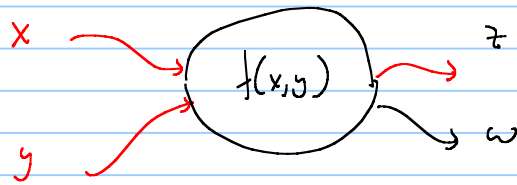


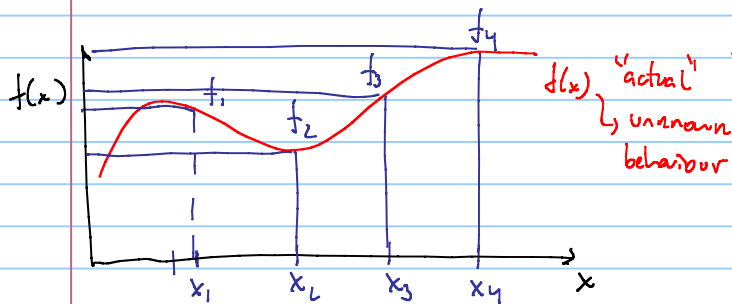
Notes to Youtube video 13

How to handle uncertain parameters in our FD calculations



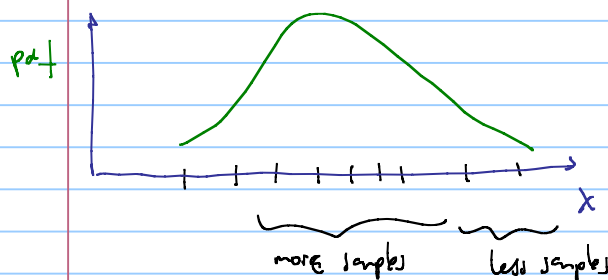
deterministic calculation: x and y have a unique known value

stochastic/probabilistic calculation: x and y exhibits a probabilistic distribution



Approach to deal with uncertainty:

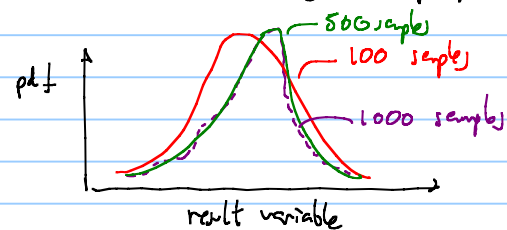
- create samples
- evaluate the function at samples
- calculate pdf and cdf of the results



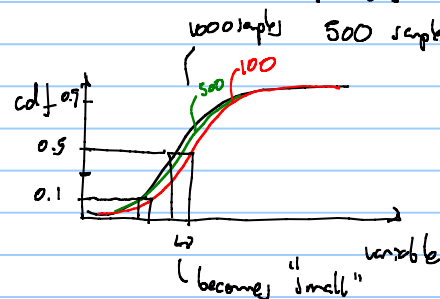
1: How many samples are needed?

2: How to generate the samples?

3: Increase the number of samples and see how the results change (pdf, cdf)



for this case, it seems 500 samples is enough

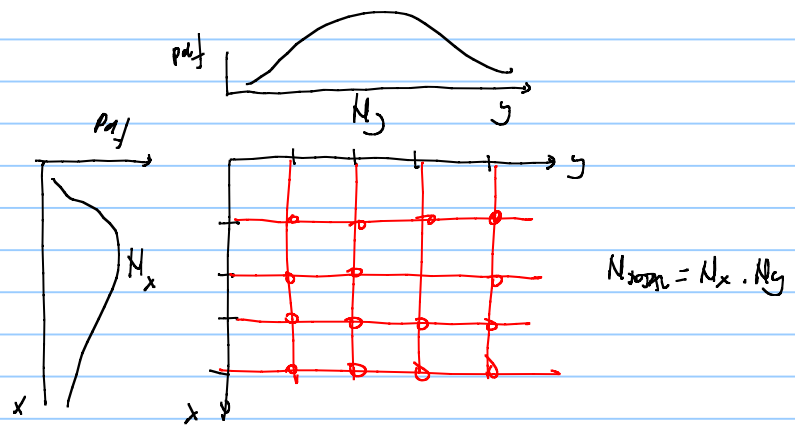
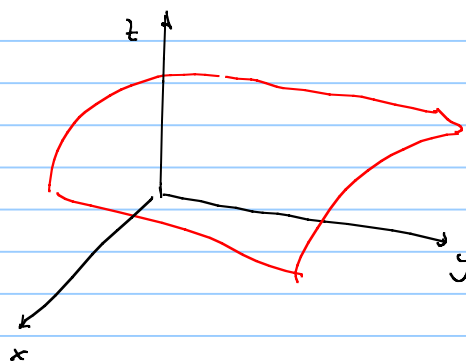


