})^2 + (P_{j\text{av}} - P_{j_2})^2 + (P_{j\text{av}} - P_{j\text{sep}})^2$$

variables

changing  $P_{j_1}$   
 $P_{j_2}$

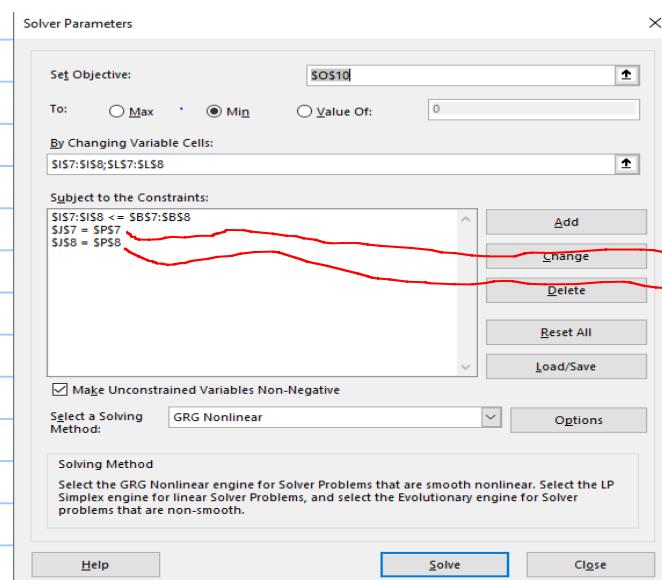
$\Delta p_{\text{choker 1}}$

$\Delta p_{\text{choker 2}}$

constraints

$$q_1 = q_{1\text{target}}$$

$$q_2 = q_{2\text{target}}$$



	IPR		Tubing		Flowline		psep	pwf	qwell	pwh	dpchoke	pdc	pjunc	error	qtarget
	P <sub>n</sub> [bara]	C [Sm <sup>3</sup> /bar <sup>2</sup> n]	n	S	C <sub>t</sub> [Sm <sup>3</sup> /bar <sup>2</sup> ]	C <sub>f1</sub> [Sm <sup>3</sup> /bar <sup>2</sup> ]									
120	52	0.8	0.13		7680	8673	69	8.00E+04	64	33	31	30	9E-11	80000	
120	40	0.75	0.11		8600	7563	87	3.00E+04	82	52	30	30	5E-11	30000	
					14080	28.6		1.10E+05						30	7E-12
									Average=					30	2E-10

**20240222**

**Outline:**

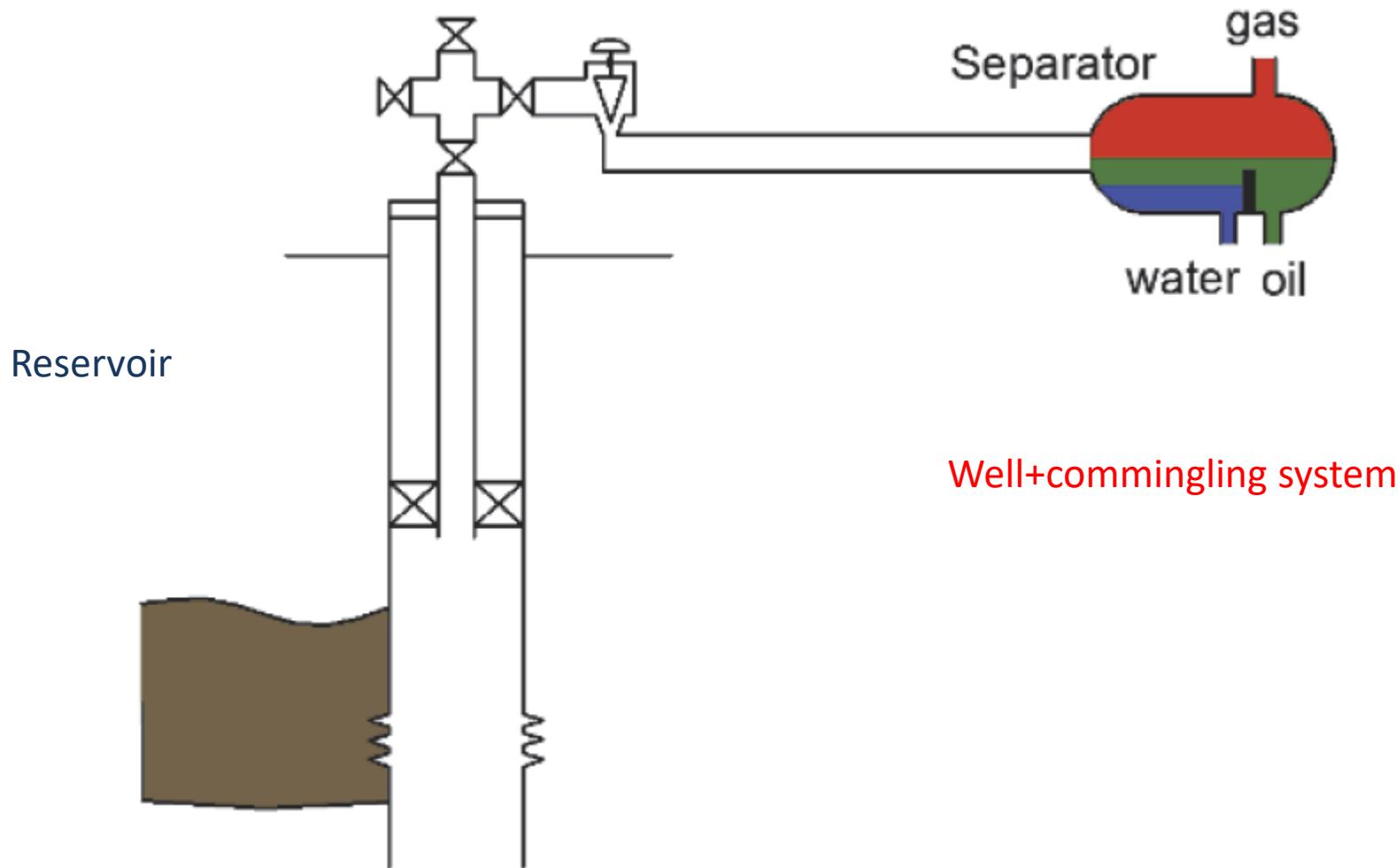
- re-cap network solving**
- approaches to generate production profiles**



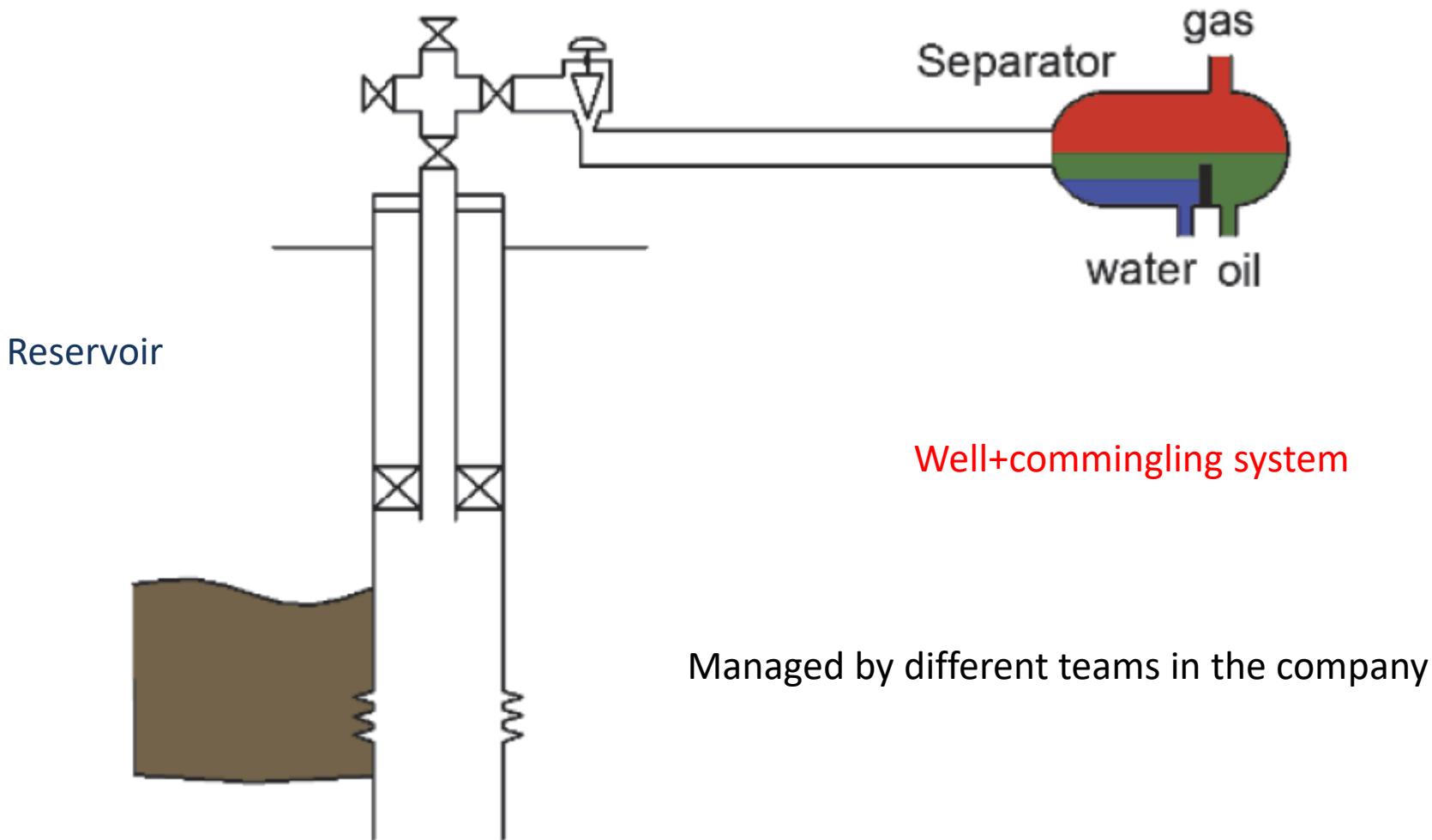
**NTNU – Trondheim**  
Norwegian University of  
Science and Technology

# **Approaches to generate production profiles**

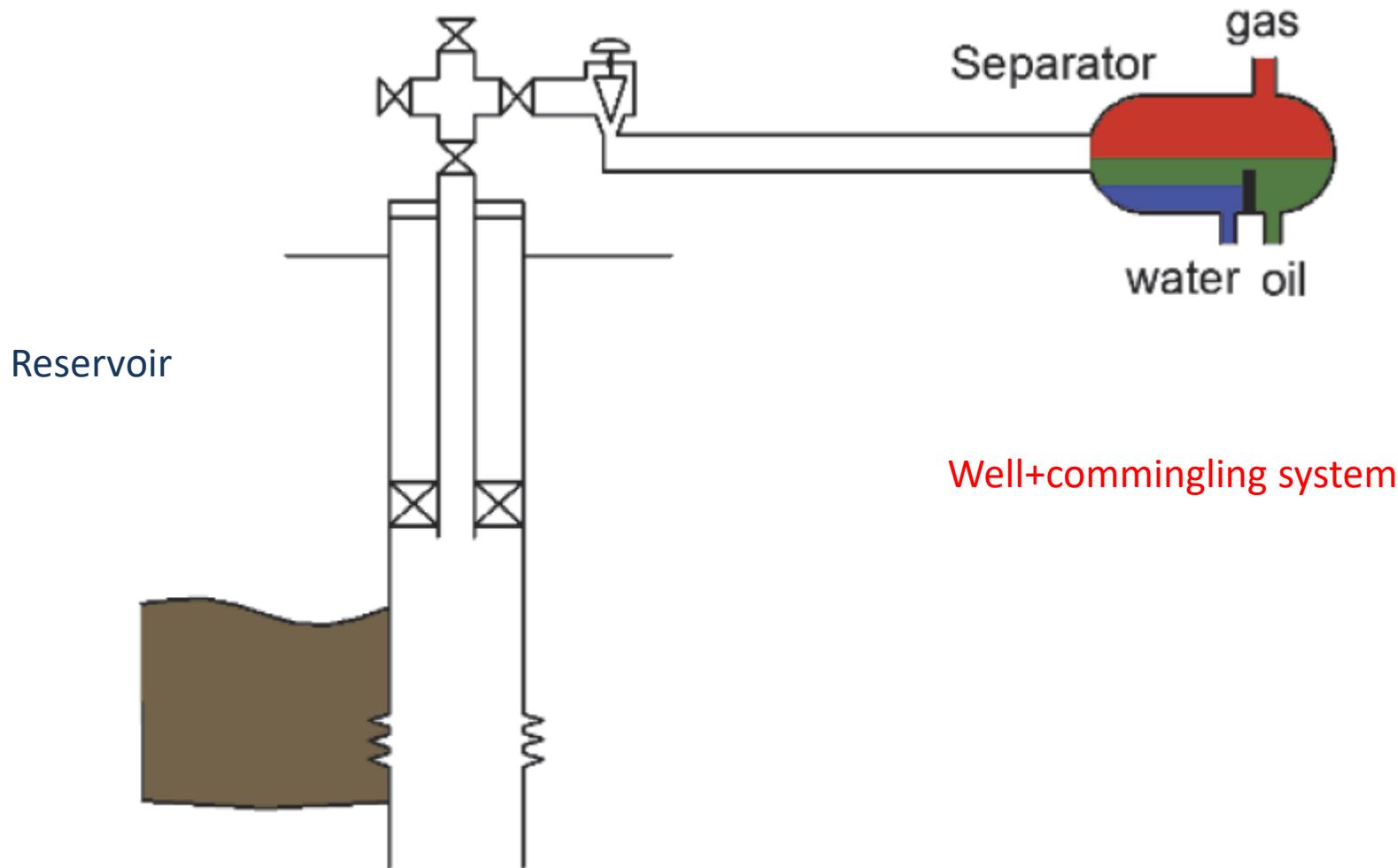
# Virtual field



# Virtual field



# Virtual field



# **Alternatives to generate production profiles**

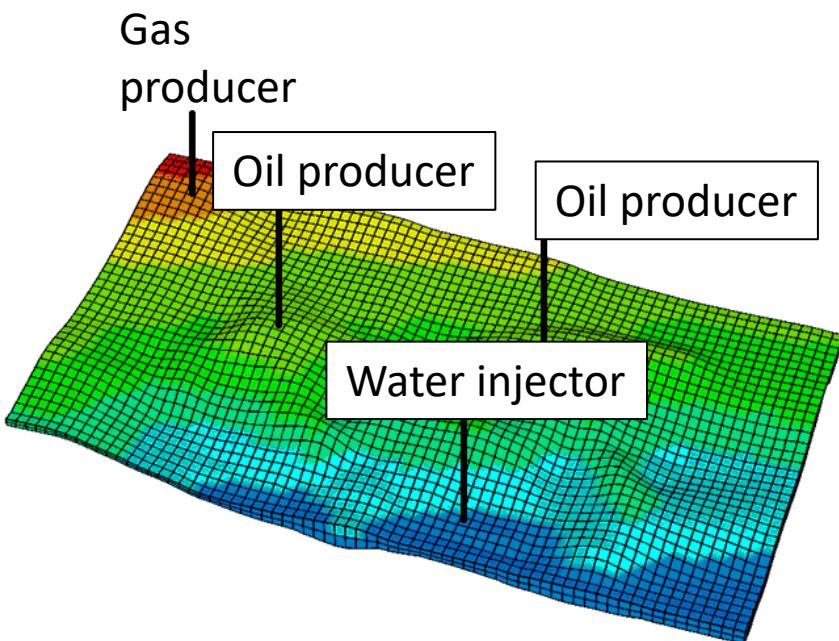
- Reservoir only
- Reservoir + network (coupled)

# Reservoir model

## Reservoir modeling alternatives

- Material balance + IPR equation (what we did in the Snowwhite exercise)
- Decline (type) curves – assuming a trend of qfield versus time (e.g. exponential)
- Reservoir simulation

# Reservoir model



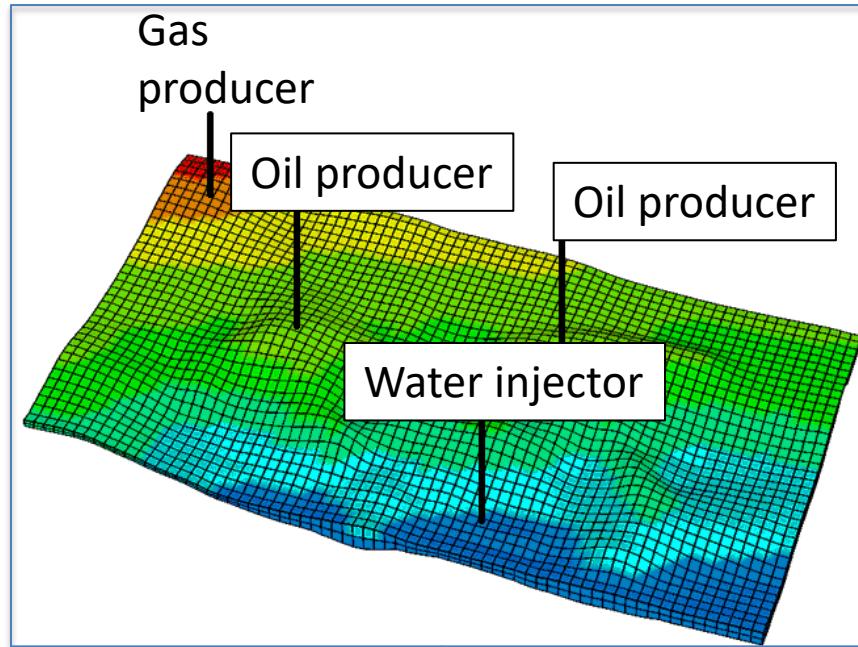
- 3D computer representation of a petroleum reservoir
- Computes the **variation** of the pressures, saturations and other properties **with time** when fluids are retrieved from or injected into the domain
- Captures the flow in porous media in the reservoir, thermal effects, thermodynamic flashing

# Reservoir model

**Boundary conditions (t):**

- Well target rate  $q_w(t)$  and  $p_{wf\ min}(t)$

**INPUT**



**OUTPUT**

- Boundary properties  $p_{wf}(t)$ ,  $q_w(t)$
- Block variables (t)
- Well variables (t)

**INPUT**

- Reservoir / system properties (Porosity, saturations, permeability, EOS, fluid composition, reservoir temperature, initial reservoir pressure)
- Well locations
- **Well status (t)**

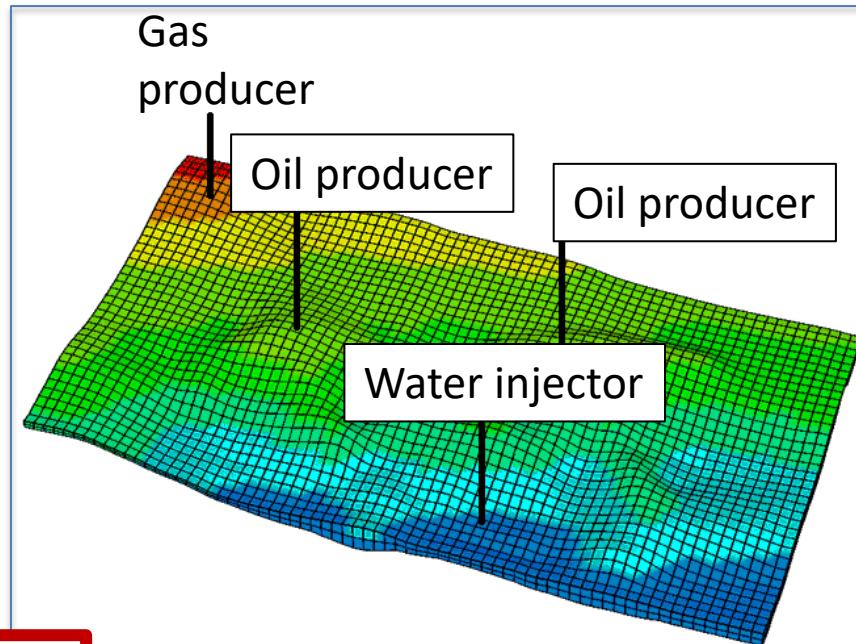
Usually variables constant for the whole simulation time or on-off (no regulation)

# Reservoir model

**Boundary conditions (t):**

- Well target rate  $q_w(t)$  and  $p_{wf\ min}(t)$

**INPUT**



A GOOD GUESS(ES) FOR  
 $p_{wf\ min}$  is required!!

**INPUT**

- Reservoir / system properties (Porosity, saturations, permeability, EOS, fluid composition, reservoir temperature, initial reservoir pressure)
- Well locations
- **Well status (t)**

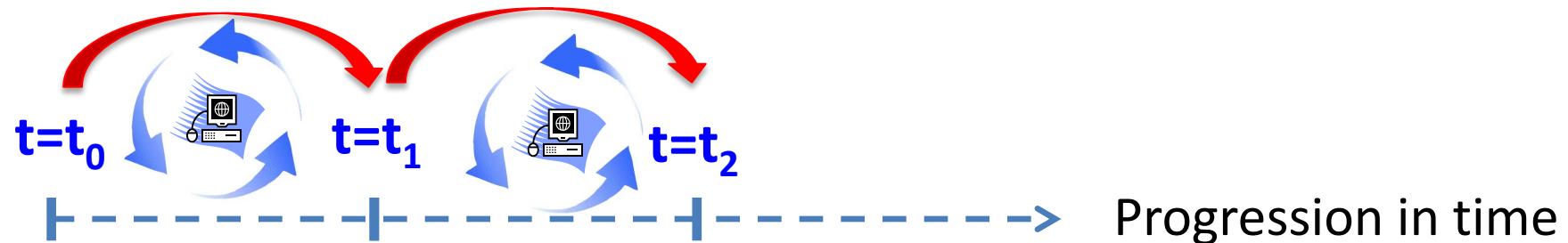
**OUTPUT**

- Boundary properties  $p_{wf}(t)$ ,  $q_w(t)$
- Block variables (t)
- Well variables (t)

Usually variables constant for the whole simulation time or on-off (no regulation)

# Operating mode

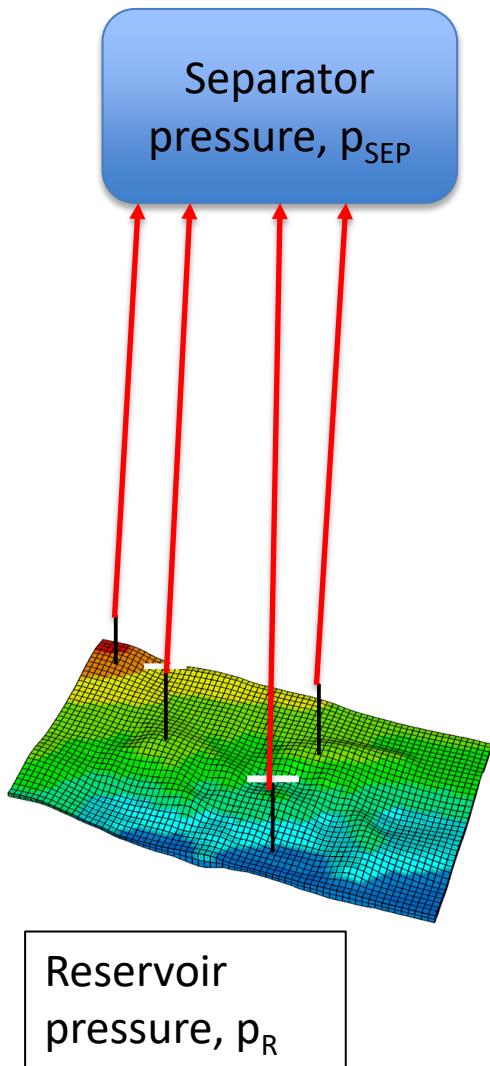
## Reservoir model



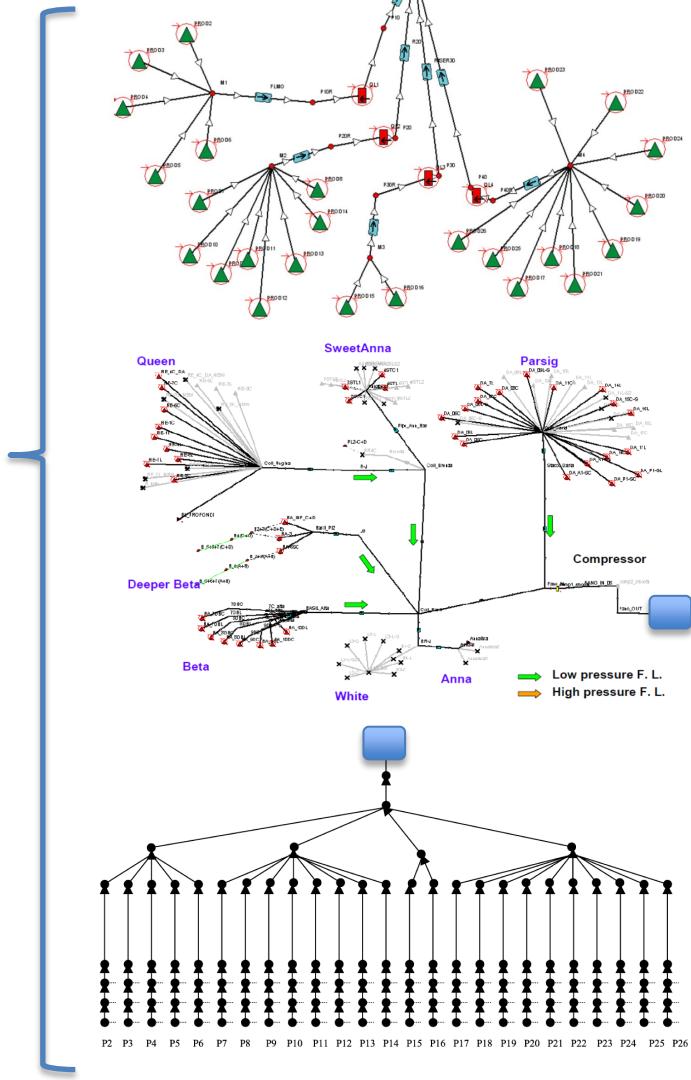
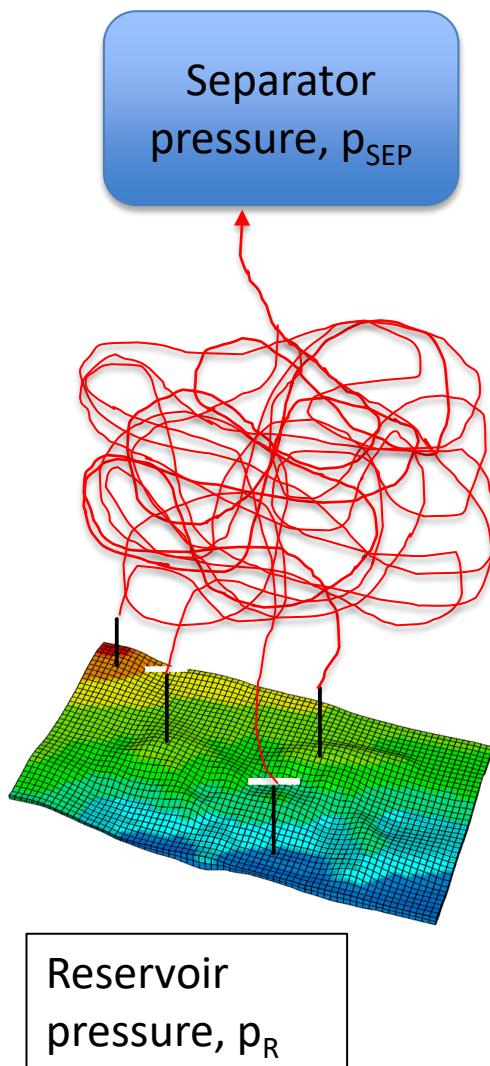
# Input file - Example

# Network model

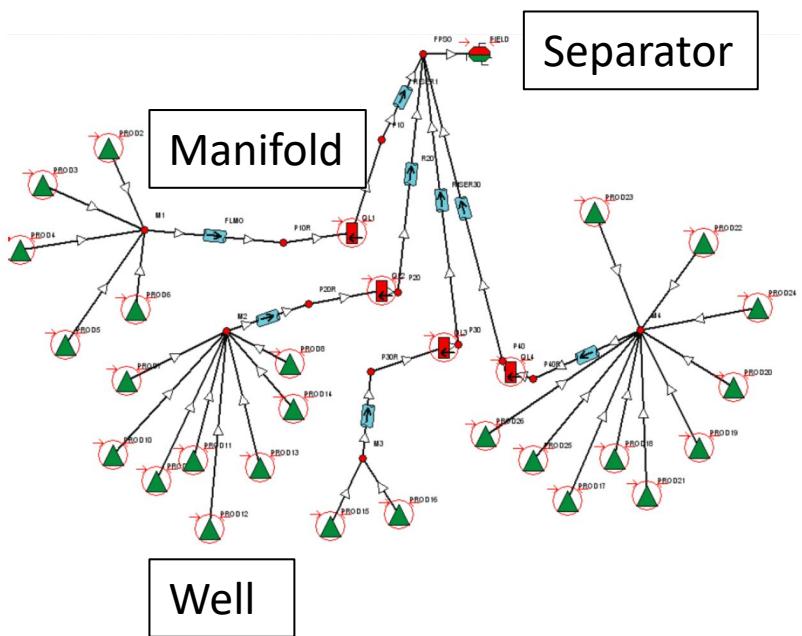
# Network model characteristics



VS.



# Network model

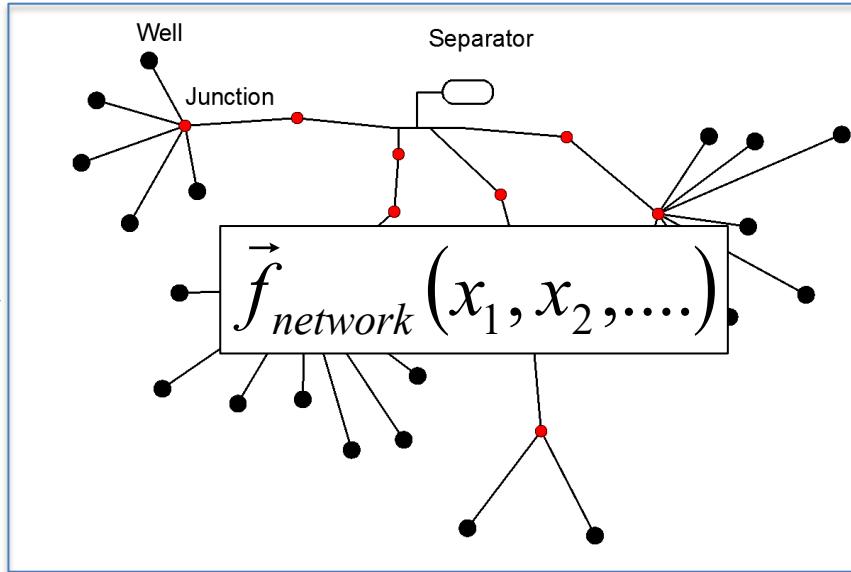


- Steady state (for a given condition in time), 1D Computer representation of a petroleum production network (wells, pipelines, equipment)
- Computes the pressure and temperature profiles in each flowline, the flow rate of each well, the conditions upstream and downstream of equipment
- Captures the single phase/multiphase flow along the production system, from the wells until the processing facilities

# Network model – v1

**Boundary conditions  
for injectors or  
producers:**  
-Well Inflow  
performance  
relationship (IPR)

INPUT



OUTPUT

- Well flow rates
- Pressure and temperature along the system

- System Properties (pipe dimensions, layout, fluid composition, EOS, separator pressure, ambient temperature)
- **Adjustable variables:** choke opening, well routing, Inflow control valves, gas lift injection rate, diluent injection rate, pump frequency, compressor.

These usually vary during the life of the field.

# Network model – v1 variation (requires an “optimizer”)

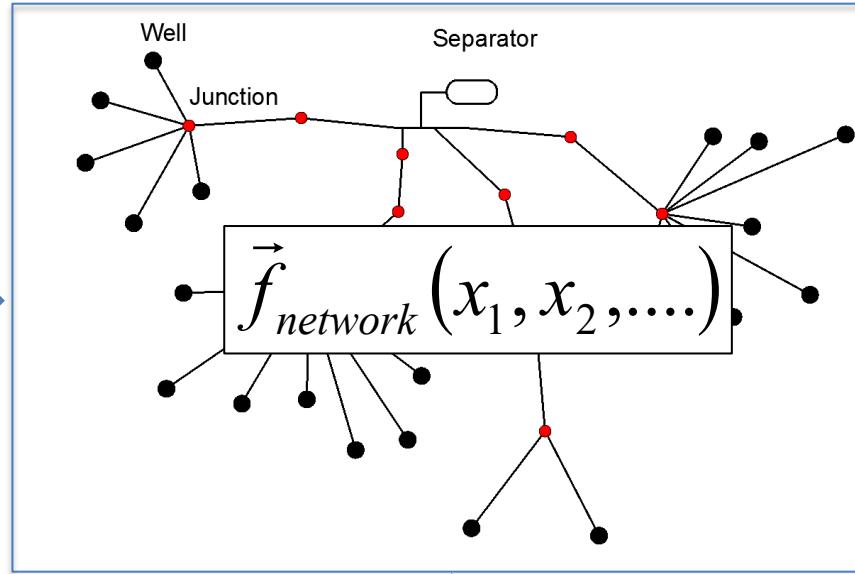
**Boundary conditions for injectors or producers:**

- Well Inflow performance relationship (IPR)

**Desired well rates**

- Adjustable variables will be changed to achieve well rates

**INPUT**



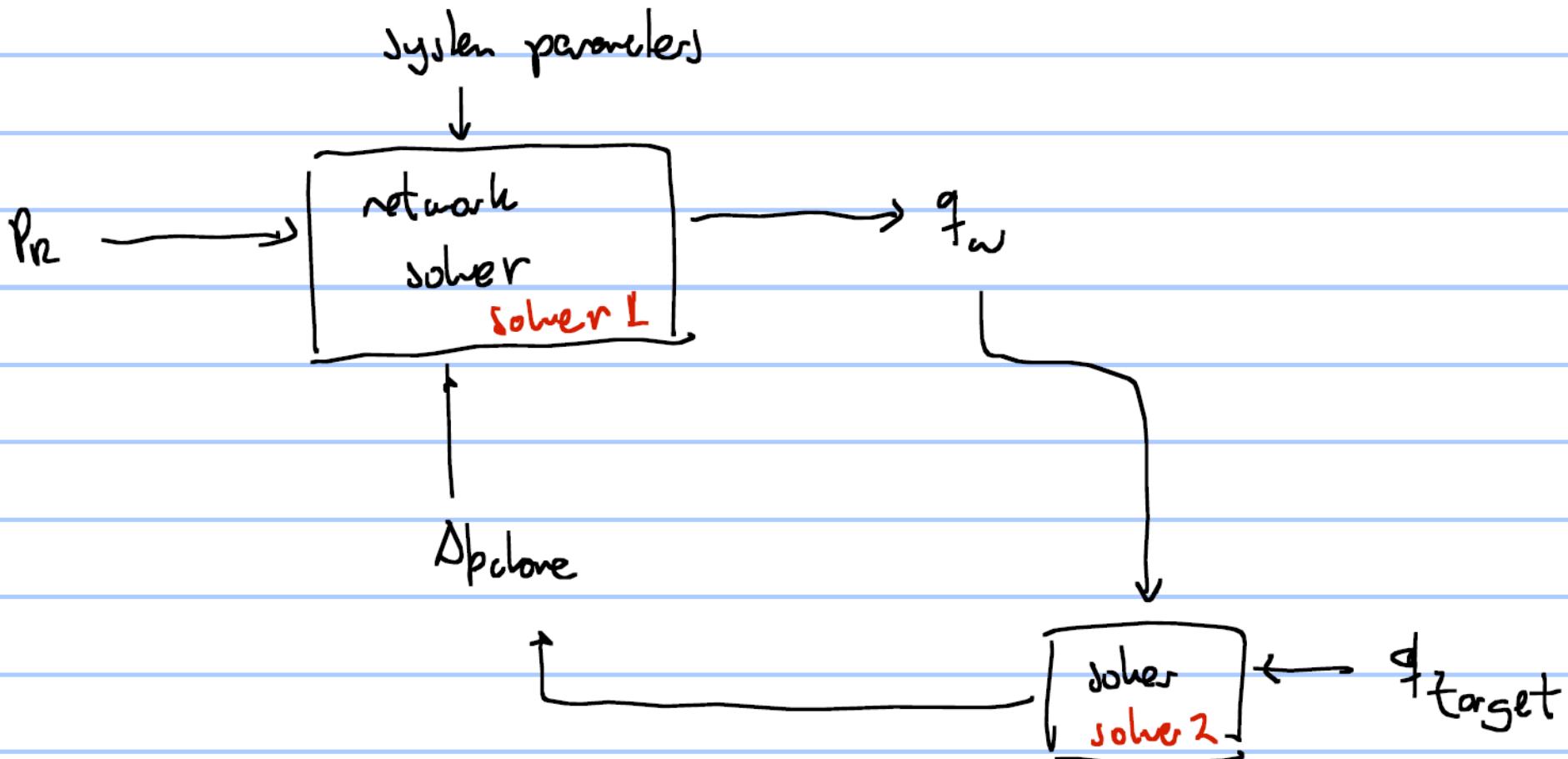
**OUTPUT**

- Well flow rates
- Pressure and temperature along the system

- System Properties (pipe dimensions, layout, fluid composition, EOS, separator pressure, ambient temperature)
- **Adjustable variables:** choke opening, well routing, Inflow control valves, gas lift injection rate, diluent injection rate, pump frequency, compressor.

These usually vary during the life of the field.

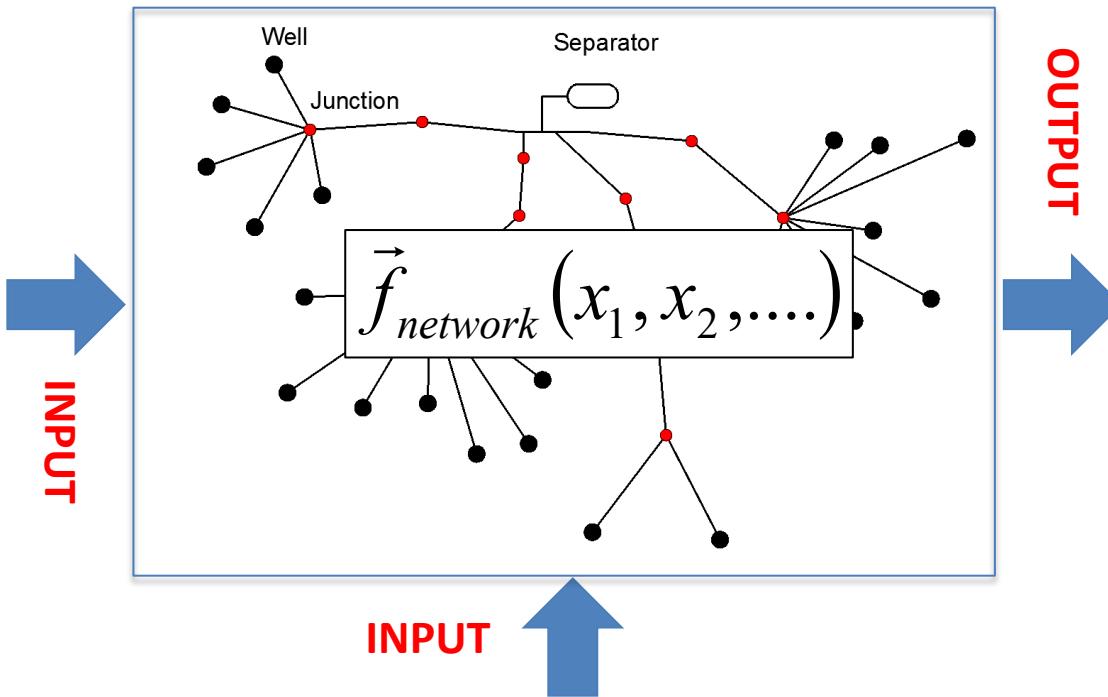
# Network model – v1 variation (requires an “optimizer”)



# Network model – v2

Boundary conditions for injectors or producers:

Desired well rates



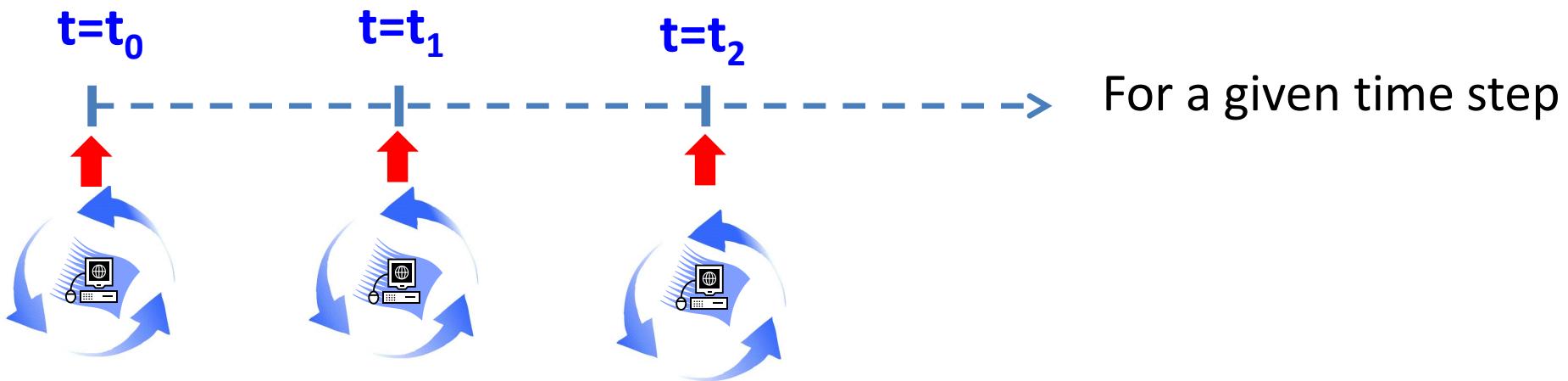
- Pressure and temperature along the system
- Pressure at the boundaries

- System Properties (pipe dimensions, layout, fluid composition, EOS, separator pressure, ambient temperature)
- **Adjustable variables:** choke opening, well routing, Inflow control valves, gas lift injection rate, diluent injection rate, pump frequency, compressor.

These usually vary during the life of the field.

# Operating mode

## Network model



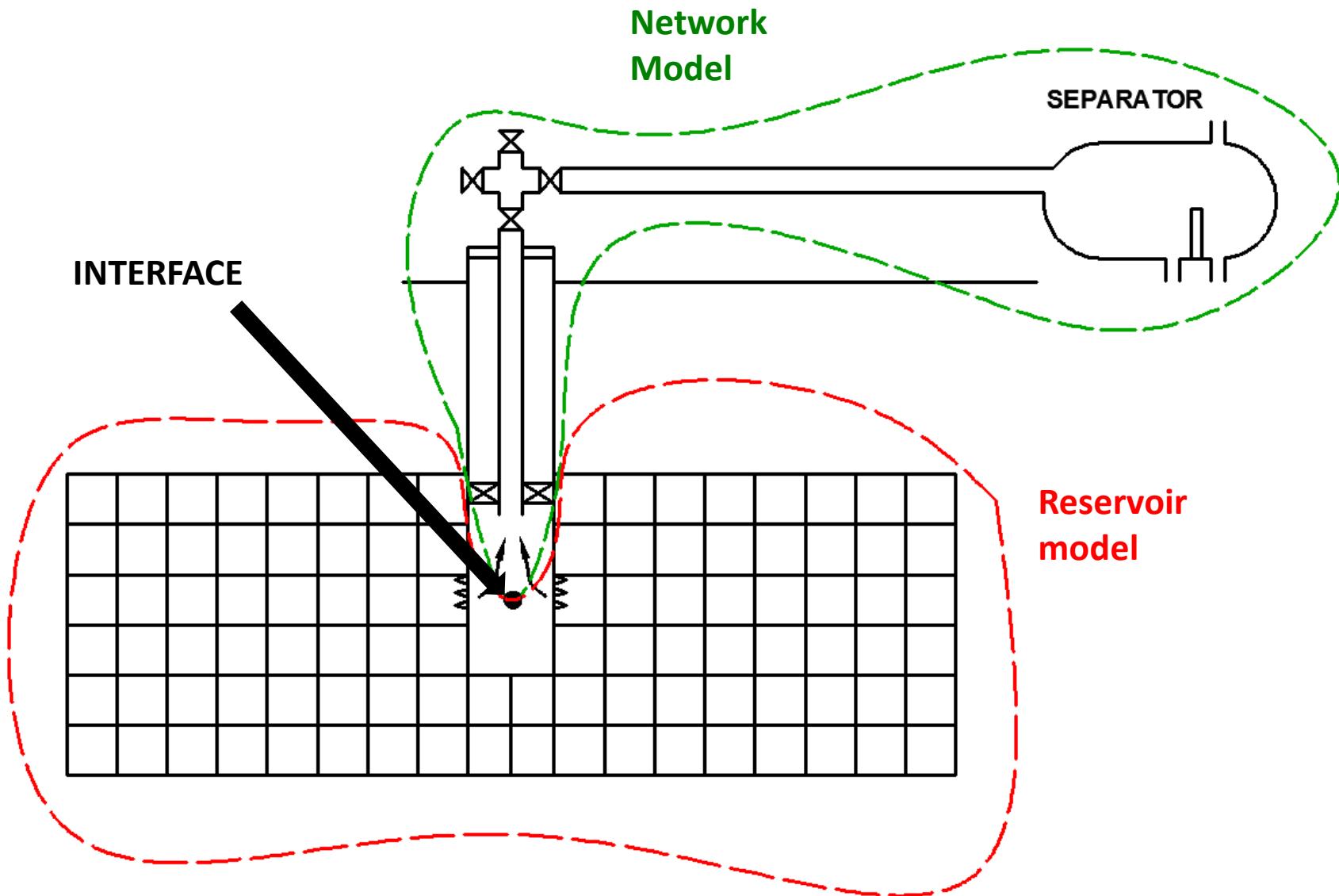
## Coupling:

Connecting reservoir and network model to achieve consistency at the interface.

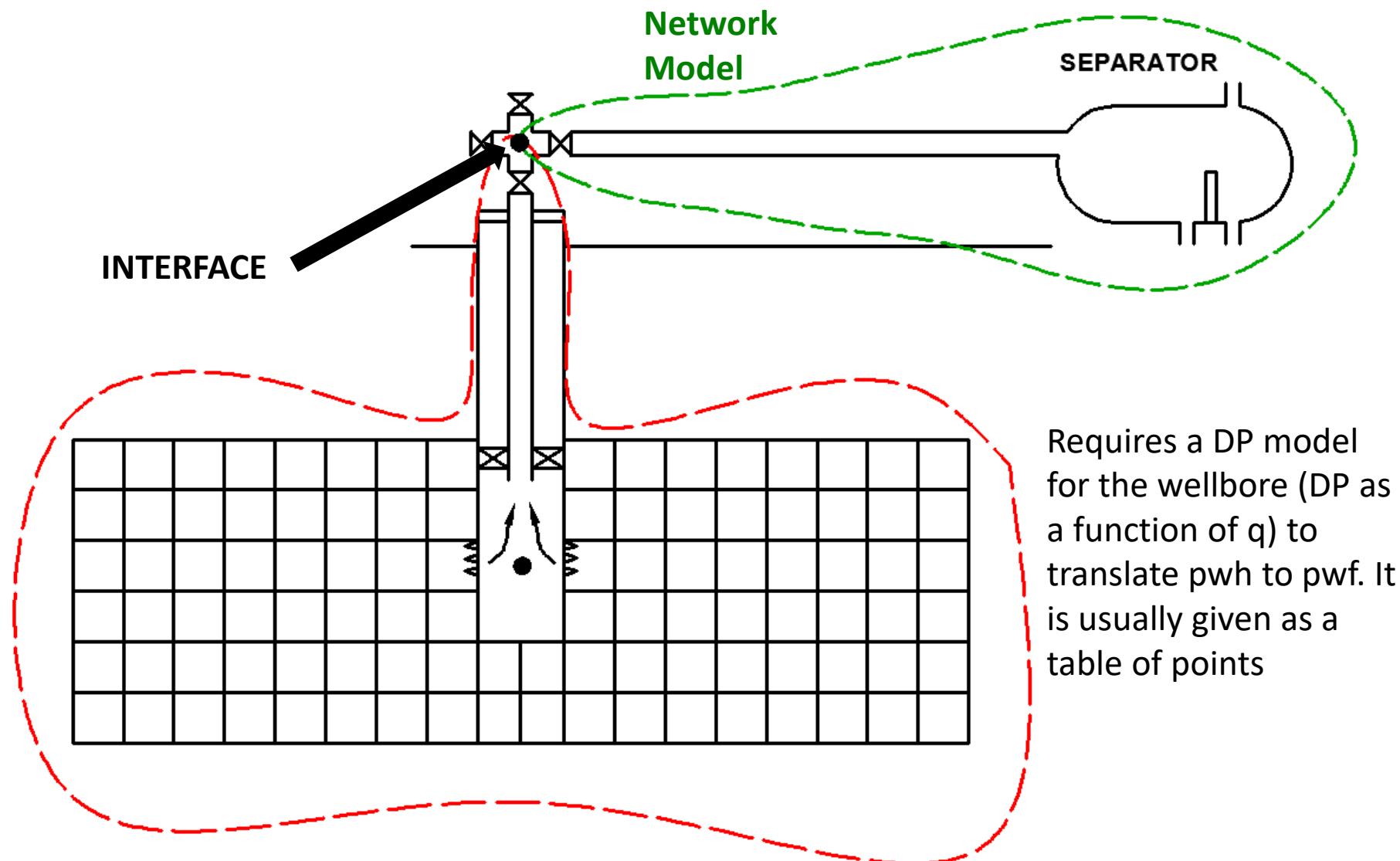
Or, equivalently:

- Will I be able to produce the reservoir rates through the well and network?
- Find realistic values for  $p_{wfmin}$

# Model's Interface: well's bottomhole



# Model's Interface: wellhead



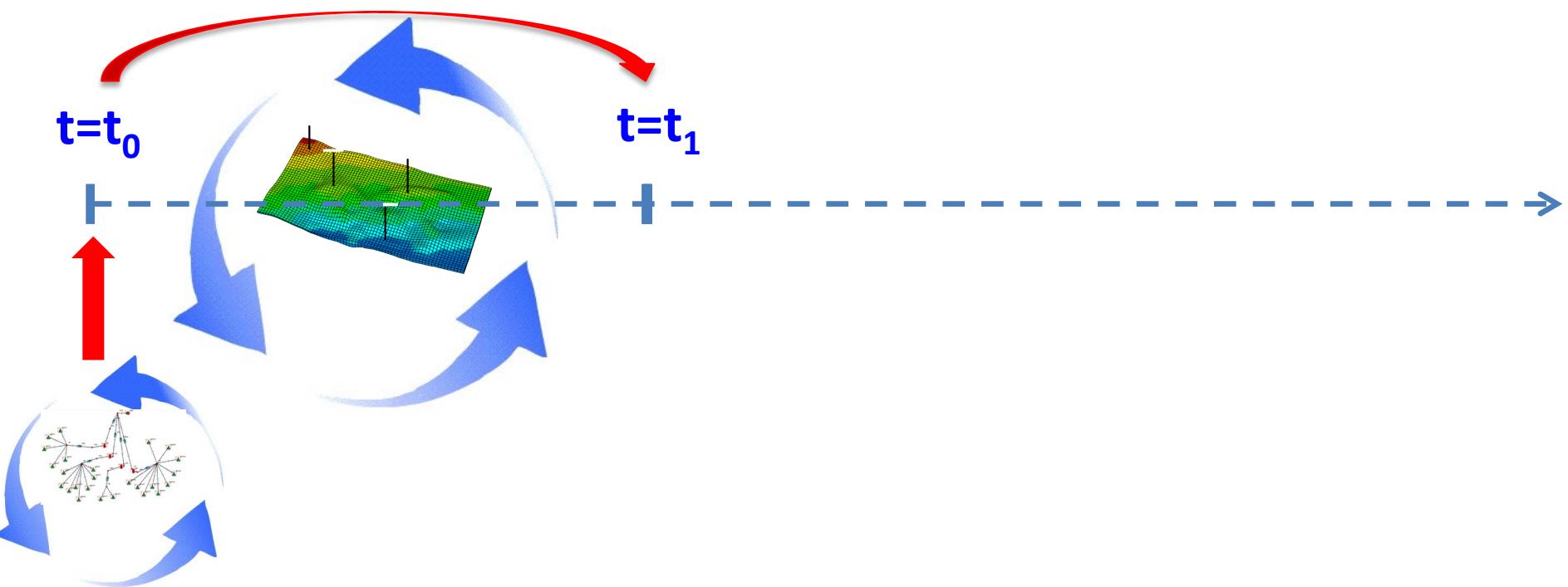
# Integration strategies

- **Explicit**



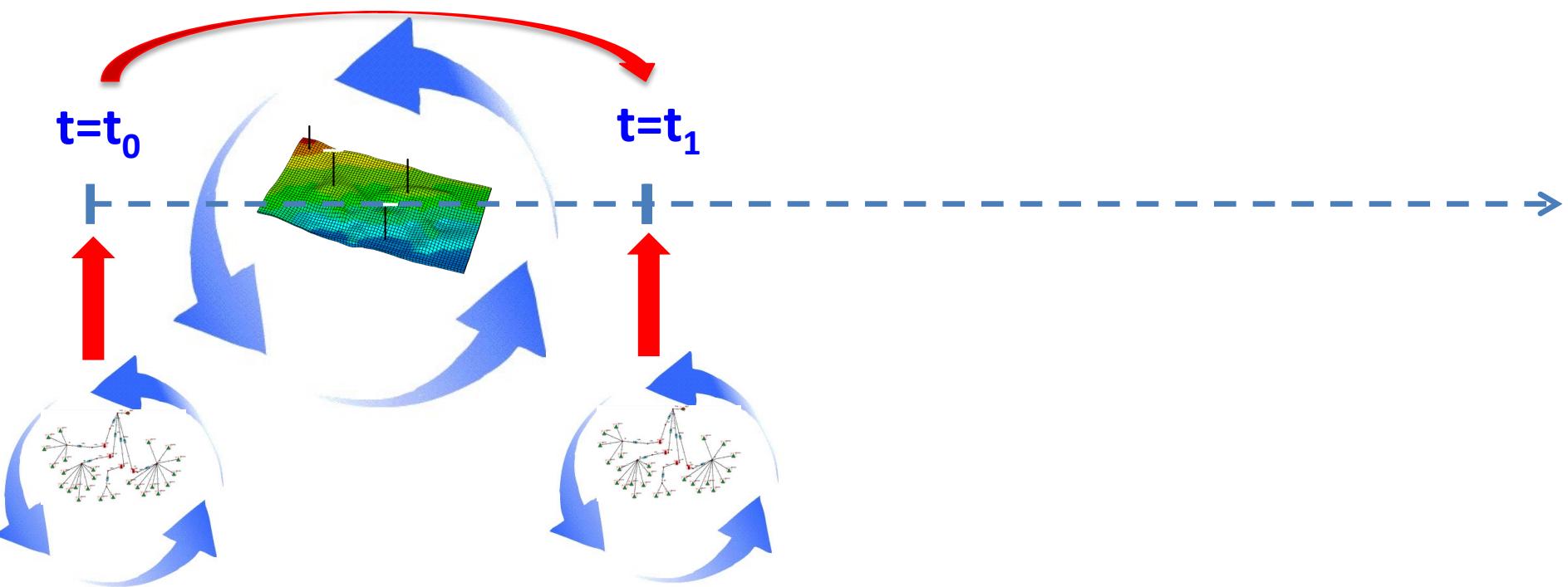
# Integration strategies

- Explicit



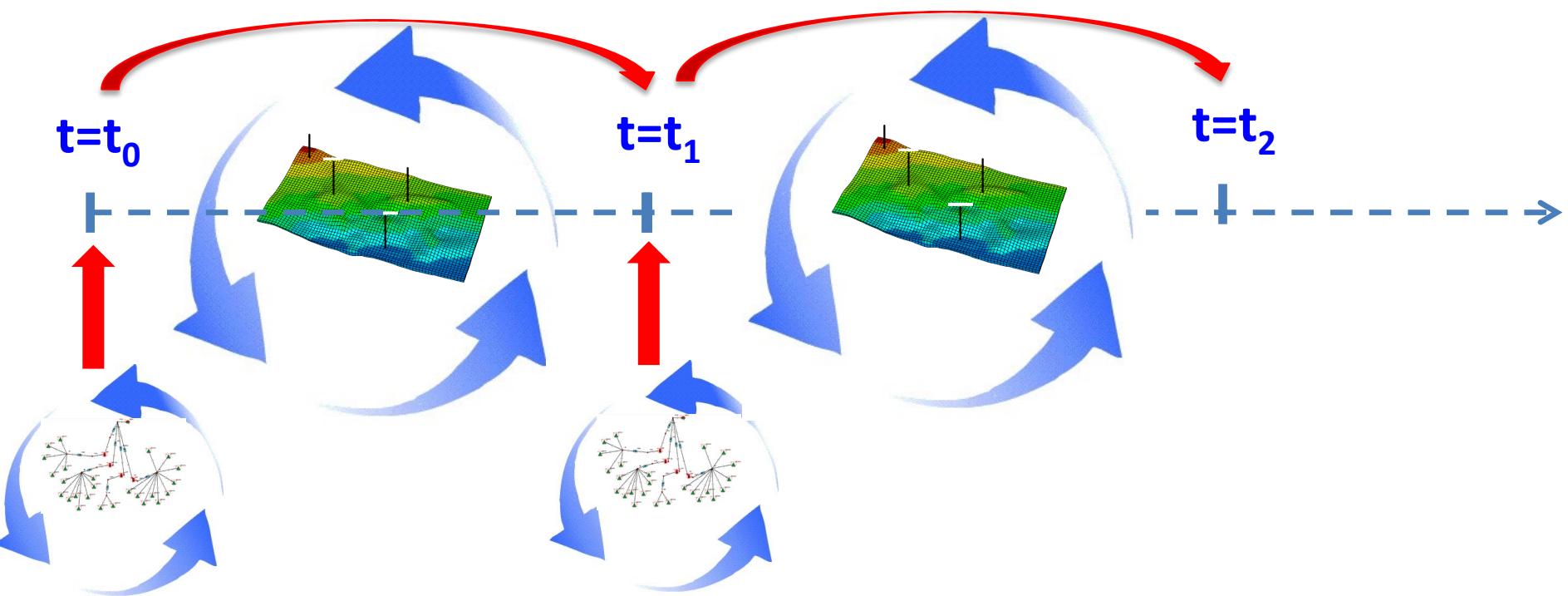
# Integration strategies

- Explicit



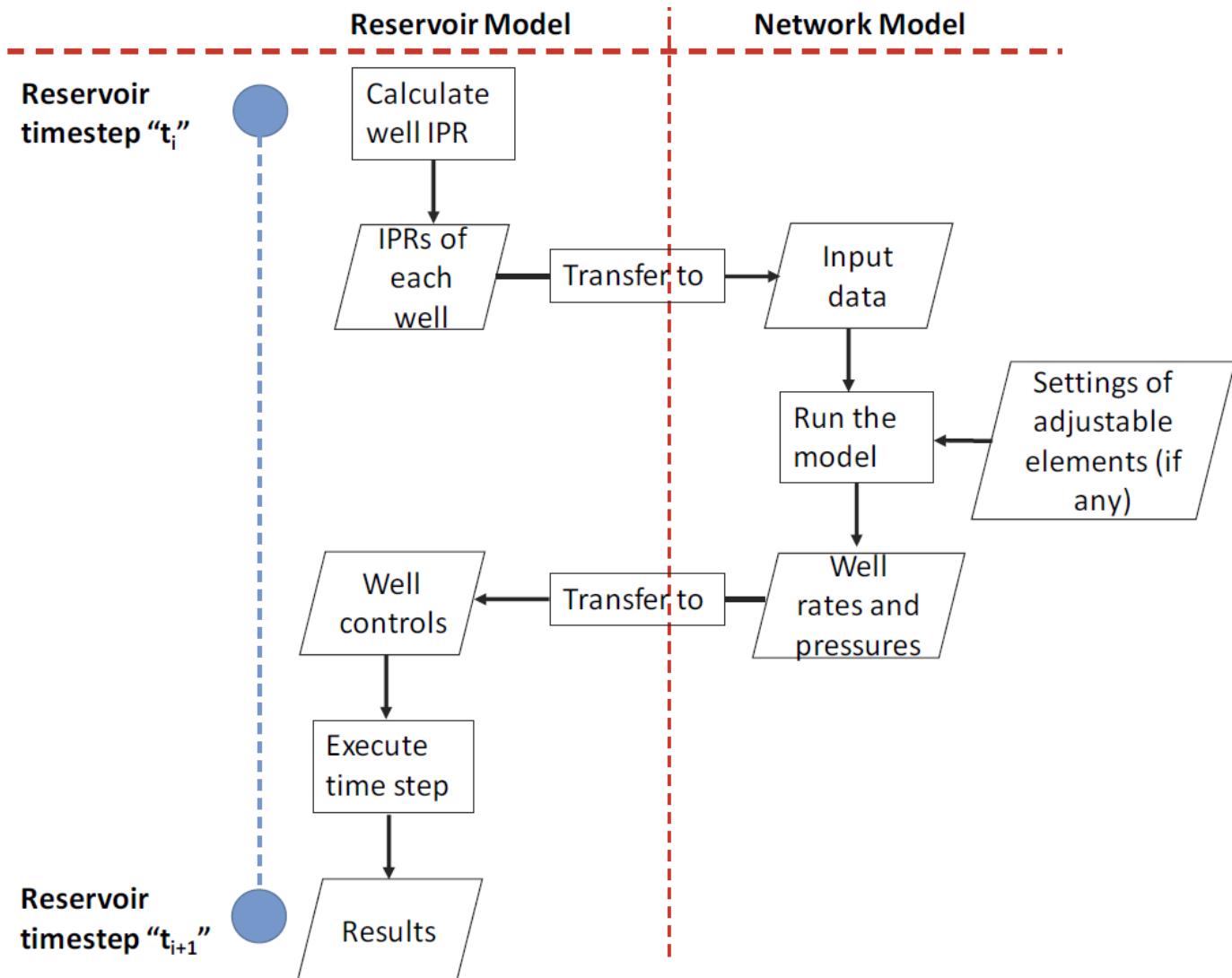
# Integration strategies

- Explicit

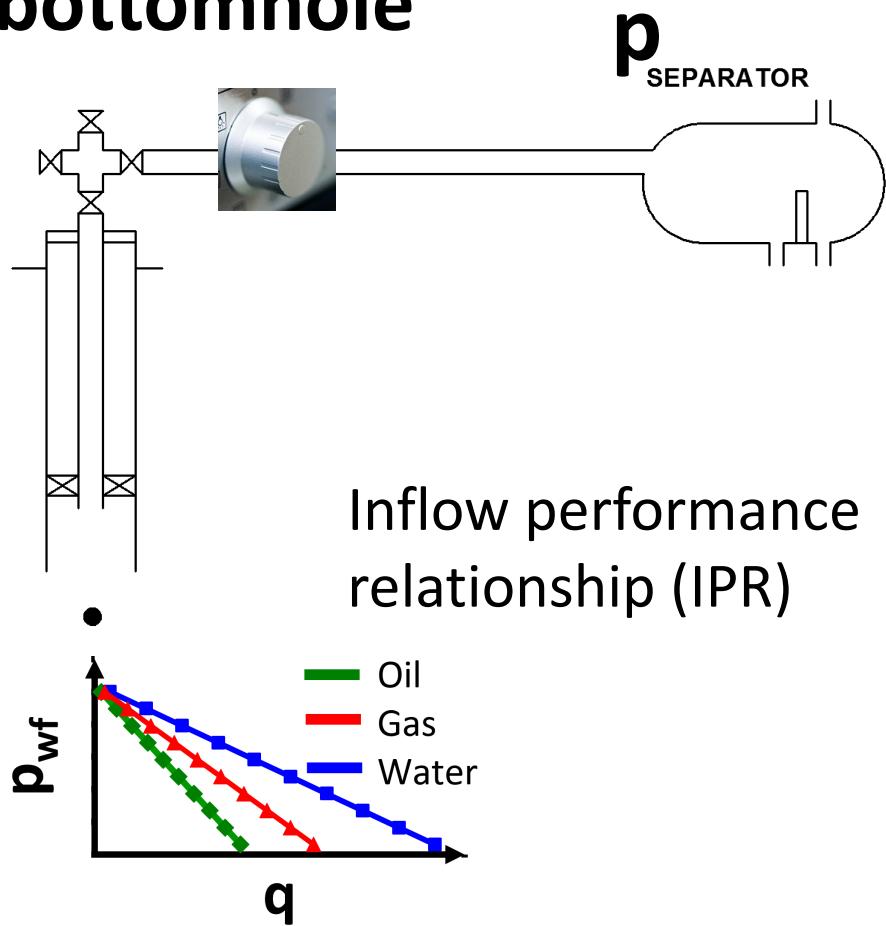
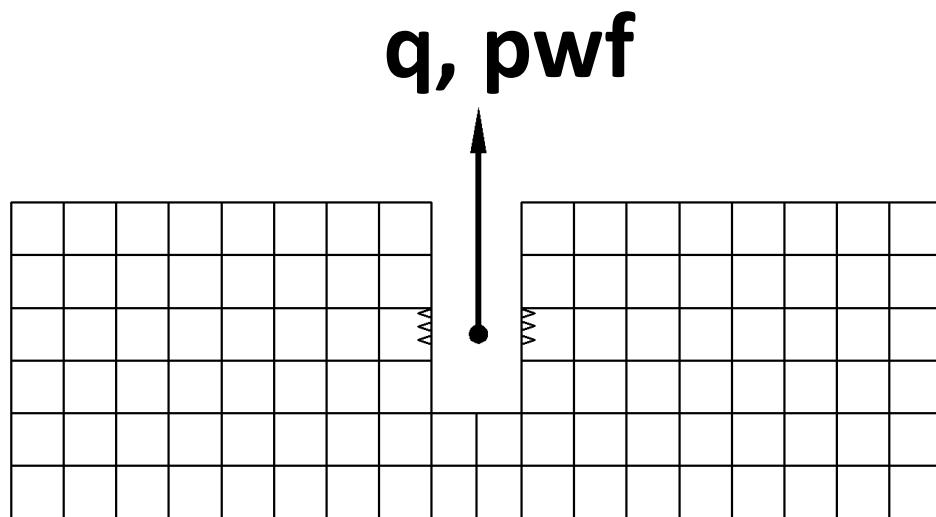


