

## ↑ PG 4230 Field Development and operations

Prof: Milan Stanko → Production engineering

Tuesdays 8:15-11:00      Thursdays 14:15-1600

mixed theory and exercise sessions

→ made by me in class  
→ done by students with my support

bring Laptop or  
team-up with a  
friend

60% written exam  
40% exercises / project

5-6 sets

date 15.05.2017 14.09:00

Consultation hours: after class

my office 230 2<sup>nd</sup> floor      milan.stanko@ntnu.no

Main communication tool is Its Learning. check it frequently  
use the "discussion tools"

Student assistants:

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Vemund Flatebakken



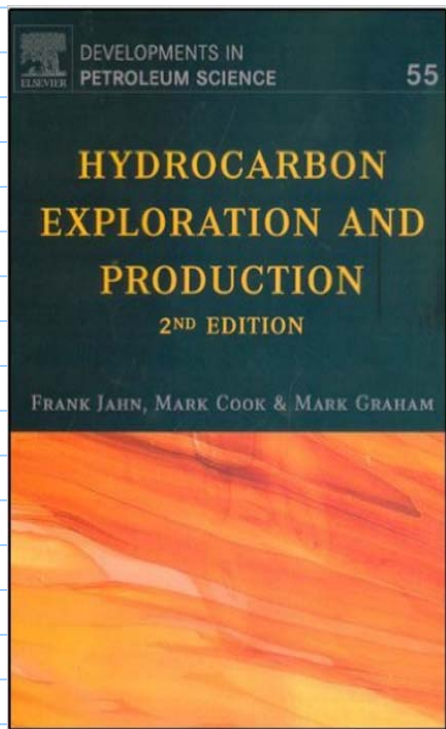
vemundf@stud.ntnu.no

- requirement for the exercises deliver all but 1  
the compound exercise grade has to be 20/40  
penalty for late delivery

Reference group:

<http://www.ipt.ntnu.no/~stanko/index.html>

Bibliography → support material



this course is focused on offshore Norway production

Field development and operations

flexibility  
uncertainty  
sensitivity analysis  
scenarios  
optimization

are tied to a physical system  
to cope with its deficiencies

• exploit its advantages

• {constrained}  
• effectivization  
• maintenance, troubleshooting

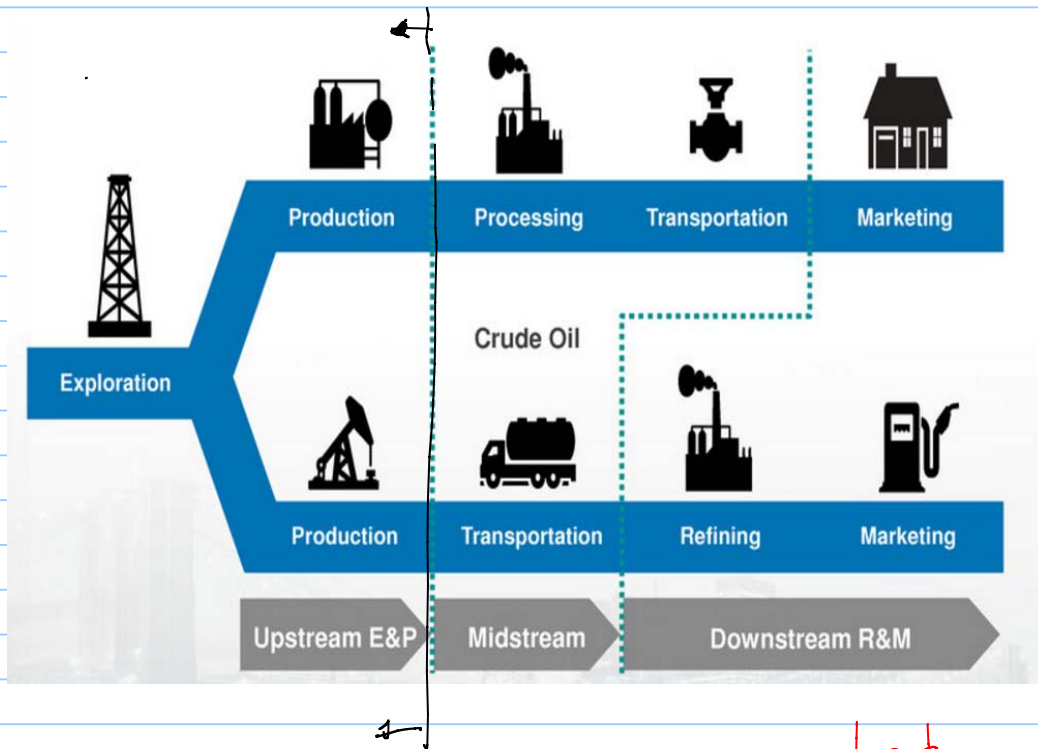


Topic	Level	Exercise	(Engineering skills)	Computational Tools
Life cycle of a hydrocarbon field	Appreciation	NO	-	-
Field development workflow - Probabilistic reserve estimation - Cost estimation and NPV calculations	Appreciation/ configuration/ (design)	YES	Gant chart, NPV calculations, Spider plot, decision trees, Monte Carlo simulation, basic probability	Excel VBA
Offshore (and some onshore) field architectures and layout of production systems - Production manifold - Pigging facilities	Configuration	YES	Engineering diagrams and drawings. Analysis	-
Dynamics of marine structures - Wave statistics	Configuration/ design	YES	Analysis. Modeling. Fast Fourier Transform for signal analysis.	Excel VBA
Reservoir depletion and field performance - Production potential - Production scheduling - Flow equilibrium in production systems, choking and boosting - Flow performance of surface and downhole production networks	Design	YES	Modeling. Programming. Problem solving	Excel VBA, Gap, Prosper (or Pipesim)
Flow assurance - Modeling of gas and condensate transport in pipeline and hydrate formation - Simplified modeling of oil and water emulsions	Appreciation, Design	YES	Modeling. Programming. Analysis. Problem solving.	Hysys, Excel VBA
ESP fundamentals, design and plan for the field life	Design	YES	Modeling. Problem solving.	Excel VBA
Early subsea boosting design	Design	YES	Modeling. Problem solving.	Excel VBA
Data management and (allocation)	Appreciation/ design	YES	Data analysis, filtering, QC, averaging, aggregating.	Excel VBA
Production optimization.	Design	YES	Analysis, modeling, critical thinking. Problem solving.	Excel VBA
Integrated asset modeling I Am	Appreciation	NO	-	-
Additional skills gained by home and class exercises			(Group work) Develop written and oral engineering communication skills.	

Material balance	TPG4145	Whitson
Reservoir simulation fundamentals, flow tables	TPG4160	Kleppe
Well inflow	TPG4245	Ashwin
Fluid phase behavior	TPG4145	
Black oil model	TPG4145	
Single and multi phase fluid flow in pipes (computation of pressure and temperature losses)	TPG4135 TPG4245	Larsen
Processing fundamentals, separation,	TPG4135	
Compression fundamentals	TPG4135	
Pumping fundamentals	TPG4135	

Introduction to subsea boosting	TPG4200	sangesland
Introduction to subsea systems	TPG4200	
Risk analysis, decision making, uncertainty	TPG4151	Bratbold
Life cycle of an oil and gas field. Fundamentals	TPG4105	Stokas

where are we? P11



location

E and P

exploration and production

understanding  
the subsurface

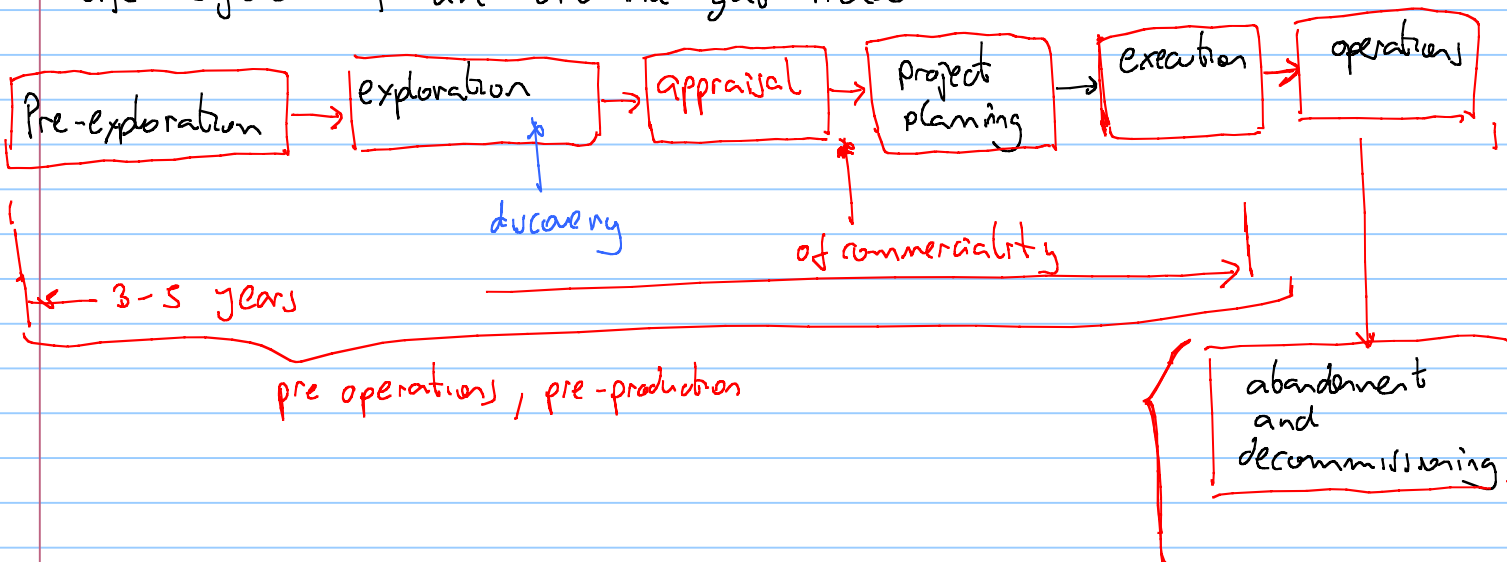
optimization of  
the development  
development phase  
operation phase

commercialize the  
resource

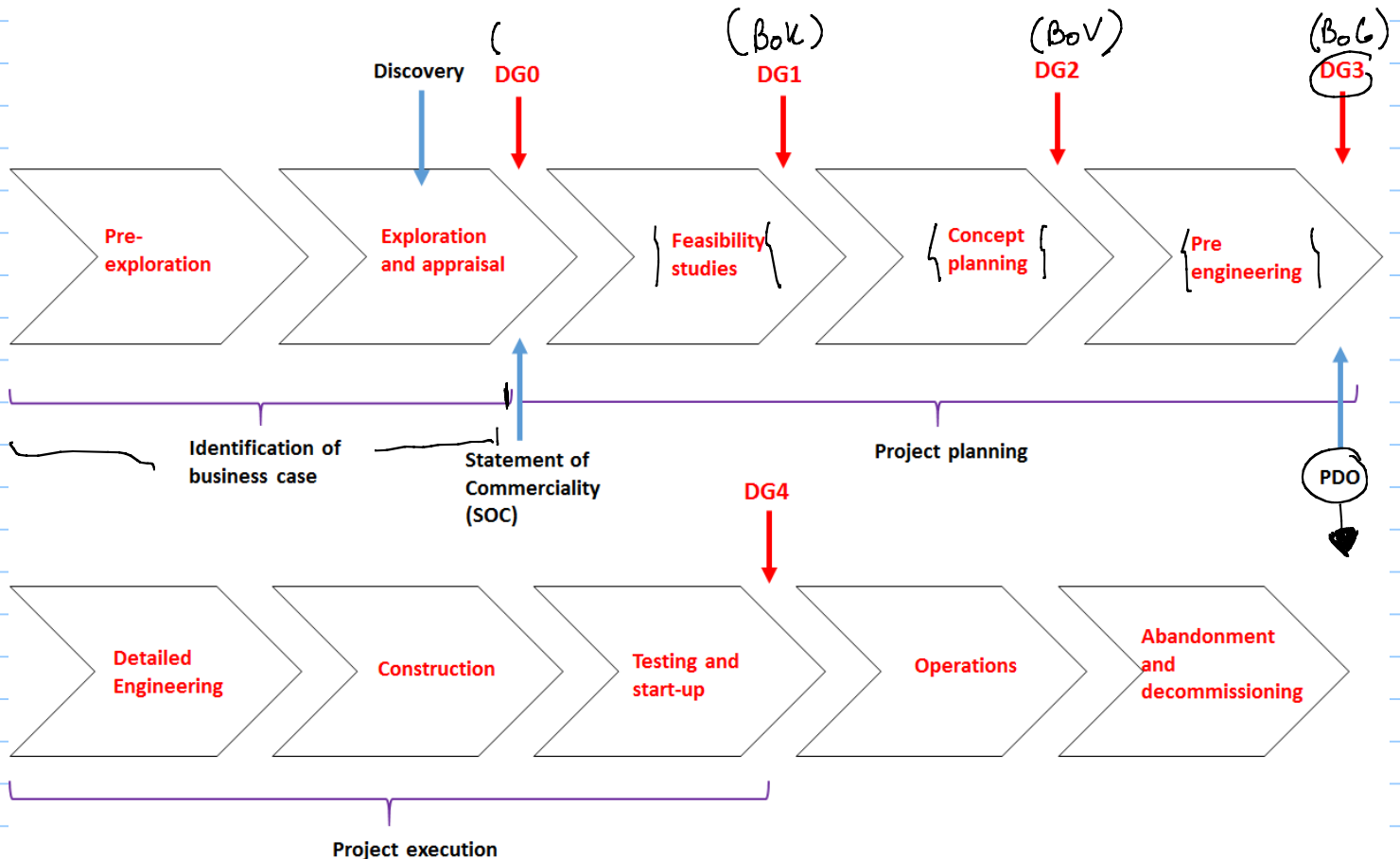
when?

30 years

life cycle of an oil and gas field



DG - decision gate



## • Identification of business case:

Demonstrate economic potential of the discovery and quantify and reduce uncertainty about recoverable reserves.

Steps: 1<sup>st</sup> pre exploration activities and scouting

- ↳ collect information on areas of interest where there might be potential for hydrocarbon accumulation
  - technical, political aspect, geographical, social, geological, environmental

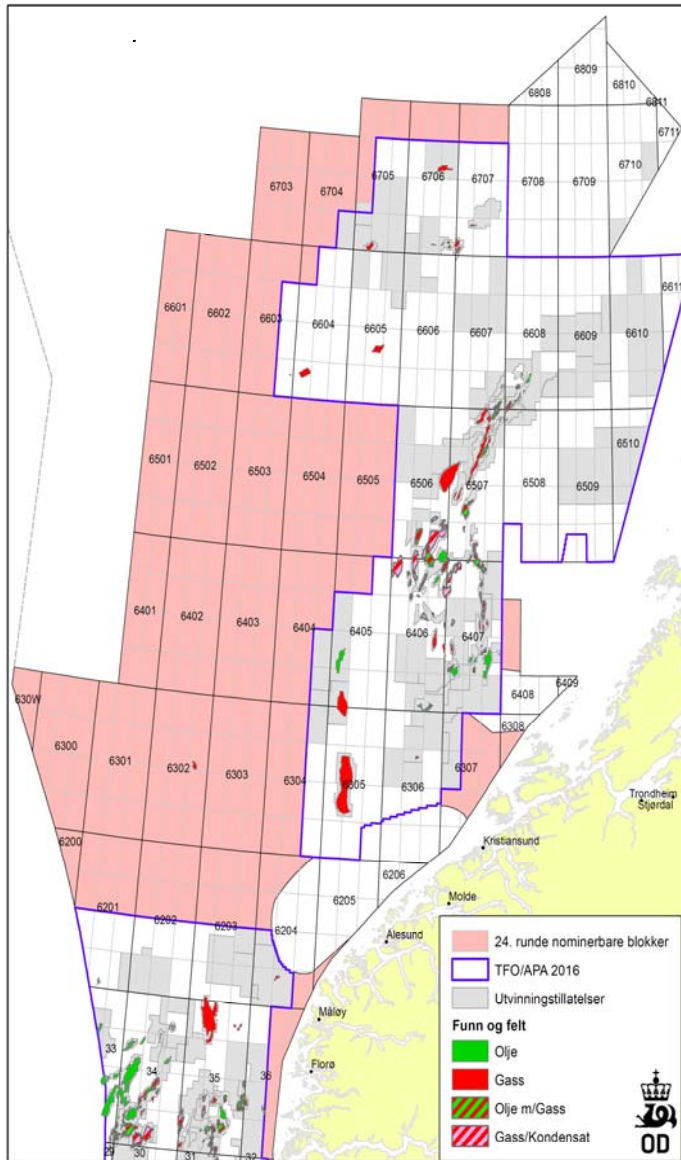
↳ chance of finding reserves and how big

2<sup>nd</sup> Getting pre-exploration access → the exploration license

non-exclusive right to an area { seismic } in MCS  
 { shallow wells }  
 ↳ Sometimes this is done by specialized companies.

3: Identity a prospect

4: Applying for a exclusive production license. In NCS  
 is max 10 years \*  
 • licensing rounds (frontier areas)  
 • APA (Awards in predefined areas)



1<sup>st</sup> year

34000 NOU/km<sup>2</sup>

2<sup>nd</sup>

68 000 NOU/km<sup>2</sup>

3<sup>rd</sup>

134 000 NOU/km<sup>2</sup>

### • Exploration

perform geological studies, geophysical survey,  
 seismic, exploration drilling.

well cores  
 well cores  
 cuttings  
 fluid samples  
 productivity test  
 logging  
 DST  
 Drill stem  
 test

### • Discovery!

- Assess the discovery further. Uncertainty, manage risk.
  - • Probabilistic reserve estimation. Identify and assess additional prospects and segments
  - Perform simplified economical evaluation
  - • Field appraisal to reduce uncertainty: more exploration wells and seismic. fault communication  
extent of reservoir  
aquifer  
woc water oil contact  
goc gas oil contact  
etc
- Reach D60
  - Issue a SOC (Statement of commerciality) and ROC  
continue to next phase
  - Do more appraisal.
  - Sell the discovery
  - Do nothing wait
  - Relinquish to the government

### Project planning phase:

- feasibility studies find one or concepts (general) that are technically, commercially and organizationally viable
- objectives of the developments
- establish feasible development scenarios
- demonstrate technical and economical feasibility

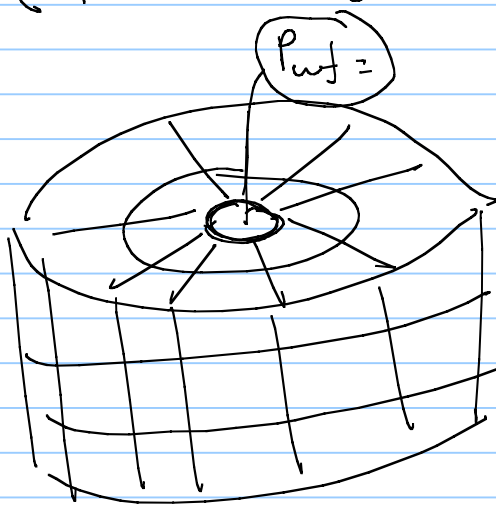
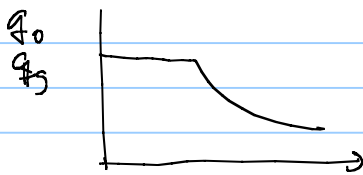
- identify potential stoppers
- Identify the need for new technology
- Cost estimation including system.

### Concept planning

Identify alternative concepts, select a "viable" concept and document it preparing for OG2

- Define the commercial aspects: legislation, agreements, licensing, financing, marketing and supply, taxes

- Reservoir behavior (depletion strategy) → production profiles



reservoir model

- static modeling
- dynamic modeling

- Reservoir simulator
- material balances + IPR equation
- Decline curve analysis

- Flow assurance
  - hydrates
  - wax
  - scale
  - slugging

- Drilling and well planning
- facilities
- operation, start-up, operations, maintenance
- Concept selection

- Cost and manpower estimates

## Pre engineering

mature, define document the selected concept -

- Selection of the final technical solution. Define all remaining technical alternatives
- execute FEED (front end engineering design)

technical requirements (arranged in packages) based on the final solution. After solution

- plan and prepare the execution phase.
- prepare submission of PDO plan for development and operations

Consequence and impact report.

PID. Plan for installation and operation of facilities for transport and utilization of petroleum

for next class read page 9-17.

Field development process

FDP field development plan

PUD Plan for utbygging og drift

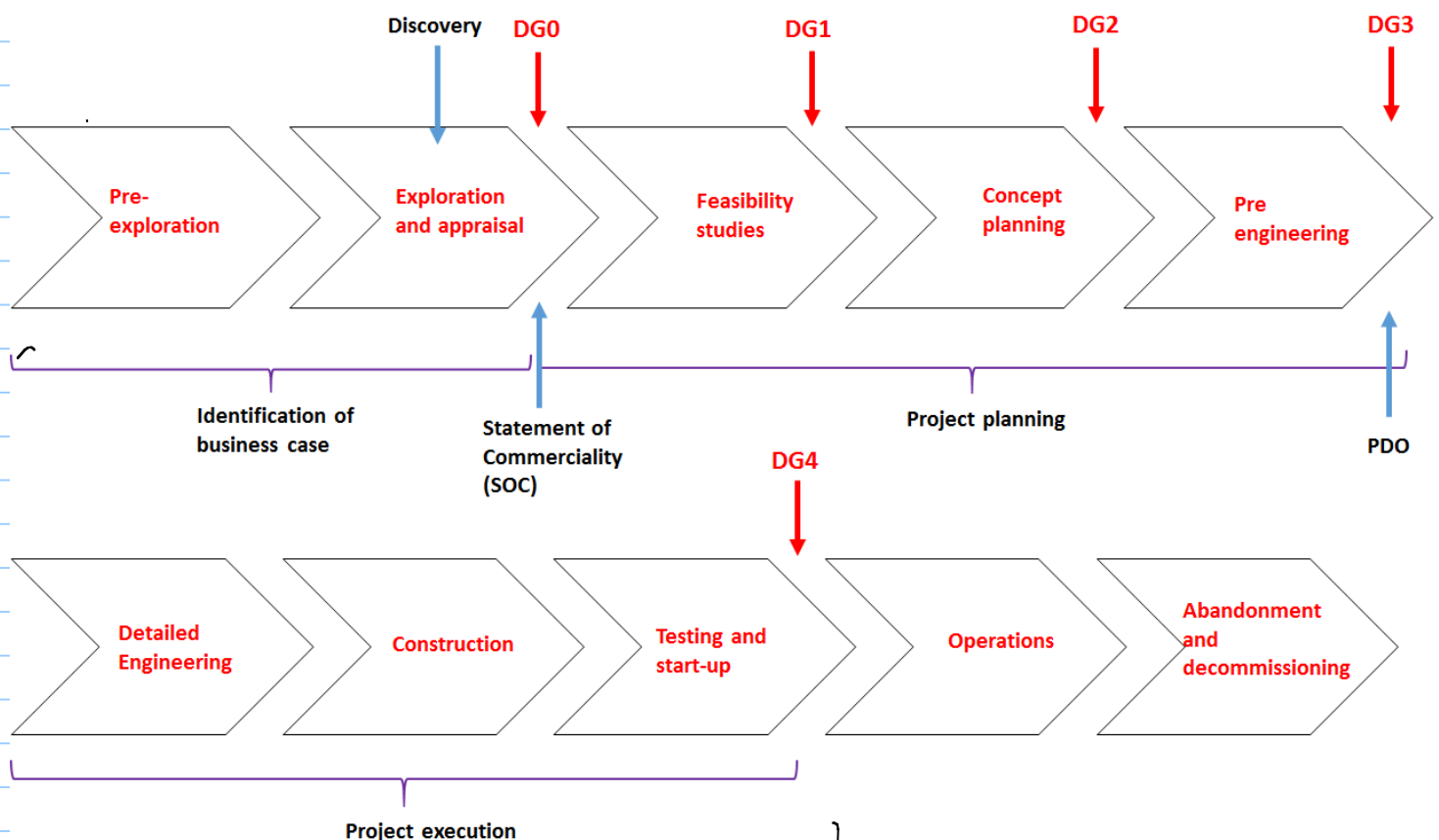
[http://www.npd.no/Global/Engelsk/5-Rules-and-regulations/Guidelines/PDO-PIO-guidelines\\_2010.pdf](http://www.npd.no/Global/Engelsk/5-Rules-and-regulations/Guidelines/PDO-PIO-guidelines_2010.pdf)

Read compendium from page 42-49

[http://folk.uio.no/hanakrem/svalex/Misc/Visund\\_PDO\\_PUD.pdf](http://folk.uio.no/hanakrem/svalex/Misc/Visund_PDO_PUD.pdf) example for Visund field

Impact assessment

Project execution phase



• Individual contracts

↳ several companies

Detailed engineering

Bids, contracts

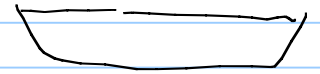
Construction, fabrication

Installation

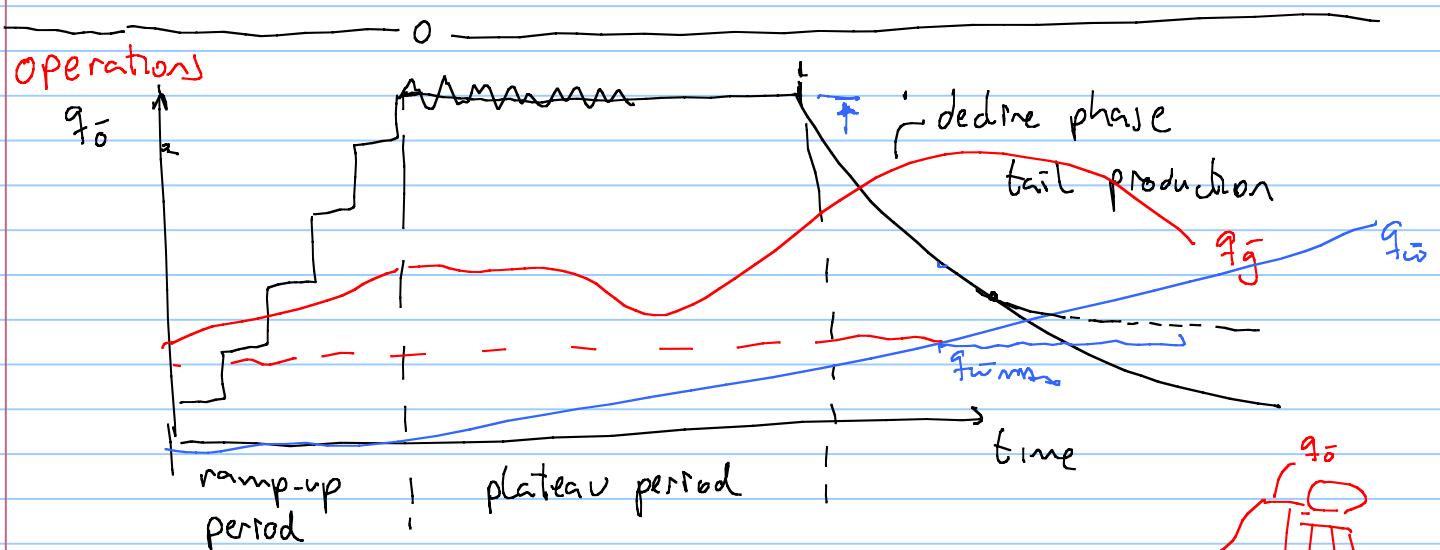
Commissioning



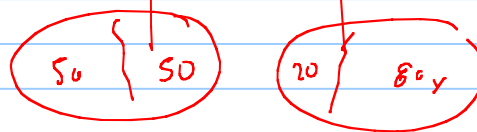
EPCM (Engineering, procurement, construction, management)  
Single company.



- Constructing well
- Perform hand over to asset, operations
- prepare for start-up, operation and management



- Maintenance
- Allocation.  $\rightarrow$  metering
- troubleshooting
- Debottlenecking



facilities have  $q_{g \max}$   
 $q_{w \max}$   
 $\rightarrow$  dealing with associated products

- IOR improved oil recovery methods.

drilling more wells  
boosting  
artificial lift  
reperforate

- stop production

## • Decommissioning phase

- Define a timeline and a plan
- Coordinate with relevant environmental agencies
- well plugging and abandonment (TPG4200)
- Cut conductor
- engineer "down and clean" flushing and clean tanks, processing equipment, piping
- prepare the offshore structure for removal
- plan and remove topside equipment
- lifting operations and transport
- remove or bury subsea pipelines
- mark and register leftover installations on marine maps
- monitoring
- Recovery of material / steel
  - recycling of equipment
    - Gas turbine
    - separator
    - pump
    - processing
- disposal of residues

Decommissioning:

Overview of activities

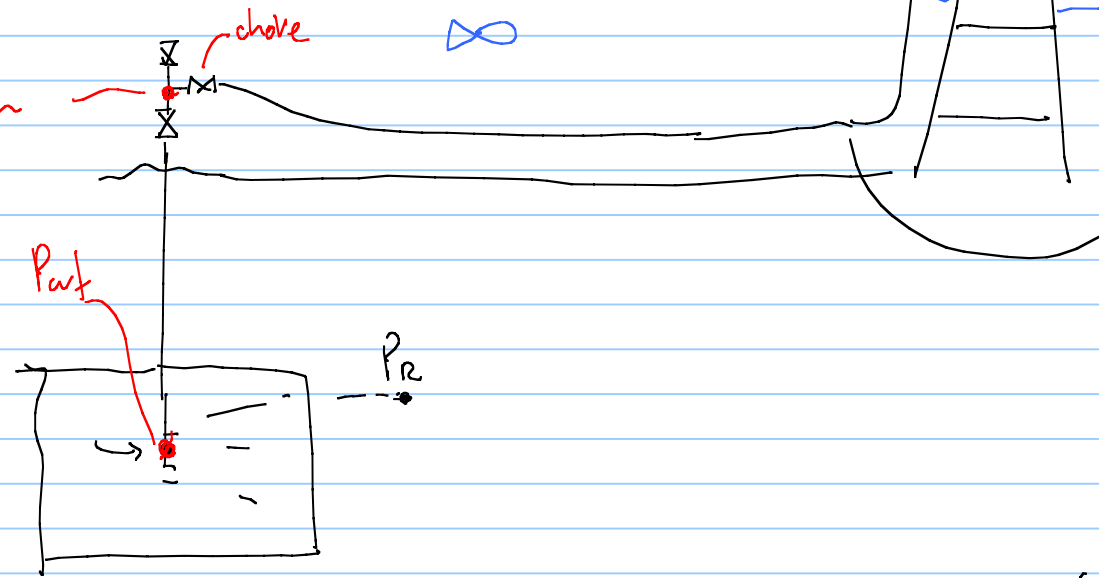
<https://www.youtube.com/watch?v=8Xm9VNZul9M>

Transport of platform and scrap yard

<https://www.youtube.com/watch?v=1GA3Elu81rw>

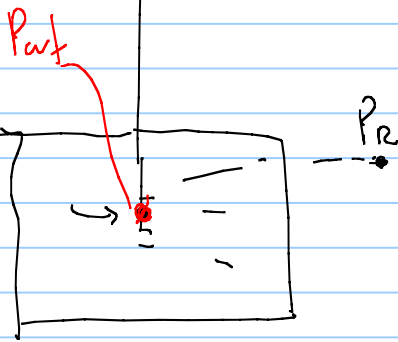
indicates standard conditions

flowing wellhead pressure  $P_{wh}$



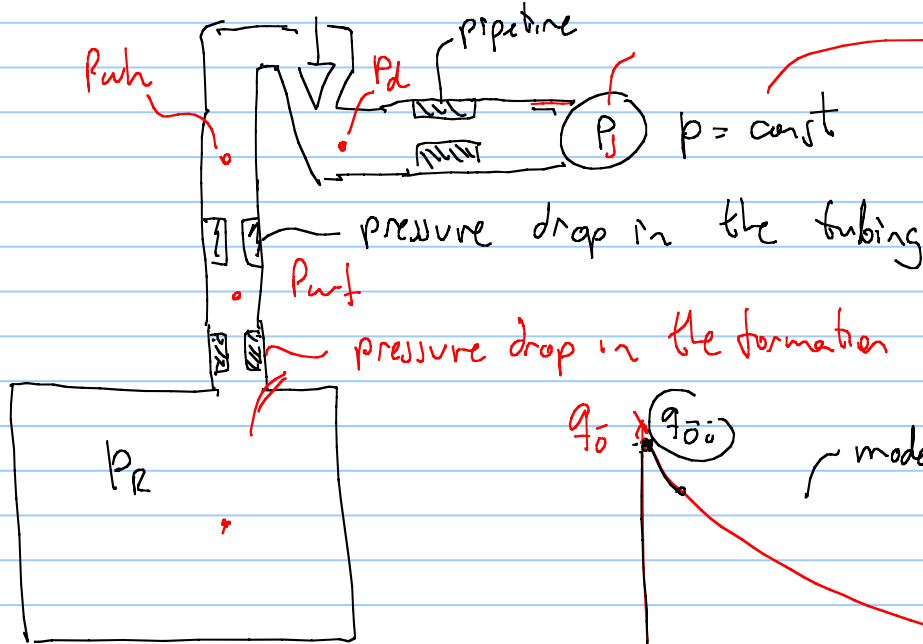
$q_5$   
 $q_0$   
 $\times \text{kg/s h}$   
 $\text{km}^3/\text{h s}$   
 $\text{stb/d}$

flowing bottomhole pressure



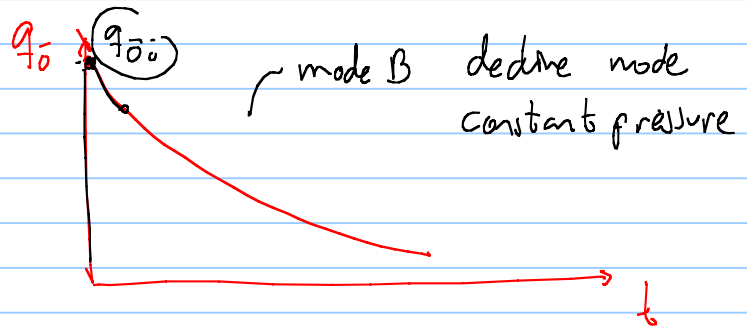
$$v = f(P, T)$$

mechanical analog of my production system



$p = \text{const}$

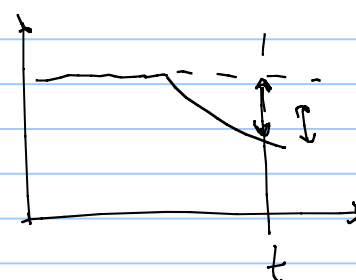
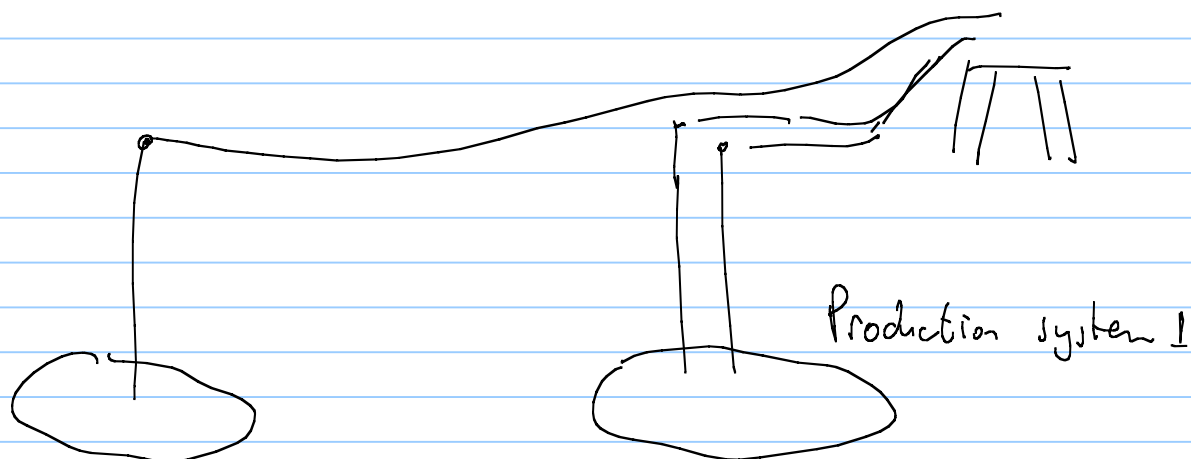
$$\Delta p = P_R - P_{sep}$$



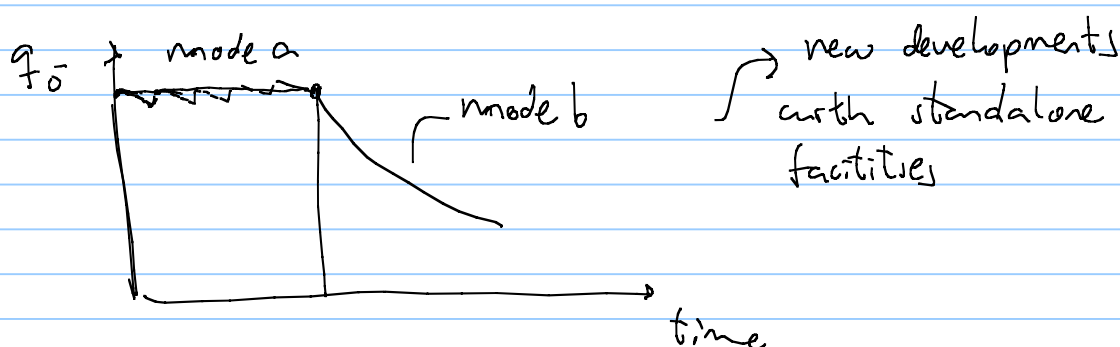
$$q = f(P_R - P_{sep})$$

Satellite field that are tied-back to existing processing facilities

not used for standalone projects.



mode a plateau mode  
constant rate mode



[http://www.ipt.ntnu.no/~stanko/Field\\_Simulator.html](http://www.ipt.ntnu.no/~stanko/Field_Simulator.html)

for fields operating in plateau mode:

a rule of thumb i drain 10% of the <sup>oil</sup> TRR  
total recoverable reserves  
in a year

IOIP(N)

IGIP(G)

TRR = N · RF

G · RF

~ recovery factor

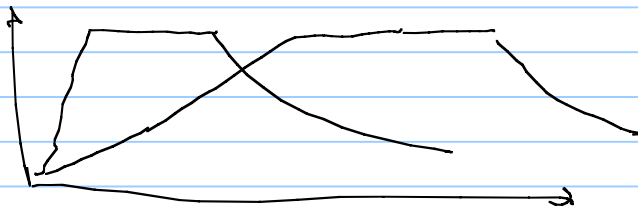
$$q_{\text{plateau rate}} = \frac{M. RF. 0.1}{365} = \text{[stb/d]}$$

for gas 0.03-0.05 per year

page 18 of the compendium

### Onshore

- there are neighboring field of easy access to tie-in production



longer ramp-up than in offshore.

longer appraisal and overlapping with production

- test and verify reservoir communication and structure  $\rightarrow$  use production data to improve reservoir models

- delay the planning of gas and water injection

oil vs gas developments

- transportability  $\sim$  oil  $\rightarrow$  shipped in tank high energy density

price oil > price gas  $\rightarrow$  gas  $\rightarrow$  pipeline  $\rightarrow$  LNG plant

### Offshore development

- short ramp-up
- short appraisal
- Get production as soon as possible to get a healthy cashflow
- Don't acquire much production data to improve my reservoir model
- plan ahead for water and gas injection
- review planning and models "on the go"

- Contract  $\rightarrow$  time, amount, price  $\text{USD}/\text{Sm}^3/\text{d}$ , gas specs  
 $\text{MMScfd}$  } heating value  
 $\text{N}_2, \text{CO}_2, \text{H}_2\text{S}$
- You need to have a buyer, contracts

If using LNG it is necessary to have an LNG infrastructure

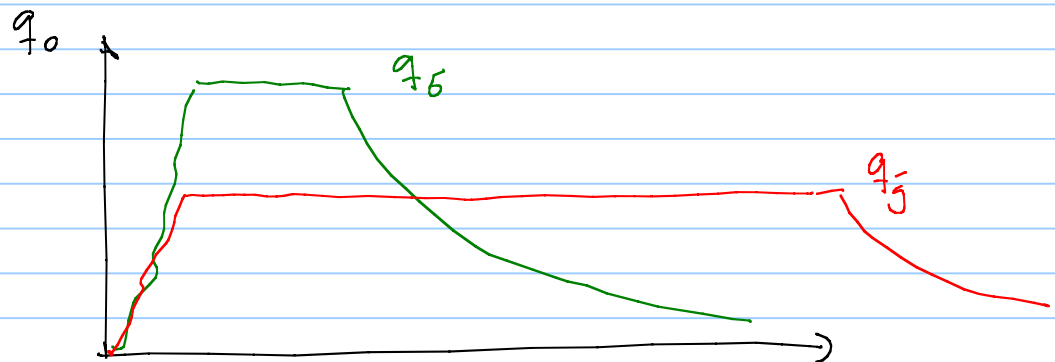
sending LNG facility

Carrier LNG

receiving LNG facility

oil fields have a plateau 2-5 years

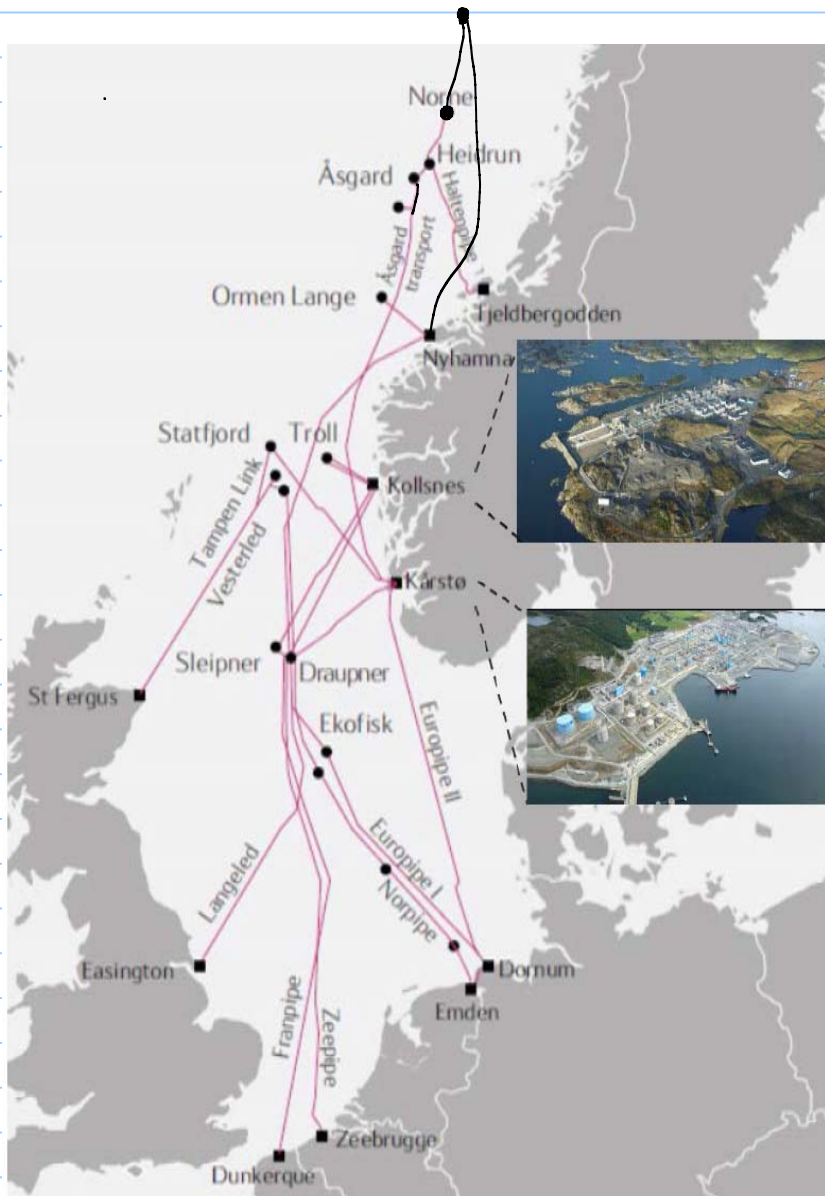
gas fields have a plateau 10-25 years  $\rightarrow$  contracts



• tentative date for first set of exercises : end of next week.

