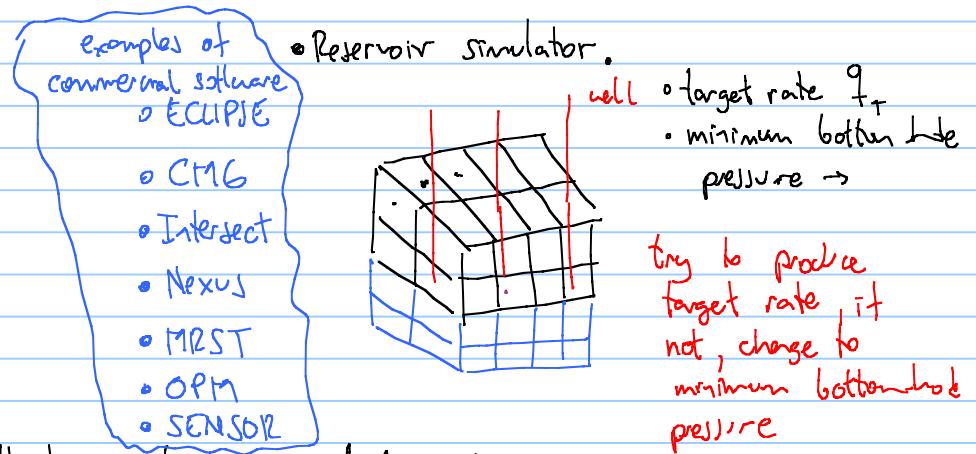


- Production scheduling
- Dry gas equations
- introduction to excel VBA (functions)
- class exercise

Production profiles (field performance) are typically estimated with:

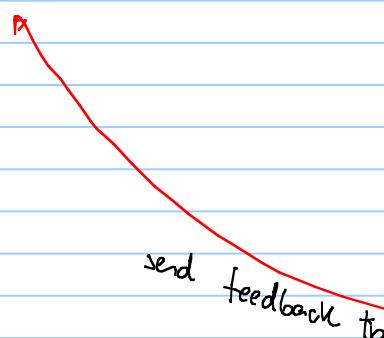


in FD, a workflow that is typically used by oil companies to compute realistic production profiles is:

Reservoir engineering

- 3D reservoir model

$$\begin{array}{l} q_{\text{target rates}}(t) \\ \sim q(t) \\ \text{Perfomr}(t) \\ \text{Pwf}(t) \end{array}$$



Production and facilities engineering

production simulator (steady-state)

check at each point in time is

$$q(t) \quad \left. \right\} \text{feasible?}$$

Perf(t) $\left. \right\} \text{is it enough to reach operator?}$

example of commercial software

- Pipesim
- Prosper, gap
- Olga
- pipesoft
- ReO

if not, try to make it feasible
flag years in which it is not possible to produce the rates

At early FD, there is usually no information on wells, gathering network or facilities, thus they are typically neglected

- Reservoir simulator "coupled" with a well + gathering network simulation in a IAM software

↳ integrated asset management

examples of software

- Resolute
- Avocet
- Pipe-it (now Tieto)