# Integration strategies

- **Explicit**



# Model's Interface: well's bottomhole

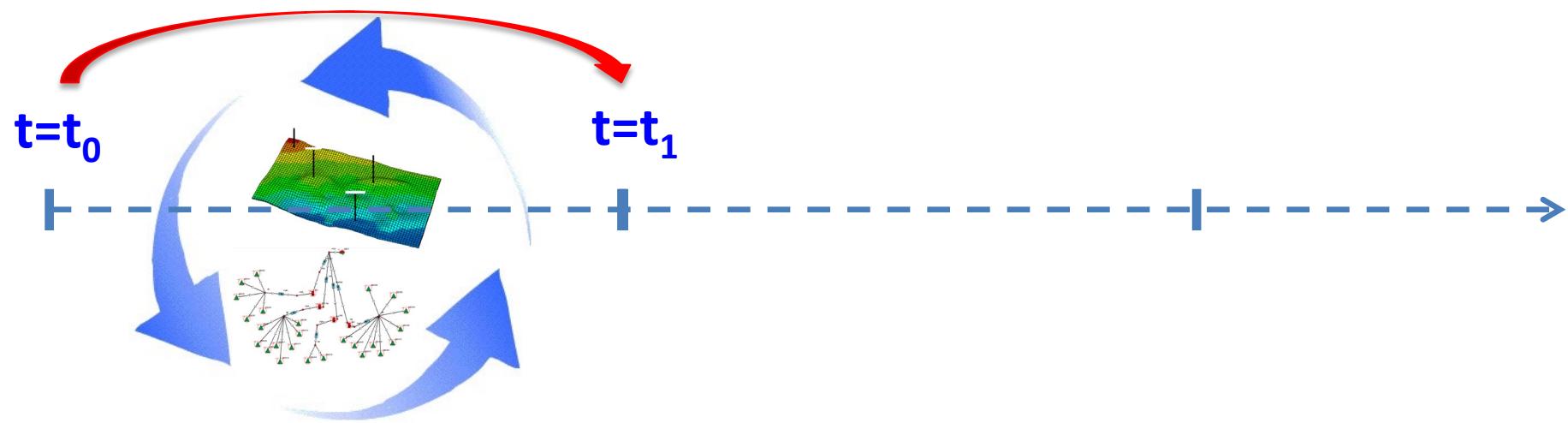


# Explicit integration strategy

- Possible to integrate software from different providers
- IPR generation is required (by reservoir simulator or by the network simulator)
- Can lead to numerical instabilities. A small time-step might be required

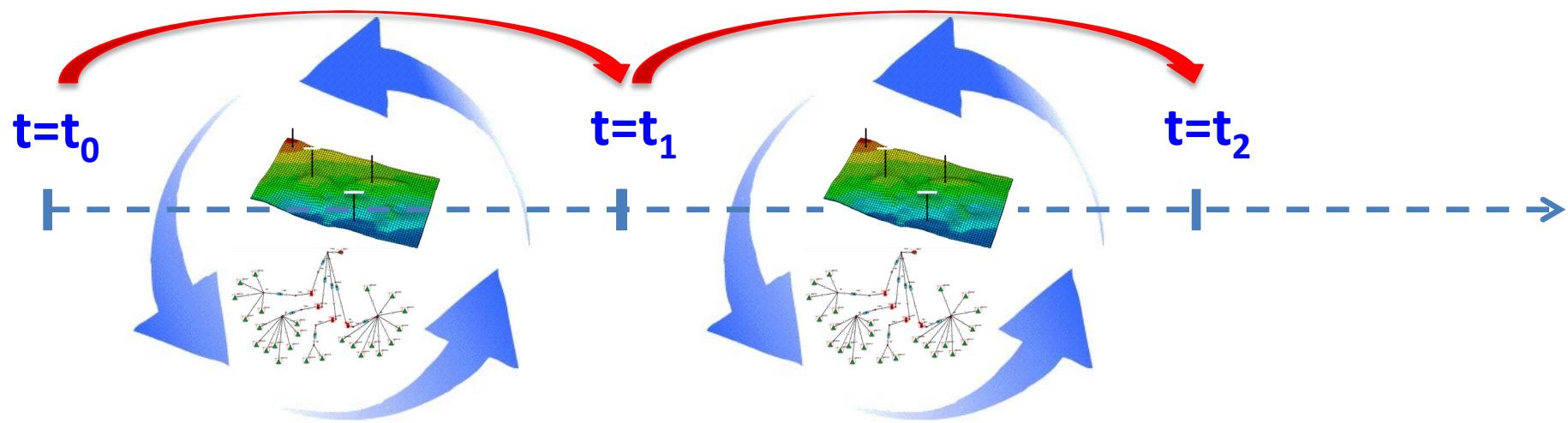
# Integration strategies

- Implicit



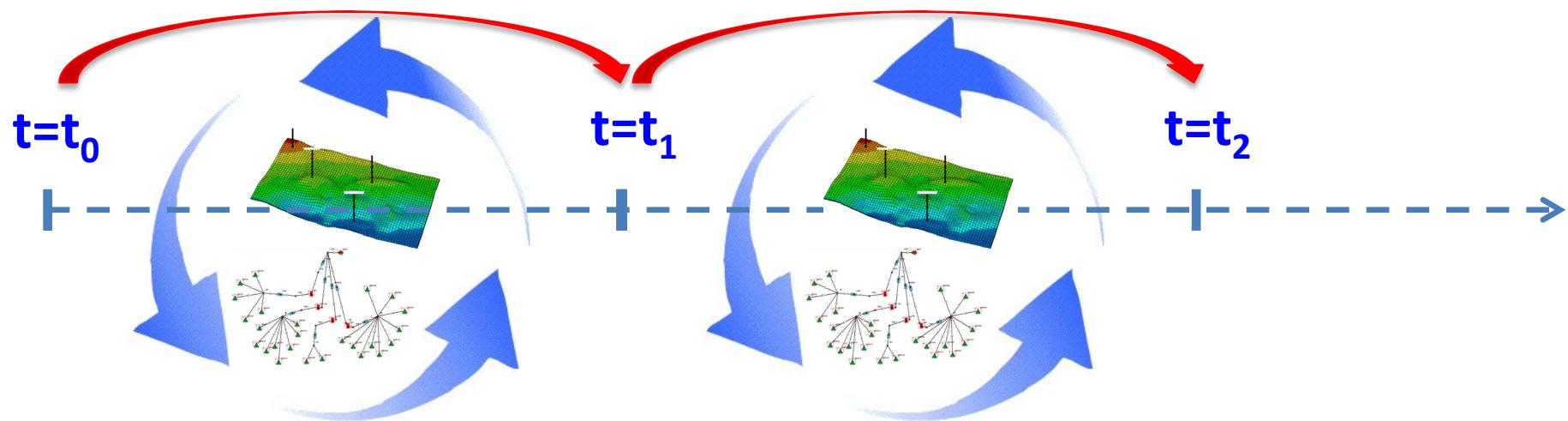
# Integration strategies

- Implicit



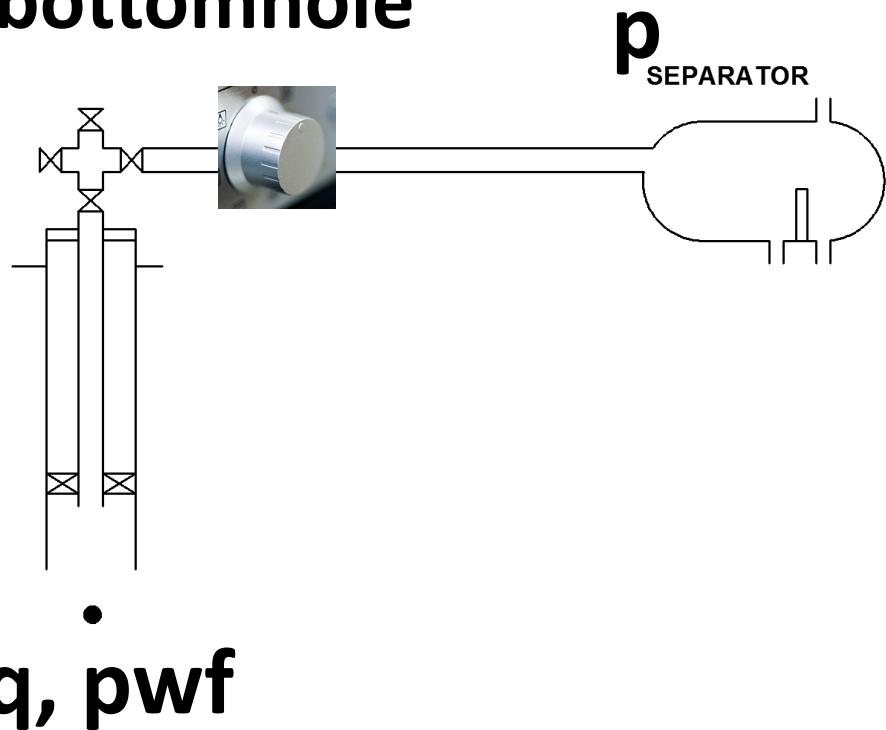
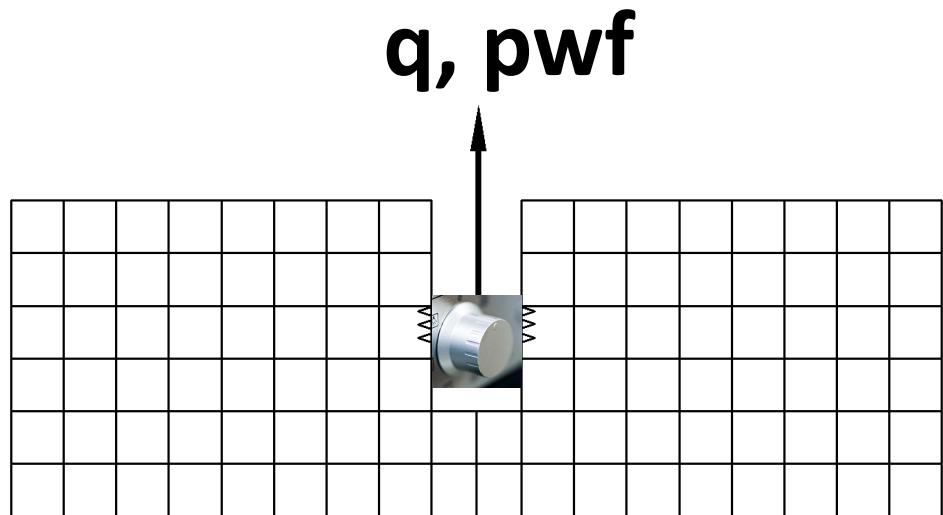
# Integration strategies

- Implicit

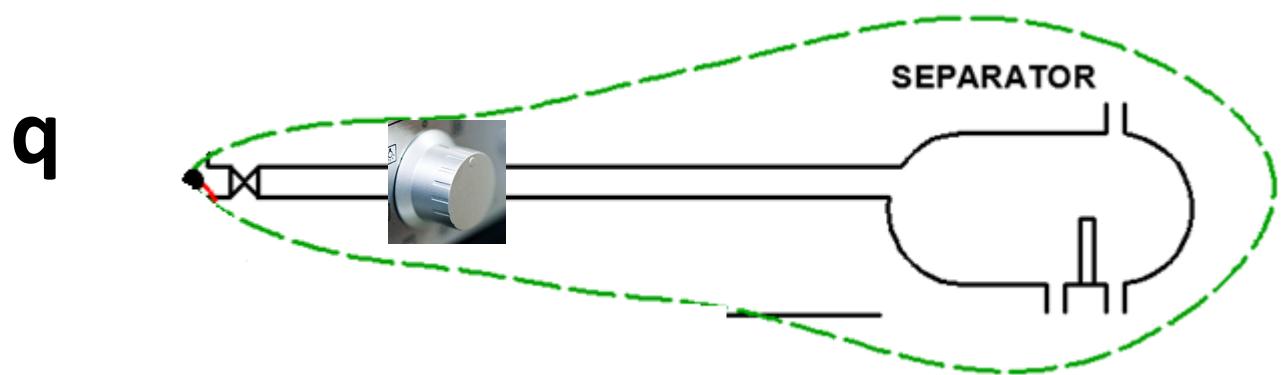


Here an IPR might not be needed

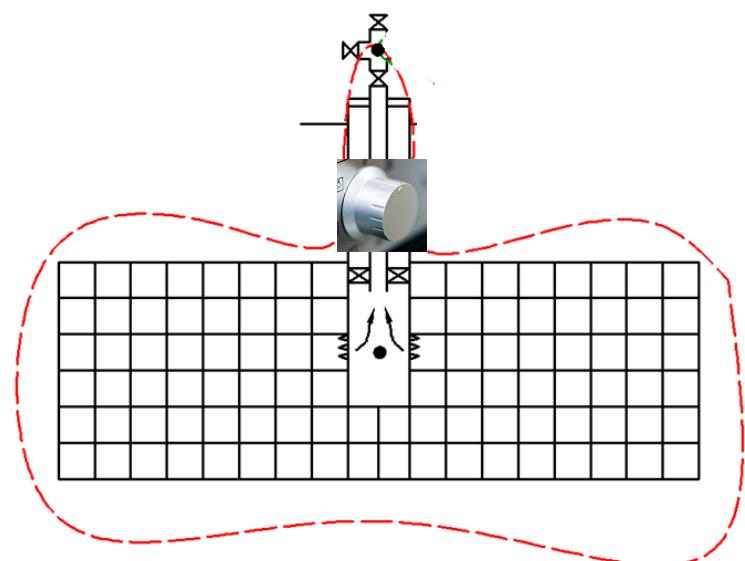
# Model's Interface: well's bottomhole



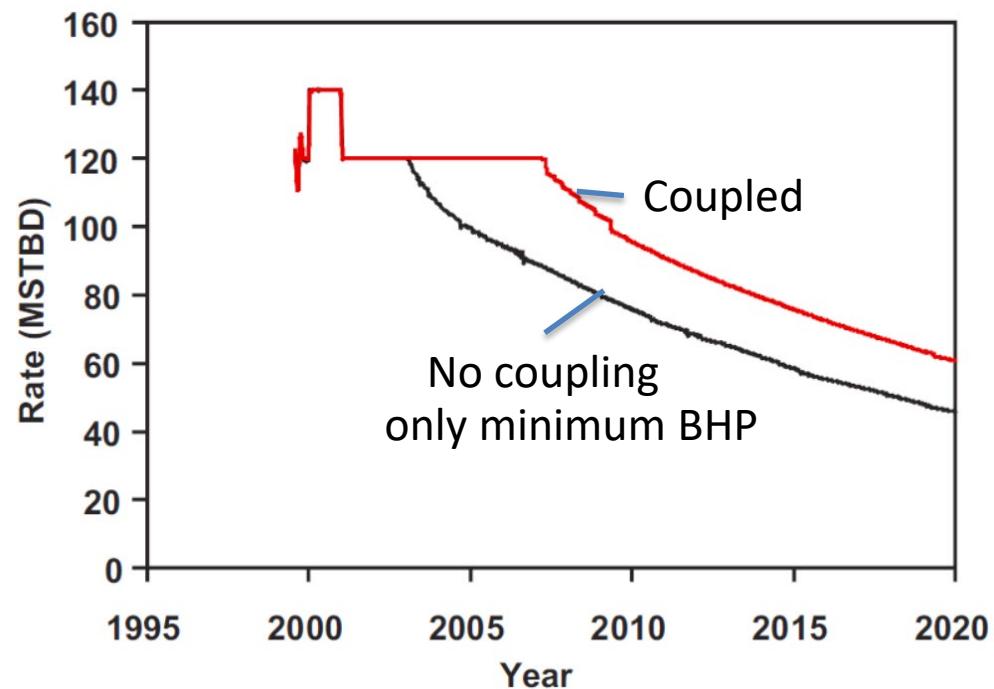
# Model's Interface: wellhead



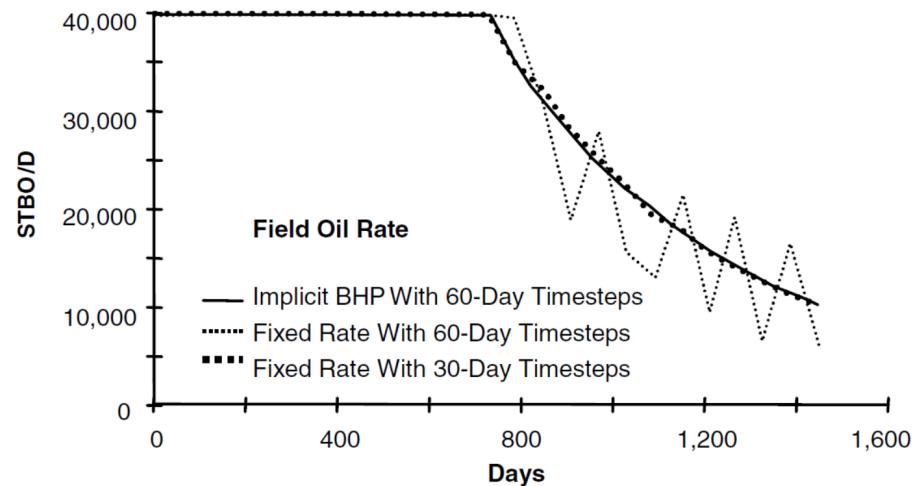
$q, pwh$



# Examples from the literature



From Al-Shaalan, 2002



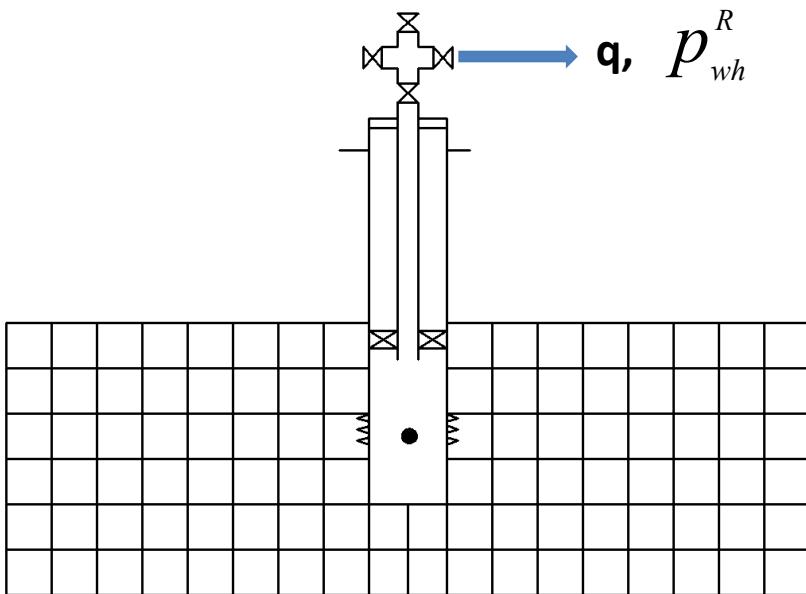
Solution instability from SPE 71120

# Implicit integration strategy

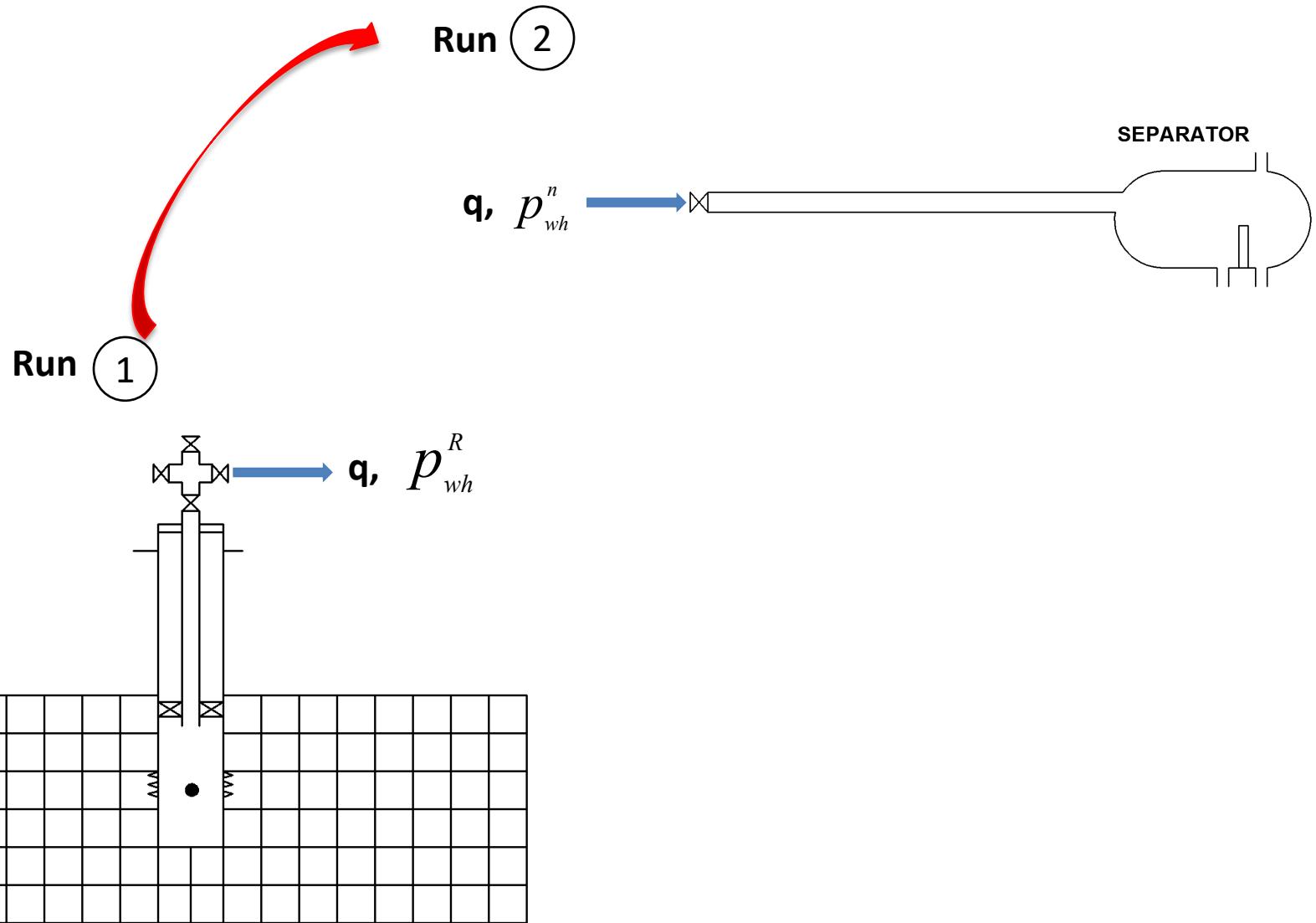
- Difficult to integrate software from different providers (for efficient solving, the source code should be integrated)
- IPR generation is not required
- More numerically stable, bigger time-steps can be used

# Coupling strategy for choked wells

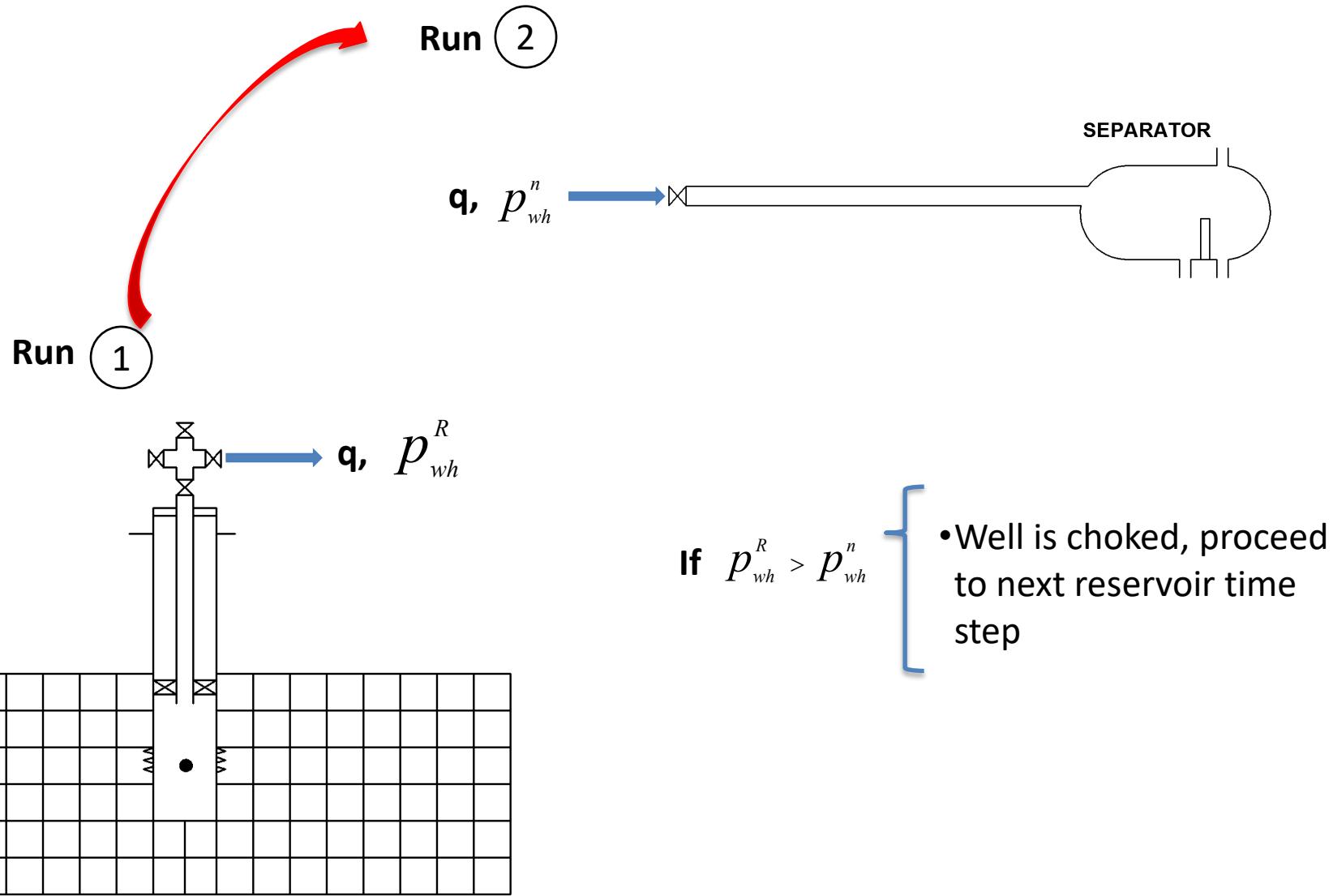
Run (1)



# Coupling strategy for choked wells



# Coupling strategy for choked wells

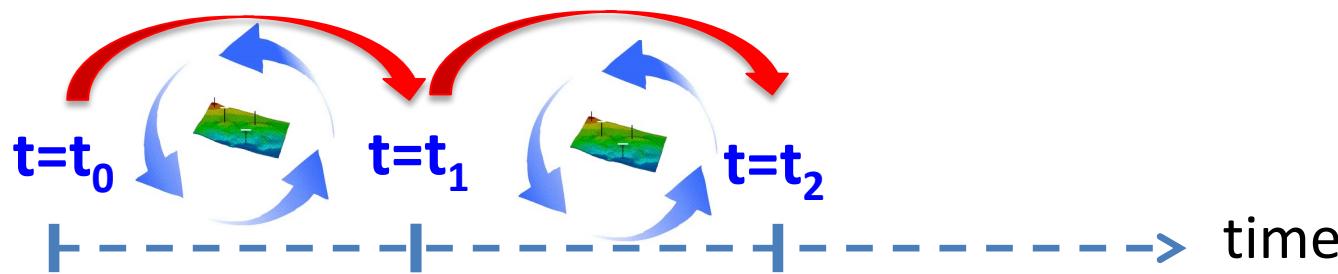


# Integration strategies

- **Loose coupling with bottom-hole coupling –most typical**

# Integration strategies

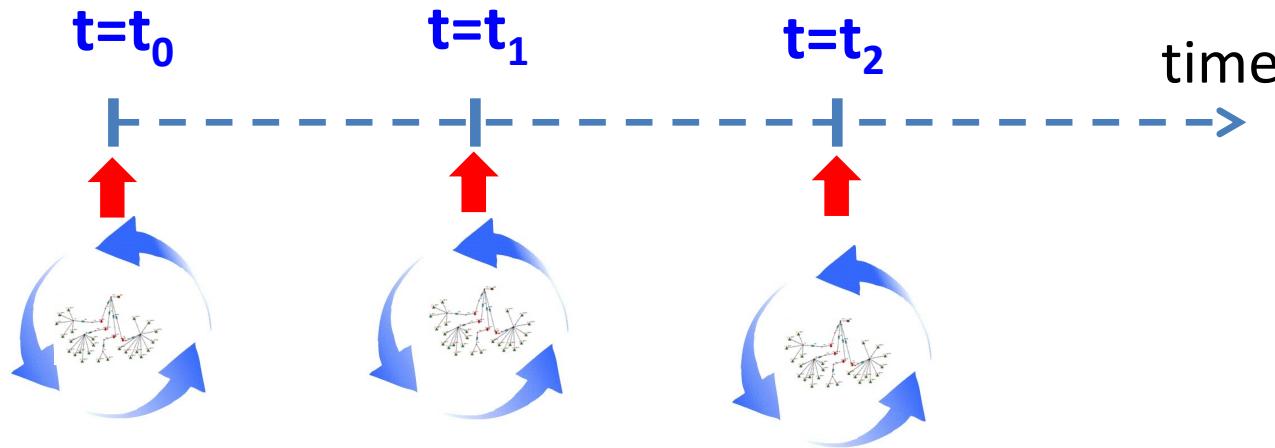
- **Loose coupling with bottom-hole coupling –most typical**
  1. Assume  $p_{wf\min}$
  2. Run reservoir simulation



Obtain profiles of  $q(t)$ ,  $p_{wf}(t)$ , IPR (t)

# Loose coupling with bottom-hole coupling

3. Run network simulation with  $IPR(t)$  from step 2



4. Verify if  $q_{\text{network}}(t) == q_{\text{reservoir}}(t)$ . If not, provide  $p_{\text{wf}}(t)$  as  $p_{\text{wfmin}}(t)$  and repeat from step 1

# Loose coupling integration strategy

- Easy to integrate software from different providers
- Practical for use for different engineering teams
- More time-consuming – several iterations are typically required to converge on a solution

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- HOHENDORFF, J.C., SCHIOZER, D.J. Evaluation on explicit coupling between reservoir simulators and production system. Proceedings of the ASME 31<sup>st</sup> International conference on Ocean, Offshore and Artic Engineering. 1-6 July, 2012.
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# References

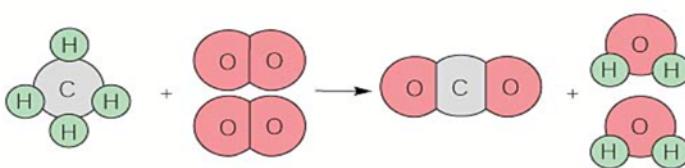
- TRICK, M.D. **A different approach to coupling a reservoir simulator with a surface facilities model.** SPE gas Technology Symposium in Calgary, Alberta, Canada. 1998.
- YANG, D.; ZHANG, Q.; GU, Y. **Integrated Production Operation Models with Reservoir Simulation for Optimum Reservoir Management.** SPE 75236. Richardson: Society of Petroleum Engineering. 2002.
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20240223-CO<sub>2</sub> emissions and CO<sub>2</sub> value chainSource of CO<sub>2</sub> emissions

Reaction: Methane reacts with oxygen to yield carbon dioxide and water



Sketches representing molecules:



Meaning: 1 molecule of methane + 2 molecules of oxygen → 1 molecule of carbon dioxide + 2 molecules of water

Beware!:

- Not all the fuel that is burned is methane, so the reaction could look slightly different
  - natural gas has other heavier components
  - liquid fuel
- there are other components that might not react (inert) like N<sub>2</sub> (but take some energy to heat up), or some compounds are generated that are undesired.

<https://web.fscj.edu/Milczanowski/psc/lect/Ch11/slide3.htm>

1 mol of methane (16 gr) gives 1 mol of CO<sub>2</sub> (44 gr). There is a ratio of 44/16=2.75

1 kg CH<sub>4</sub> combusted → 2.75 kg CO<sub>2</sub> generated

Purpose of combustion: For power/electricity generation or heating

Energy in an oil barrel:

\*1,700 kilowatt-hours (kWh) of energy.

10 691 kWh/Sm<sup>3</sup>

Teslas have batteries that range from 50-100kWh. Teslas average range is 576km meaning they can travel long distances in one charge. All Tesla models are covered by 8 years' warranty, with a minimum of 70% battery capacity retention.

 ActewAGL evHub  
<https://electricvehiclehub.com.au/information-centre/>

How long does a Tesla Battery Last - ActewAGL evHub

Energy in natural gas:

Calorific value of natural gas:  
42-55 MJ/kg\*\*

34-52 MJ/Sm<sup>3</sup>

1 MJ → 0.2777 kWh

9.44-14.44 kWh/Sm<sup>3</sup>

1000 Sm<sup>3</sup> gas → 1 Sm<sup>3</sup> o.e.\*\*\*

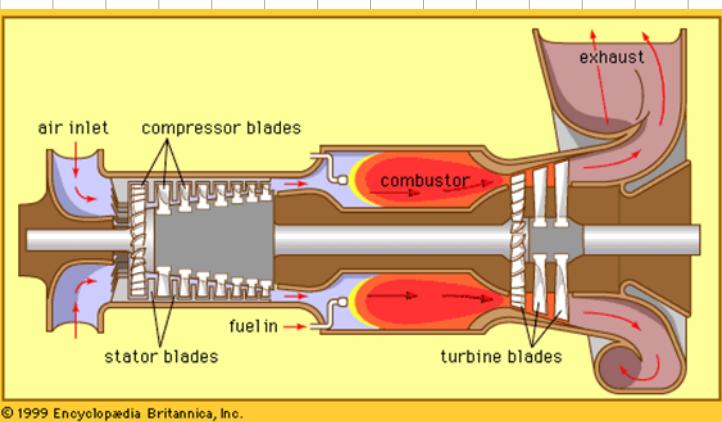
9444-14440 kWh/Sm<sup>3</sup> o.e.

\*<https://www.investopedia.com/terms/b/barrellofoilequivalent.asp>

\*\*<https://group.met.com/en/media/energy-insight/calorific-value-of-natural-gas>

\*\*\*<https://www.sodir.no/en/about-us/use-of-content/conversion-table/>

If using a gas turbine to generate power:



[https://en.wikipedia.org/wiki/Gas\\_turbine](https://en.wikipedia.org/wiki/Gas_turbine)

GT for offshore applications have efficiencies 40-50%. Using an approximation:

$$\eta_{GT} = \frac{\dot{W}_{out}}{\dot{Q}_{in}} = \dot{m}_g \cdot Cv \quad \text{calorific value}$$

\*[https://www.havtil.no/contentassets/3391c6686b2b4265abe8585294151335/2020\\_18\\_62\\_rapport-equinor-hammerfest-lng-granski\\_ng.pdf](https://www.havtil.no/contentassets/3391c6686b2b4265abe8585294151335/2020_18_62_rapport-equinor-hammerfest-lng-granski_ng.pdf)

If output power is e.g. 45 MW (1 GT at Melkøya\*, out of 5)

$$P \cdot t$$

This gives, in a year:

-Energy: 3.94 E8 kWh

-Gas burned:  $54.6 \times 10^6 - 104 \times 10^6 \text{ Sm}^3 \rightarrow 38 \times 10^6 - 73 \times 10^6 \text{ kg}$  (assuming , GT effic: 0.4-0.5, deng\_sc=0.7 kg/m<sup>3</sup>)

-CO<sub>2</sub> emissions:  $105 \times 10^6 - 201 \times 10^6 \text{ kg} \rightarrow 105-201 \times 10^3 \text{ t}$  (assuming 2.75 kg CO<sub>2</sub>/1 kg gas)

$$1 \text{ tonne} \cdot t = 1000 \text{ kg}$$

Melkøya past 2030. Moreover, electrification of the plant is one of the most extensive climate measures in Norway, reducing CO<sub>2</sub> emissions by 850,000 tonnes per year.

$$\dot{m}_g = \left( \frac{\dot{W}_{out}}{\eta_{GT}} \right) \frac{1}{Cv}$$

$0.4 \rightarrow 0.5 \quad 9.44 \quad 14.44$

\*\*<https://www.equinor.com/magazine/future-of-melkoya-lng-plant>

Numbers to remember! (Gas turbine)

1 Sm<sup>3</sup> of gas --> 1.95 kg CO<sub>2</sub> --> 4.7-7.2 kWh

\*\*\*<https://www.rte-france.com/en/eco2mix/co2-emissions>

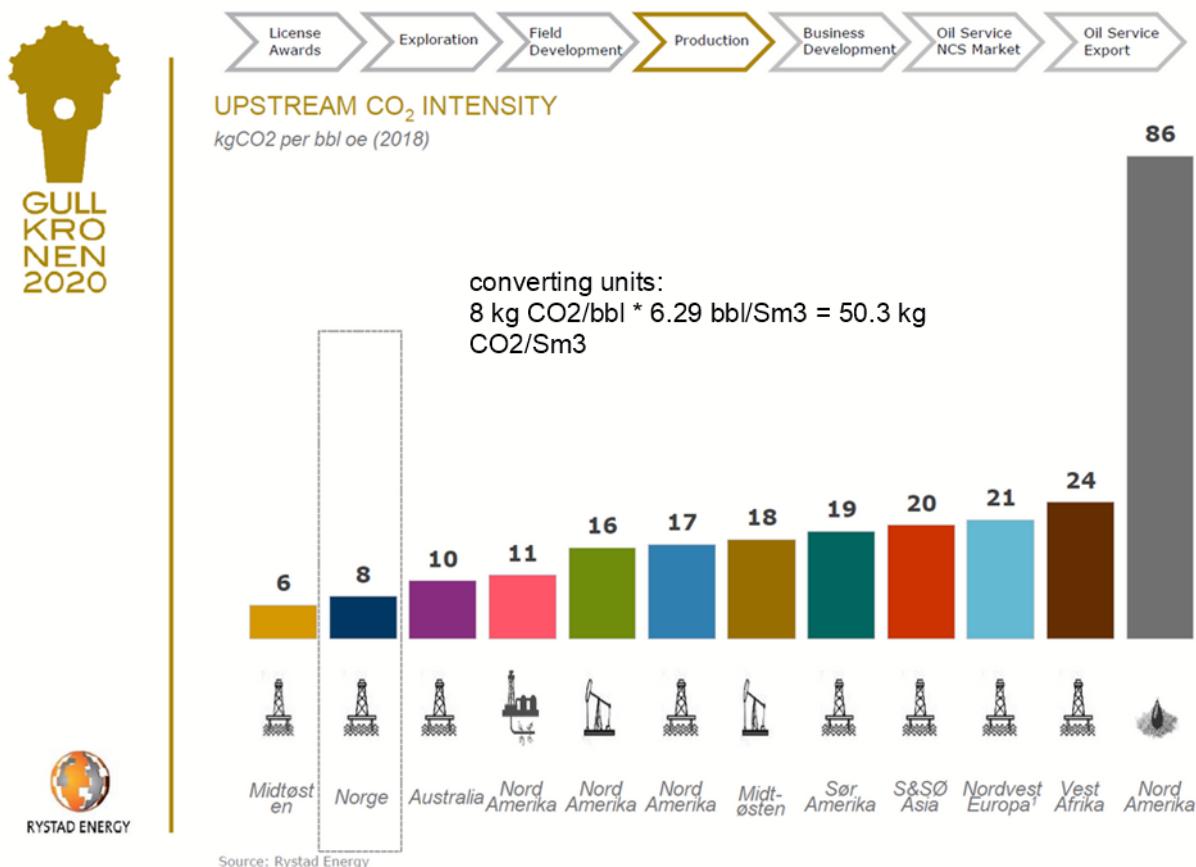
1 MWh --> 139-213 Sm<sup>3</sup>-->0.27- 0.5 t CO<sub>2</sub> (similar to \*\*\*)

- Scope 1 emissions**— This one covers the Green House Gas (GHG) emissions that a company makes directly — for example while running its boilers and vehicles.
- Scope 2 emissions** — These are the emissions it makes indirectly – like when the electricity or energy it buys for heating and cooling buildings, is being produced on its behalf.
- Scope 3 emissions** — Now here's where it gets tricky. In this category go all the emissions associated, not with the company itself, but that the organisation is indirectly responsible for, up and down its value chain. For example, from buying products from its suppliers, and from its products when customers use them. Emissions-wise, Scope 3 is nearly always the big one.

<https://www2.deloitte.com/uk/en/focus/climate-change/zero-in-on-scope-1-2-and-3-emissions.html>

### Scope 1 CO<sub>2</sub> emissions in the oil and gas industry:

- Gas turbines used for electricity generation, shaft power, and from heaters. (MOST SIGNIFICANT)
- Transport of personnel and goods to and from the platform
- Drilling, completion and intervention
- Tanker transport of oil to refineries
- Gas transport to customer (LNG or pipeline)



Usually to estimate CO<sub>2</sub> emissions it is necessary to :

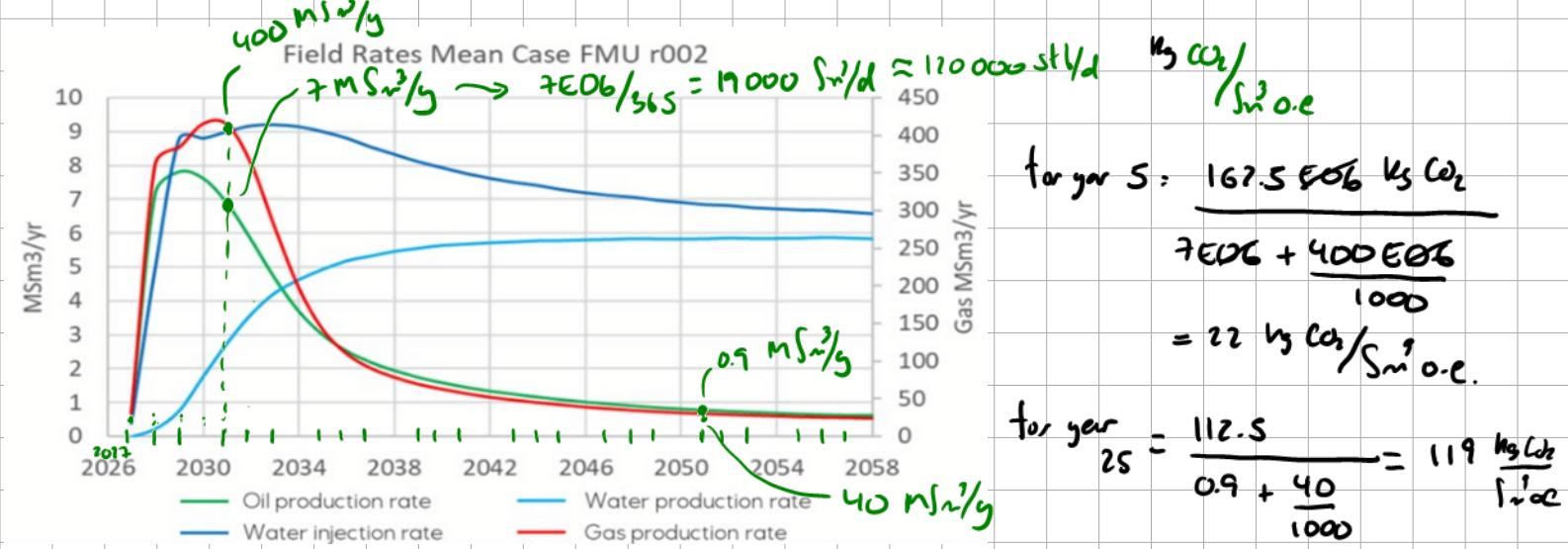
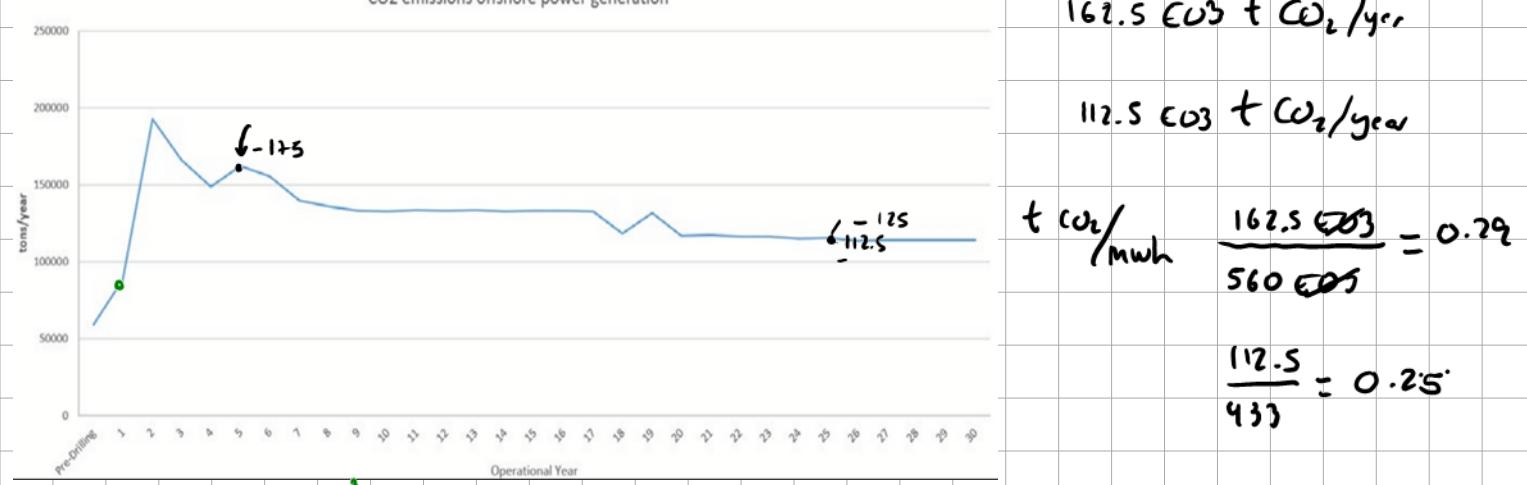
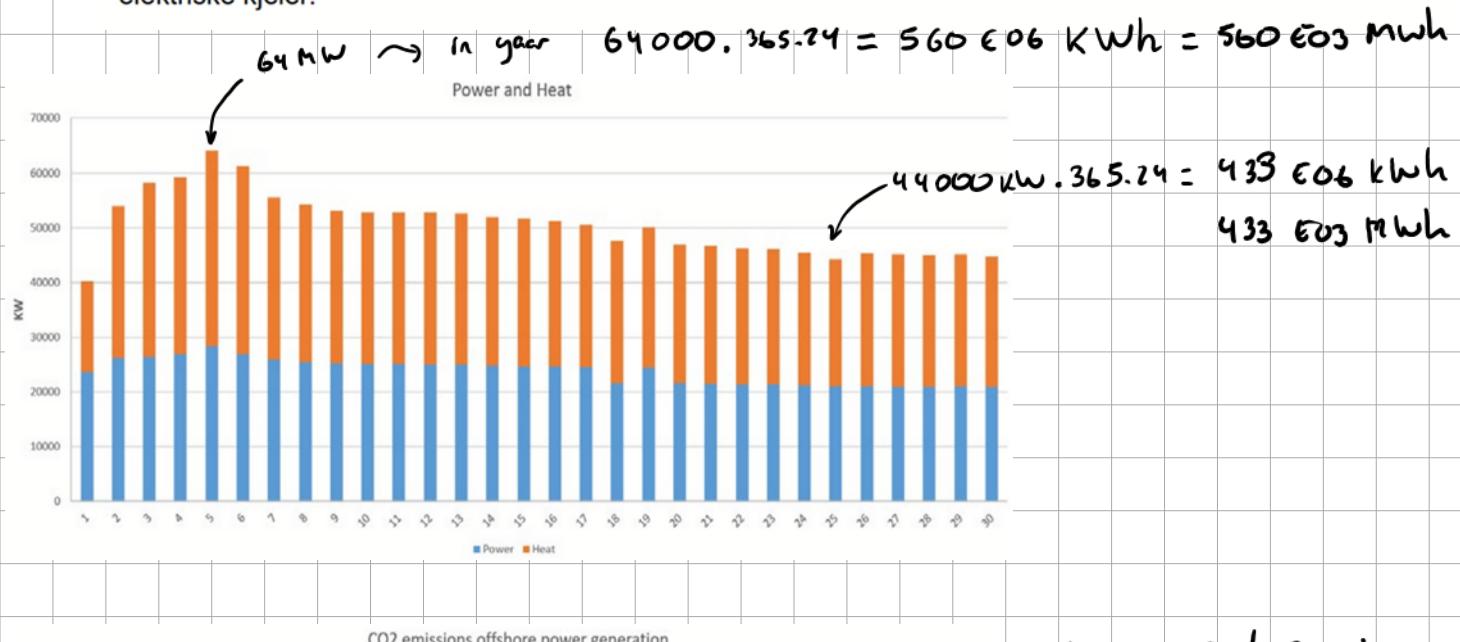
Calculate energy requirements --> calculate gas to burn --> calculate CO<sub>2</sub> emissions

An example:

<https://www.equinor.com/content/dam/statoil/documents/impact-assessment/wisting/equinor-wisting-forslag-til-ku-program-05-01-21.pdf>

#### Kilder til utsipp

Kilder til utsipp til luft i driftsfasen inkluderer normalt utsipp fra kraftgenerering på produksjonsenheten (turbiner), borerigg og fartøy (diesel), omlasting av råolje, lasteskip og helikopter. Ved import av kraft fra land vil det ikke være behov for gassturbiner på produksjonsinnretningen. Varmebehovet vil da dekkes gjennom elektriske kjeler.



- What is the average energy required to produce a barrel (or Sm<sup>3</sup>) of oil:

kWh/  
Sm<sup>3</sup> o.e.

$$\text{for year 5: } \frac{560 \text{ E}06 \text{ kWh}}{7E06 + \frac{400E06}{1000}} = 75.6 \text{ kWh/Sm}^3 \text{ o.e.}$$

$$\text{for year 25: } \frac{433}{0.9 + \frac{40}{1000}} = 460 \text{ kWh/Sm}^3 \text{ o.e}$$

Energy contained in the HC / required to produce ?

10 691 kWh/Sm<sup>3</sup>

141 trees

23 trees

Scope 3 emissions:

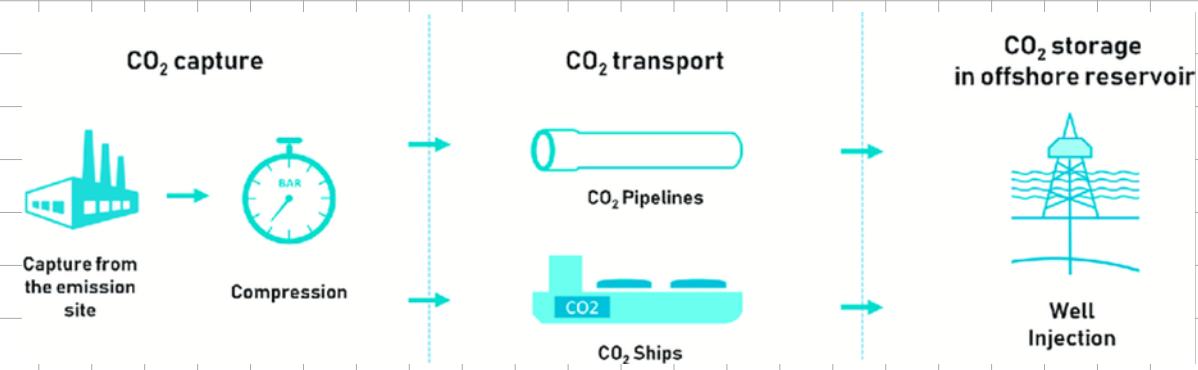
-emissions of oil and gas sold to the market (e.g. gas sold for electricity generation)

CO<sub>2</sub> emitted to produce compared to CO<sub>2</sub> emitted by burning the gas?

