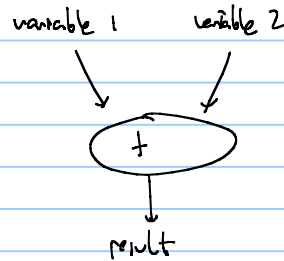


Uncertainty quantification

especially big during the development phase

One way already covered: Ceteris Paribus $\rightarrow$ sensitivity analysis $\rightarrow$ purpose

evaluate how KPI (key performance indicator) varies with inputs



Does not allow to evaluate ALL possible outcomes

Probabilistic reserve estimation

$$N = \frac{V_R \cdot \Phi \cdot S_o \cdot N_{TG}}{B_o}$$

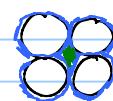
Net to gross



Box-shaped reservoir

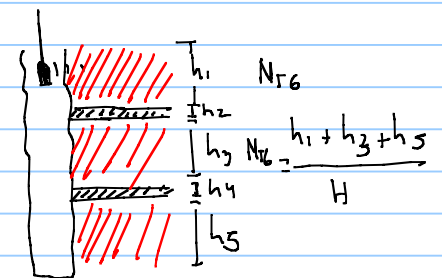
OOIP

there are variations on all variables in that formula



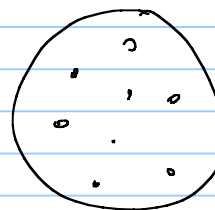
A probability distribution is typically used for variables that are uncertain

An example of 2287 core samples taken from exploration wells

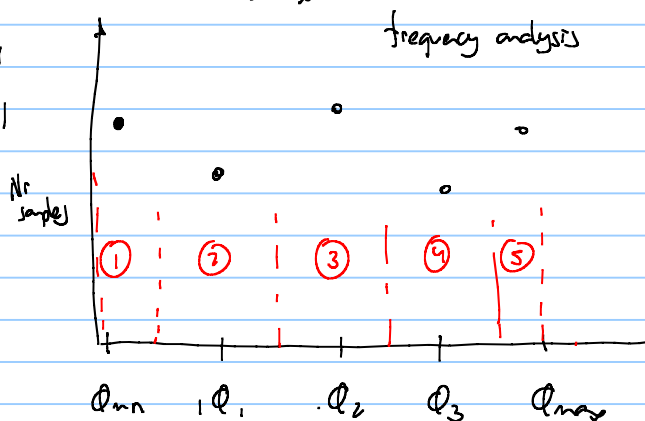


Sample	Observed
1	Q_1
2	Q_2
3	Q_3
4	Q_4
...	...
...	...
...	...