- material balance + Inflow performance relationship

P_r
So vsi t
 S_g
 S_w

$$q = f(P_r, \text{Inj})$$

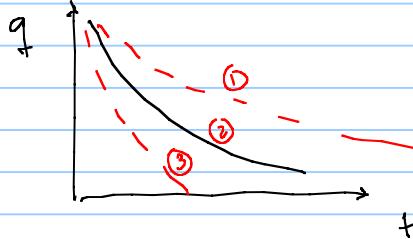
needs assumption on
Pact min

- material balance + well + network model

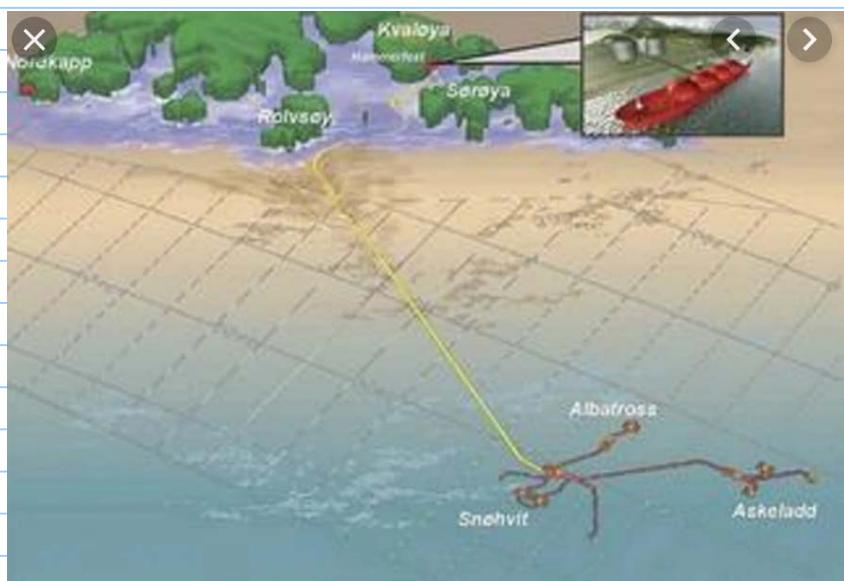
P_r
So vsi +
 S_g
 S_w

$$q = f(P_r, P_{wp})$$

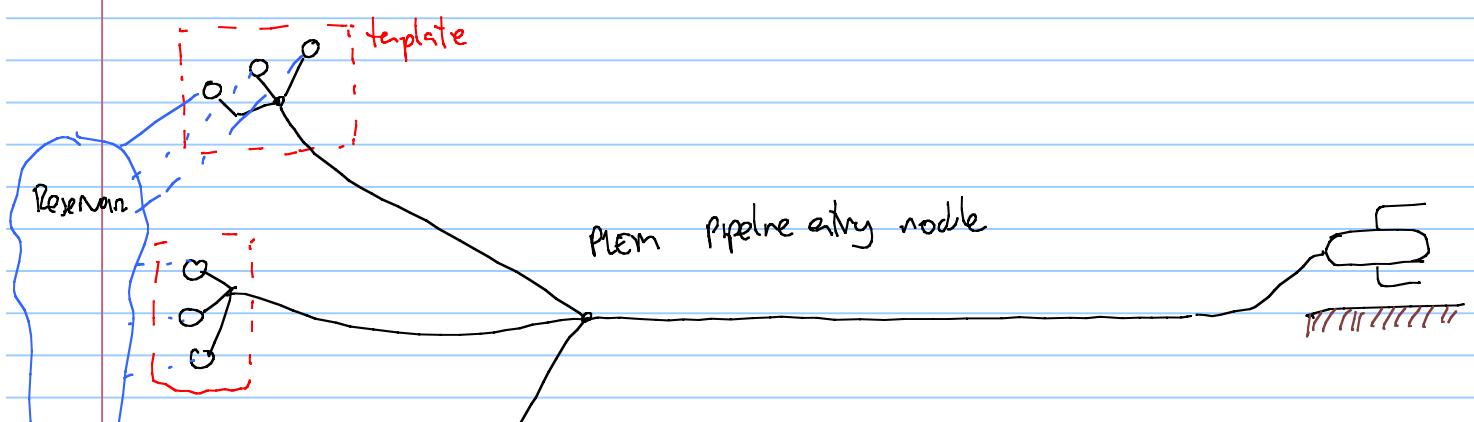
- decline or type curves



Class exercise: Production scheduling of Snowwhite field



Dry gas field



Our main task is to compute $q_g(t)$

Contact to deliver 20E6 Sm³/d to customer

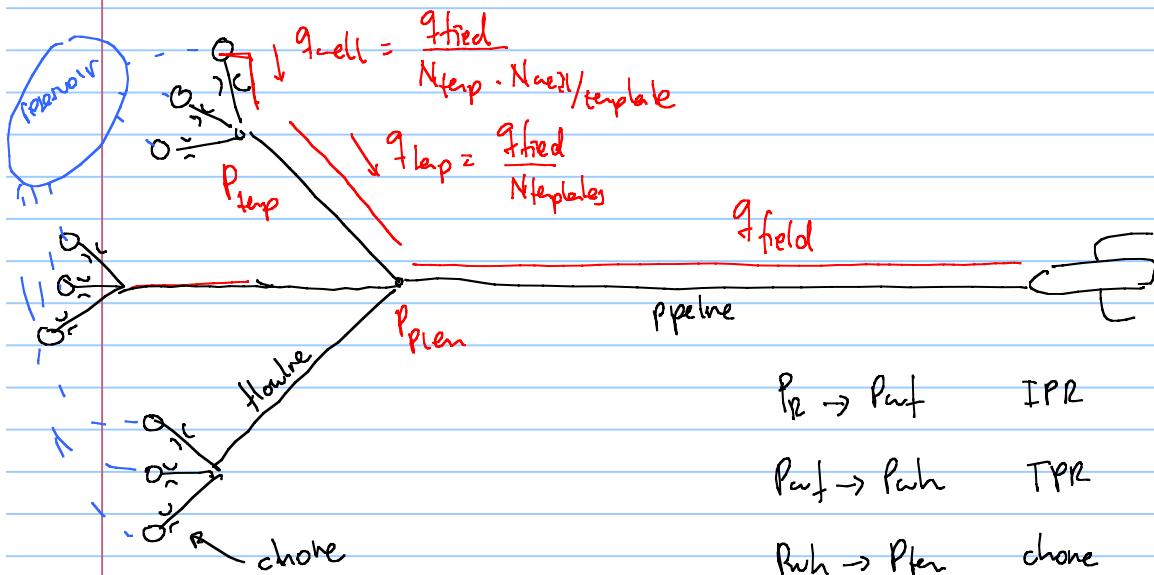
Our task, to compute

- plateau duration and post-plateau production

- Only dry gas, no liquid
 - { no condensate
no water
no production chemicals}

- all wells are identical (same production, same characteristics)

- templates are located symmetrically from the plan



$$P_R \rightarrow P_{\text{art}} \quad \text{IPR} \quad q_{\bar{g}} = f(P_R, P_{\text{art}})$$

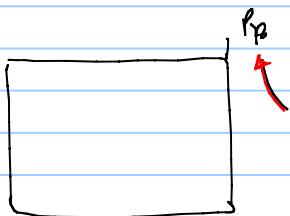
$$P_{\text{art}} \rightarrow P_{\text{wh}} \quad \text{TPR} \quad q_{\bar{g}} = f(P_{\text{art}}, P_{\text{wh}})$$

$$P_{\text{wh}} \rightarrow P_{\text{ten}} \quad \text{choke} \quad q_{\bar{g}} = f(P_{\text{wh}}, P_{\text{ten}}, C_d)$$