22 - 119 kg CO<sub>2</sub>/  
Sm<sup>3</sup> o.e.

emitted during production

$$\frac{1.95 \text{ kg CO}_2}{\frac{1 \text{ Sm}^3 \text{ gas}}{1000 \text{ Sm}^3 \text{ oil}}} = 1950 \text{ kg CO}_2/\text{Sm}^3 \text{ o.e.}$$

CO<sub>2</sub> value chain - Capture and storage

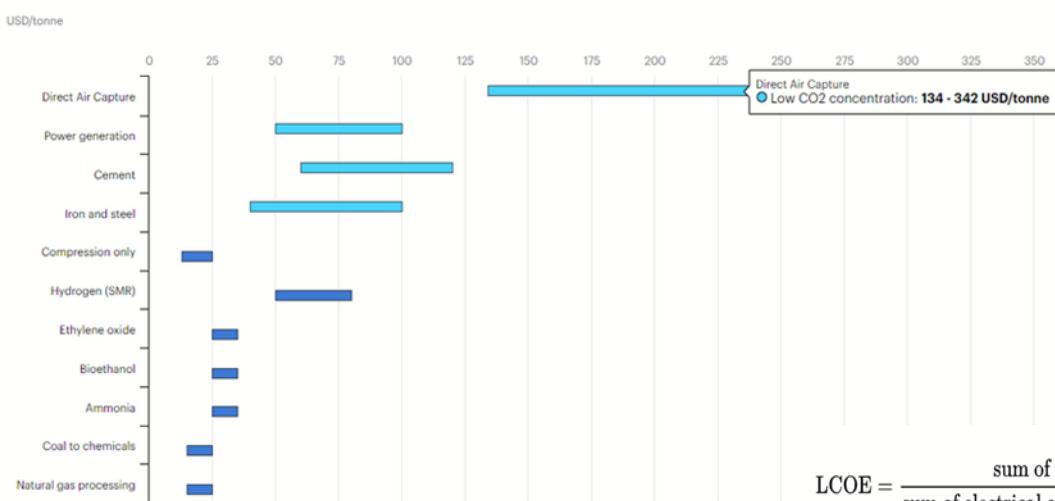
[https://www.researchgate.net/publication/338819648\\_Effects\\_of\\_CO2\\_on\\_polymeric\\_materials\\_in\\_the\\_CO2\\_transport\\_chain\\_A\\_review](https://www.researchgate.net/publication/338819648_Effects_of_CO2_on_polymeric_materials_in_the_CO2_transport_chain_A_review)



<https://www.equinor.com/magazine/climate-solution-for-european-industry>

Levelised cost of CO<sub>2</sub> capture by sector and initial CO<sub>2</sub> concentration, 2019

Open



$$\text{LCOE} = \frac{\text{sum of costs over lifetime}}{\text{sum of electrical energy produced over lifetime}} = \frac{\sum_{t=1}^n \frac{I_t + M_t + F_t}{(1+r)^t}}{\sum_{t=1}^n \frac{E_t}{(1+r)^t}}$$

IEA\_Licence: CC BY 4.0

● Low CO<sub>2</sub> concentration   ● High CO<sub>2</sub> concentration

"the cost of onshore pipeline transport is in the range of USD 2-14/t CO<sub>2</sub>,"

<https://www.iea.org/commentaries/is-carbon-capture-too-expensive>

", more than half of onshore storage capacity is estimated to be available below USD 10/t CO<sub>2</sub>"

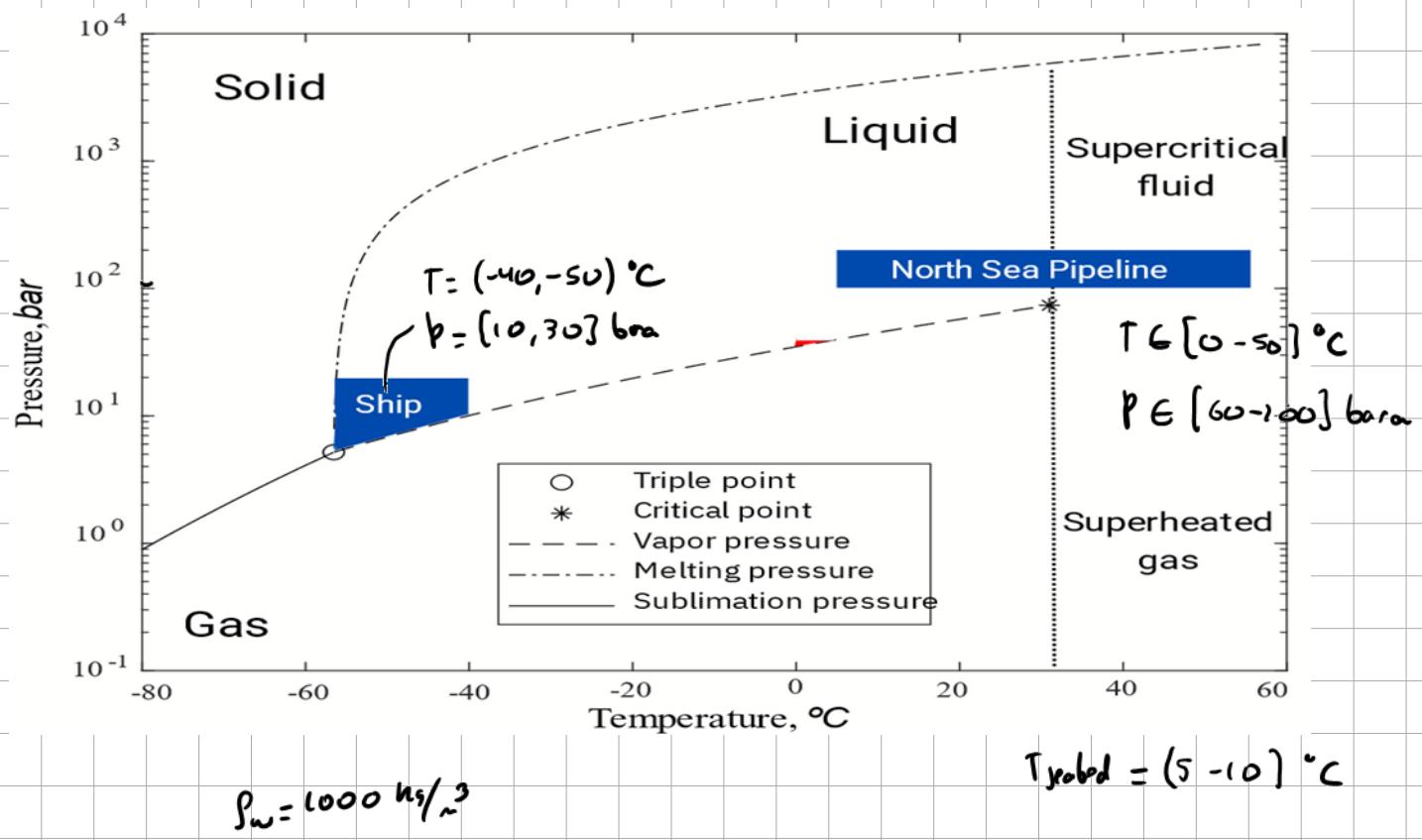
In 2023, the tax rates are  
respectively NOK 761 ....  
per tonne of CO<sub>2</sub>

<https://energifaktanorge.no/en/et-baerekraftig-og-sikkert-energisystem/avgifter-og-kvoteplikt>

$$\frac{761 \text{ NOK}}{\text{t CO}_2} \approx 76.1 \text{ USD/t CO}_2$$

$$\begin{aligned} & \text{Capture + barge + stor} \\ & 50-100 + 2-14 + 10 = 62-124 \end{aligned}$$

P-T conditions of CO<sub>2</sub> in pipeline transportation and injection using subsea wells



		T [°C]					
		0	10	20	30	40	50
p [bara]	DENSITY [kg/m³]	940	587	144	125	114	105
		948	882	567	175	150	136
50		955	893	808	487	201	173
60		962	903	827	692	287	221
70		968	912	843	743	482	288
80		974	920	856	771	620	387
90		980	928	868	792	682	499
100		985	935	878	809	717	582
110		990	942	887	823	743	635
120		995	948	896	836	763	672
130		1000	954	904	847	780	699
140		1004	960	911	857	795	722
150		1008	965	918	866	808	741
160		1012	970	925	875	819	757
170		1017	975	931	883	830	771
180		1021	980	937	891	840	784

		T [°C]					
		0	10	20	30	40	50
p [bara]	Viscosity [Pa s]	1.04E-04	5.92E-05	1.66E-05	1.67E-05	1.70E-05	1.74E-05
		1.07E-04	8.83E-05	5.11E-05	1.79E-05	1.78E-05	1.80E-05
50		1.09E-04	9.10E-05	7.29E-05	3.80E-05	1.92E-05	1.89E-05
60		1.11E-04	9.36E-05	7.66E-05	5.52E-05	2.25E-05	2.04E-05
70		1.13E-04	9.59E-05	7.97E-05	6.22E-05	3.49E-05	2.30E-05
80		1.15E-04	9.82E-05	8.25E-05	6.66E-05	4.70E-05	2.82E-05
90		1.17E-04	1.00E-04	8.50E-05	7.02E-05	5.41E-05	3.60E-05
100		1.19E-04	1.02E-04	8.74E-05	7.32E-05	5.88E-05	4.33E-05
110		1.21E-04	1.04E-04	8.96E-05	7.59E-05	6.25E-05	4.88E-05
120		1.22E-04	1.06E-04	9.17E-05	7.84E-05	6.57E-05	5.32E-05
130		1.24E-04	1.08E-04	9.37E-05	8.07E-05	6.84E-05	5.67E-05
140		1.26E-04	1.10E-04	9.56E-05	8.28E-05	7.10E-05	5.98E-05
150		1.27E-04	1.11E-04	9.74E-05	8.48E-05	7.33E-05	6.26E-05
160		1.29E-04	1.13E-04	9.92E-05	8.67E-05	7.54E-05	6.50E-05
170		1.31E-04	1.15E-04	1.01E-04	8.86E-05	7.75E-05	6.73E-05
180		1.32E-04	1.16E-04	1.03E-04	9.03E-05	7.94E-05	6.95E-05
190							
200							

$$\dot{m}_w = 1 \text{ E-3 Pa} \cdot \text{s}$$

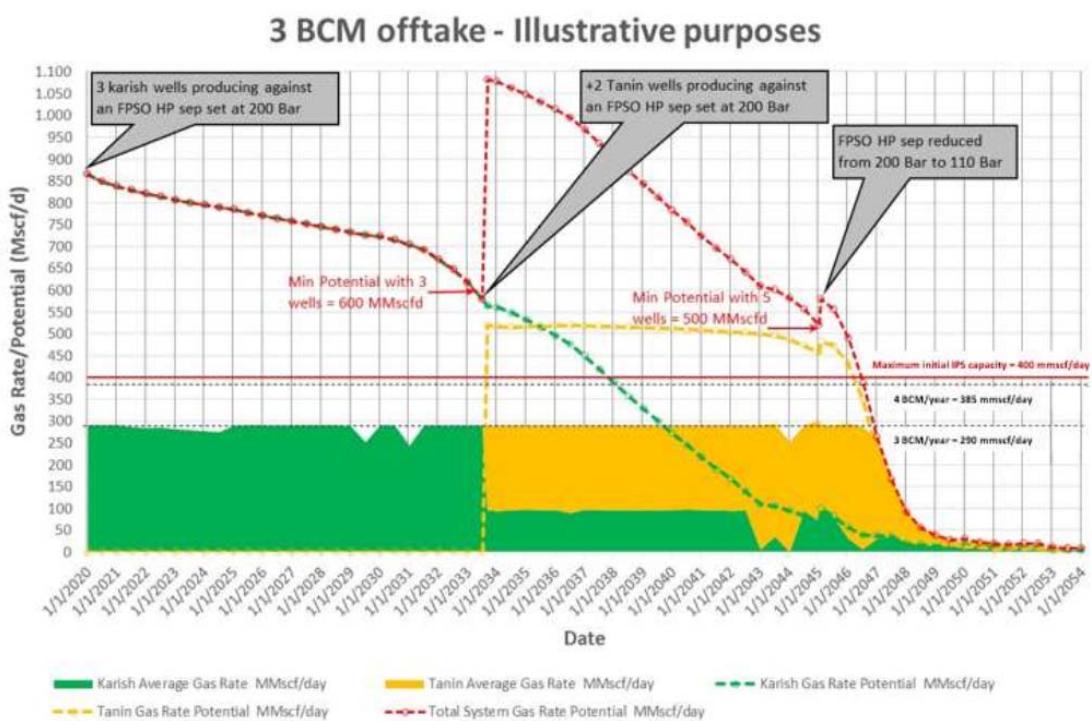
in subsea injection  
systems has density as a  
liquid but viscosity as a  
gas

$$\Delta p = \Delta p_u + \Delta p_f$$

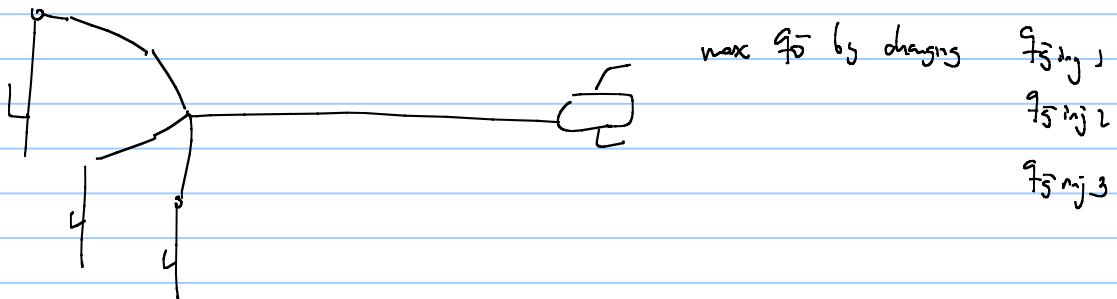
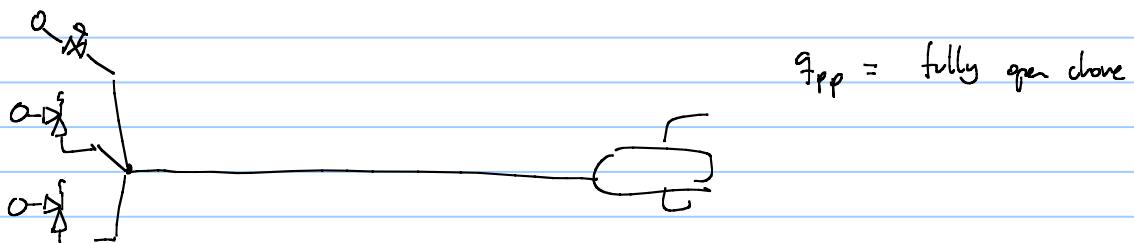
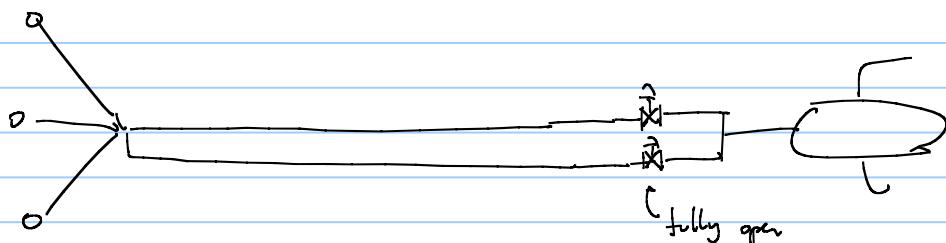
$$\tau_{\text{PT}}$$

$$\gamma_f(\mu) \downarrow m$$

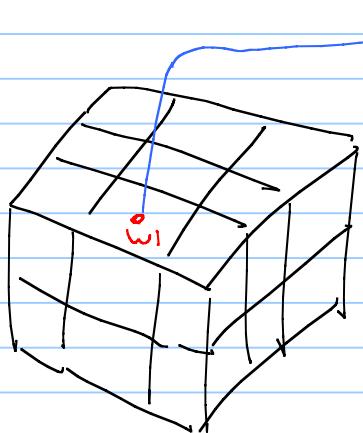
$$\begin{aligned} t-4 &\rightarrow M_3 \\ E-S & \end{aligned}$$



Production potential maximum rate the production system can deliver at a given time



Production potential is also used in reservoir simulation



boundary conditions on well 1  $\rightarrow q_{\text{target}}$

$p_{\text{min}}$

in each time step

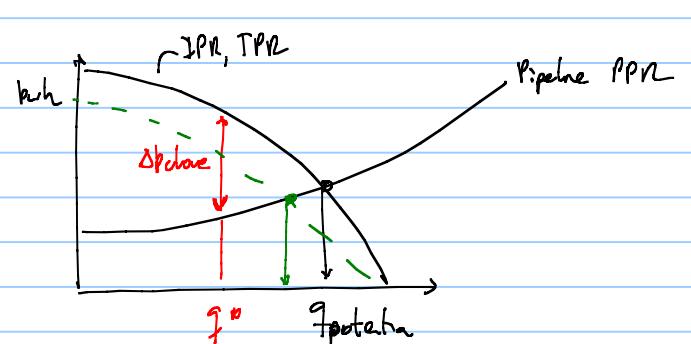
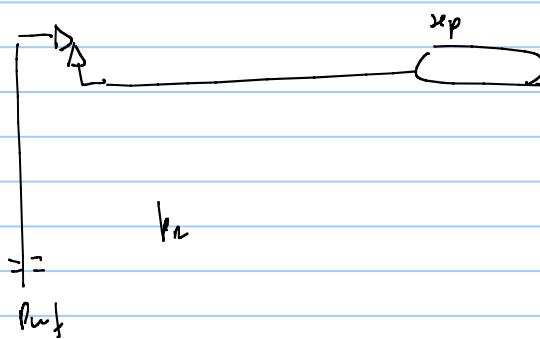
- tries  $p_{\text{min}} \rightarrow q_{\text{potential}}$

- if  $q_{\text{potential}} > q_{\text{target}}$

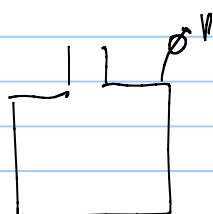
$\hookrightarrow q_{\text{target}}$  can be produced  
 increase  $p_{\text{min}}$   
 $q_{\text{well}} = q_{\text{target}}$

if  $q_{\text{pot}} < q_{\text{target}}$

$\hookrightarrow q_{\text{target}}$  cannot be produced  
 $p_{\text{ref}} = p_{\text{min}}$   
 $q_{\text{well}} = q_{\text{potential}}$



- Production potential is actually a function of  $P_e$

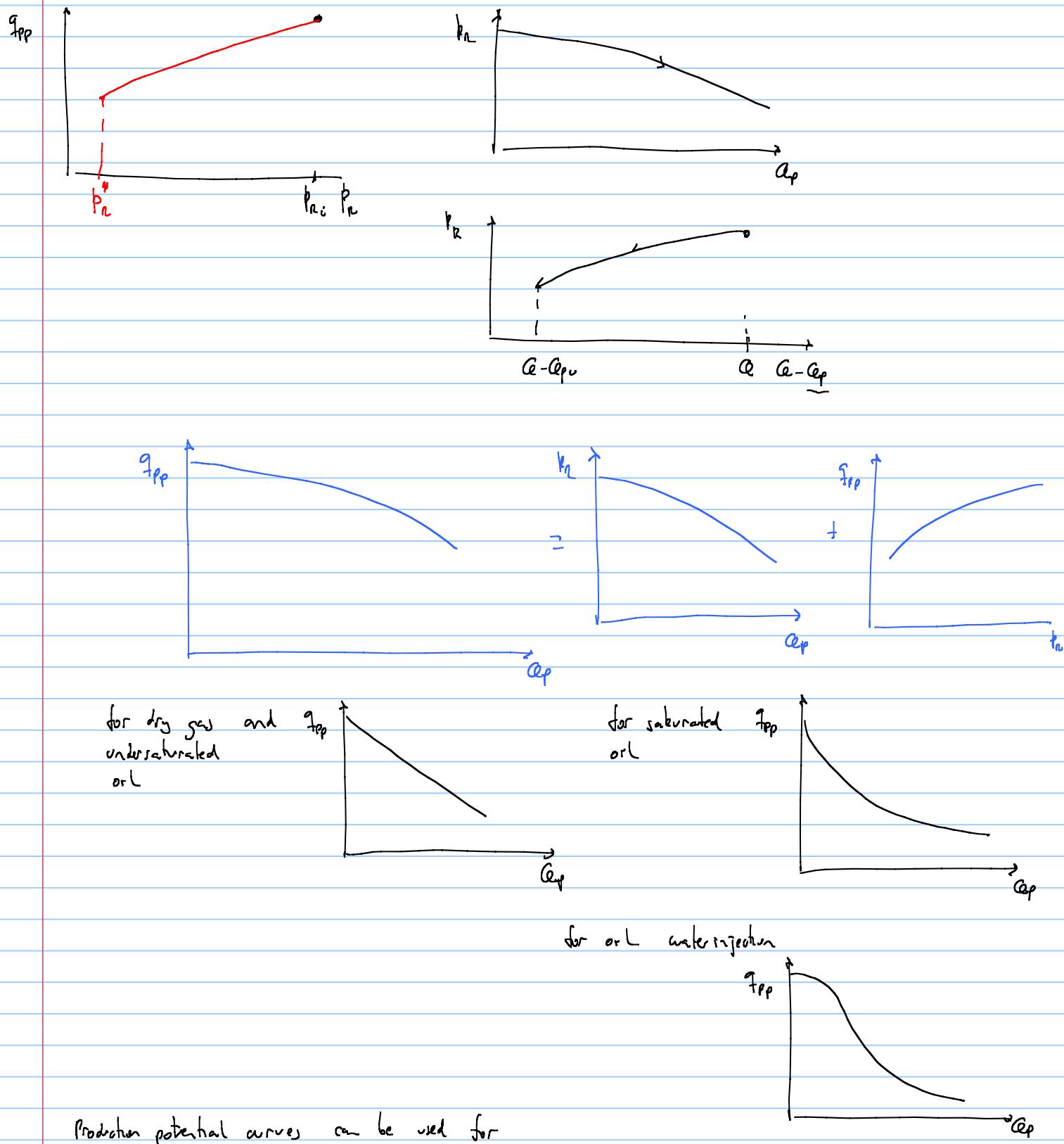


$\hookrightarrow$  and  $P_e$  is usually a function of  
 $Q_p \rightarrow G_p$  (gas)  
 $\hookrightarrow N_p$  (oil)

$$P_n = f(Q - Q_p)$$

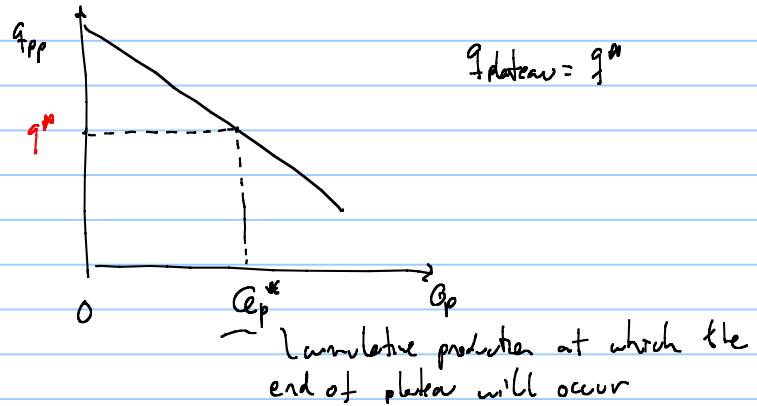
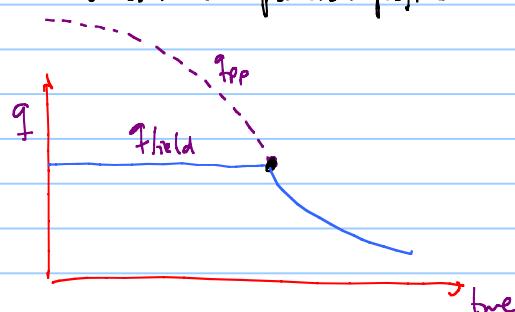
$$P_n(t) = f(Q - Q_p(t))$$

$$P_n = f(Q_p)$$



Production potential curves can be used for

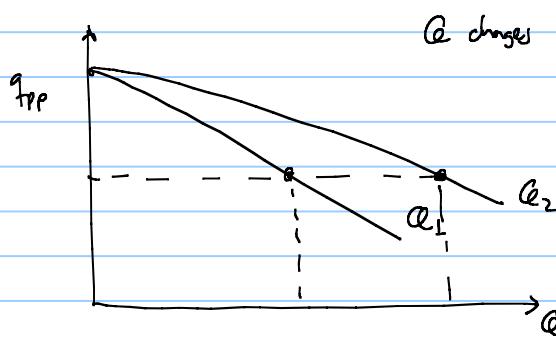
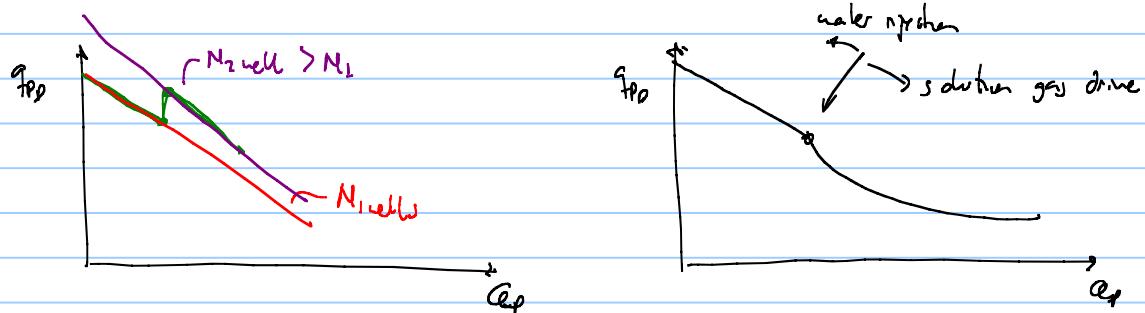
- determine plateau duration
- estimate production profile



$Q \rightarrow Q_p^*$  has been produced at constant rate  $q^*$

$$t_{\text{plateau}} = \frac{Q_p^* [ \text{days} ]}{q^* [ \text{m}^3/\text{d} ] \text{ uptime}} \rightarrow \frac{\text{nr. operational days}}{\text{year}}$$

Production potential curve is affected by changes to the production system



$$P_o = f(N_f)$$

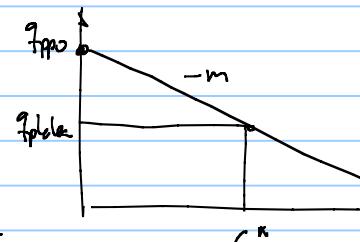
$$R_{f_1} = \frac{Q_p}{Q_1} \quad R_{f_2} = \frac{Q_p}{Q_2}$$

$$N_{f_2} < N_{f_1}$$

If we assume  $q_{pp}$  is linear  $q_{pp} = -m Q_p + q_{ppo}$

derive analytically  $q_f(t)$  from  $q_{pp}$

$$q_f(t) \begin{cases} q_{\text{plateau}} & \text{for } t \leq t_{\text{plateau}} = \left( \frac{q_{ppo}}{q_{\text{plateau}}} - 1 \right)^{-1} \\ q_{\text{field}} = q_{ppo} & \text{for } t > t_{\text{plateau}} \end{cases}$$



$$q_{\text{plateau}} = q_{ppo} = -m Q_p^* + q_{ppo}$$

$$Q_p^* = \frac{q_{ppo} - q_{\text{plateau}}}{m}$$

$$q_{pp} = -m \left( Q_p^* + \int_{t_{\text{plateau}}}^t q_{pp} dt \right) + q_{ppo}$$

$$t_{\text{plateau}} = \frac{Q_p^*}{q_{\text{plateau}}} = \left( \frac{q_{ppo}}{q_{\text{plateau}}} - 1 \right)^{-1}$$

$$q_{pp} = -m \left( \frac{q_{ppo} - q_{\text{plateau}}}{m} - m \int_{t_{\text{plateau}}}^t q_{pp} dt \right) + q_{ppo}$$

$$q_{pp} = q_{\text{plateau}} - m \int_{t_{\text{plateau}}}^t q_{pp} dt$$

→ a solution to this equation is

$$q_{pp} = q_{\text{field}} = q_{\text{plateau}} \cdot e^{-m(t-t_{\text{plateau}})}$$

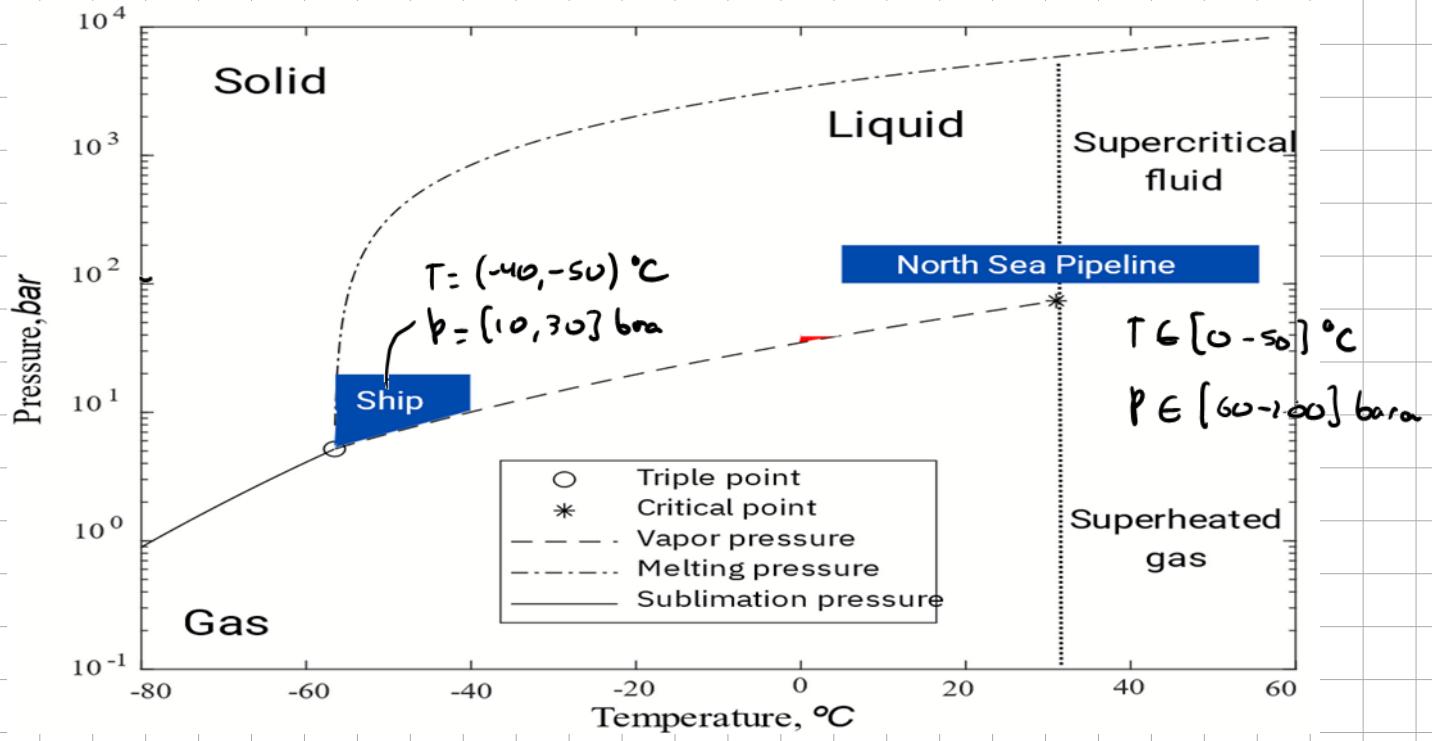
$$q_f(t) \left\{ \begin{array}{ll} q_{plateau} & \text{if } t \leq t_{plateau} = \left( \frac{q_{final}}{q_{plateau}} - 1 \right)^{\frac{1}{m}} \\ q_{plateau} e^{-m(t-t_{plateau})} & \text{if } t > t_{plateau} \end{array} \right.$$



20240229

## OUTLINE:

- CO<sub>2</sub> P-T conditions in subsea injection systems
- Injection scheduling for a subsea field (ala Snøhvit)

P-T conditions of CO<sub>2</sub> in pipeline transportation and injection using subsea wells

$z_{\text{sub}} = 2500 \text{ m}$   $1000 \text{ kg/m}^3$   $p_w = 1000 \text{ Pa/m}^3$

$\Delta p_h = \frac{g \cdot h \cdot \Delta}{1ES} = \frac{25E6}{1ES} \sim 250 \text{ bar}$

$T_{\text{Tyrobed}} = (5 - 10) \text{ }^{\circ}\text{C}$

		T [°C]						T [°C]						
		0	10	20	30	40	50	0	10	20	30	40	50	
p [bara]		50	940	587	144	125	114	105	50	1.04E-04	5.92E-05	1.66E-05	1.67E-05	1.70E-05
p [bara]		60	948	882	567	175	150	136	60	1.07E-04	8.83E-05	5.11E-05	1.79E-05	1.78E-05
p [bara]		70	955	893	808	487	201	173	70	1.09E-04	9.10E-05	7.29E-05	3.80E-05	1.92E-05
p [bara]		80	962	903	827	692	287	221	80	1.11E-04	9.36E-05	7.66E-05	5.52E-05	2.25E-05
p [bara]		90	968	912	843	743	482	288	90	1.13E-04	9.59E-05	7.97E-05	6.22E-05	3.49E-05
p [bara]		100	974	920	856	771	620	387	100	1.15E-04	9.82E-05	8.25E-05	6.66E-05	4.70E-05
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p [bara]		120	985	935	878	809	717	582	120	1.19E-04	1.02E-04	8.74E-05	7.32E-05	5.88E-05
p [bara]		130	990	942	887	823	743	635	130	1.21E-04	1.04E-04	8.96E-05	7.59E-05	6.25E-05
p [bara]		140	995	948	896	836	763	672	140	1.22E-04	1.06E-04	9.17E-05	7.84E-05	6.57E-05
p [bara]		150	1000	954	904	847	780	699	150	1.24E-04	1.08E-04	9.37E-05	8.07E-05	6.84E-05
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p [bara]		180	1012	970	925	875	819	757	180	1.29E-04	1.13E-04	9.92E-05	8.67E-05	7.54E-05
p [bara]		190	1017	975	931	883	830	771	190	1.31E-04	1.15E-04	1.01E-04	8.86E-05	7.75E-05
p [bara]		200	1021	980	937	891	840	784	200	1.32E-04	1.16E-04	1.03E-04	9.03E-05	7.94E-05

$$M_w = 1 \times 10^{-3} \text{ Pa} \cdot \text{s}$$

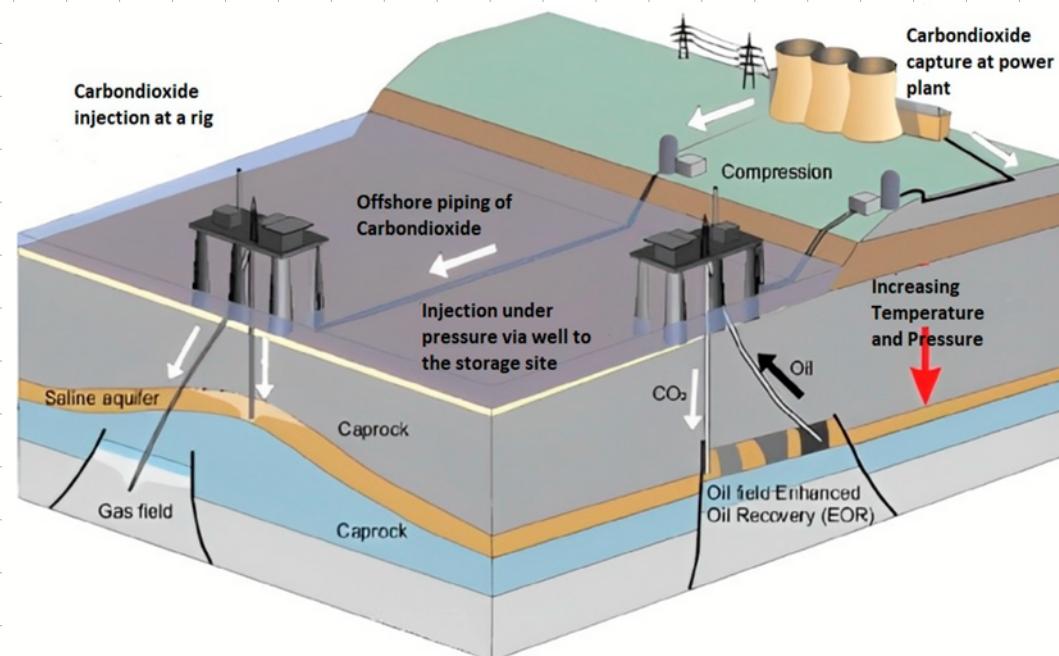
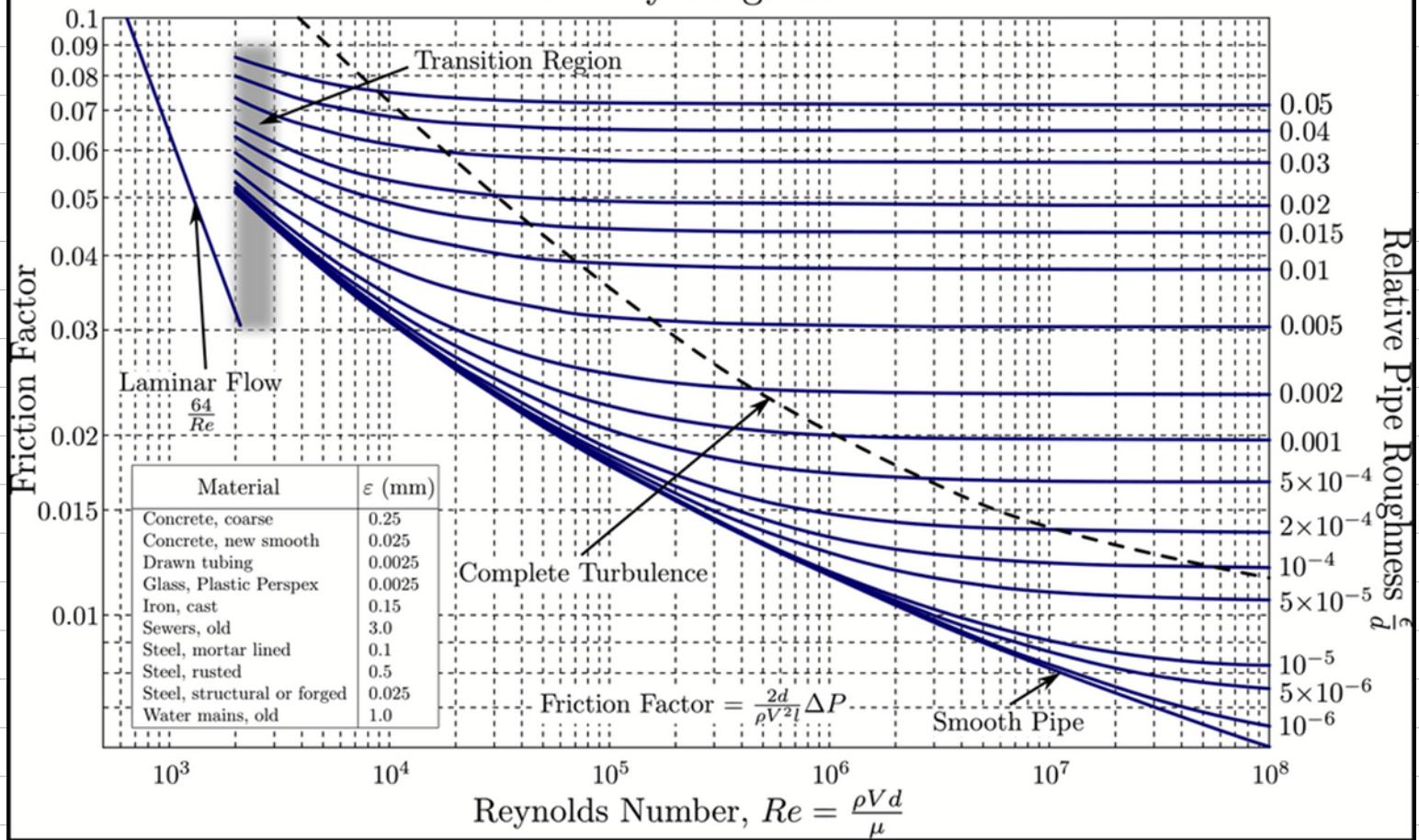
$\text{CO}_2$  in subsea injection systems has density as a liquid but viscosity as a gas

$$\Delta p = \Delta p_u + \Delta p_f$$

$$\tau_{\text{PT}} \downarrow f(\mu) \downarrow n \downarrow$$

$$t=4 \rightarrow M_3 \\ E-S$$

## Moody Diagram



<https://www.mdpip.com/2071-1050/15/8/6599>

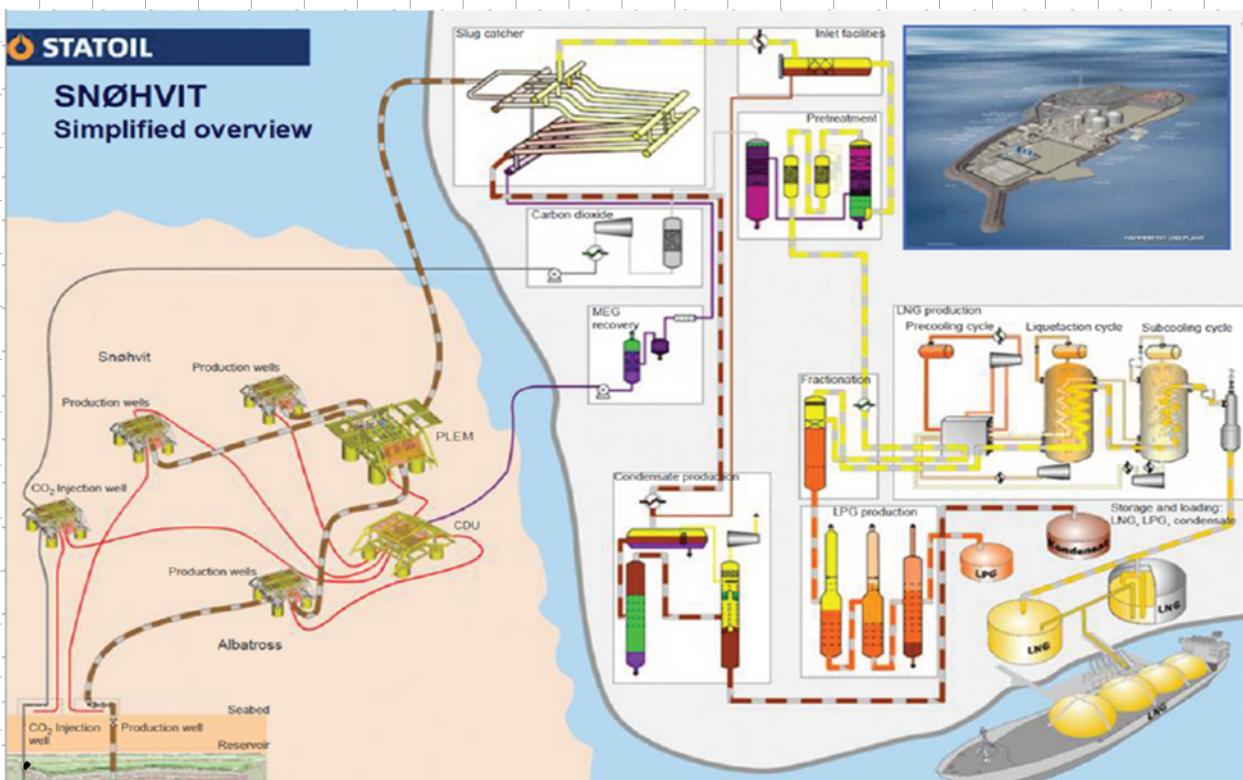
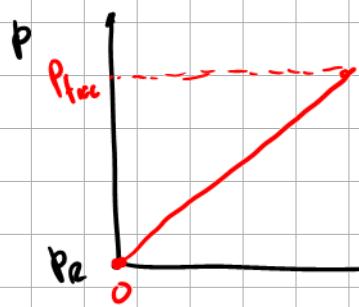


Diagram illustrating a flow system with multiple wells. The left side shows a vertical stack of wells with arrows indicating flow. A blue line labeled "PLEM" represents the liquid level in the wells. A red line represents the water level. The water level is constant across all wells. A horizontal black line at the top represents the ground surface. A blue arrow labeled  $q_f$  points downwards from the ground surface towards the wells. A red arrow labeled  $q_t$  points upwards from the wells towards the ground surface. A blue arrow labeled  $q$  points upwards from the bottom well. A red arrow labeled  $q$  points downwards from the top well. Labels include "W0" at the top right, "Piture" and "G" near the ground surface, "Piture required", "Ab", and "q". Text in the center says "all wells are identical" and "no wellbore chores". A small graph shows pressure ( $P$ ) versus time ( $t$ ).

$$IPR \text{ for liquid} \quad P_{sat}^{pr} \xrightarrow{\text{gas}} \left( \frac{P_g}{P_{sat}} = C_2 (P_a^2 - P_{sat}^2)^n \right)$$

(inflow performance relationship)

injection performance  
relationship



Pray (to avoid fracturing the reveror)

$$q_{\text{CO}_2} = \underbrace{\left( \frac{P_{\text{sat}} - P_e}{S_{\text{sat}}/d} \right)}_{\text{bar}} \text{ bar}$$

$t/d$  mass units

$$\text{J} \left[ \frac{s_{\text{av}}}{d/b_{\text{ave}}} \right] \xrightarrow{\quad} \left[ \frac{t/d}{b_{\text{ave}}} \right]$$

$$s_{\text{av}} \rightarrow h_g$$

$$\text{J} \cdot \underbrace{s_{\text{CO}_2}}_{\sim} = \text{J}_{\text{mole}}$$

$$\hookrightarrow 1.8 \text{ kg/m}^3$$



$$q_{sc} = \left( \frac{\pi}{4} \right) \cdot \left( \frac{R}{M_{\text{air}}} \right)^{0.5} \cdot \left( \frac{T_{sc}}{p_{sc}} \right) \cdot \left( \frac{D^5}{f_M \cdot L \cdot \gamma_g \cdot Z_{av} \cdot T_{av}} \right)^{0.5} \cdot \left[ \left( p_{wf}^2 - p_t^2 \cdot e^S \right) \cdot \left( \frac{S}{e^S - 1} \right) \right]^{0.5}$$

$$C_T = \left( \frac{\pi}{4} \right) \cdot \left( \frac{R}{M_{\text{air}}} \right)^{0.5} \cdot \left( \frac{T_{sc}}{p_{sc}} \right) \cdot \left( \frac{D^5}{f_M \cdot L \cdot \gamma_g \cdot Z_{av} \cdot T_{av}} \right)^{0.5} \cdot \left( \frac{S \cdot e^S}{e^S - 1} \right)^{0.5}$$



$$S = 2 \cdot L \cdot C_a = 2 \cdot \frac{M_g}{Z_{av} \cdot R \cdot T_{av}} \cdot L \cdot g \cdot \cos(\alpha)$$



angle with respect  
to:

$$\cos(180^\circ) = -1$$

Properties taken from the website of NIST

<https://webbook.nist.gov/cgi/cbook.cgi?ID=C124389&Mask=4>

$$V_{R,CO_2} = \frac{n_{inj} \cdot R \cdot Z_R \cdot T_R}{p_R}$$

$$V_{R,CO_2} = c_e \cdot V_{T,i} \cdot (p_R - p_{Ri})$$

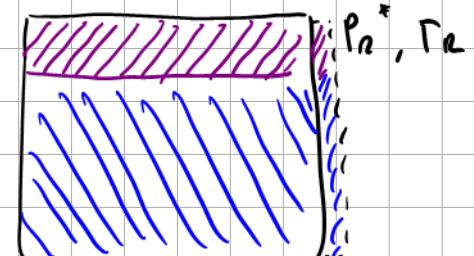
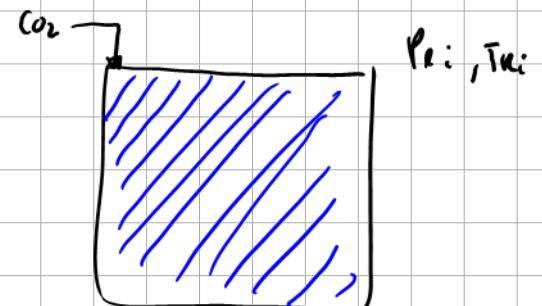
$$\frac{n_{inj} \cdot R \cdot Z_R \cdot T_R}{c_e \cdot V_{T,i} \cdot p_R} = (p_R - p_{Ri})$$

$$p_R^2 - p_{Ri} \cdot p_R - \frac{m_{inj} \cdot \bar{R} \cdot Z_R \cdot T_R}{c_e \cdot V_{T,i}} = 0$$

$$p_R = \frac{p_{Ri} \pm \sqrt{p_{Ri}^2 + 4 \cdot \frac{m_{inj} \cdot \bar{R} \cdot Z_R \cdot T_R}{c_e \cdot V_{T,i}}}}{2}$$

The physical solution is the positive, then

$$p_R = \frac{p_{Ri} + \sqrt{p_{Ri}^2 + 4 \cdot \frac{m_{inj} \cdot \bar{R} \cdot Z_R \cdot T_R}{c_e \cdot V_{T,i}}}}{2}$$



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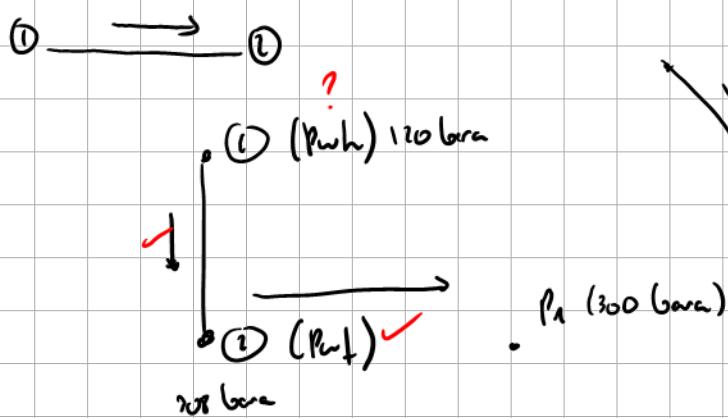
## OUTLINE

- Ala Snohvit CO<sub>2</sub> injection scheduling (cont)
  - Intro to Class exercise: CO<sub>2</sub> injection network

Exhibit a CO<sub>2</sub> injection well  $q_{CO_2,well} = 1.5 \text{ EOB t/g}$

$$\text{in von exerce } q_{\text{field}, w_2} = 18000 \text{ t/d} \xrightarrow{\cdot 365} 6.57 \times 10^6 \text{ t/y}$$

$$q_{\text{well,cor}} = \frac{q_{\text{field,cor}}}{q} = 0.7 \text{ coul by}$$



$$P_{wh} = P_{wh} + \Delta b_4 - \Delta b_f$$

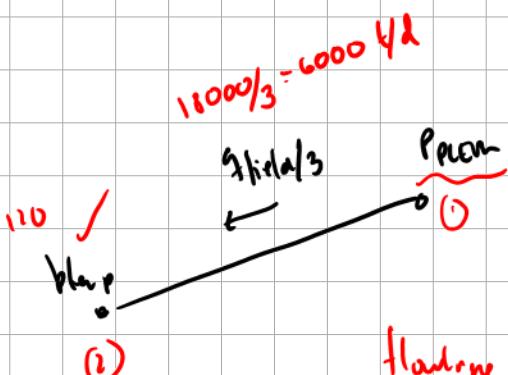
$$\int_{C_2} g \cdot h$$

~216 lava - Aft

$$P_{wh} = P_{wf} - \underline{\delta b_{w4}} + \delta p_f$$

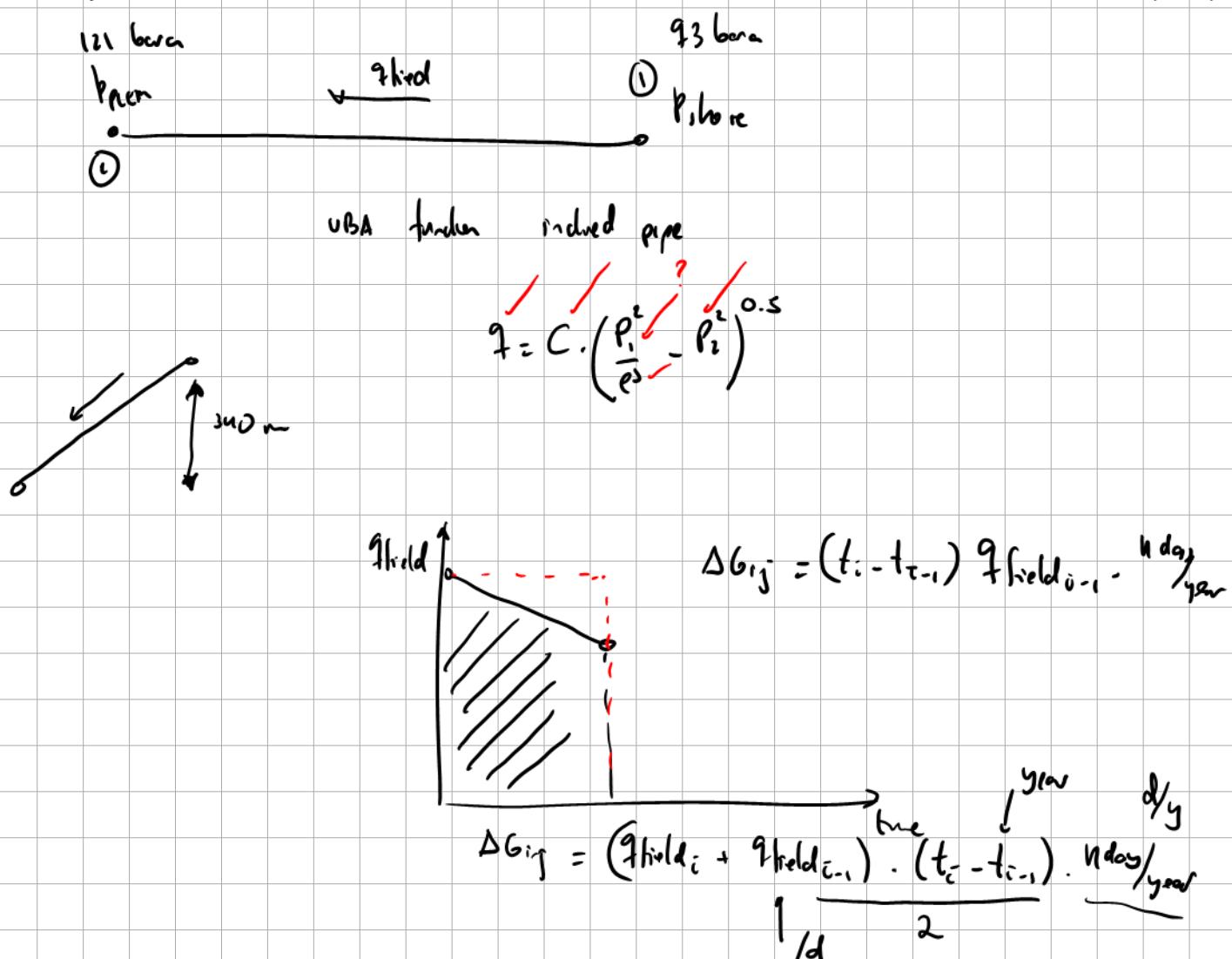
$$170 = 308 + 216 +$$

$$\Delta p_1 = 28 \text{ bars}$$

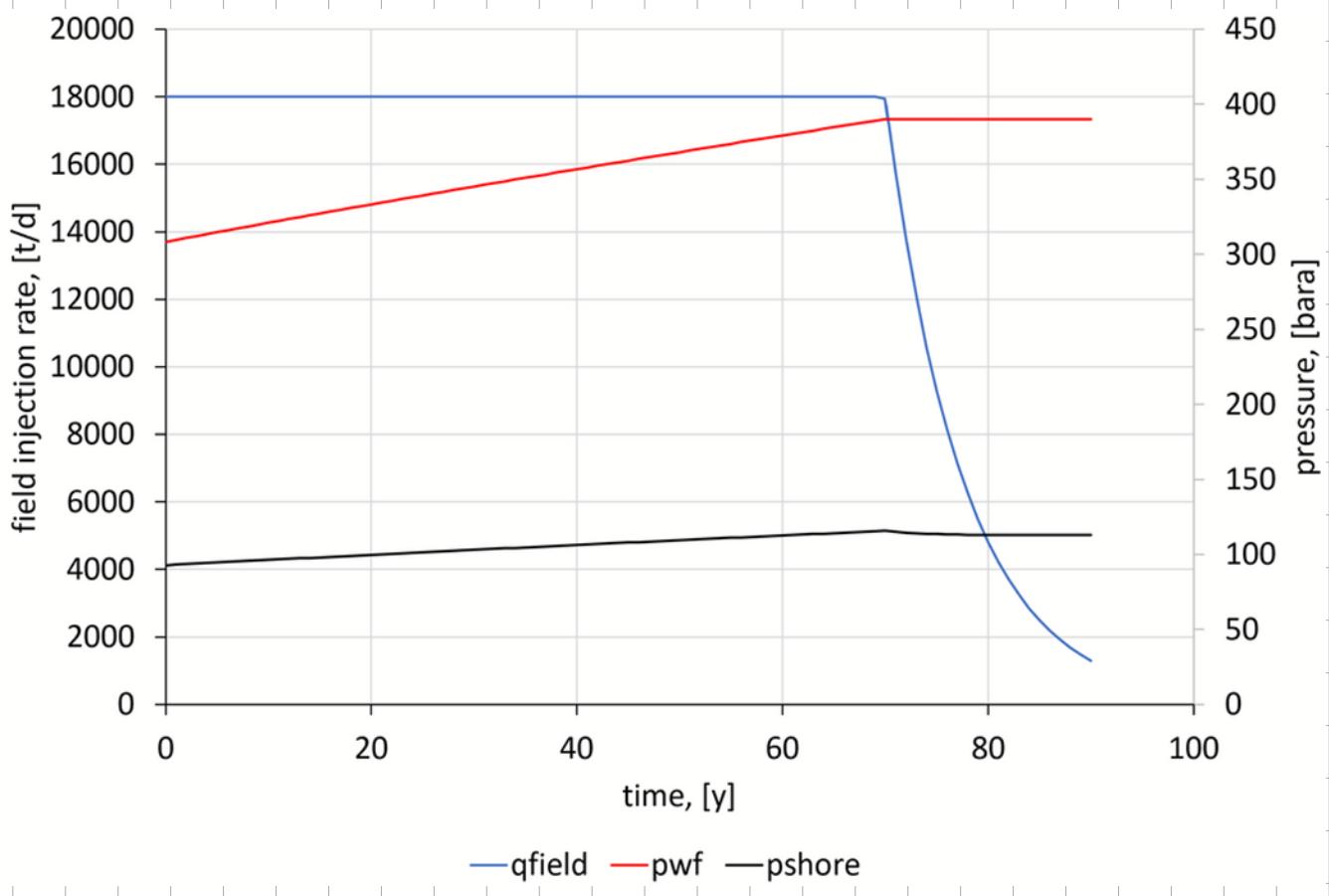


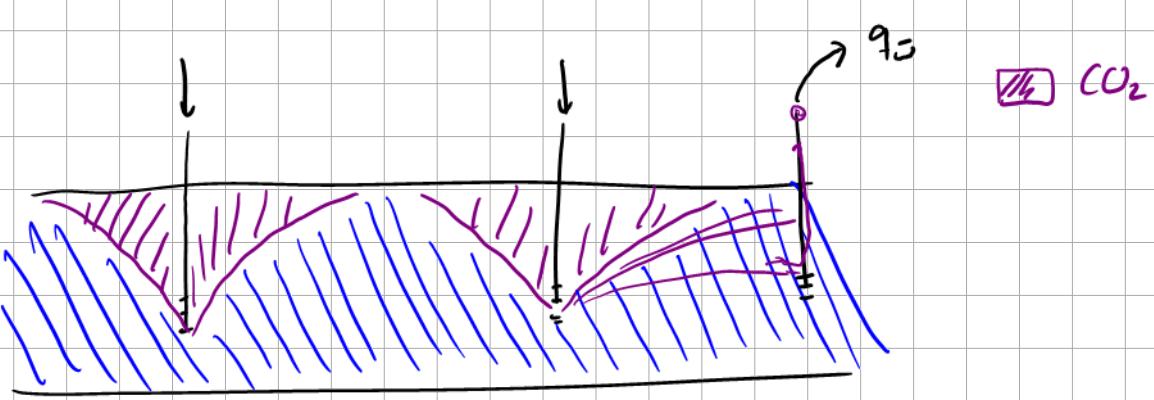
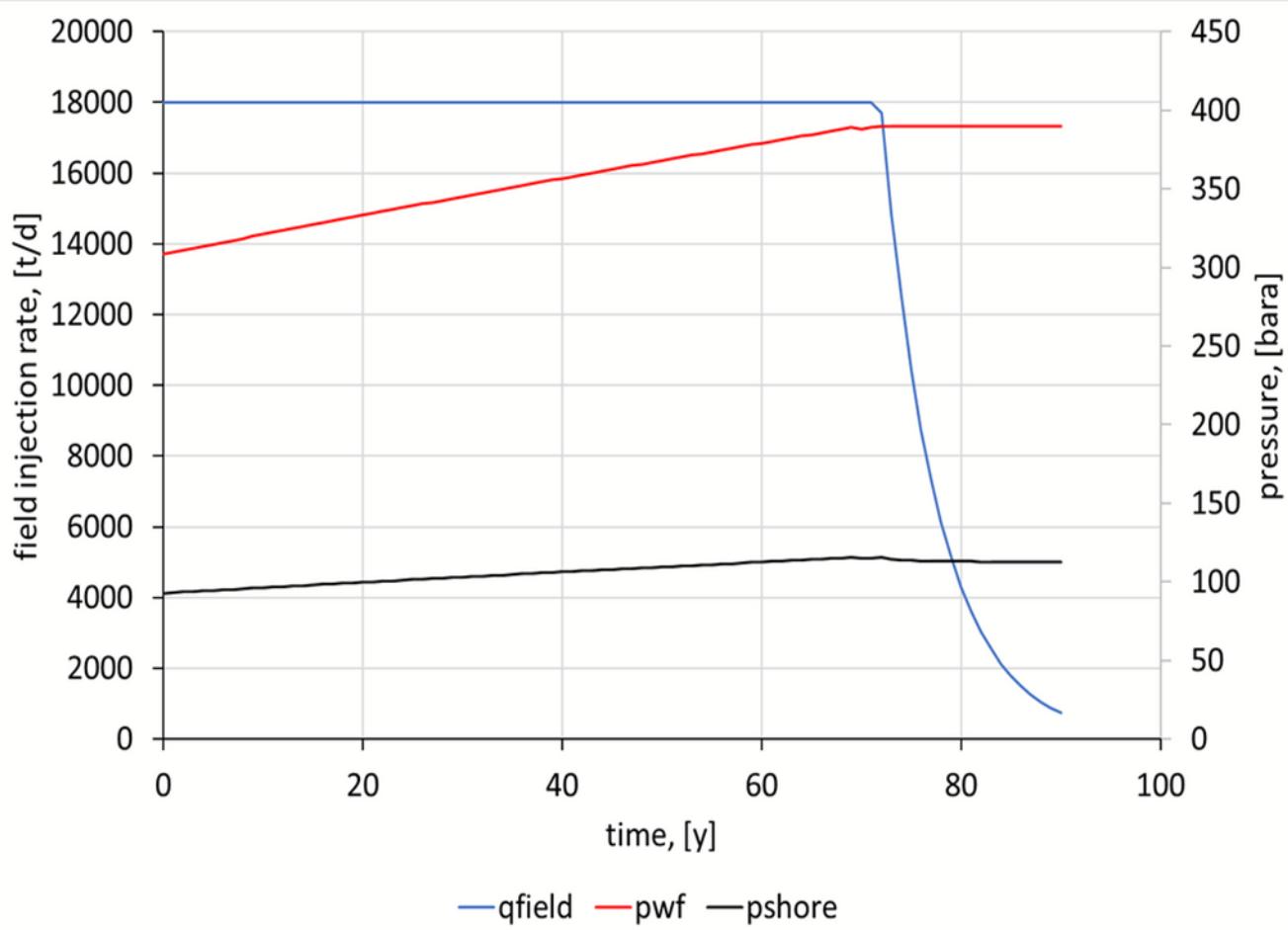
$$q = C_{FL} \left( \frac{P_i^2 - P_j^2}{P_i^2} \right)^{0.5}$$

VBA func line p.