• things that were missing from last class:

for gas developments using a gas distribution network a tariff must be paid (in Norway is Gassco)

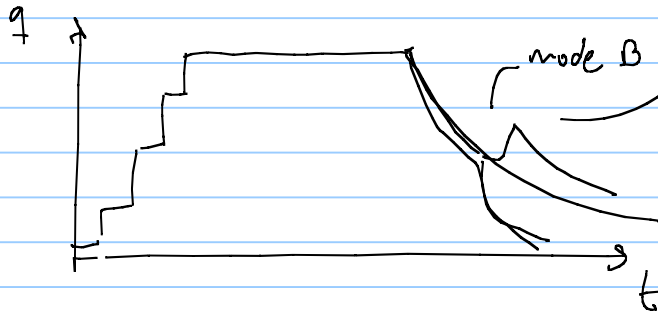


in gas contracts one usually has a : • DCC (daily contract quantity)

• Swing factor (multiplier to DCC) 1.2, 1.3

• penalty clause : how much the producer has to pay if doesn't deliver DCC.

about the production profile



changes in the decline are due to changes in the production system: wellbore collapse, scale in tubing, liquid loading, wax accumulation

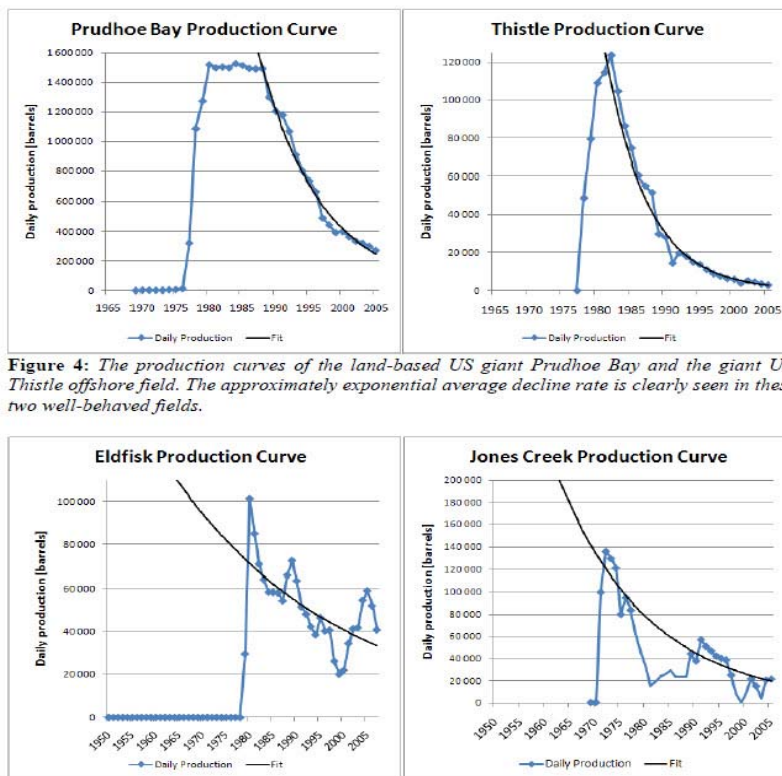
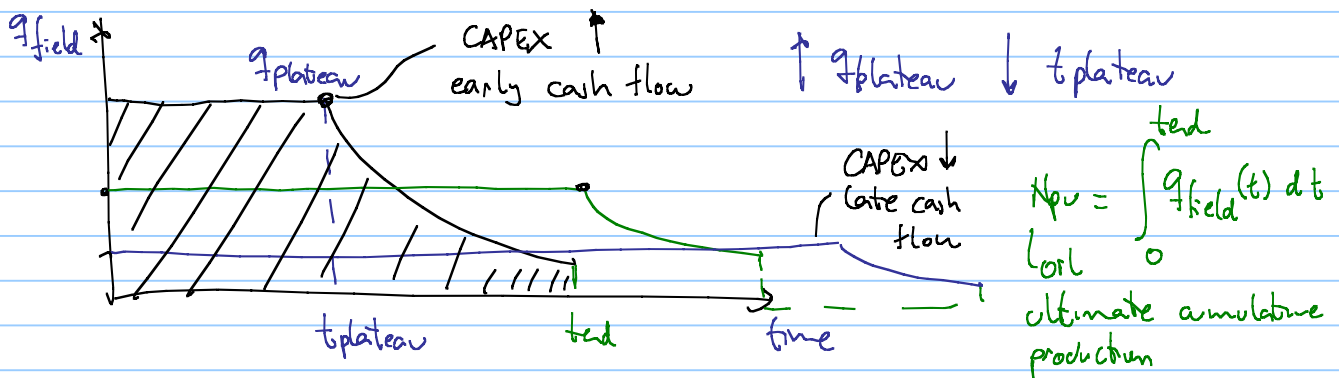


Figure 4: The production curves of the land-based US giant Prudhoe Bay and the giant UK Thistle offshore field. The approximately exponential average decline rate is clearly seen in these two well-behaved fields.

<https://grandemotte.wordpress.com/oil-and-gas-5-production-decline-rates/>

- there is a very close relationship between plateau length and plateau height



how do I decide a proper plateau length? { economical analysis  
max NPV



for a fixed production system.

- height is dictated by physics (engineering)
  - if  $q$  is higher:
    - produce excessive sand
    - erosion
    - damage
  - economics
- length is dictated by physics

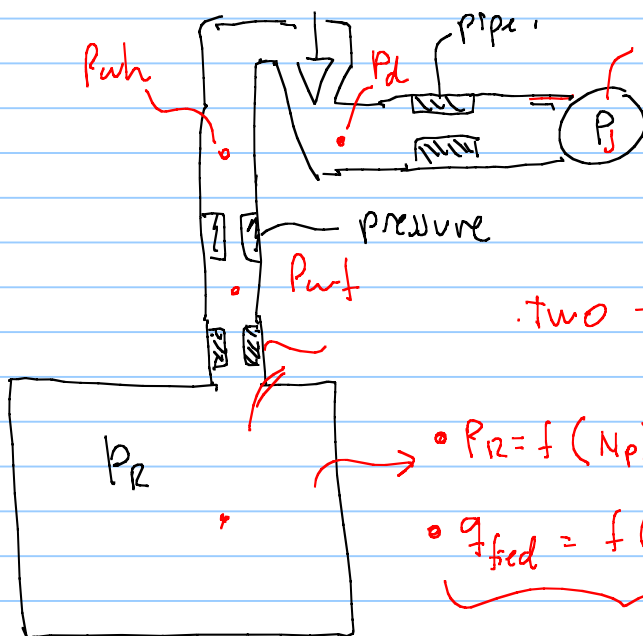
Production is the ONLY SOURCE OF REVENUE IN THE FIELD!

- how to compute production profiles?

$N_p$  oil

$G_p$  gas

$Q_p$  ~ generic



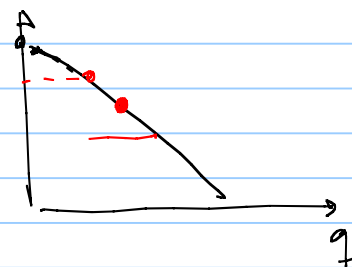
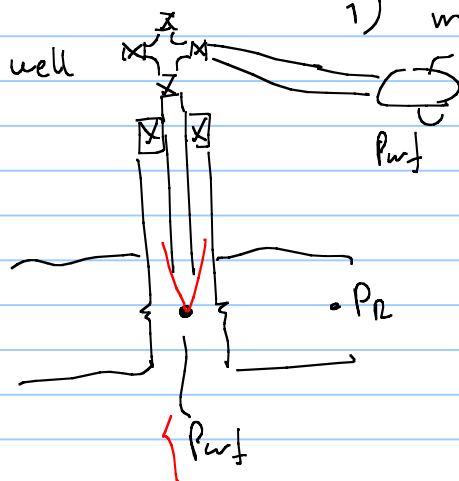
TWO THINGS ARE REQUIRED

- $P_z = f(N_p)$  → static reservoir equation
- $q_{\text{fixed}} = f(P_z, P_s, \text{restrictions})$  → dynamic model

material balance

Inflow performance relationship

1) material balance + IPR equation



how much production will I get from the reservoir if I exert certain  $P_{wf}$

neglects all the system downstream the well bottomhole

??

It is important to use a  $P_{wf}$  that is realistic and that allows the fluid to flow from bottomhole to separator (required  $P_{wf}$ )

- a too high  $P_{wf}$  will give less production and be <sup>too</sup> pessimistic
- a too low  $P_{wf}$  will give more production and be <sup>too</sup> optimistic.

required  $P_{wf}$  usually changes with time  $\nabla$ .  $f(q_{well}) \nabla$

2) Reservoir simulator (mass conservation  
momentum conservation)  $\nabla$

areal distribution of parameters.

$\uparrow$  big uncertainty in the input  $\longrightarrow \uparrow$  big uncertainty in the output

---

Uncertainty quantification and management in the field planning process

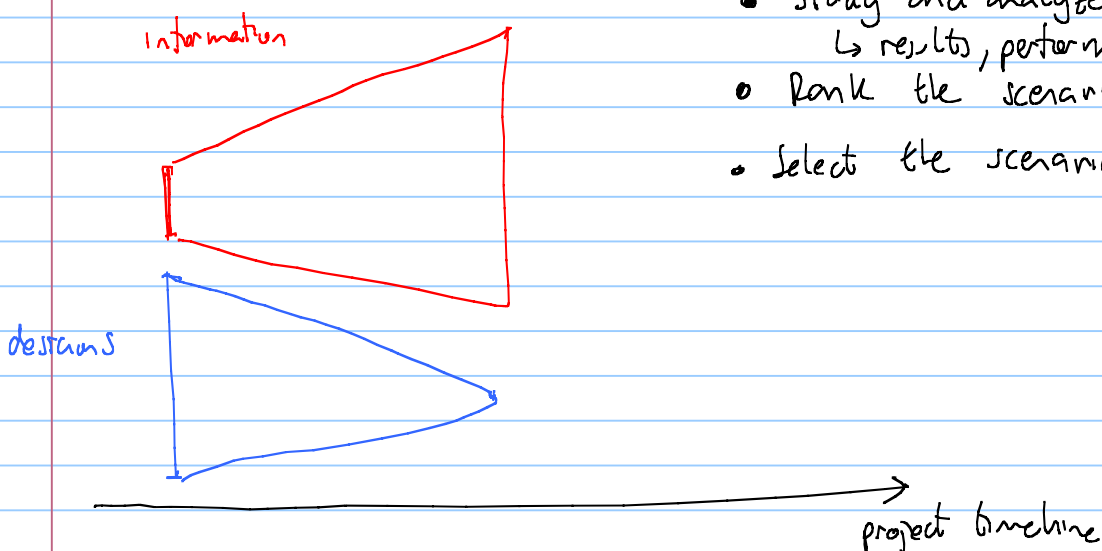
the main tasks of field planning: • Identity field development scenarios

• Perform a pre-design of each scenario

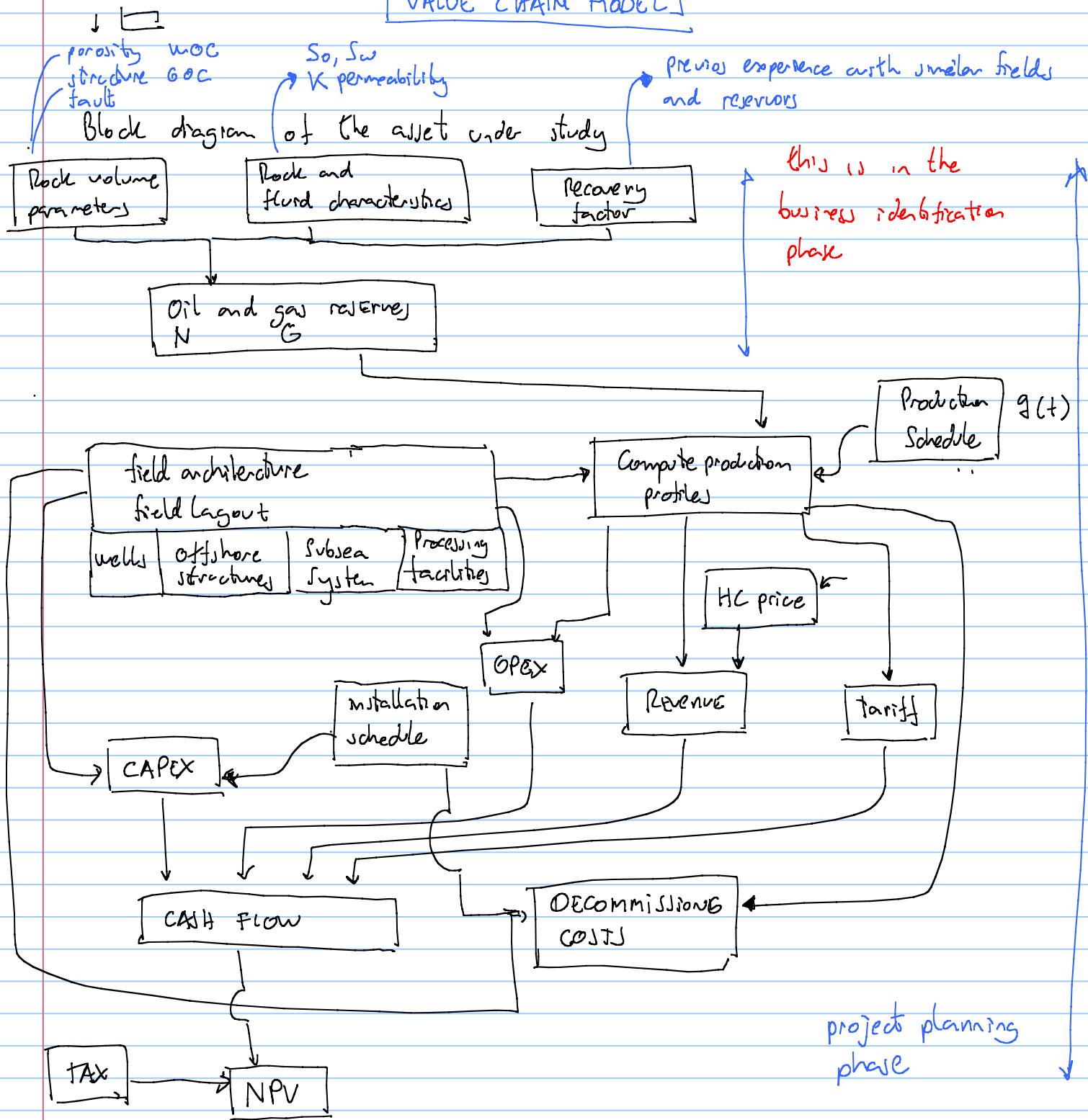
• study and analyze each scenario  
 $\hookrightarrow$  results, performance

• Rank the scenarios using a criteria

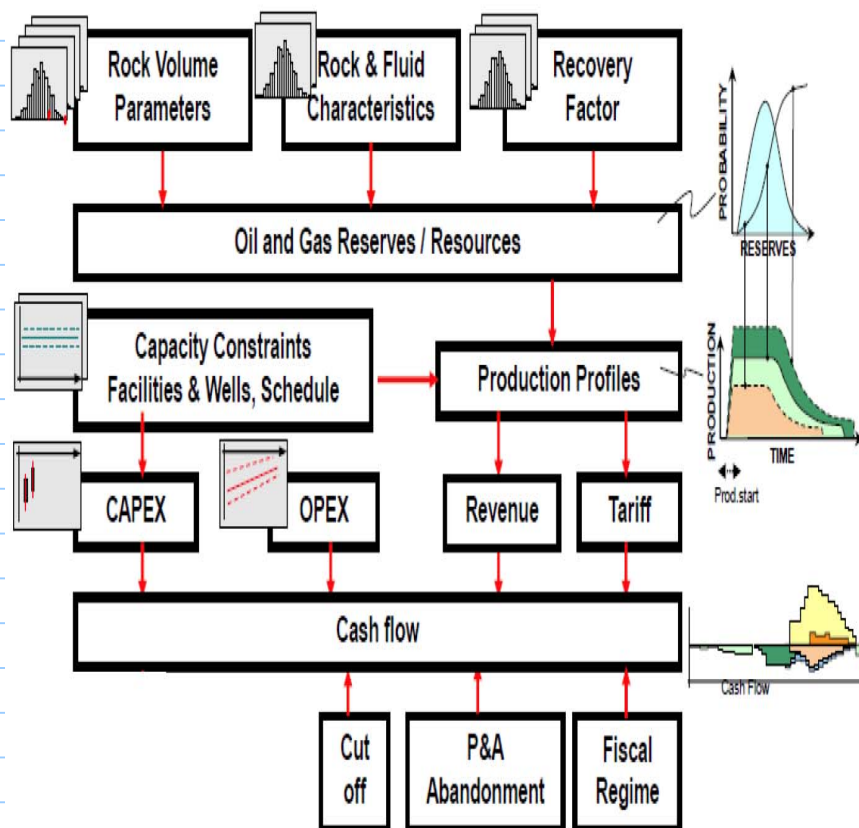
• Select the scenario (Best case)



# VALUE CHAIN MODEL



- there is a team of experts working constantly in every box.
- interdisciplinary :
- geologist
  - geophysicists
  - reservoir engineer
  - offshore engineer
  - accountant, economist
  - drilling engineer
- non technical - petroleum disciplines
- HSE
  - political advisor



## Evaluation criteria

### ① Economic

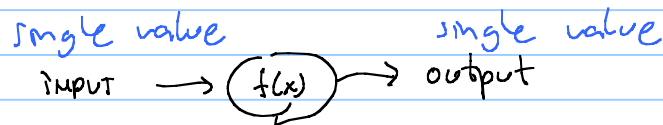
- Cost
- Revenue
- Cash flow investment
- NPV

### Schedule

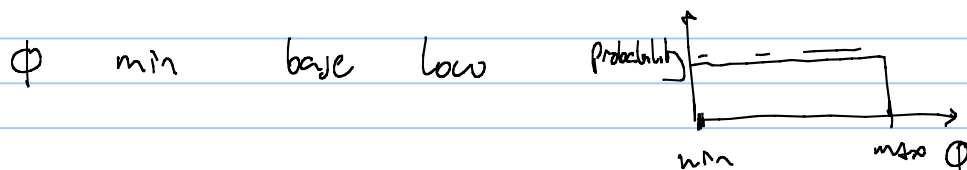
- timeline
- resources
- project management

### Risk

this is not a deterministic process



probabilistic: there is a probabilistic distribution for each input range of values for the input



Probability: chance of occurrence of an event

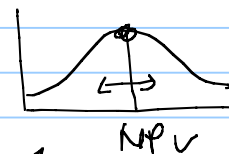
Deterministic: discrete outputs (calculated based on min, mean, max)

cannot guarantee that mean case is the base case

it is very unlikely that the <sup>maximum or</sup> minimum will occur simultaneously for all variables

NPV<sub>min</sub>, NPV<sub>max</sub>, NPV<sub>base</sub>

Probabilistic • full range of possible outcomes

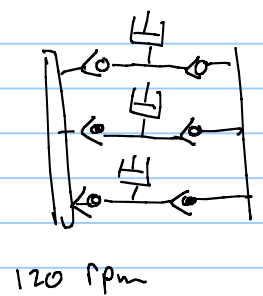
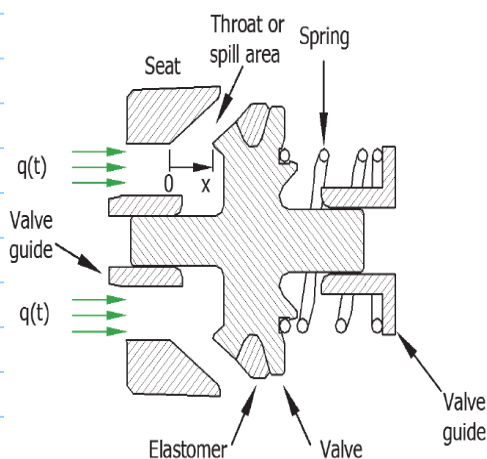
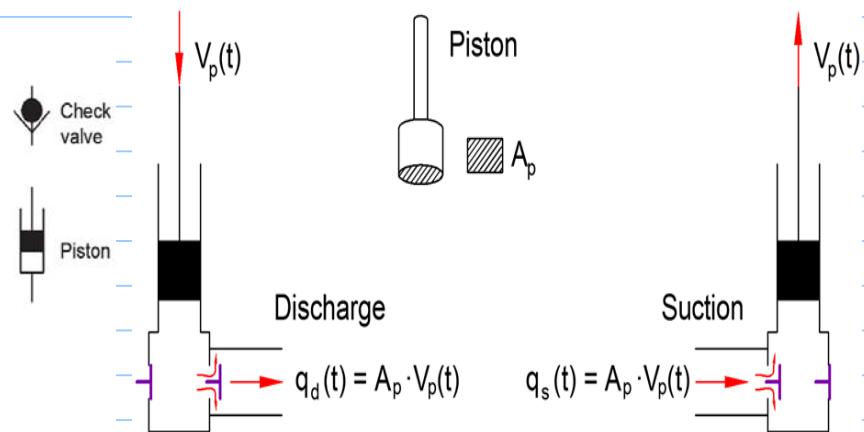
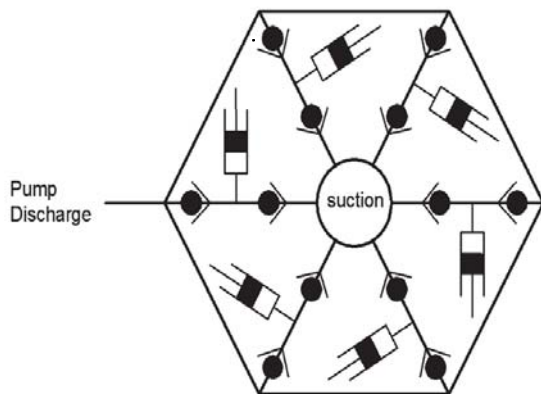
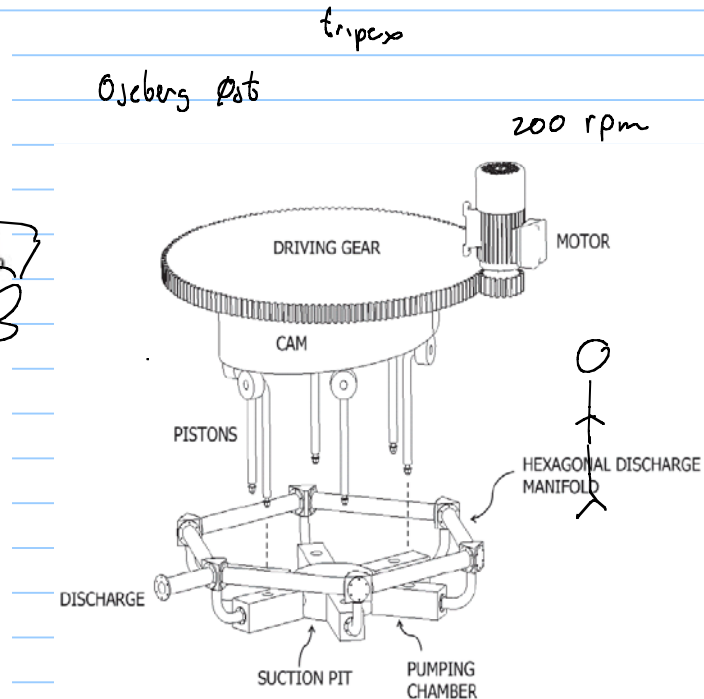
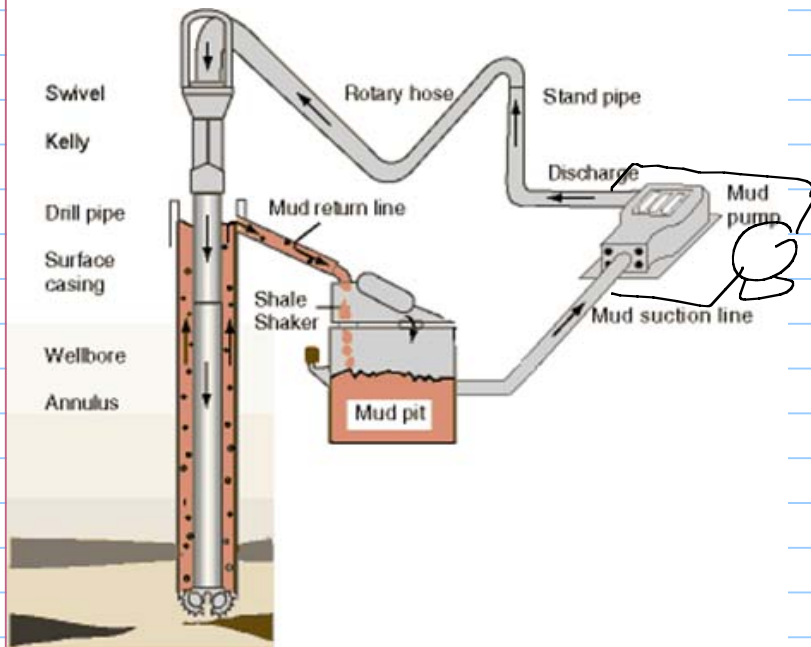


there are several tools to evaluate a project:

- Probability plots
- time plots
- Decision trees
- ternado plots (spider plots)
- summary tables advantages disadvantages
- Qualitative ranking <sup>assigns grade</sup> to a quality

Probability → reserve estimation → probability distribution  
 Monte Carlo

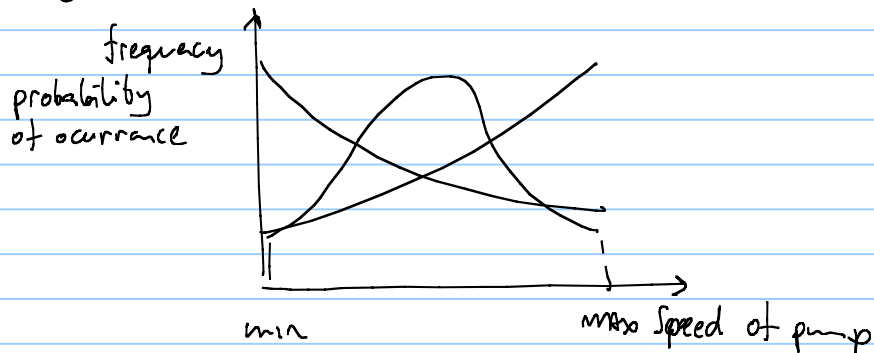
start with an example in excel.



high pump speed  $\leadsto$  high valve failure?



mud logging data every 10s, for



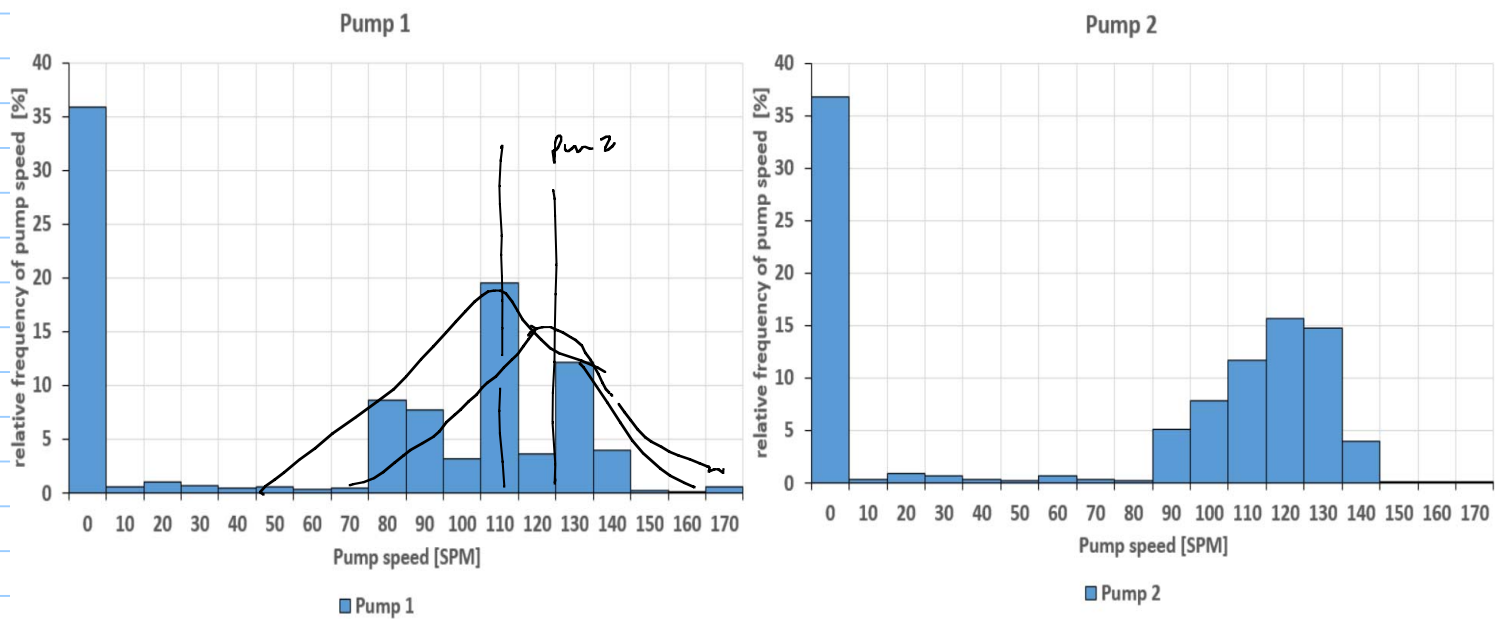
tricks in Excel

-5  
 0  
 <5  
 10 5.1 ≤  
 20 14.999  
 30

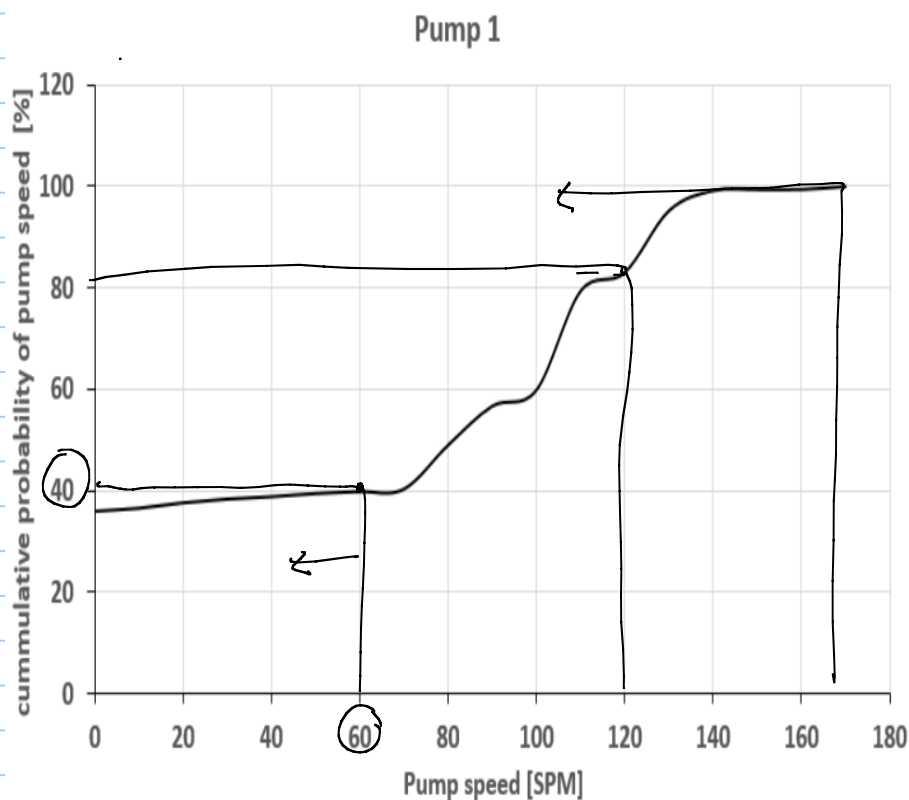
• to send the selection all the way to the end  
press sequentially ctrl+shift+down

• to apply a mathematical function (takes vector and returns vector)

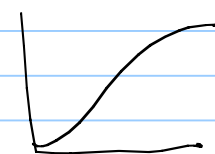
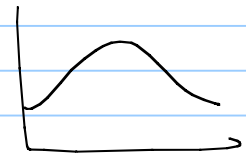
instead of pressing "enter" press ctrl+shift+enter sequentially



relative frequency plots. probability density function pdf  
cumulative probability:



pdf

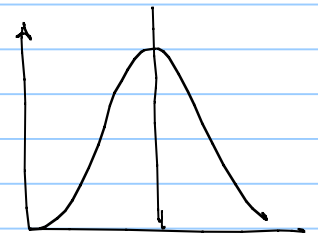


We have worked so far with a discrete distribution. It is possible to use continuous dist. using analytical equation



pdf  $\nearrow$  variable of interest

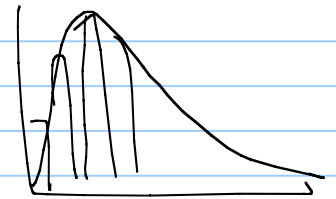
$$f_{\zeta}(\zeta) = \frac{1}{\sigma_{\zeta}\sqrt{2\pi}} \exp \left[ -\left( \frac{\zeta}{\sigma_{\zeta}\sqrt{2}} \right)^2 \right] \sim \text{Gaussian}$$