2: how to generate the samples

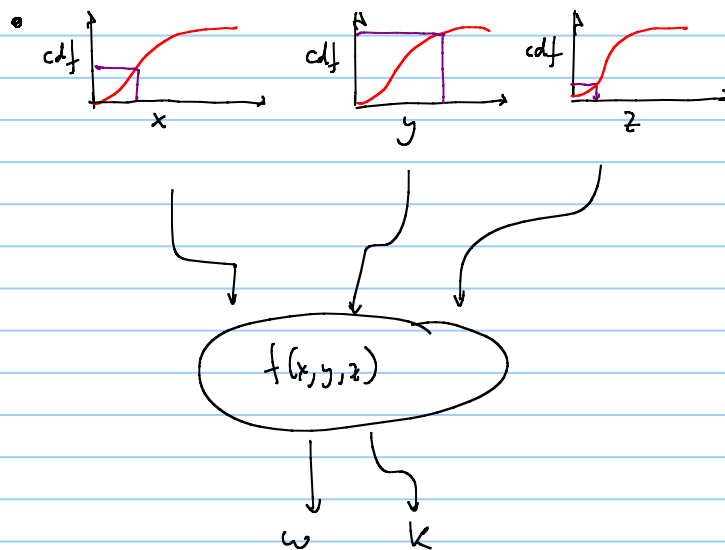
- Monte Carlo method
- Latin hypercube sampling

efficient sampling → less number of samples to achieve convergence

brute-force sampling



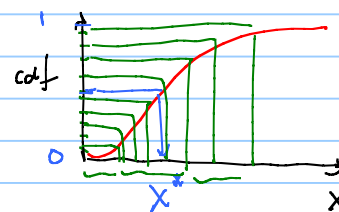
it is impractical for large number of variables / samples



① For each variable

1.1 pick a random number between 0-1

1.2 enter cdf and read the value of the variable



② perform a simulation with the samples

③ repeat "many" times steps 1-2

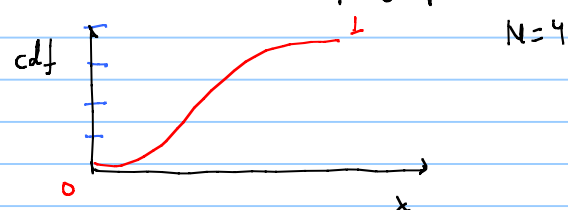
④ perform a frequency analysis on the results → pdf cdf

• Latin hypercube sampling (LHS)

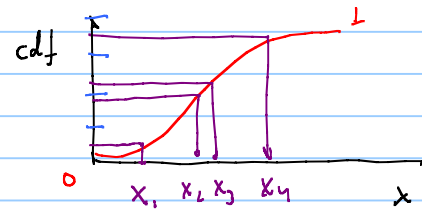
① Define a number of samples "N"

① For each variable

1.1. subdivide the cumulative probability in "N" intervals (equally-spaced)



1.2. Pick a random number in the interval
find the corresponding value of the
variable



$$\begin{matrix} \left\{ \begin{matrix} x_1 \\ x_2 \\ x_3 \\ x_4 \end{matrix} \right\} & \left\{ \begin{matrix} y_1 \\ y_2 \\ y_3 \\ y_4 \end{matrix} \right\} & \left\{ \begin{matrix} z_1 \\ z_2 \\ z_3 \\ z_4 \end{matrix} \right\} \end{matrix}$$

1.3. shuffle randomly the sample vector(s)

sim 1	x_3	y_1	z_3
sim 2	x_1	y_3	z_2
sim 3	x_4	y_4	z_1
sim 4	x_2	y_2	z_4

② perform simulations for sample variables that are
in the same row

③ perform a frequency analysis on the results
↳ cdf, pdf