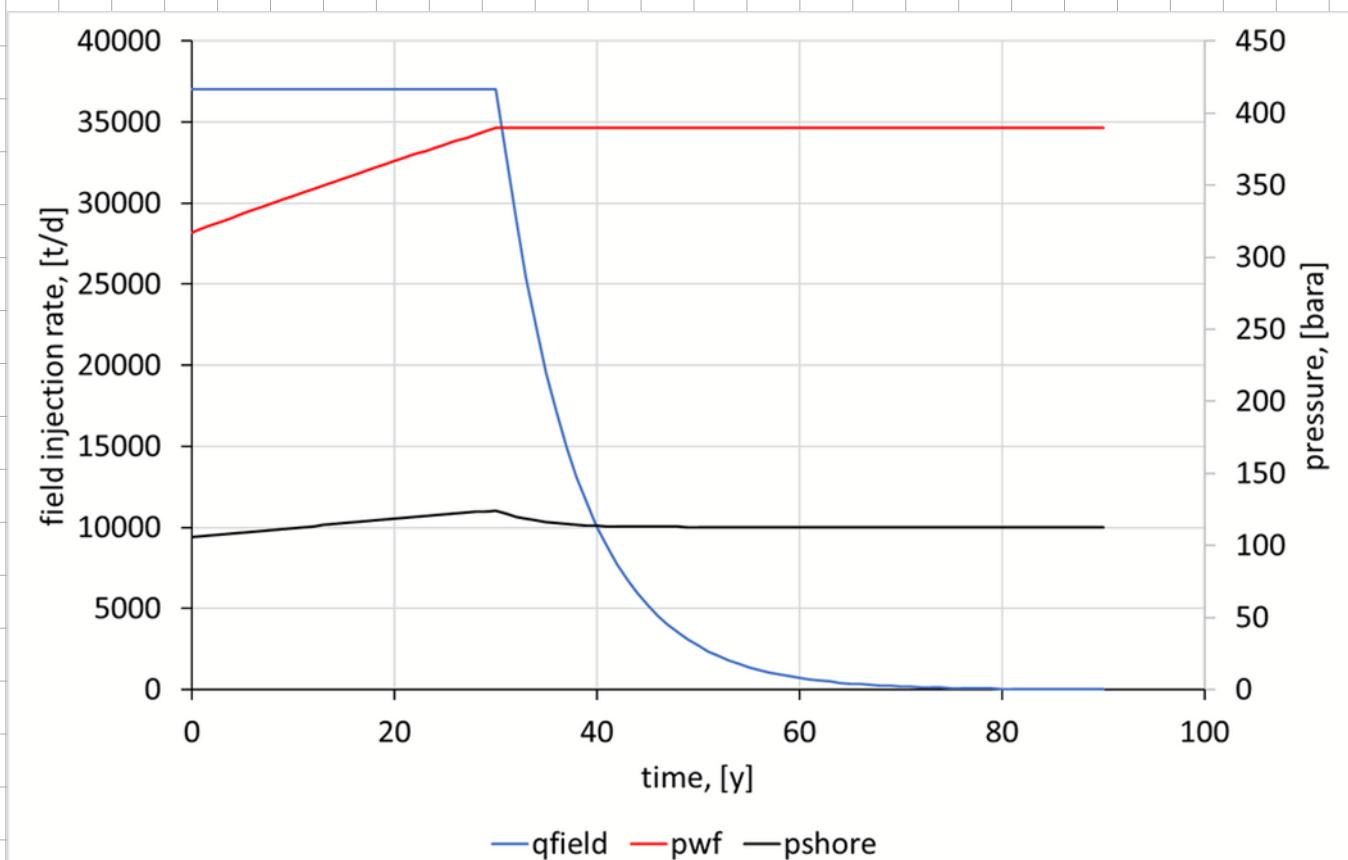
$$q_{field} = 18000 \text{ t/d, 9 wells}$$





drilling water producers to maintain reservoir pressure limited.

$$\text{Using Eanor dong} \quad q_{\text{field}} = 1.5 \times 6 \frac{\text{t}}{\text{g}} \cdot 9 = 13.5 \times 0.6 \frac{\text{t}}{\text{g}} \rightarrow \\ \sim 37000 \frac{\text{t}}{\text{d}}$$



$$NPV_{calc} = \sum_{i=0}^N \frac{C_{Fi}}{(1+d)^i}$$

$$C_{Fi} = \underbrace{\text{revenue}_i}_{\sim} - \underbrace{\text{expenses}_i}_{\sim}$$

$$\Delta G_{ij} = \text{Price of disposal of CO}_2 \\ \frac{\text{USD}}{t} \quad \frac{\text{NOK}}{t}$$

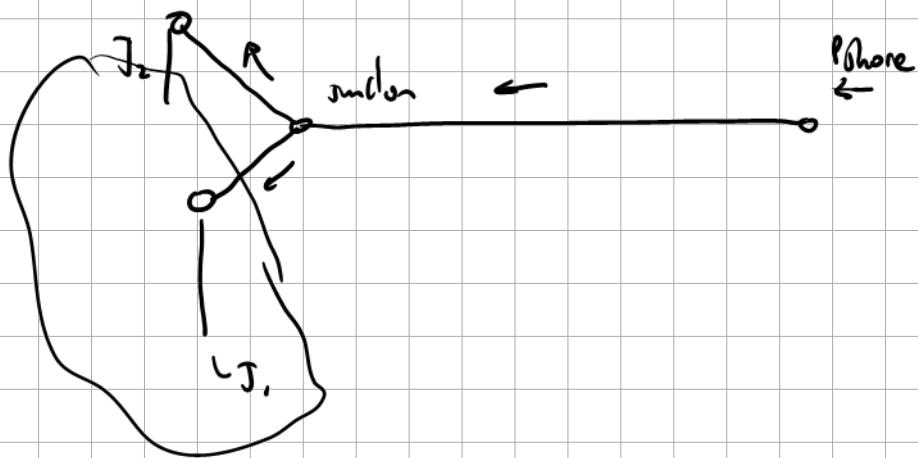
", more than half of onshore storage capacity is estimated to be available below USD 10/t CO<sub>2</sub>

$$\underbrace{10 \text{ USD}}_t \cdot 13 \text{ E06 t} = \underbrace{130 \text{ E06 USD}}_t / y$$

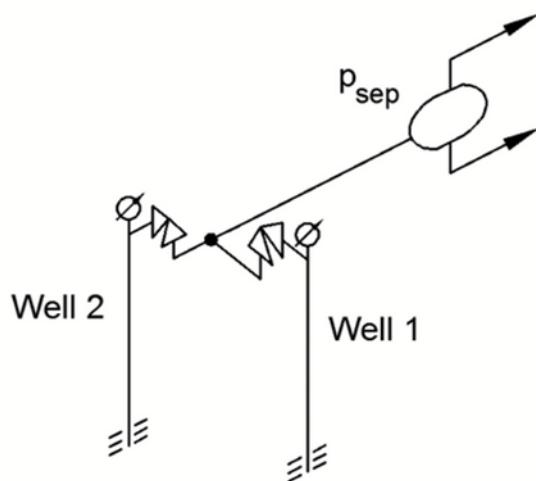
$$\text{Expenses}_i = \text{Drill}_i + \text{Subsea}_i + \text{OPEx}_i$$

Drill       $\underbrace{\text{Subsea}}_{\substack{\text{Well cost each} \\ \text{well}}} \quad \underbrace{\text{OPEx}}_{\substack{\text{flowline} \\ \text{PLM} \\ \text{template}}}$   
 maintenance  
 power requirement

Network solving for CO<sub>2</sub> injection system



### Network solving in a CO<sub>2</sub> injection network



Using the Excel file provided, and using the learnings from the dry gas network videos, perform the following calculations

1. Sheet “no choke\_field rate given”: given a desired field injection rate, calculate flow rate injected per well with fully open chokes (natural flow).
2. Sheet “no choke\_shore pressure given”: given a shore pressure, calculate field injection rate and flow rate injected per well with fully open chokes (natural flow).
3. Sheet “choke\_field well rate psh given”: calculate choke pressure drop in each well to produce the well rates indicated and with the shore pressure provided.

How to deal with quantity uncertainty in field development

for example in our Snøhvit case

$$\hookrightarrow G, N \quad , \quad q_g = C_p (P_g^2 - P_{gw}^2)^n$$

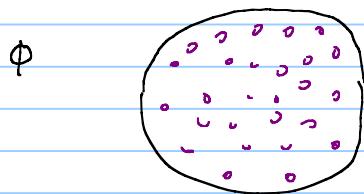


$$\text{uptime } \frac{90 - 100}{365} \text{ (nr days producing in year)}$$

- ↳ cause additional OPEX
- ↳ cut in production  $\rightarrow$  cut in revenue

input variables used in engineering studies in FD are highly uncertain

$\phi_{min} \leq \phi \leq \phi_{max}$  and affect the value of KPIs that are used to discriminate and select development alternatives.



number sample	$\phi$
-	-
-	-
-	-
-	-

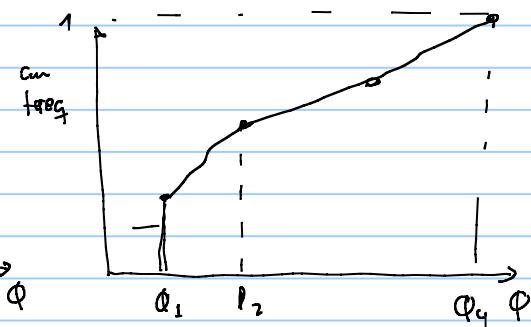
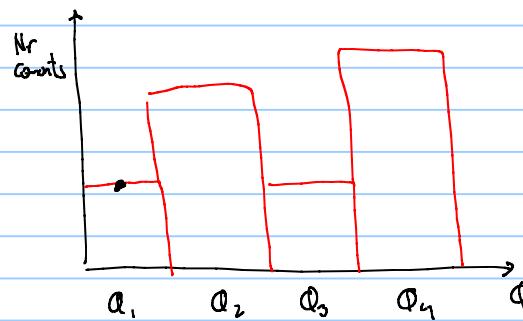
discrete frequency analysis

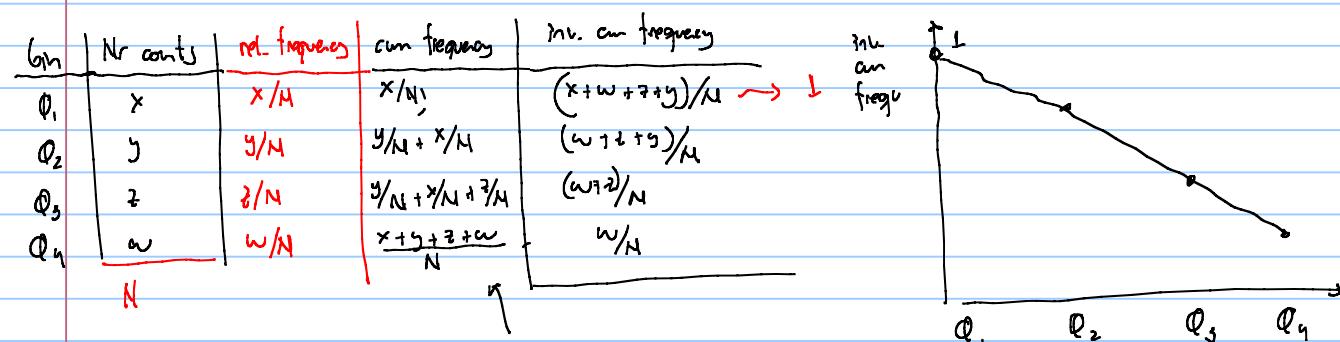
create bins mm  $\underline{\phi_1 (0.15)}$  if  $\phi_i = 0.18$

$\phi_2 (0.20) \leftarrow \phi_i \leq \phi_i \leq \phi_2$

$\phi_3 (0.25)$  if  $\phi_i < \frac{(\phi_2 - \phi_1)}{2} + \phi_1 \rightarrow$  counted as part of  $\phi_1$

max  $\phi_4 (0.30)$





how to do frequency analysis in excel :

	A	B	C	D	E	F	G
1	Variable			min	1		
2	10			max	10		
3	7			Nr bins	5		
4	2			delta	2.25		
5	6						
6	1			bins	nr counts		
7	8			1	4		
8	1			3.25	4		
9	7			5.5	1		
10	3			7.75	3		
11	9			10	7		
12	1						
13	4						
14	8						
15	2						
16	8						
17	1						
18	9						
19	3						
20	10						
..							

to create bins :

find max

find min

define Nr bins

$$\text{calculate delta} = \frac{\text{max} - \text{min}}{(\text{Nr bins} - 1)}$$

compute each bin

$$\text{bin}_i = \text{bin}_{i-1} + \text{delta}$$

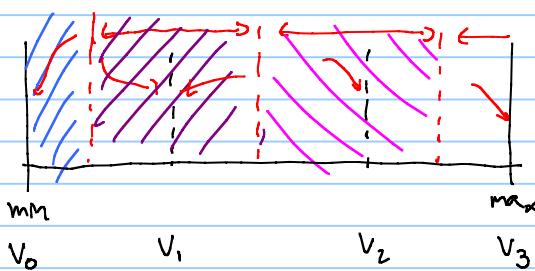
starting from  $\text{bin}_0 = \text{min}$

to apply frequency function:

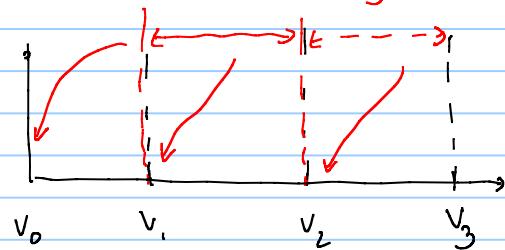
ctrl + shift + enter (in sequence and leave it pressed)

Selecting bins must take into account

- o nr data points



be careful how the frequency is accounted for



what happens if there are no measurements?

frequency  $\rightarrow$  probability

nd frequency  $\rightarrow$  pdf probability density function

cum frequency  $\rightarrow$  cdf cumulative distribution function

poor boy, no data pdf  $\phi$  continuous probability



$$A_{\text{min}} = (\phi_{\text{max}} - \phi_{\text{min}}) \cdot p_1 = 1$$

$$p_1 = \frac{1}{(\phi_{\text{max}} - \phi_{\text{min}})}$$

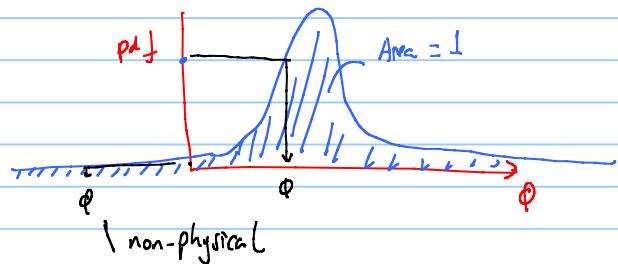
Continuous distributions are advantageous because:

- There is an analytical expression
- I need only few values to define the distribution
- There is no data to determine a discrete distribution

*Warning: many continuous distributions go from  $-\infty \rightarrow +\infty$*

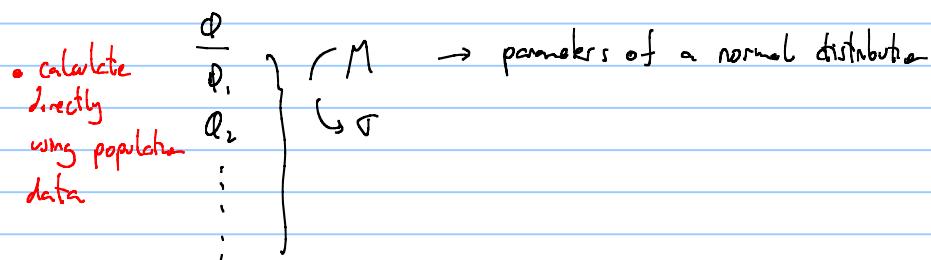
There are many parameters in FD that exhibit typical distributions:

- cost ---Normal
- Porosity --- Normal
- Initial oil/gas in place --- Log Normal

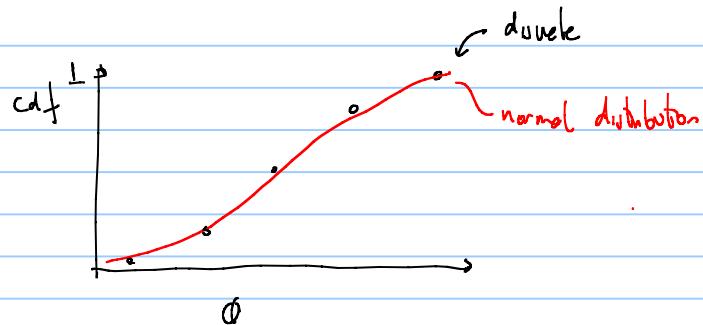


so bounding is necessary

discrete distribution  $\rightsquigarrow$  continuous distribution



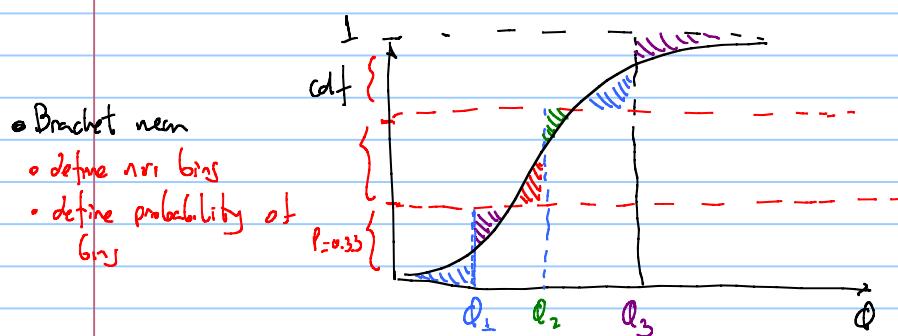
• tune parameters in the continuous distribution to represent the discrete distribution



$$\frac{1}{\sigma\sqrt{2\pi}} e^{-\frac{1}{2} \left(\frac{x-\mu}{\sigma}\right)^2}$$

change  $\mu, \sigma$  until diff discrete  
and continuous is minimal

continuous distribution  $\rightarrow$  discrete distribution



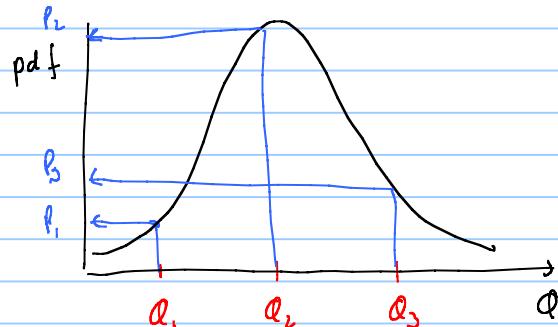
$\Phi$	P
$\Phi_1$	0.33
$\Phi_2$	0.33
$\Phi_3$	0.33

find  $\Phi_1$ , such that  $\boxed{P} = \boxed{0.33}$

• value discretization

• pick nr. bins in  $\Phi$

• read probabilities from pdf



$\Phi$	P
$\Phi_1$	$p_1^*$
$\Phi_2$	$p_2^*$
$\Phi_3$	$p_3^*$

• Normalize probabilities using the sum

$$p_1^* = \frac{p_1}{p_1 + p_2 + p_3}$$

$$p_2^* = \frac{p_2}{p_1 + p_2 + p_3}$$

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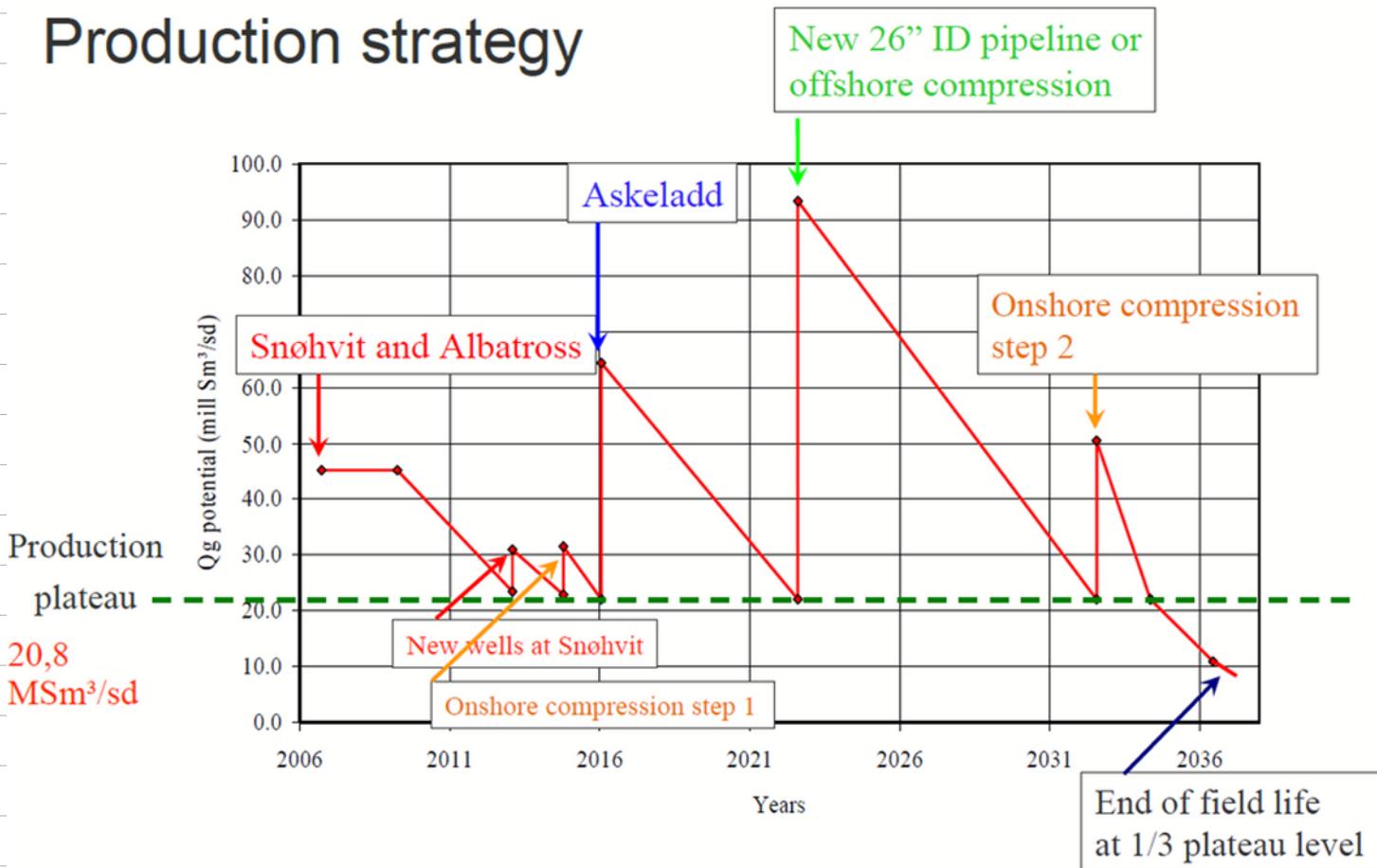
## Outline:

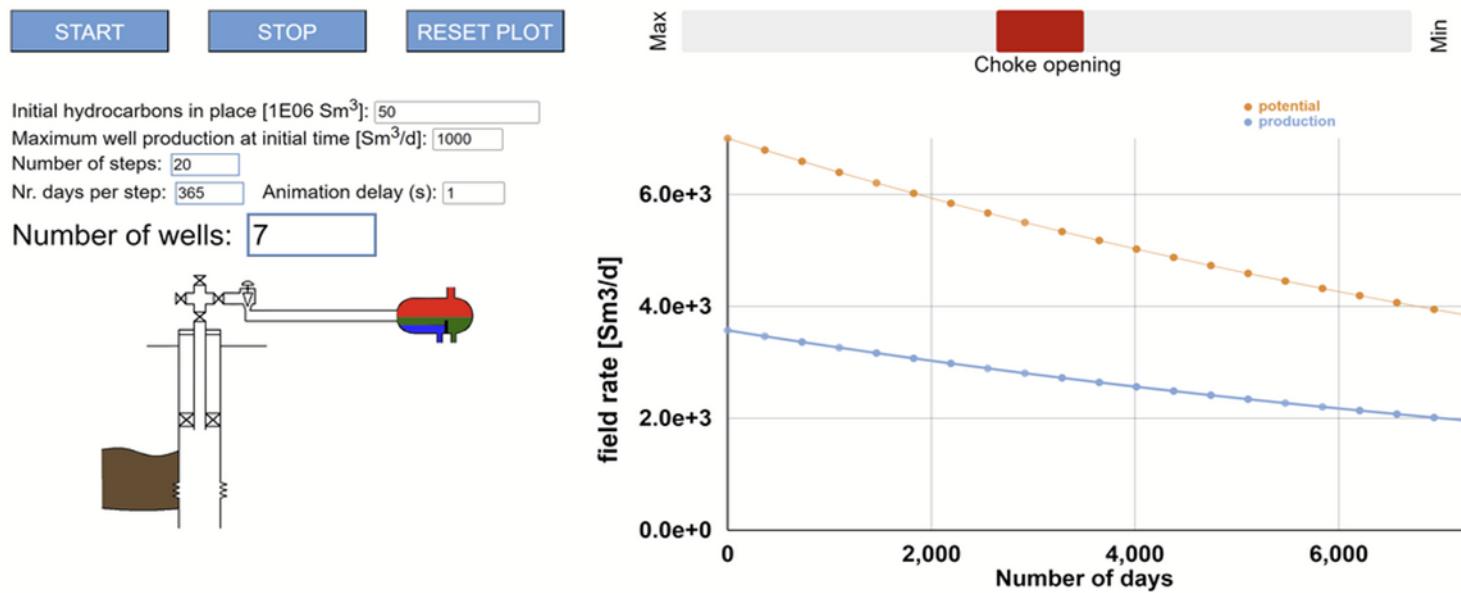
- Recap on video lecture: production potential
- Production potential exercise

## Information:

- 2nd meeting of reference group today after class
- Changing the deadline of mandatory exercise set 3 for next week (Thursday)?

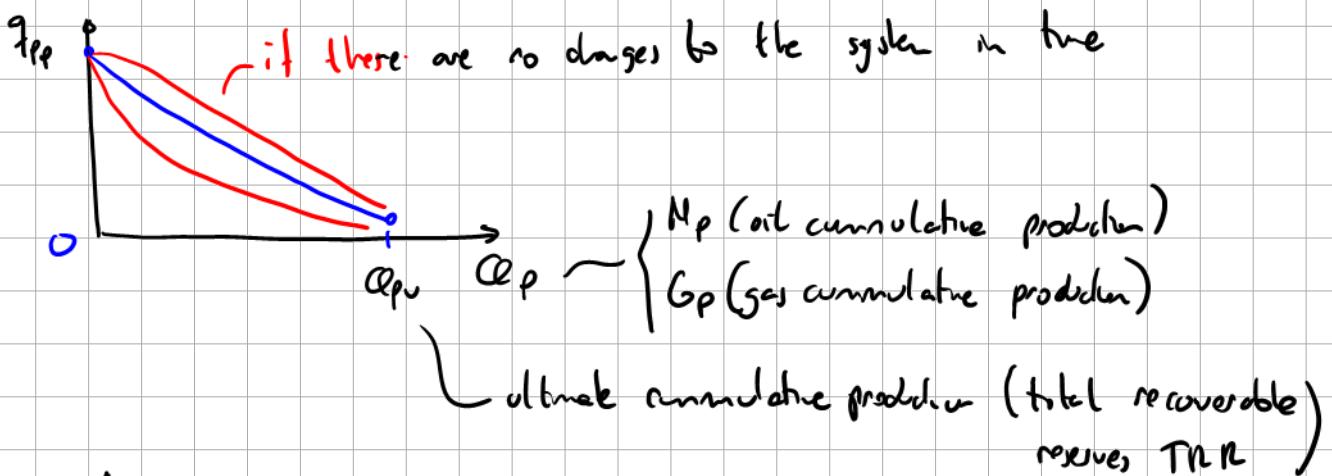
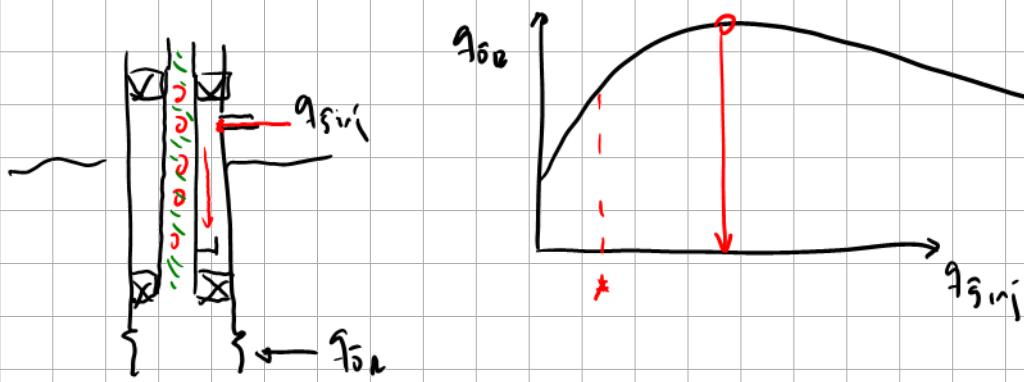
# Production strategy





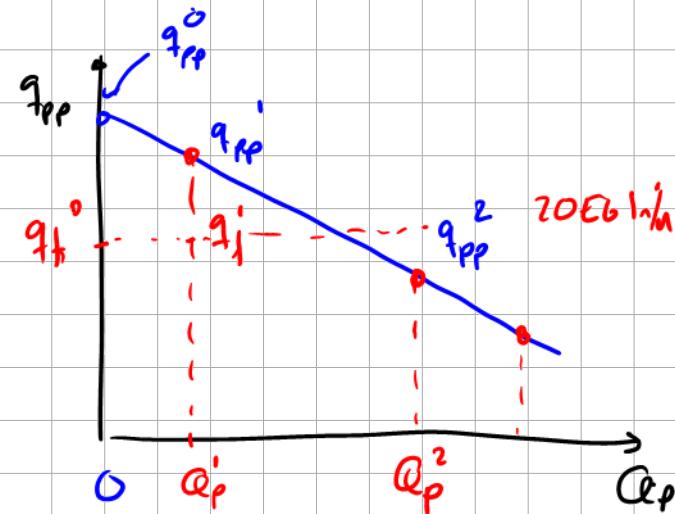
I could be operating below potential and still be in decline (mode B), for example:

- To limit the maximum well rate to avoid erosion, wellbore stability issues, sand production
- We might not know that we are not at potential (it is trivial for wells with chokes, but for e.g. gas lift, we need to find the maximum mathematically)

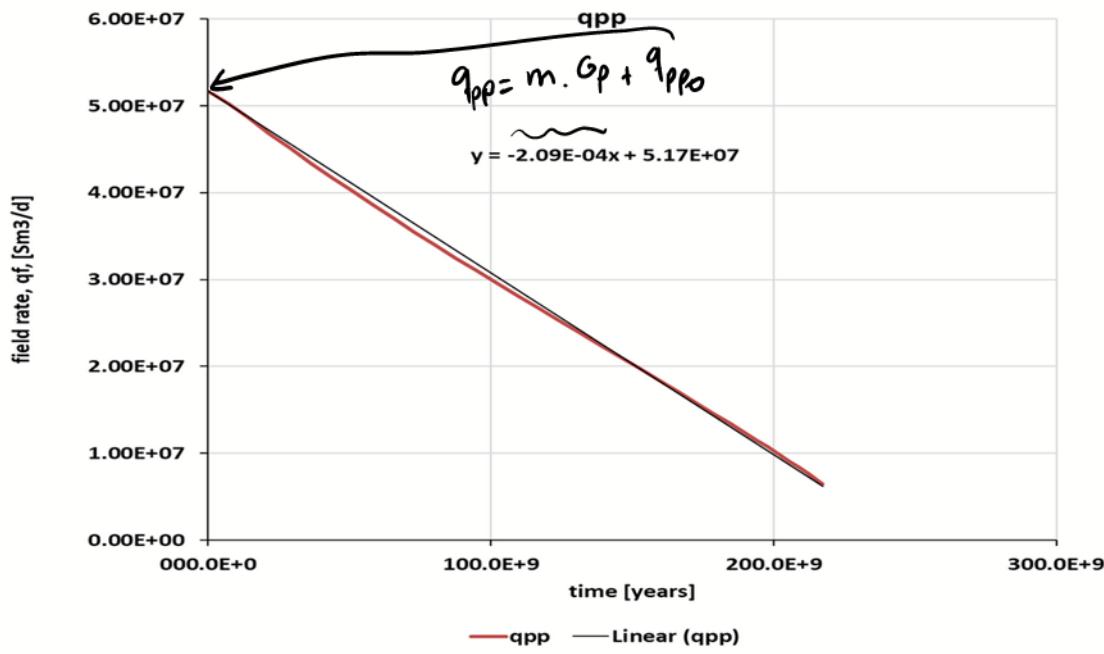
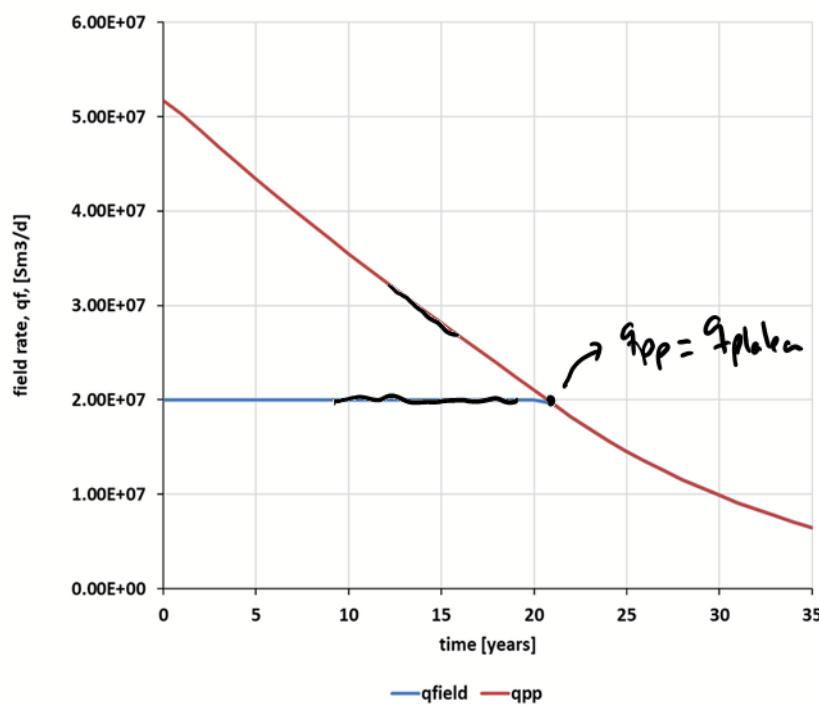


Production potential curves can be used to calculate production profiles!

time	$q_{\text{field}}$	$q_{\text{pp}}$	$Q_p$
0	$q_j^0$	$q_{\text{pp}}^0$	0
1	$q_j^1$	$q_{\text{pp}}^1$	$Q_p^1 = q_j^0 + q_{\text{pp}}^0 (1 - \alpha) N_{\text{days}} / t = q_j^1$
2	$q_j^2$	$q_{\text{pp}}^2$	$Q_p^2 = q_j^1 + q_{\text{pp}}^1 (2 - 1) N_{\text{days}} = q_j^2$
	$q_j^3$	$q_{\text{pp}}^3$	



For the Snowwhite field:



### PROBLEM 1. (25 POINTS)

The Mnazi Bay is a gas field located in the south-eastern shores of Tanzania. The field will be produced with standalone vertical wells to a gas processing center (dehydration and refrigeration). The gas will be sent further via pipeline to feed the main power plant in Dar es Salaam, a local power plant in Mtwara/Lind and a Urea and Cement plant.



1. Estimate the minimum number of wells required to produce in plateau for 10 years with a field rate of  $2.5 \times 10^6 \text{ Sm}^3/\text{d}$ . Determine the exact plateau duration (in days).
2. Using the results from question 1, and assuming that the minimum economic rate (field abandonment rate) is  $0.2 \times 10^6 \text{ Sm}^3/\text{d}$ , what is the ultimate recovery factor expected from the field?
3. The values of  $q_{ppo,well}$  and  $G$  are highly uncertain. Experts have estimated that they may vary within the ranges described below.

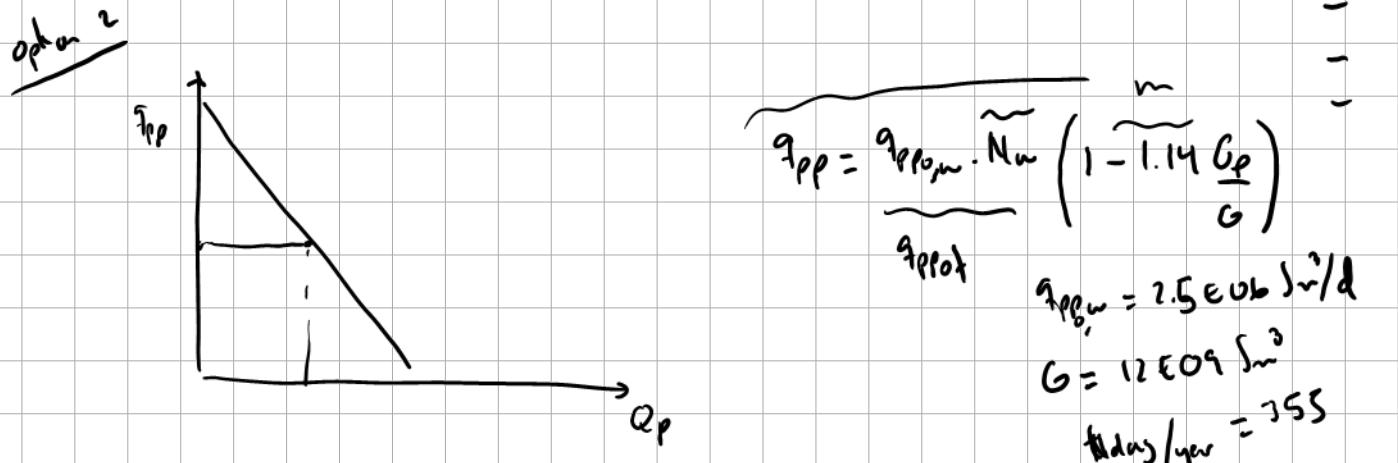
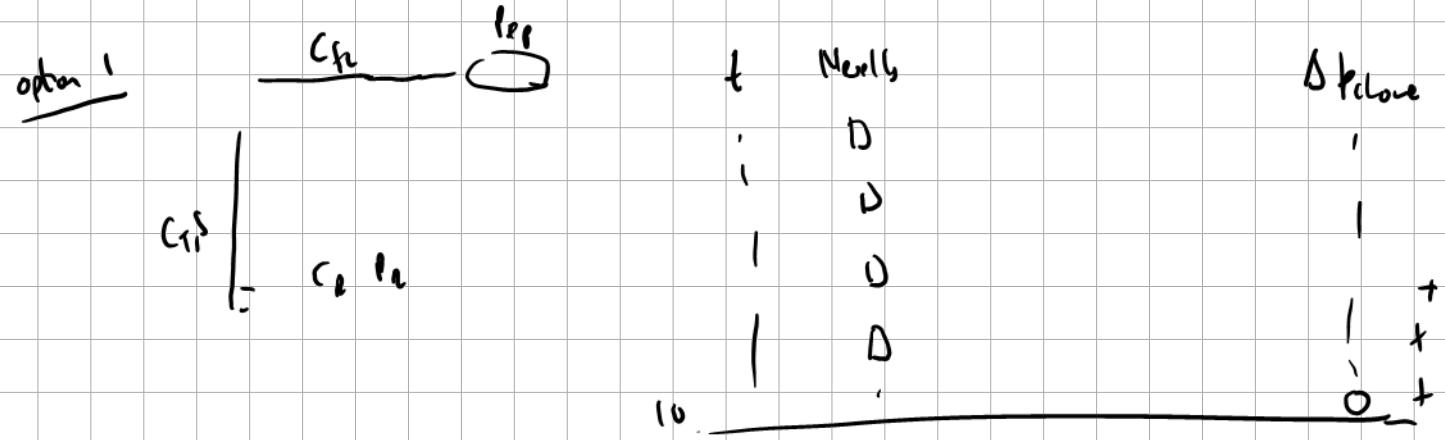
	min	max
$q_{ppo,well} [10^6 \text{ Sm}^3/\text{d}]$	2	3
$G [10^9 \text{ Sm}^3]$	11	18

Considering these uncertainties, and using a conservative approach, determine the number of wells needed to ensure the field delivers a reservoir plateau rate of  $2.5 \times 10^6 \text{ Sm}^3/\text{d}$  for at least 10 years.

$$t_{plateau} > 10 \text{ years}$$

$$t_{plateau} = ?$$

$$q_{field} = 7.5 \times 10^6 \text{ Sm}^3/\text{d}$$



at plateau end  
 $G_p^*$ ,  $10 \cdot q_{plateau} \cdot 365 = 8.875 \text{ E } 7 \text{ Sm}^3$

$\frac{1}{2.5 \text{ E } 06}$

at plateau end ( $G_p^*$ )  $q_{pp} = q_{plateau}$

$$q_{plateau} = q_{pp,0,w} \cdot N_w \cdot \left( 1 - 1.14 \cdot \frac{G_p^*}{G} \right)$$

$$\frac{\frac{7.5 \text{ E } 06}{2.5 \text{ E } 06}}{1 - 1.14 \left( \frac{8.875}{12} \right)} = \frac{1}{0.1569} = N_w$$

$$6.32 = N_w$$

$\boxed{N_w = 7}$

$$q_{pp} = q_{pp,0,w} \cdot N_w \left( 1 - 1.14 \cdot \frac{G_p^*}{G} \right) \quad 12 \text{ E } 09$$

$$\text{end of plateau occurs at } G_p^* = \left(1 - \frac{q_{pp}}{q_{ppo,w} \cdot N_w}\right) \frac{1}{1.14} \cdot G$$

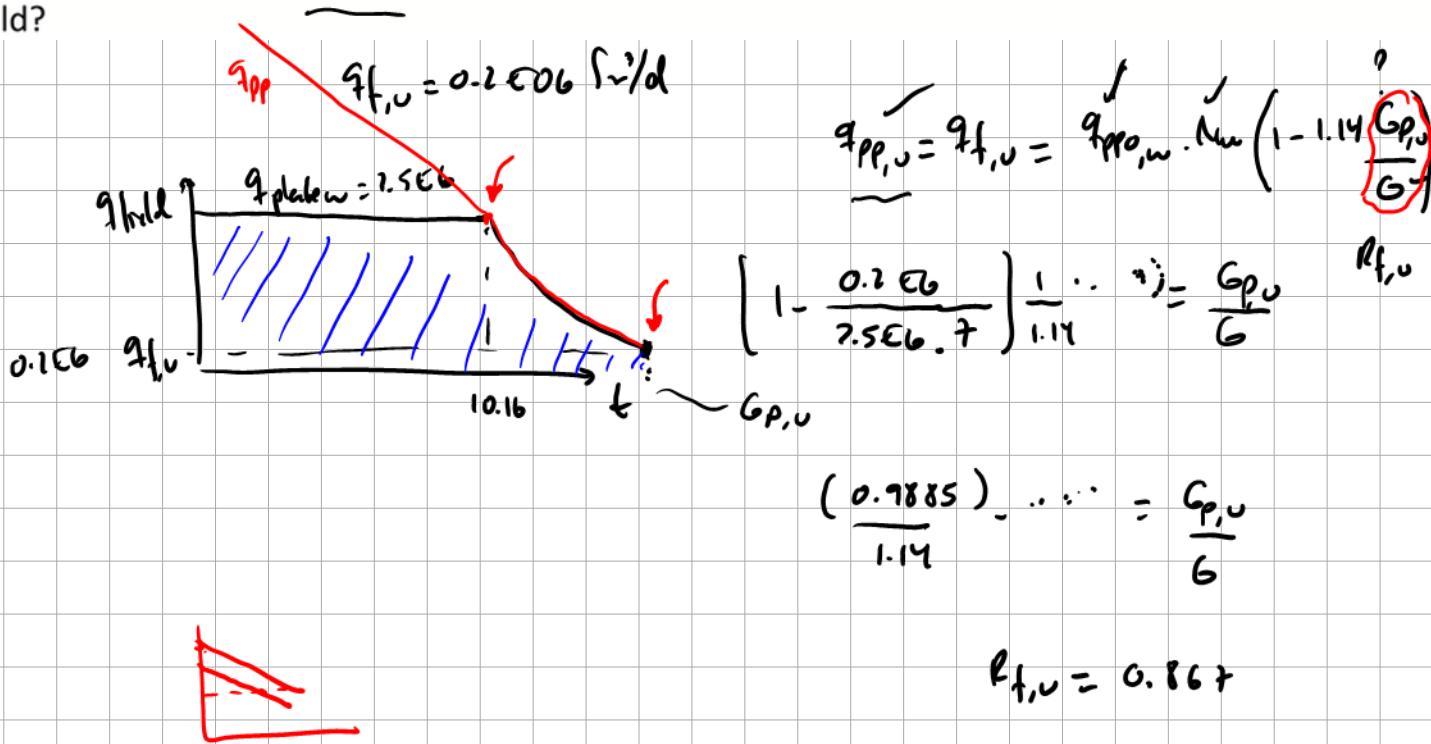
$$G_p^* = \left(1 - \frac{1}{7}\right) \frac{1}{1.14} \cdot 12 \text{ E9}$$

$$G_p^* = \left(\frac{6}{7} \cdot \frac{12}{1.14}\right) = 9.02 \text{ E9 Sm}^3$$

$$G_p^* = t_{plateau} \cdot q_{plateau} \cdot \text{Mday/year}$$

$$\frac{9.02 \text{ E9}}{7.5E06 \cdot 355} = t_{plateau} \rightarrow t_{plateau} = 10.16 \text{ y}$$

2. Using the results from question 1, and assuming that the minimum economic rate (field abandonment rate) is 0.2 E06 Sm3/d, what is the ultimate recovery factor expected from the field?



3. The values of  $q_{ppo,w}$  and  $G$  are highly uncertain. Experts have estimated that they may vary within the ranges described below.

2 - 2.5

$$\underline{q_{ppo,w}} = \underline{q_{ppo,w}} \cdot N_w$$

2.5

2

	min	max
$q_{ppo,w}$ [1E06 Sm <sup>3</sup> /d]	2	3
$G$ [1E09 Sm <sup>3</sup> ]	11	18

Considering these uncertainties, and using a conservative approach, determine the number of wells needed to ensure the field delivers a reservoir plateau rate of 2.5 E6 Sm3/d for at least 10 years.

repeat question 1 with  $G=11 \text{ E09}$ ,  $q_{ppo,w}=2$

$$\dot{q}_{\text{plateau}} = \frac{\dot{q}_{\text{PP0,w}}}{2} \cdot N_w \cdot \left( 1 - 1.14 \cdot \frac{G^*}{G} \right) \quad 88 \text{ tsc'9}$$

{20% produksjon  
7.5 → 2  
12 → 11  
7 → 16 2x}

$$N_w = \frac{1.25}{0.08} = 15.6 \approx 16$$

4. Using the results from Task 1, compute the NPV of the project. Consider **only** the revenue from gas sales in the 10-year plateau period and the DRILLEX.

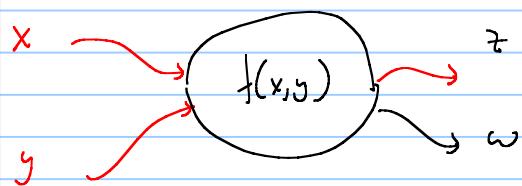
Task 4 (5 POINTS):

$$NPV = -\text{CAPEX} - \text{DRILLEX} + NPV_{rev}$$

Gas price	[USD/Sm3]	0.11
discount rate	[‐]	0.08
DRILLEX per well	[USD/well]	5.00E+06
DRILLEX TOTAL	[USD]	3.50E+07
	NPV [USD]	4.46E+08
end of year	yearly cum prod	DCF (revenue)
	[Sm3]	[USD]
5	8.88E+08	6.64E+07
6	8.88E+08	6.15E+07
7	8.88E+08	5.70E+07
8	8.88E+08	5.27E+07
9	8.88E+08	4.88E+07
10	8.88E+08	4.52E+07
11	8.88E+08	4.19E+07
12	8.88E+08	3.88E+07
13	8.88E+08	3.59E+07
14	8.88E+08	3.32E+07

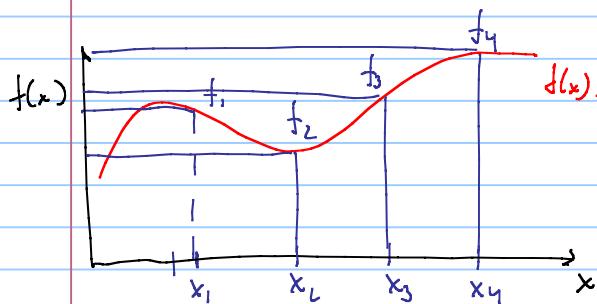
## Notes to Youtube video 13

How to handle uncertain parameters in our FOF calculations



deterministic calculation:  $x$  and  $y$  have a unique unknown value

stochastic/probabilistic calculation:  $x$  and  $y$  exhibit a probabilistic distribution

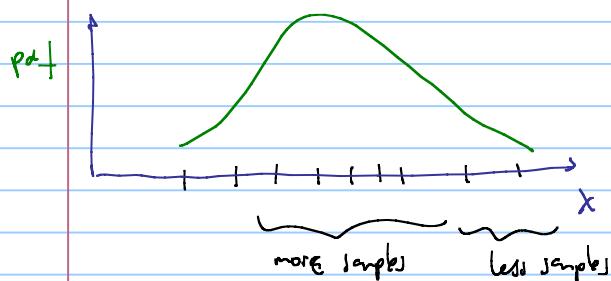


Approach to deal with uncertainty:

- create samples

- evaluate the function at samples

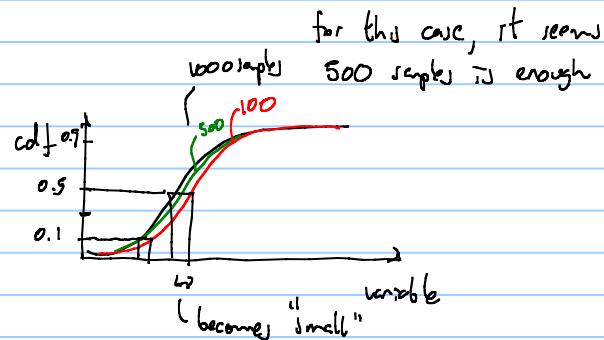
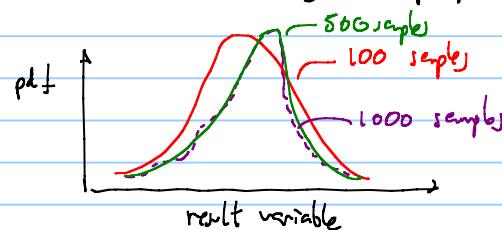
- calculate pdf and cdf of the results



1: How many samples are needed?

2: How to generate the samples?

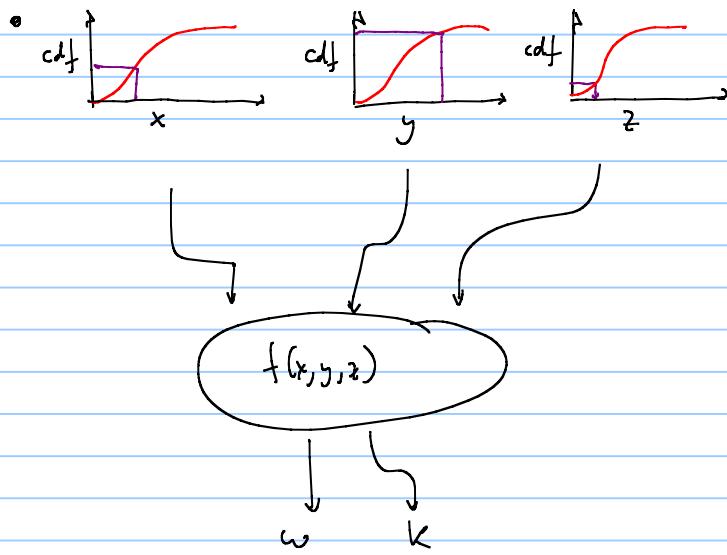
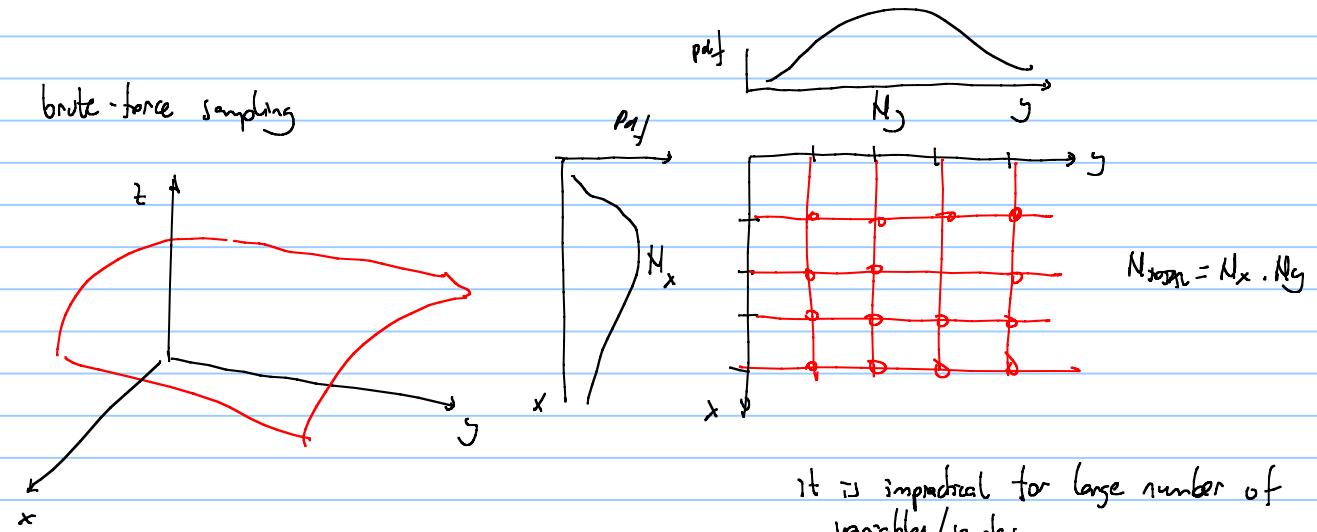
3: Increase the number of samples and see how the results change (pdf, cdf)



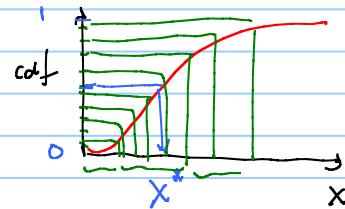
2: how to generate the samples

- Monte Carlo method
- Latin hypercube sampling

} efficient sampling  $\rightarrow$  less number of samples to achieve convergence



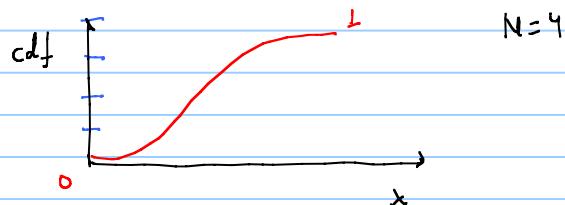
- ① For each variable
  - 1.1 pick a random number between 0 - 1
  - 1.2 enter cdf and read the value of the variable
- ② perform a simulation with the samples
- ③ repeat "many" times steps 1-2
- ④ perform a frequency analysis on the results  $\rightarrow$  pdf cdf



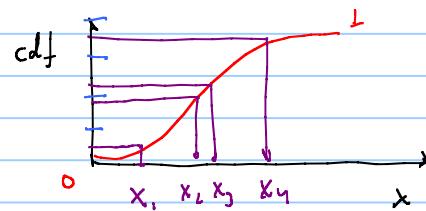
### • Latin hypercube sampling (LHS)

- ① Define a number of samples "N"
- ② For each variable

1.1. subdivide the cumulative probability in "N" intervals (equally-spaced)



1.2. Pick a random number in the interval  
find the corresponding value of the  
variable



$$\left\{ \begin{array}{c} x_1 \\ x_2 \\ x_3 \\ x_4 \end{array} \right\} \quad \left\{ \begin{array}{c} y_1 \\ y_2 \\ y_3 \\ y_4 \end{array} \right\} \quad \left\{ \begin{array}{c} z_1 \\ z_2 \\ z_3 \\ z_4 \end{array} \right\}$$

1.3. shuffle randomly the sample vector(s)

$$\begin{array}{l} \text{sim 1} \\ \text{sim 2} \\ \text{sim 3} \\ \text{sim 4} \end{array} \quad \left( \begin{array}{c} x_3 \\ x_1 \\ x_4 \\ x_2 \end{array} \right) \quad \left( \begin{array}{c} y_1 \\ y_3 \\ y_4 \\ y_2 \end{array} \right) \quad \left( \begin{array}{c} z_3 \\ z_2 \\ z_1 \\ z_4 \end{array} \right)$$

② perform simulations for sample variables that are  
in the same row

③ perform a frequency analysis on the results  
↪ cdf, pdf

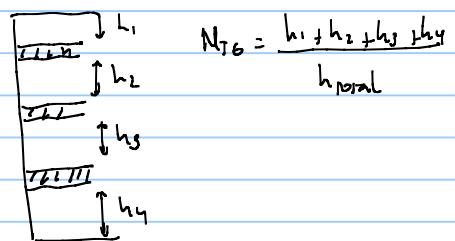
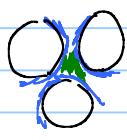
## Notes to Youtube video 14

Reserve extraction : case undersaturated oil reservoir

$$\text{TRR} = N_{pu} = \frac{V_R \cdot \phi \cdot N_{tg} \cdot S_o \cdot F_{au}}{B_o}$$

total recoverable  
reserves      ↓  
ultimate  
cumulative  
production

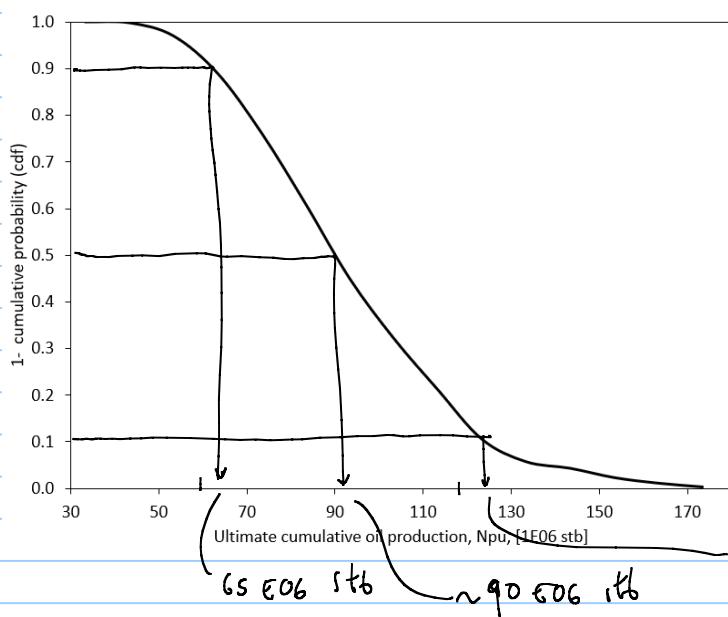
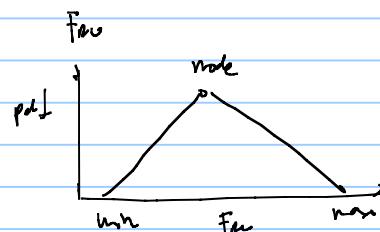
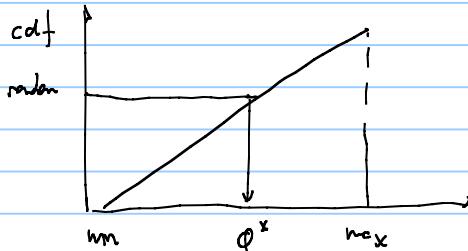
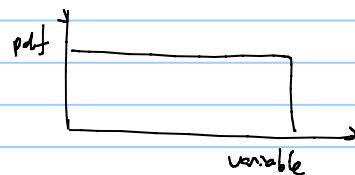
recovery  
factor



$$N_{pu} = \frac{V_R \cdot \phi \cdot N_{tg} \cdot S_o \cdot F_{au}}{B_o}$$

$N_{pu}$

$V_R, \phi, N_{tg}, S_o, F_{au}, B_o$  have a uniform pdf



expectation curve

- Conservative estimate (90%) p90 }
- Average estimate (50%) p50
- optimistic estimate (10%) p10

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## OUTLINE:

- Recap
- Probability trees mini-theory
- Probability trees exercise
  - Including TRR MC simulation using Python

## Decision/Probability Trees:

Is a visual tool often used for decision support. It consists of a tree-like model of decisions/events and their possible consequences, including chance event outcomes, resource costs, and utility.

It is often used instead of Monte Carlo simulation usually when there are discrete variables, that are challenging to express mathematically with a probability distribution (e.g. choices of offshore structure, choices regarding appraisal, etc.).