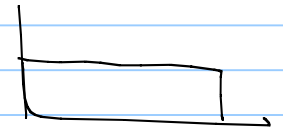
$\nearrow$  variable of interest

$$f_H(H) = \frac{H}{4\sigma_{\zeta}^2} \exp \left[ -\left( \frac{H}{\sigma_{\zeta}\sqrt{8}} \right)^2 \right] \sim \text{Rayleigh distribution}$$

$\nwarrow$  standard deviation



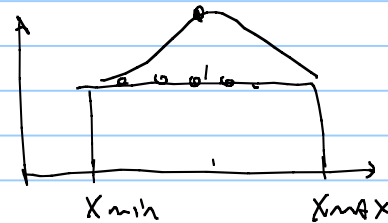
it is possible with discrete data to tune to  
a analytical probability expression



- Reference group:
  - Wilfred, Erca
  - Kjørslevik, Erik Kristoffer Carlsen
  - Mkinga, Oras Joseph

- Uncertainty quantification and management.

for each variable in my field development process it is necessary to determine a probability distribution



Probabilistic estimation of total recoverable reserves

oil	$G$	TRR	$G_{pu}$	ultimate cumulative gas production
gas	$N$		$N_{pu}$	ultimate cumulative oil production

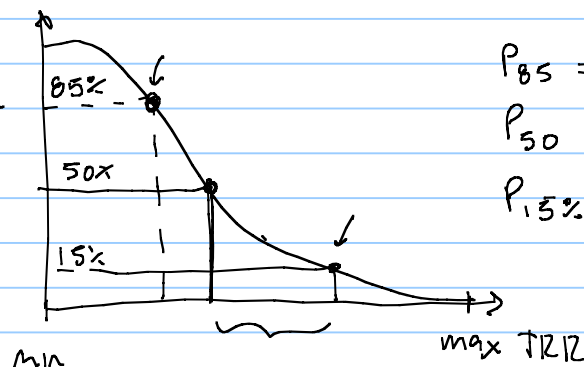
recovery factor  
 $RF, F_{RU} = \frac{N_{pu}}{N}$   
 $= \frac{G_{pu}}{G}$

$\left\{ \begin{array}{l} 20\% \\ 50\% \\ 30\% \end{array} \right.$

$N_{pu} = \int_0^{t_{end}} q_{\frac{1}{2}}(t) dt$

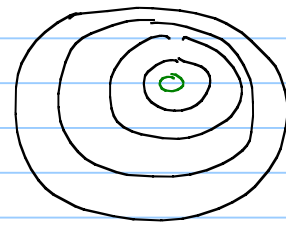
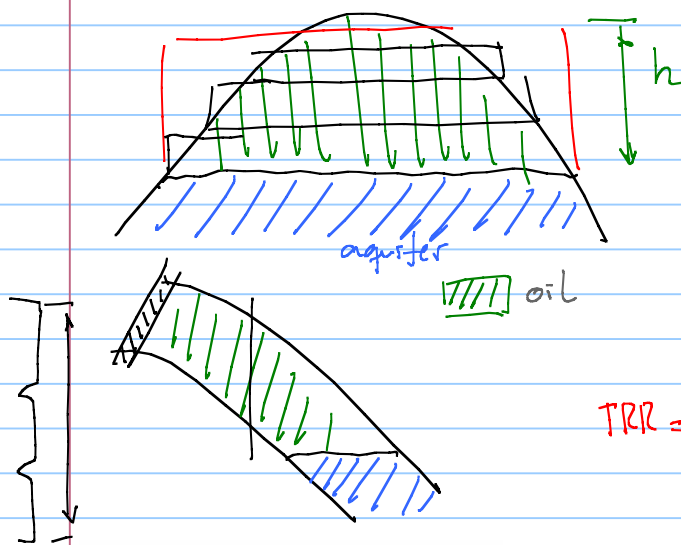
$\left\{ \begin{array}{l} 70-80\% \end{array} \right.$

Desired output  
 cumulative distribution  
 probability  
 TRR



$P_{85} = \text{proven}$   
 $P_{50} = \text{proven} + \text{probable}$   
 $P_{15\%} = \text{proven} + \text{probable} + \text{possible}$

oil reservoir



view from top

$$V_{PR} = h \cdot A$$

$$V_{PR} = \sum_{i=1}^n h_i \cdot A_i$$

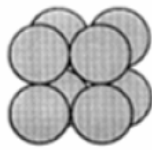
$$\phi = \frac{\text{pore volume}}{\text{total volume}}$$

$$TRR = N_{PO} = \frac{V_{PR} \cdot \phi \cdot (1 - S_w) \left(\frac{N}{G}\right) \cdot F_{Ru}}{B_o}$$

$$B_o = \frac{V}{V_{sc}}$$

$$B_o = \frac{V}{V_{sc}} \left( \frac{P}{P_{sc}} \right)^{1.56} \left( \frac{T}{T_{sc}} \right)^{1.01325}$$

Cubic:



$$\text{Porosity} = \frac{\text{Pore volume}}{\text{Bulk volume}} =$$

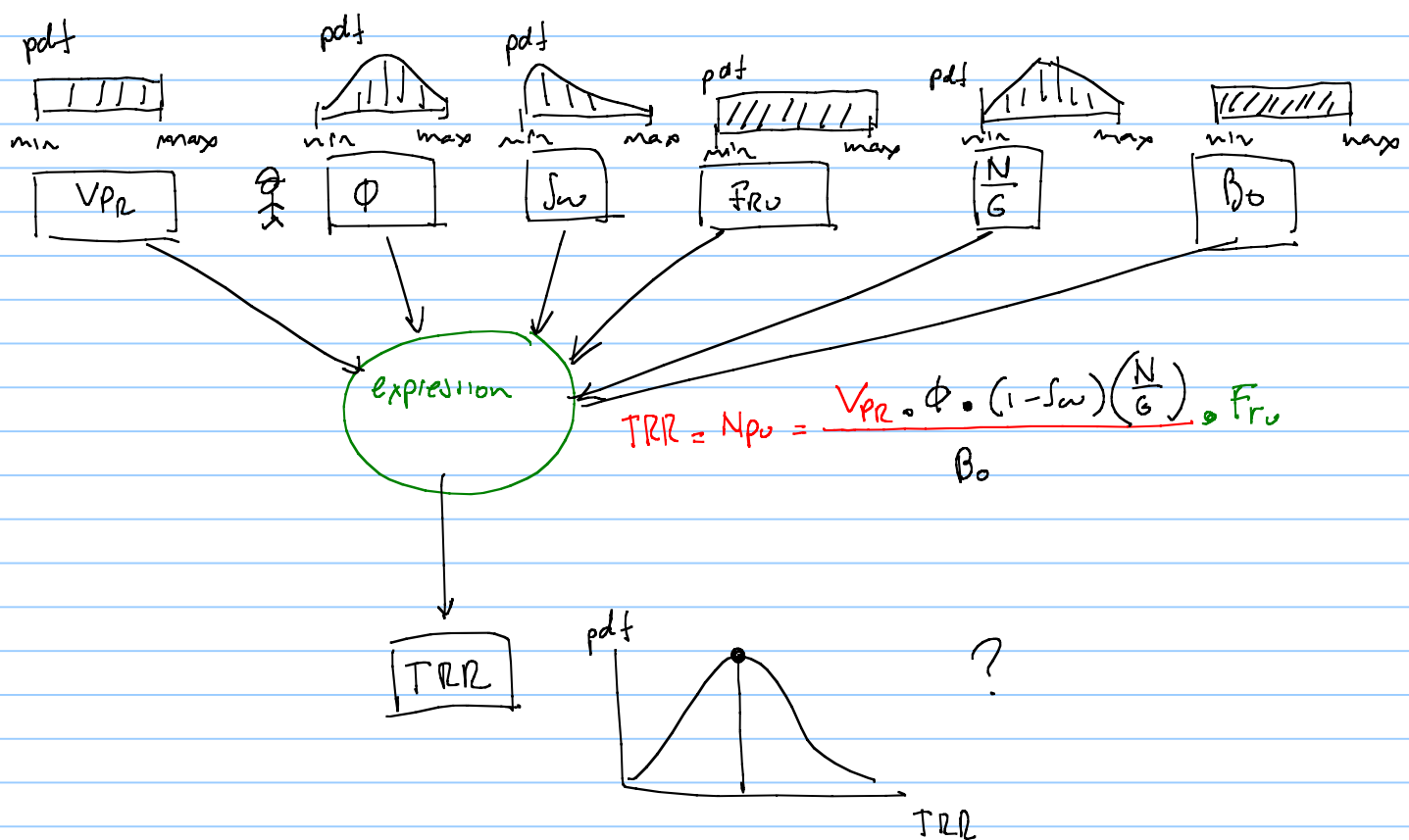
$$B_o = \frac{V}{V_{sc}} \left( \frac{P}{P_{sc}} \right)^{1.56} \left( \frac{T}{T_{sc}} \right)^{1.01325}$$

## Uncertainties in IOIP Estimation

Factor	Typical source of estimate	Approximate range of expected accuracy (%)
Area	drill holes	± 10-20
	geophysical data	± 10-20
	regional geology	± 50-80
	cores	± 5-10
Pay thickness	logs	± 10-20
	drilling time records and samples	± 20-40
	regional geology	± 40-60
Porosity	cores	± 5-10
	logs	± 10-20
	production data	± 10-20
	drill cuttings	± 20-40
	correlations	± 30-50
Interstitial water saturation	capillary pressure data	± 5-15
	oil base cores	± 5-15
	saturation logs	± 10-25
	routine cores with adjustments	± 25-50
Formation volume factor	correlations	± 25-60
	pressure volume temperature analysis of fluid samples	± 5-10
	correlation	± 10-30

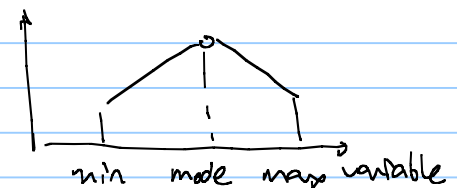
• Recovery factor,  $F_R$  depends on:

- Permeability and Permeability distribution
- Relative permeability characteristics
- Drive mechanism
- Pressure support, displacement and sweep efficiency
- Reservoir architecture-continuity, shape, layering, fault blocks
- Reservoir anisotropy
- Reservoir fluid properties
- Well placement. Number of wells
- Artificial lift
- Minimum economical field rate



for the input variables engineers usually use a <sup>rectangle</sup> uniform distribution or a triangle distribution

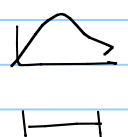
• to obtain the probability distribution of TRR engineers often use the Monte-Carlo method



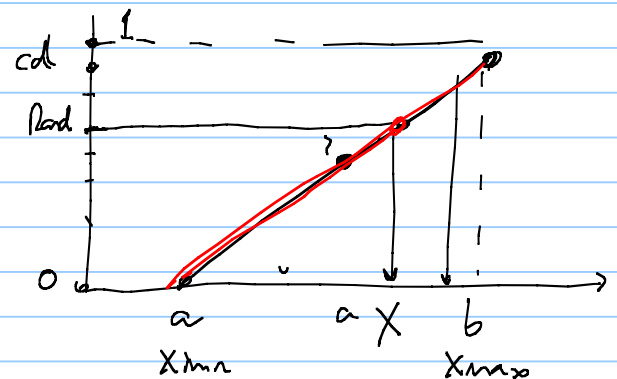
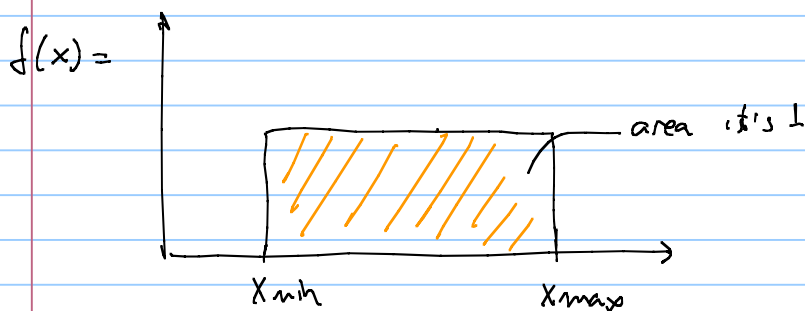
( Stanislaw Ulam, Los Alamos 1940 } Monte-Carlo  
Von-Neuman

- ① • Define a domain of possible values for each input variable propose, find  
a probability  
distribution
- ② • Generate a random input for each variable using its pdf
- ③ • Perform a deterministic calculation using equation  
simulator  
routine } depending on the model available  
compute the value(s) of interest.
- ④ • Repeat step 2. for "many" time. for our case 8000 iterations  
achieved required number of iterations  
Aggregate all results TRN(s) and perform, compute its pdf, cd

the applicability of Monte-Carlo method depends on how long it takes for step 3 to complete

	Rock volume	Porosity	Net to Gros	Oil Saturation	Formation Volume Factor	Ultimate Recovery Factor	
	bbl	fraction	N/G fraction	So=(1-Sw) fraction	Bo Res bbl/STB	Fr fraction	
Min	2000000000	0.18	0.3	0.8	1.35	0.42	
Max	2500000000	0.3	0.5	0.9	1.6	0.65	

uniform distribution



$$\frac{1 - 0}{x_{\max} - x_{\min}} = \frac{Rand - 0}{(X) - x_{\min}}$$

$$X = x_{\min} + (x_{\max} - x_{\min}) Rand$$

we need  
Rand()  
Rand()

			Net to Gros	Oil Saturation	Formation Volume Factor	Ultimate Recovery Factor
	Rock volume	Porosity	N/G	So=(1-Sw)	Bo	Fr
	bbl	fraction	fraction	fraction	Res bbl/STB	fraction
Min	2000000000	0.18	0.3	0.8	1.35	0.42
Max	2500000000	0.3	0.5	0.9	1.6	0.65

$$V_{PR} = V_{PRmin} + Rand_{V_{PR}} (V_{PRmax} - V_{PRmin})$$

	$V_{PR}$ [bbl]	$\phi$ [-]	$N/G$ [-]	$S_o$ [-]	$B_o$ [bbl/STB]	$F_{ro}$ [-]	$TRR$
①	0						0
②							
③							
1							
1							
1							
1							
3000							

we formula

$$TRR = \frac{\phi \cdot V_{PR} (S_o) R_{f/M}}{B_o}$$

compute pdf for this  
cd column

- Usually Monte Carlo is non practical for heavy models (Reservoir Simulator).  
thus another method called Latin Hypercube Sampling is used.

Continuation of the discussion from last class: Probabilistic estimation of reserves

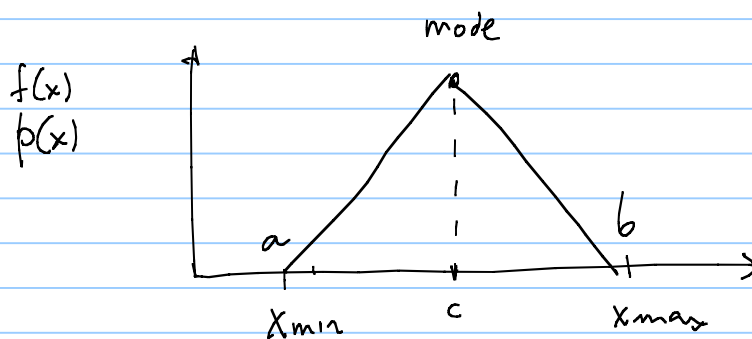
max ↑ P90 the quantity for which there is a 90% probability that the quantities actually recovered will equal or exceed the estimate.

median ↓ P50 the quantity for which there is a 50% probability that the quantities actually recovered will equal or exceed the estimate.

min ↓ P10 the quantity for which there is a 10% probability that the quantities actually recovered will equal or exceed the estimate.

typically triangular or uniform probability distributions are used during early stages of the planning phase.

### triangle distribution



$$0 \leq u \leq 1$$

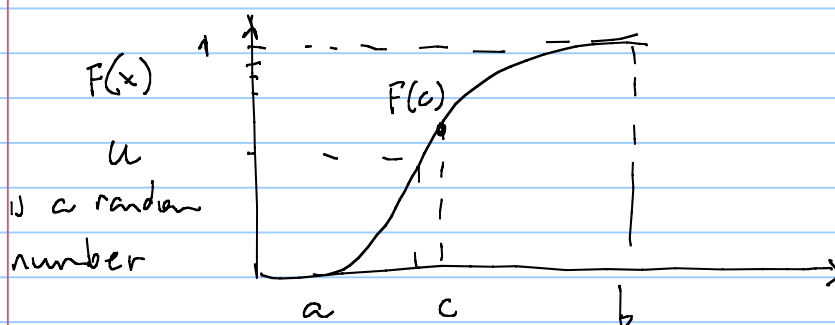
function  $(u, a, b, c)$

for  $0 < u < F(c)$

$$x = a + \sqrt{u(b-a)(c-a)}$$

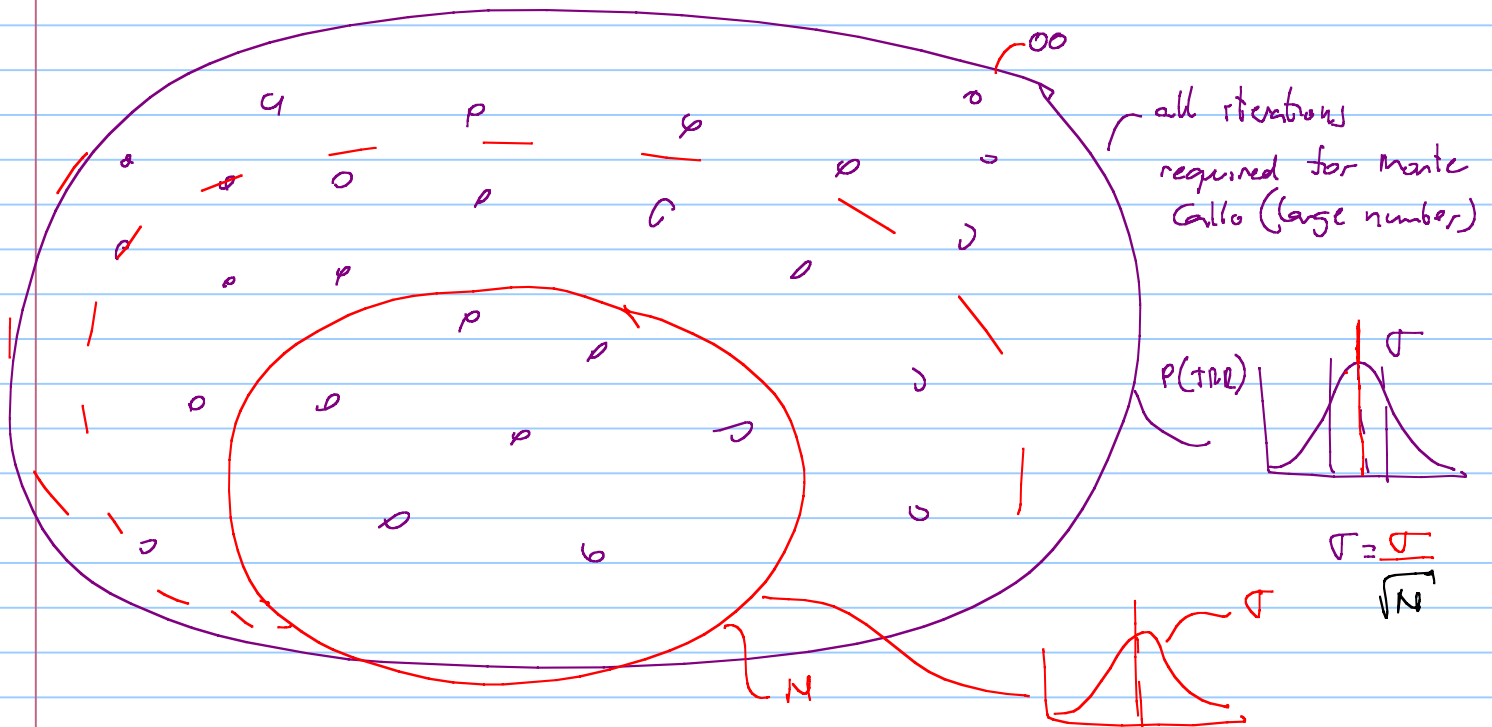
for  $1 > u > F(c)$

$$x = b - \sqrt{(1-u)(b-a)(b-c)}$$



$$F(c) = \frac{(c-a)}{(b-a)}$$

How many iterations are required in Monte-Carlo?



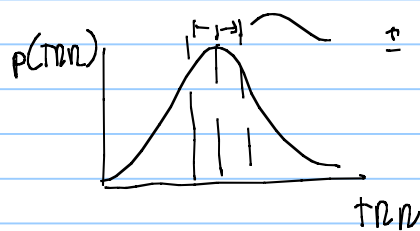
Estimating confidence interval. Estimating number of samples  
number of iterations

$$N = \left( \frac{\frac{\sigma}{\sqrt{N}}}{E} \right)^2$$

confidence level associated with  
the error range

95%, 98%, 99%

$E$  is the desired error of  
the most probable value



$\pm E$  number within  
units  
 $\pm \times$  number of  
std,  $\sigma_n^3$

function in excel

$$Z = \text{NORM.S.INV}(\text{confidence range in fraction})$$

0.95  
0.98  
0.998

$\sigma$  standard deviation of  
the population.

so it is necessary to assume  
an initial number of iterations  
and calculate  $N$ .

$$Z = 3$$

$$N = \left( \frac{3 \sigma}{E} \right)^2 \quad \% \text{ of the average.}$$

2% Average  $\pm$  2% (average)



Some engineers don't estimate beforehand the required number of iterations, just run increasing the number of iterations until the results don't change much

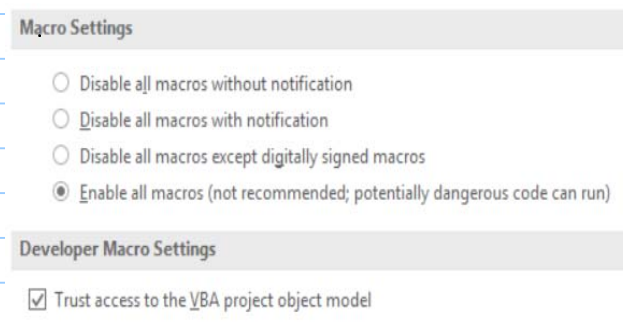
pol  
cd 1%  
0.5%  
3%

## Excel practices in petroleum engineering

### • initial setup:

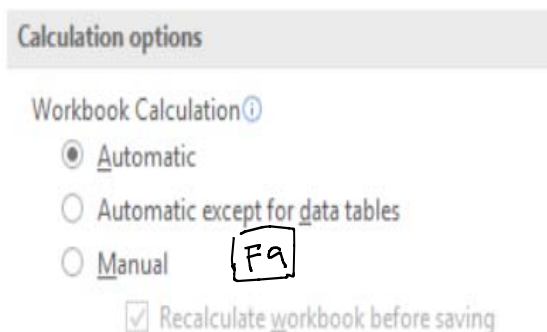
- Reduce macro security: to be able to run macros

options → trust center → macro setting



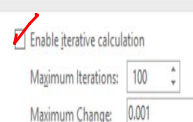
- Automatic cell calculation

options → formula



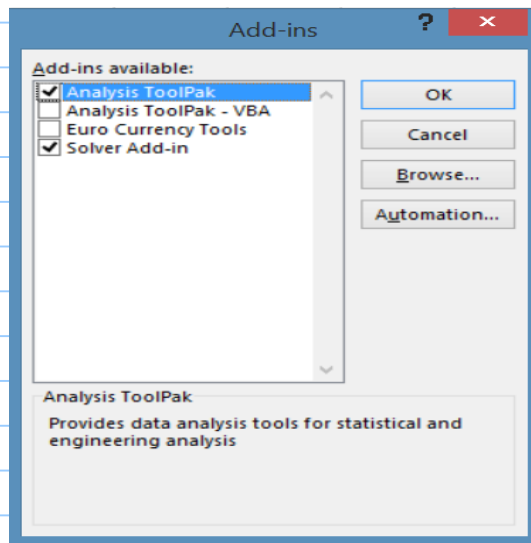
- activate circular references.

general - formula



- Enable solver add-in and analysis toolpack

options → add-in → "go"  
(bottom window)



- Etiquette:

- IO sheet

	A	B	C	D	E	F
1	Milan Stanko, 20170124, Probabilistic estimation of reserves					
2						
3	name	date	title			
4		yyyy-mm-dd				

- Color convention for cell info

Red for user input

blue for calculated cells, in long columns we use black

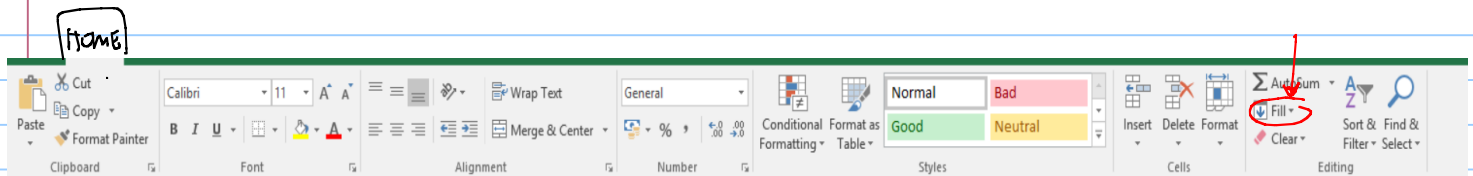
- figures should be in a separate sheet

- for each column: variable name, variable symbol, units in brackets

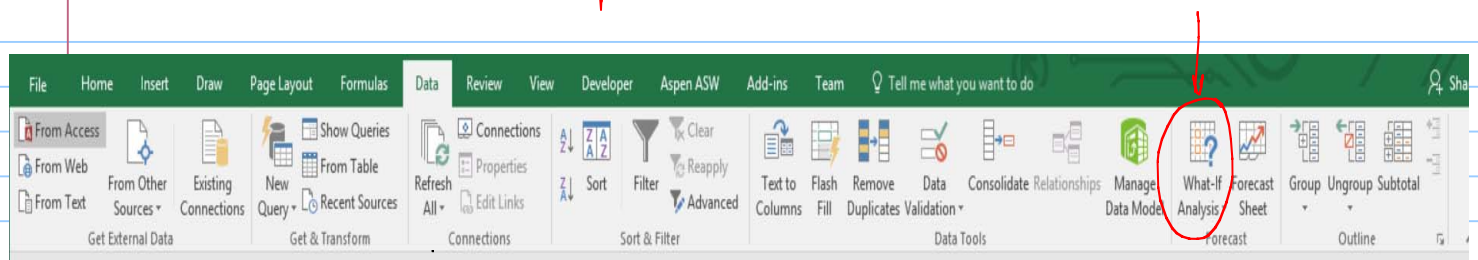
porosity,  $\phi$   
 ↳ [-]  
 ↳ fraction.

- Use common sense imagine that another person will use your excel sheet

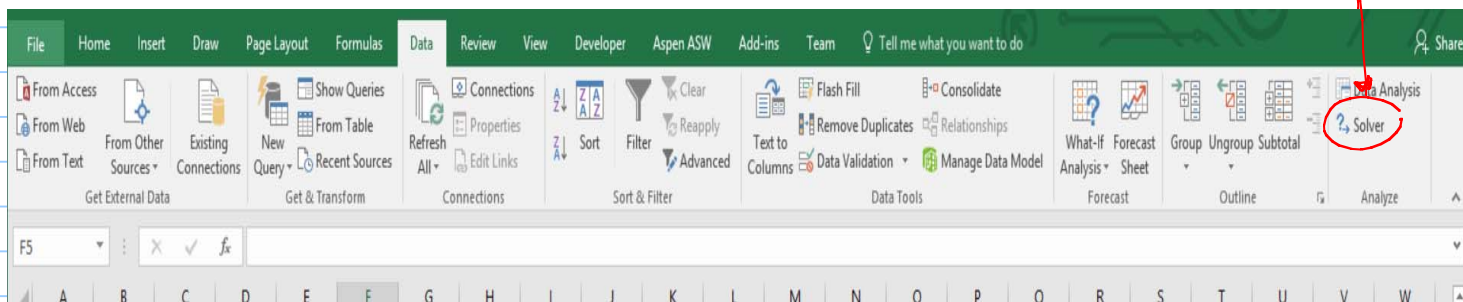
- built functions and utilities → use the upper menu
- fill → apply values to many cell (rows columns)



- Goalseek (solver but simplified)

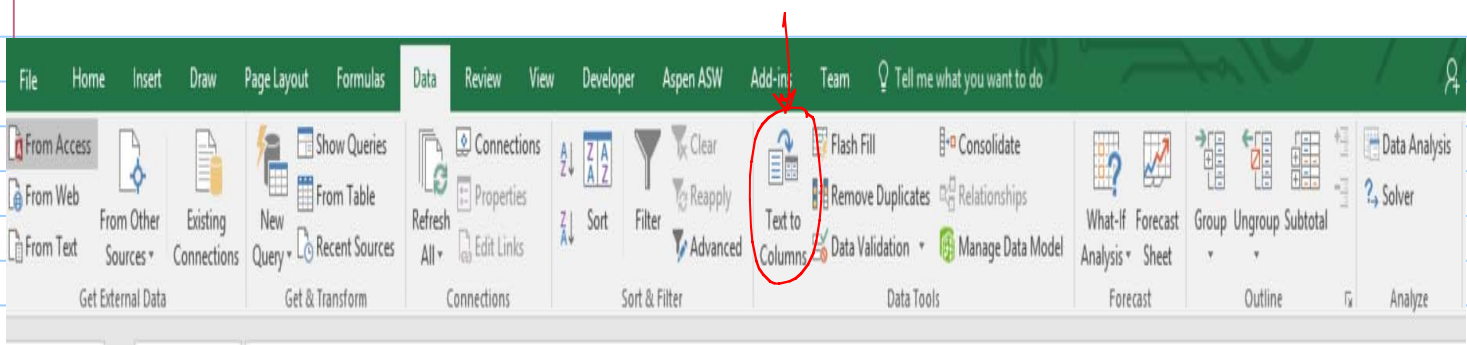


- Solver



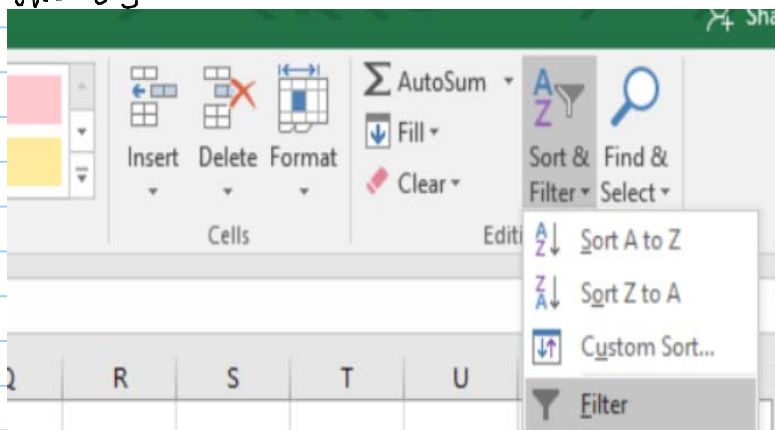
- making frequency table (frequency function) matrixial function  
apply function with data + data + enter.

- Paste text in excel



- Sorting, filtering cells

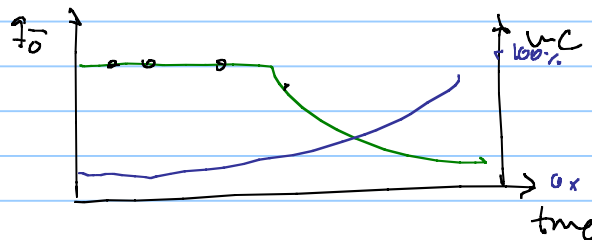
[Home]



## • Plotting

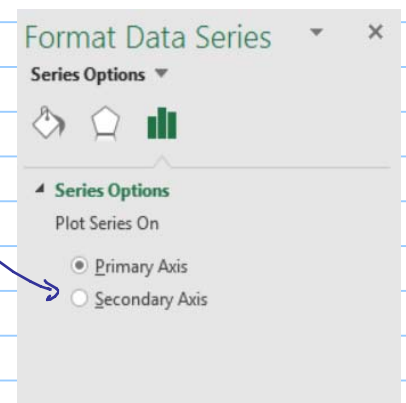
- in its own sheet
- appearance: font size (14-18), bold. Add line data point. point size should be visible (4-6). White background. outside tick marks on the axis, vertical grid. change color on vertical and horizontal axis to black. Adjust data range (min max)

optional to plot another variable that has significantly different values  
secondary vertical axis.