$$P_{\text{ten}} \rightarrow P_{\text{pl}} \quad \text{FPR} \quad q_{\bar{g}} = f(P_{\text{ten}}, P_{\text{pl}})$$

$$P_{\text{pl}} \rightarrow P_{\text{sep}} \quad \text{PPR} \quad q_{\bar{g}} = f(P_{\text{pl}}, P_{\text{sep}})$$

Reservoir model



Dry gas material balance

$$P_R = P_{\text{ri}} \frac{z_R}{z_i} \left(1 - \frac{G_p}{G} \right) \quad f(q_{\bar{g}})$$

$\underbrace{\frac{G_p}{G}}_{\text{uncertain value}}$

R_F recovery factor

gas deviation factor

$$\frac{z}{f(P_r, T_r)} \quad \frac{T_r}{T_c}$$

$\underbrace{\frac{P_r}{P_c}}_{\text{gas composition}} \sim f(\text{gas composition})$

MB dry gas equation is implicit

Given R_F , assume P_r

with P_r compute z_r

verifying that $\epsilon = P_r - P_{\text{ri}} \frac{z_R}{z_i} \left(1 - R_F \right) = 0 \leq \text{TOLerance}$

if not,

3.3.2 Z-Factor Correlations. Standing and Katz⁴ present a generalized Z-factor chart (**Fig. 3.6**), which has become an industry standard for predicting the volumetric behavior of natural gases. Many empirical equations and EOS's have been fit to the original Standing-Katz chart. For example, Hall and Yarborough^{21,22} present an

accurate representation of the Standing-Katz chart using a Carnahan-Starling hard-sphere EOS,

$$Z = ap_{pr}/y, \dots \quad (3.42)$$

where $a = 0.06125t \exp[-1.2(1-t)^2]$, where $t = 1/T_{pr}$.