A decision tree consists of three types of nodes:

Decision nodes – typically represented by squares

Chance nodes – typically represented by circles

End nodes – typically represented by triangles

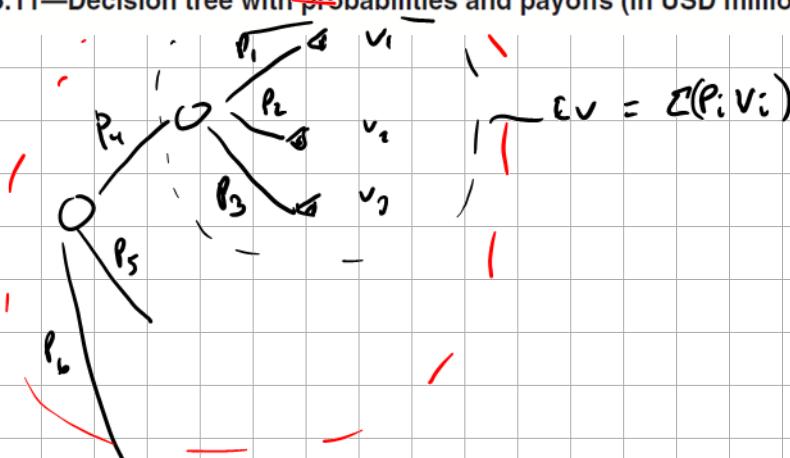
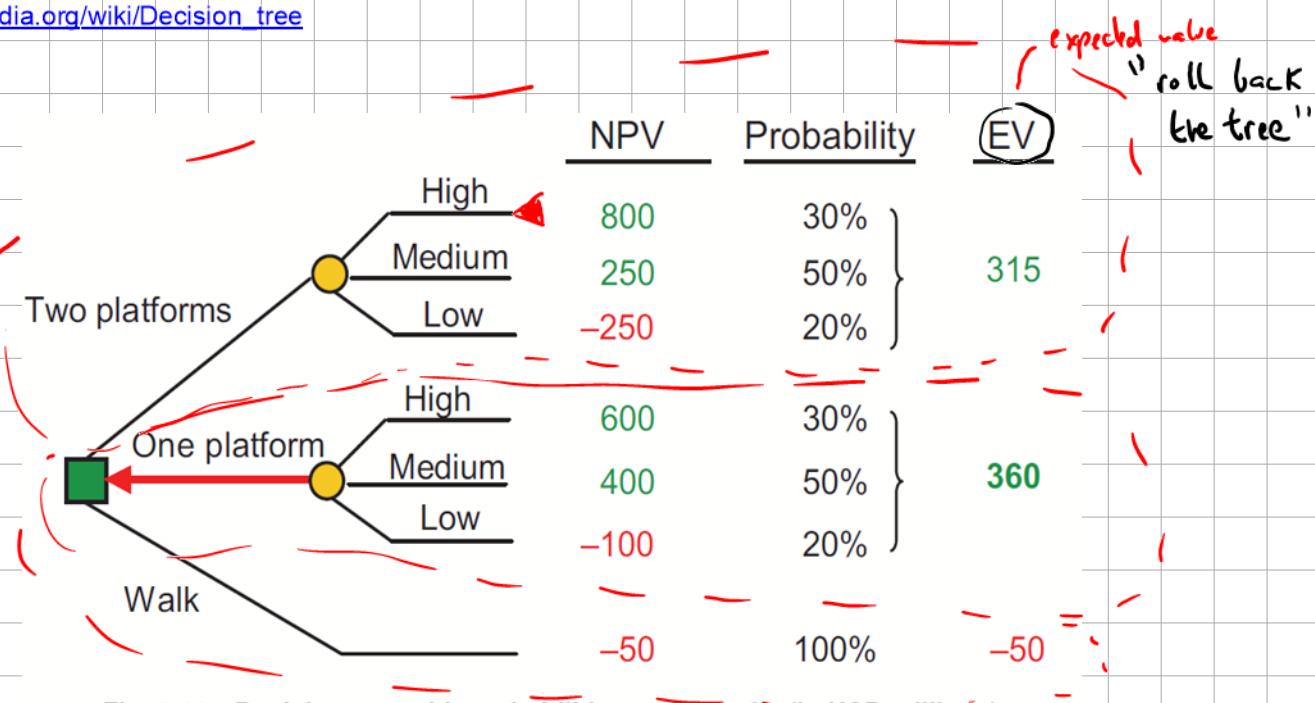
-To calculate probability outcomes, multiply the probability values of the connected branches.

-To calculate the probability of multiple outcomes, add the probabilities together. The probability of all possible outcomes should always equal one. If you get any other value, go back and check for mistakes.

## Sources:

<https://www.mashupmath.com/blog/probability-tree-diagrams>

[https://en.wikipedia.org/wiki/Decision\\_tree](https://en.wikipedia.org/wiki/Decision_tree)



An oil reservoir has been discovered in the Barents Sea, 310 km from Hammerfest. Seismic data and a few exploration wells have been drilled that provide enough information to perform an initial reserve estimation and economic valuation.



The company is currently in the business identification phase (leading to DG0) and is currently considering the following options:

- Go forward with the development
- Drill an appraisal well to find more information about the reservoir
- Relinquish to the government

To help the company to take the decision, you are considering employing a probability tree together with Monte Carlo simulations.

The cost of the appraisal well campaign is 100 million USD. The campaign could have two outcomes:

- a. If the appraisal wells give a positive indication of hydrocarbons, It will confirm the upper value and lower values of the rock volume. If this is the case, 9 wells will be used, and 3 of those will be subsea, which require a heavier capital investment in facilities (1500 million USD).
- b. If the appraisal wells give a negative indication of hydrocarbons, the maximum and minimum rock volumes must be reduced by 40%. If this is the case, only 6 wells can be used, and the capital investment in facilities is less (900 million USD).

### **Additional information**

For estimating the economic value of the project, you must use the following simplified expression (in million USD)

$$NPV = P_o \cdot F_D \cdot N_{pu} - DRILLEX - CAPEX$$

Where:

- $P_o$  is the price per barrel of oil [USD/bbl]. Use 60.
- $CAPEX$  is the cost of facilities, in million USD.
- $DRILLEX$  is the cost of drilling, equal to  $N_w \cdot 50$  million USD, where  $N_w$  is number of wells.

- $F_D$  is a discounting factor [-], representing that reserves are recovered and discounted gradually within a period of time, instead of at time zero. This value will depend on the production profile, but for your analysis, assume it is equal to 0.4.
- $N_{pu}$  is the ultimate cumulative oil production [in Million stb] (or total recoverable reserves). Only oil is recovered from this field (due to lack of gas transport infrastructure).

The ultimate cumulative oil production is  $N_{pu} = N \cdot F_R$ , where

- $F_R$  is the ultimate recovery factor [-].
- $N$  is the initial oil in place [stb], estimated by the expression

$$N = \frac{V_R \cdot \phi \cdot S_o \cdot N_{tg}}{B_o}$$

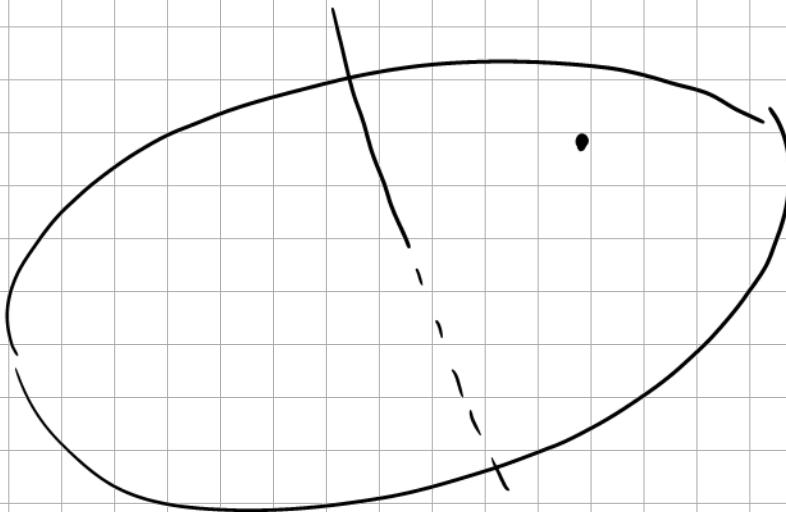
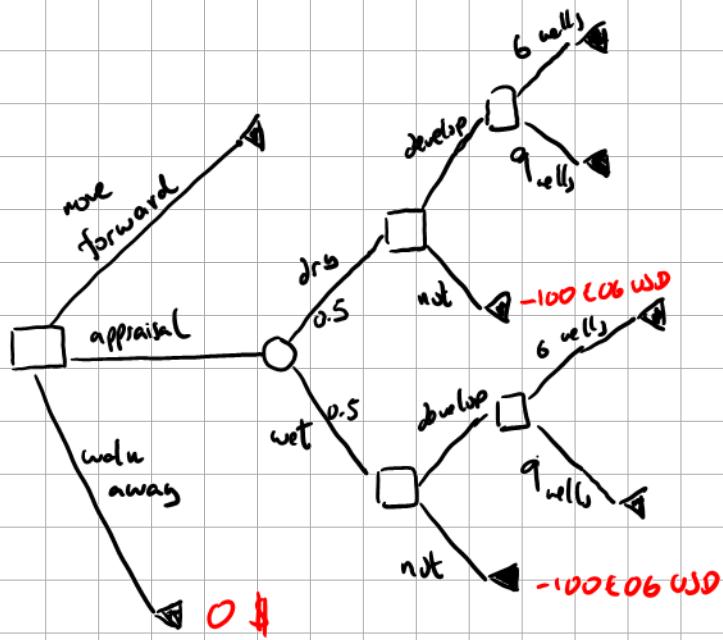
Where:

- $V_R$  Rock volume [bbl]
- $\phi$  porosity [-]
- $S_o$  oil saturation [-]
- $N_{tg}$  Net to gross [-]
- $B_o$  Oil formation volume factor [bbl/stb]

Values for the parameters and their probability distributions are provided in the table below:

			Net to Gross	Oil Saturation	Formation Volume Factor	Ultimate Recovery Factor
	Rock volume	Porosity	N/G	So=(1-Sw)	Bo	Fr
	bbl	fraction	fraction	fraction	Res bbl/STB	fraction
Min	5.00E+09	0.18	0.3	0.8	1.35	0.18
Max	6.25E+09	0.3	0.5	0.9	1.6	0.35
Mode						0.25

## Class exercise



Calculate economic value using this equation:

$$r^{60} r^{0.4}$$

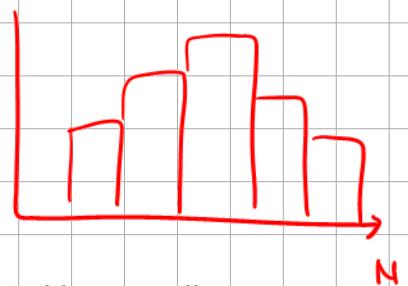
$$(N_w \cdot 50)$$

6  
a  
N\_w = 9

$$\begin{aligned} & \text{Lit } N_w = 9, 1500 \text{ EOB USD} \\ & \text{Lit } N_w = 6, 900 \text{ EOB USD} \end{aligned}$$

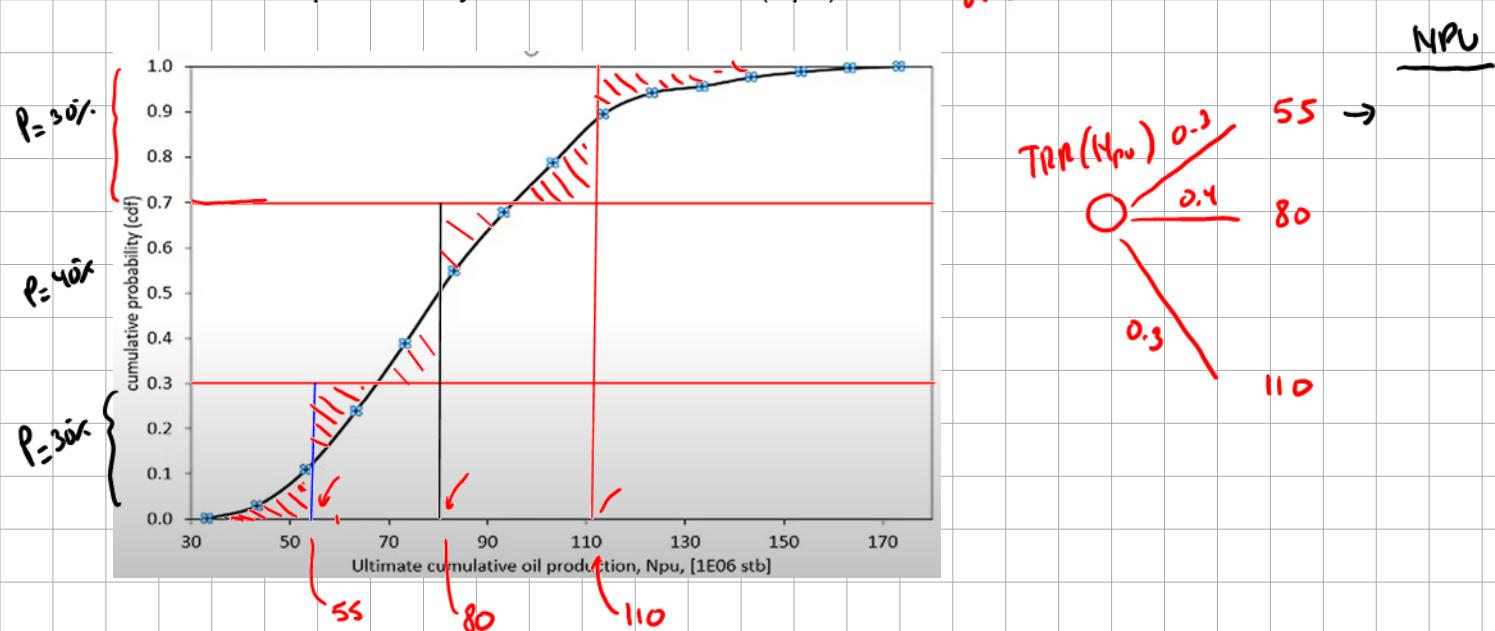
$$NPV = P_o \cdot F_D \cdot N_{pu} - DRILLEX - CAPEX$$

$$N_{pu} = \frac{V_p \cdot \phi \cdot f_o \cdot F_{pu} \cdot N_{ig}}{B_0}$$



Calculated in an earlier  
Youtube video

Discretize the probability distribution of TRR (Npu)



P	$N_{pu}$ (positive appraisal)	$NPV(6 \text{ wells})$	$NPV(9 \text{ wells})$
0.3	55	120	-630
0.4	80	720	-30
0.3	110	1440	690

$$NPV(6 \text{ wells}) = 60 \cdot 55 \cdot 0.4 - 6 \cdot 50 - 900 = \\ 1320 - 300 - 900 = 120$$

$$NPV(9 \text{ wells}) = 60 \cdot 55 \cdot 0.4 - 9 \cdot 50 - 1500 = -630$$

If the appraisal well is dry:

	Rock volume	Porosity	Net to Gross	Oil Saturation	Formation Volume Factor	Ultimate Recovery Factor
	bbl	fraction	N/G	So=(1-Sw)	Bo	Fr
Min	5.00E+09	0.18	0.3	0.8	1.35	0.18
Max	6.25E+09	0.3	0.5	0.9	1.6	0.35
Mode						0.25

$\rightarrow 3 \times 10^9$   
 $\rightarrow 3.75 \times 10^9$

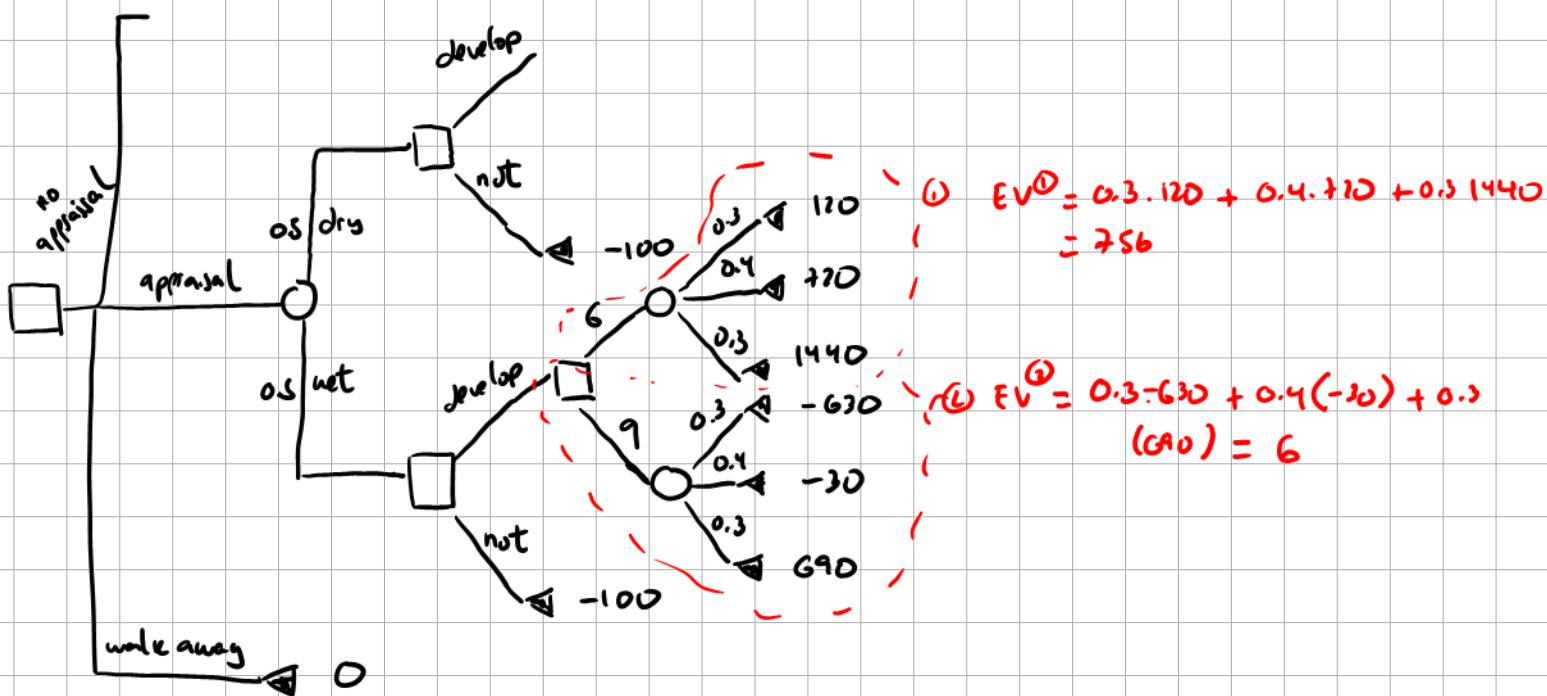
so in principle, I would need to repeat the MC simulation

$$N_{pu} = \frac{V_R \cdot \Phi \cdot N_g \cdot So}{B_0} \cdot F_{pu}$$

$$V_{e_{new}} = V_{e_{old}} \cdot 0.6$$

So, as an approximation, I assume I will obtain the same distribution in the new MC, but scaled by 0.6!

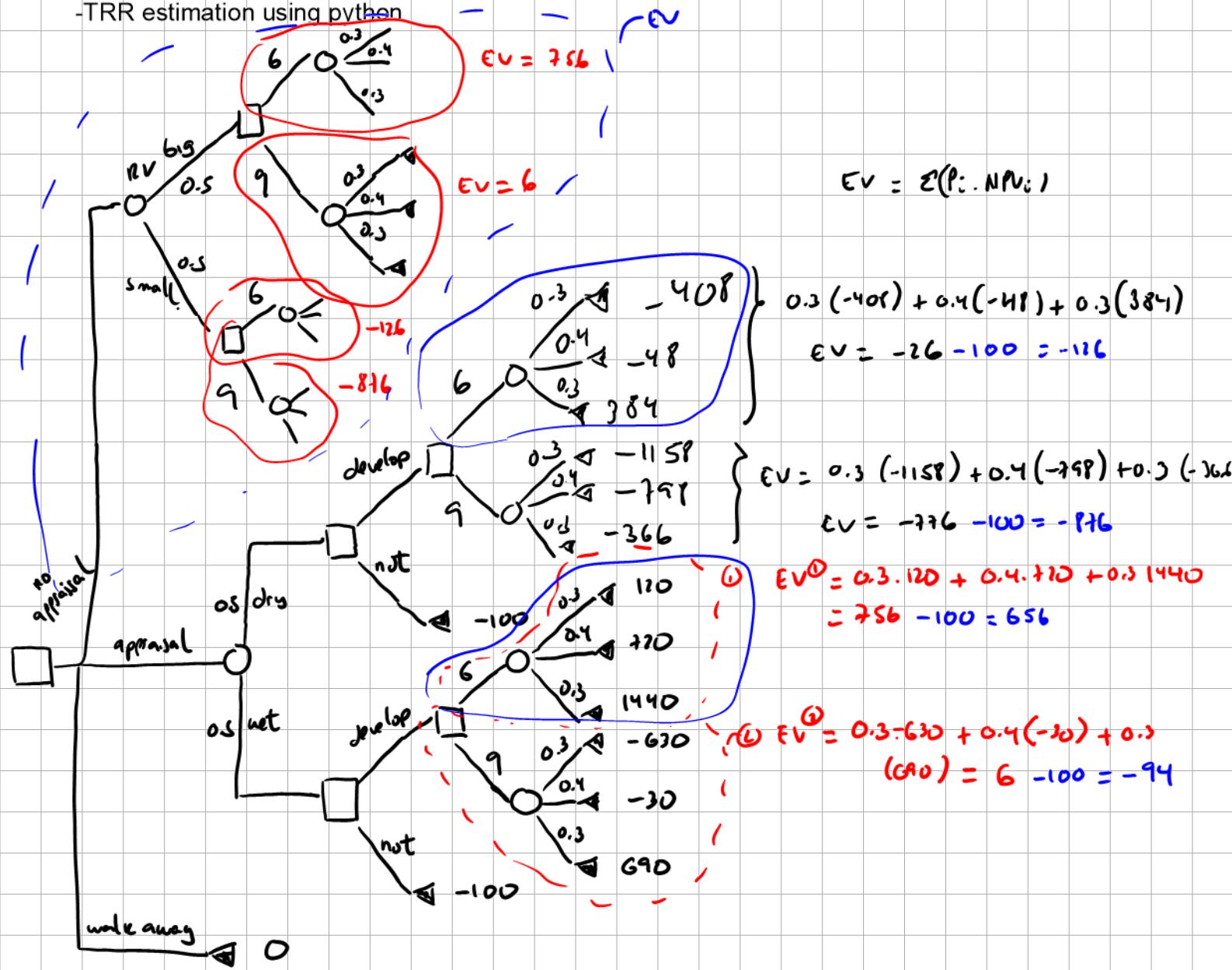
$P$	NPV (3 wells appraisal)	NPV (6 wells)	NPV (9 wells)
0.3	$55 \cdot 0.6 = 33$	-408	-1158
0.4	$80 \cdot 0.6 = 48$	-48	-798
0.5	$110 \cdot 0.6 = 66$	384	-366



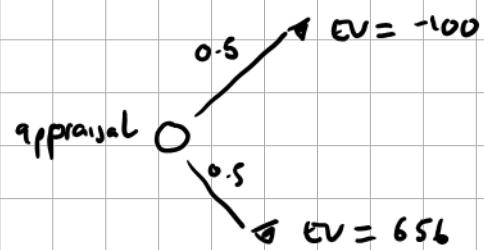
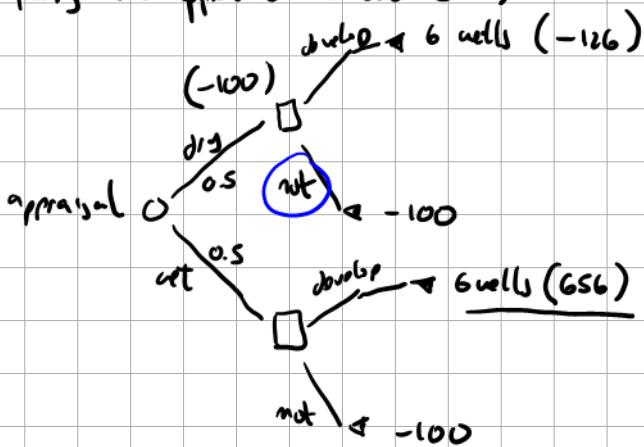
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## Outline

- Cont of exercise on probability trees
- TRR estimation using python



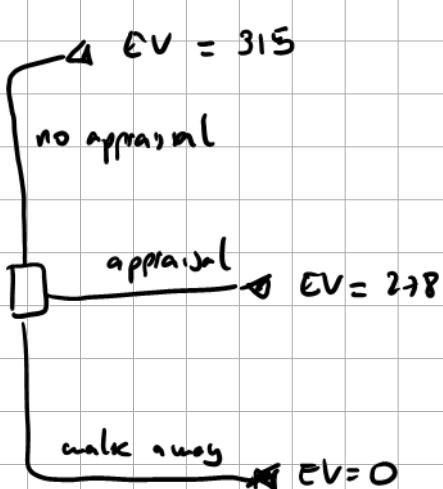
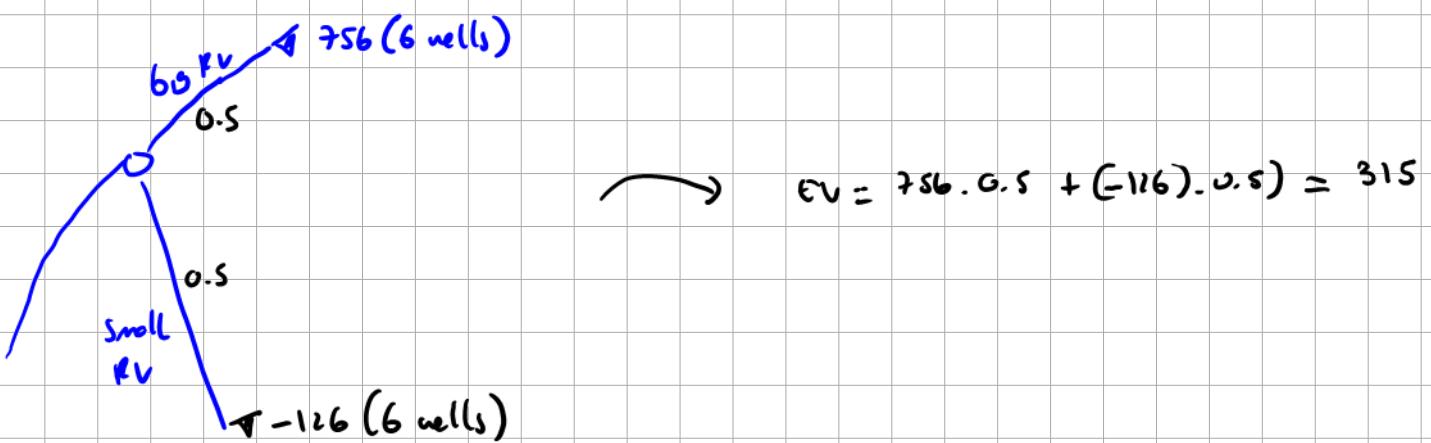
Simplify the appraisal branch (EV)



$$\text{appraisal } EV = 0.5 \cdot (-100) + 0.5 \cdot (656)$$

$$EV = 278$$

Simplify the "no appraisal" branch

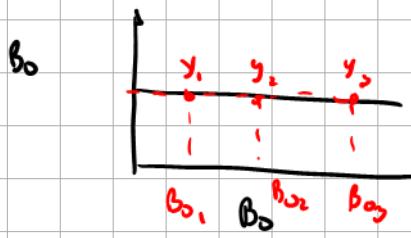


it seems the best solution is

- no appraisal
- 6 wells

How would you solve the MC TRR problem using probability trees?

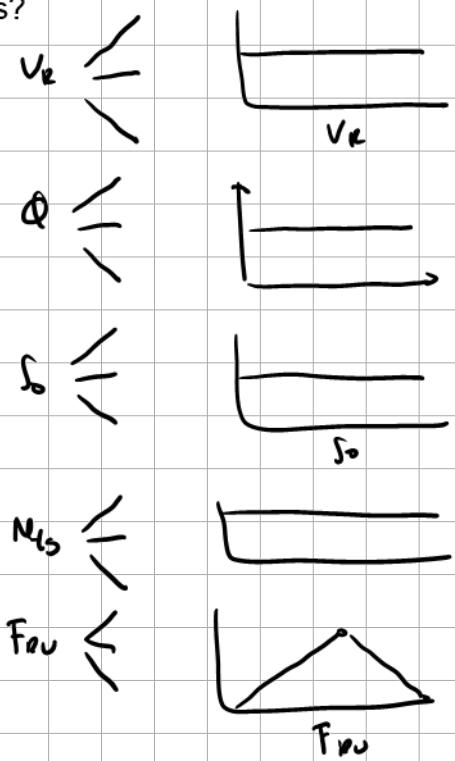
$$N_{PV}(\text{TRR}) = \frac{V_R \cdot \Phi \cdot S_0 \cdot N_{gj} \cdot F_{PV}}{b_0}$$



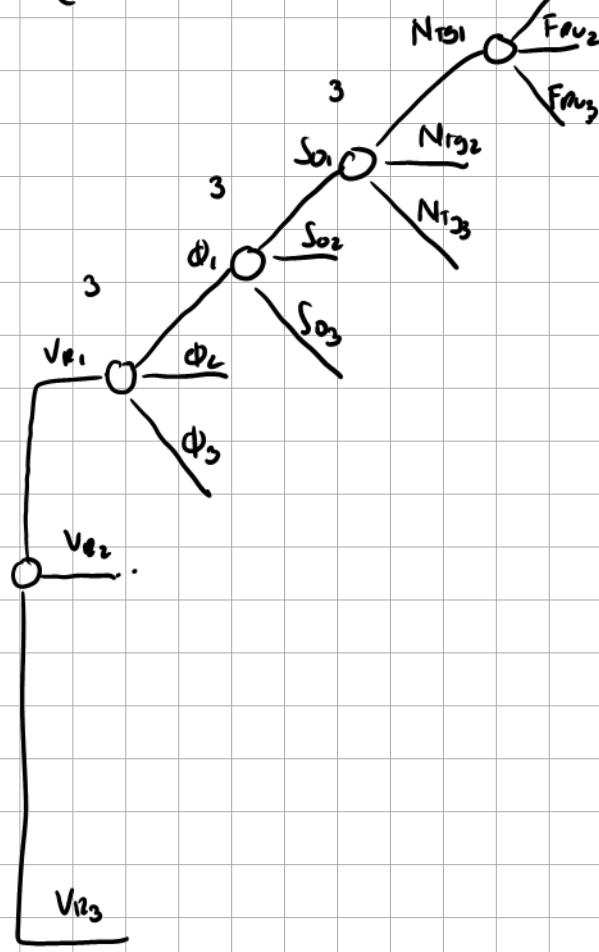
O

$$p_1 = \frac{y_1}{y_1 + y_2 + y_3}$$

$$p_2 = \frac{y_2}{y_1 + y_2 + y_3}$$



$$(3)^6 = 729$$



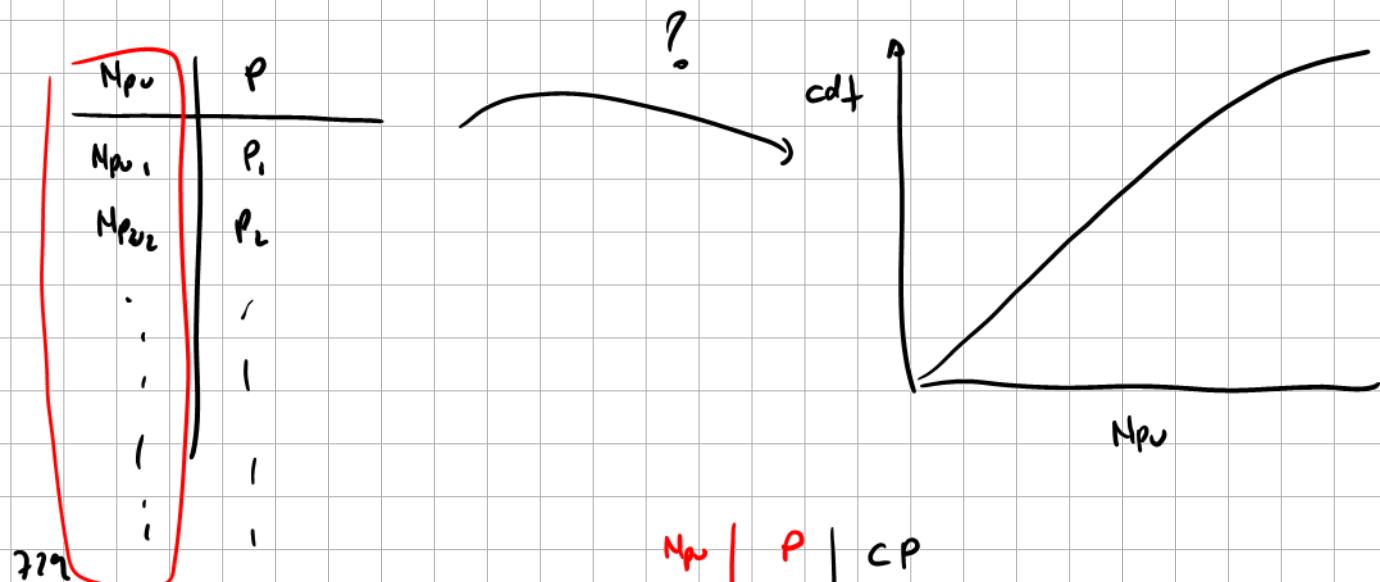
$P = P_{V_{R_1}} \cdot P_{Q_1} \cdot P_{S_{O_1}} \cdot P_{N_{Q_1}} \cdot P_{F_{Q_1}} \cdot P_{S_{O_2}} \cdot P_{N_{Q_2}} \cdot P_{F_{Q_2}} \cdot P_{S_{O_3}} \cdot P_{N_{Q_3}} \cdot P_{F_{Q_3}} \cdot \dots \cdot P_{S_{O_n}} \cdot P_{N_{Q_n}} \cdot P_{F_{Q_n}}$

?

( ) ( ) ( )

4

Result



Sort from small to big

N <sub>Pu</sub>	P	CP
N <sub>Pu_2</sub>	P <sub>2</sub>	P <sub>2</sub>
N <sub>Pu_100</sub>	P <sub>100</sub>	P <sub>2</sub> + P <sub>100</sub>
...	...	...
1	1	P <sub>2</sub> + P <sub>100</sub> + ...

### Useful links:

- General information about python:  
[https://en.wikipedia.org/wiki/Python\\_\(programming\\_language\)](https://en.wikipedia.org/wiki/Python_(programming_language))
- Creator of python: [https://en.wikipedia.org/wiki/Guido\\_van\\_Rossum](https://en.wikipedia.org/wiki/Guido_van_Rossum)
- Origin of the name: [https://en.wikipedia.org/wiki/Monty\\_Python](https://en.wikipedia.org/wiki/Monty_Python)
- To install python, Jupyter Notebook, libraries, etc. on your computer:  
<https://www.anaconda.com/>
- Online jupyter notebook by Google (no need to install):  
<https://colab.research.google.com/>
- Desktop editors for python: <https://www.jetbrains.com/pycharm/> ,  
<https://code.visualstudio.com/> , spyder (included in Anaconda)  
<https://www.spyder-ide.org/>
- Information about code version control and backup:  
[https://www.w3schools.com/git/git\\_intro.asp?remote=github](https://www.w3schools.com/git/git_intro.asp?remote=github) , <https://github.com/>
- Course that Milan took on python:  
<https://www.coursera.org/specializations/python#courses> ,  
<https://www.dr-chuck.com/> , <https://www.py4e.com/lessons>
- numpy documentation: <https://numpy.org/doc/stable/index.html>

## Using python to perform MC simulation of the TRR

### Probabilistic estimation of reserves\_MCS

```
#importing needed libraries
import numpy as np #for math operations
import matplotlib.pyplot as plt #library for plotting
import pandas as pd #for creating and displaying a table

#declaring necessary functions
def Npu(por, RV, NTG, So, Bo, Fr):
    #returns ultimate cumulative oil production in [stb, Sm3]
    #input:
    #por, porosity in [-]
    #RV, rock volume, in [bbl, m3]
    #NTG, net to gross ratio, [-]
    #So, oil saturation, [-]
    #Bo, oil formation volume factor [bbl/stb, m3/Sm3]
    #Fr, ultimate recovery factor in [-]
    TRR=por*RV*NTG*So*Fr/Bo
    return TRR

#defineing input
#porosity
por_min=0.18
por_max=0.3
#rock volume [1E06 bbl]
RV_min=5000
RV_max=6250
#Net to gross [-]
NTG_min=0.3
NTG_max=0.5
#oil saturation [-]
So_min=0.8
So_max=0.9
#Oil formation volume factor [bbl/stb]
Bo_min=1.35
Bo_max=1.6
#recovery factor, Fr, [-]
Fr_min=0.18
Fr_max=0.35
Fr_mode=0.25

#creating random samples
n=1000 #number of samples
por_v=np.random.uniform(por_min,por_max,n)
RV_v=np.random.uniform(RV_min,RV_max,n)
NTG_v=np.random.uniform(NTG_min,NTG_max,n)
So_v=np.random.uniform(So_min,So_max,n)
Bo_v=np.random.uniform(Bo_min,Bo_max,n)
Fr_v=np.random.triangular(Fr_min,Fr_mode,Fr_max,n)

#MC simulation
Npu_v=Npu(por_v, RV_v, NTG_v, So_v, Bo_v, Fr_v)

#frequency analysis on the results
nr_bins=15
bins=np.linspace(Npu_v.min(),Npu_v.max(),nr_bins)
counts=np.histogram(Npu_v,bins)[0]
pdf=counts/n
bins_for_pdf_plotting=0.5*(bins[0:-1]+bins[1:])
#plot pdf
plt.xlabel('ultimate cumulative oil production, Npu, [1E06 stb]')
plt.ylabel('frequency')
plt.plot(bins_for_pdf_plotting,pdf,label='pdf')
plt.legend()
plt.show()

#plot cdf
cdf=np.cumsum(pdf)
bins_for_cdf_plotting=bins[1:]
plt.xlabel('ultimate cumulative oil production, Npu, [1E06 stb]')
plt.ylabel('cumulative probability distribution, cdf')
plt.plot(bins_for_cdf_plotting,cdf,label='cdf')
plt.legend()
plt.show()
```

P90= np.percentile(Npu\_v,10)

P10= np.percentile(Npu\_v,90)

P50= np.percentile(Npu\_v,50)

## Notes for Youtube video offshore structures 1

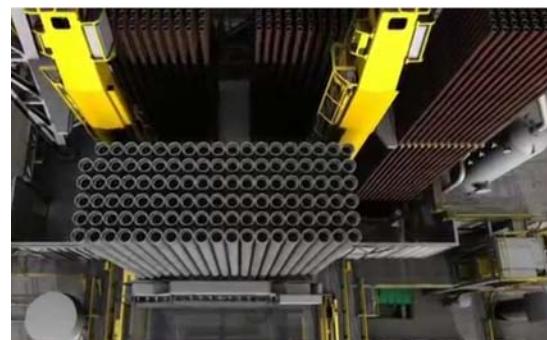
# Offshore structures for oil and gas production

Prof. Milan Stanko (NTNU)

1

## Components

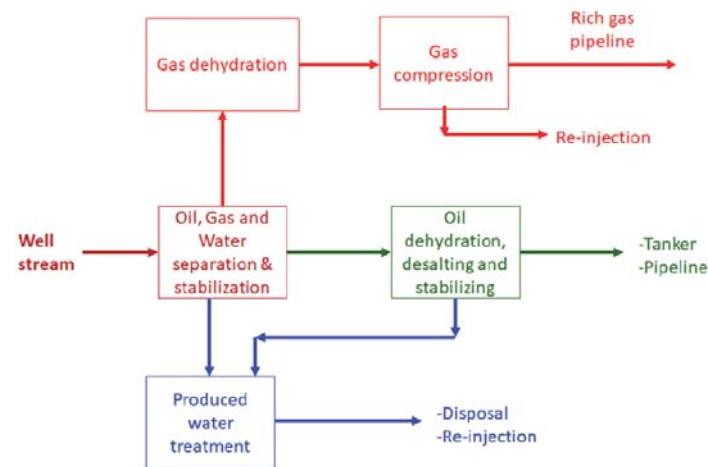
- Facilities for drilling and full intervention. This includes drilling tower, BOP, drilling floor, mud package, cementing pumps, storage deck for drill pipes and tubulars, drilling risers.



2

# Components

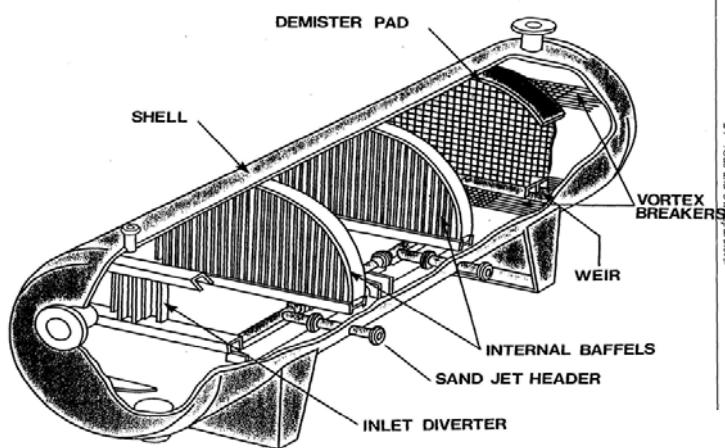
- Facilities for light well intervention.
- Processing facilities: separator trains for primary oil, gas and water separation, gas processing train, water processing train.
- Gas injection system
- Gas compression units for pipeline transport
- Water injection system



3

# Components

- Facilities for light well intervention.
- Processing facilities: separator trains for primary oil, gas and water separation, gas processing train, water processing train.
- Gas injection system
- Gas compression units for pipeline transport
- Water injection system



4

## Components

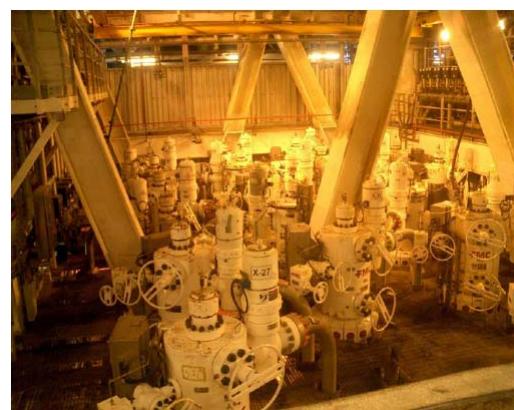
- Living quarters
- Helideck.
- Power generation.
- Flare system.
- Utilities (hydraulic power fluid, compressed air, drinking water unit, air condition system, ventilation and heating system)



5

## Components

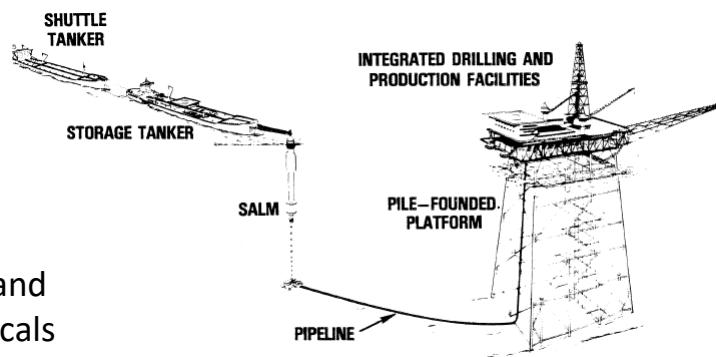
- Bay for wellheads and X-mas trees
- Production manifolds
- Oil storage
- Facilities for oil offloading
- Control system
- Monitoring system
- System for storage, injection and recovery of production chemicals (wax, scale, hydrate or corrosion inhibitors)
- Repair workshop



6

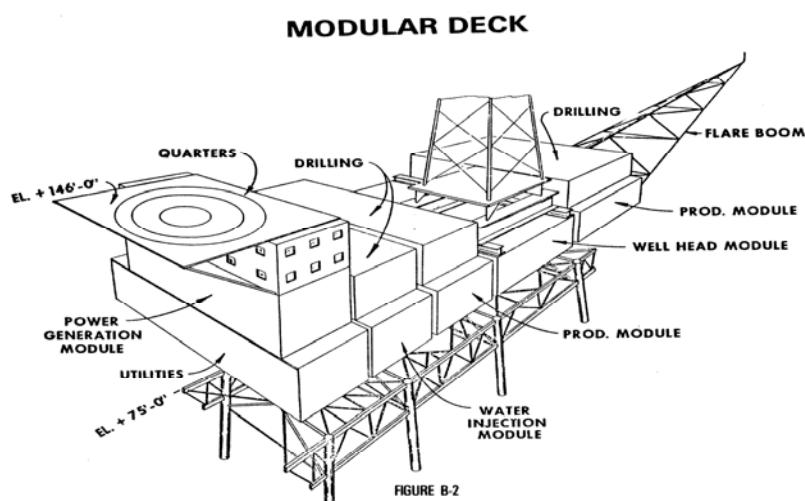
# Components

- Bay for wellheads and X-mas trees
- Production manifolds
- Oil storage
- Facilities for oil offloading
- Control system
- Monitoring system
- System for storage, injection and recovery of production chemicals (wax, scale, hydrate or corrosion inhibitors)
- Repair workshop



7

# Components



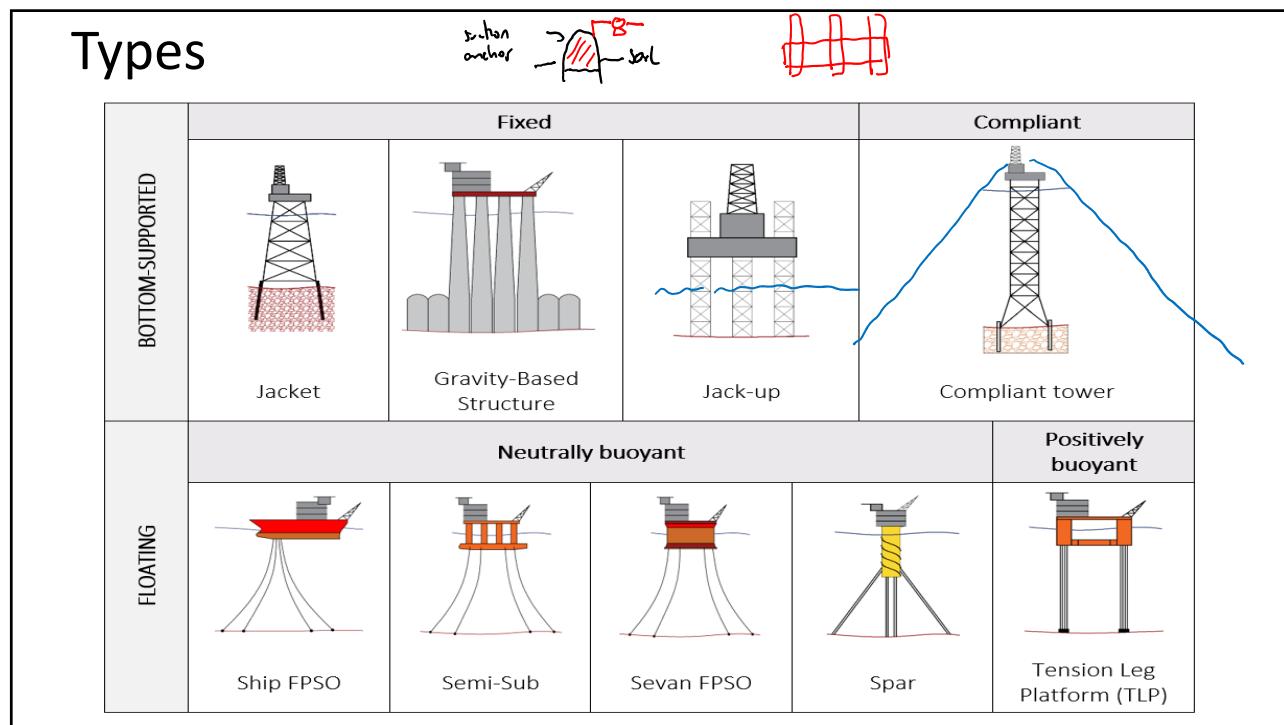
8

## Components – can be spread



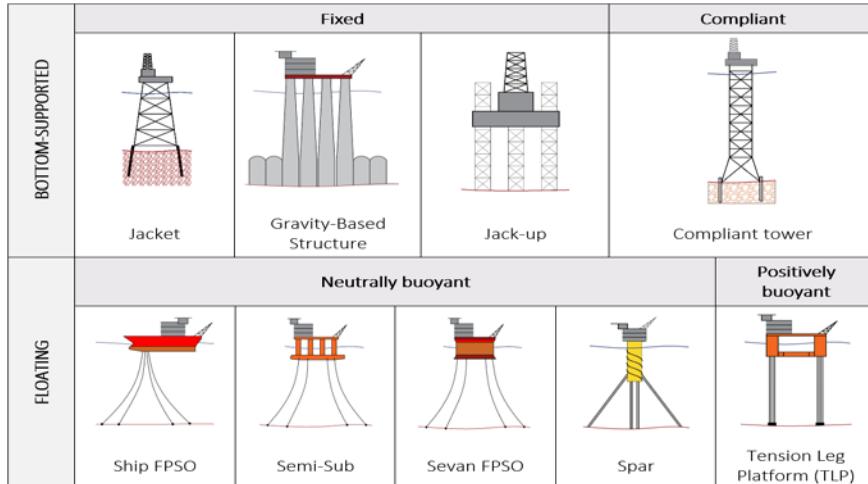
<https://www.akerbp.com/produksjon/valhall/>

9



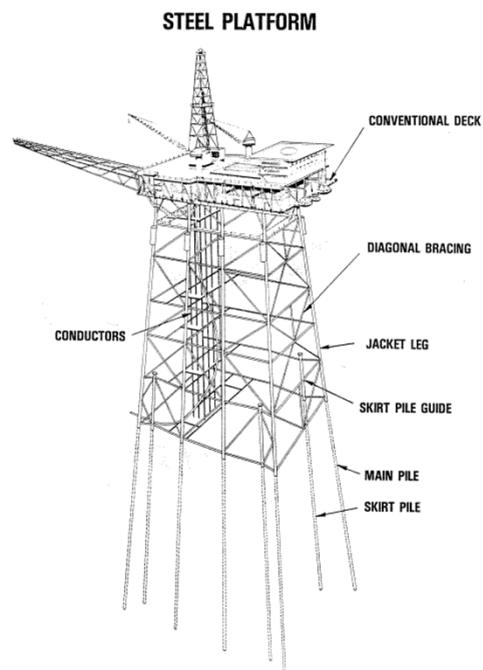
10

# Types



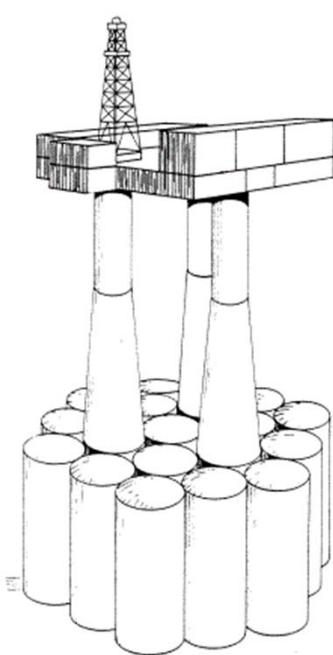
11

## Jacket



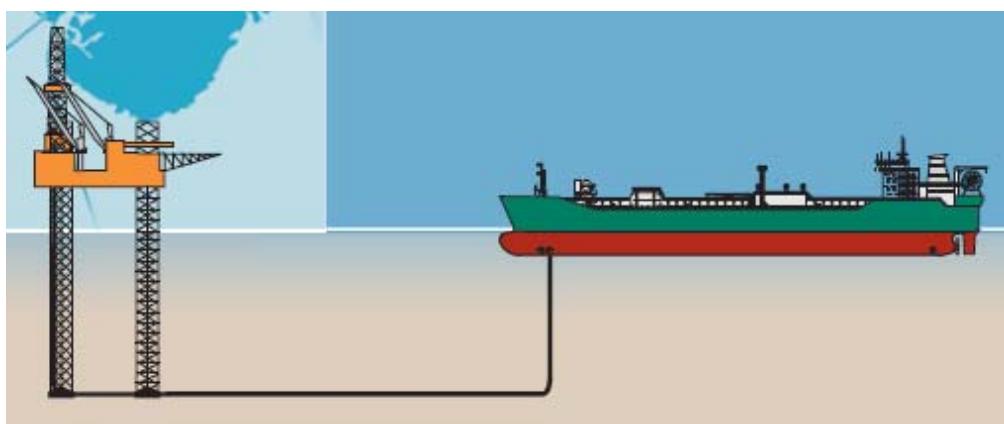
12

## GBS



13

## JACKUP



Taken from Volvo PDO

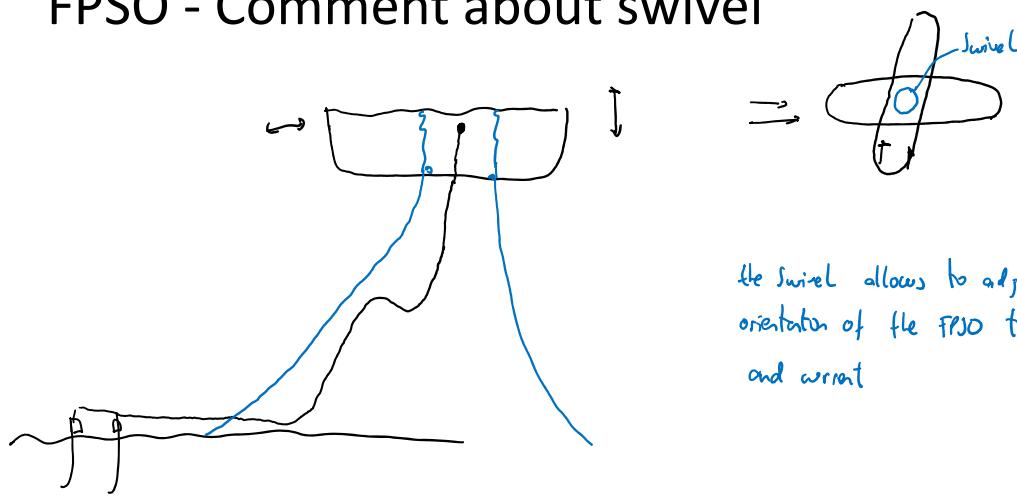
14

# FPSO



15

## FPSO - Comment about swivel



16

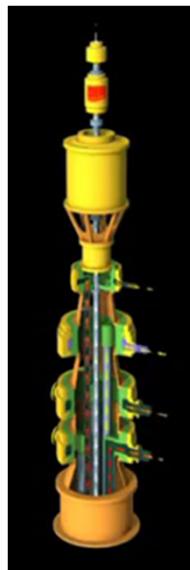
## FPSO - Swivel



<https://www.youtube.com/watch?v=70XwYmmZFWs>

17

## FPSO - Swivel



<https://www.youtube.com/watch?v=cCiUggjUhY0>

<https://www.youtube.com/watch?v=Sfjay0Rt3hU>

18

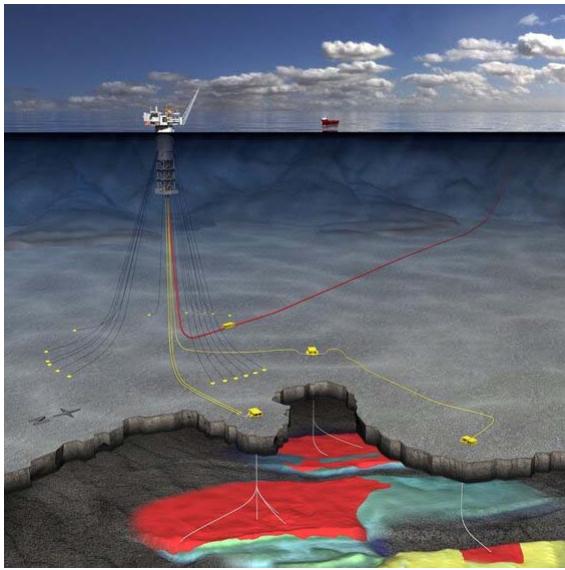
## FPSO - Swivel



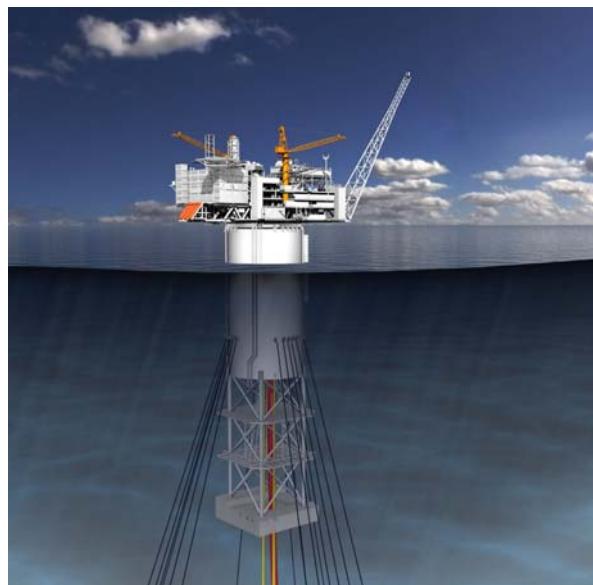
<https://www.youtube.com/watch?v=HbJh1ar0u1s>

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## SPAR

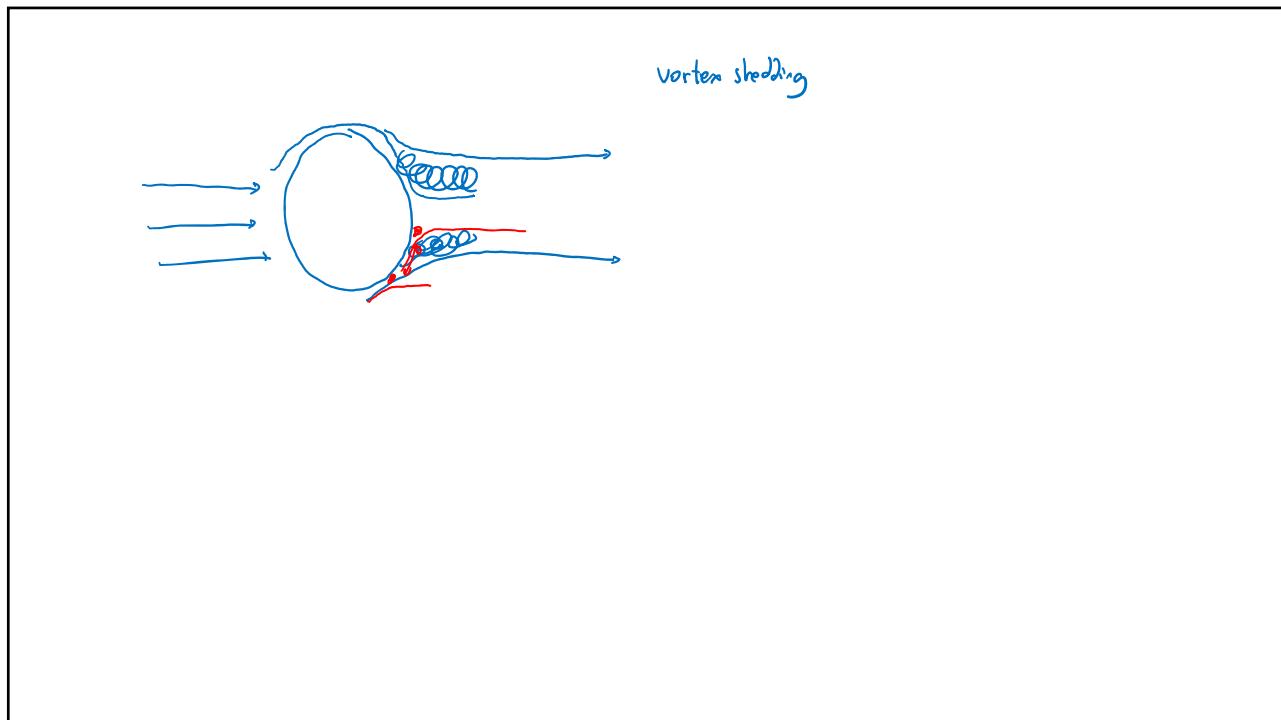


<https://www.tu.no/artikler/industri-kvaerner-sikrer-enda-et-aasta-hansteen-oppdrag/225940>



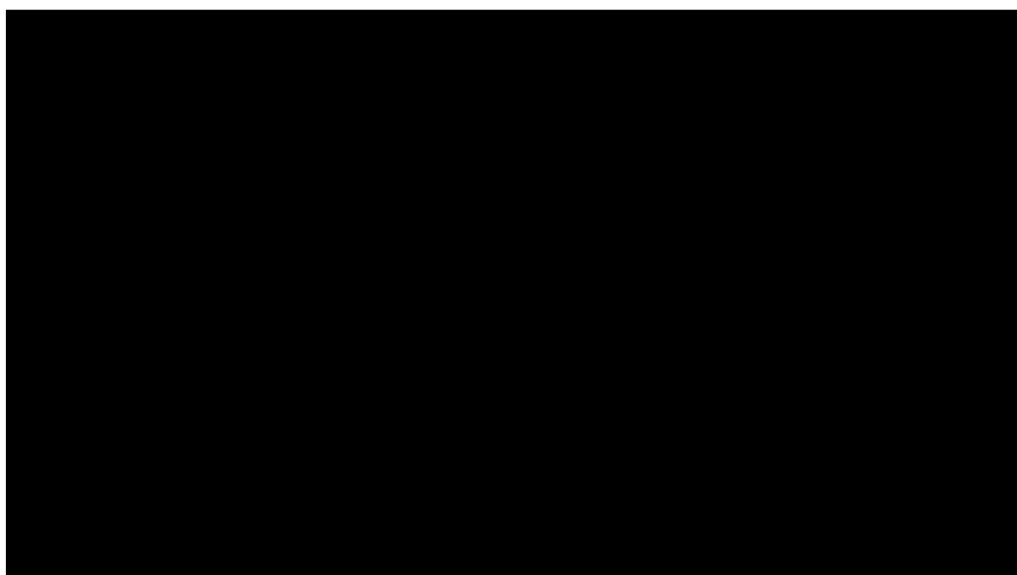
<https://www.tu.no/artikler/industri-kvaerner-sikrer-enda-et-aasta-hansteen-oppdrag/225940>

20



21

## SPAR – Vortex induced vibrations



<https://www.youtube.com/watch?v=Hbbkd2d3H8&feature=youtu.be>

22

## SPAR – Vortex induced vibrations

Summary of project.