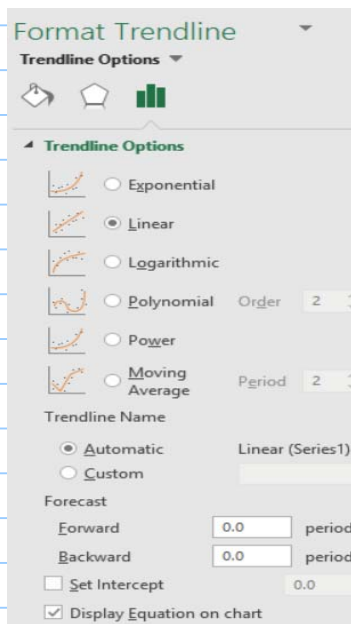
select series right click → properties data series

use log scale when required



- types of plots ~ scatter with lines  
 ↳ bar (no gap between the bars)

- trendline



## • Programming in Excel

• Accessing VBA environment - `Alt + F11`

• UDF — user defined function, Remember to comment  $\rightarrow$  purpose  
 ↳ input, units  
 ↳ clarify an action if necessary  
 ↳ apostrophe before  
 \_ \_ \_

## • Key shortcuts

ctrl + shift + enter apply matrix functions

ctrl + shift + down / up  
 right / left brings to the end of the column, row

## CLASS EXERCISE

• in Windows there are two options to save the file :

1997-2003 excel file .xls  $\left\{ \begin{array}{l} \text{save both the} \\ \text{sheet and} \\ \text{the macro} \end{array} \right.$

if you want to use the latest format then

$\rightarrow$  .xlsx  $\sim$  only sheets

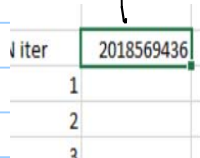
.xlsm  $\sim$  sheets + macro

$X_{uniform}(\$B\$5, B6)$

freeze n column  
 freeze n row

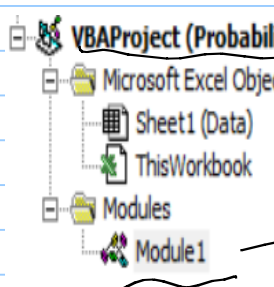
two extra tricks  $\rightarrow$  fill: to fill n iter column from 1-1000 and double

click on the right bottom corner to apply automatically until the end



Observations / sources of error:

- Some computers use ; for separator in function arguments  
 $f(a, b, c)$  or  $f(a; b; c)$  be careful!
- in computers with norwegian language rand() is frlfteldig()
- Once you create the UDF, save it!
- module 1 should be located in the excel sheet where you are working



your excel file

this is where your macro should be

random has a volatile behavior any change a new number will be generated

if after some iterations the value doesn't change, I recommend  
 to put rand inside vba function

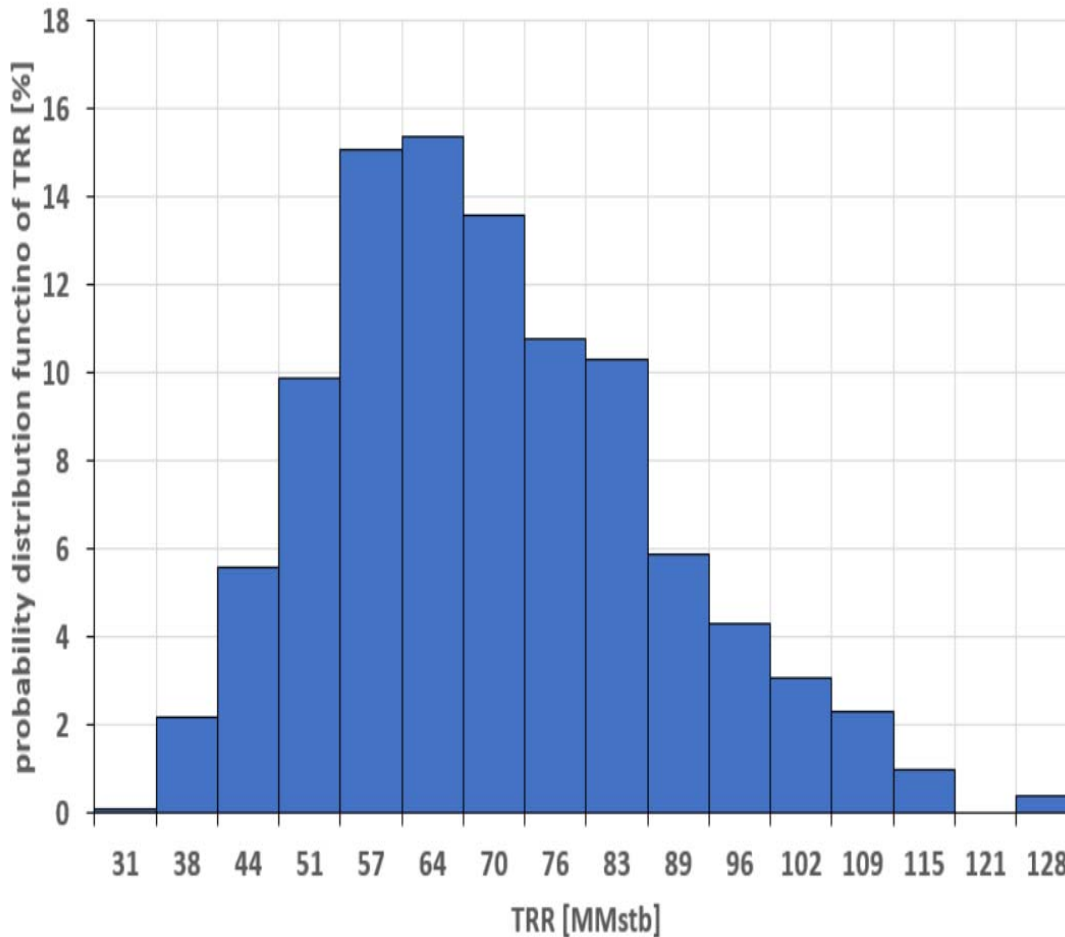
Function X\_uniform(a, b) ·  
 'value of the variable X for a uniform probability distribution  
 'a is the minimum value of X  
 'b is the maximum value of X  
 Application.volatile(true)  
 U=Rnd()  
 $X_{\text{uniform}} = a + (b - a) * U$   
 End Function

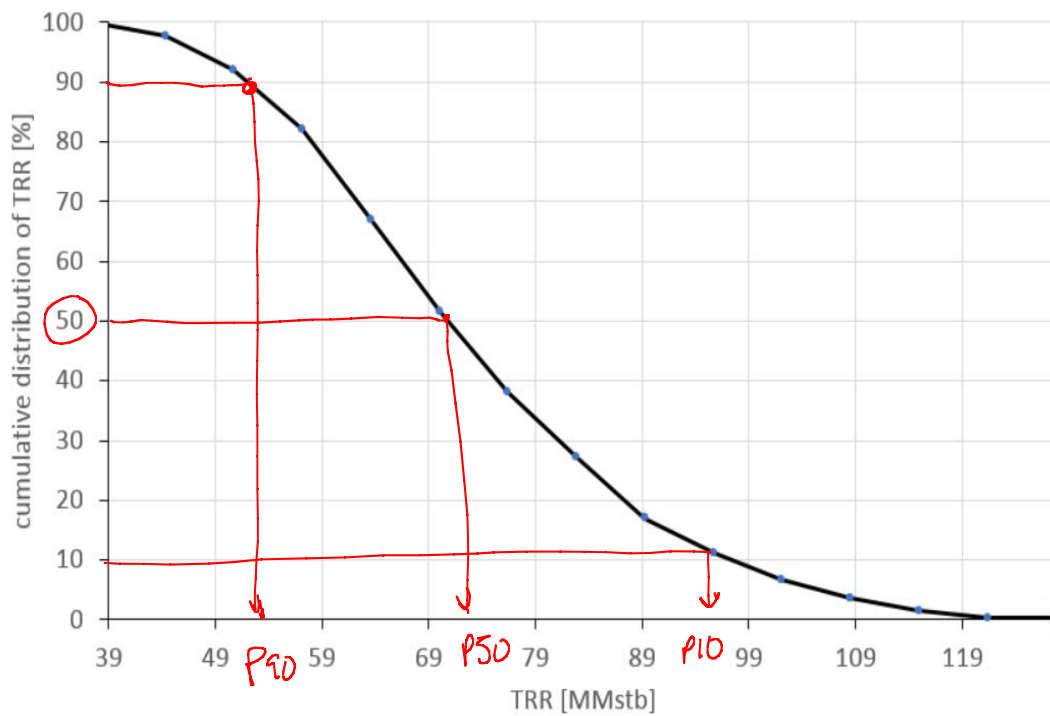
TRR	count	relative freq	cumulative freq
[MMstb]		%	{%}
31	1	0.1	100
38	22	2.2	99.9
44	56	5.6	97.7
y <sub>1</sub> 51	99	9.9	x <sub>1</sub> 92.1
y <sub>2</sub> 57	151	15.1	x <sub>2</sub> 82.2
64	154	15.4	67.1
70	136	13.6	51.7
76	108	10.8	38.1

p90

$\sim 90\% \quad x_3 \rightarrow y_3$

$$\frac{y_2 - y_1}{x_2 - x_1} \approx \frac{y_2 - y_3}{x_2 - x_3}$$





$$N = \left( \frac{z \cdot \sigma}{E} \right)^2$$

sigma	[MMStb]	17
average	[MMStb]	66
E (2% of average)	[MMStb]	1
Z factor (for 98% confidence)		2
Required N		693

σ (Popul)

~ Average (Col)

2 ~ 99.9%

2% of the average

$$\frac{2\sigma - \text{Average}}{100} = E$$



for more detailed economical calculations → Petroleum Economics Tryave-Strøm (TPG5110)

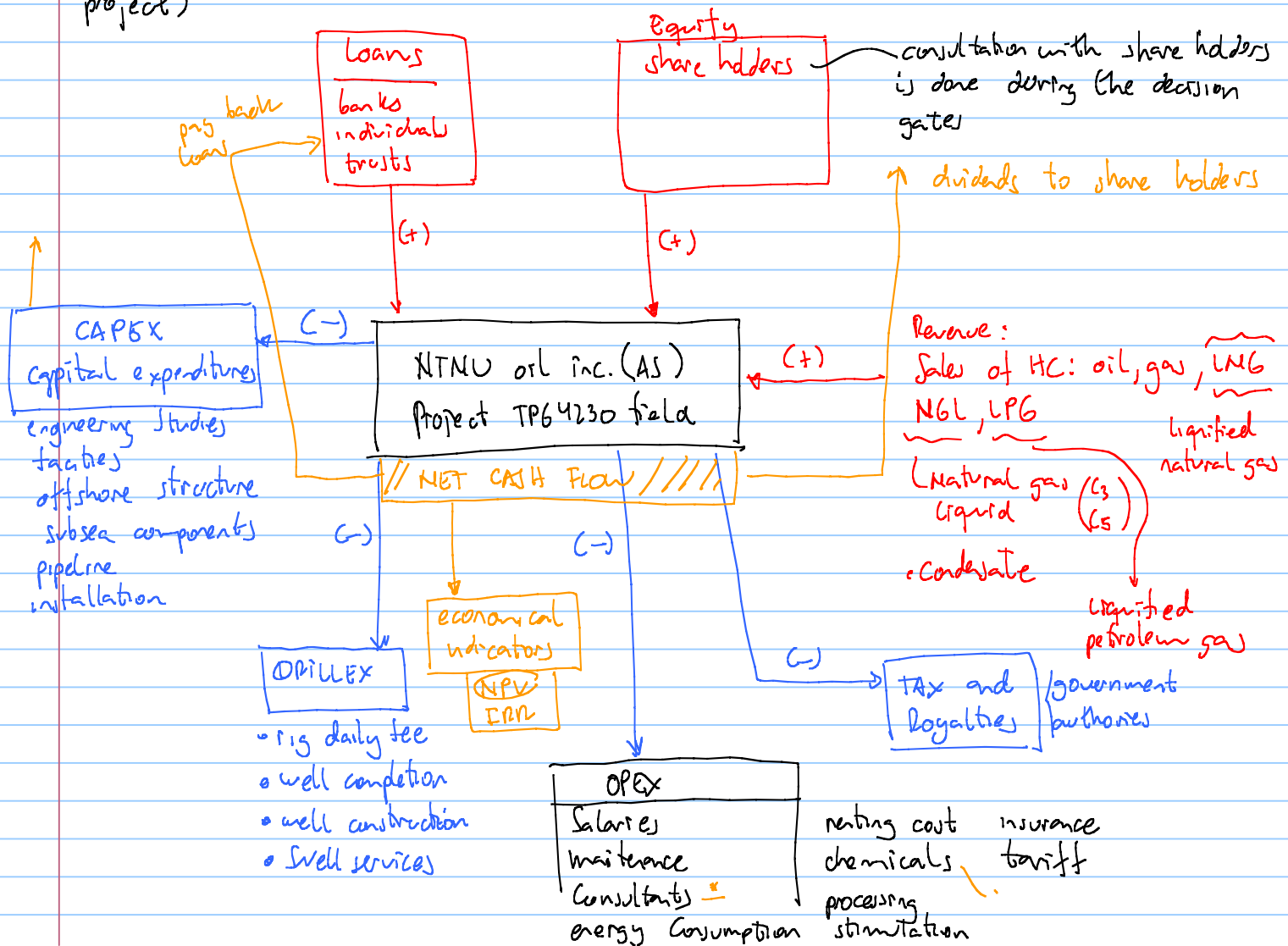
TRR [MMstb]	count	relative freq %
31	1	0.1
38	22	2.2
44	56	5.6
51	99	9.9
57	151	15.1
64	154	15.4
70	136	13.6
76	108	10.8
83	103	10.3
89	59	5.9
96	43	4.3
102	31	3.1
109	23	2.3
115	10	1
121	0	0
128	4	0.4

if I sum from bottom up

} probability that my TRR is equal or lower than 51

← probability that my TRR is equal or higher than

Cash flow and economic indicators of the project (Fried development project)



Cash flow with time

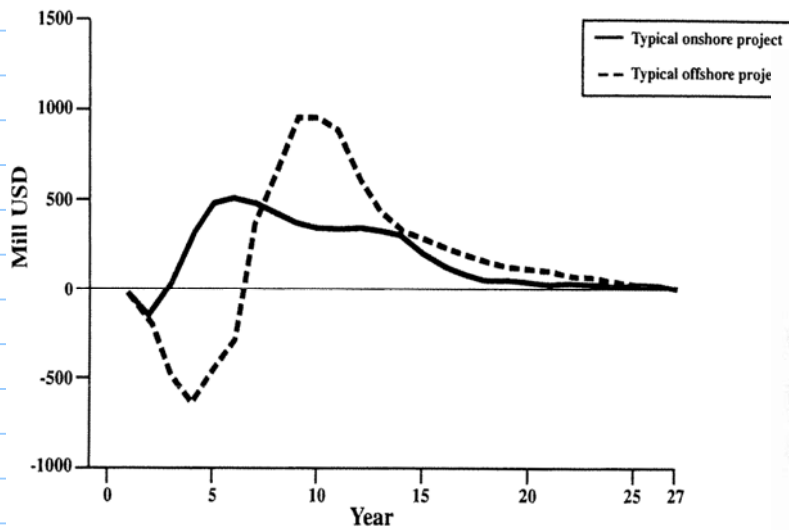
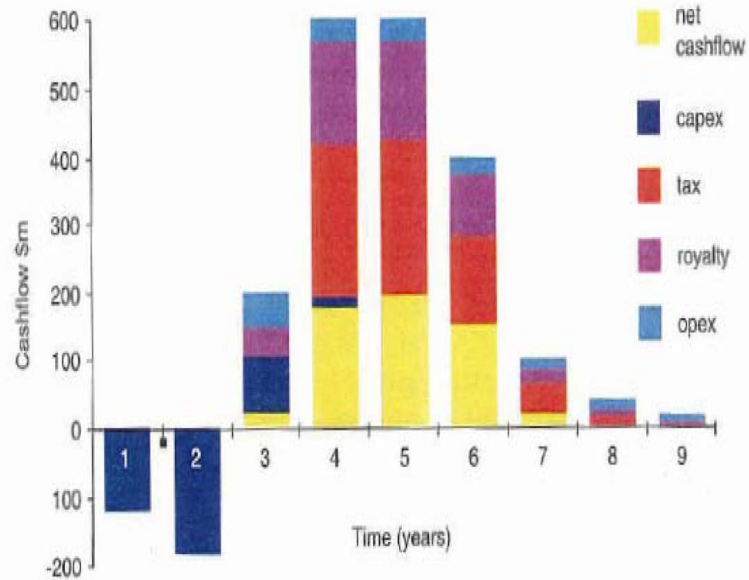


Fig. 9. Typical before tax cash flow profiles for offshore and onshore projects.



Cash flow is calculated on a yearly basis.

060

Year	CAPEX	OPEX	ORILLEX	TAX AND ROYALTIES	EXPENSES	Revenue	Cash flow	PV of cashflow
{0}	-	0	-	0	-	0	-	
1	-	0	-	0	-	0	-	
2	0	-	0	-	-	+	+	
3	0	-	0	-	-	+	+	

Present value: the current worth of a future sum of money

Present value

future value

$$V_p = V_f$$

$$\frac{1}{(1+i)^n}$$

interest, discount rate ~

(1+i) compound factor

$\left(\frac{1}{1+i}\right)$  ~ discount factor

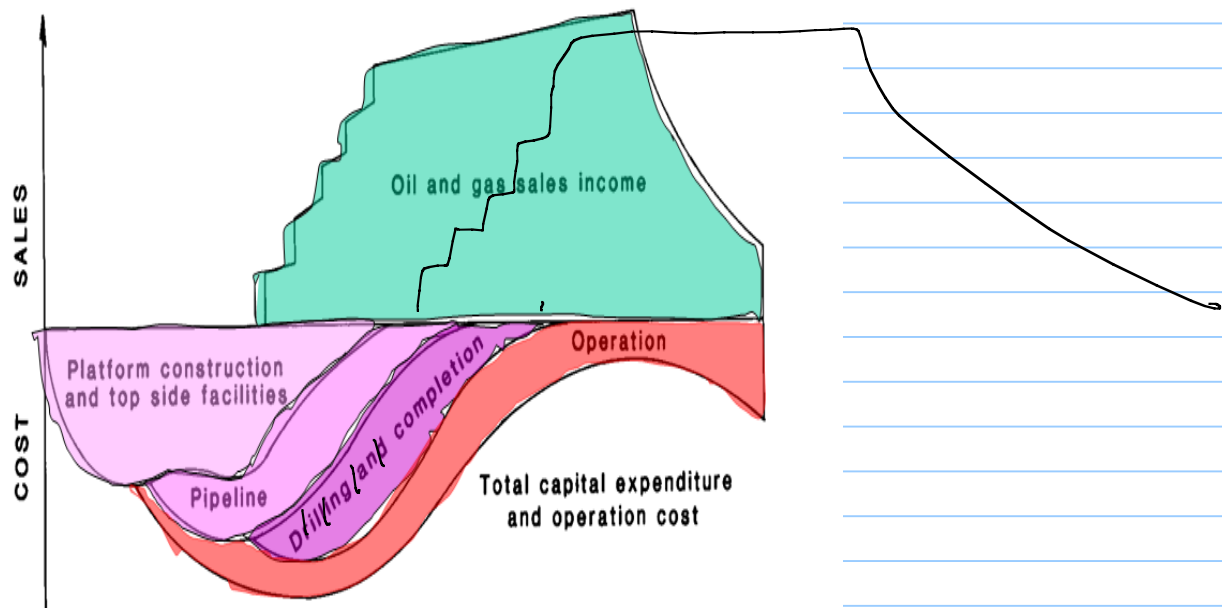
is the year were the future value is spent or gained

main economical indicator of the project

Net present value

has to be (+)

# Revenue and Cost Profiles



## The Ultimate driver in E&P operations

*total number of years*

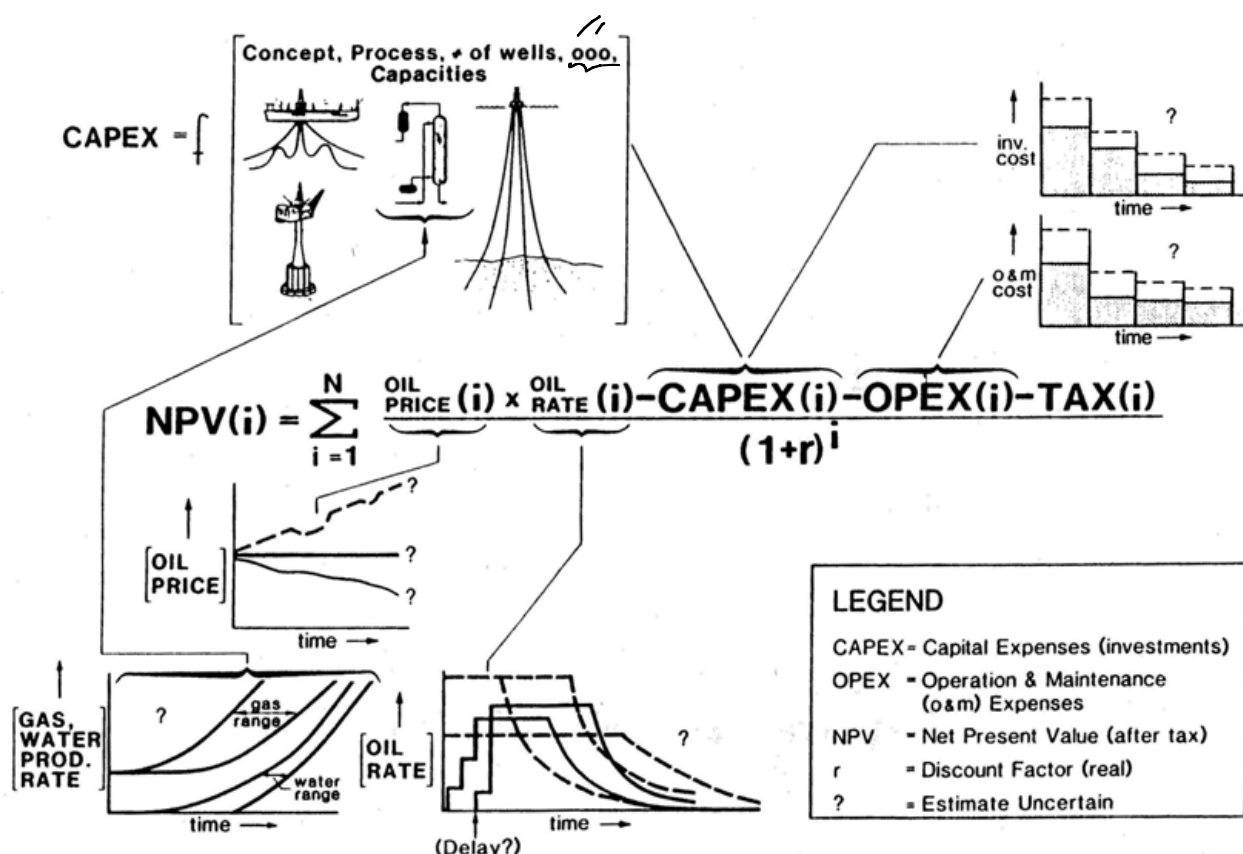
$$NPV = \sum_{i=0}^N \frac{\text{OIL PRICE}(i) \times \text{OIL PROD}(i) + \text{gas prod}(i) \times \text{gas price}(i) - \text{CAPEX}(i) - \text{OPEX}(i) - \text{TAX}(i)}{(1+r)^i}$$

*year*

*interest, discount rate*

*neglected in this course*

## What can we control?



to get accurate estimates of cost values (and production rates) we need the input from the following specialists:

petroleum engineer : Reserves, location and nr wells,  
production scheduling, fluids

Drilling engineer : Drilling and completion costs (OILLEX)

facilities engineer: production processing facilities  
(processing) equipment required.  
transportation

size cost

operations and maintenance : maintenance costs, manpower requirements

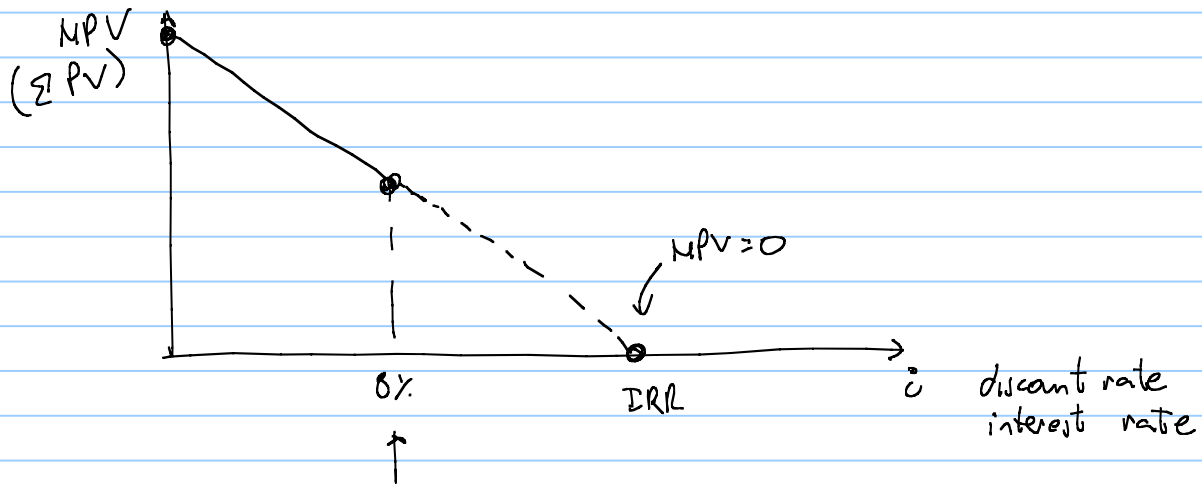
Offshore engineer : offshore structure, layout of the system

Project manager. tax, royalties

Human resources; Fiscal system expert, corporate planner

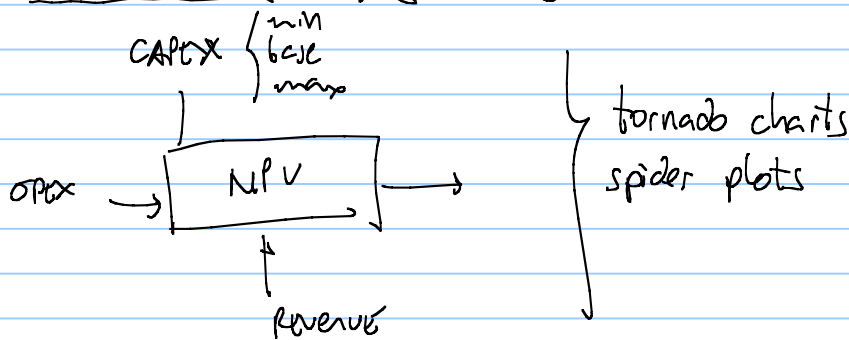
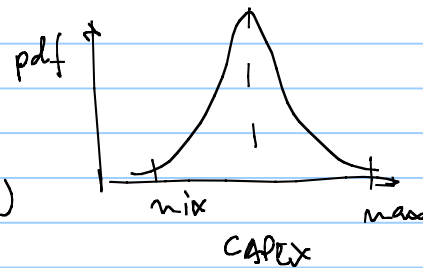
Another indicator of economical health of the project. IRR

internal rate of return: the interest rate that makes the project  $NPV = 0$



how do we quantify the effect of uncertainty in the NPV?

Sensitivity studies using the principle of "Ceteris Paribus"  $\rightarrow$  (all others same)

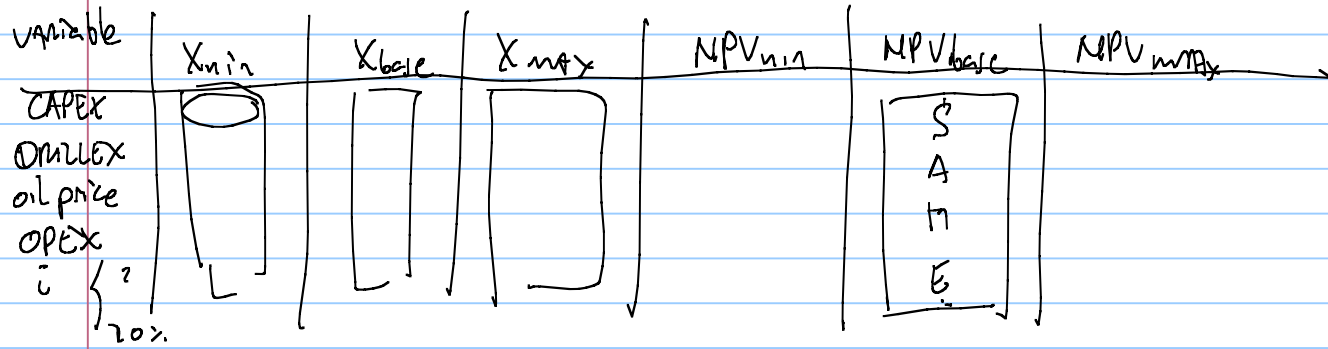


- ① Define a base case scenario base value for  $\left\{ \begin{array}{l} \text{oil price} \\ \text{CAPEX} \\ \text{opex, etc} \end{array} \right.$
- ② Define a range for each variable. E.g. oil price  $\left\{ \begin{array}{l} \text{min} \\ \text{base} \\ \text{max} \end{array} \right.$
- ③ Calculate value of interest (economic indicator NPV) changing (one at a time) the variables (while keeping all other variables at their base value)

min price  $\rightarrow$  calculate NPV

base oil price  $\rightarrow$  NPV

max oil price  $\rightarrow$  NPV



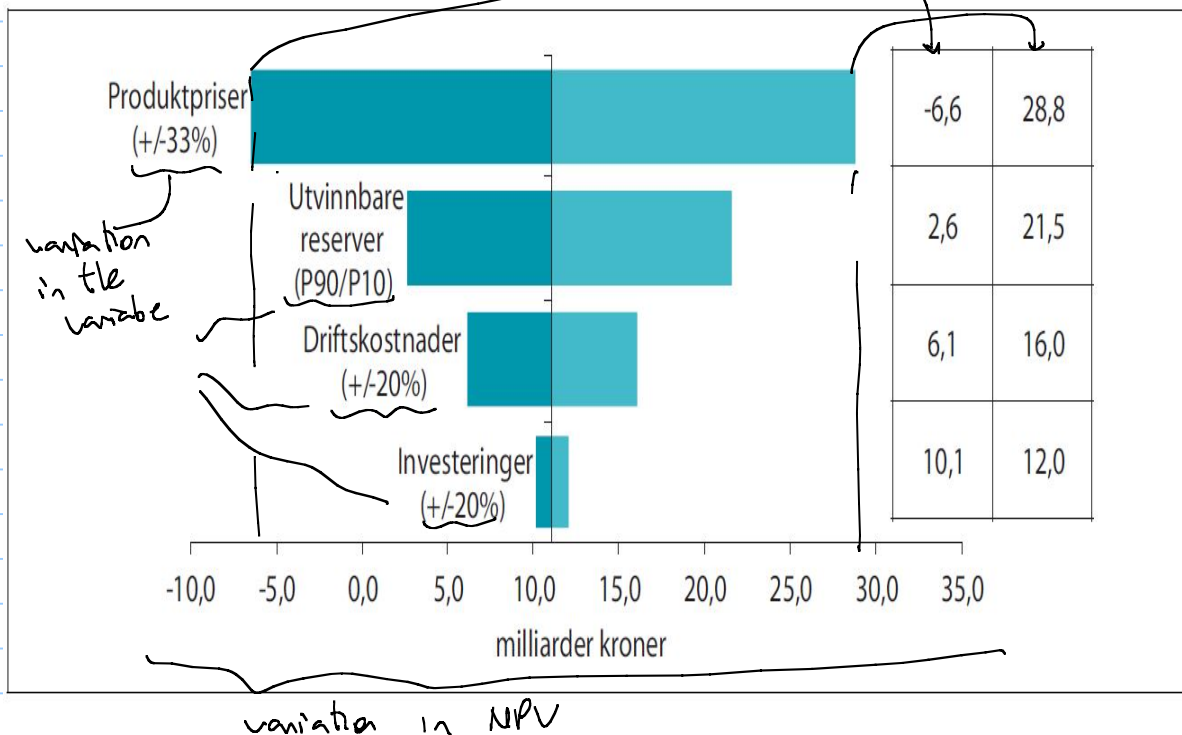
apply normalization

$X_{normalized}$   $X_{base}$   $X_{max}$

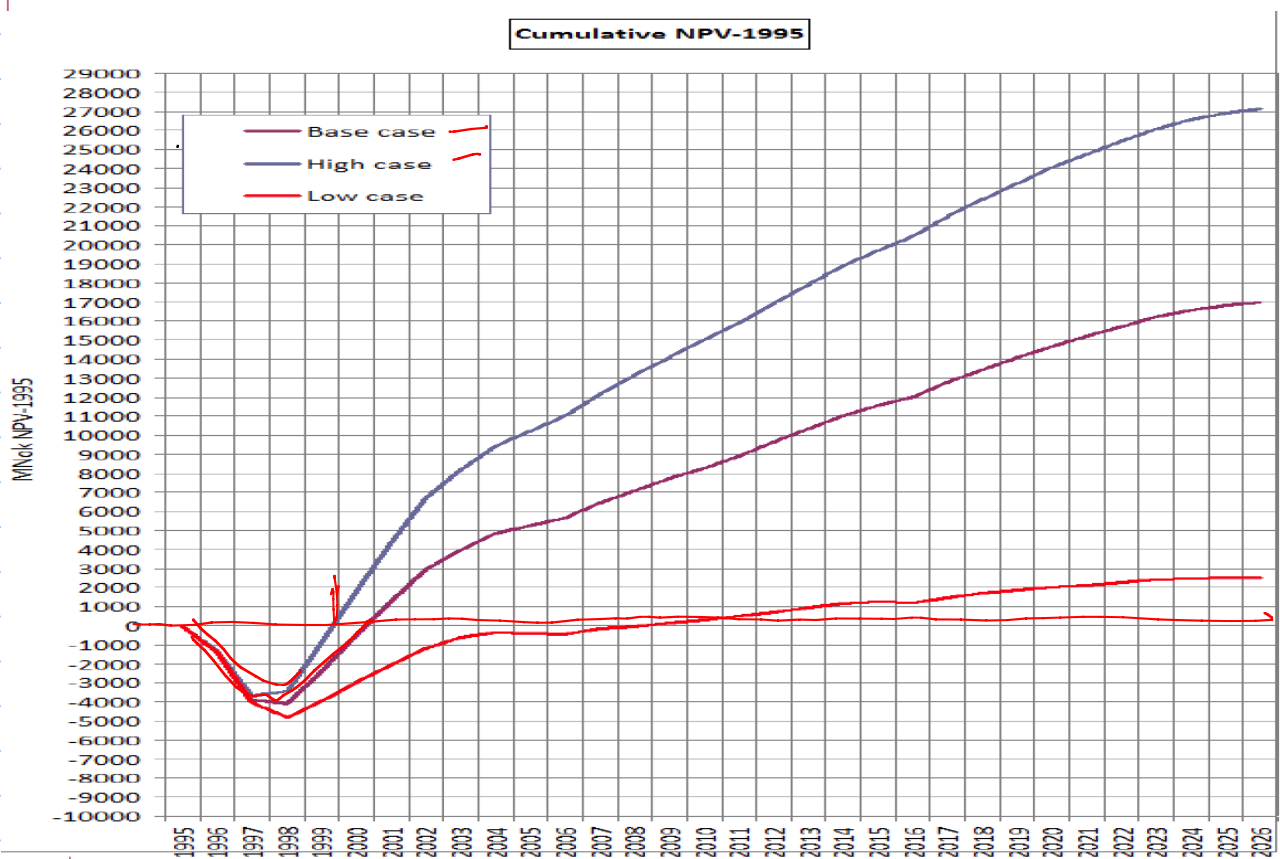
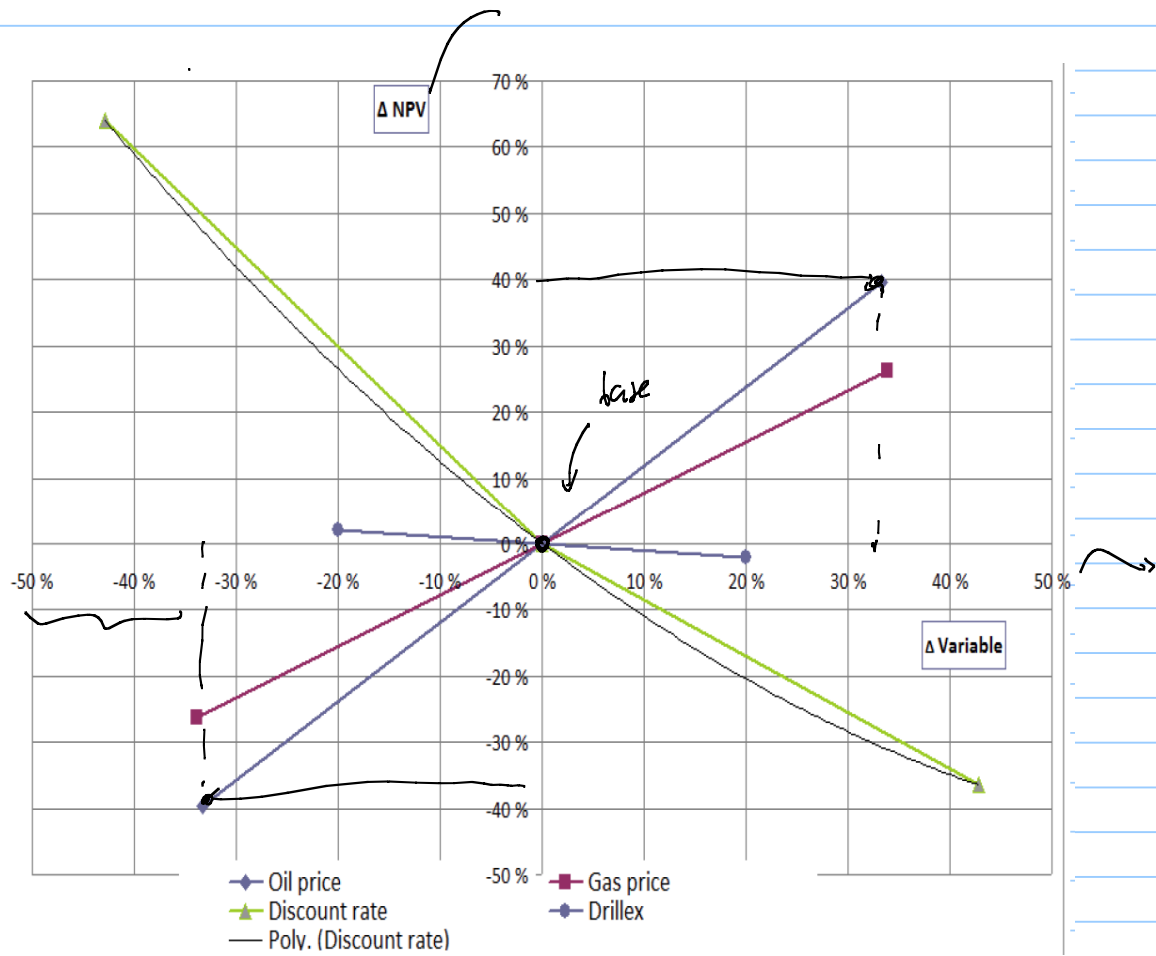
% NPV  
normalize

CAPEX	$\frac{X_{min} - X_{base}}{X_{base}} \cdot 100$	0%	$\frac{X_{max} - X_{base}}{X_{base}} \cdot 100$	$\frac{NPV_{min} - NPV_{base}}{NPV_{base}} \cdot 100$
OMUPEX	11	0%	11	
oil price	11	0%	11	

ternario chart

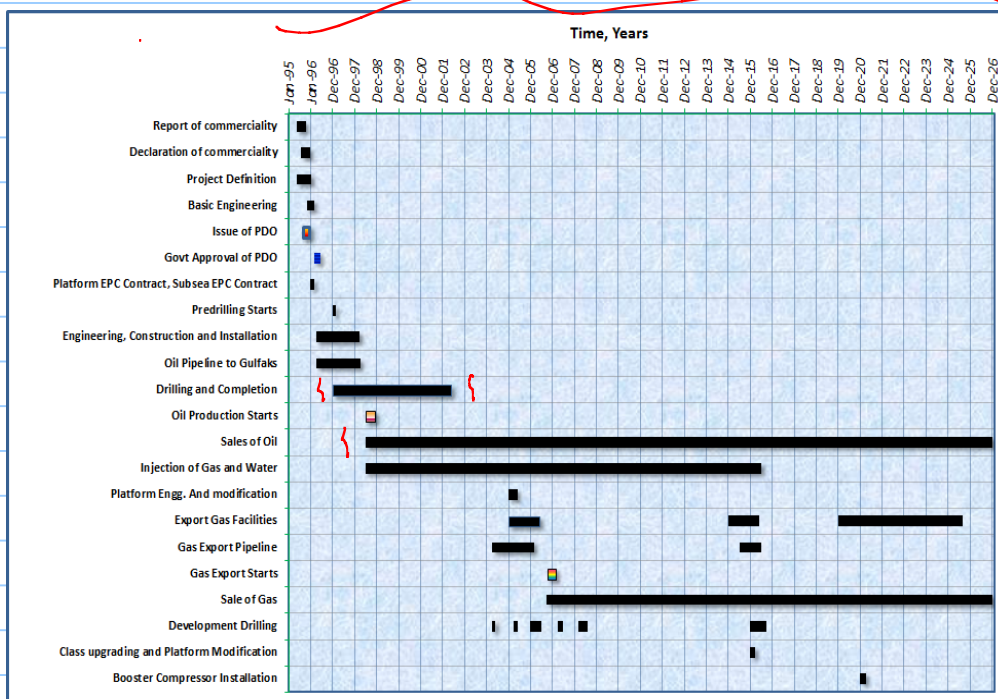


Sproder plot





Gantt diagrams Special chart diagram used in project management that shows when and the duration of important events in the design and construction of the field



Henry Gantt (1861-1919), a mechanical engineer, management consultant, and industrial advisor developed Gantt charts in the 1910's. Not as commonplace as they are today, Gantt charts were innovative and new during the 1920's, where Gantt charts were used on large construction projects like the Hoover Dam started in 1931 and the Eisenhower National Defense Interstate Highway System started in 1956.



Henry Gantt

Every time we, in our project management careers, go through the rigmarole of our projects, trying to meet and beat our own-set goals, a silent word of gratitude goes to the heavens for Henry Gantt for conceiving this intuitive diagram for charting project timelines, for the Gantt Diagram allows us to excel in this chosen career.

<https://www.smartsheet.com/blog/gantt-chart-excel>

useful for exercise.