The reduced-density parameter, y (the product of a van der Waals covolume and density), is obtained by solving

$$\begin{aligned} f(y) = 0 = & -ap_{pr} + \frac{y + y^2 + y^3 - y^4}{(1-y)^3} \\ & - (14.76t - 9.76t^2 + 4.58t^3)y^2 \\ & + (90.7t - 242.2t^2 + 42.4t^3)y^{2.18+2.82t}, \quad \dots \quad (3.43) \end{aligned}$$

$$\begin{aligned} \text{with } \frac{df(y)}{dy} = & \frac{1 + 4y + 4y^2 - 4y^3 + y^4}{(1-y)^4} \\ & - (29.52t - 19.52t^2 + 9.16t^3)y \\ & + (2.18 + 2.82t)(90.7t - 242.2t^2 + 42.4t^3) \\ & \times y^{1.18+2.82t}. \quad \dots \quad (3.44) \end{aligned}$$

The derivative $\partial Z/\partial p$ used in the definition of c_g is given by

$$\left(\frac{\partial Z}{\partial p}\right)_T = \frac{a}{p_{pc}} \left[\frac{1}{y} - \frac{ap_{pr}/y^2}{df(y)/dy} \right]. \quad \dots \quad (3.45)$$

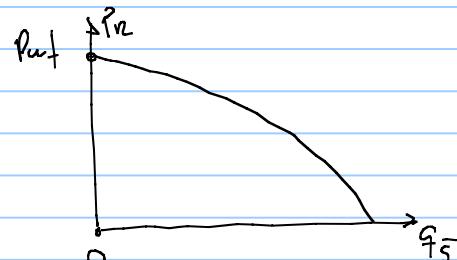
$$P_n \rightarrow P_{nf}$$

IPL equation

low pressure dry gas equation

$$q_g = C_R (P_n^2 - P_{nf}^2)^n \quad \begin{matrix} \leftarrow \text{back pressure exponent} \\ \text{linear } n \approx 1 \\ \text{turbulent } n \approx 0.5 \end{matrix}$$

inflow coefficient $\{ T_R, K, h, s \text{ (skin factor)} \}$



- pseud-steady state regime
(boundary dominated flow)
page 37 of compendium

equation approximation to Z chart

to predict T_c, p_c we will use
Sutton correlations

Sutton⁷ suggests the following correlations for hydrocarbon gas mixtures.

$$T_{pcHC} = 169.2 + 349.5\gamma_{gHC} - 74.0\gamma_{gHC}^2 \quad \dots \quad (3.47a)$$

$$\text{and } p_{pcHC} = 756.8 - 131\gamma_{gHC} - 3.6\gamma_{gHC}^2. \quad \dots \quad (3.47b)$$

$$\gamma_g = \frac{M_{wgas}}{M_{wair}} \quad (28.97)$$

$$M_{wgas} = \sum_{i=1}^N z_i M_{wi}$$

- $P_{wf} \rightarrow P_{wh}$

Dry gas tubing equation

$$\bar{q}_g = C_T \left(\frac{P_{wf}^2}{e^S} - P_{wh}^2 \right)^{0.5}$$

elevation coefficient
tubing coefficient (friction loss)

$$\bar{q}_g = 0$$

$$P_{wf} = P_{wh} e^{S/2}$$

(hydrostatic losses)