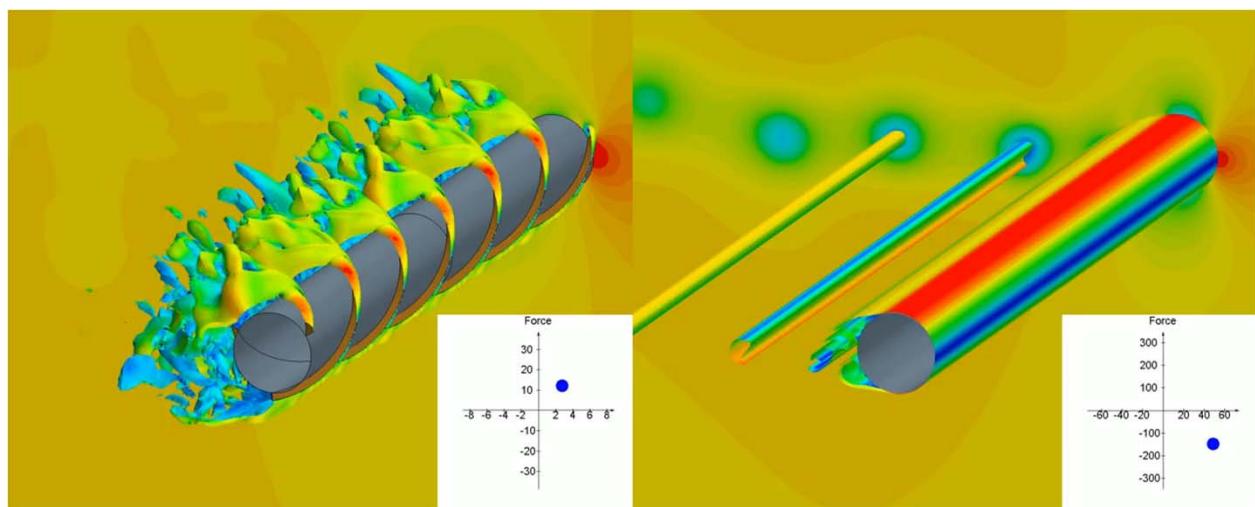
$$A^{*max} = Y_{max}/D$$

"Fixed" means the cylinder is not allowed to oscillate. "VIV" means it is based on vortex shedding.

[https://www.youtube.com/watch?v=24tBX\\_UD3fM](https://www.youtube.com/watch?v=24tBX_UD3fM)

23

## SPAR – Effect of helical strakes



<https://www.youtube.com/watch?v=W-zXwPT2r14>

24

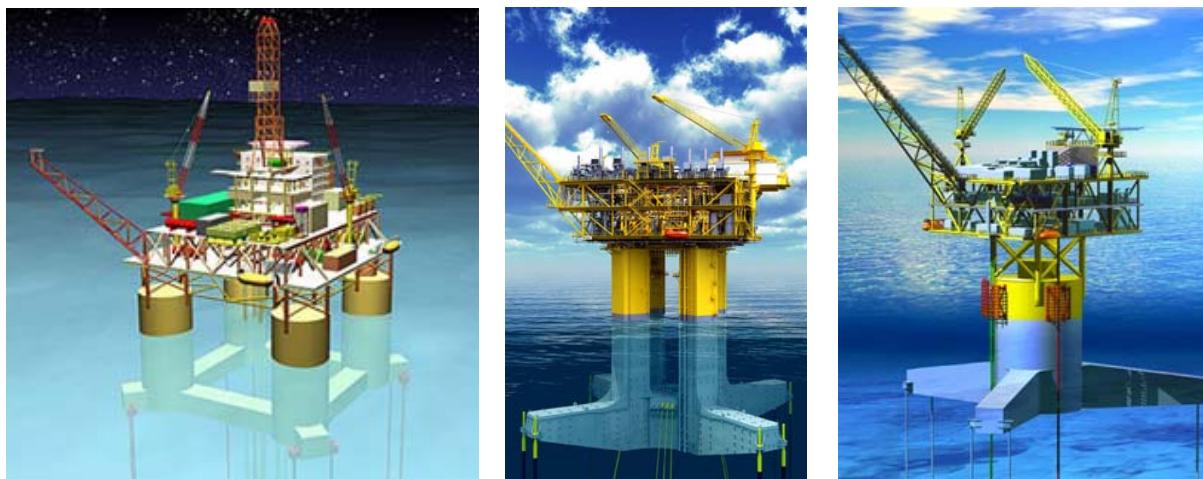
## SEVEN FPSO



<https://www.upstreamonline.com/epaper/sevan-fpso-selected-for-bream/1-1160389>

25

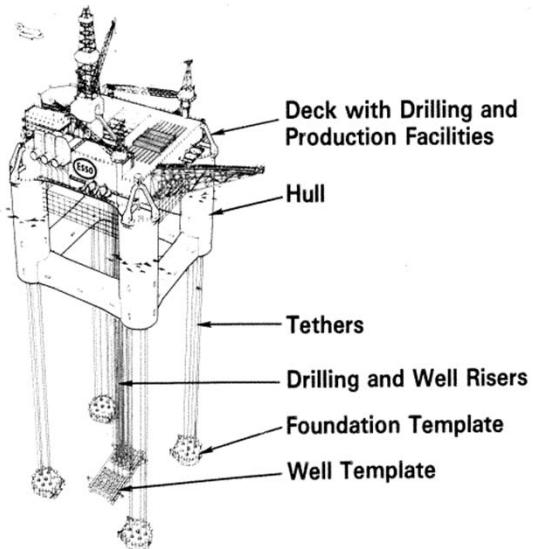
## Tension leg platform



[https://www.rigzone.com/training/insight.asp?insight\\_id=305&c\\_id=](https://www.rigzone.com/training/insight.asp?insight_id=305&c_id=)

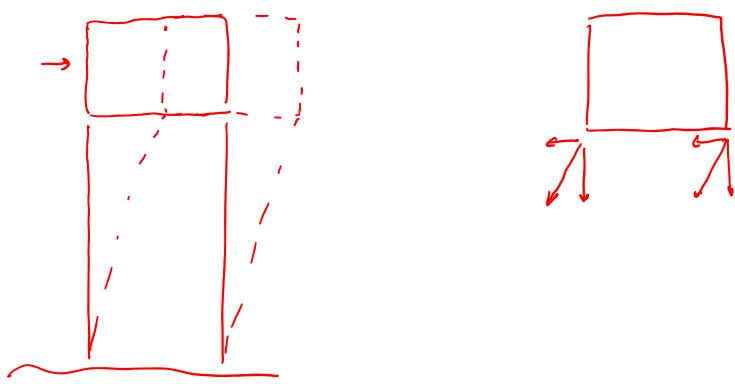
26

## Tension leg platform



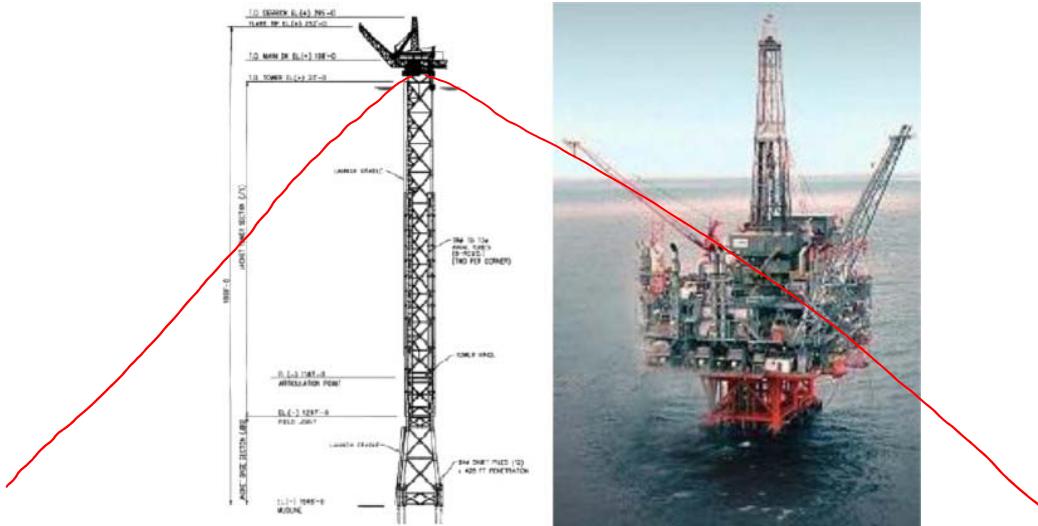
27

## Comment about Tension leg platform



28

# Compliant tower



<https://www.sciencedirect.com/science/article/pii/S0951833914000148>

29

# Semi-Sub



<https://www.oedigital.com/news/453987-jack-st-malo-flows-for-chevron>



<https://www.bairdmaritime.com/work-boat-world/offshore-world/offshore-extraction-and-processing/offshore-drilling/awilco-orders-second-semi-submersible-drilling-rig-from-keppel-fels/>

30

## Some selection criteria for offshore structures

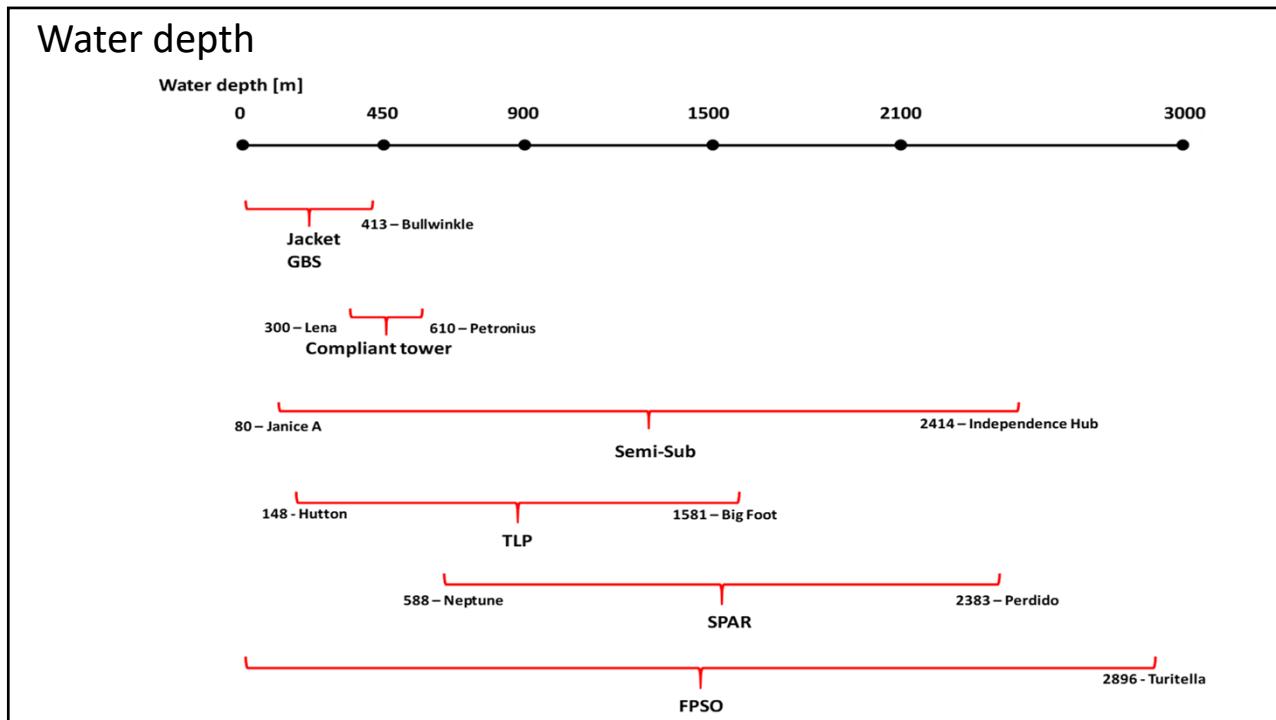
- Water depth
- Type of X-mas tree
  - Well intervention needs
    - Tubing replacement
    - Completion modifications
    - Artificial lift (ESP)
  - Infill drilling needs
  - Reservoir spread and structure
- Need for oil/condensate storage
- Marine loads Oceanographic environment
  - Wind, waves, current

31

## Some selection criteria for offshore structures

- **Water depth**
- Type of X-mas tree
  - Well intervention needs
    - Tubing replacement
    - Completion modifications
    - Artificial lift (ESP)
  - Infill drilling needs
  - Reservoir spread and structure
- Need for oil/condensate storage
- Marine loads Oceanographic environment
  - Wind, waves, current

32



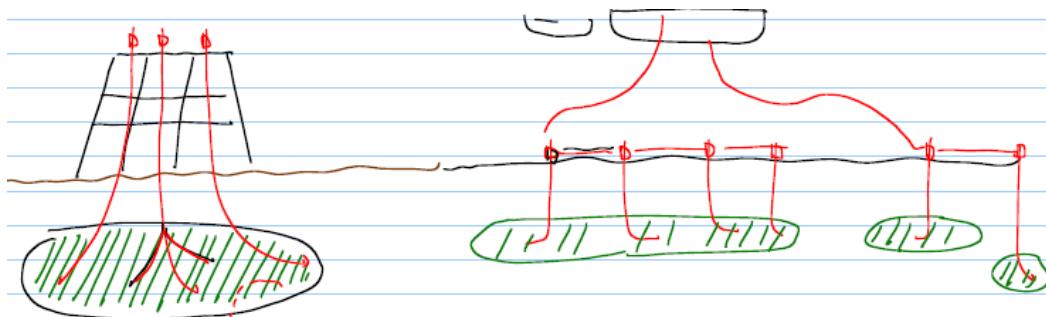
33

## Some selection criteria for offshore structures

- Water depth
- **Type of X-mas tree**
  - Well intervention needs
    - Tubing replacement
    - Completion modifications
    - Artificial lift (ESP)
  - Infill drilling needs
  - Reservoir spread and structure
- Need for oil/condensate storage
- Marine loads – Oceanographic environment
  - Wind, waves, current

34

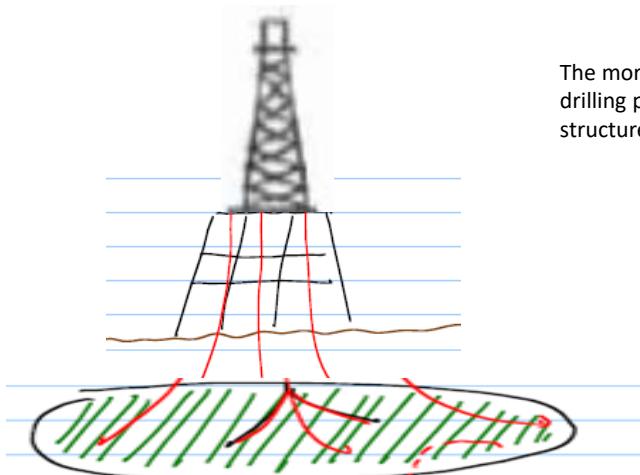
## Reservoir spread and structure



- Long deviated wells (\$\$\$)
- Wells are drilled from one location, no need to spend mobilization time (\$\$)
- Production startup must be delayed until all wells are drilled
- Shorter, vertical wells (\$)
- The drilling rig must be mobilized often which costs money (\$\$\$)
- Production can start in ramp up mode (if topside is in place)

35

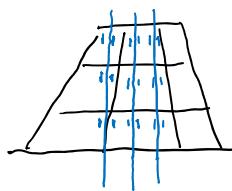
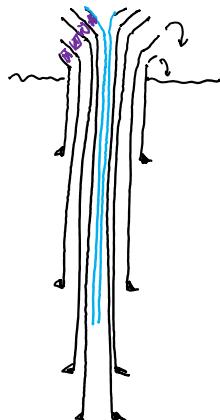
## Reservoir spread and structure



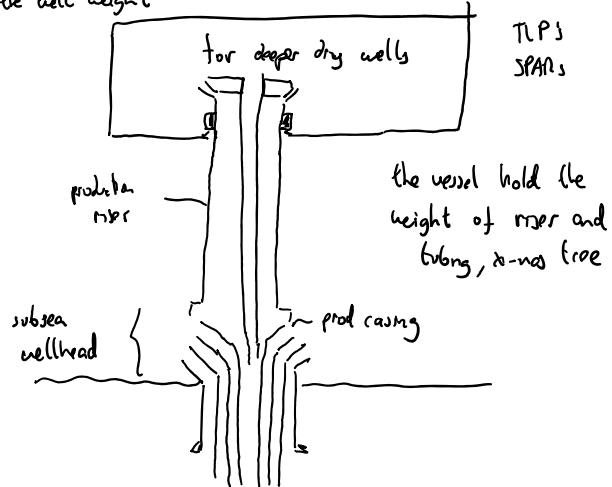
The more spread - requires a bigger and more costly drilling package – more weight on the structure, bigger structure (\$\$\$)

36

## Transfer of well weight to soil and to offshore structure

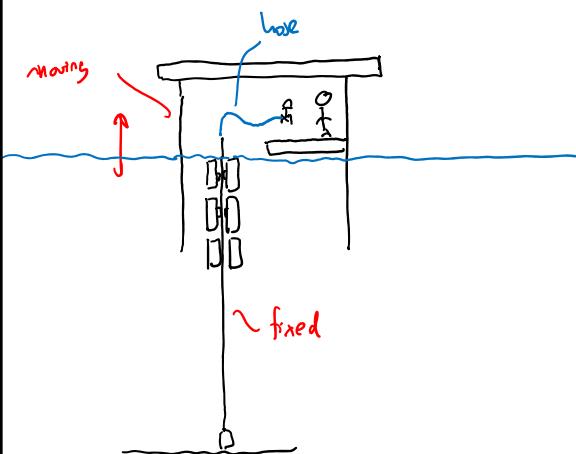


for "shallow" water depth  
dry well are  
called just like onshore well,  
the structure doesn't take  
the well weight



37

## Transfer of well weight to soil and to offshore structure



38

19

## Support system for dry X-mas trees – deep water

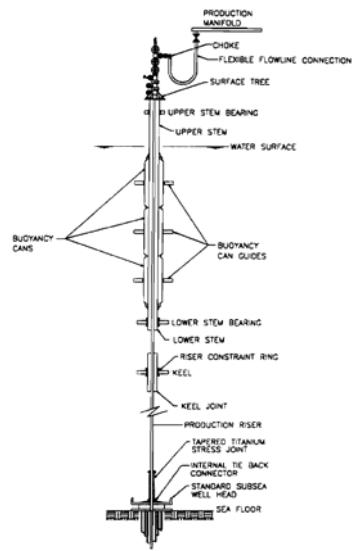
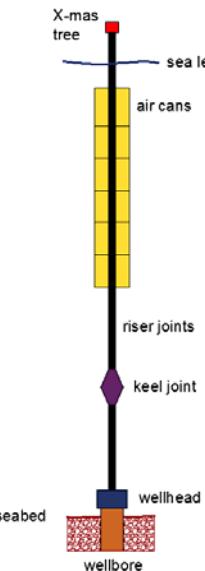


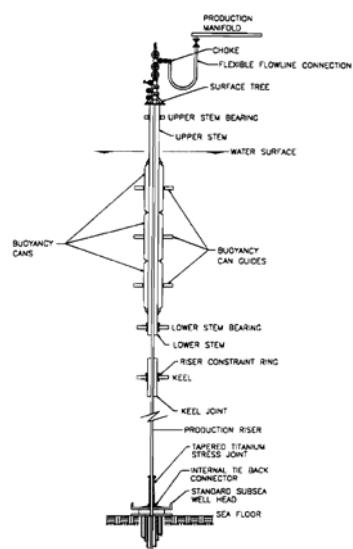
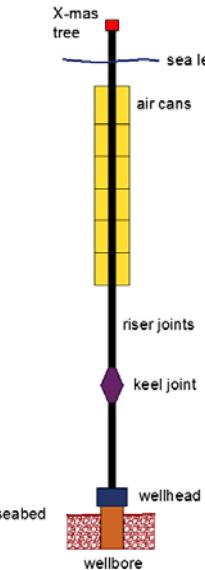
Figure 6 - Well System

OTC 8382

Neptune Project: Spar History and Design Considerations  
R.S. Glenville, J.E. Halkyard, R.L. Davies, A. Steer, F. Firth, Deep Oil Technology, Inc.

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## Support system for dry X-mas trees – deep water



**Real State on offshore structure is critical,  
not more slots than what is needed!**

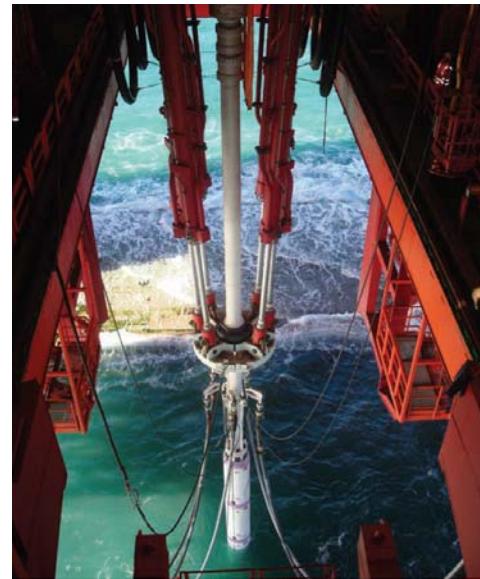
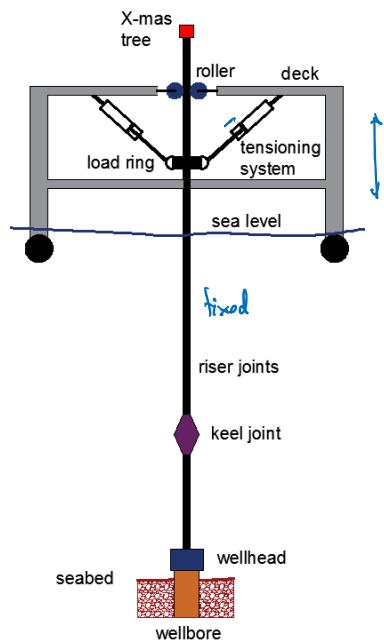
Figure 6 - Well System

OTC 8382

Neptune Project: Spar History and Design Considerations  
R.S. Glenville, J.E. Halkyard, R.L. Davies, A. Steer, F. Firth, Deep Oil Technology, Inc.

40

## Support system for dry X-mas trees – deep water



41

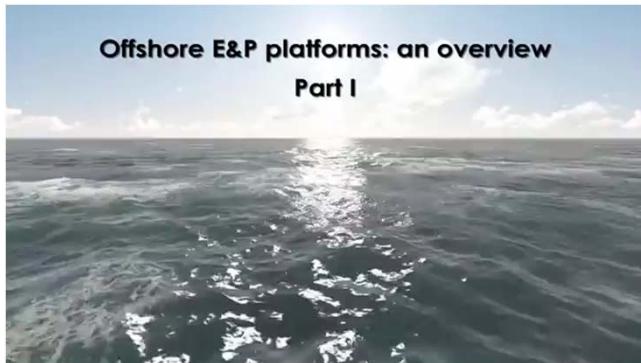
## Some selection criteria for offshore structures

- Water depth
- **Type of X-mas tree**
  - Well intervention needs
    - Tubing replacement
    - Completion modifications
    - Artificial lift (ESP)
  - Infill drilling needs
  - Reservoir spread and structure
- Need for oil/condensate storage
- Marine loads – Oceanographic environment
  - Wind, waves, current

Only floating structures SPAR, TLPs and Semi-subs have “small” movement ranges suitable for dry X-mas trees

42

## Possibility for jackets without drilling package



<https://www.youtube.com/watch?v=-vJmAvqn6dU>



43

## Possibility for jackets without drilling package



44

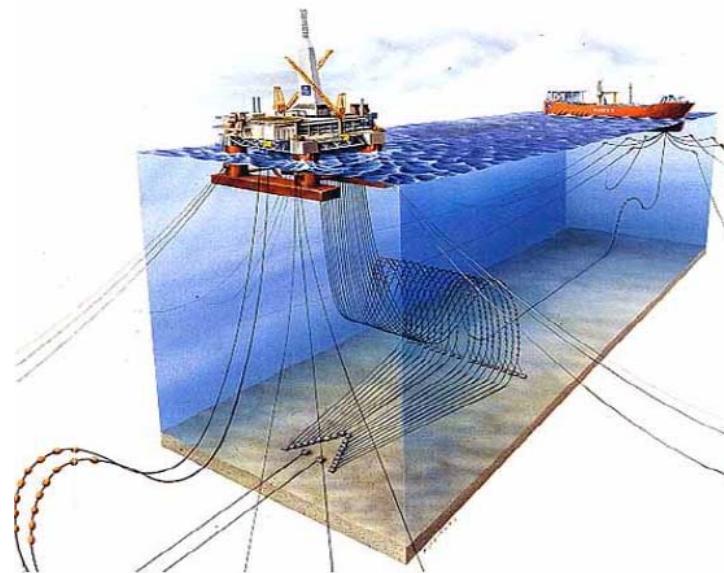
## Possibility for jackets without drilling package



<https://www.offshoreenergytoday.com/offshore-safety-watchdog-to-investigate-maersk-invincible-incident/>

45

## Njord: subsea wells with well intervention possibility



46

### Layout of subsea systems – template wells

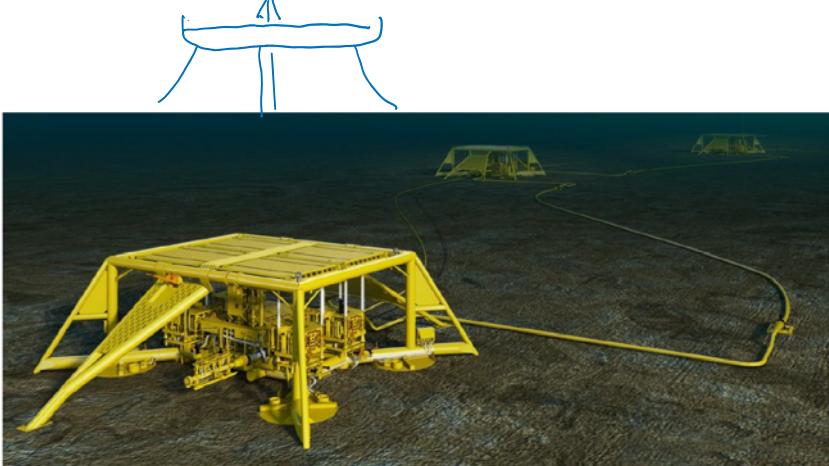
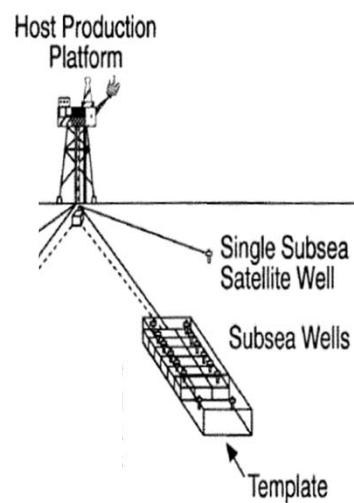


Figure 3.3 Typical NCS tie-back solution (Image: Statoil ASA)

47

### Layout of subsea systems – template wells



48

## Satellite wells

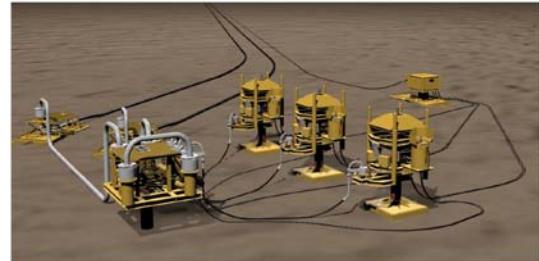
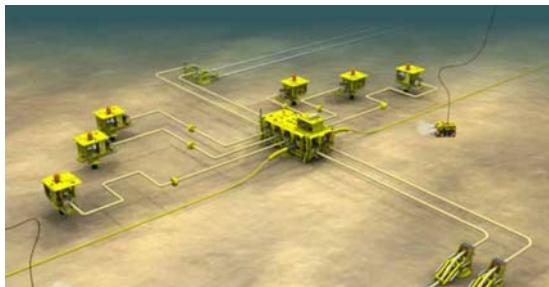
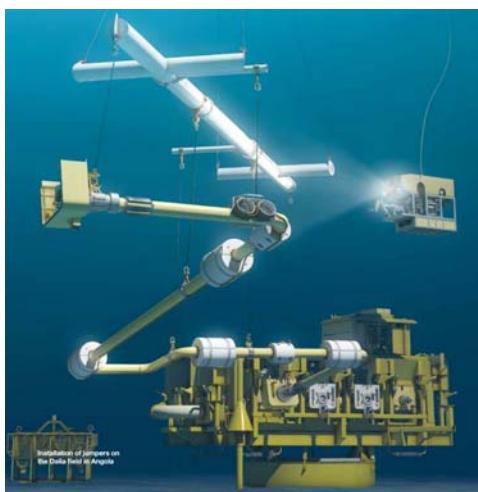


Figure 3.4 Typical GOM subsea tie-back

49

## Jumpers for satellite wells (if close)

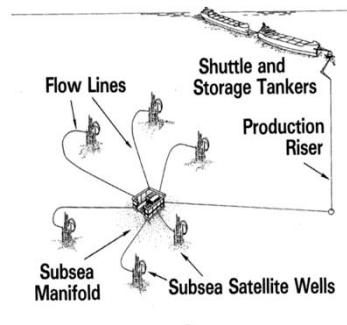


50

## Template wells vs satellite wells – similar dilemma to dry versus wet X-mas tree



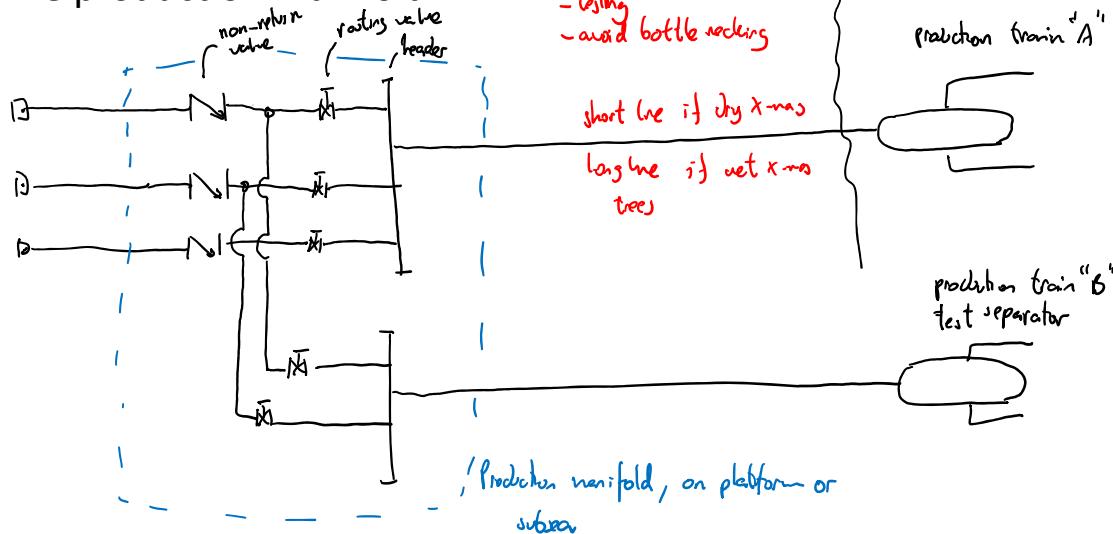
Figure 3.3 Typical NCS tie-back solution (Image: Statoil ASA)



- Long deviated wells
- Wells are drilled from one location, no need to spend rig mobilization time
- Less subsea equipment
- Shorter, vertical wells
- The drilling rig must be mobilized often which costs money
- More flowlines, pipelines. Manifolds are required

51

### The production manifold



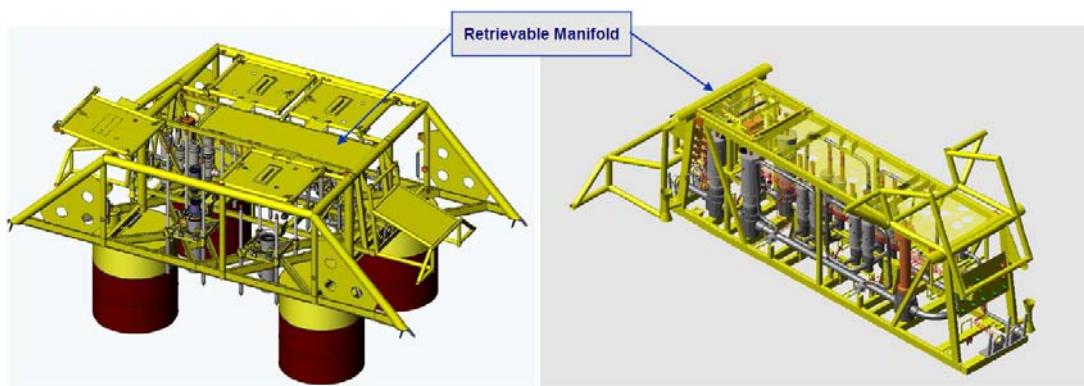
52

## The production manifold



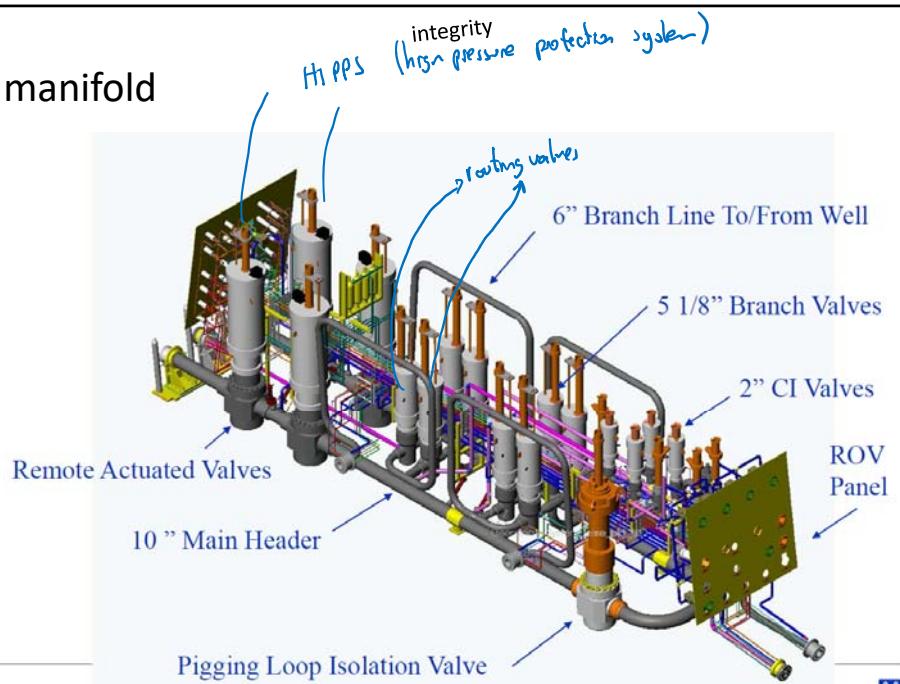
53

## 4 well template – the production manifold



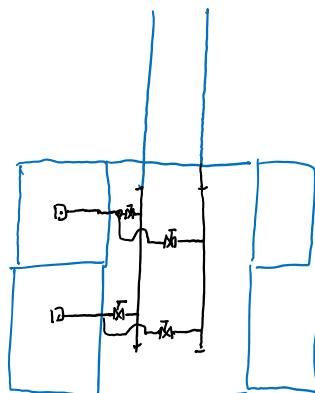
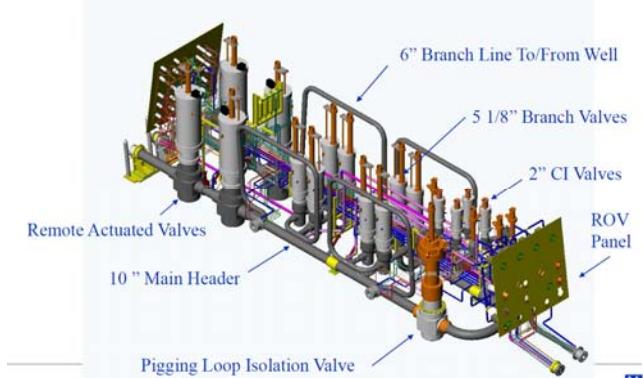
54

## The manifold



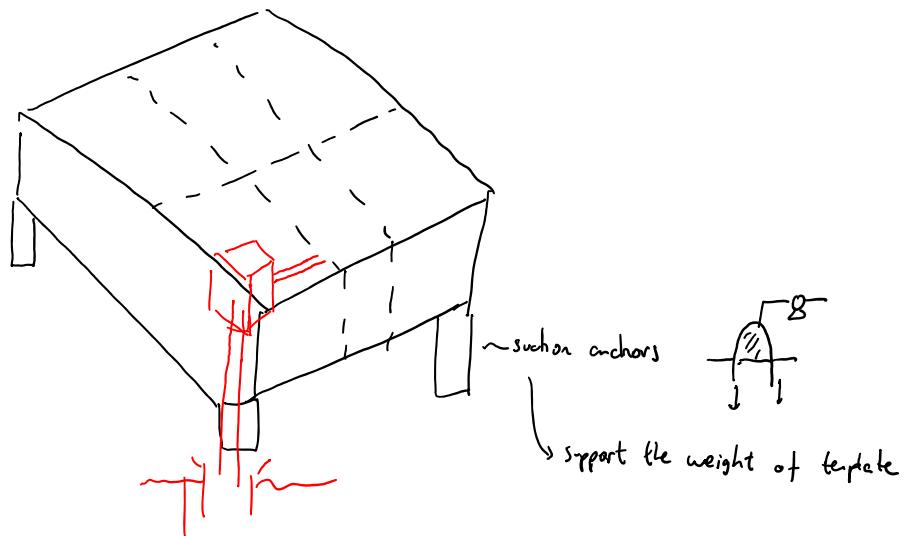
55

## The manifold – reality vs sketch



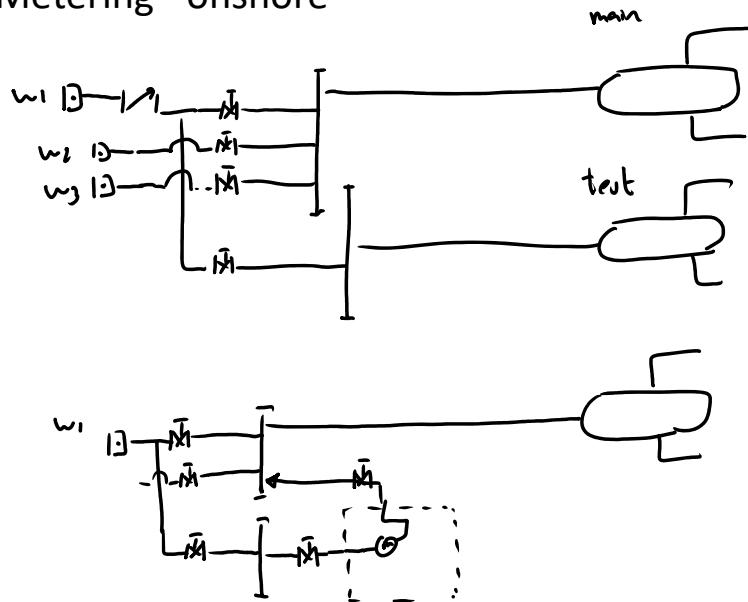
56

### 4 well template – weight transfer



## notes for Youtube video offshore structures 2

## Metering - onshore



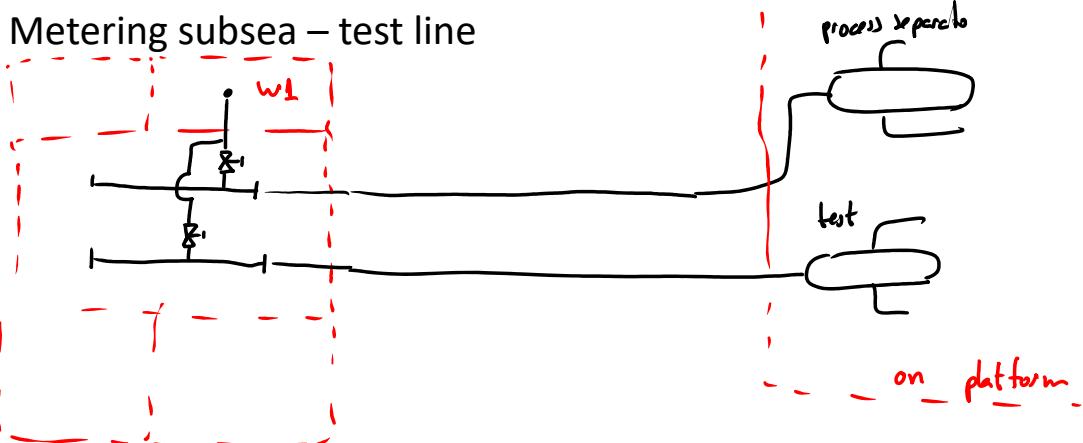
instead of separating, a multiplex meter can also be used, instead of a test separator

55

## Metering onshore – test separator

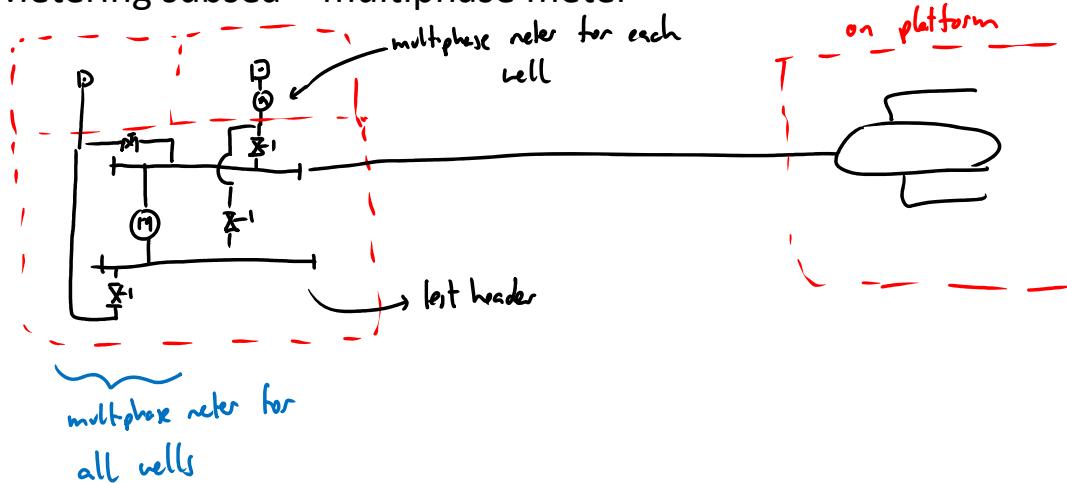


56



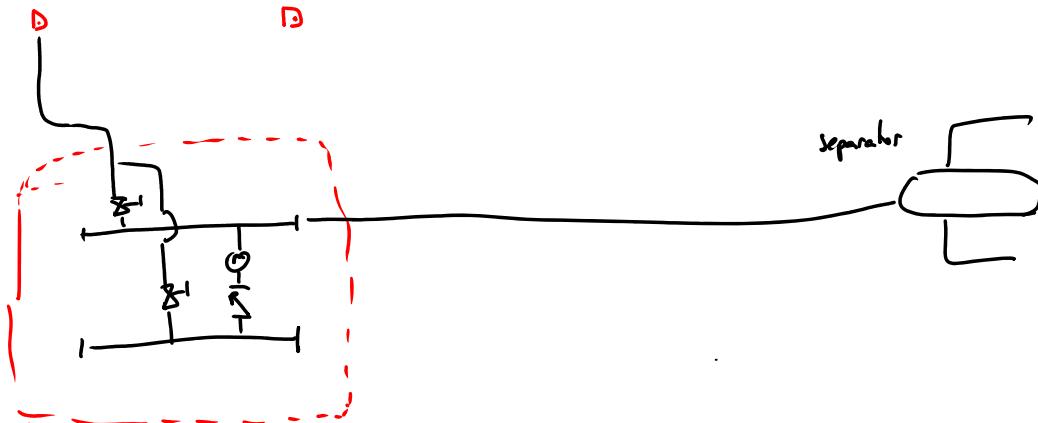
57

Metering subsea – multiphase meter



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*multiphase meter - satellite wells*



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## Metering requirements affect field layout - Brazil

**RESOLUÇÃO CONJUNTA ANP/INMETRO Nº 1, DE 10.6.2013 - DOU 12.6.2013 –  
RETIFICADA DOU 17.6.2013**

### 7.2.7. Testes de poços

7.2.7.1. Nos casos em que os resultados dos testes de poços sejam utilizados somente para

apropriação da produção aos poços, cada poço em produção deve ser testado com um intervalo entre testes sucessivos não superior a noventa dias, ou sempre que houver mudanças nas condições usuais de operação ou quando forem detectadas variações na produção.

7.2.7.2. Quando os resultados dos testes de poços forem utilizados para apropriação da produção a um campo, em casos de medição fiscal compartilhada, cada poço em produção deve ser testado em intervalos não superiores a quarenta e dois dias, ou sempre que houver mudanças nas condições usuais de operação ou quando forem detectadas variações na produção.

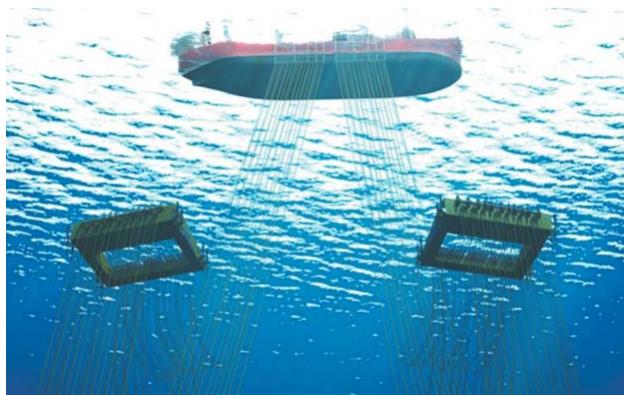
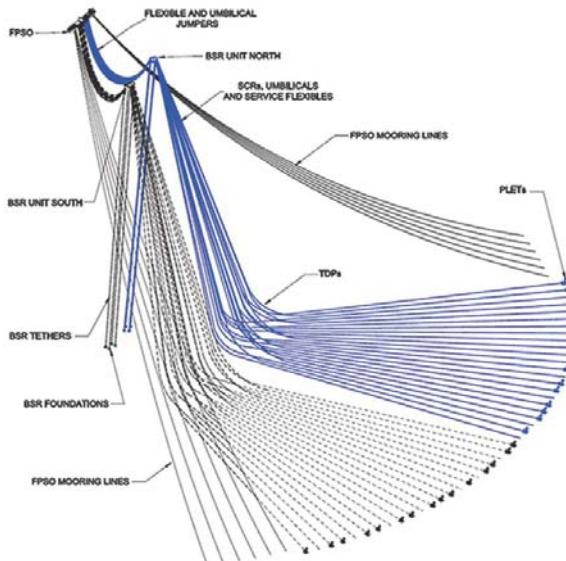
7.2.7.4. Devem ser utilizados separadores de testes ou tanques de testes nos testes de poços. Outros métodos de testes, utilizando novas tecnologias, devem ser previamente aprovados pela ANP.

<http://www.anp.gov.br/wwwanp/?dw=66648>

60

## Metering requirements - Brazil

\$\$\$



<https://www.marinetechologynews.com/news/reviewing-sapinho-system-564661>

61

## Metering requirements - Norway

[http://www.npd.no/Global/Engelsk/5-Rules-and-regulations/NPD-regulations/Maaleforskriften\\_e.pdf](http://www.npd.no/Global/Engelsk/5-Rules-and-regulations/NPD-regulations/Maaleforskriften_e.pdf)

**REGULATIONS RELATING TO MEASUREMENT OF PETROLEUM FOR FISCAL PURPOSES AND FOR CALCULATION OF CO<sub>2</sub>-TAX (THE MEASUREMENT REGULATIONS)**

*Multiphase measurement*

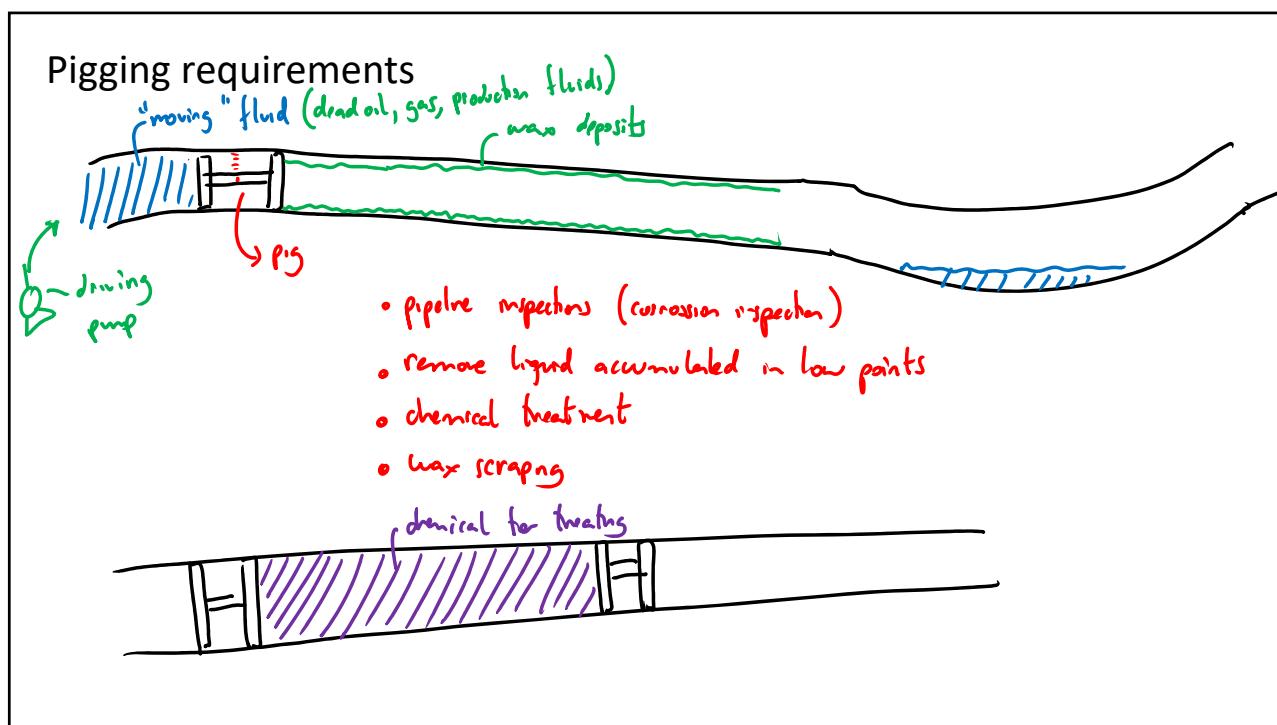
Multiphase measurement may be used if traditional single phase measurement of hydrocarbons is not possible for financial reasons. The multiphase meter can then be used as a fiscal meter.

The following elements shall be satisfactorily documented to allow use of a concept based on multiphase measurement, cf. Chapter VII and Section 18:

- The operator shall present a concept to the Norwegian Petroleum Directorate for comments and formal processing well before submitting the Plan for Development and Operation (PDO). An estimate of the expected measurement uncertainty shall be presented, combined with financial figures for the risk of loss between production licenses (cf. NORSOX I-105), Annex C.
- The main principles of the operations and maintenance philosophy shall be described.
- Possibility to calibrate meters against test separator or other reference.
- Redundancy in sensors and robustness in the design of the measurement concept.
- Relevant PVT (equation of state) model and representative sampling opportunity to be able to perform a sound PVT calculation.
- Design of inlet pipes to ensure similar conditions if multiple meters are used in parallel.
- Flexibility in the system for handling varying GVF (gas volume fraction).
- The planned method for condition monitoring and/or planned calibration interval shall be described.
- The planned method and interval for sampling and updating PVT data shall be described.

When the multiphase meters are part of the fiscal measurement system, they shall be treated as other fiscal measurement equipment and the administrative requirements which apply pursuant to these Regulations shall therefore be fulfilled.

62

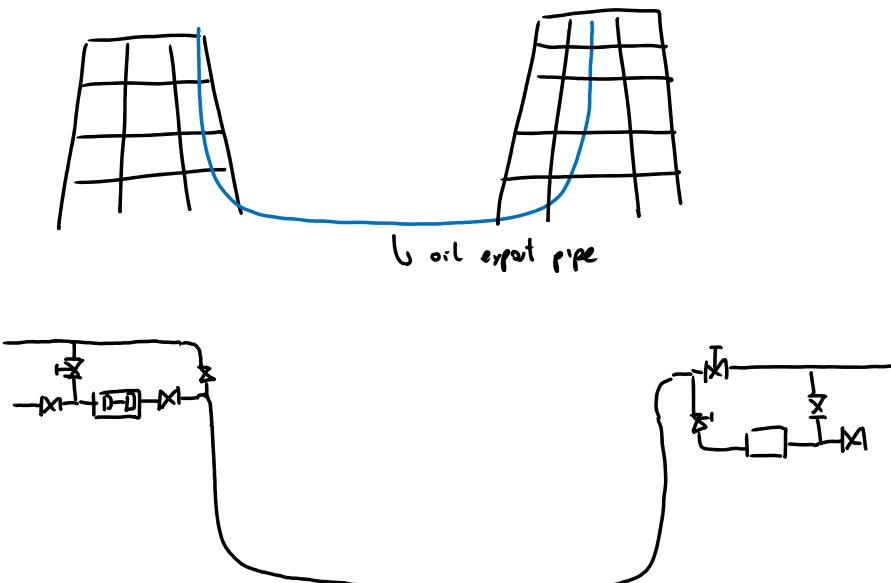


63

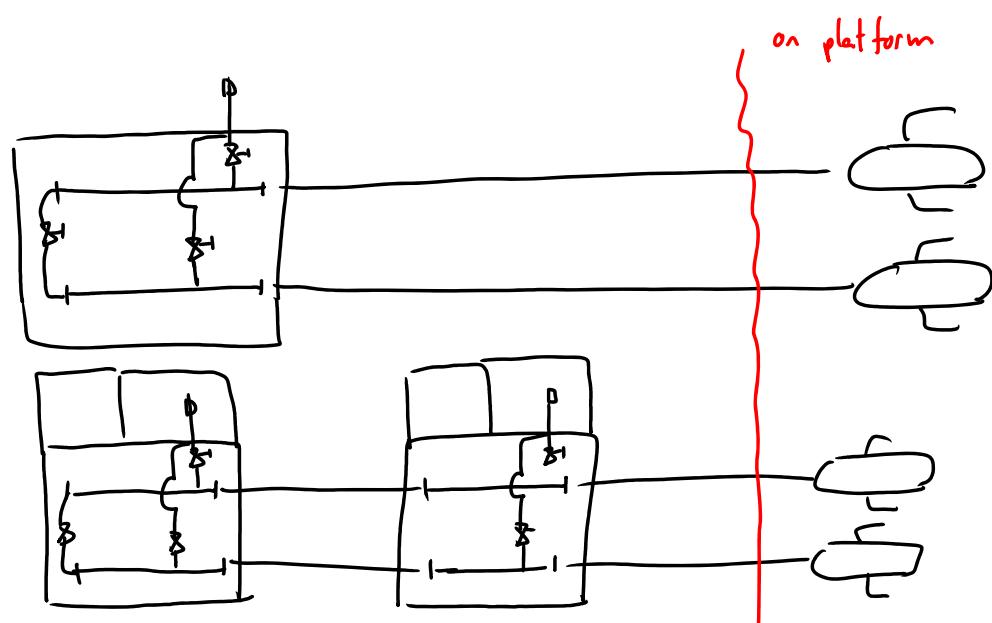


64

### Pigging loop and subsea pig launcher

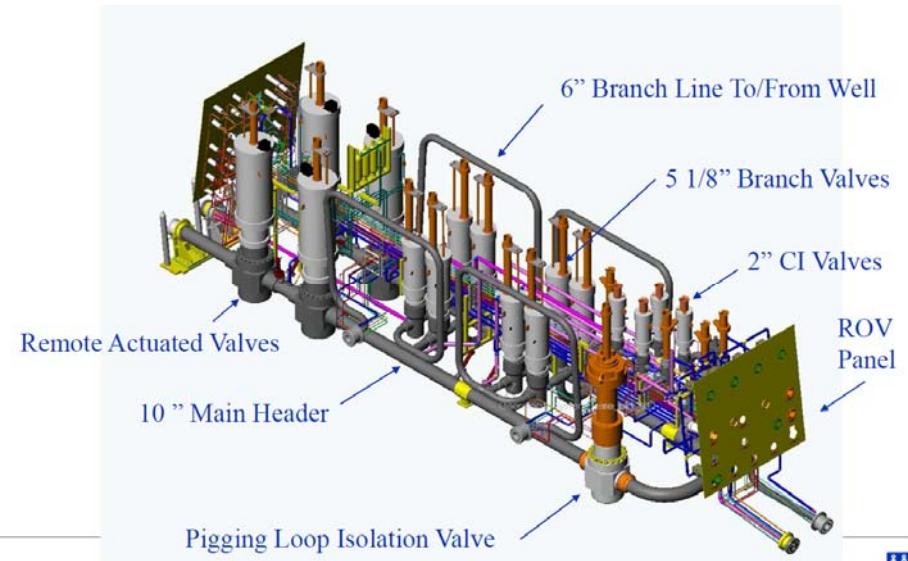


65



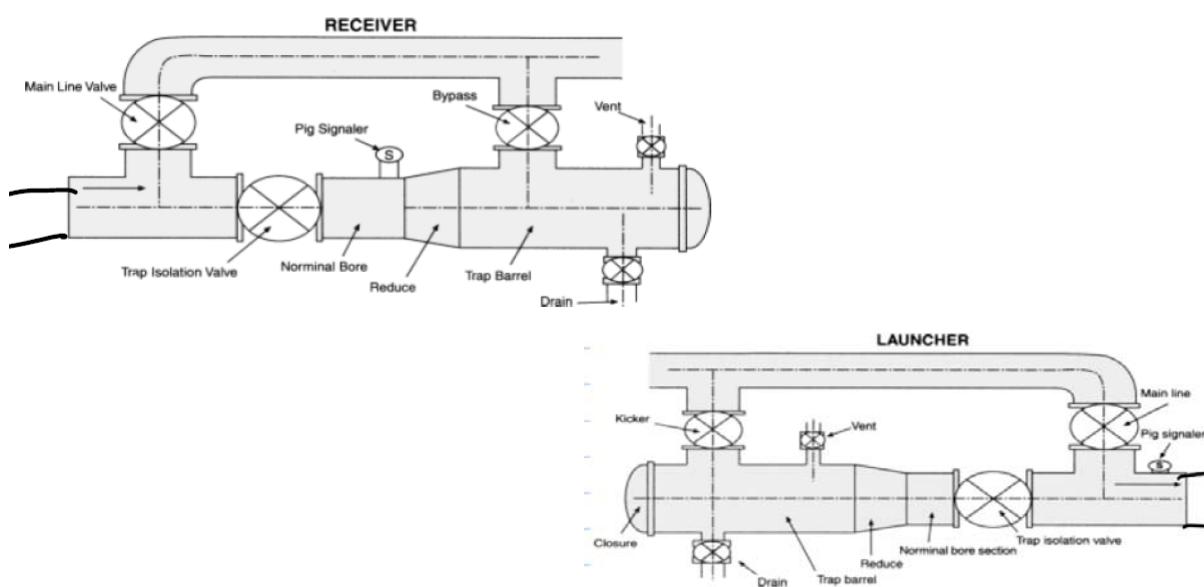
66

## The pigging valve



67

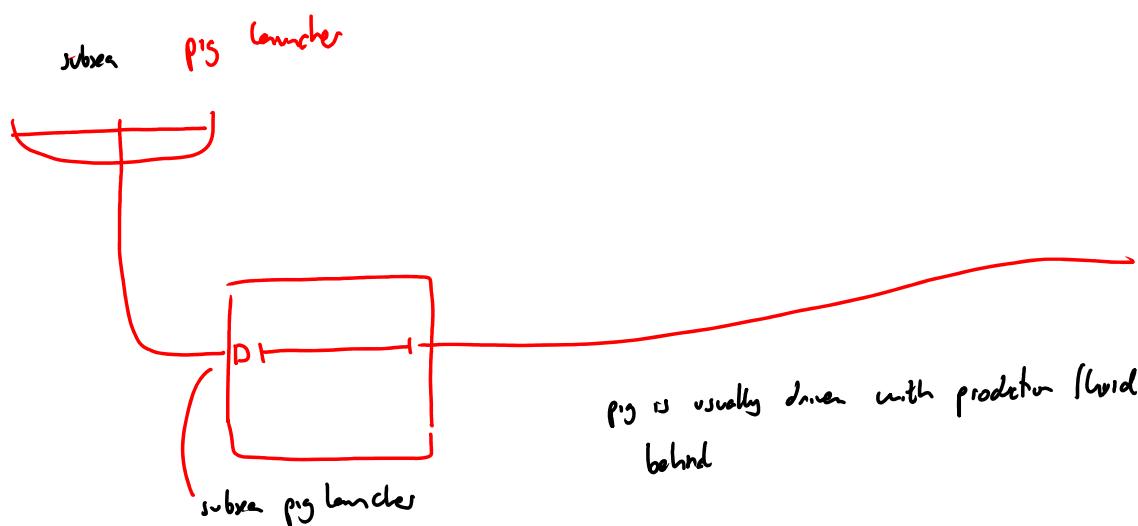
## Pig launcher and receiver



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## Pigging - video

69



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## Summary table

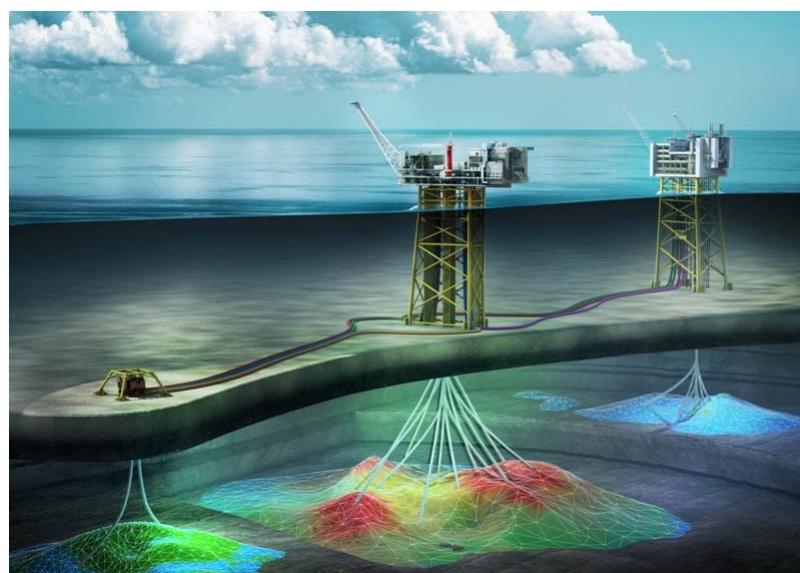
	Dry X-mas trees	Wet X-mas trees
Deep water (1700 m+)		X
Reservoir is “spread” or multiple reservoirs		X
Frequent well intervention	X	
Flow assurance concerns	X	
Plans for infill drilling (and coping with reservoir uncertainty)*	X	X
Progressive production startup		X

Jacket, GBS, SPAR,  
TLP

ALL

71

## Combinations can be used



<https://www.akerbp.com/en/our-assets/production/ivar-aasen/the-development-solution/>

72

## Some selection criteria for offshore structures

- Water depth
- Type of X-mas tree
  - Well intervention needs
    - Tubing replacement
    - Completion modifications
    - Artificial lift (ESP)
  - Infill drilling needs
  - Reservoir spread and structure
- **Need for oil/condensate storage**
- Marine loads – Oceanographic environment
  - Wind, waves, current

73

### Need for liquid storage

No or limited storage	Steel Jackets, Semi-subs, TLPs, Spars <sup>20</sup>
Medium - Large storage (up to 2.500.000 STB)	FPSOs, GBS

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## Other selection criteria for offshore structures

- Previous experience
- Riser issues
- Topside upgrade flexibility
- Manufacturing workshop availability
- Maturity of technology
- Maintenance and OPEX

Class 20240411

**Outline:**

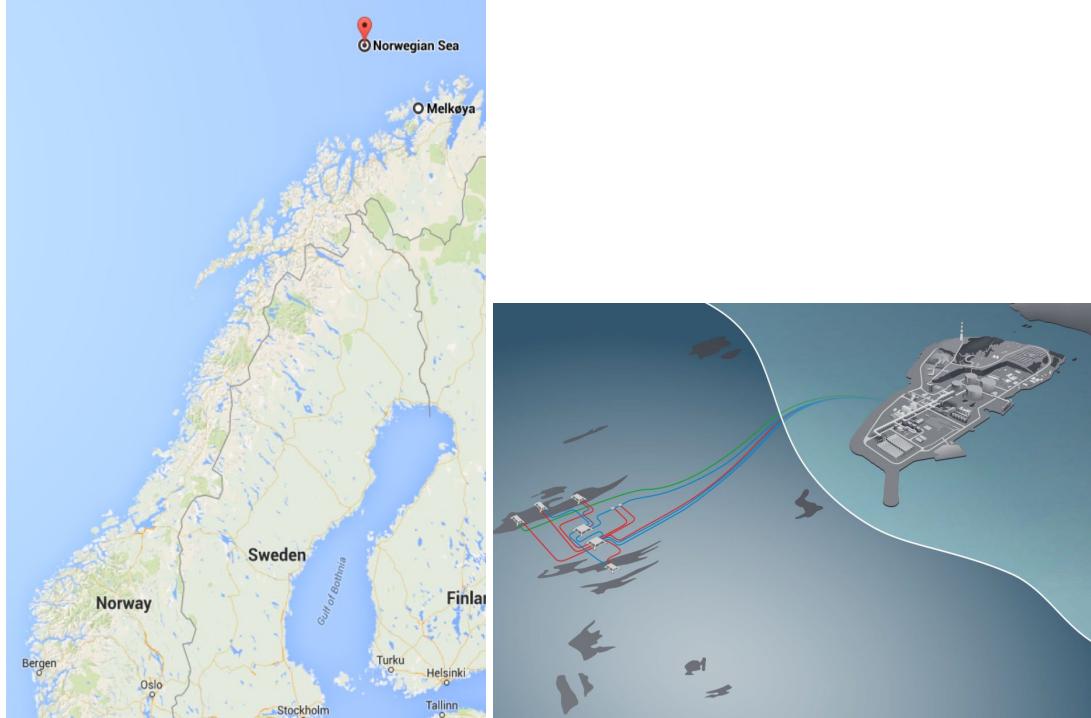
Recap of content covered in previous weeks:

- How to quantify the effect of uncertainty in field development
- Offshore structures

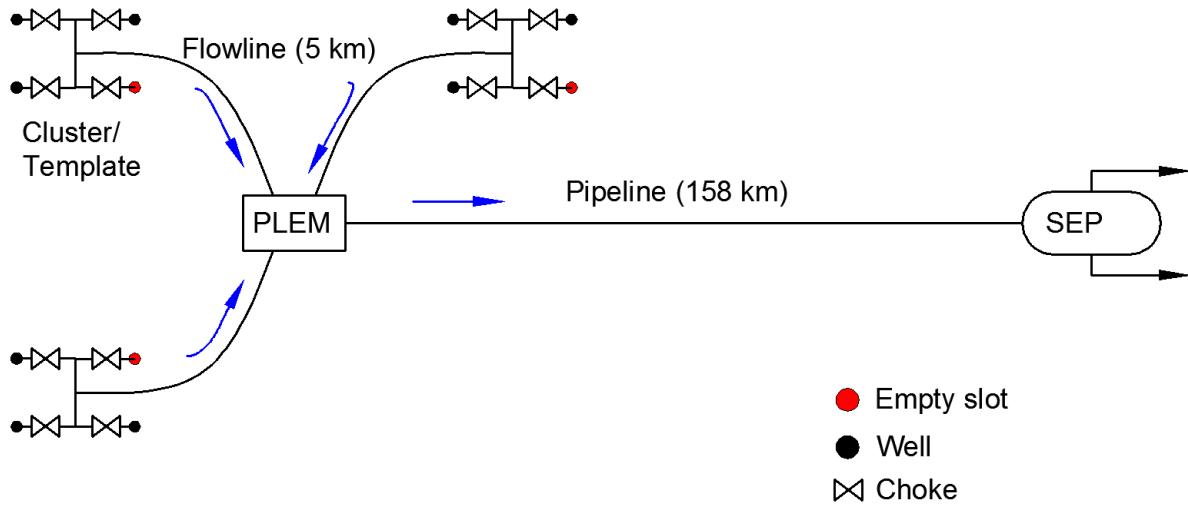
Review of exam questions (2023) related to offshore structures

## **Flow assurance analysis of the Snøhvit pipeline using Hysys**

Snøhvit is an offshore gas field located in the Barents Sea 158 km from Hammerfest currently under development. The field will be developed with the “subsea to beach” concept. The gas production will be taken by an LNG plant and transported further in LNG carrier to customers in US and Spain. The plateau rate of the field has been set to 20 E6 Sm<sup>3</sup>/d and Equinor plans to maintain it until year 2032.