Q_{min}
 Q_1
 Q_2
 Q_3
 Q_{max}

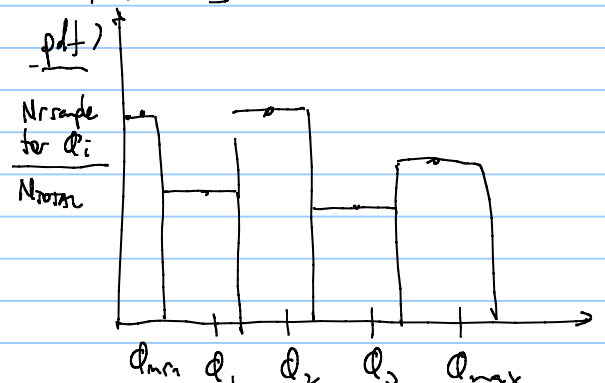


frequency analysis

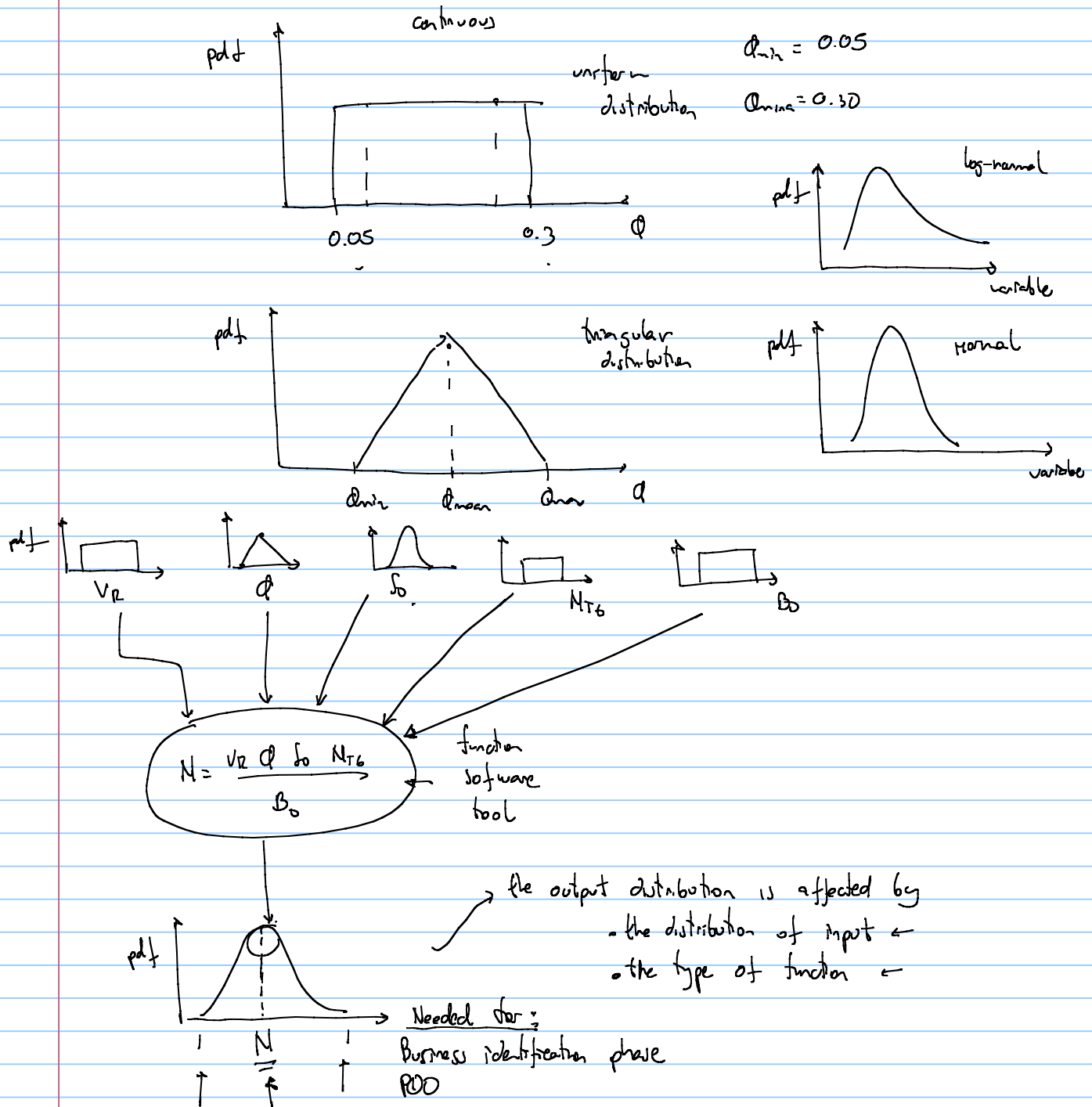


discrete

probability distribution function



if I haven't made any measurements of porosity, I can assume a distribution



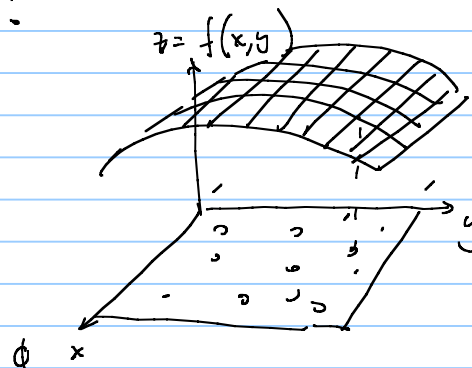
How to calculate the pdf of the output?

Sampling methods

Random sampling

$$x_1, y_1 \rightarrow z_{1,1}$$

$$x_1, y_1 \rightarrow z_{1,2}$$



this is called Monte-Carlo method

JOURNAL OF THE AMERICAN STATISTICAL ASSOCIATION

Number 247

SEPTEMBER 1949

Volume 44

THE MONTE CARLO METHOD

NICHOLAS METROPOLIS AND S. ULAM
Los Alamos Laboratory

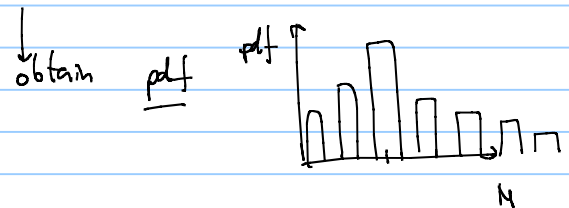
We shall present here the motivation and a general description of a method dealing with a class of problems in mathematical physics. The method is, essentially, a statistical approach to the study of differential equations, or more generally, of integro-differential equations that occur in various branches of the natural sciences.