How to deal with uncertainty in decisions or with integer variables

variables {

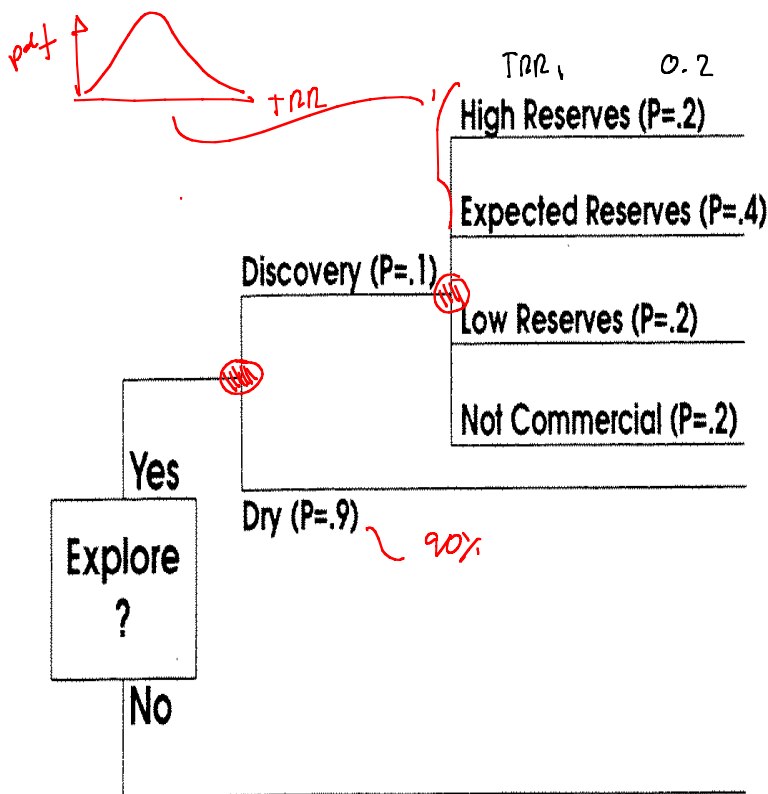
- decisions
- development options {
  - platform
  - subject to beach
  - FPSO

Decision trees allow to deal with integer variables (not continuous)

□ ~ decision nodes

○ ~ chance nodes

◁ ~ end node



multiplication of all probabilities (chance nodes) of that particular branch

i	Prob <sub>i</sub>	NPV <sub>i</sub>	Prob <sub>i</sub> x NPV <sub>i</sub>	
1	0.02	A	(.02) A	Σ P <sub>i</sub> x NPV <sub>i</sub>
2	0.04	B	(.04) B	
3	0.02	C	0.02 <del>(.02) C</del>	
4	0.02	D	(.02) D	
5	0.90	E	(.90) E	
6	1.00	0	0	=

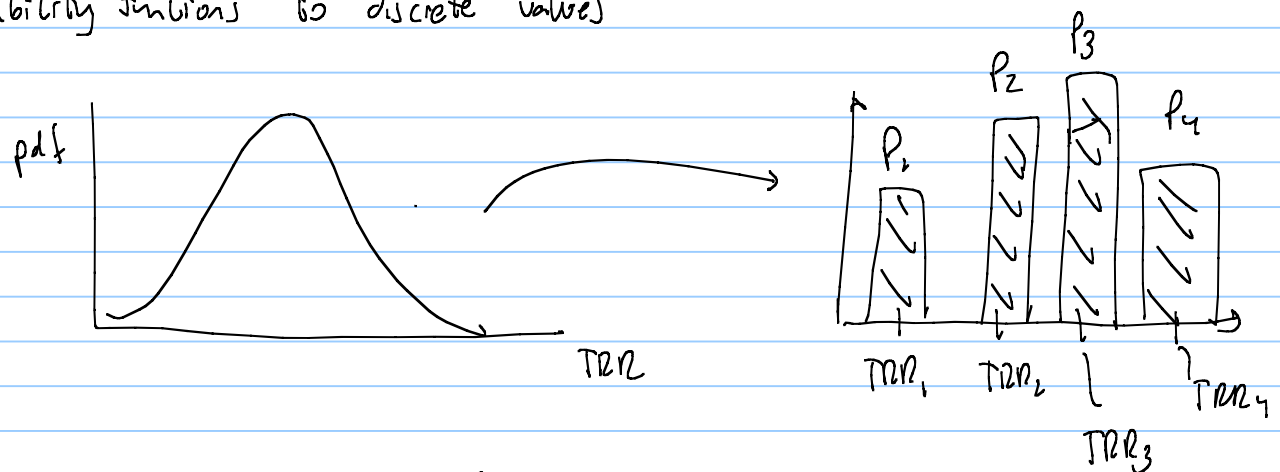
A) B) C) D) E negative (d)

EPV

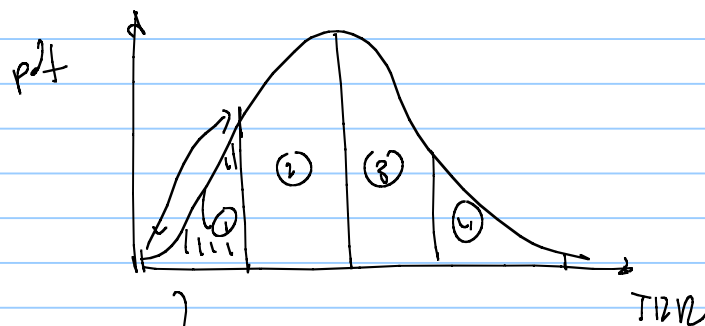
(NPV)

- Weighted AVG. NPV ('Yes-Branch') =  $\sum_{i=1}^5 (\text{Prob}_i) \times \text{NPV}_i = G$
- NPV ('No-Branch') = 0
- IF  $G > 0$ , Explore!
- A-E; Shows the spread in NPV-Outcome for this venture

in decision trees we sometimes have to convert - continuous probability functions to discrete values



one way to do it is the following:  
divide the pdf in sections



area under the curve provides the probability of the section

for the value  $TRN_1$  calculate the most probable value in the section (mode of each section)

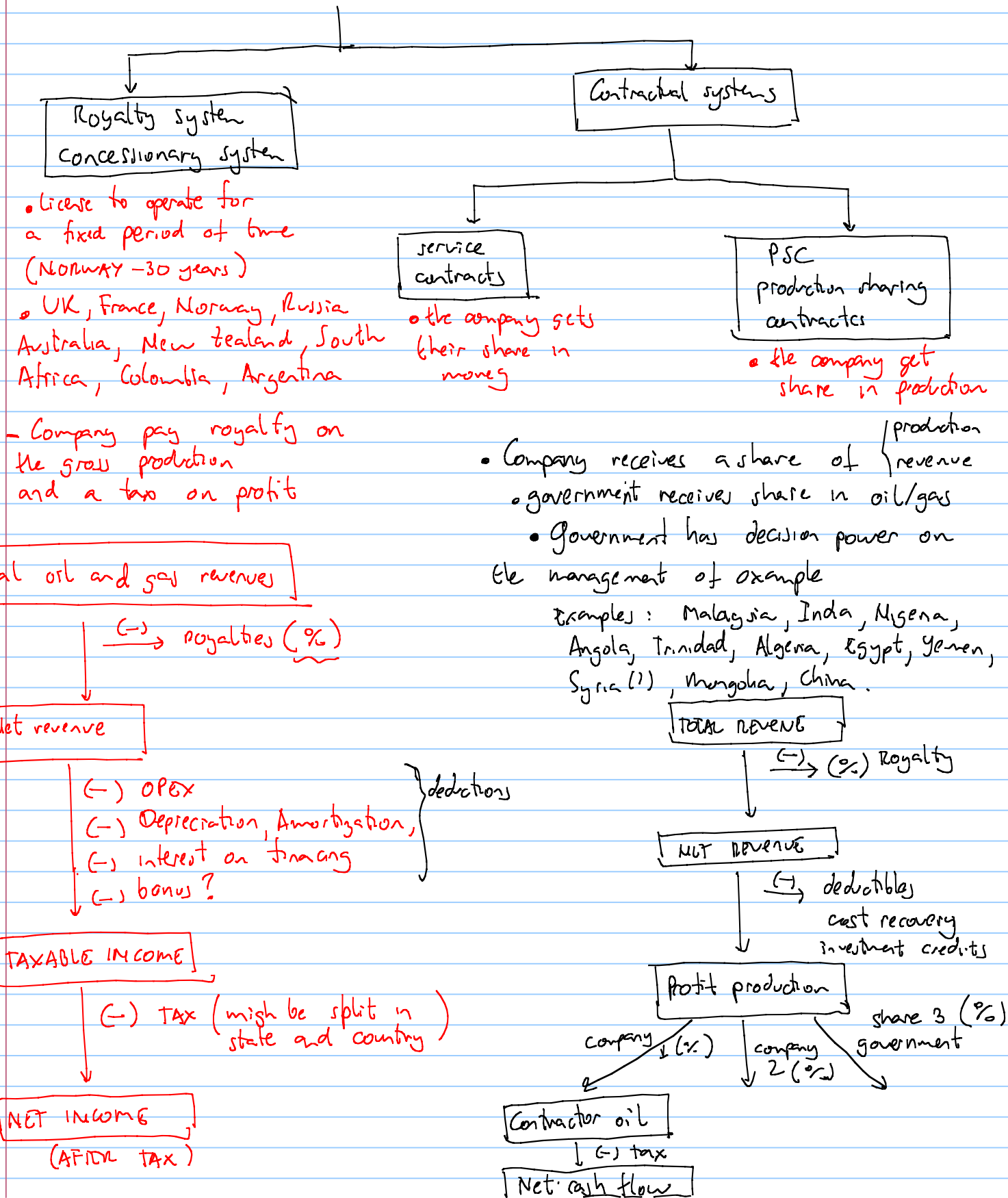
Price \$/Bbl.	Initial Investment \$MM	Reserves MM Bbls.	Case	Prob.	NPV	NPV x Prob.
10	50	50 P = .20	1	.042	60	2.52
10	50	30 P = .70	2	.147	15	2.21
10	50	20 P = .10	3	.021	-10	-0.21
10	60	50 P = .20	4	.056	53	2.97
10	60	30 P = .70	5	.196	8	1.57
10	60	20 P = .10	6	.028	-17	-0.48
8	50	50 P = .20	7	.042	46	1.93
8	50	30 P = .70	8	.147	1	0.15
8	50	20 P = .10	9	.021	-24	-0.50
8	60	50 P = .20	10	.018	35	0.63
8	60	30 P = .70	11	.063	0	0.00
8	60	20 P = .10	12	.009	-20	-0.18
8	50	50 P = .20	13	.024	28	0.67
8	50	30 P = .70	14	.084	-7	-0.59
8	50	20 P = .10	15	.012	-27	-0.32
8	60	50 P = .20	16	.018	21	-0.38
8	60	30 P = .70	17	.063	-14	-0.88
8	60	20 P = .10	18	.009	-35	-0.32
Weighted Avg. NPV				9.55		

MEV mean expected value

## Petroleum fiscal systems (brief)

- ✓ in almost every country in the world the owner of the mineral rights is the government (except in the USA).

↳ the individuals pay a tax to state.



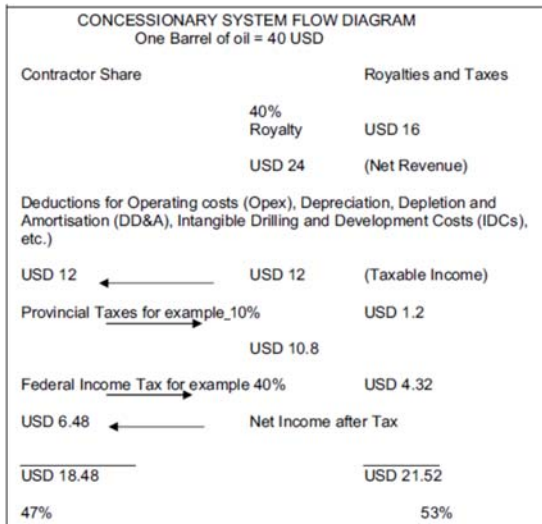


Figure 1.4 Example concessionary system flow diagram

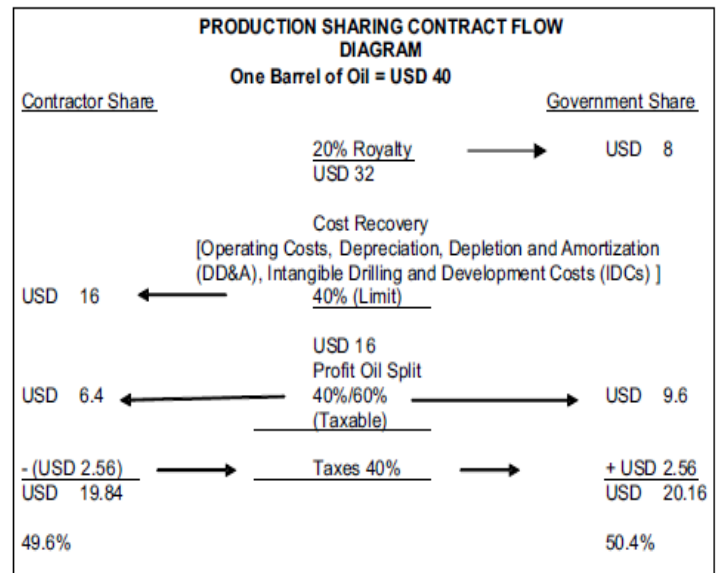
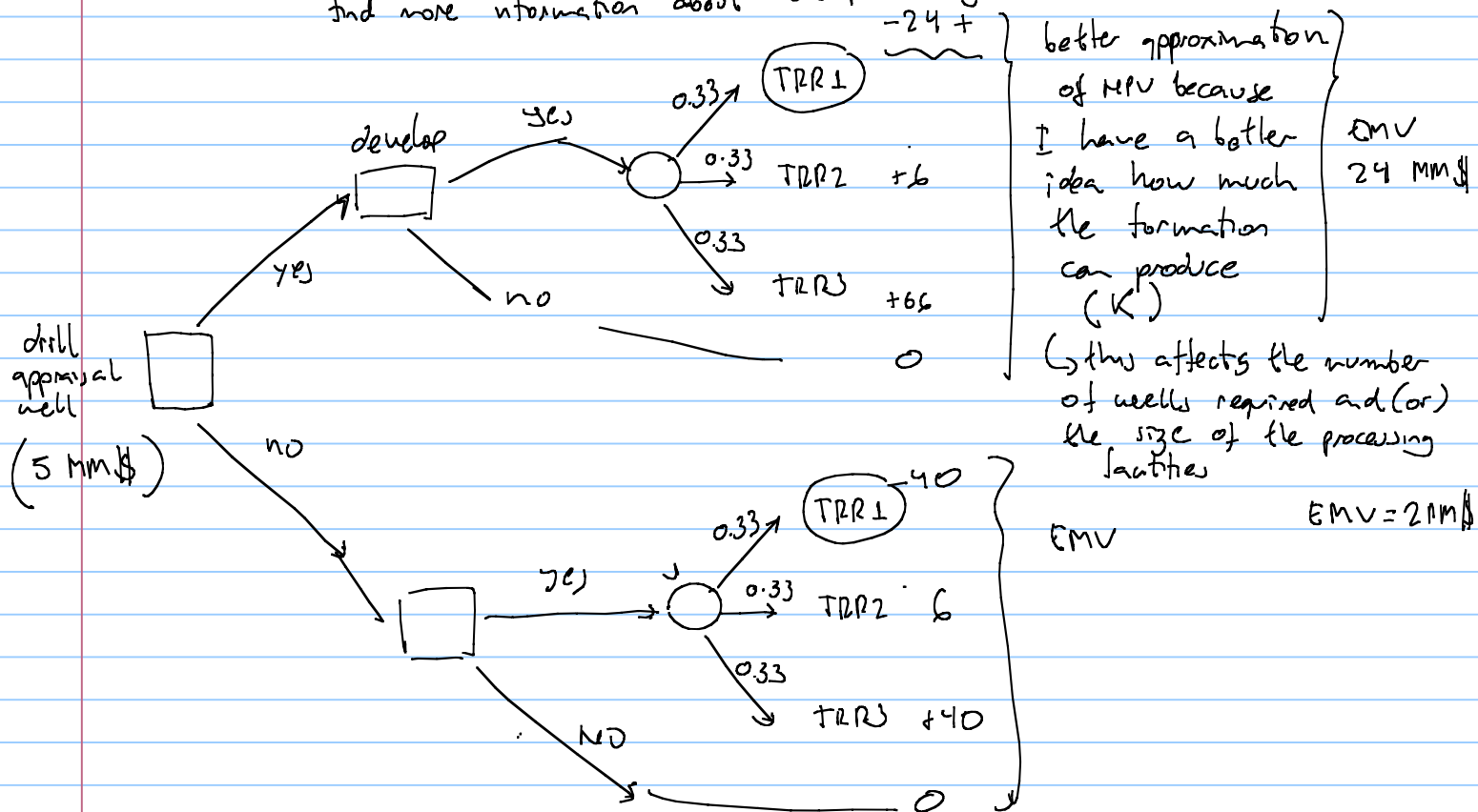


Figure 1.9 Example production sharing contract flow diagram

Decision trees can be used to determine the value of new information given by a specific activity. Determining the value of information.

An example: Drilling an appraisal well to find more information about well productivity  $NPV( \text{MM} \$ )$



Value of appraisal information = EMV with appraisal - EMV without appraisal =  $22 \text{ MM} \$$

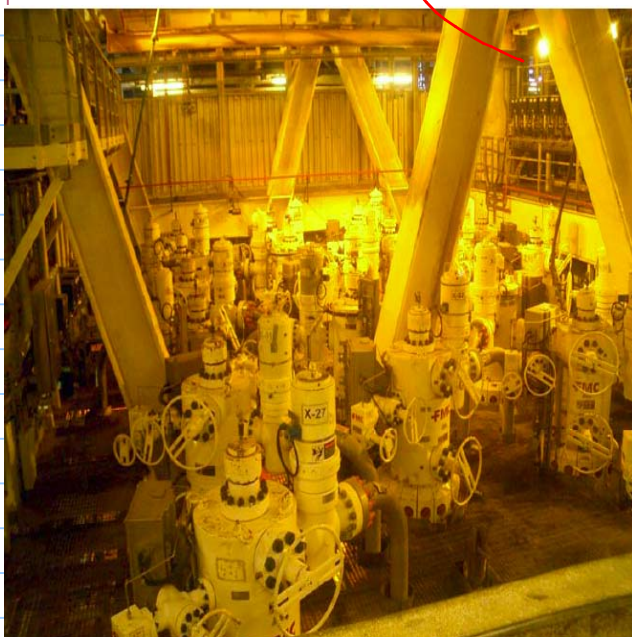
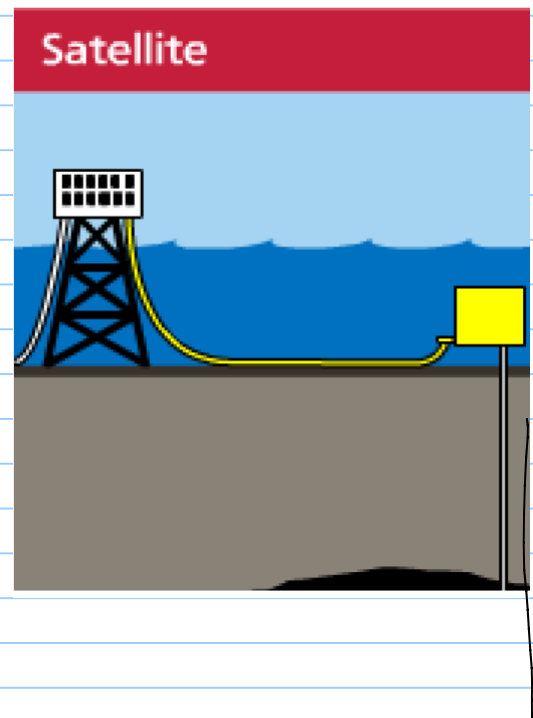
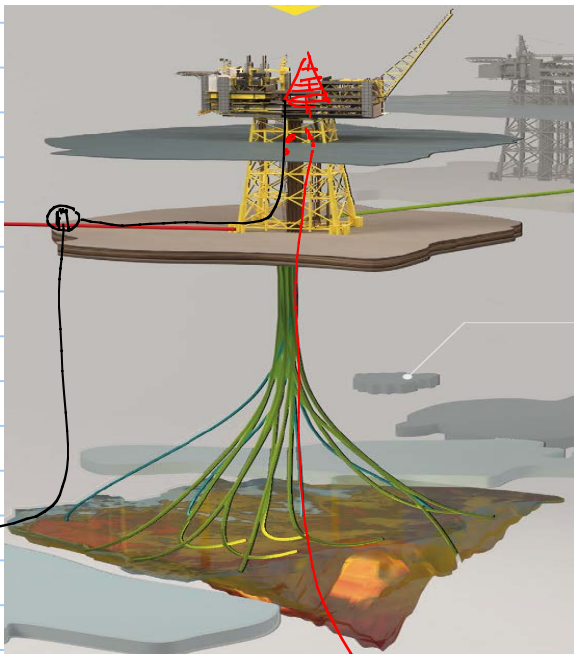
# Layout of hydrocarbon production systems: (focusing offshore Norway)

dry christmas trees + (subsea wells)  
(platform wells)

- wells are drilled similar to onshore
- wells are deviated (highly deviated)
- careful for intersecting well paths

wet christmas trees  
(subsea wells)

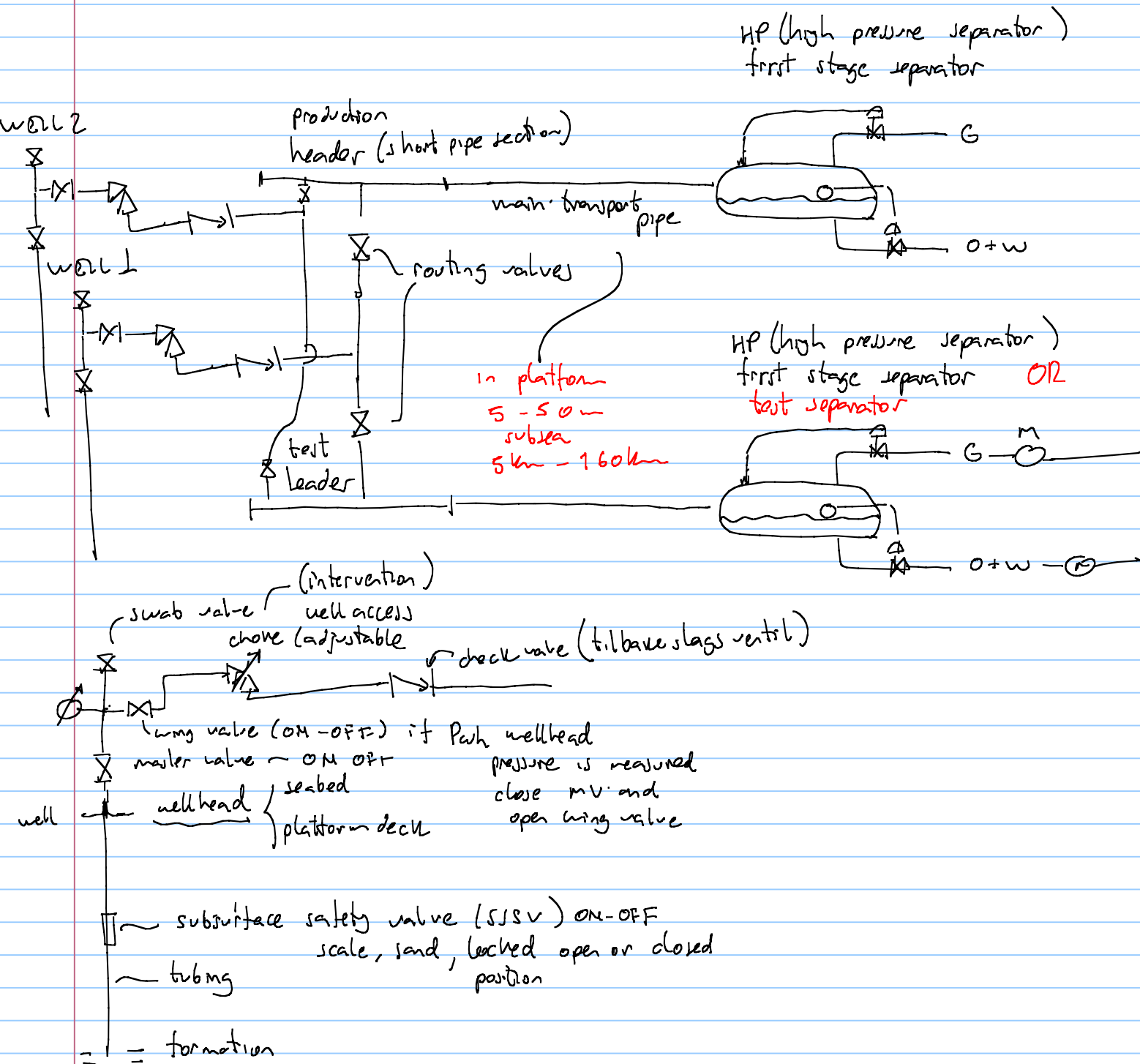
- Drilling is done with a drilling vessel (ship, semi-sub)
- wells are not so deviated if they are not grouped in clusters.



well bay

## • Production manifold:

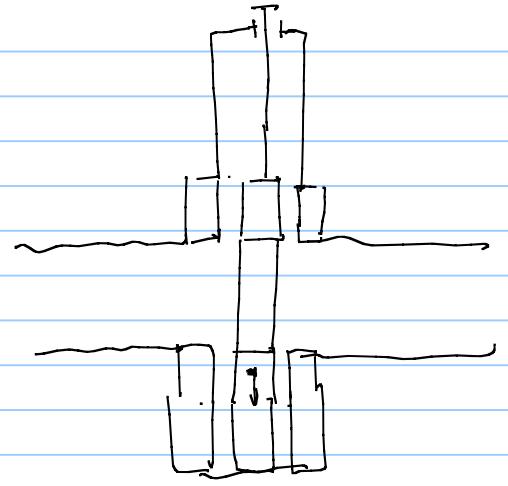
- Comingle (merge production from different sources)
- Test the well
  - to route the well production to a particular separator
- determine production shares (allocation)
- estimate the productivity of the well (IPR) inflow performance relationship.
- to generate data to tune reservoir models (history matching) and improve predictions
- to sample the fluids → to determine fluid behavior





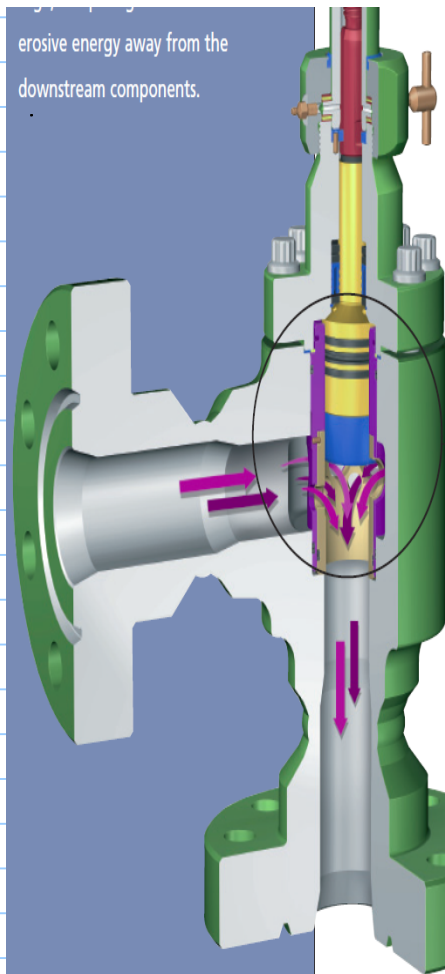
master valve  
wing valve  
routing valve

they are usually gate valves



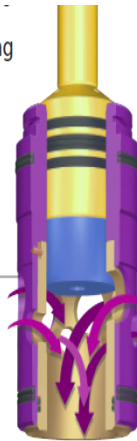
choke is a control valve, adjustable valve

needle choke  
cage choke



of operating conditions, including high sand concentrations.

- Available in manually operated or actuated models.

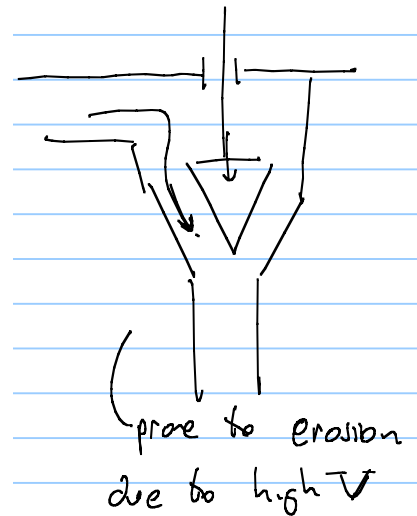


Control Choke  
Cage-Style Trim Design

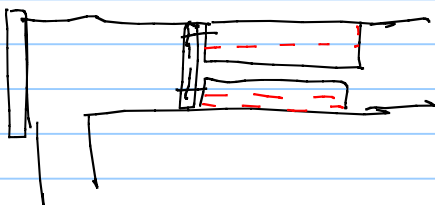
#### TABLE OF CONTENTS

Plug and Cage Control Choke	2
External Sleeve Control Choke	3
Multi-Stage Control Choke and Trims	4
CC15 Control Choke	5
CC20 Control Choke	6
CC30 Control Choke	7
CC40 Control Choke	8
CC60 Control Choke	9
CC70 Control Choke	10
CC80 Control Choke	11
High Temperature and High Pressure	12

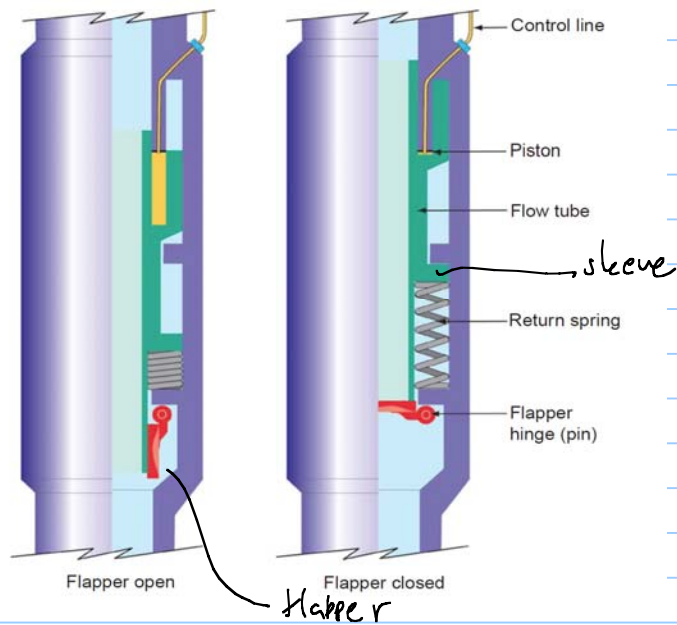
needle choke



in onshore fields bean choke is often used to control the production. are not adjustable  
cartridge that is replaced with time.







subsurface safety valve  $\square$  always energized with a hydraulic line  
 $\sim 100$  m  $\sim$  below the x-mas tree.



Gulf war (1990's)  
 Kuwait bombed -

Production manifold for platform wells or onshore wells



manifolds (hybrid)

routing valves

test header

main production header



Colombia

?

Very big difference between dry X-mas trees vs. subsea wells

(tree is cheaper.)

### Christmas Tree Systems



Onshore tree



Offshore tree



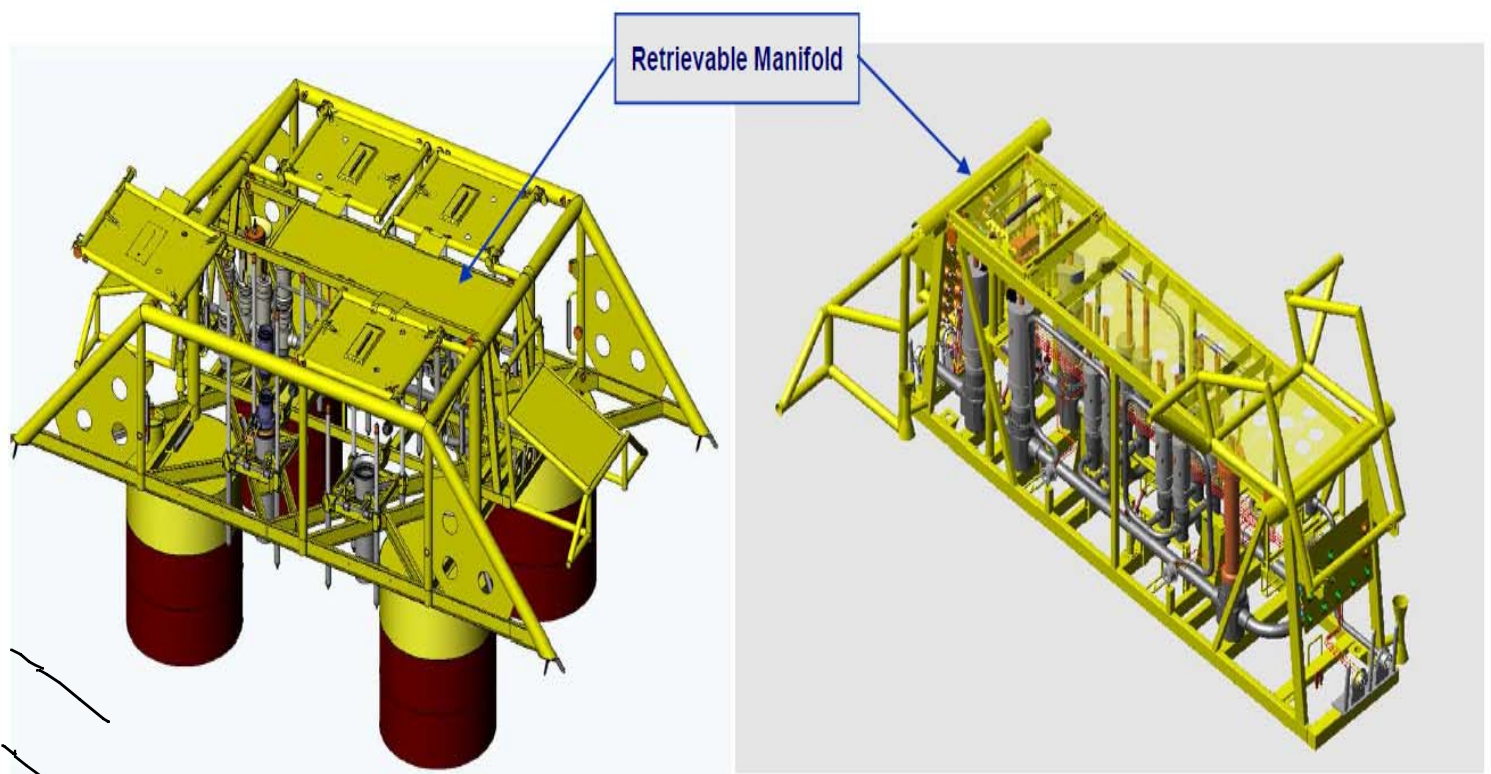
Subsea tree

ROV to operate  
alignment,  
remote operation  
protection  
pressure resistance.

platform wells are very deviated  
subsea wells are less deviated (usually)

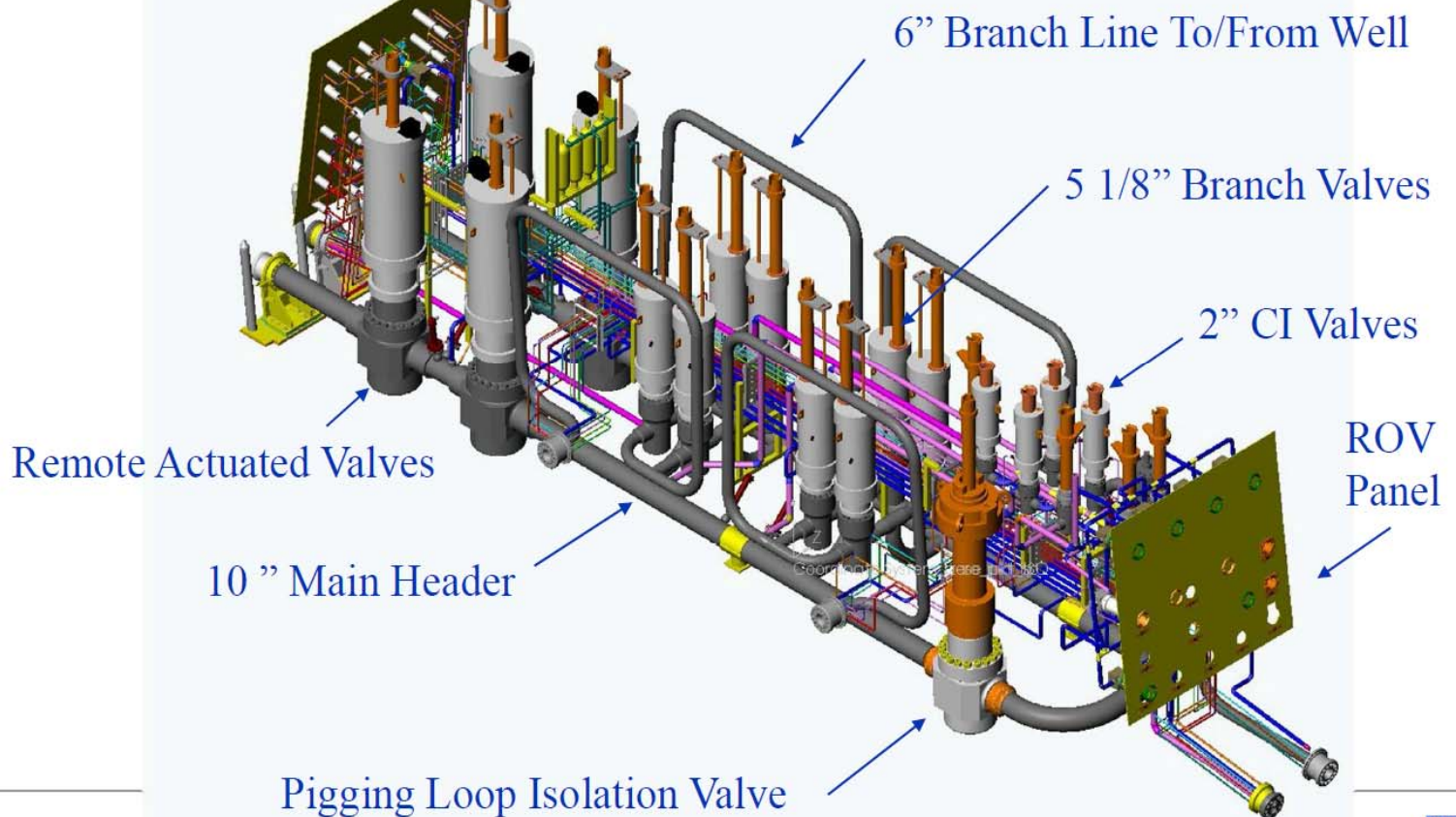
focusing on subsea systems.

- the production manifold has another function: allow for pigging.