Page 156, Appendix A of compendium

$$q_{sc} = \left(\frac{\pi}{4} \right) \cdot \left(\frac{R}{M_{air}} \right)^{0.5} \cdot \left(\frac{T_{sc}}{p_{sc}} \right) \cdot \left(\frac{D^5}{f_M \cdot L \cdot \gamma_g \cdot Z_{av} \cdot T_{av}} \right)^{0.5} \cdot \left[(p_{wf}^2 - p_t^2 \cdot e^S) \cdot \left(\frac{S}{e^S - 1} \right) \right]^{0.5}$$

$$C_T = \left(\frac{\pi}{4} \right) \cdot \left(\frac{R}{M_{air}} \right)^{0.5} \cdot \left(\frac{T_{sc}}{p_{sc}} \right) \cdot \left(\frac{D^5}{f_M \cdot L \cdot \gamma_g \cdot Z_{av} \cdot T_{av}} \right)^{0.5} \cdot \left(\frac{S \cdot e^S}{e^S - 1} \right)^{0.5}$$

$$S = 2 \cdot L \cdot C_a = 2 \cdot \frac{M_g}{Z_{av} \cdot R \cdot T_{av}} \cdot L \cdot g \cdot \cos(\alpha)$$

$P_{wh} \rightarrow P_{tapp}$ choke no need for equation

$P_{tapp} \rightarrow P_{plen}$ flowline \rightarrow tubing equation can be used for flowline

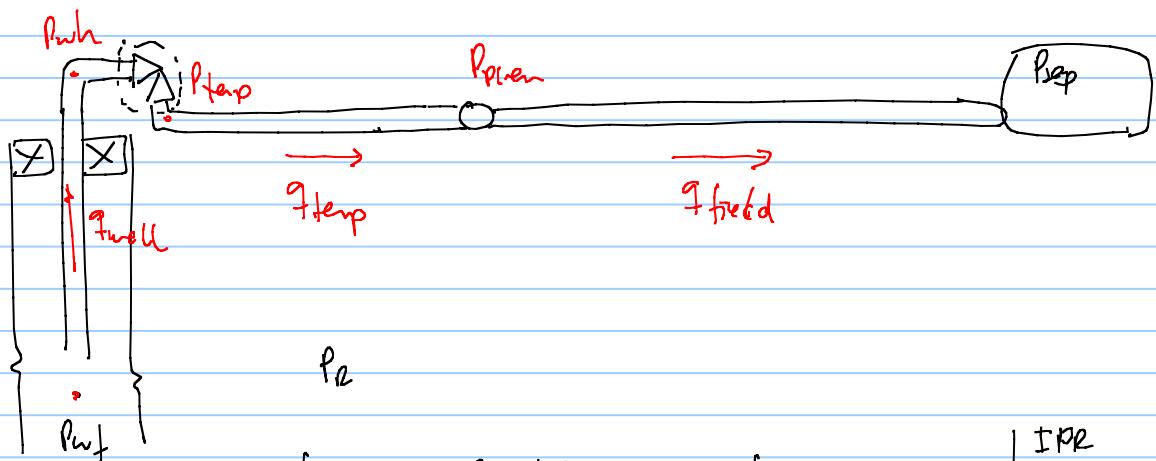
horizontal flowline, the tubing equation simplifies to

$$\bar{q}_g = C_{FL} \left(P_{tapp}^2 - P_{plen}^2 \right)^{0.5}$$

$S=0$ (l'Hopital)

$P_{plen} \rightarrow P_{sep}$

$$\bar{q}_g = C_{PL} \left(P_{plen}^2 - P_{sep}^2 \right)^{0.5}$$



fix rate. Calculate p_{wh} from reservoir $\left\{ \begin{array}{l} \text{IPR} \\ \text{TPR} \end{array} \right.$

Calculate P_{sep} from sep $\left\{ \begin{array}{l} \text{PPR} \\ \text{FPR} \end{array} \right.$