to calculate pdf of output

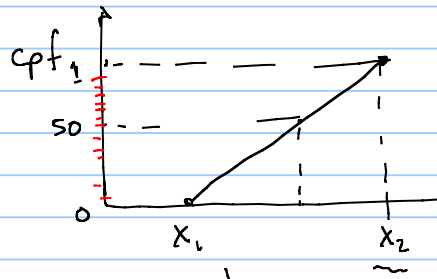
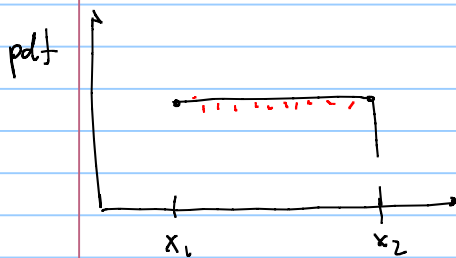
- assume a random number for input (for each variable)
 - run simulation / calculate outputs
 - Register / store output
- repeat for N times

N should be chosen such as the resulting pdf doesn't change significantly

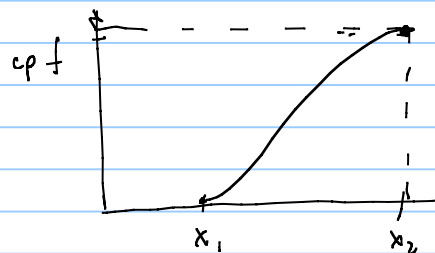
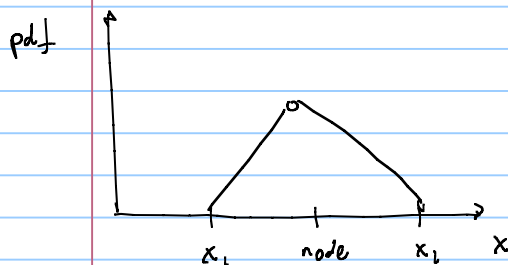
Apply a frequency analysis on outputs



the random sampling is typically done on cdf (cumulative probability function)



$$X = X_{min} + \text{Rand}() (X_{max} - X_{min})$$



```

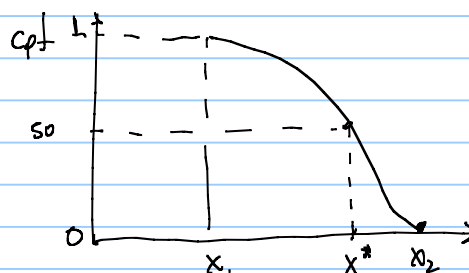
****Triangular distribution****
'Value of the variable X, randomly generated

'a = minimum value
'b = maximum value
'c = mode

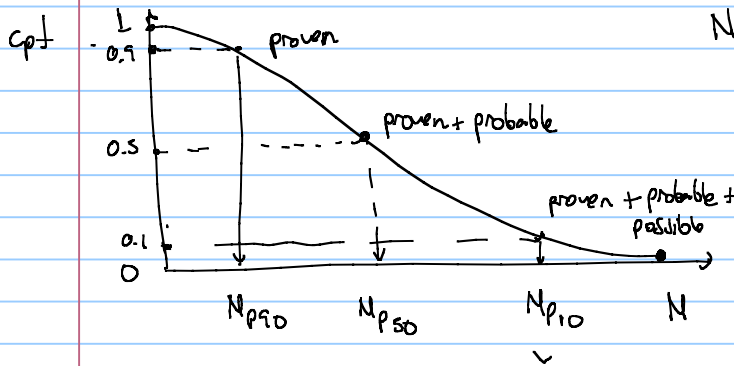
Function X_triang(a, b, c)
U = Rnd()
Fc = (c - a) / (b - a)
Application.Volatile (True)
If U < Fc Then
X_triang = a + (U * (b - a) * (c - a)) ^ 0.5
Else
X_triang = b - ((1 - U) * (b - a) * (b - c)) ^ 0.5
End If
End Function