According to the base case Scenario (BCS) selected for the study, the field is completed subsea with three subsea templates, each with 3 wells.



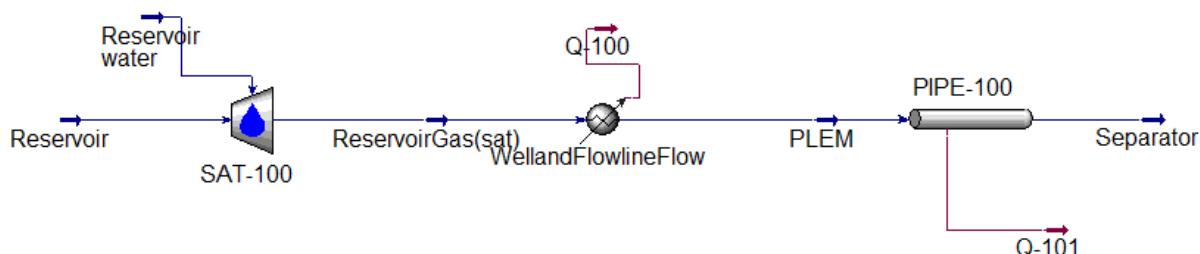
You are asked to perform a steady-state, 1D simulation using the simulator Hysys to compute pressure and temperature drop along the main transportation pipeline from the PLEM to the slug catcher. The main goal is to assess hydrate formation. You have to perform your calculations for the plateau phase.

**Tasks:**

- Tabulate and plot pressure, temperature and liquid holdup along the pipeline. Compute the total amount of liquid in the pipeline (this can be calculated by integrating the holdup along the pipeline).
- Plot the phase envelope (p-T diagram) of the gas mixture illustrating the saturation lines (bubble and dew point lines) and the quality lines inside the two-phase region (0.01, 0.02, 0.03, 0.04, 0.05, 0.1, 0.2). Plot also the hydrate line provided. Indicate in your plot the following:
  - Cricondenbar and Cricondentherm points
  - Plot the p-T along the pipeline on top of the p-T diagram. Detect if there is any condensate retrograde behavior. In this context condensate retrograde behavior is when the liquid stops condensing in the pipeline and it starts evaporating (the quality,  $m_{\text{liquid}}/m_{\text{total}}$ , starts to diminish)
  - Will hydrates form in the pipeline?

**Solving suggestions**

- Suggested layout in Hysys is shown below. First saturator representing saturation with water at reservoir conditions (276 bara and 92 °C), then heat exchanger, to bring pressure and temperature of the stream from reservoir conditions to plem conditions. Then pipeline to model pressure and temperature drop in the pipeline.

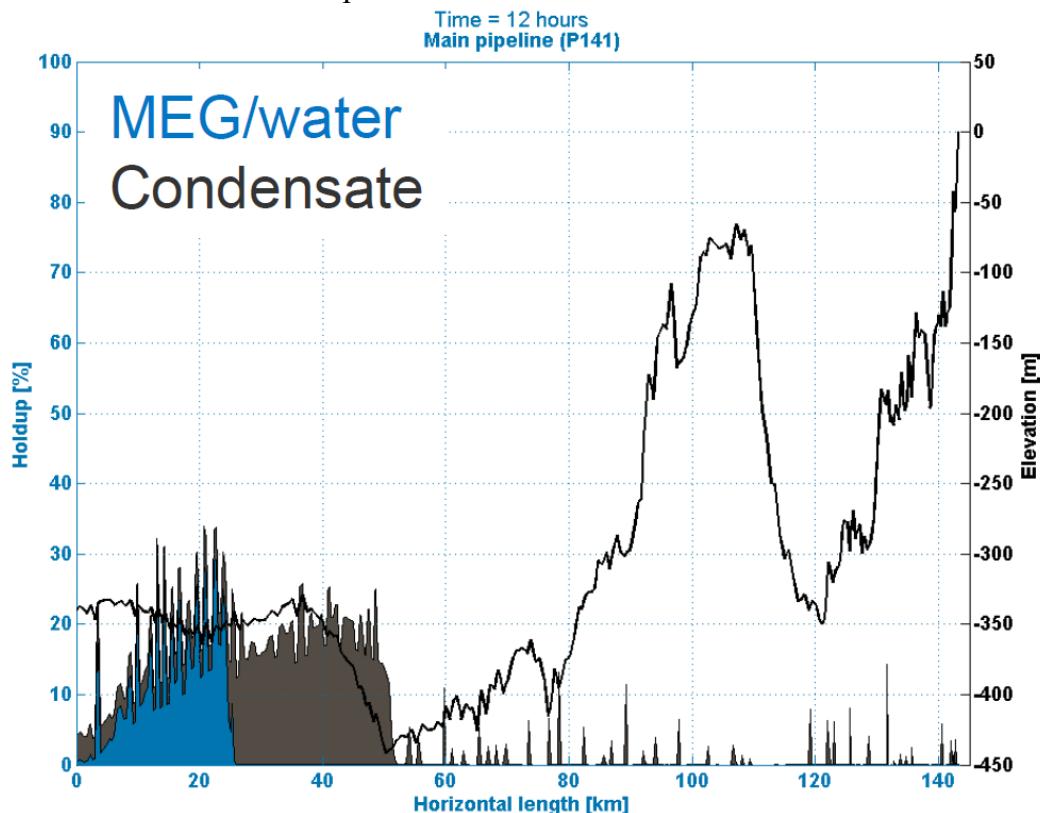


Pressure and temperature are specified in the streams “Reservoir water”, “Reservoir” and “PLEM”. Composition is specified in Streams “Reservoir water” and “Reservoir”. Mass rate is specified in stream “Reservoir”. The mass rate can be estimated by multiplying the standard conditions gas rate of the field times the density of the gas at standard conditions ( $20 \times 10^6 \text{ Sm}^3/\text{d} \times 0.67 \text{ kg/m}^3$ )

- Remember that Hysys performs its calculations co-current. This means that you provide a plem pressure and temperature, and a molar rate at the inlet of the pipeline, then Hysys calculates the separator pressure. However, separator pressure has to be 30 bara. Therefore, it is necessary to use an ADJUST to iterate on plem pressure to get 30 bara at the separator.
- Get the points for the elevation profile of the pipeline using the webplot digitizer <https://automeris.io/WebPlotDigitizer/>
- Water should be included in your calculations. Assume the well stream is saturated with water at reservoir pressure and temperature (92 °C). For this use the water saturator unit available in hysys.
- There might be a mismatch between the pressure drop calculations in Hysys and the ones performed previously with Excel. Hysys considers the effect of liquid on the pipe and the variation of density and viscosity of the fluids.
- Use increments of 1 km for your calculations.
- The hydrate equilibrium line can be found in the “envelope” attachment to a stream in Hysys.

## Available information

- Pipeline profile. Use the program webplotdigitizer (<https://automeris.io/WebPlotDigitizer/>) to “steal” the points from the chart below. Use at least 10 points.



Pout (Slug catcher pressure)	[bara]	30
Tseabed	[C]	6

Component	Mole %
Nitrogen	2.525
Carbondioxide	5.262
Methane	81.006
Ethane	5.027
Propane	2.534
i-Butane	0.4
n-Butane	0.83
i-Pentane	0.281
n-Pentane	0.308
Hexanes	0.352
Heptanes	0.469
Octanes	0.407
Nonanes	0.203
Decanes+	0.397

Density of Decane+: 814 kg/m<sup>3</sup>

MW of Decane+: 172 kg/kmol

The overall heat transfer coefficient of the pipeline assuming that the pipe is “naked” is: 10 W/m<sup>2</sup> K

Pipe diameter information:

Inner diameter of the steel pipe ID, [mm]	<b>678.2</b>
Outer diameter of the steel pipe OD [mm]	<b>711.2</b>

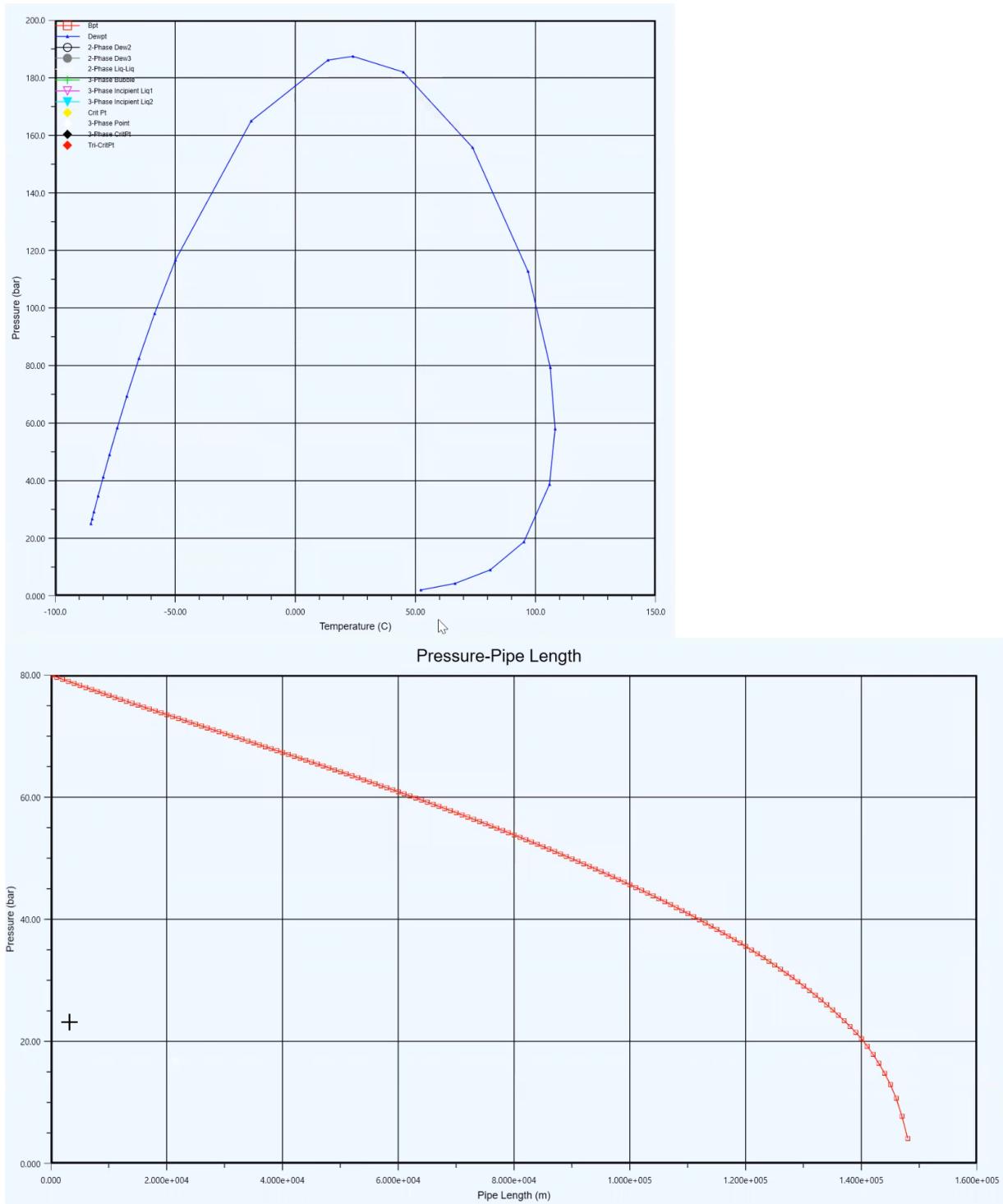
### **Some help with Hysys:**

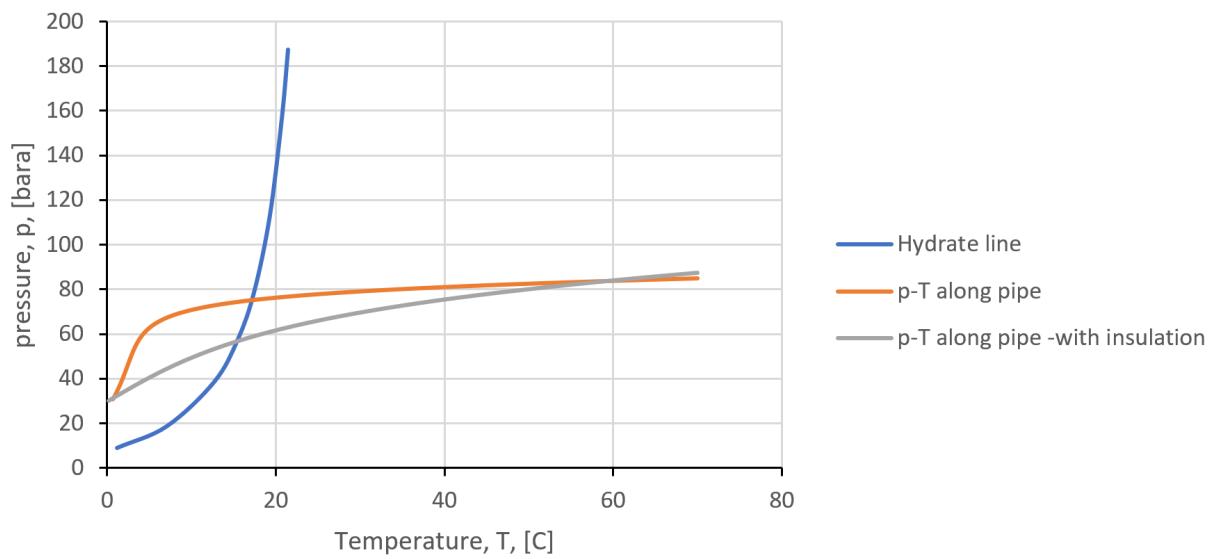
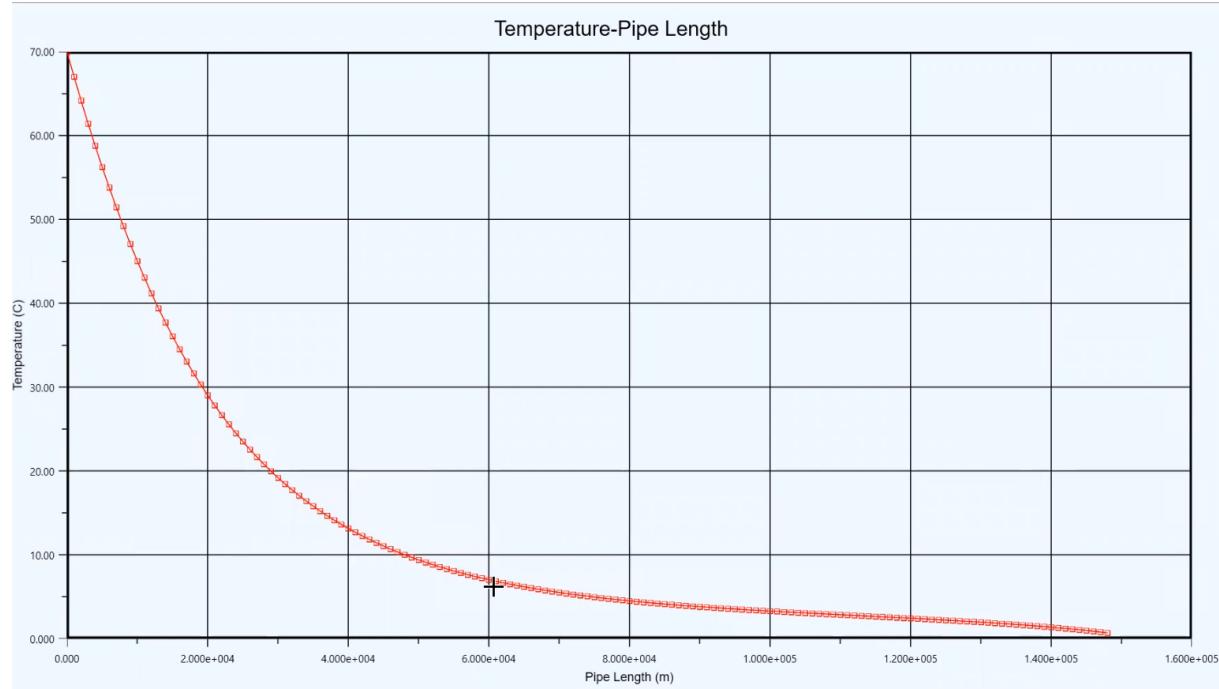
You can run Hysys remotely from your computer using

<https://farm.ntnu.no>

Alternatively, Hysys is installed in some computers in the computer lab on the 3rd floor.

### Solution (worked out in class):





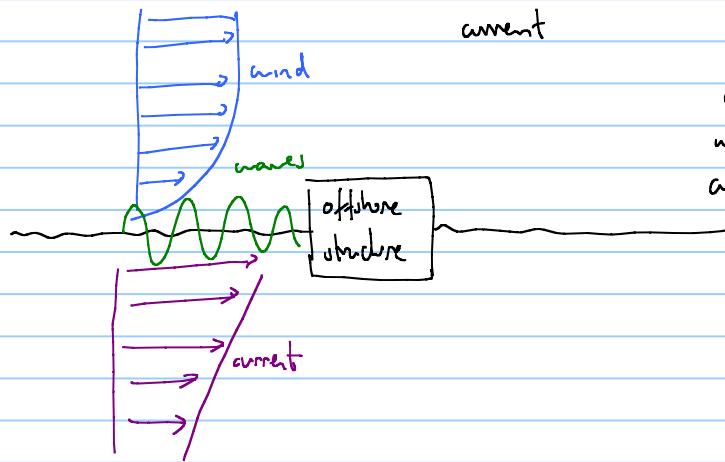
Note Title

## Notes for Youtube video Marine loads and offshore structures for hydrocarbon production

Offshore structure for oil and gas production

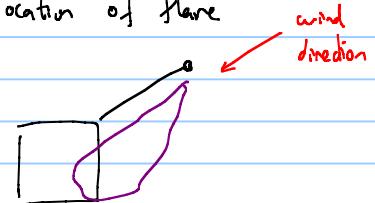
- effect of oceanographic environment: wind

waves  
current

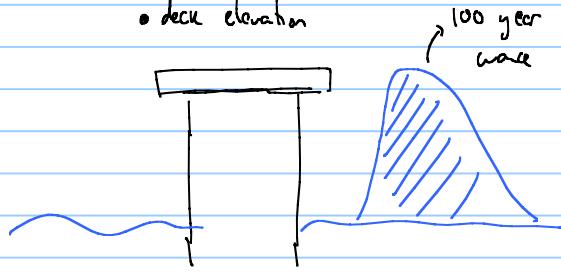


and must be taken into account  
waves when designing the offshore  
current structure

- location of flare



- deck elevation



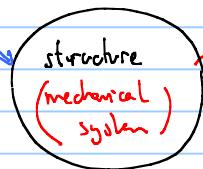
- design wave, for a range of periods  
↳ most likely in the area

- storm (100 year storm)

- long term variations  $\rightarrow$  fatigue

forces and

wave loads  
on structure  
(t)



$\rightarrow$  movement (t)  
stress (t)  $\rightarrow$  maximum stress  
fatigue design

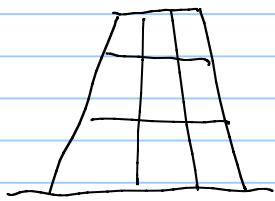


each structure, depending on its characteristics (mass, flexibility, damping)

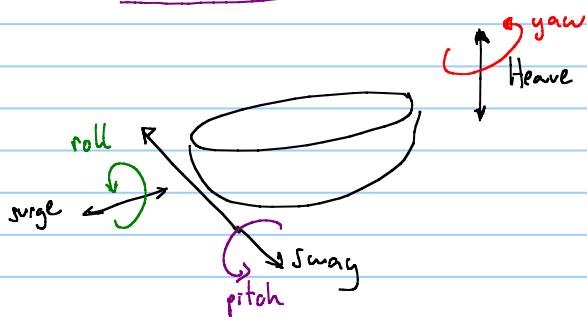


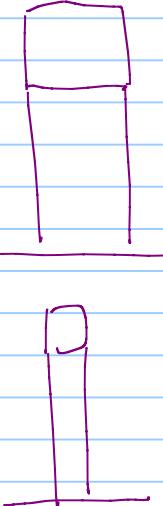
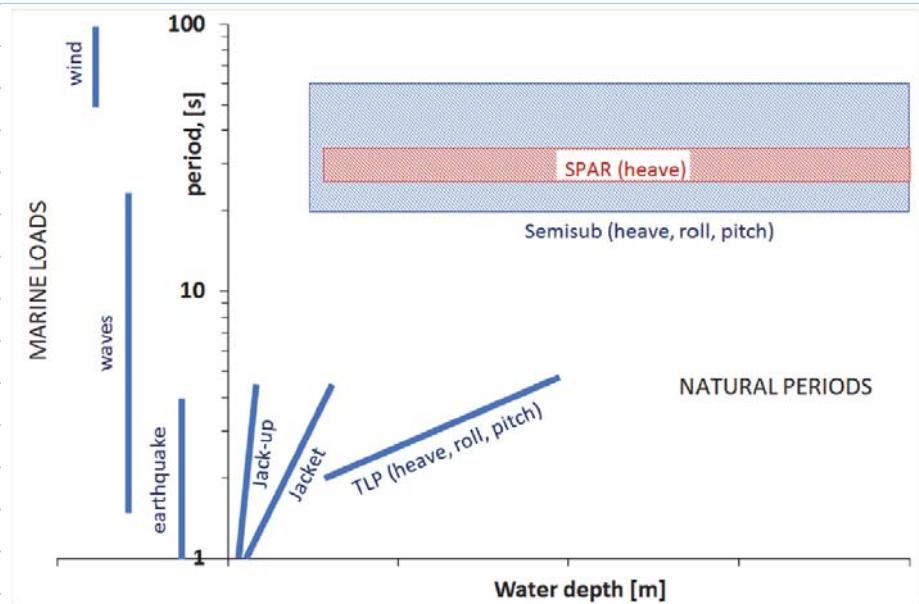
will have a natural frequency that if excited at this frequency might exhibit maximum movement and stress.

fixed structure

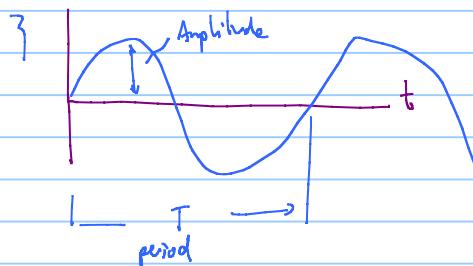


floating structure





$$\text{Response amplitude operator (RAO)} = \frac{\text{amplitude of response}}{\text{amplitude of excitation}} = \frac{\text{Heave [m]}}{\text{wave amplitude [m]}}$$



$$RAO = 2$$

$$f = \frac{1}{T} \text{ cycle/s}$$

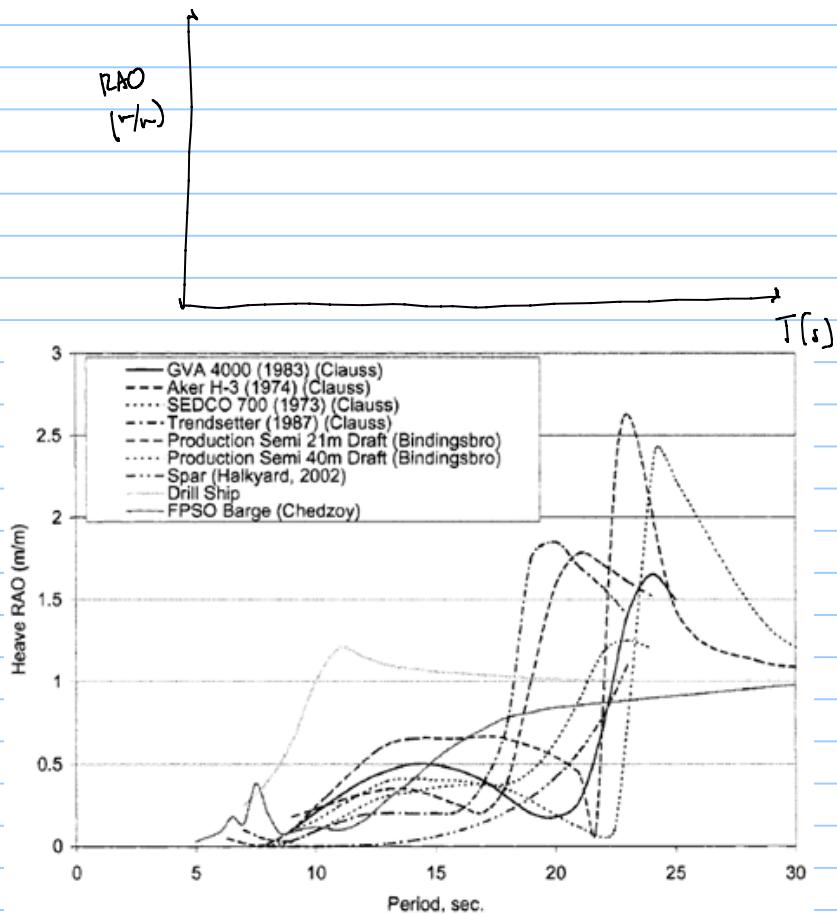
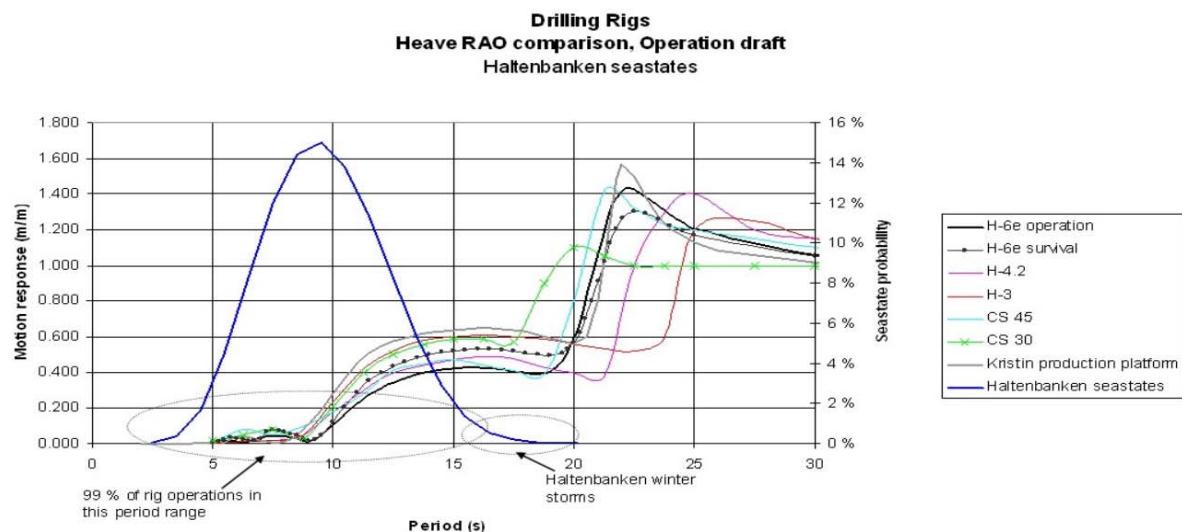
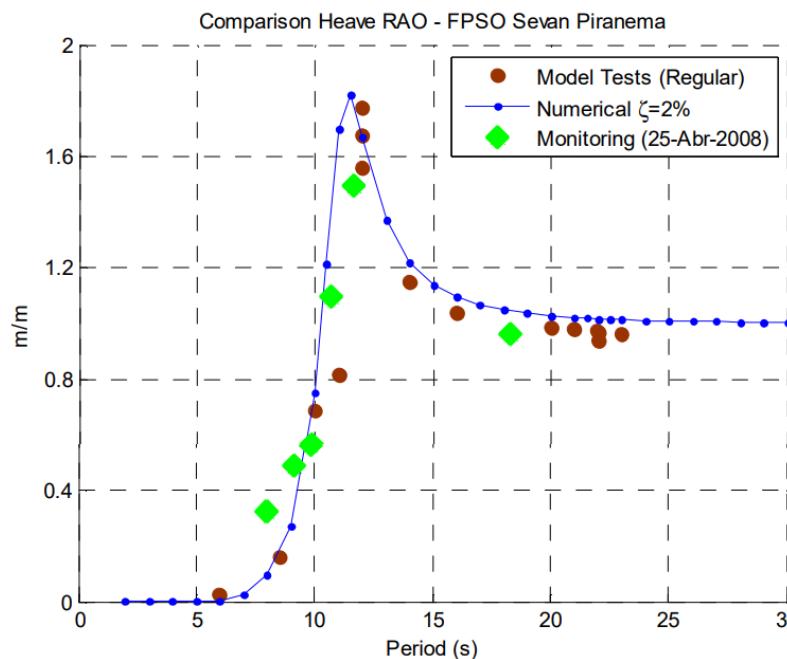
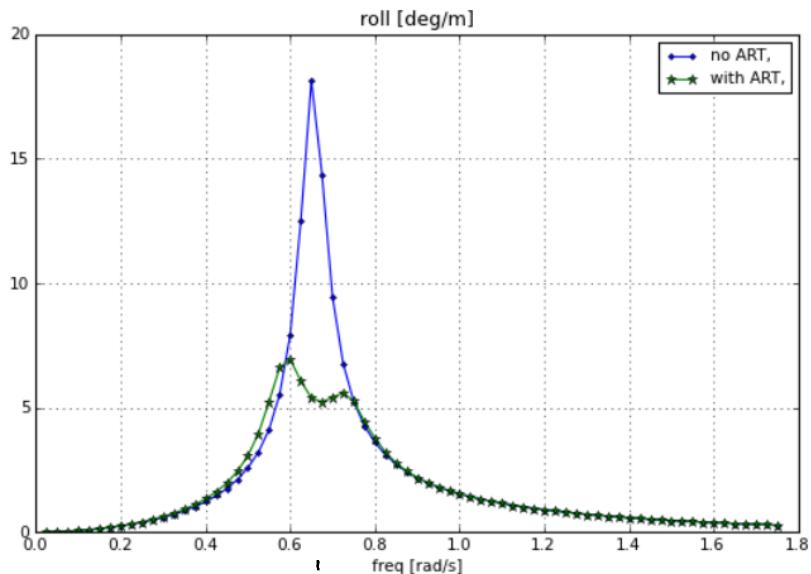


Figure 7.3 Example heave RAOs of various floaters

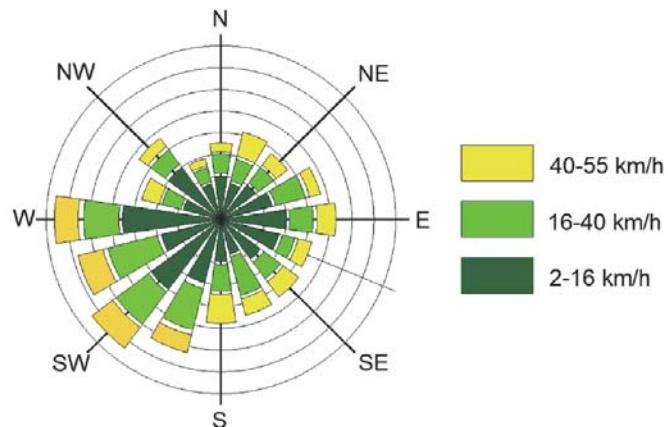


**Figure 16.2:** RAO published on the AKER Drilling website.



**Figure 1:** Typical RAO of roll of a ship with and without ART.

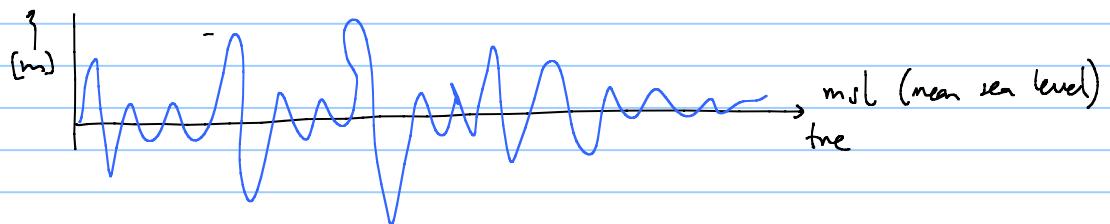
Wind



wind rose

wind and current are typically assumed constant and using the maximum value. (wind direction also must be taken into account)

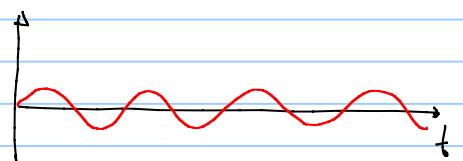
Waves



Fourier

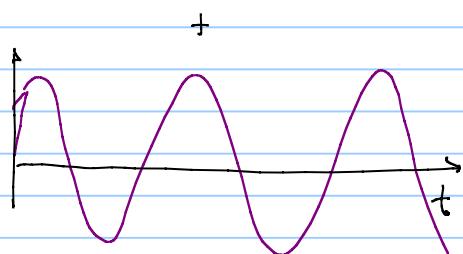
$$f(t) = \sum_{i=1}^N A_i \sin(\omega_i t + \phi_i)$$

~ phase shift  
amplitude ( $m$ )

angular frequency  $\omega_i = 2\pi f_i$ 

$$\omega_i = \frac{\text{rad}}{\text{s}}$$

$$\left[ \frac{\text{cycle}}{\text{s}} \right] \left[ \frac{2\pi \text{ rad}}{\text{cycle}} \right]$$

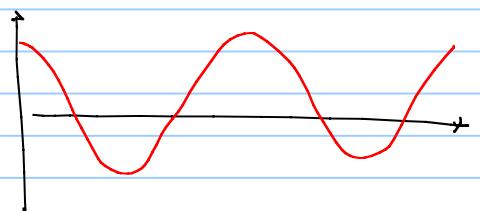


Discrete Fourier transform

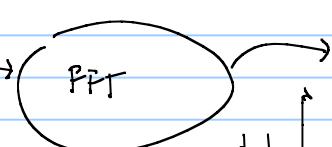
FFT Fast Fourier transform

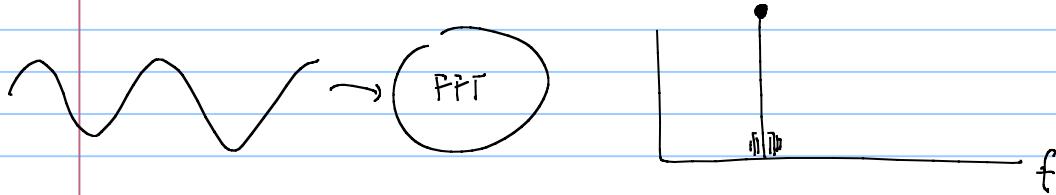
spectral peak period  
dominant frequency

=



$t$	value
D	D
D	D
D	D
D	D

(A<sub>i</sub>)sometimes analytical  
equations are used  
Pierson-Moskowitz, JONSWAP



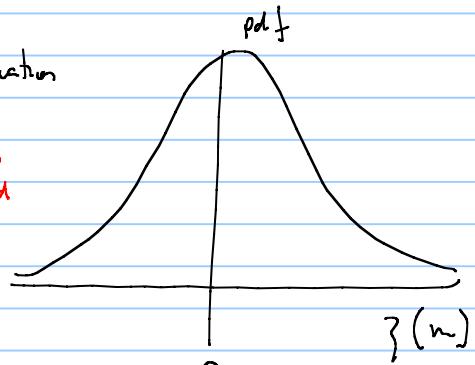
to deal with the variability of waves in time, we apply FFT on the signal and report spectral peak period

the spectral peak period does not change significantly in 3 hours  
sea state

what to do with amplitudes?

statistics on wave elevation

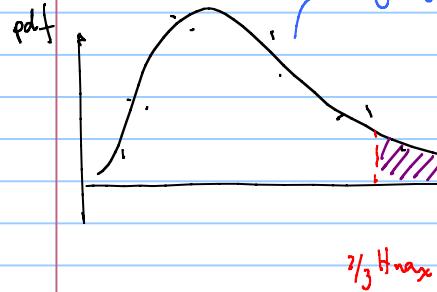
wave height



Rayleigh distribution

mean: significant wave height  
 $H_s$

$H_{max}$  [m]



to characterize a sea state (3 hrs)  $H_s$  and  $T_p$  are used

wave Data must be gathered for at least 2 years to obtain a representative sample of wave conditions in the area

How many sea states are in 2 years

$$2 \text{ years} \quad \frac{365 \text{ day}}{\text{year}} \quad \frac{24 \text{ hrs}}{\text{day}} \quad \frac{1 \text{ sea state}}{3 \text{ hr}} = 5840$$



with all measured data, compute  $T_p$ ,  $H_s$  for all

Scatter diagram of long term wave statistics

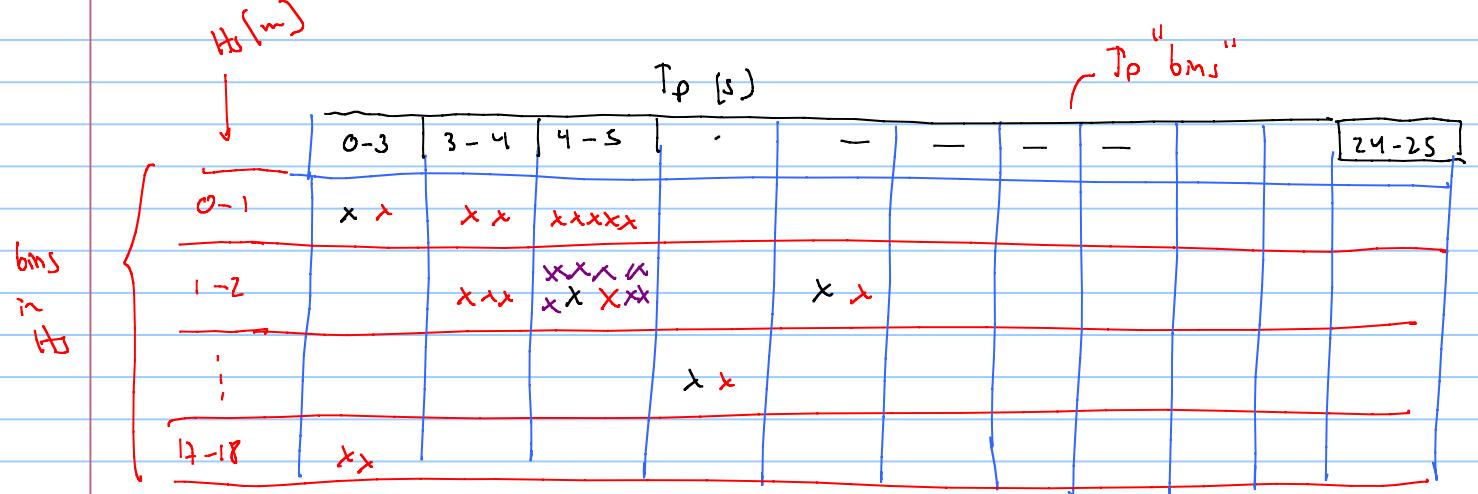
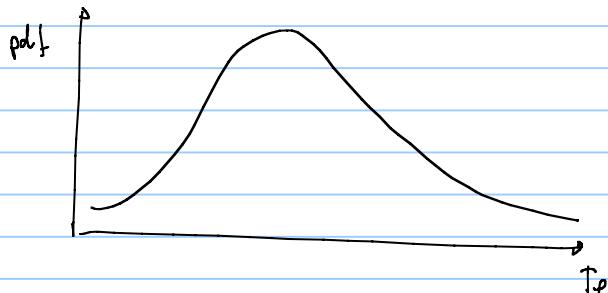


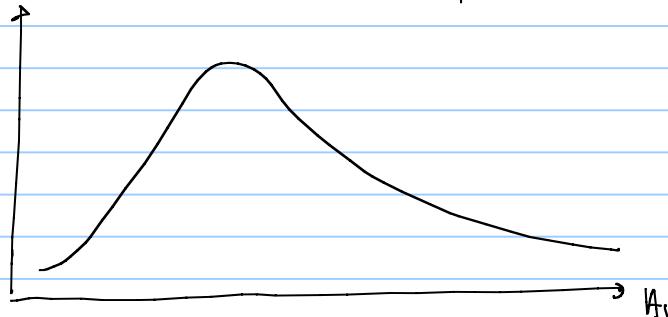
FIGURE 6-18. SCATTER DIAGRAM OF LONG TERM WAVE STATISTICS

for a fixed wave  $H_s$



$\frac{292172}{2420} \approx 120$  years  
 $\frac{\text{stages}}{1 \text{ year}}$

for a fixed  $T_p$

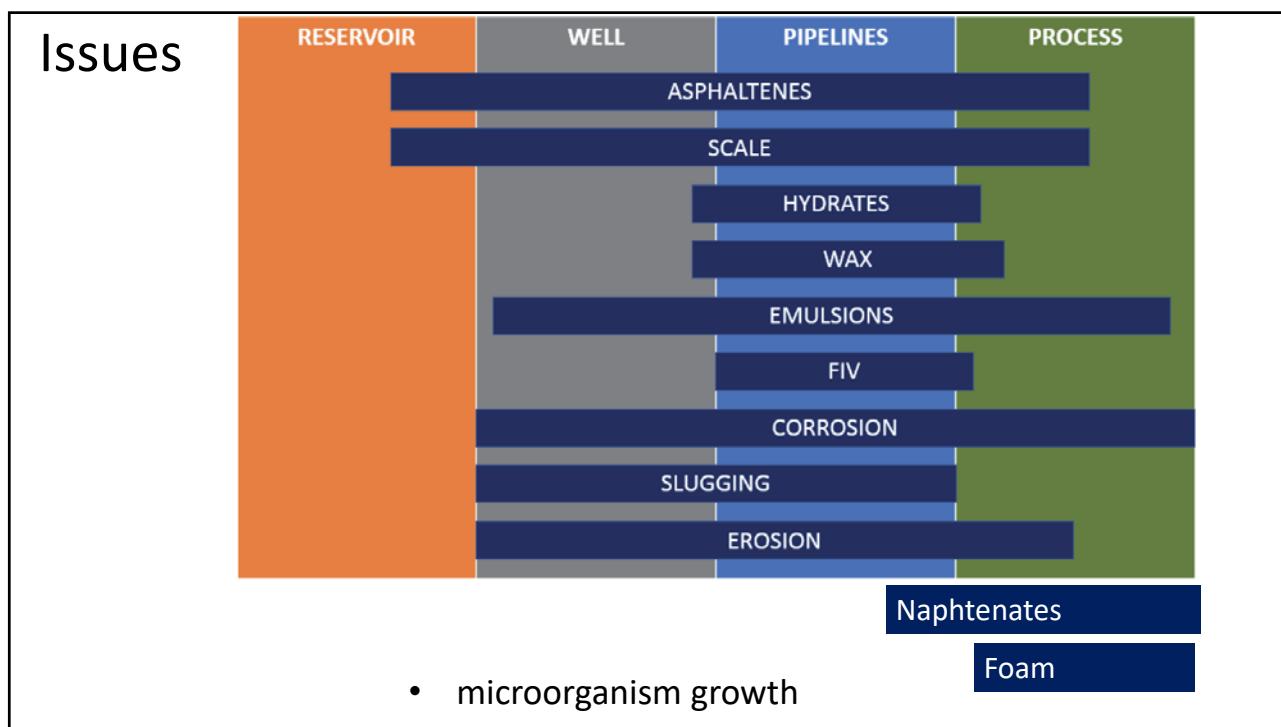


Notes for Youtube video Flow assurance considerations in Field development

# Flow assurance considerations in hydrocarbon field development and planning

Prof. Milan Stanko (NTNU)

1

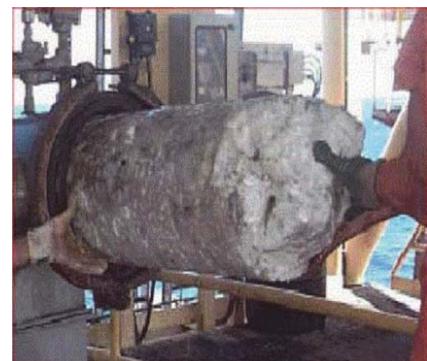
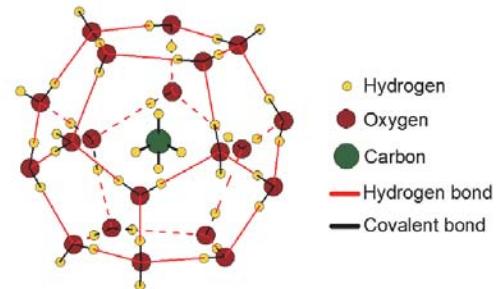


2

# Hydrates



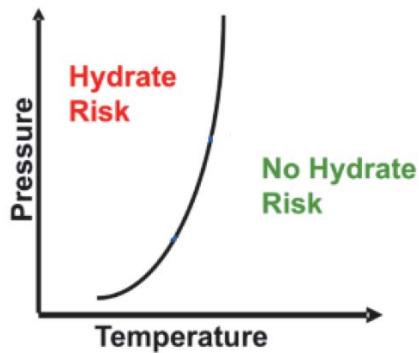
<https://www.youtube.com/watch?v=Oz4NLXfdqpA>



3

## Hydrates - conditions

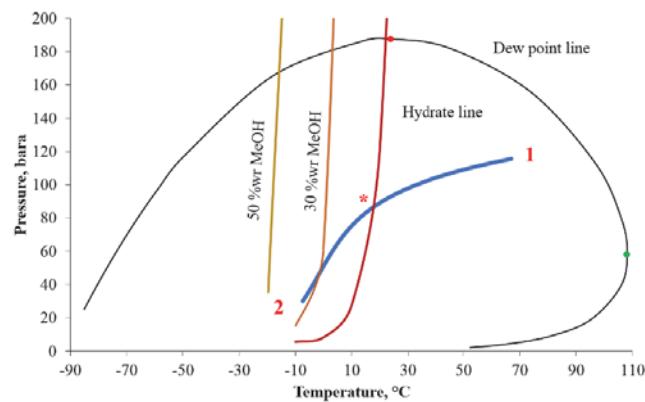
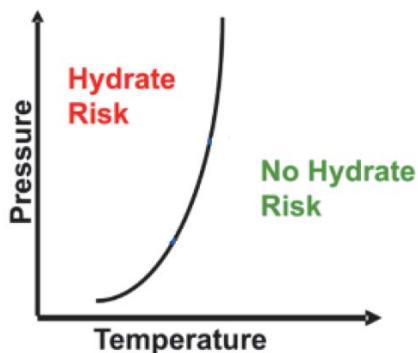
- Free water (in liquid phase)
- Small hydrocarbon molecules
- Particular range of pressure and temperature.



4

## Hydrates - conditions

- Free water (in liquid phase)
- Small hydrocarbon molecules
- Particular range of pressure and temperature.