4-well template





Pigging: Send a "pig" through the pipe to execute different tasks

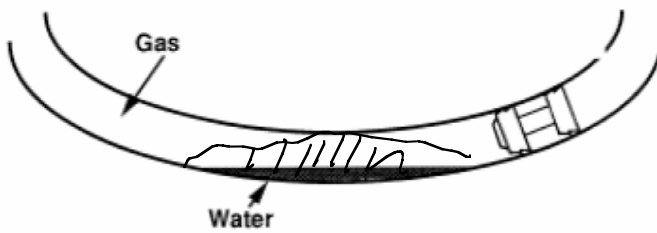
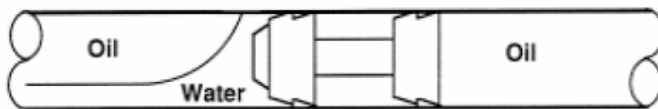
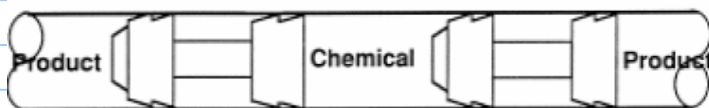
Various pig types



Wax plug-North Sea line pigging



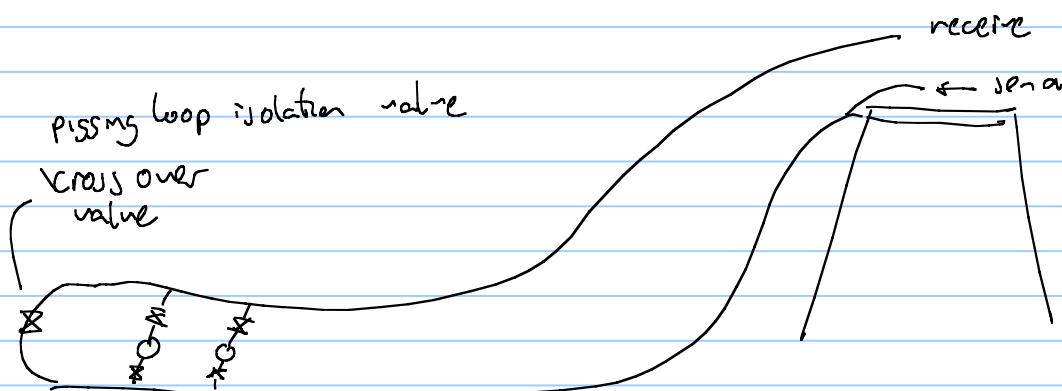
wax: at a particular P and T heavy hydrocarbon chains precipitate out of the liquid and form wax

Removing water in a gas flow systemRemoving water in a oil systemTreating by chemicalsRemoval of Wax

|| high pressure drop  
 ~ reduced production

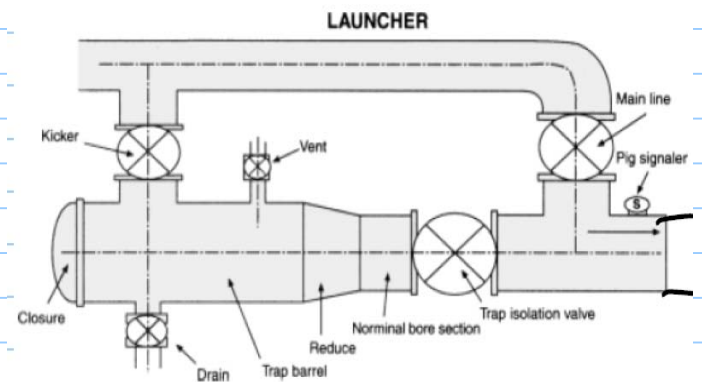
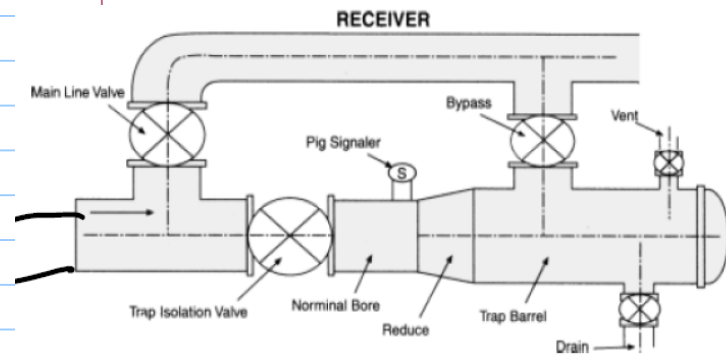
high pressure fluid

In systems with oil prone to generate wax pigging is done regularly

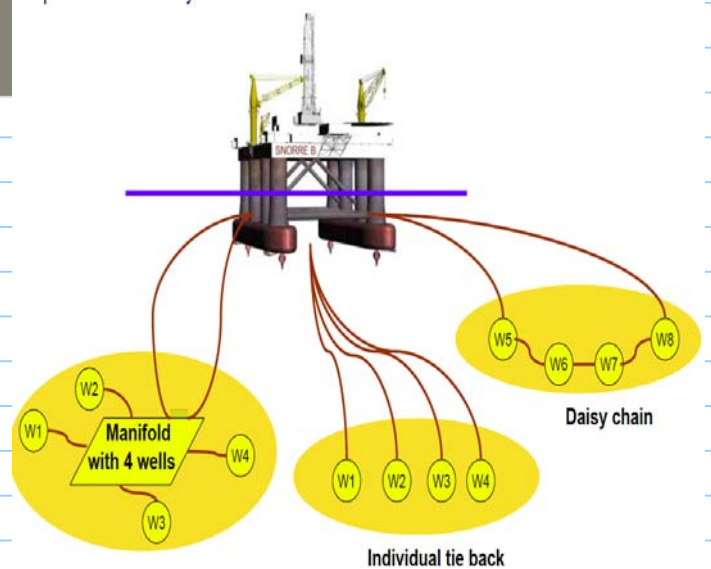
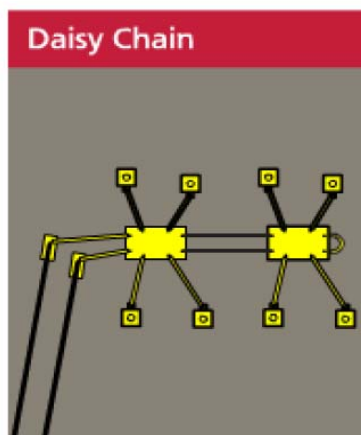
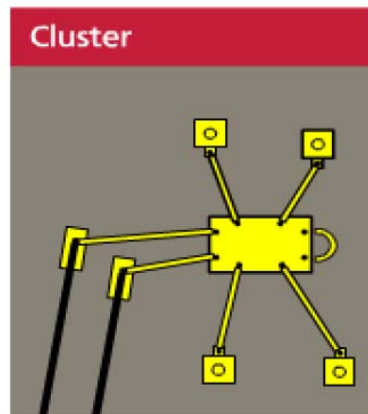
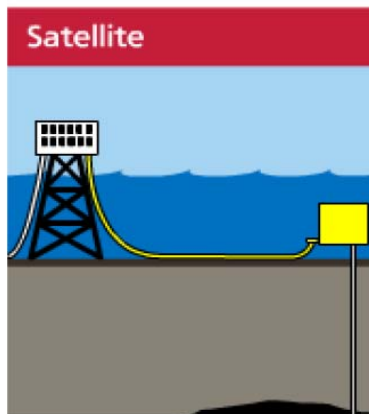


pig receiver

pig launcher



Some other subsea field architectures:

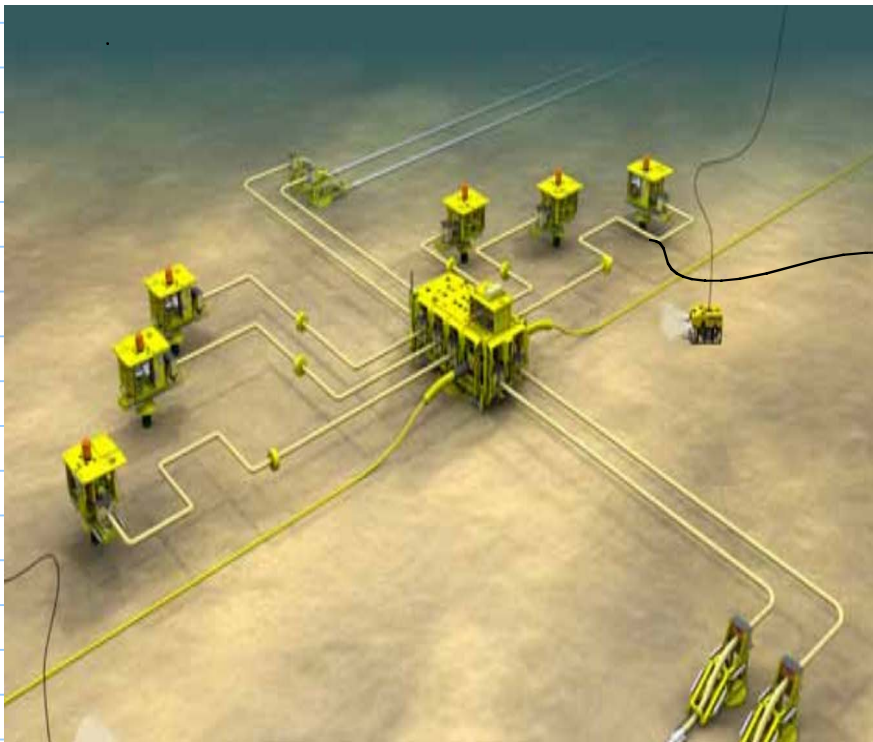




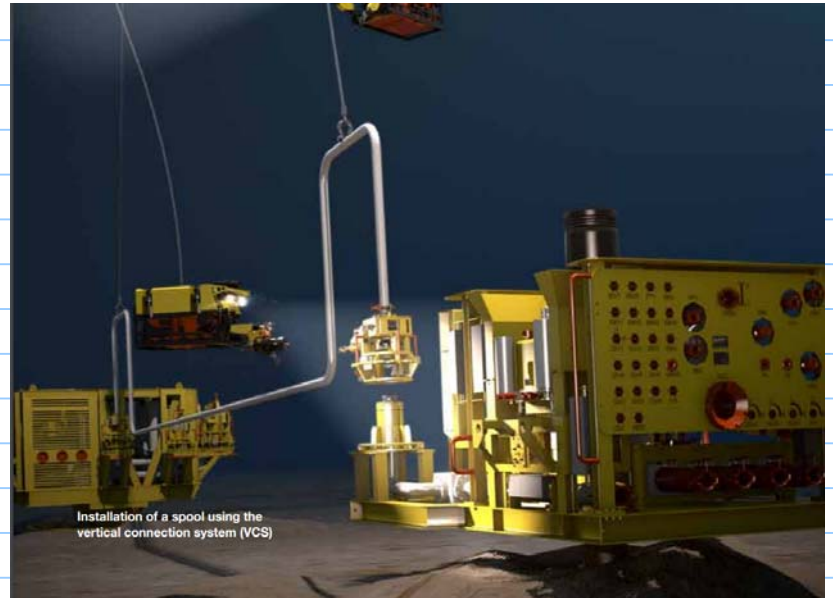
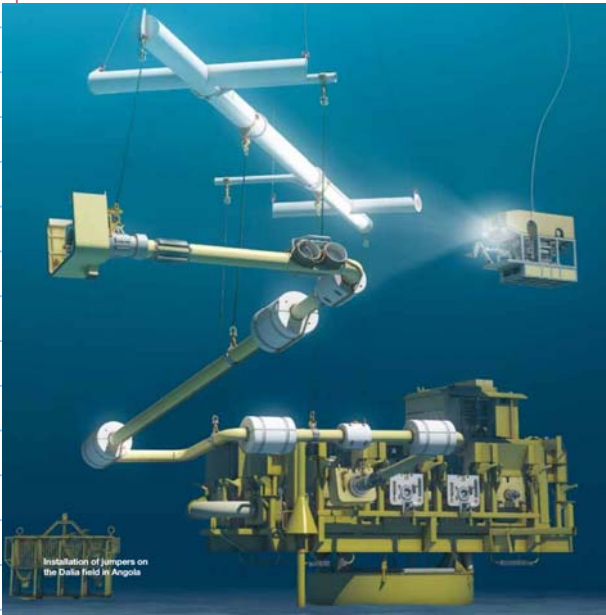


template well + manifold  
 - manifold  
 • subsea separation  
 • subsea boosting.

wells and manifold are not in the same template

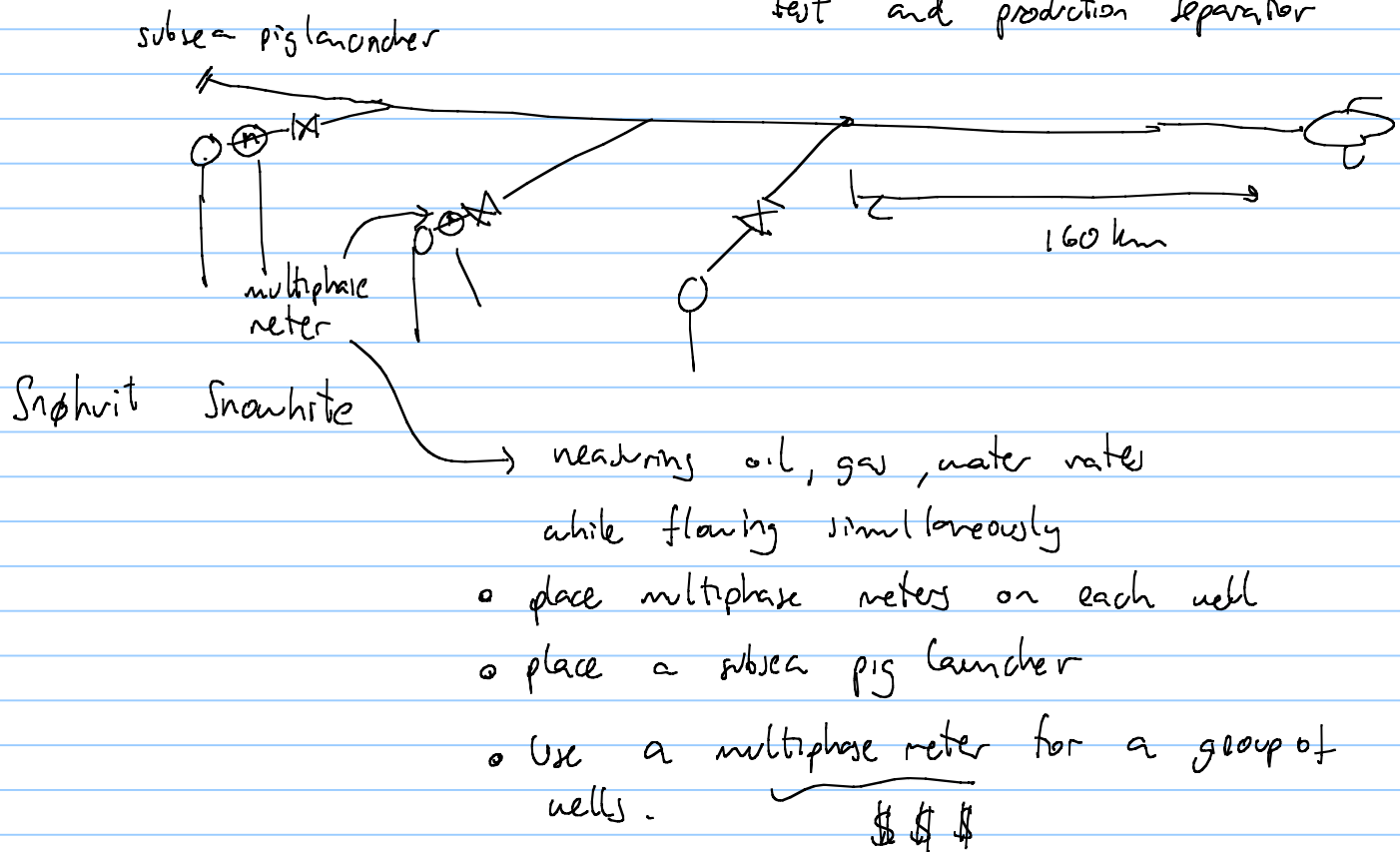


connection between  
 templates well and  
 manifold is called  
 jumper  
 rigid piece of pipe



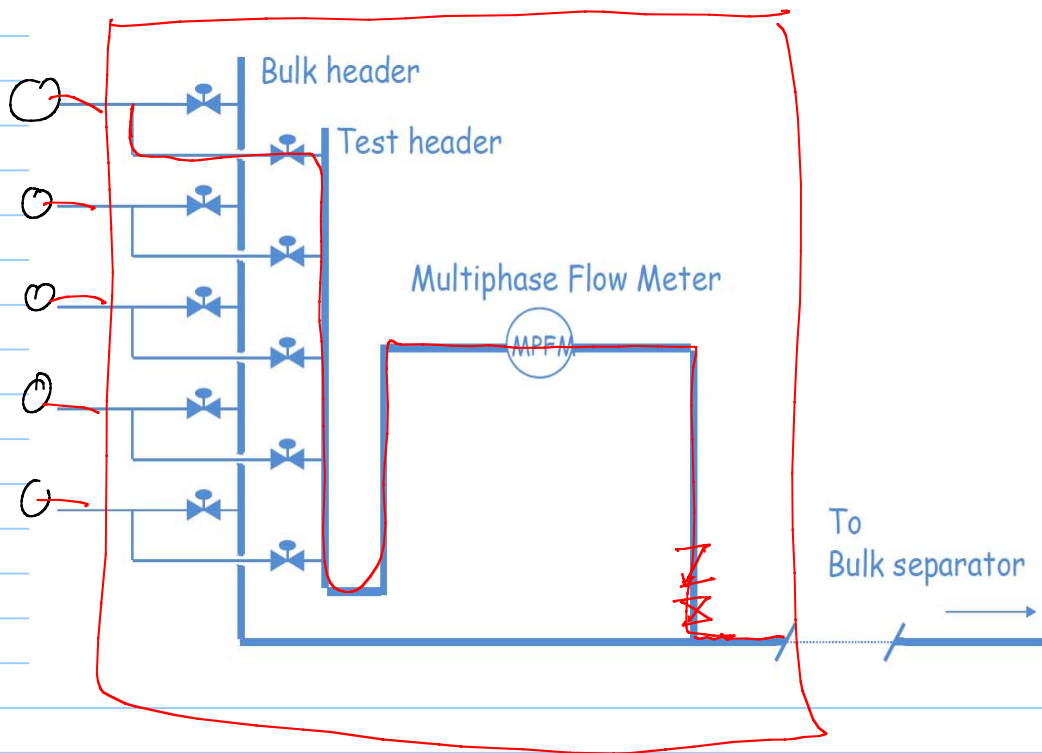
how do we test subsea systems  
or onshore systems

where I don't have two  
separate lines that go to  
test and production separator





Use a manifold to route the well production through the mpm  
multiphase  
meter



In onshore systems a portable test separator (see below) is often used in this arrangement instead of the multiphase meter.



## Offshore structures for oil and gas production

- not discussed here
- drilling vessels, ships
- vessel to lay equipment pipes,
- tankers
- supply vessels

- Drilling package: facilities for well drilling and intervention. drilling tower, BOP, mud pumping and processing system, cementing system

mud package  
storage deck for tubulars, drilling risers

- facilities for light well intervention. { wireline, coiled tubing }
- Processing facilities {
  - gas processing train
  - oil separation train
  - water processing train (polishing unit)

- gas injection system { compressor trains }
- gas compression system for pipeline transport
- gas lift system { compressor trains, pipes, valves }
- water injection system { seawater treatment, pumping }

- Living quarters

- Helideck or access points

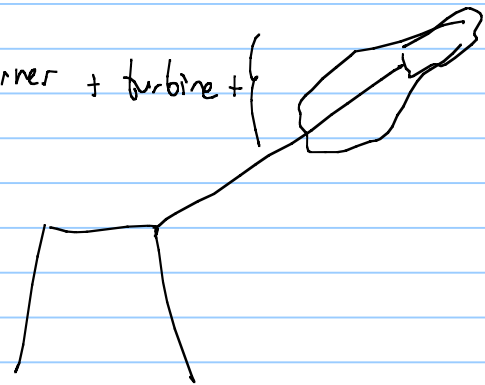
- Power generation { gas turbines { compressor + burner + turbine + }

flare system: burn gas when needed

- Utilities: hydraulic power fluid, compressed air

drinking water, air condition  
ventilation and heating system

seals of  
rotating machinery



- well bay
- production manifolds
- metering
- oil storage

- facilities for oil offloading
- Control system
- monitoring system
- System to recover production chemicals (corrosion, scale, wax, demulsifier, hydrate)
- Repair workshop

# Classification of offshore structures

Fixed

Compliant

Bottom supported

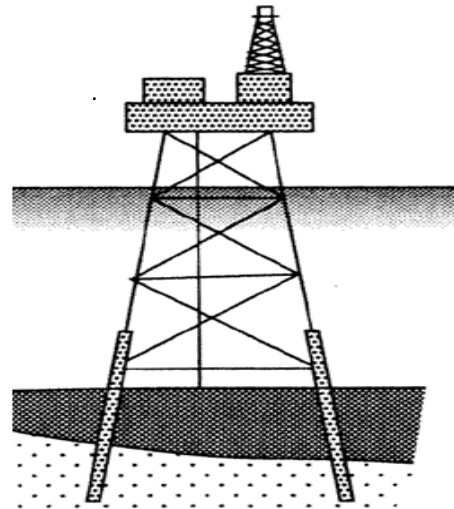
Jacket

Gravity Based structures

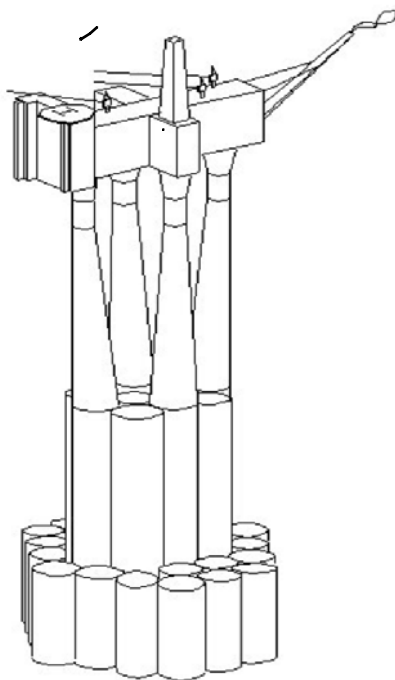
Compliant tower

most of the loads are transferred to seabed, soil

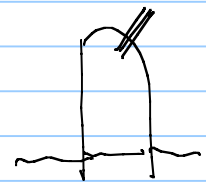
Jacket



Gravity based structures



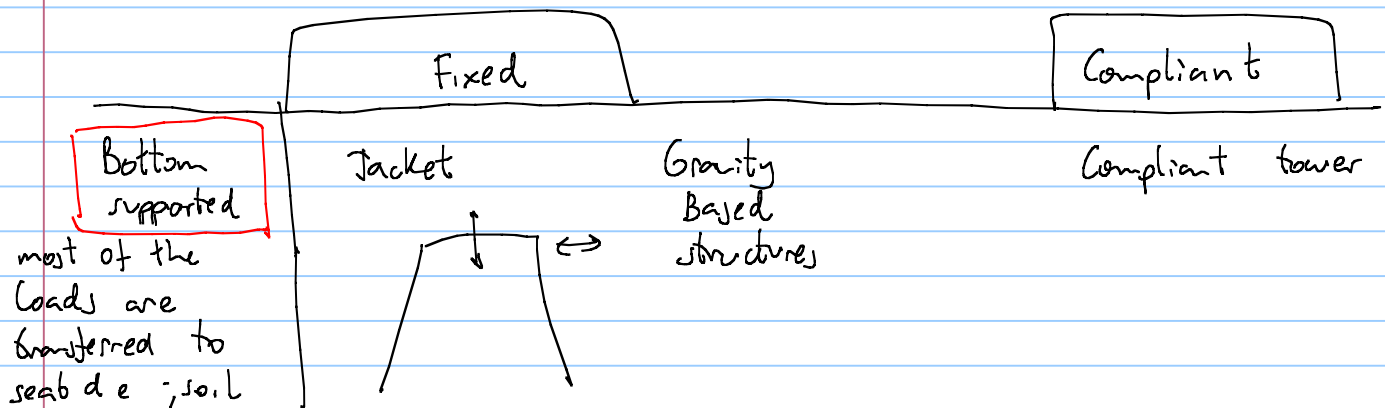
Suction anchor



# Compliant tower



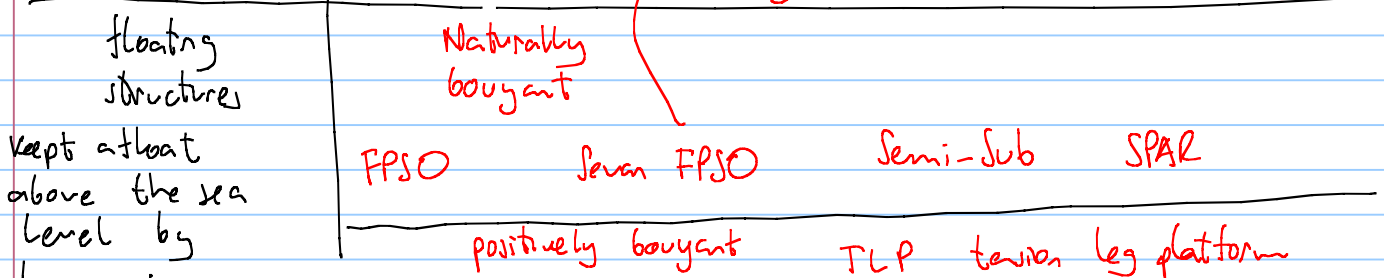
guyed tower



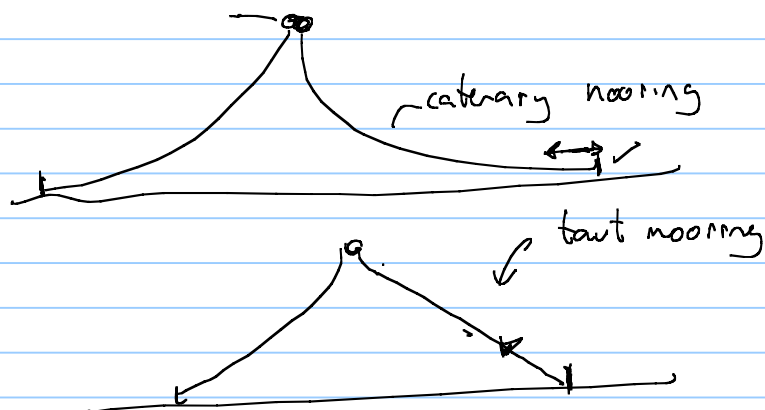
have reduced movement in the vertical and horizontal direction



## Floating Production Storage Offloadings

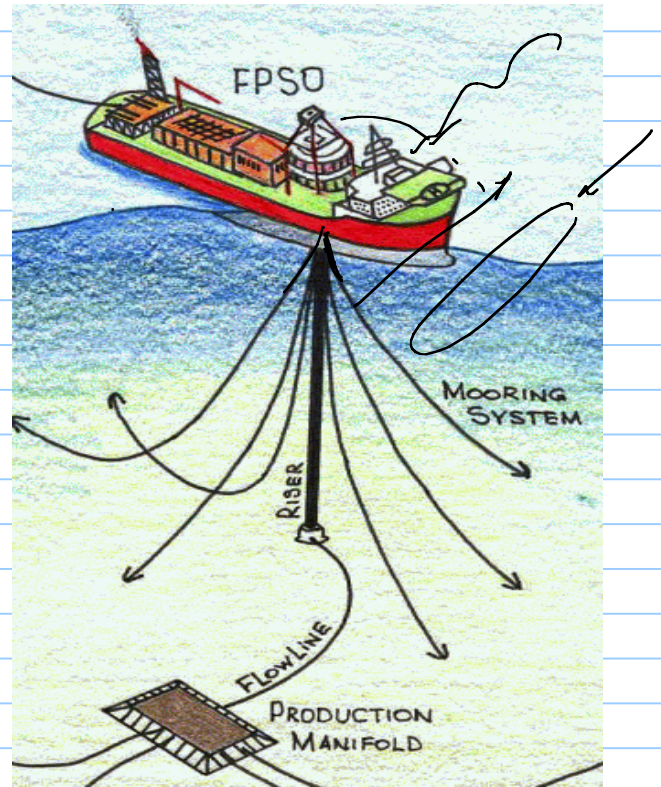


ballast tanks allow to control buoyancy  
the one typically moored with steel chains or pretensioned composite lines

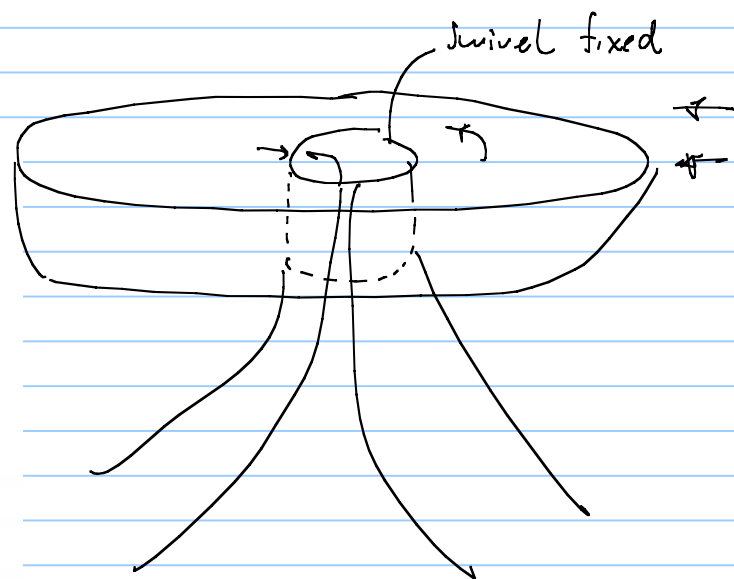




FPSO-ship



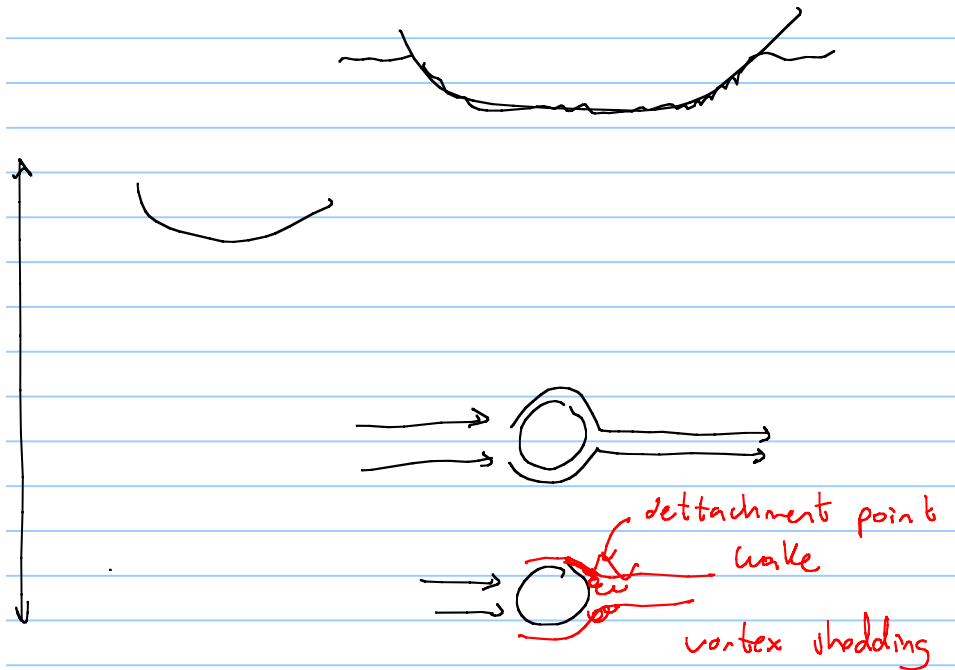
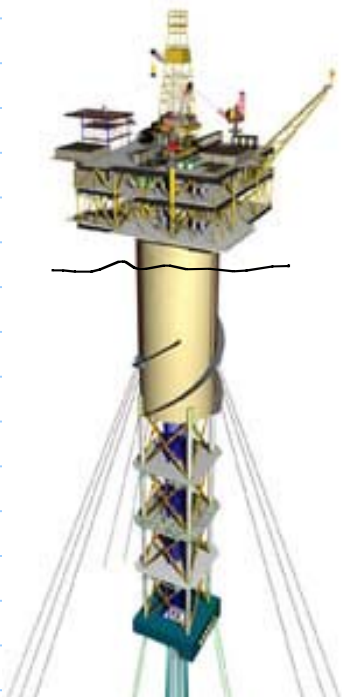
Sevan type FPSO



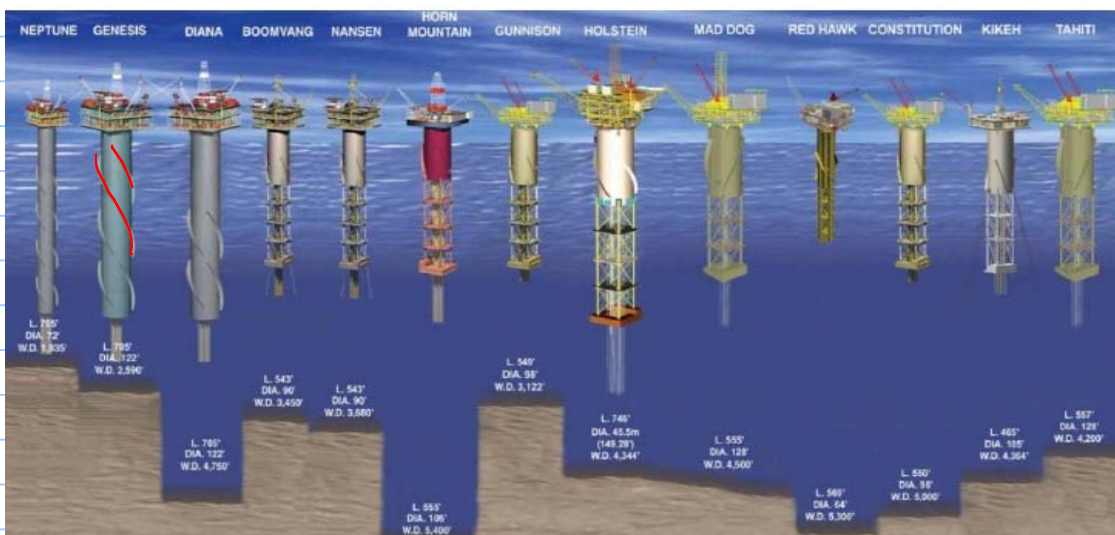
Semi-submersible



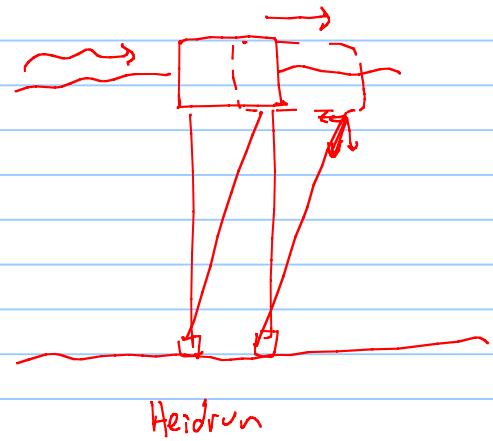
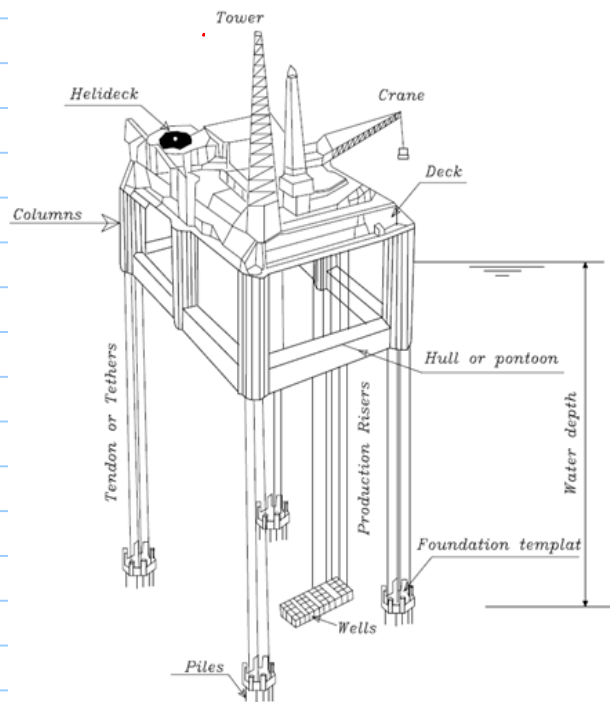
SPAR → deep hull structures



## SPAR Projects



induces big vibrations in the structure that is why we have the spinals

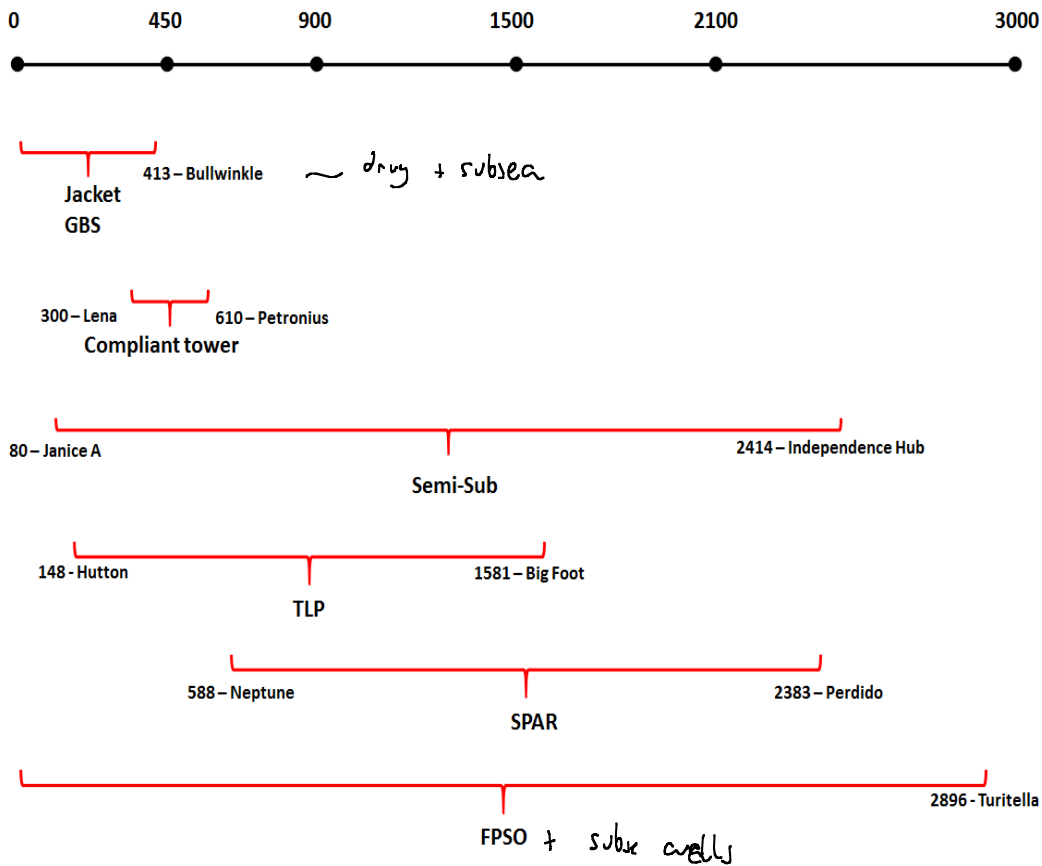


How do we choose offshore structures?