```

cdf can also be plotted



for reserves we used the "reversed" cdf



N_{p90} there is 90% probability that N is equal or higher than $p90$

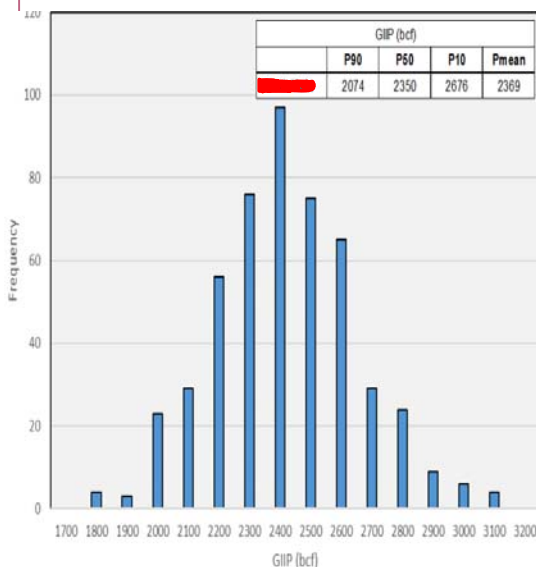
N_{p50} there is 50% probability that N is equal or higher than $p50$

N_{p10} there is 10% probability that N is equal or higher than $p10$

Some companies/countries use different %

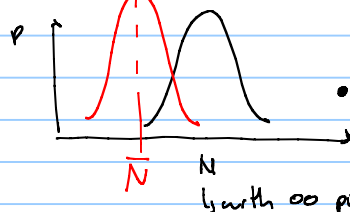
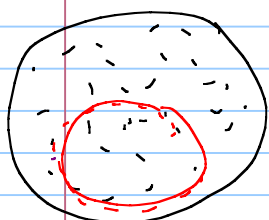
Table 5.2-1: Hebron Ben Nevis (Pool 1) In-Place Volumes Range

Hebron Ben Nevis Oil	Upside Volumes		Best Estimate Volumes		Downside Volumes	
	MBO	Mm ³	MBO	Mm ³	MBO	Mm ³
D-94 Fault Block	1601	255	1328	211	1077	171
I-13 Fault Block	252	40	187	30	141	22
Total Hebron Ben Nevis	1870	297	1515	241	1204	191



the applicability of Monte Carlo depends on the running time of "function" "simulator"

How many iterations are needed?

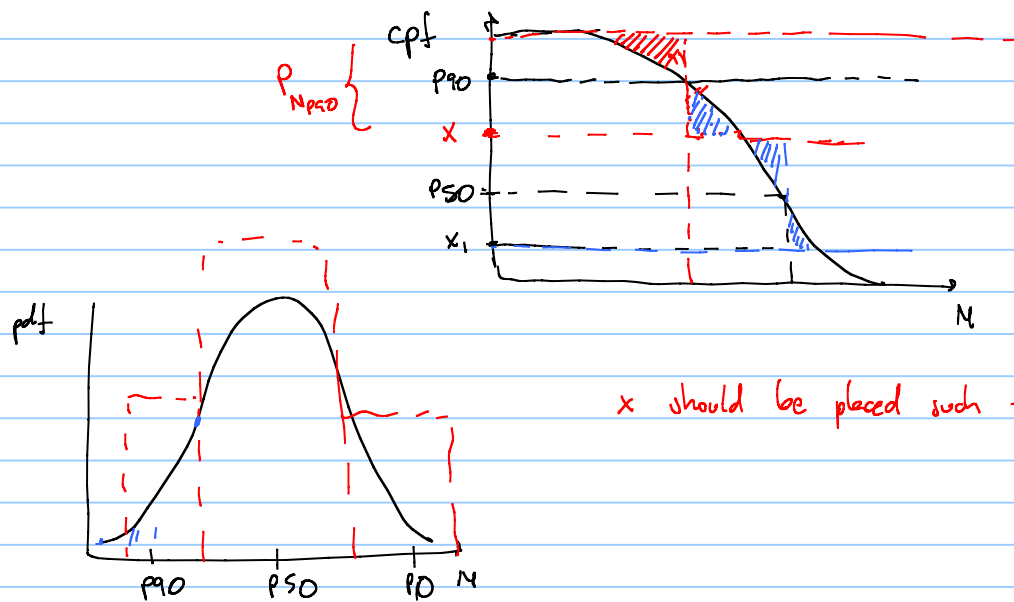


- Procedure 1 trial and error increase "N" until results don't change
- 3-1 standard deviation
- 2 central limit theorem

$$n_{1+} = \left(\frac{3 \cdot S_x}{\text{Error}} \right)^2$$

3-7% $\bar{N}$ - average of simulation point

if I wish to use $N_1 = P10$ what are probabilities?
 $N_2 = P50$
 $N_3 = P90$



x should be placed such that $\text{red box} = \text{blue box}$

option n to calculate the EMV of a branch

$$EMV_{\text{branch}} = \sum_{i=1}^N P_i EMV_i \quad \text{of all options on that branch}$$