verify $p_{\text{wh}} > P_{\text{sep}} \rightarrow$ rate is feasible

$p_{\text{wh}} < P_{\text{sep}} \rightarrow$ rate not feasible, must be reduced

http://www.ipt.ntnu.no/~stanko/files/Courses/TPG4230/2020/Class_files/20200124/

VBA Visual basic for applications

for pipe equations in VBA ① is upstream

\overrightarrow{q}

② is downstream

① ②

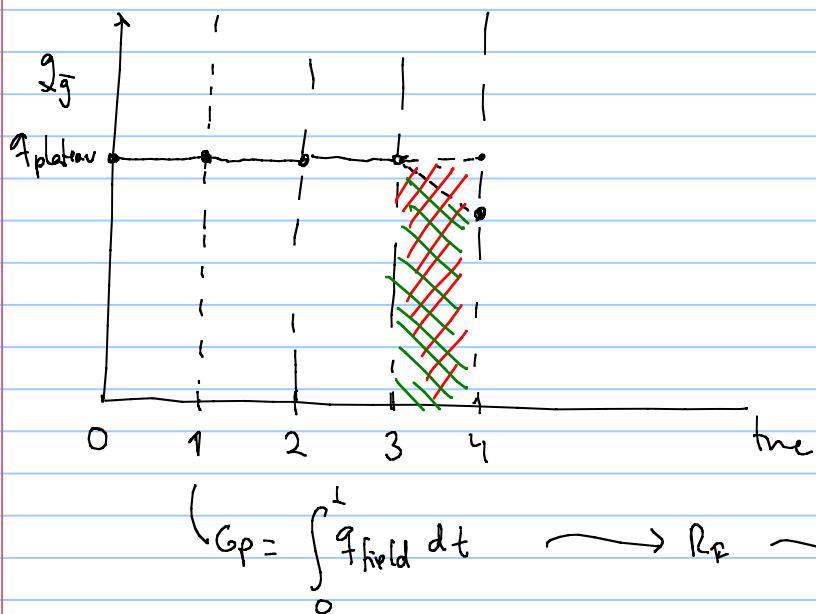
① p_{wh}

① p_{wf}

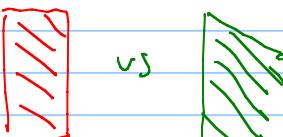
① P_{sep}

② $P_{\text{reservoir}}$

② q_{sep}



rectangular integration give a poor approximation of G_p when in decline phase



- improvement
- use smaller time-step
- use a better integration

$$\Delta G_p = \frac{(q^{i-1} + q^i)}{2} \Delta t$$

A 2 P_n

Approximation, q_{field}^0 is constant between $0 \rightarrow 1$

G=IGIP	270E+09 Sm3											
Annual production rate	0.027 fraction of IGIP											
Production days per year	365 day											
T _R	92 oC											
P _i , initial Res pressure	276 bara											
C _i , inflow Back pressure coefficient	1000 Sm3/bar ⁿ											
n, backpressure, exponent	1											
C _t , Tubing coefficient (2100 MDx0.15)	4.03E+04 Sm3/bar											
Elevation coeff, S	0.155											
C _{FL} , Flowline Template-PLEM (5000x0.1)	2.83E+05 Sm3/bar											
C _{PL} , Pipeline PLEM-Shore (158600x0.6)	2.75E+05 Sm3/bar											
Separator (slug catcher) pressure	30 bara											
Gas molecular weight (Methane)	16 kg/kmole											
Gas specific gravity	0.55 Gas specific gravity											
Gas density at Sc	0.67 kg/m ³											
Number of templates	3											
Number of wells	9											
Desired plateau	20 years											
qfield	20.0E+06 [Sm ³ /d]											
Field gas rate for abandonment	5.00E+06 [Sm ³ /d]							for each well				
time	qfield	Gp	Z	PR	qwell	Pwf	Pwh avail	Ptemp req	Pplem req	Psep	qtemp	DeltaPchoke
[years]	[Sm ³ /d]	[Sm ³]	[-]	[bara]	[Sm ³ /d]	[bara]	[bara]	[bara]	[bara]	[bara]	[Sm ³ /d]	[bar]
0	20.0E+06	000.0E+0	0.967291	276.0E+0	2.2E+6	272.0	245.6	82.0	78.6	30.0	6.7E+6	164
1	20.0E+06	7.29E+09	0.962615	269	2.2E+6	264.4	238.4	82.0	78.6	30.0	6.7E+6	156
2	20.0E+06	1.46E+10	0.957442	260	2.2E+6	255.5	230.0	82.0	78.6	30.0	6.7E+6	148
3	20.0E+06	2.19E+10	0.952572	251	2.2E+6	246.6	221.5	82.0	78.6	30.0	6.7E+6	139
4	20.0E+06	2.92E+10	0.948138	242	2.2E+6	237.8	213.1	82.0	78.6	30.0	6.7E+6	131