- water depth ✓
- reservoir structure and extent ✓
- Ocean conditions → loads  
wind ✓  
waves ✓  
current ✓
- soil characteristics
- well artificial lift ✓
- dry vs. subsea wells ✓
- storage ✓
- future development plans
- delivery time availability
- experience of the company.

Water depth:

Water depth [m]



• Dry vs. subsea wells

X-mas

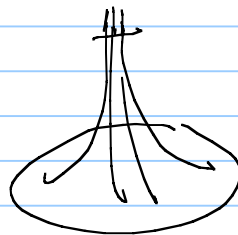
- 1) on the offshore structure
- 1) in the seabed

Dry well ~ max depth  
1700 m

I choose dry X-mas trees if:

- frequent well intervention  
1) required

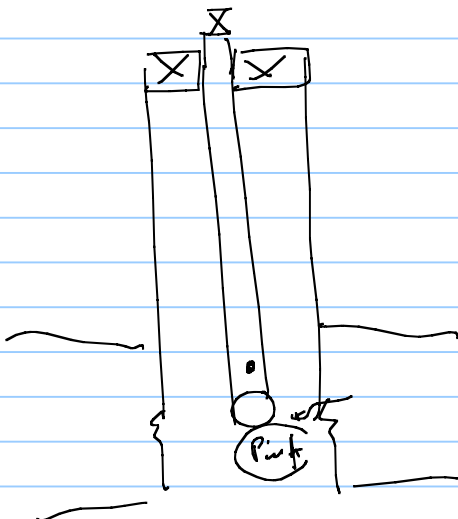
① reservoir structure



compact, not spread

- if well have ESPs  
electro submersible pump  
lifetime 1-2 years  
need to access the  
wellbore often

in contrast subsea wells have  
an average intervention time of  
5 years.

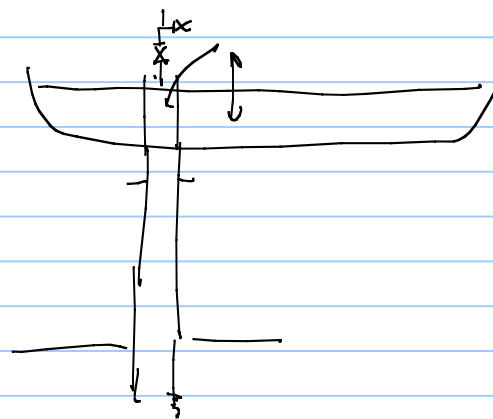




what is the meaning of spread reservoir / localized } depends on the drilling package



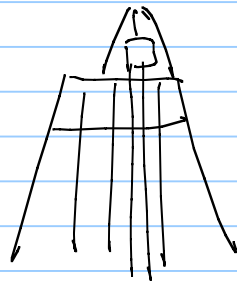
the only structures that have low movement, that allow to have dry wellhead is



bottom supported structures } jacket  
GBS  
tower

TLP  
SPAR }  $\pm 3$  m

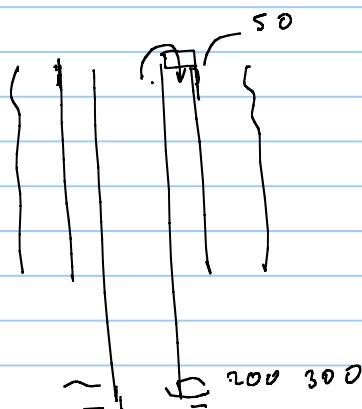
jackets on GBS wells are drilled just like onshore

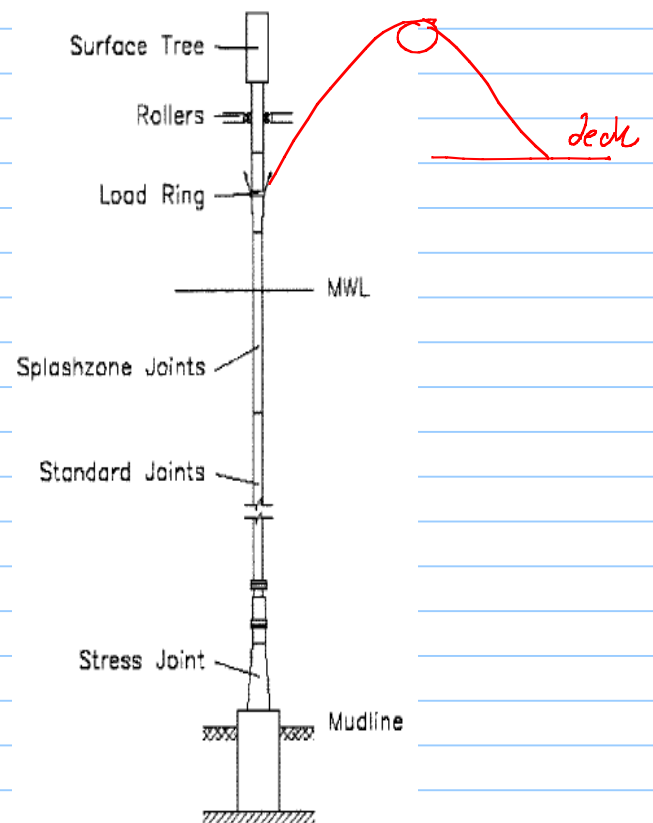
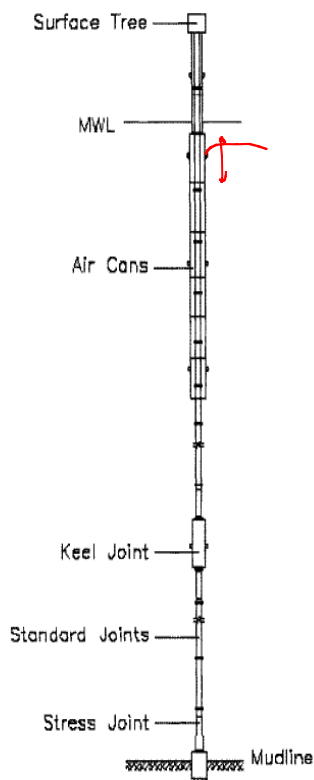
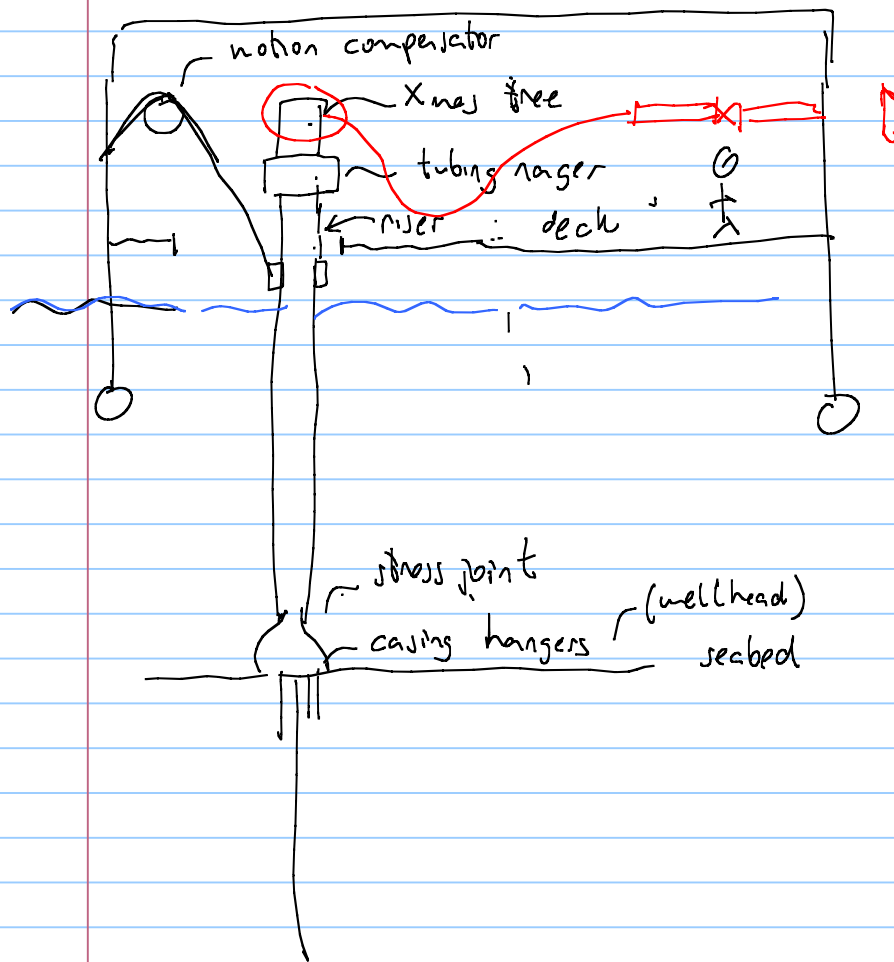


for TLP, SPARs and compliant towers the movement is significant

have a wellhead in the seabed:

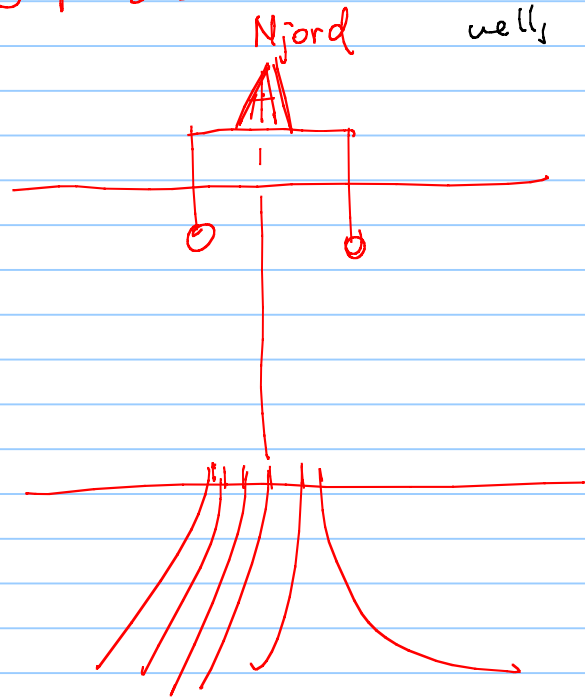
- ↳ support casing
- ↳ transfer load of X-mas tree to conductor (soil)
- ↳ seal between annular spaces in the casing





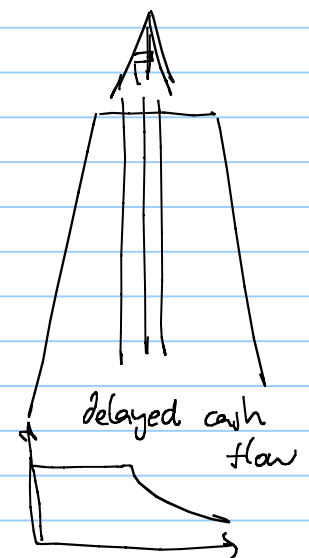
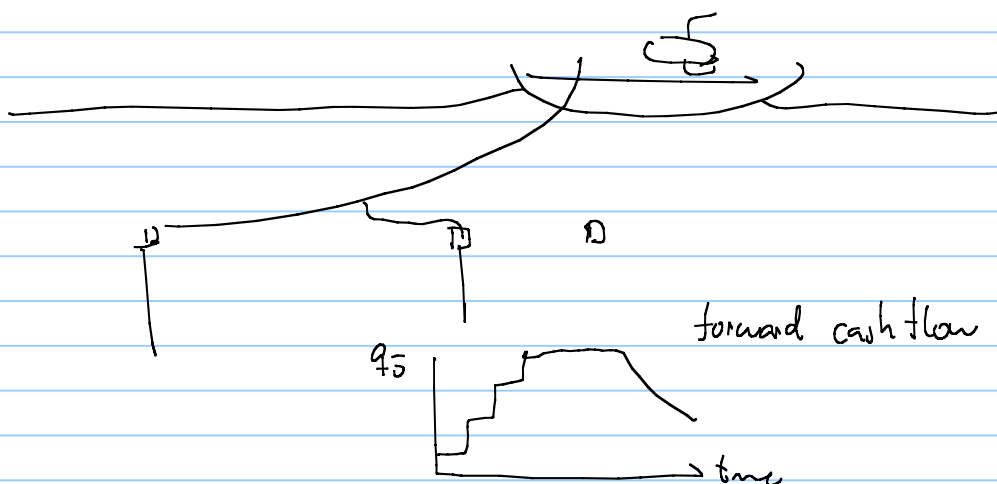
if dry wells are used usually the offshore structure has a drilling package

when wells are subsea sometime (not often) the offshore structure has a drilling package)



wells are exactly below the offshore structure

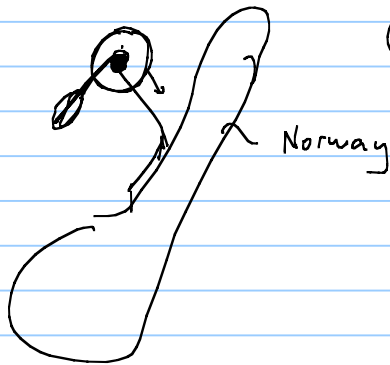
- Dry well structures have limited number of well slots available  
not suitable for infill drilling (maintain the production rates)
- Systems with subsea wells: have to perform flow assurance
- in systems with subsea wells production can start gradually as soon as the offshore structure is in place



- Storage of oil : only structures that allow storage are:

FPSO	~ 2.5 mmbbls
GBS	~ 300.000 bbls

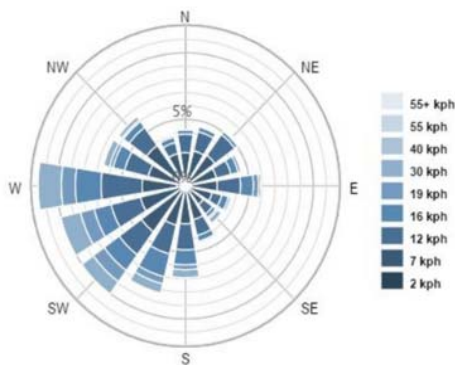
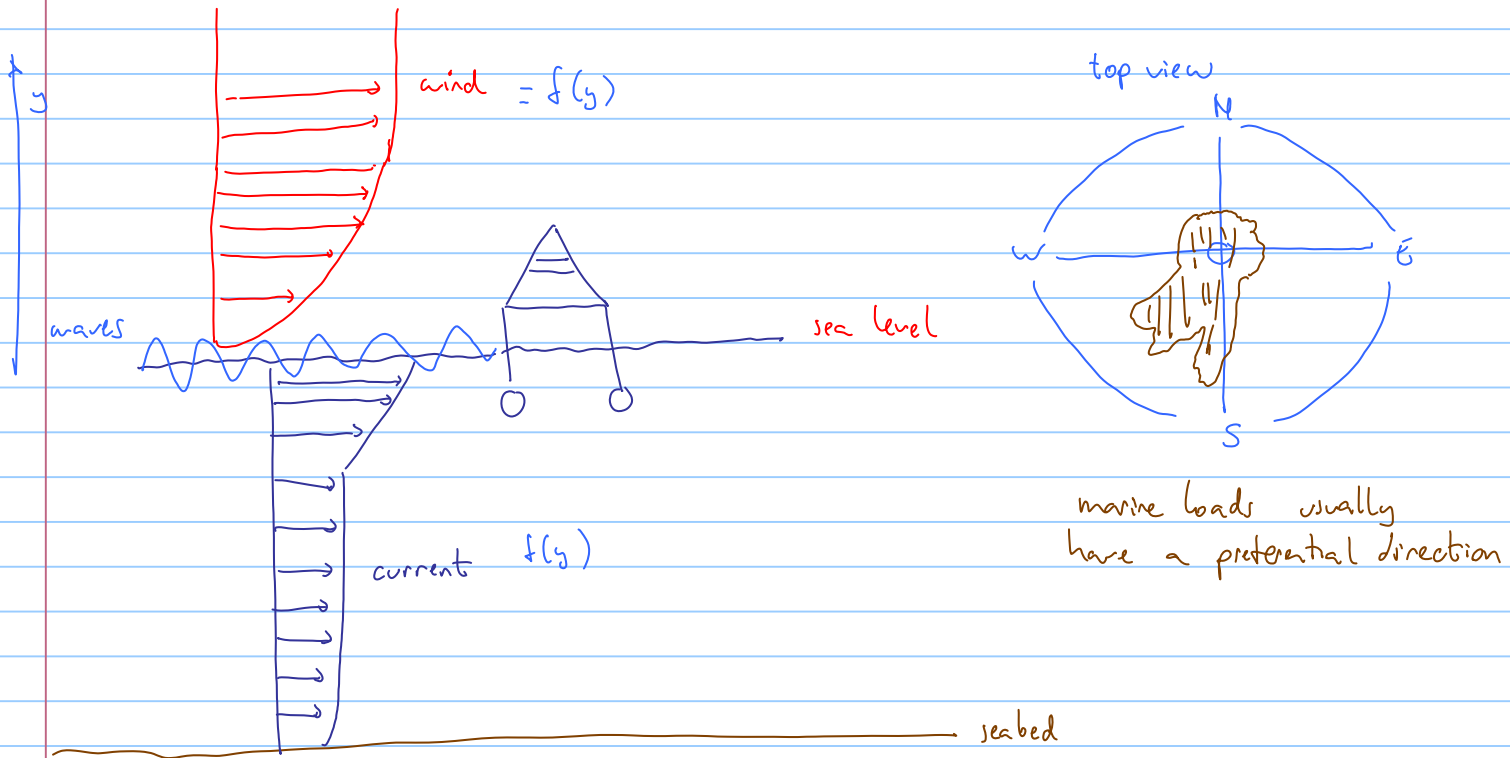
SPAR Aasta Hansteen it's the only spar with storage capacity  
(up to date) 150.000 bbls



- Marine loads on offshore structure { next class



## Marine loads in offshore structures



### • for practical purposes:

- wind is considered with a uniform constant value (exception some floating structures)

values vary with minutes

- current: the spatial variation is considered. Considered constant with time (a high value is usually used (100 years current))

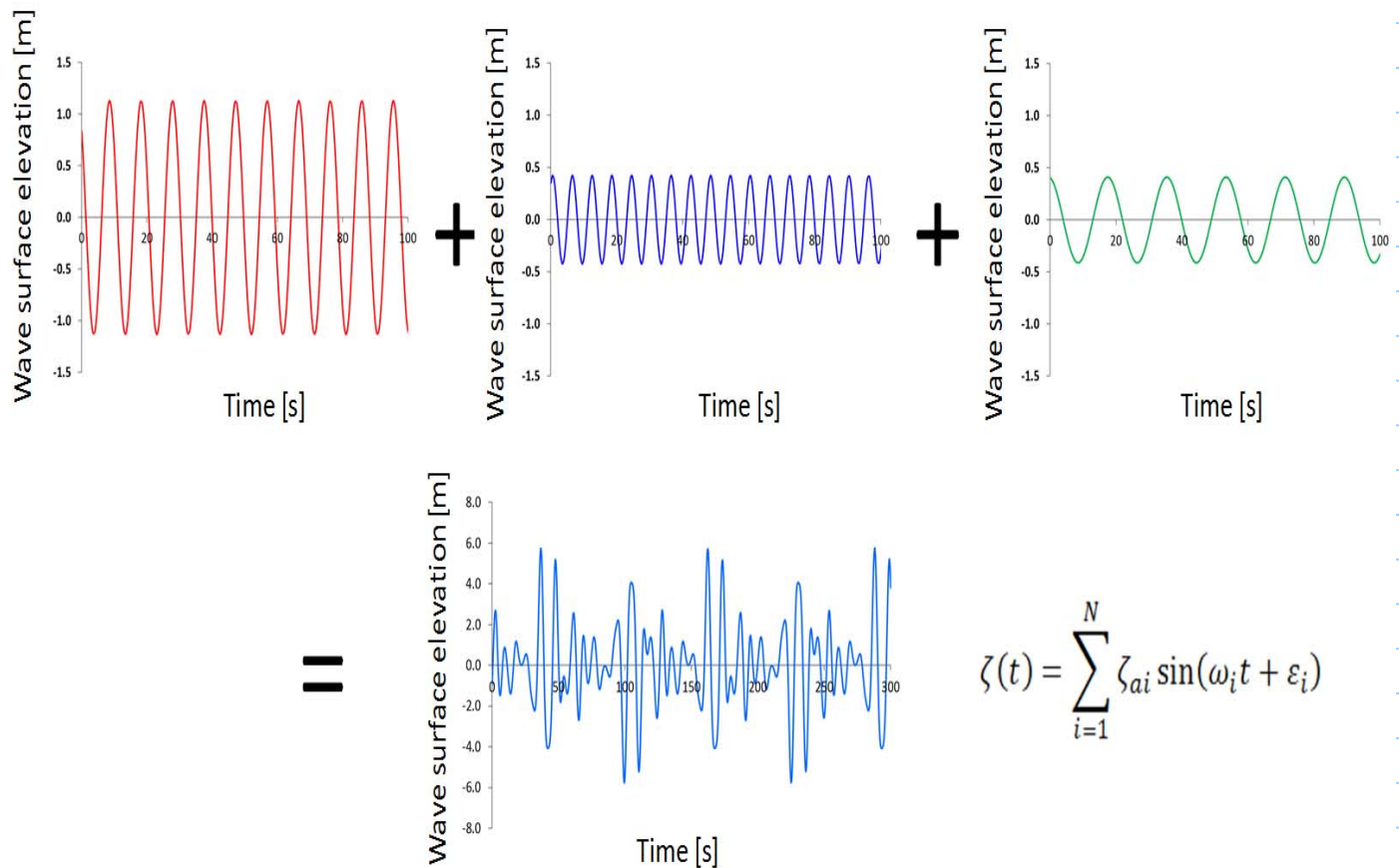
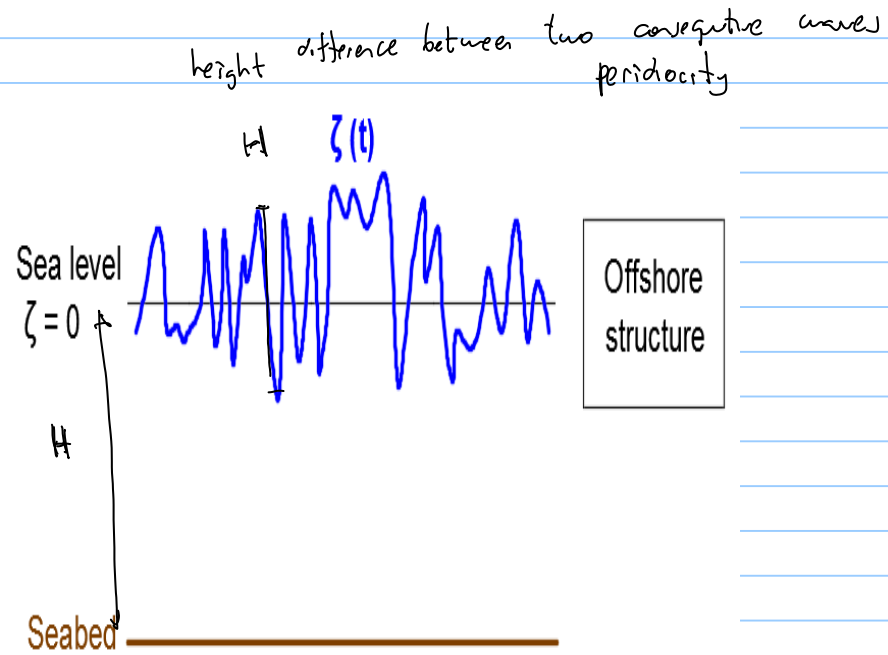
values usually change within hours

### • waves:

• waves

wave elevation

fourier theorem

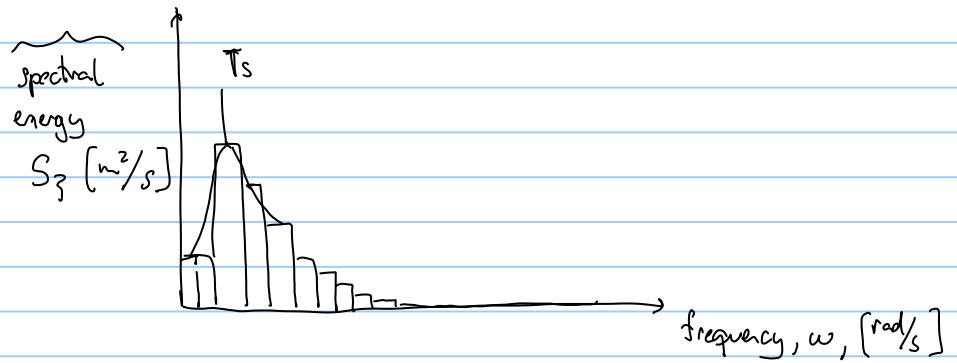


measurement of wave statistics

buoys attached to merchant ships  
measurement ships  
existing offshore structures.



FFT fast fourier transform



wave energy spectrum

To convert from energy to elevation:

$$\zeta_i = \sqrt{2 \cdot S_{\zeta_i} \cdot \Delta \omega_i}$$

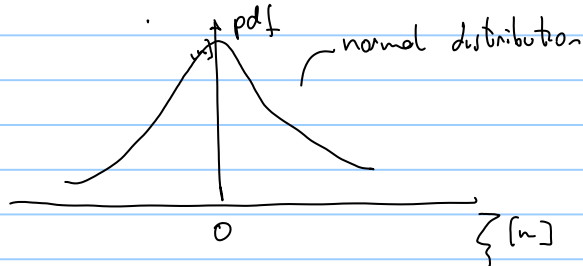
Some formulas that are typically used for spectrum

Pierson moskowitz (P-M)

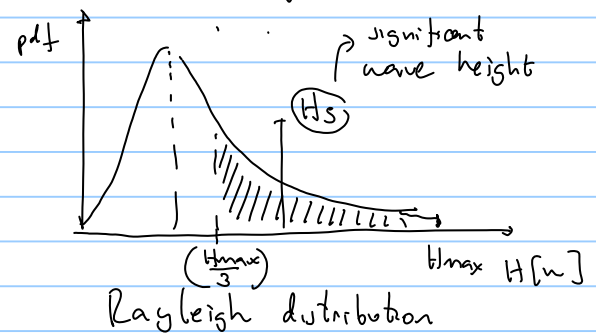
JONSWAP

for short periods of time (sea state)  $\rightarrow$  3hrs : there is a significant period near period which is dominant and is usually considered constant.

the wave elevation



the wave height



$T_s, H_s$  characterize a sea state

# Scatter diagram of long term wave statistics Aasta Hansteen for 15 years

	Spectral Peak period ( $T_p$ ) [s]																										
Hs [m]	0-3	3-4	4-5	5-6	6-7	7-8	8-9	9-10	10-11	11-12	12-13	13-14	14-15	15-16	16-17	17-18	18-19	19-20	20-21	21-22	22-23	23-24	24-25	Sum			
0-1	15	290	1367	2876	3716	3527	2734	1849	1138	656	362	192	101	52	26	13	7	3	2	1	0	0	0	18927			
1-2	1	81	1153	5308	12083	17323	18143	15262	10980	7053	4169	2316	1229	631	315	155	75	36	17	8	4	5	1	96348			
2-3	0	2	94	1050	4532	10304	15020	15953	13457	9752	5991	3403	1795	894	426	197	88	39	17	7	3	1	1	83026			
3-4	0	0	2	72	686	2782	6171	8847	9189	7493	5082	2991	1577	762	345	148	61	24	9	4	1	0	0	46246			
4-5	0	0	0	2	51	433	1645	3495	4807	4750	3638	2286	1229	584	251	100	37	13	5	1	0	0	0	23327			
5-6	0	0	0	0	2	39	294	1037	2069	2664	2440	1709	968	463	193	72	25	8	2	1	0	0	0	11986			
6-7	0	0	0	0	0	2	32	215	692	1264	1485	1228	767	382	159	57	18	5	1	0	0	0	0	6307			
7-8	0	0	0	0	0	0	2	27	157	447	730	762	555	302	130	46	14	4	1	0	0	0	0	3177			
8-9	0	0	0	0	0	0	0	2	23	112	276	392	355	223	104	38	11	3	1	0	0	0	0	1540			
9-10	0	0	0	0	0	0	0	0	2	19	77	160	192	148	79	31	9	2	0	0	0	0	0	719			
10-11	0	0	0	0	0	0	0	0	0	2	16	50	85	85	55	24	8	2	0	0	0	0	0	327			
11-12	0	0	0	0	0	0	0	0	0	0	2	12	29	40	33	18	7	2	0	0	0	0	0	143			
12-13	0	0	0	0	0	0	0	0	0	0	0	2	8	15	17	12	5	2	0	0	0	0	0	61			
13-14	0	0	0	0	0	0	0	0	0	0	0	0	2	5	7	6	4	1	0	0	0	0	0	25			
14-15	0	0	0	0	0	0	0	0	0	0	0	0	0	1	2	3	2	1	0	0	0	0	0	9			
15-16	0	0	0	0	0	0	0	0	0	0	0	0	0	0	1	1	1	1	0	0	0	0	0	4			
16-17	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0			
17-18	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0			
Sum	16	373	2616	9308	21070	34410	44041	46687	42514	34212	24268	15503	8892	4587	2143	921	372	146	55	22	8	6	2	292172			

Design is usually made using values for longer periods. thus an extrapolation is required.

looking at  $T_p \sim$  spectral peak period



$H_{s[15 \text{ years}]} =$   
 $15 \text{ years} \sim 292000 \text{ states of } (3 \text{ h})$

it has an associated probability of  $\left( \frac{1}{292000} = 7.6 \times 10^{-6} \right)$

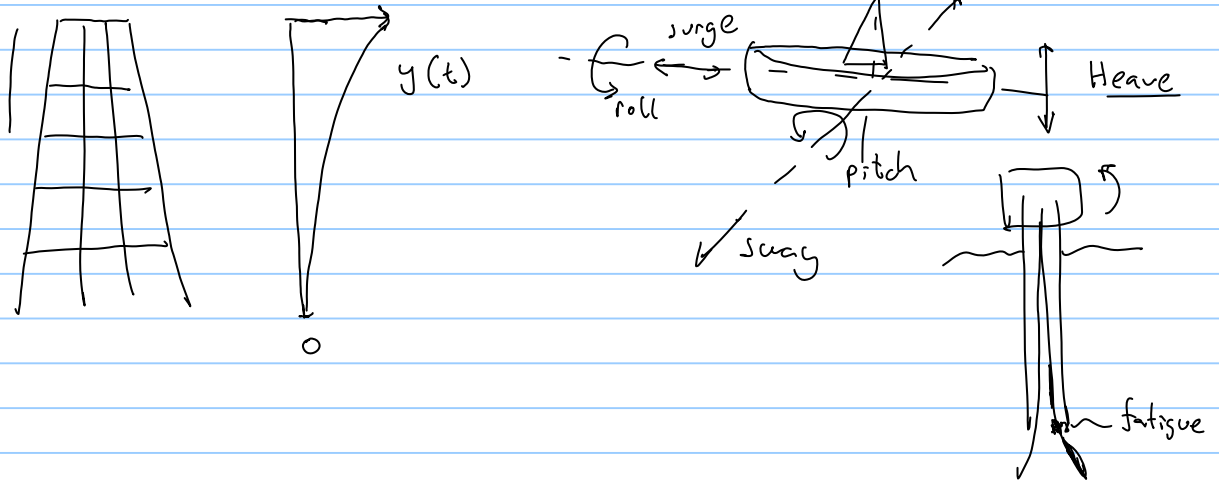
we assume that significant wave heights in different time periods follow a logarithmic equation

$$\log(P(H)) = \frac{1}{a} H$$

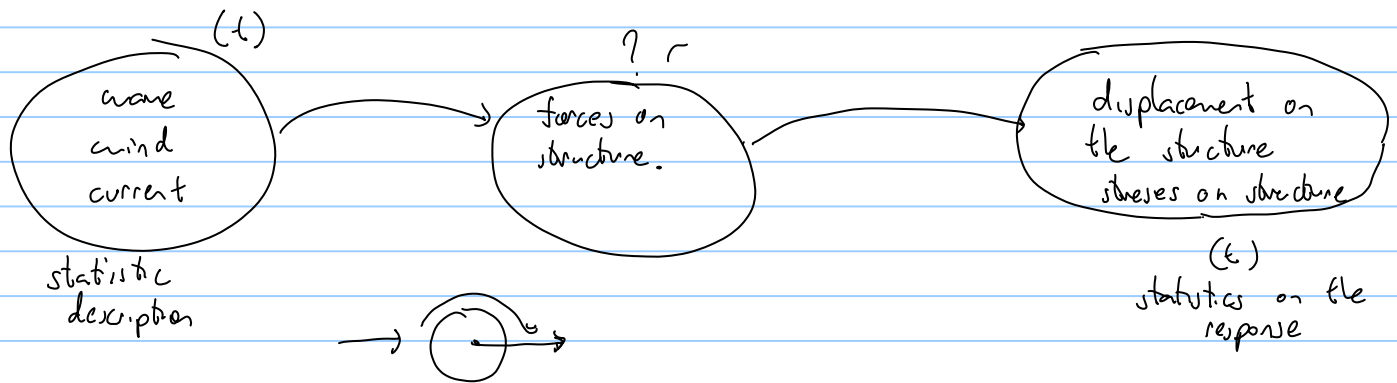
$$\log(7.6 \times 10^{-6}) = \frac{1}{a} H_{15}$$



- Calculation of displacements of offshore structures  
bottom supported structures



- $H_{s(100 \text{ years})}$  is used to design deck height



three types of analysis are usually made

- Design wave  $H_{s,100} \rightarrow$  with a range of periods.  $NORSOK N-003$  suggests using  $\sqrt{6.5 H_{s,100}} \leq T \leq \sqrt{11 H_{s,100}}$   
 $H_{s,100} = 1.9 \cdot H_s$

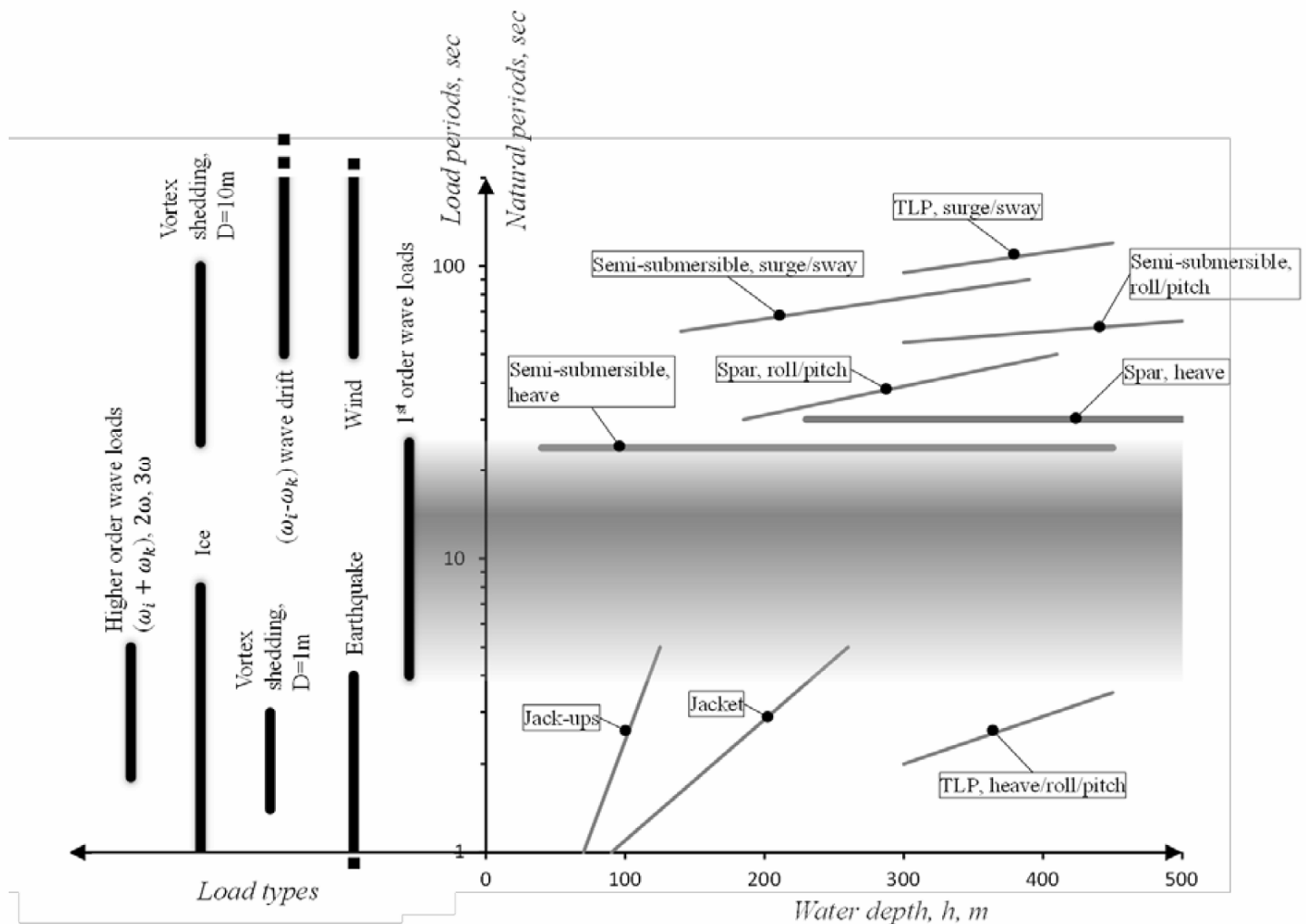
- short term design  $H_s, T_s \rightarrow$  usually to calculate maximum loads and stresses on components, storm

- long term design: varying  $H_s, T_s$ , is usually used to calculate fatigue.