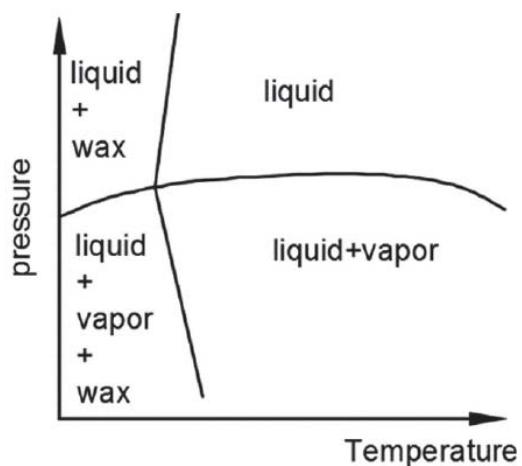


5

## Wax



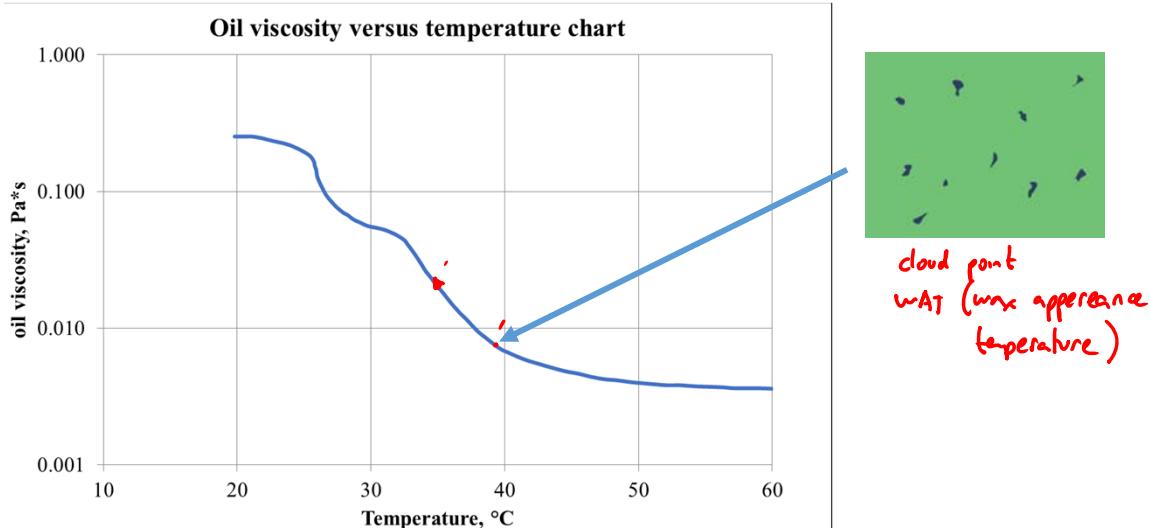
TAKEN FROM EQUINOR



Paraffins (C18 - C36)

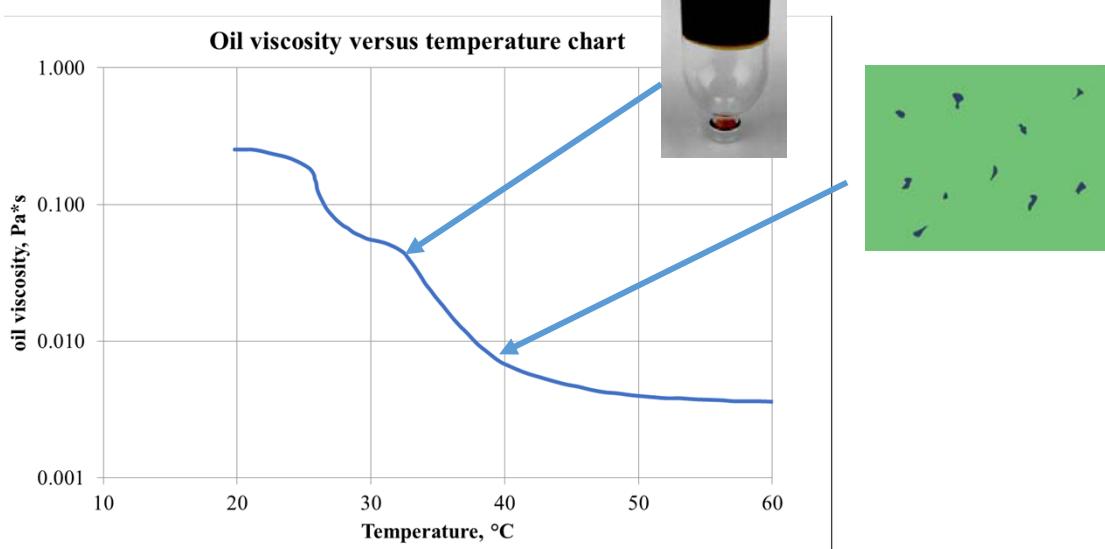
6

## Wax



7

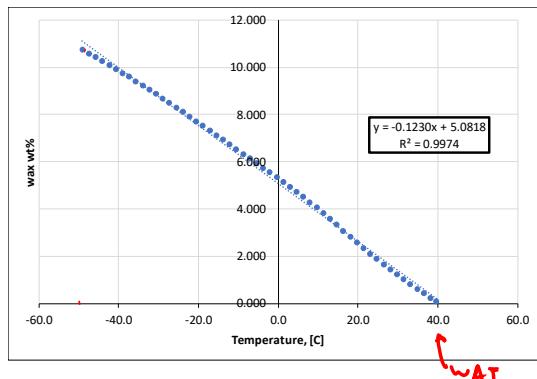
## Wax



8

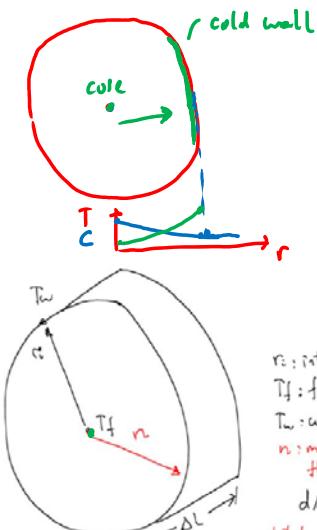
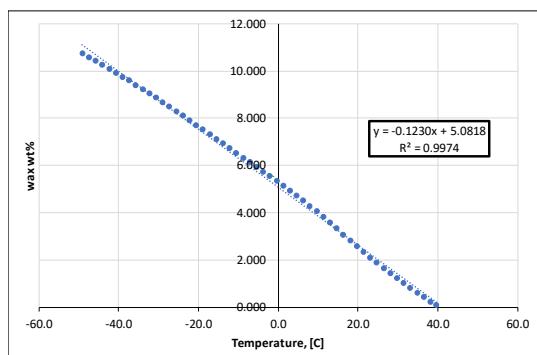
# Wax

weight of wax particles, 100  
total weight



9

# Wax

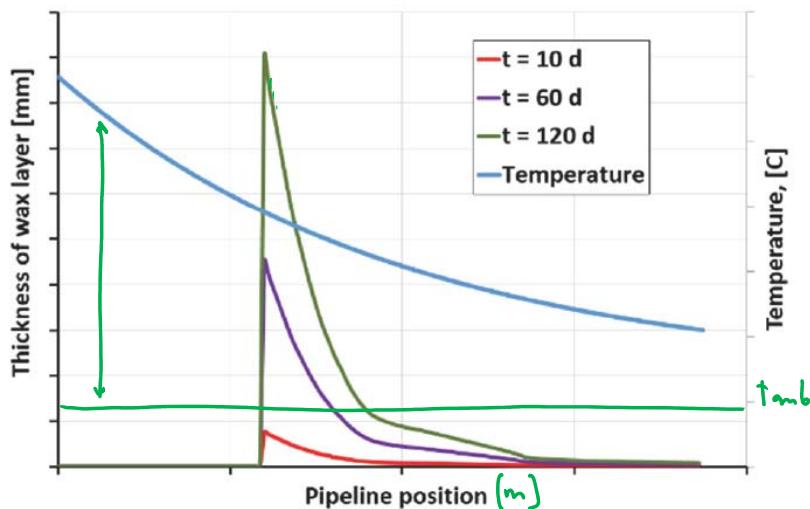


$r_i$ : internal pipe diameter  
 $T_f$ : fluid temperature  
 $T_w$ : wall temperature  
 $n$ : mass flux of wax from fluid to wall [ $\text{kg/s m}^2$ ]  
 $dA = \pi r_i^2 dL$   
 total mass flow of wax ( $m_w$ ) deposited in a section  
 $m_w = n \cdot dA$

$$n = \rho_{wax} \cdot \frac{B}{\mu_o} \cdot \frac{dC}{dT} \cdot \frac{dT}{dr}$$

10

## Wax

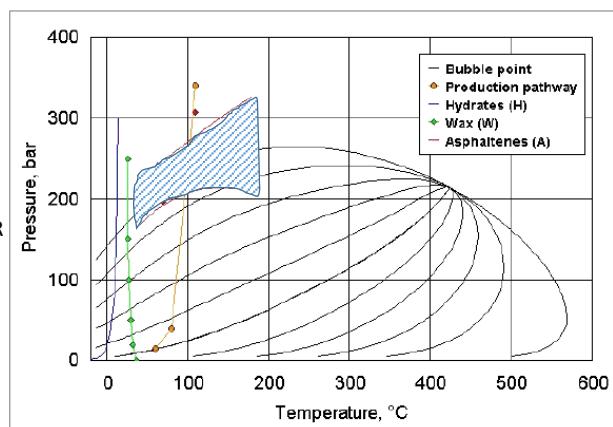
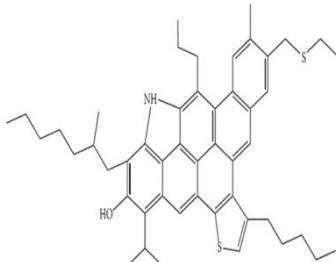


11

## Asphaltenes



TAKEN FROM EQUINOR  
(KALLEVIK)



12

## Scale



Choke on FCM 100018142 S/N1 01

Ion	Formasjonsvann [mg/l]	Seawater [mg/l]
Na	14 800	10 680
K	520	396
Mg	13	1 279
Ca	378	409
Ba	410	8
Sr	228	0
Fe	58	0
Cl	23 600	19 220
SO <sub>4</sub>	0	2 689

$Ba^{2+} + SO_4^{2-} = BaSO_4(s)$

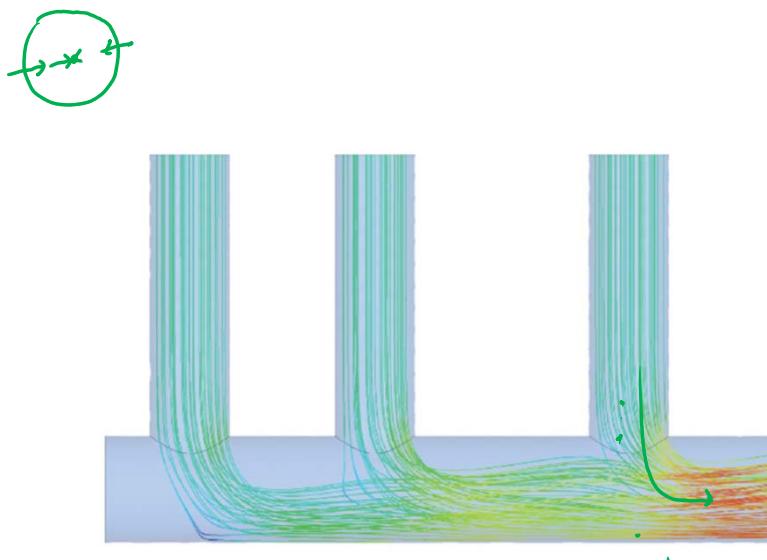
$Ca^{2+} + CO_3^{2-} = CaCO_3(s)$

$p \downarrow \quad T \uparrow \quad \rightarrow$

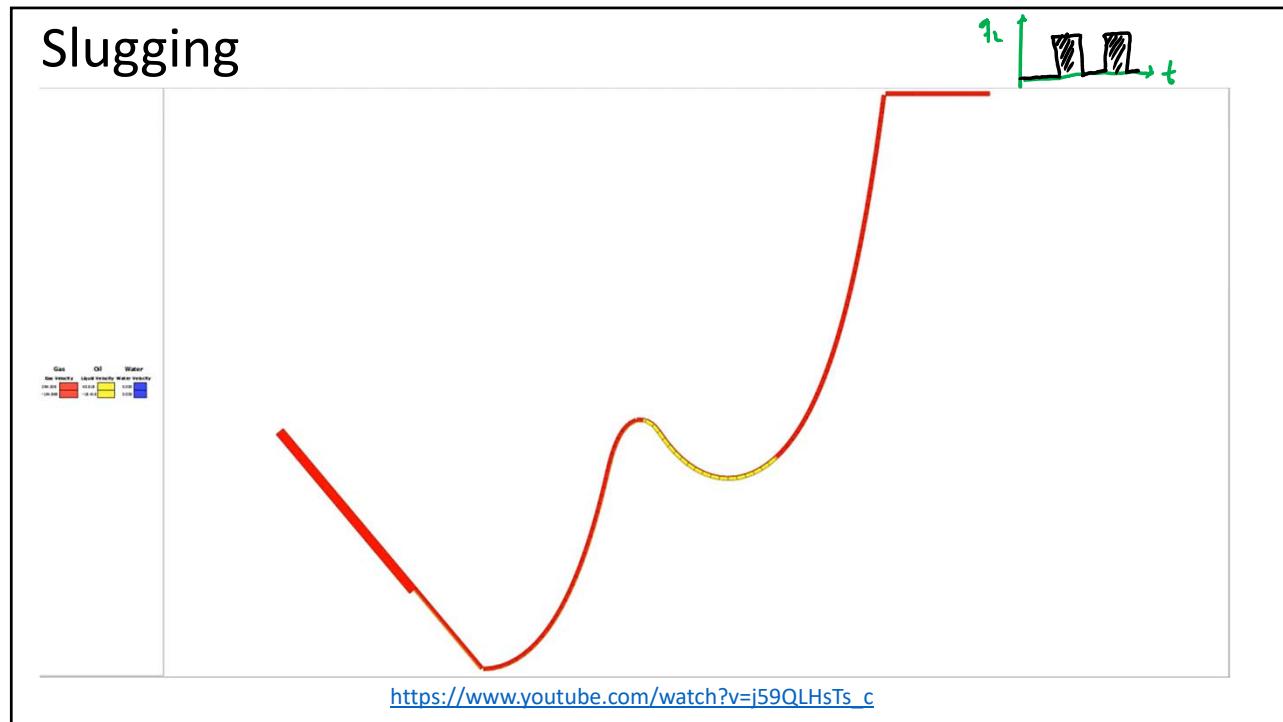
TAKEN FROM EQUINOR (SANDENGEN)

13

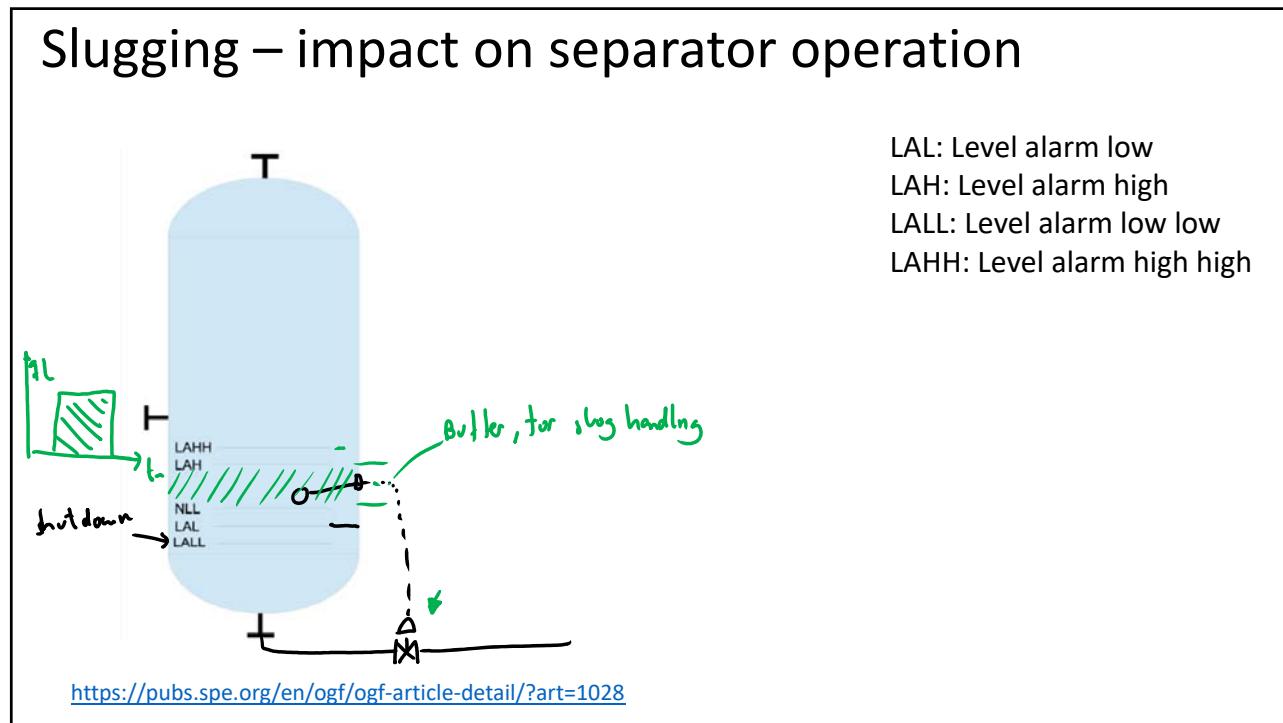
## Erosion

14

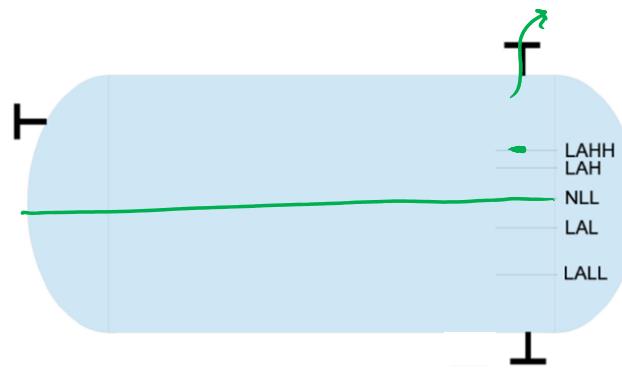


15



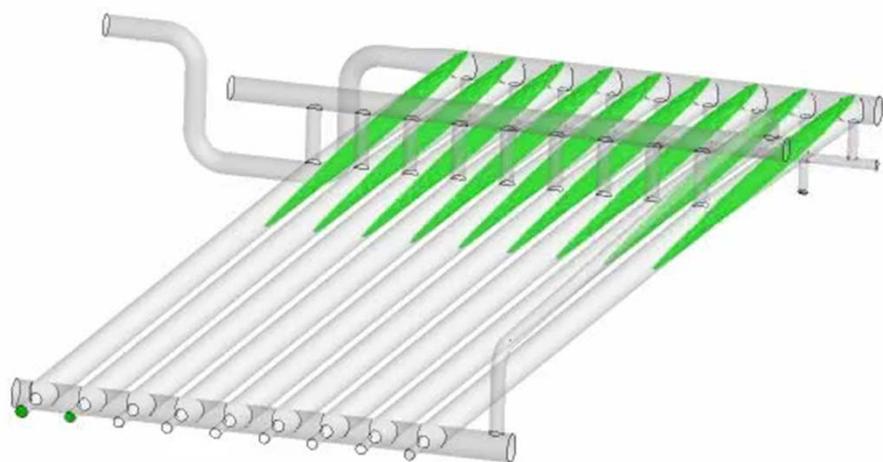
16

## Slugging – impact on separator operation



17

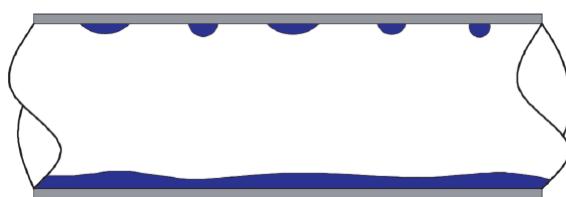
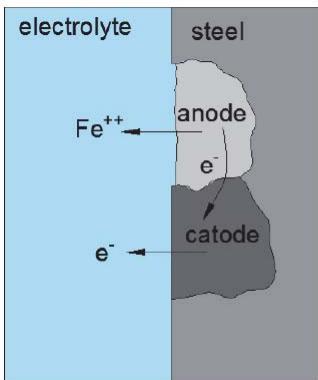
## Slugging – slugcatcher handling slugs



<https://www.youtube.com/watch?v=LKLW5284adI>

18

## Corrosion



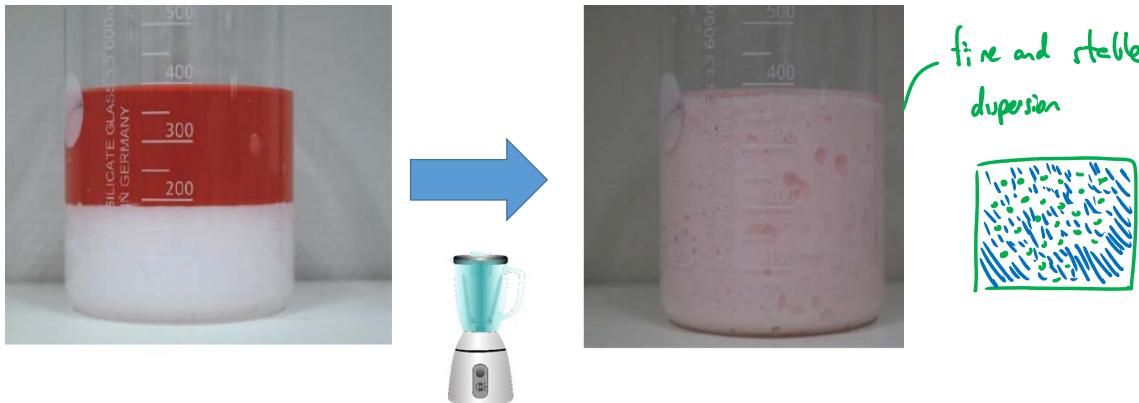
19

## Oil-water emulsions



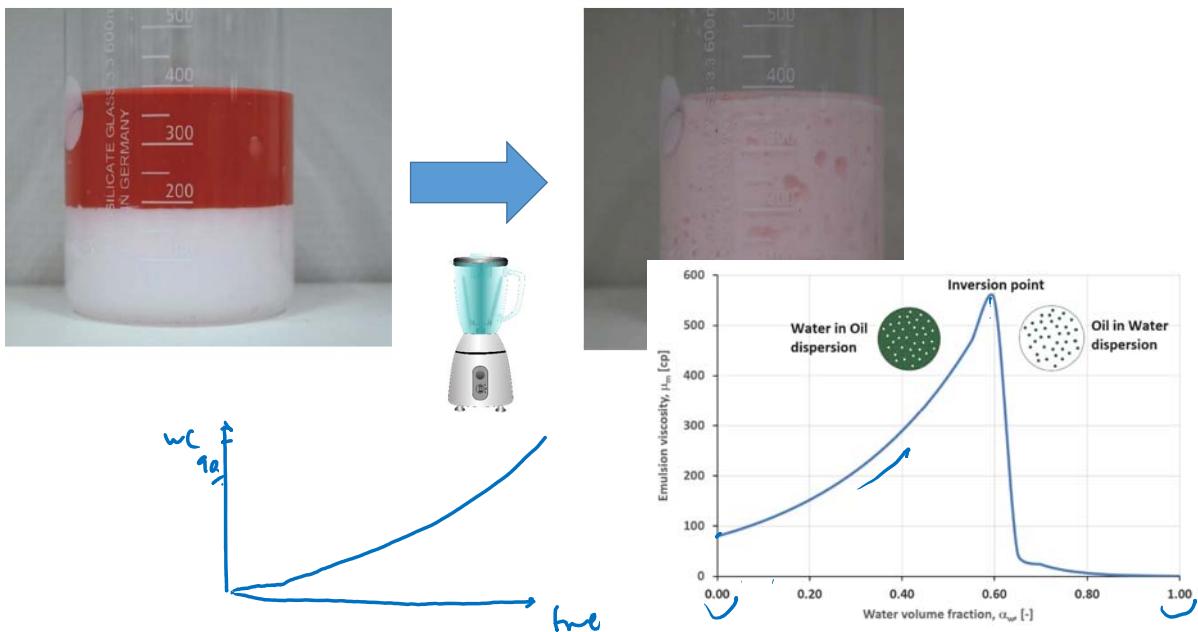
20

## Oil-water emulsions



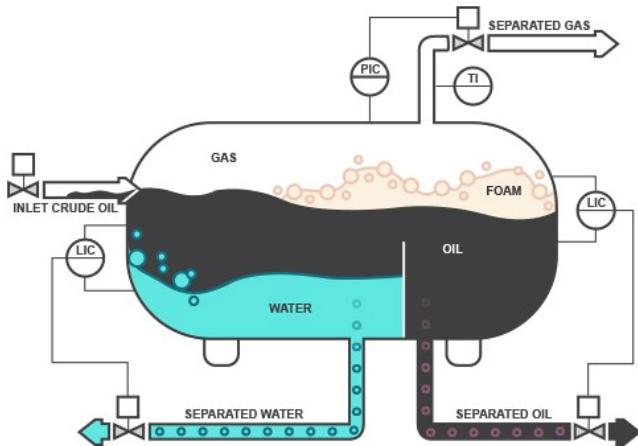
21

## Oil-water emulsions

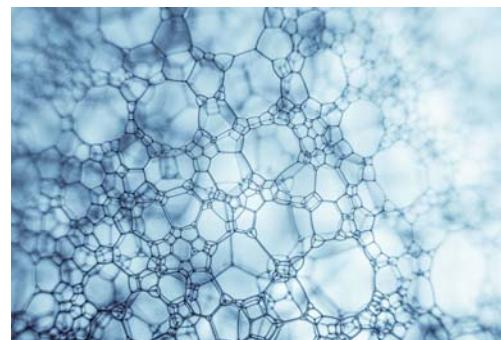


22

# Foam



<https://www.arab-oil-naturalgas.com/foam-in-oil-gas-separators/>



<https://www.crodaoilandgas.com/en-gb/discovery-zone/functions/foamers>

23

Flow assurance issue	Causes	Potential Consequences	Prevention/solution	Tools available for analysis
<b>Hydrates</b>	<ul style="list-style-type: none"> <li>Small gas HC molecules</li> <li>Free water</li> <li>Begin to form at a given p and T (low T, high P) given by thermodynamic equilibrium of the hydrate phase.</li> </ul>	<ul style="list-style-type: none"> <li>Blockage of flowlines and pipelines</li> </ul>	Reduce the hydrate formation region: <ul style="list-style-type: none"> <li>Continuous or on-demand injection of chemical inhibitor (MEG or MEOH)</li> <li>Stay out of hydrate formation region:               <ul style="list-style-type: none"> <li>Improve thermal insulation</li> <li>Electric heating</li> <li>Others:                   <ul style="list-style-type: none"> <li><b>Cold flow*</b></li> <li><b>Water removal and gas dehydration*</b></li> </ul> </li> </ul> </li> </ul>	To determine Hydrate formation conditions: <ul style="list-style-type: none"> <li>Laboratory tests</li> <li>Empirical correlations</li> <li>Thermodynamic simulators (e.g. Hysys, PVTsim, Unisim)</li> </ul> To determine p and T along the pipe: <ul style="list-style-type: none"> <li>Multiphase simulator (Olga, LedaFlow).</li> <li>Computational fluid dynamics (CFD)</li> </ul>
<b>Wax</b>	<ul style="list-style-type: none"> <li>Composition of the crude oil</li> <li>Begins to form at given p and T due to changes in solubility</li> <li>Cold wall</li> </ul>	In wells, flowlines and pipelines: <ul style="list-style-type: none"> <li>Increase pressure drop (pipe roughness)</li> <li>Reduction of cross section area</li> <li>Pipe blockage</li> <li>Changes fluid rheology</li> <li>Gelling (problem for startup)</li> </ul>	<ul style="list-style-type: none"> <li>Pigging</li> <li>Thermal insulation</li> <li>Electric heating</li> <li>Chemical inhibitors</li> <li>Chemical dissolvers</li> <li>Pipe coating</li> <li><b>Cold flow*</b></li> </ul>	<ul style="list-style-type: none"> <li>Laboratory tests</li> <li>Transient multiphase simulators (e.g. Olga, LedaFlow)</li> <li>Computational fluid dynamics (CFD)</li> </ul>
<b>Slugging</b>	<ul style="list-style-type: none"> <li>Dynamics of multiphase flow of liquid and gas</li> <li>Reduction of rate</li> <li>Liquid accumulation on low points</li> </ul>	In wells, pipelines and flowlines: <ul style="list-style-type: none"> <li>Fluctuating liquid and gas input to processing facilities</li> </ul> In flowlines and pipelines: <ul style="list-style-type: none"> <li>Vibration</li> <li>Added pressure drop</li> <li>Fatigue</li> </ul>	<ul style="list-style-type: none"> <li>Change separator size</li> <li>Pipeline dimensioning</li> <li>Maintain flow above minimum flow rate</li> <li>Gas lift in riser base</li> <li>Choking topside</li> <li>Pipeline re-routing</li> <li><b>Subsea separation*</b></li> </ul>	<ul style="list-style-type: none"> <li>Transient multiphase simulator (OLGA, LEDA)</li> <li>Structural analysis (usually with FEA, e.g. Ansys)</li> <li>Laboratory experiments</li> </ul>
<b>Scaling</b>	<ul style="list-style-type: none"> <li>Changes in solubility (e.g. changes in P and T conditions, changes in pH, mixture of incompatible water, CO<sub>2</sub> injection)..</li> <li>Irregularities on surface</li> </ul>	In wells, pipelines and flowlines: <ul style="list-style-type: none"> <li>Reduction of cross section area</li> <li>Pipe blockage</li> <li>Malfunctioning of valves and equipment</li> </ul>	<ul style="list-style-type: none"> <li>Continuous injection of chemical inhibitors</li> <li>Dilution by adding more water</li> <li>Chemical dissolvers</li> <li>Mechanical removal</li> <li>Coating</li> </ul>	<ul style="list-style-type: none"> <li>Laboratory tests</li> <li>Simulation tools</li> </ul>

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Flow assurance issue	Causes	Potential Consequences	Prevention/solution	Tools available for analysis
Erosion	<ul style="list-style-type: none"> <li>• Sand production</li> <li>• High flow velocities</li> <li>• Liquid droplets in the gas</li> <li>• Gas droplets in the liquid</li> </ul>	In wells, pipelines and flowlines: <ul style="list-style-type: none"> <li>• Structural damage</li> <li>• Vibration</li> <li>• Leaks</li> <li>• Corrosion</li> </ul>	<ul style="list-style-type: none"> <li>• Change geometry</li> <li>• Replacement and maintenance of components</li> <li>• Reduce flow rate (reduce formation drawdown)</li> <li>• Sand separation*</li> <li>• Coatings</li> </ul>	<ul style="list-style-type: none"> <li>• Standards (DNV-RP-0501)</li> <li>• Computational fluid dynamics</li> <li>• Laboratory testing</li> </ul>
Corrosion	<ul style="list-style-type: none"> <li>• Water</li> <li>• O<sub>2</sub></li> <li>• CO<sub>2</sub></li> <li>• H<sub>2</sub>S</li> </ul>	<ul style="list-style-type: none"> <li>• Leaks</li> <li>• Integrity</li> </ul>	<ul style="list-style-type: none"> <li>• Coatings</li> <li>• Material selection</li> <li>• Surface passivation</li> </ul>	<ul style="list-style-type: none"> <li>• Laboratory testing</li> </ul>
Emulsions	<ul style="list-style-type: none"> <li>• Emulsification agents in the crude</li> <li>• Mixing, shear when flowing through valves, chokes, etc</li> </ul>	<ul style="list-style-type: none"> <li>• Added pressure drop</li> <li>• Increased separation time</li> </ul>	<ul style="list-style-type: none"> <li>• Injection of demulsifiers</li> <li>• Heating</li> </ul>	<ul style="list-style-type: none"> <li>• Laboratory tests</li> <li>• Multiphase models</li> </ul>
Asphaltenes	<ul style="list-style-type: none"> <li>• Crude with asphaltenes</li> <li>• Pressure reduction</li> <li>• Addup of light hydrocarbon components</li> </ul>	<ul style="list-style-type: none"> <li>• Blockage of formation, well, flowline and pipeline</li> <li>• Loss of equipment functionality</li> <li>• Emulsification and foamification</li> </ul>	<ul style="list-style-type: none"> <li>• Mechanical removal</li> <li>• Chemical injection</li> </ul>	<ul style="list-style-type: none"> <li>• Laboratory tests</li> <li>• Some simulation tools</li> </ul>

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## Measures and consequences

- **Chemical injection**
- System design, e.g.
  - pipe and component insulation
  - heat tracing
  - dead legs
  - pipeline routing
- Well intervention needs
- Water injection strategy
- Define procedures when shutting down and starting up
- Ensure proper distribution of chemicals



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## Example of chemical injection program

**Tabell 5-2. Foreløpig oversikt over kjemikalietyper**

Type kjemikalie	Konsentrasjon (ppm vol.)	Tilsettes i	Frekvens
Avleiringshemmer A	50	Produsert vann	Kontinuerlig
Avleiringshemmer B	20-50	Sjøvann	Kontinuerlig
Korrosjonshemmer	50	Produsert vann	Kontinuerlig
Emulsjonsbryter	50	Total væske 1)	Kontinuerlig ved behov
Skumdemper	5	Total væske	Periodisk
Flokkulant	10	Produsert vann	Kontinuerlig
Vokshemmer	150	Total væske 1)	Periodisk
Biocid	80	Total væske 1)	Kontinuerlig
Oksygenfjerner	5	Sjøvann	Kontinuerlig
H <sub>2</sub> S fjerner	150	Produsert vann	Kontinuerlig ved behov
MEG	Batch	Brønnstrøm	Ved behov

1) Olje og produsert vann.

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## Release and disposal of chemicals

**Tabell 7-1 Klassifisering av kjemikaler i henhold til OSPAR**

	Svart kategori: Stoffer som er lite nedbrytbare og samtidig viser høyt potensial for bioakkumulering og/eller er svært akutt giftige. I utgangspunktet er det ikke lov å slippe ut kjemikaller i svart kategori. Tillatelse til bruk og utsipp til spesifikke kjemikaller gis dersom det er nødvendig av sikkerhetsmessige og tekniske grunner.
	Rød kategori: Stoffer som brytes sakte ned i det marine miljøet, og viser potensielle for bioakkumulering og/eller er akutt giftige. Kjemikaller i rød kategori kan være miljøfarlige og skal derfor prioriteres for utskifting med mindre miljøfarlige alternativer. Tillatelse til bruk og utsipp gis kun av sikkerhetsmessige og tekniske hensyn.
	Gul kategori: Kjemikaller i gul kategori omfatter stoffer som ut fra iboende egenskaper ikke defineres i svart eller rød kategori og som ikke er oppført på PLONOR-listen (se under). Ren gul kategori er uorganiske kjemikaller med lav giftighet eller kjemikaller som brytes ned >60% innen 28 dager. Gul-Y1 er 20-60% nedbrutt og forventes å brytes ned fullstendig over tid. Gul-Y2 er moderat nedbrytbare til ikke giftige og ikke-nedbrytbare komponenter. Y2 skal forsøkes substituert på lik linje med røde kjemikaller.
	Grunn kategori: Stoffer som er oppført på OSPAR-konvensjonens PLONOR-liste (Substances used and discharged offshore which are considered to Pose Little Or No Risk to the Environment). Disse kjemikaliene vurderes å ha ingen eller svært liten negativ miljøeffekt. Kjemikaller i grunn kategori omfatter også vann som inngår i kjemikaliene.

From Ivar Aasen PDO,  
Del 2

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## Release and disposal of chemicals

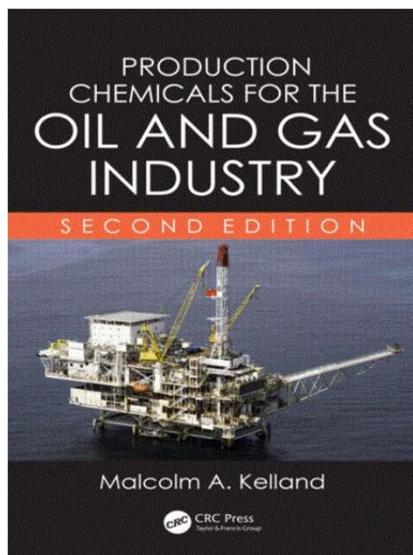
Tabell 7-4 Miljømessige egenskaper til produksjonskjemikalier som vil følge produsert vann fra Johan Castberg-feltet

Type kjemikal	Vannfase/oljefase	Klassifisering
Avleiringshemmer	Vannløselig. Følger produsert vann.	Det er antatt at gult kjemikalie (i klassen Y2) kan velges. Kjemikaliet er moderat bionedbrytbart til ikke bionedbrytbart Det er ikke giftig og vil ikke bioakkumuleres i næringskjeden.
Emulsjonsbryter	Oljeløselig. Følger hovedsakelig oljefasen (95%). 5% følger produsert vann.	
Vokshemmer	Oljeløselig. Følger oljefasen.	Alle disse kjemikaliene er klassifisert som røde, pga det ikke er bionedbrytbart.
Skumdemper	Oljeløselig. Følger i all hovedsak oljefasen, lave konsentrasjoner i produsert vann.	De er ikke giftige og vil ikke bioakkumuleres i næringskjeden.
Flokkulant	Vannløselig, men binder seg til oljedråper. Følger hovedsakelig oljefasen (80%). 20% er antatt å følge produsert vann.	
Biocid/Glutaraldehyd	Vannløselig. Følger injeksjonsvannet eller produsert vann.	Kjemikalie er klassifisert som gult pga giftighet. Det er ikke nedbrytbart og vil ikke bioakkumuleres i næringskjeden.

From Johan Castberg  
PDO, Del 2

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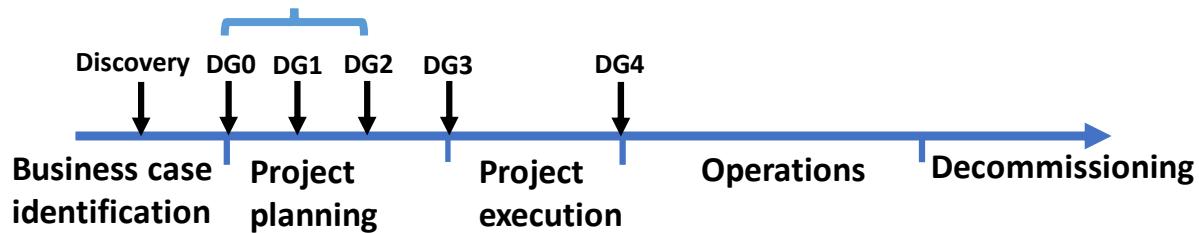
## More about production chemicals



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## Flow assurance evaluation during field planning

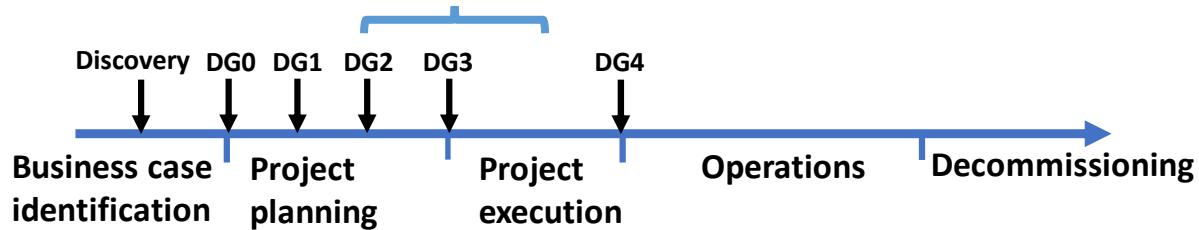
- Detect potential showstoppers and communicate technical constraints and repercussions to field planner
- Laboratory tests



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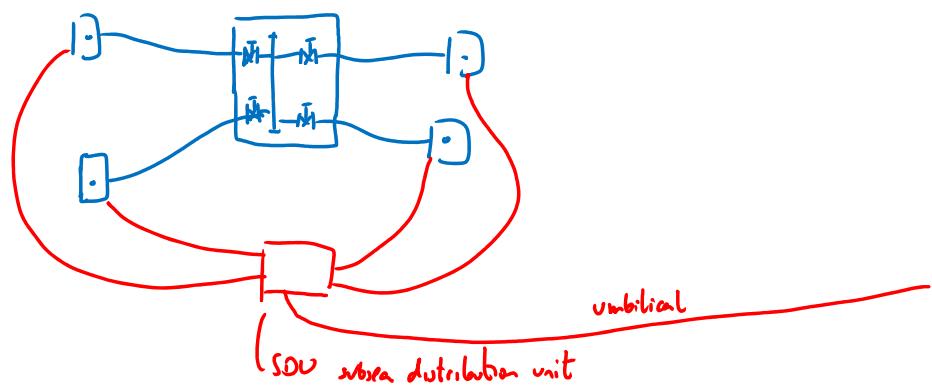
## Flow assurance evaluation during field planning

Refine the flow assurance strategy  
 -More laboratory tests  
 -Management plan  
 -prediction of p and T  
 -Study of startup and shutdown  
 -System design and verification  
 -FIV



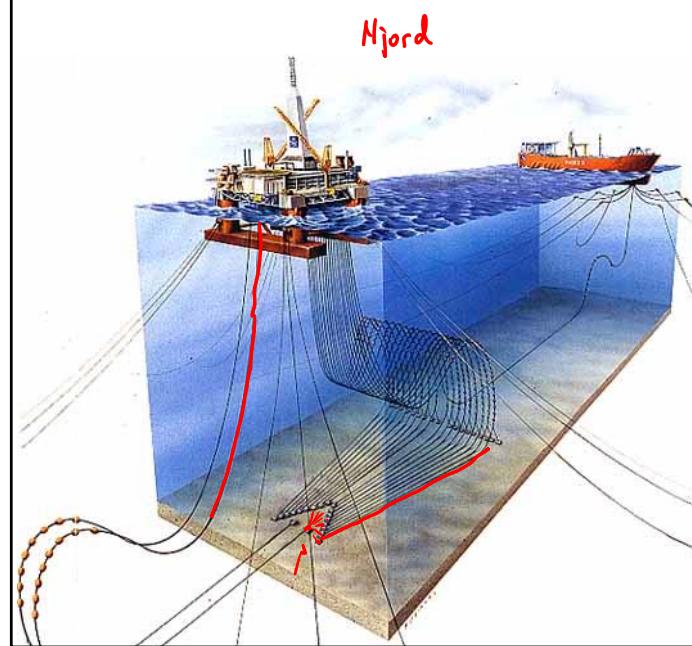
32

## Injection of production chemicals subsea



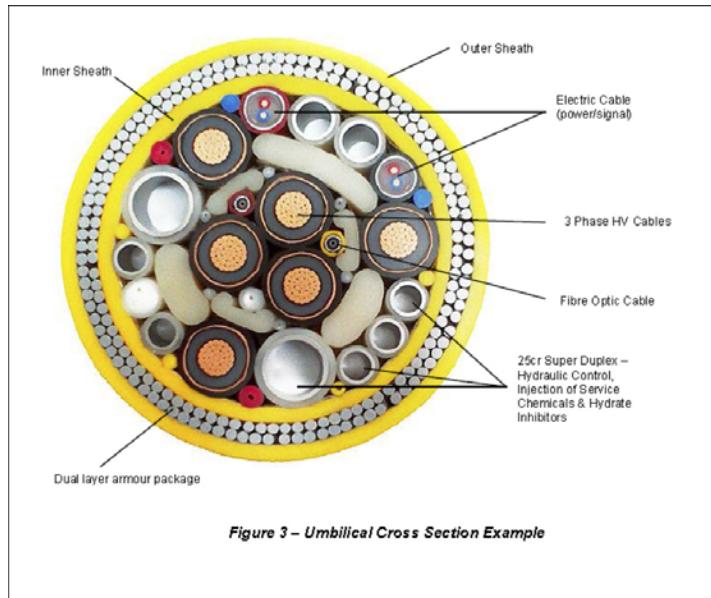
33

## Injection of production chemicals



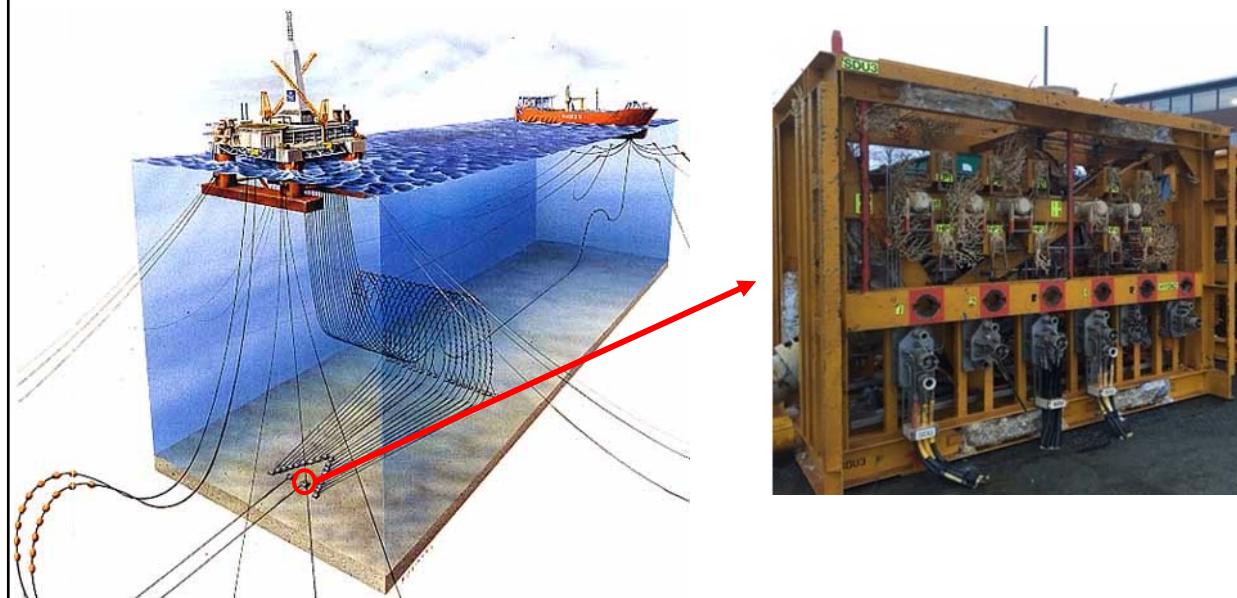
34

## Umbilicals, injection of production chemicals



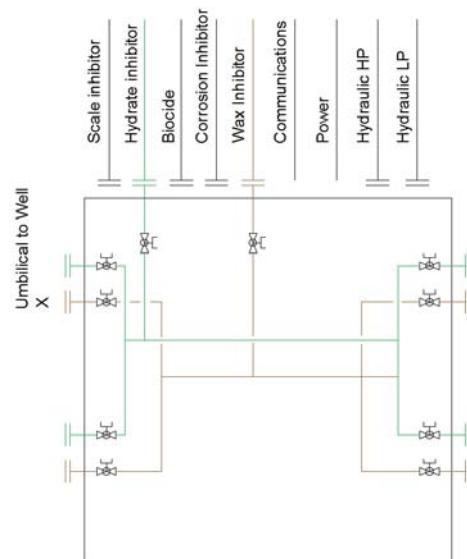
35

## Umbilicals, injection of production chemicals

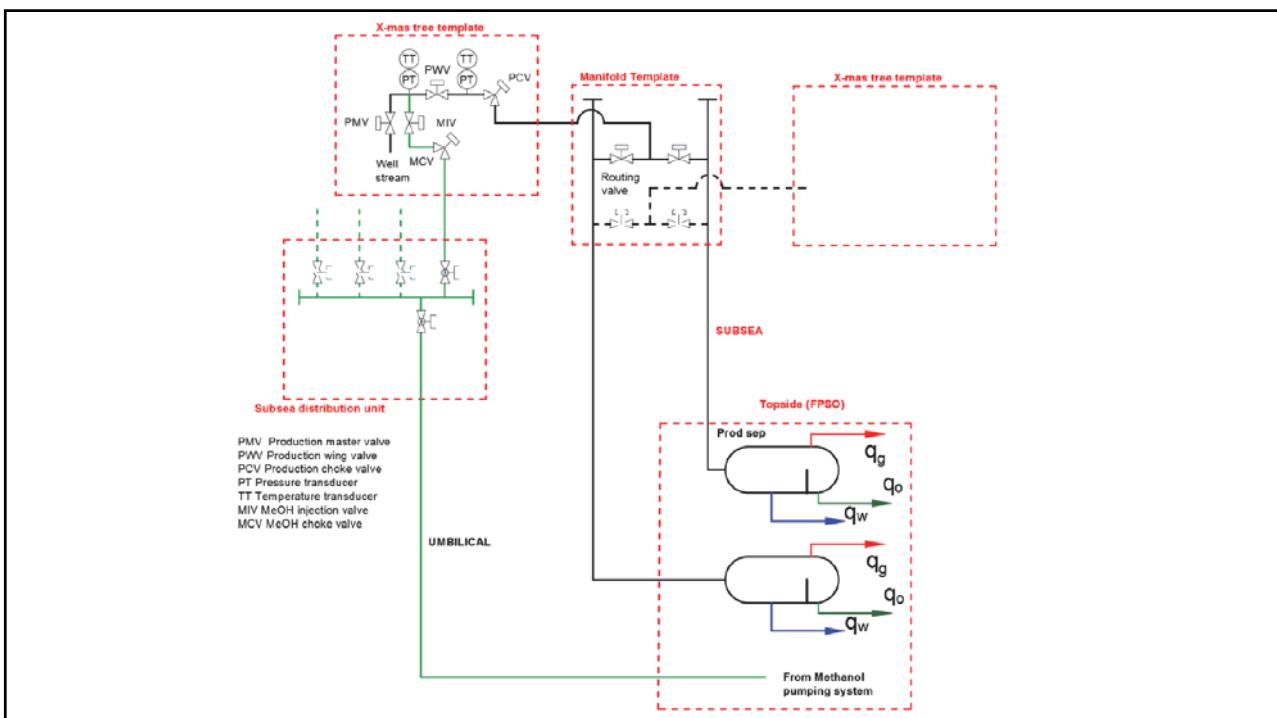


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## Release and disposal of chemicals

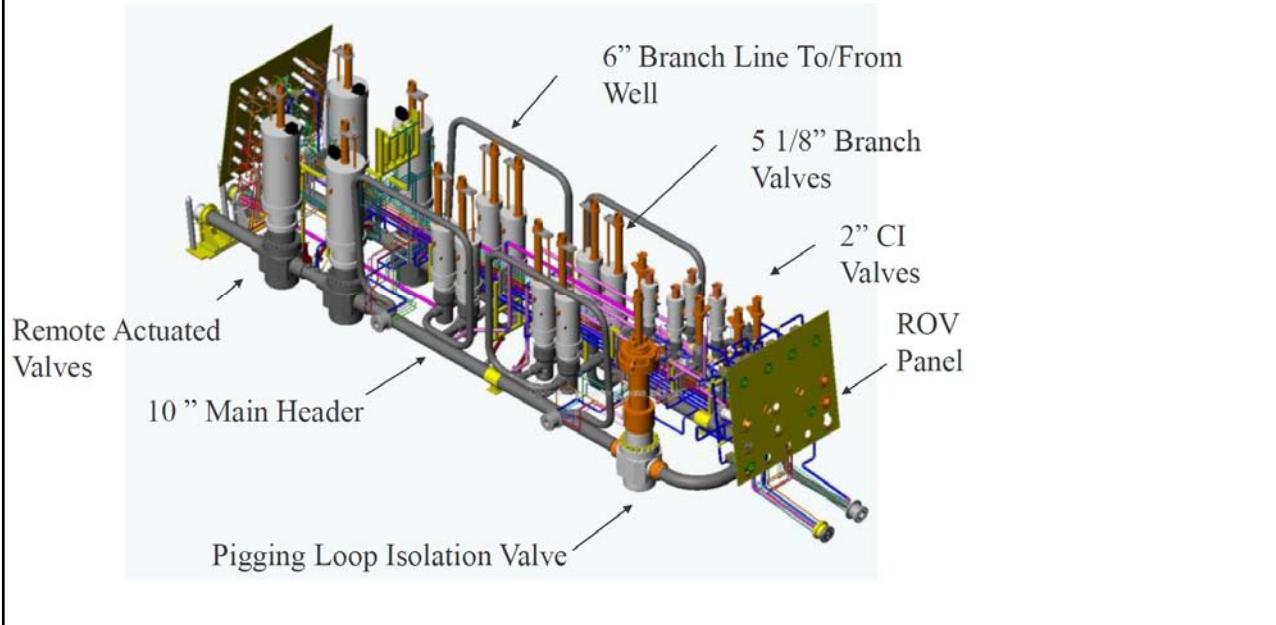


37



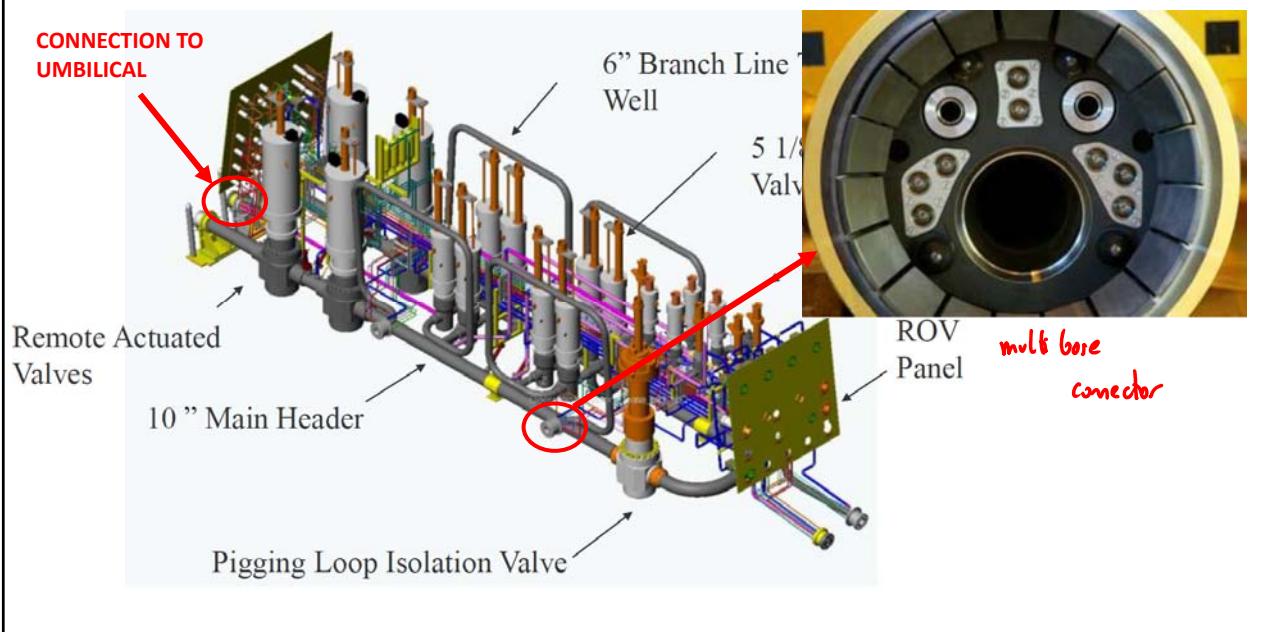
38

## Injection of production chemicals – template wells

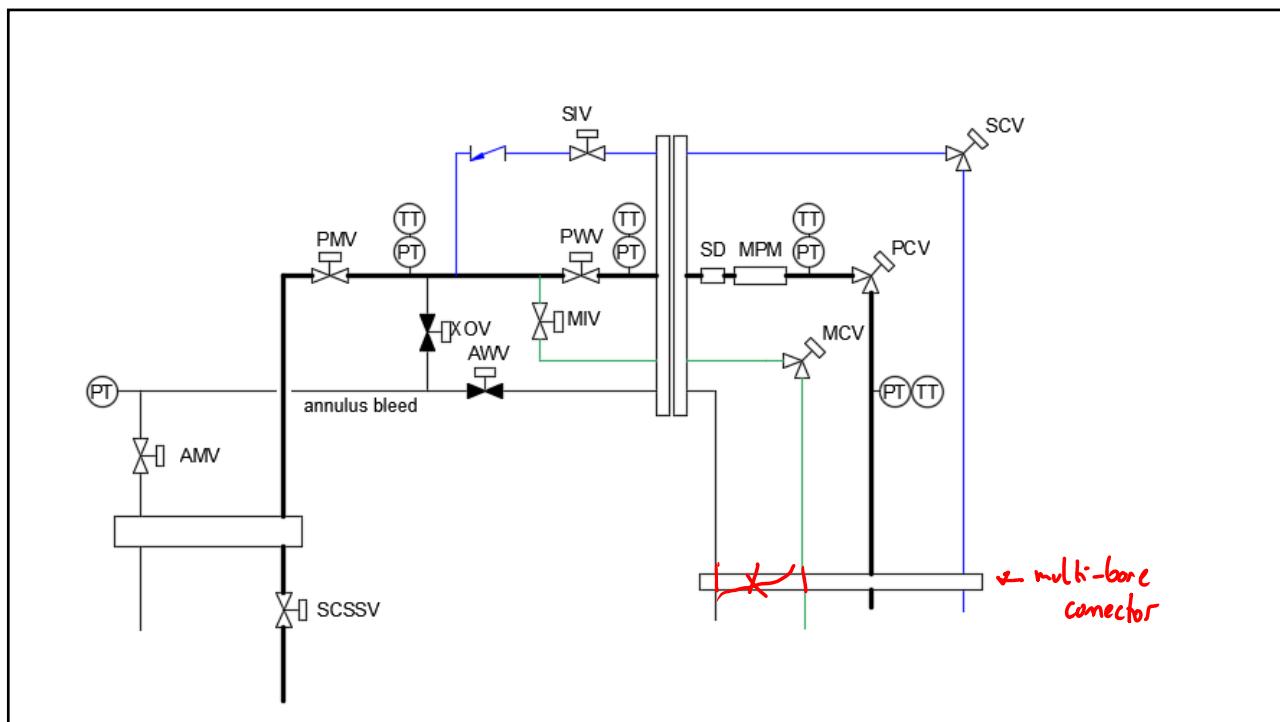


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## Injection of production chemicals – template wells

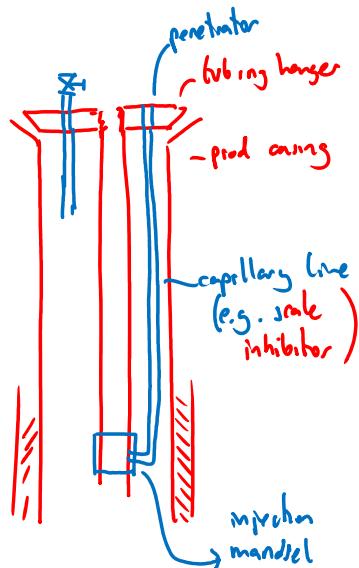


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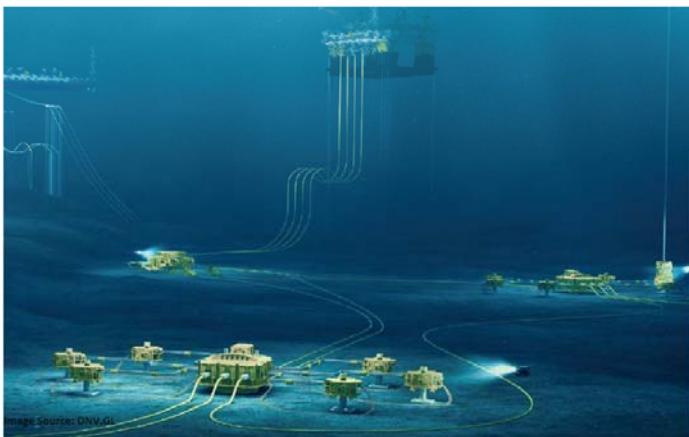
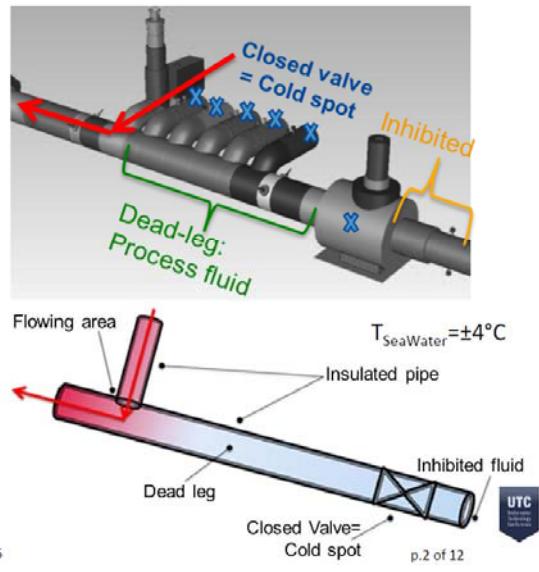
## Injection of production chemicals in well



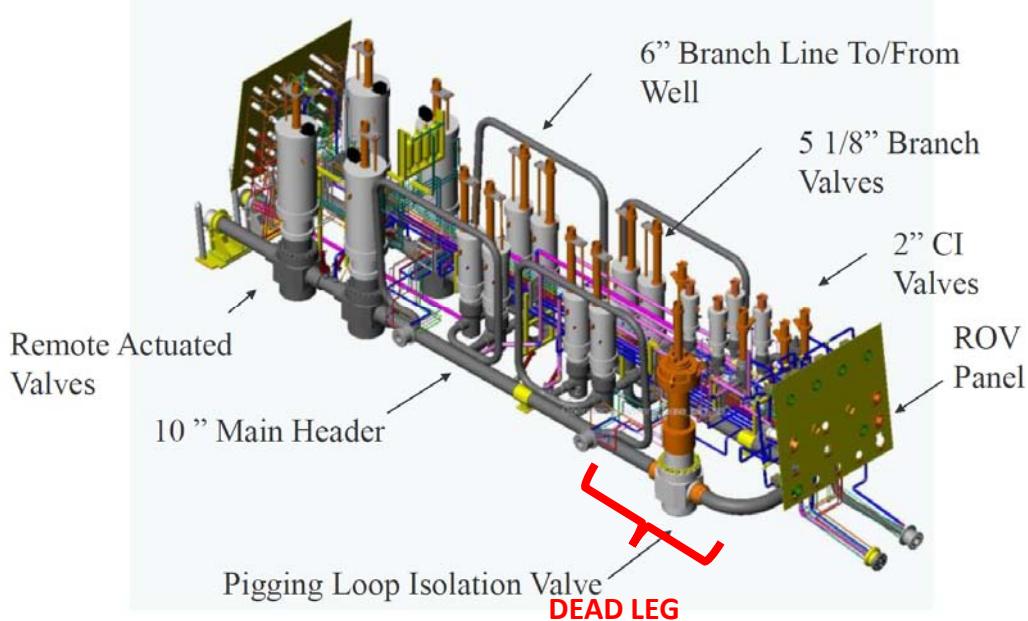
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## Subsea manifold and dead-leg geometry

- Dead-legs are inherently present

UTC Bergen - 16<sup>th</sup> June 2016

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## Tools for analysis

- Laboratory tests of fluids (oil, gas, water)
- Steady state flow simulators (Hysys, Gap, Pipesim, Olga, Leda, FlowManager)
- Transient flow simulators (Olga, LedaFlow, FlowManager, Hysys)
- Thermodynamic or PVT simulators (PVTsim, Hysys)
- Standards (DNV, API)
- CFD simulation for 3D flow analysis of pressure and temperature (Comsol, Ansys)
- Finite element analysis for structural analysis and heat transfer in solids (Abacus, Ansys)

**PENSUM:**

- Field development workflow.
  - Lifecycle of a hydrocarbon field
  - Overview – The field development process
  - Production modes
  - Discounting
  - Relationship between plateau height and length
  - Rule of thumb between plateau height and TRR
  - Bottlenecking and processing capacity (separation capacity)
  - Onshore vs offshore
  - Oil vs gas
  - Video recording of presentation about Aasta Hansteen development
  - Familiarization with SODIR website
- Excel VBA, functions, and routines.
- Topside processing
  - Overview
  - O-G-W Separation and stabilization (Exercise with Hysys)
  - Separation capacity
    - Droplet settling theory
    - Droplet size distribution
  - Horizontal separator design
  - Oil content in disposed water
- Field production performance
  - Estimation of production profiles
  - Dry gas production system: material balance, IPR, TPR, FPR, choke, flow equilibrium.
  - Production scheduling
  - Measures to prolong the plateau.
  - Boosting
  - Approaches to generate production profiles, coupling reservoir and wellbore models
  - Dry gas networks.
  - CO<sub>2</sub> accountancy
    - CO<sub>2</sub> emissions and CO<sub>2</sub> value chain
    - Injection scheduling for the Snøhvit field
  - Production potential
- Value chain model, cost estimation and NPV calculations
- Dealing with uncertain parameters in FD
  - Probabilistic reserve estimation
    - Monte Carlo
  - Decision and probability tree analysis
- Introduction to Python, Jupyter Notebook
- Offshore structures
  - Overview
  - Layout of production systems
  - Marine loads on offshore structures
- Flow assurance considerations
  - General overview
  - Inhibitor subsea system. Disposal.

**Home exercises**

**Class exercises/Class group work**

**Quizzes**

- Simulation of pipeline using commercial software (Hysys)

**Lecture material :**

- Live lectures
- Youtube videos
- Reading material

### **Q&A before the exam**

If you have questions from now until the date of the exam, I suggest the following alternatives:

- Use the Blackboard forum
- Send an email to the TA or to me
- We can arrange general Q&A sessions for several people with the TA or me, or both, if this is necessary. Please, send an email to the TA or to me to make this request.

### **Final exam**

-Date: 6th June, 2024, 15:00-19:00. SL311 brun sone

-The exam accounts for 100/100 points, and it will be conducted in Inspera. The exam questions will add up to 100 points that will then be converted to grade letter.

-You can see examples of previous exams in the side menu of Blackboard, under the point "Previous exams"

-The exam covers all the materials provided during the course, but emphasis is made on the material covered in the class exercises/group work, home exercises, quizzes, and lectures.

The following items will NOT be covered in the exam:

- Python, HYSYS.
- The presentation on Aasta Hansteen

-The value of each exam task will be provided in Inspera.

-The exam will be applied in Inspera, using an NTNU computer and in a NTNU examination room. No aids are permitted. A specific basic calculator is allowed (although it is not necessary). In the examination computer you will have access to the internet browser to see the Inspera test, the Windows Explorer, and some basic Windows programs such as Microsoft Office (Word, Excel, PowerPoint).

-Milan will pass by at approximately 1 hour after the examination has started. The total duration of the exam is 4 hrs. If you need to reach Milan before or after that, contact the invigilators to call me.

-If you need to deliver several files as part of your answer, use a compressed (for example zip) file.

-The exam hasn't been prepared yet, but it could be a combination of long answer questions, value-fill questions in Inspera, and questions using Excel (where the problem must be solved in Excel and the Excel file is delivered).

-After the exam is ready, Milan will publish information about number and type of questions on Inspera (1-2 weeks before the exam date).

A long exam question may be structured in the following way:

- Question text (indicating the number of points that the problem is worth)
- Data
- Link to download an Excel file (if any). The Excel file contains, in most cases, the problem's data, a suggested structure layout to solve the problem and some useful VBA functions.
- A long answer field, to provide a brief explanation about how you solved the problem
- A link to upload the Excel file containing your solution (if any)

- A link to upload additional files, e.g. images, sketches, word document, pdf, etc. (if any).

-When solving the exam, make sure that you make clear the procedure used to solve it, either by adding text to the Excel file, or by filling the text box.

-During the exam, when working with Excel, remember to save often.

-When you first download and open the Excel file, make sure to enable macros and make it a trusted document, otherwise you will have issues using the VBA functions. You can also save it with a different name so the computer recognizes it as its own.

-If you want to provide hand-written notes, **I believe you will need to use the tablet provided on the table.**

-Other relevant information:

- <https://innsida.ntnu.no/wiki/-/wiki/English/Pack+and+unpack+zip+files>

### Evaluation

-In most questions, you will be graded based on both procedure and results. You could have made an error in a calculation, but if the procedure is correct, you will still get points.

-The course will be evaluated using percentage points, later converted to letters. The following limits will be used: <https://innsida.ntnu.no/wiki/-/wiki/English/Grading+scale+using+percentage+points>