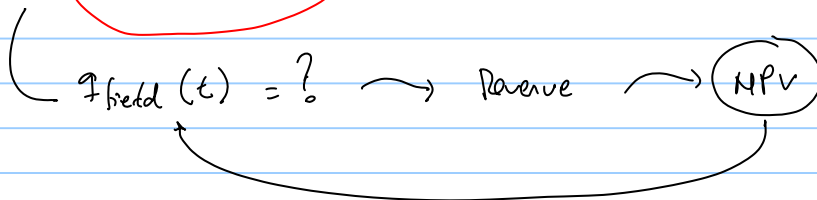
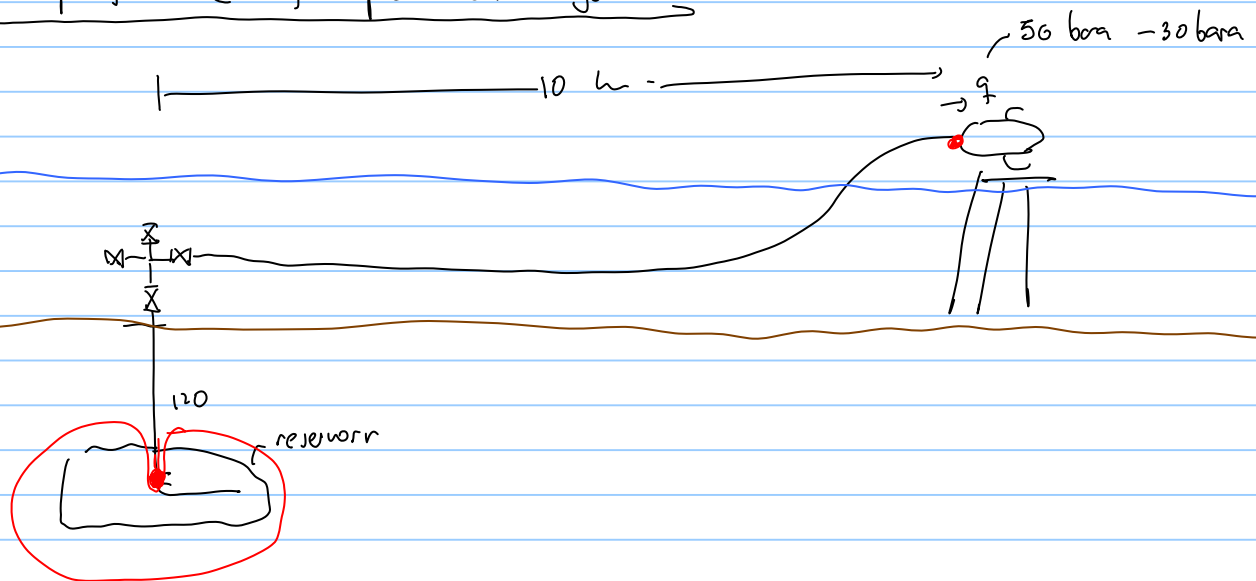
Each offshore structure has a natural frequency  $\left\{ \begin{array}{l} \text{flexibility of structure} \\ \text{weight of structure} \\ \text{damping of structure} \end{array} \right.$



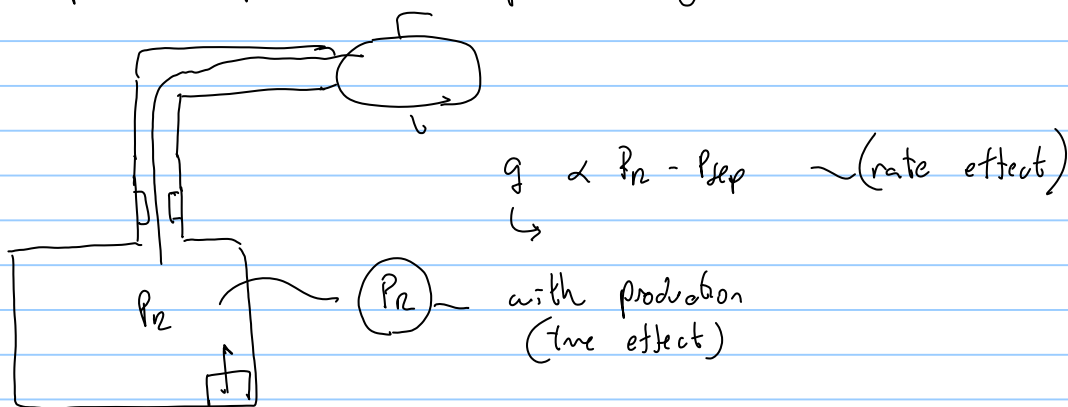
Resonance excite the structure with natural frequency and amplitudes will be <sup>big</sup>  
 stress and loads are usually big



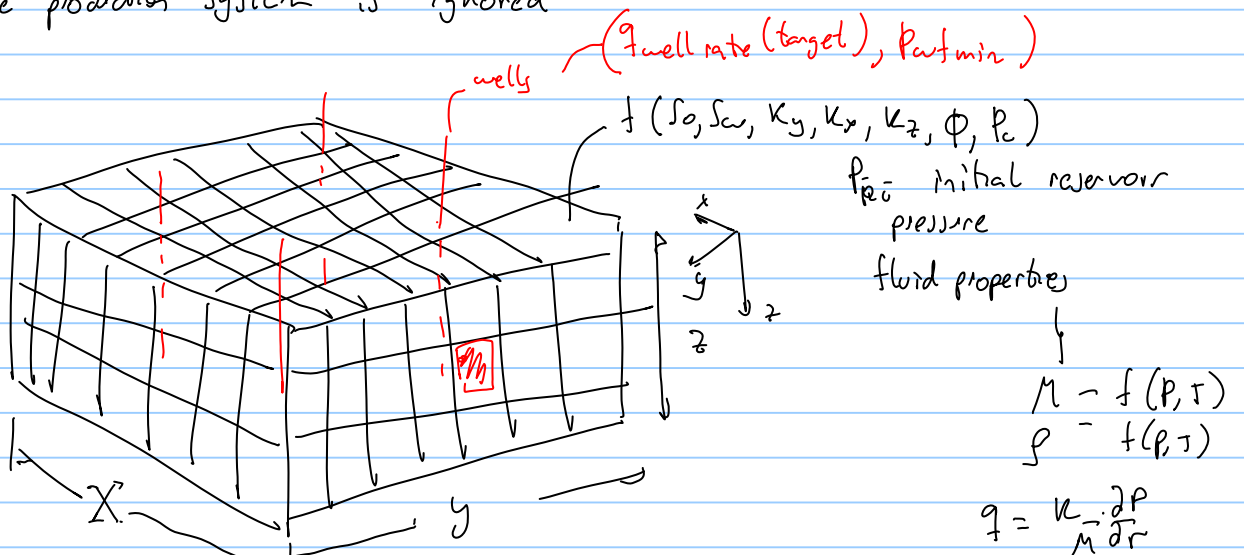
## Flow performance of production system:



to compute the performance of production system we use numerical models



In early phases of field development reservoir simulator is often used and the surface production system is ignored



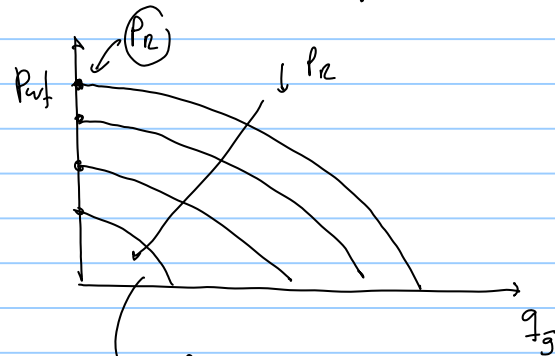
Result of reservoir simulator  $\omega$   $p_{wf}^i(t)$   
 $q_w^i(t)$

Snowhite. dry gas example. Proxy  $\rightarrow$  surrogate of a reservoir model



• material balance  $\rightarrow$

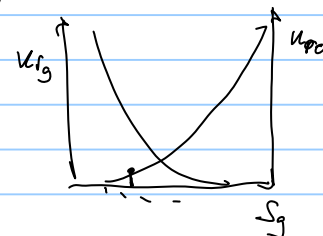
• productivity of well IPR  
 in flow performance relationship



Backpressure equation

$$q_g = C_R (p_R^2 - p_{wf}^2)^n$$

$\leftarrow k, \mu, S$



material balance  $\int_0^t q_g dt$

$$p_R z_i \left( 1 - \frac{G_p}{G} \right) = p_i z_i \left( 1 - \frac{G_p}{G} \right)$$

$\leftarrow$  initial reservoir pressure  
 $\leftarrow$  initial deviation factor  
 $\leftarrow$  deviation factor @ current  $p_R$

$\leftarrow$  initial gas in place

<https://www.youtube.com/watch?v=ssmJrENliwq&list=PLqktb39S1tGcix-up7-23QyYhNeUuhMX0&index=1>

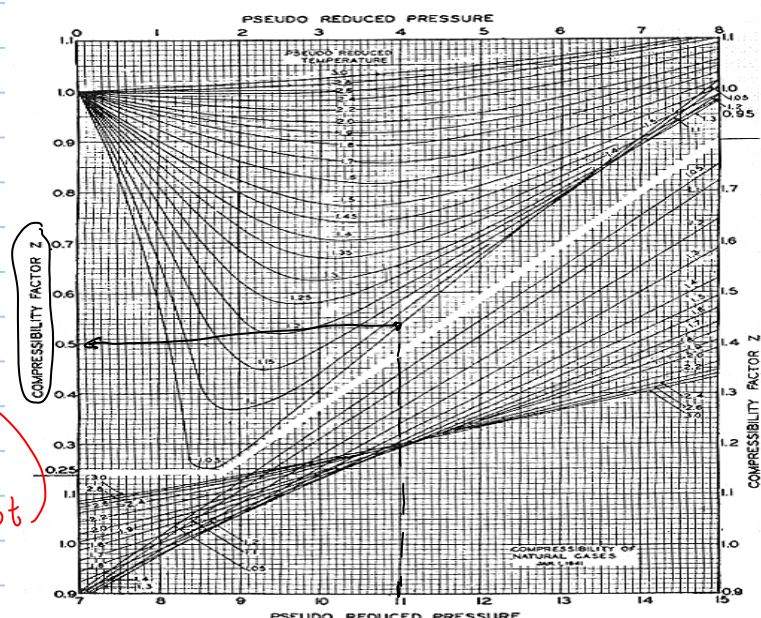
provide  $p_i, z_i, \frac{R_F}{G_p, G}$

$$z = f\left(\frac{p}{p_c}, \frac{T}{T_c}\right)$$

$$p_c, T_c = f(p_g)$$

implicit equation

- assume  $p_R$ , calculate  $z$
- calculate  $p_R$  from MB
- check if  $p_{calc} = p_{assum}$ . if not



[http://folk.ntnu.no/stanko/Courses/TPG4230/2017/Class\\_files/20170214/](http://folk.ntnu.no/stanko/Courses/TPG4230/2017/Class_files/20170214/)

Annual oftake for gas  $(2-3\%)(G)$   
 $20 \text{E}6 \text{ Sm}^3/\text{d}$

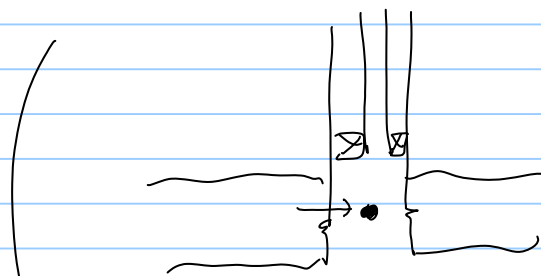
### Atila East gas Field (Base Case Data)

G=IGIP	270E+09 Sm <sup>3</sup>
T <sub>R</sub>	92 oC
P <sub>i</sub> , initial Res pressure	276 bara
C, inflow Back pressure coefficient	1000 Sm <sup>3</sup> /bar <sup>2n</sup>
n, backpressure, exponent	1
Gas molecular weight (Methane)	16 kg/kmole
Gas specific gravity	0.55 Gas specific gravity
Number of wells	4
pwfmin	120 [bara]
qfield_target	2.00E+07 [Sm <sup>3</sup> /d]

time	qw <sub>well_pot</sub>	q <sub>field_pot</sub>	q <sub>field</sub>	ΔG <sub>p</sub>	G <sub>p</sub>	Z	RF	PR
[years]	[Sm <sup>3</sup> /d]	[Sm <sup>3</sup> /d]	[Sm <sup>3</sup> /d]	[Sm <sup>3</sup> ]	[Sm <sup>3</sup> ]	[-]	[-]	[bara]
0				0.00E+00		0.9672446		276
1								
2								
3								
4								
5								
6								
7								
8								
9								
10								

the end of  
the year

Calculating well potential by applying the provided pwf<sub>min</sub> in the sand phase



$$q_s = C_0 (P_R(t)^2 - P_{wfmin}^2)^n$$

$q_{s,por}$  = maximum rate that the well can produce

$q_{s,pot} > q_{s,target}$  the target rate provided is feasible  
 $q_{s,pot} < q_{s,target}$  i cannot produce the target rate provided

Predicting production profile of Snohvit field - Reservoir simulator proxy - Milan Stanko, 20170214

**Snohvit gas Field**

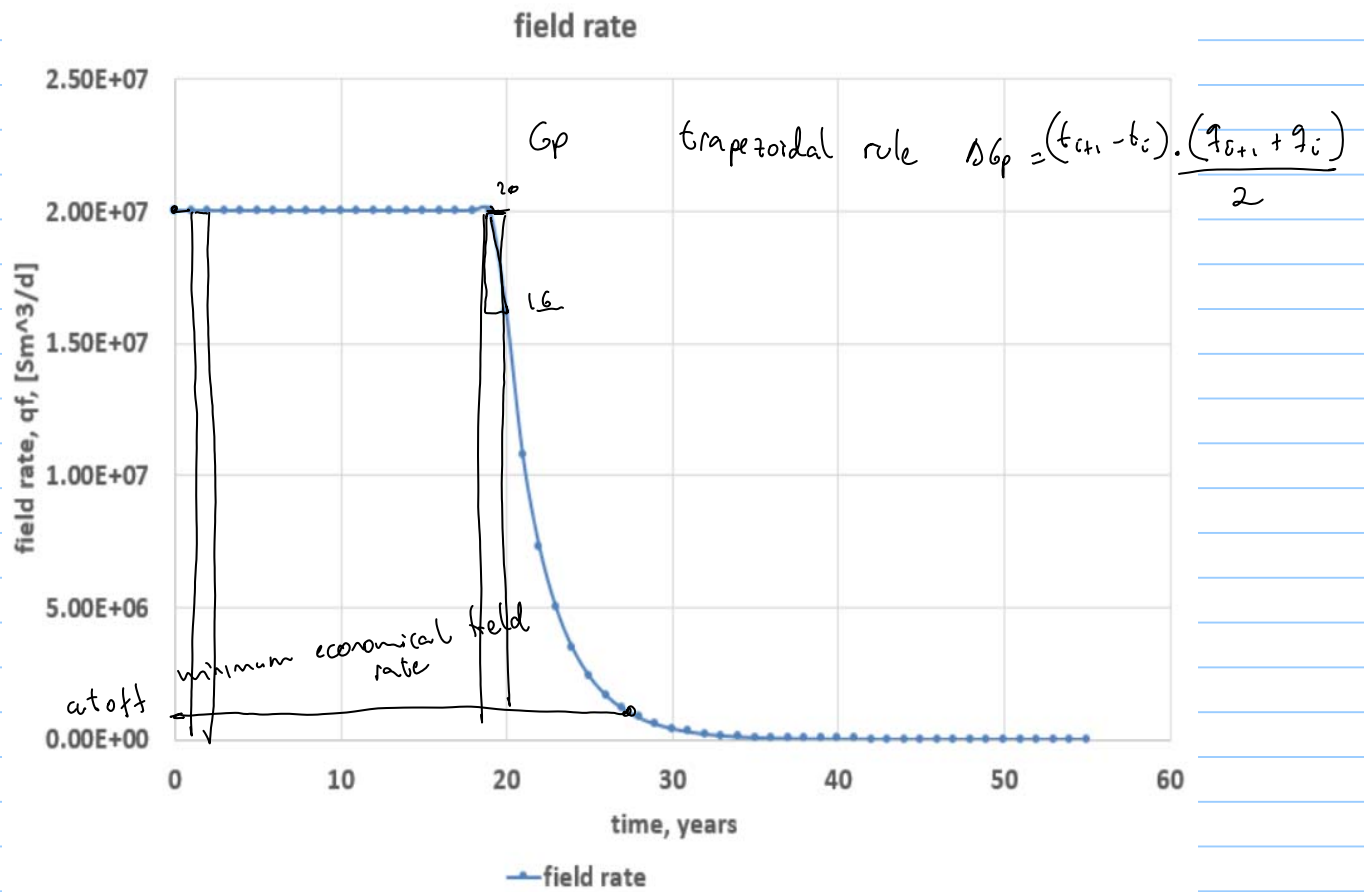
G=IGIP	270E+09 Sm3
T <sub>R</sub>	92 oC
P <sub>i</sub> initial Res pressure	276 bara
C, inflow Back pressure coefficient	1000 Sm3/bar^2n
n, backpressure, exponent	1
Gas molecular weight (Methane)	16 kg/kmole
Gas specific gravity	0.55 Gas specific gravity
Number of wells	4
pwfmin	120 [bara]
qfield_target	2.00E+07 [Sm^3/d]

	time	qwll_pot	qfield_pot	qfield	pwf	ΔGp	Gp	Z	RF	PR
	[years]	[Sm^3/d]	[Sm^3/d]	[Sm^3/d]	[bara]	[Sm^3]	[Sm^3]	[-]	[-]	[bara]
	0	61776000	2.47E+08	2.00E+07	267	0.00E+00	0.00E+00	0.9672446	000.0E+0	276
	1	58113872.7	2.32E+08	2.00E+07	260	6.57E+09	6.57E+09	0.9672446	24.3E-3	269
	2	53941551.6	2.16E+08	2.00E+07	252	6.57E+09	1.31E+10	0.9630236	48.7E-3	261
	3	49857914.9	1.99E+08	2.00E+07	243	6.57E+09	1.97E+10	0.9583206	73.0E-3	253
	4	45961532.4	1.84E+08	2.00E+07	235	6.57E+09	2.63E+10	0.9538497	97.3E-3	246
	5	42258575.5	1.69E+08	2.00E+07	227	6.57E+09	3.29E+10	0.9497312	121.7E-3	238
	6	38740056.4	1.55E+08	2.00E+07	219	6.57E+09	3.94E+10	0.9459766	146.0E-3	231
	7	35395346.7	1.42E+08	2.00E+07	212	6.57E+09	4.60E+10	0.9425795	170.3E-3	223
	8	32214305.9	1.29E+08	2.00E+07	204	6.57E+09	5.26E+10	0.9395311	194.7E-3	216
	9	29187545.5	1.17E+08	2.00E+07	196	6.57E+09	5.91E+10	0.9368227	219.0E-3	209
	10	26306418.5	1.05E+08	2.00E+07	189	6.57E+09	6.57E+10	0.9344457	243.3E-3	202
	11	23562975	9.43E+07	2.00E+07	182	6.57E+09	7.23E+10	0.932392	267.7E-3	195
	12	20949917.2	8.38E+07	2.00E+07	174	6.57E+09	7.88E+10	0.9306539	292.0E-3	188
	13	18460558.4	7.38E+07	2.00E+07	167	6.57E+09	8.54E+10	0.9292238	316.3E-3	181
	14	16088783.8	6.44E+07	2.00E+07	160	6.57E+09	9.20E+10	0.9280946	340.7E-3	175
	15	13829016.2	5.53E+07	2.00E+07	152	6.57E+09	9.86E+10	0.9272597	365.0E-3	168
	16	11676183.7	4.67E+07	2.00E+07	145	6.57E+09	1.05E+11	0.9267125	389.3E-3	161
	17	9625689.72	3.85E+07	2.00E+07	138	6.57E+09	1.12E+11	0.926447	413.7E-3	155
	18	7673386.72	3.07E+07	2.00E+07	131	6.57E+09	1.18E+11	0.9264573	438.0E-3	149
	19	5815551.3	2.33E+07	2.00E+07	123	6.57E+09	1.25E+11	0.9267379	462.3E-3	142
	20	4048861.89	1.62E+07	1.62E+07	120	6.57E+09	1.31E+11	0.9272836	486.7E-3	136
	21	2689377.84	1.08E+07	1.08E+07	120	5.32E+09	1.37E+11	0.9280894	506.4E-3	131
	22	1824335.63	7.30E+06	7.30E+06	120	3.53E+09	1.40E+11	0.928925	519.5E-3	127
	23	1251902.59	5.01E+06	5.01E+06	120	2.40E+09	1.43E+11	0.9295651	528.3E-3	125
	24	865700.421	3.46E+06	3.46E+06	120	1.65E+09	1.44E+11	0.9300388	534.4E-3	124
	25	601733.801	2.41E+06	2.41E+06	120	1.14E+09	1.45E+11	0.9303821	538.6E-3	122

In this time, potential rate is smaller than the target rate. The mode changes to constant bottomhole pressure

MIN : =IF(D16>=\$B\$12,\$B\$12,D16)

	A	B	C	D	E	F	G	H	I	J	K	L
1	Predicting production profile of Snohvit field - Reservoir simulator proxy - Milan Stanko, 20170214											
2	<b>Snohvit gas Field</b>											
3	G=IGIP	270E+09 Sm3										
4	T <sub>R</sub>	92 oC										
5	P <sub>i</sub> initial Res pressure	276 bara										
6	C, inflow Back pressure coefficient	1000 Sm3/bar^2n										
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9	Gas specific gravity	0.55 Gas specific gravity										
10	Number of wells	4										
11	pwfmin	120 [bara]										
12	qfield_target	2.00E+07 [Sm^3/d]										
13												
14		time	qwll_pot	qfield_pot	qfield	pwf	ΔGp	Gp	Z	RF	PR	
15		[years]	[Sm^3/d]	[Sm^3/d]	[Sm^3/d]	[bara]	[Sm^3]	[Sm^3]	[-]	[-]	[bara]	
16		0	61776000	2.47E+08	=IF(D16>=\$B\$12,\$B\$12,D16)	267	0.00E+00	0.00E+00	0.9672446	000.0E+0	276	
17		1	58113872.7	2.32E+08	2.00E+07	260	6.57E+09	6.57E+09	0.9672446	24.3E-3	269	
18		2	53941551.6	2.16E+08	2.00E+07	252	6.57E+09	1.31E+10	0.9630236	48.7E-3	261	
19		3	49857914.9	1.99E+08	2.00E+07	243	6.57E+09	1.97E+10	0.9583206	73.0E-3	253	
20		4	45961532.4	1.84E+08	2.00E+07	235	6.57E+09	2.63E+10	0.9538497	97.3E-3	246	
21		5	42258575.5	1.69E+08	2.00E+07	227	6.57E+09	3.29E+10	0.9497312	121.7E-3	238	



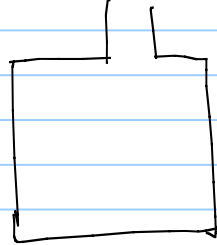


How do we predict reservoir performance

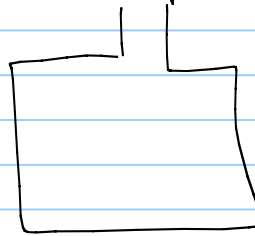
RF  
 $q_o, q_g, q_w$  vs time  
 $P_{wf}$  flowing bottomhole pressures  
 for each well

- material balance

tank approach with uniform properties



$n_{gi}$

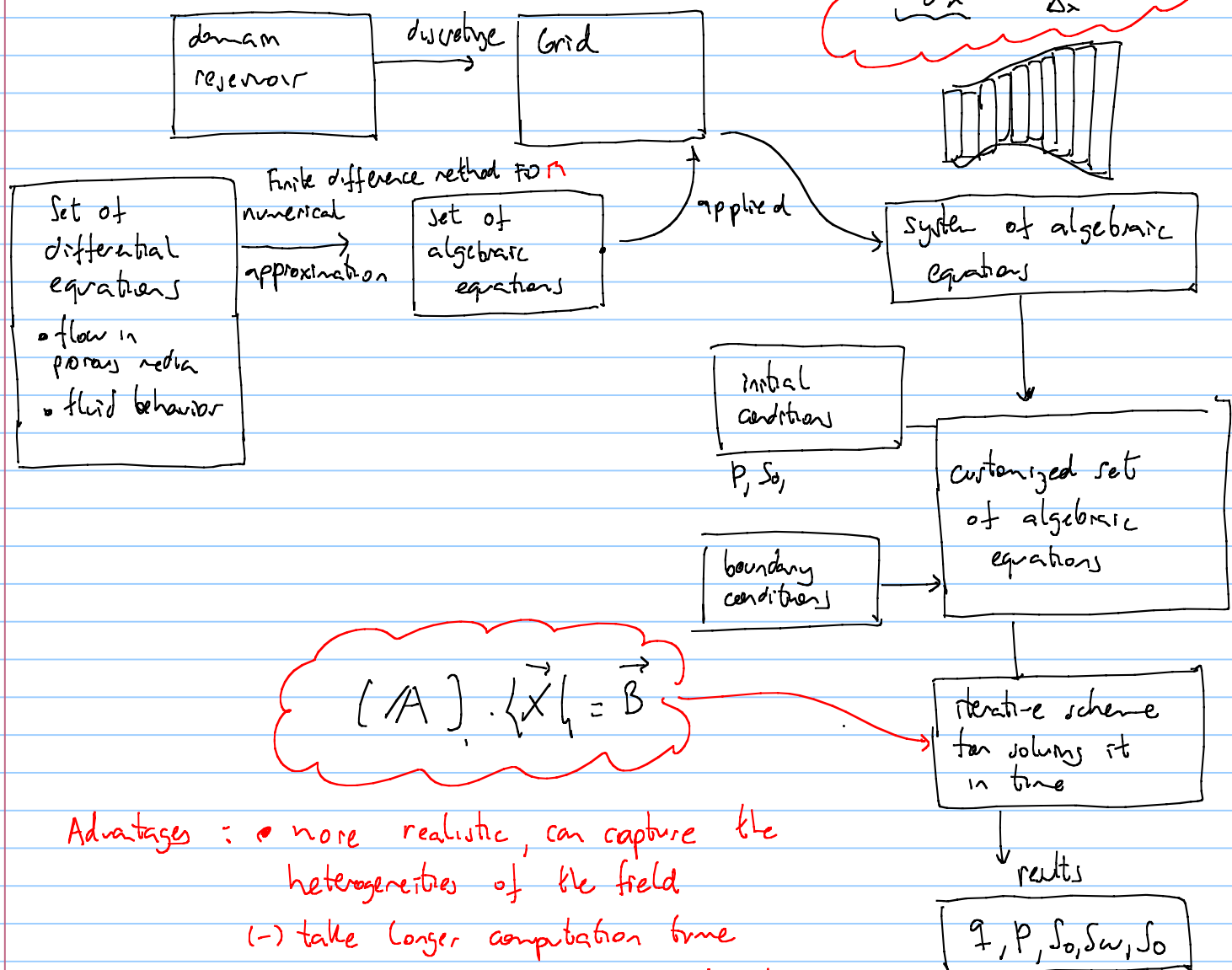


$n_{gi+1}$

$$n_{gi+1} - n_{gi} = \Delta h$$

$P$   
 $+$   
 $S_o, S_w, S_g$   
 $K$   
 $\phi$

- Reservoir simulator



FDM

$$\frac{\partial p}{\partial x} = \frac{p_{i+1} - p_i}{\Delta x}$$

$$[A] \cdot \{X\} = \vec{B}$$

Advantages : • more realistic, can capture the heterogeneities of the field

(-) take longer computation time

(-) requires large input ~ in early phase we need to extrapolate or assume



water :

$$\nabla_o \left[ \frac{[k]k_{rw}}{\mu_w B_w} (\nabla p_w - \gamma_w \nabla d) \right] + Q_w = \frac{\partial}{\partial t} \left( \phi \frac{S_w}{B_w} \right)$$

oil :

$$\nabla_o \left[ \frac{[k]k_{ro}}{\mu_o B_o} (\nabla p_o - \gamma_o \nabla d) \right] + Q_o = \frac{\partial}{\partial t} \left( \phi \frac{S_o}{B_o} \right)$$

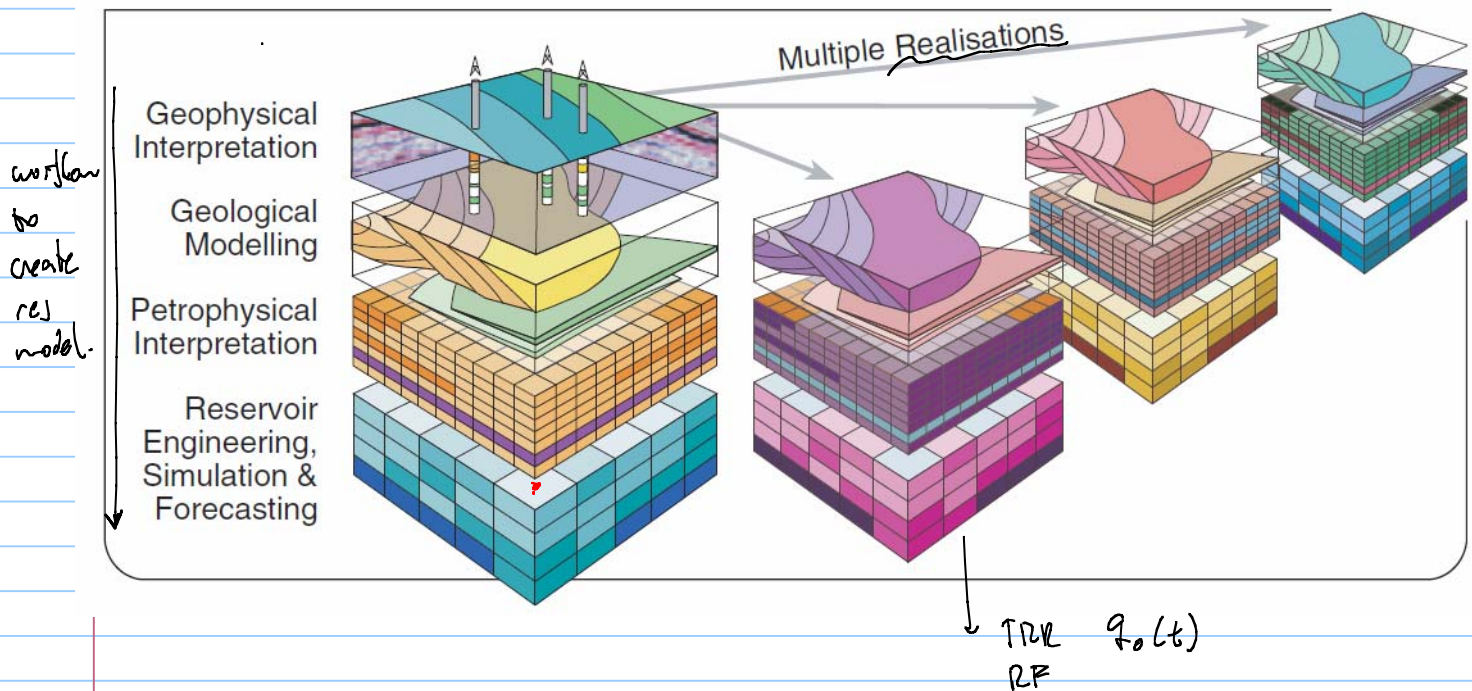
gas :

$$\nabla_o \left[ \frac{[k]k_{rg}}{\mu_g B_g} (\nabla p_g - \gamma_g \nabla d) \right] + \nabla_o \left[ \frac{[k]k_{ro}}{\mu_o B_o} R_s (\nabla p_o - \gamma_o \nabla d) \right] + Q_g = \frac{\partial}{\partial t} \left( \phi \frac{S_g}{B_g} + \phi \frac{S_o R_s}{B_o} \right)$$

water :

$$\Delta_y T_{wy} \Delta_y \Psi_w = \left( \frac{k_y k_{rw}}{\mu_w B_w \Delta y} \right)_{j+1/2} \Delta x_i \Delta z_k (\Psi_{w,j+1} - \Psi_{w,j}) - \left( \frac{k_y k_{rw}}{\mu_w B_w \Delta y} \right)_{j-1/2} \Delta x_i \Delta z_k (\Psi_{w,j} - \Psi_{w,j-1})$$

there is a high uncertainty in the subsurface



there are 3 ways to address uncertainty in the creation of the subsurface model

- Define a base case ~ the most likely realization
- run sensitivity analysis on that case.

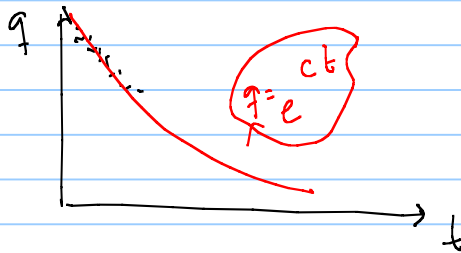
- define a limited number of cases (4-5) - assign a probability to each case. ask expert \$\$\$  
0-0  
sum

↳ run sensitivity analysis on each one of the realizations

- built a stochastic model and compute the most likely outcome using Monte-Carlo, latin Hypercube sampling. ✓

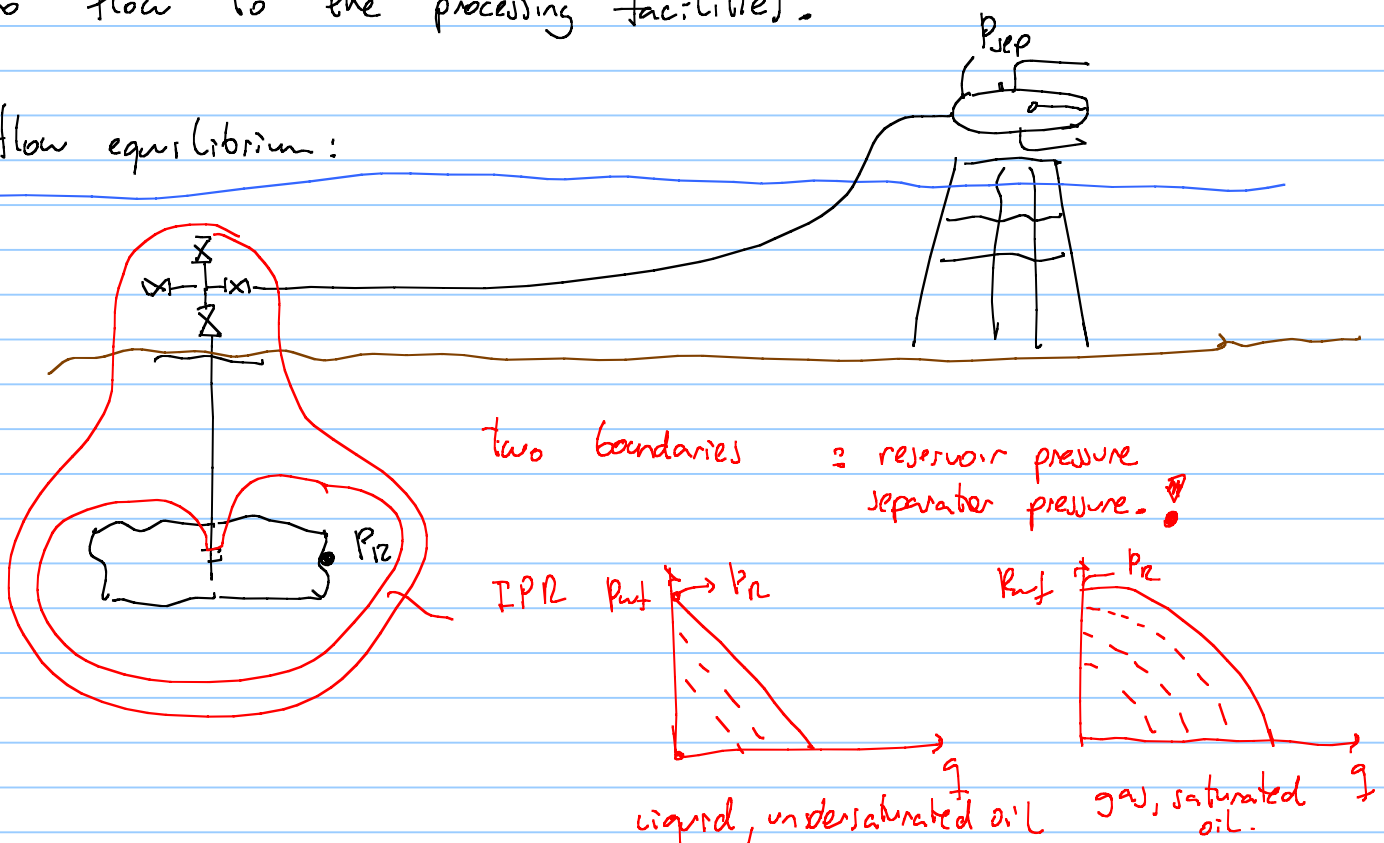
↳ very computationally expensive process due to the high number of cells and variables per cell.

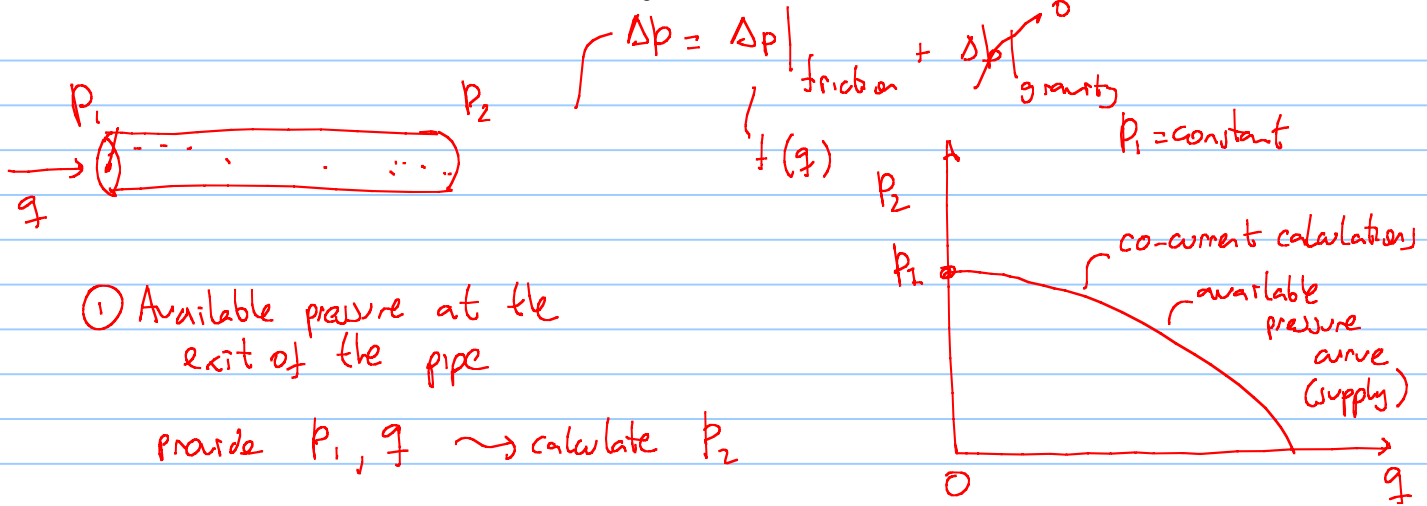
- decline curve analysis (DCA) { material balance equation + IPR equation  
+ empirical information



How to capture properly the pressure required at the bottom hole to flow to the processing facilities?

flow equilibrium:



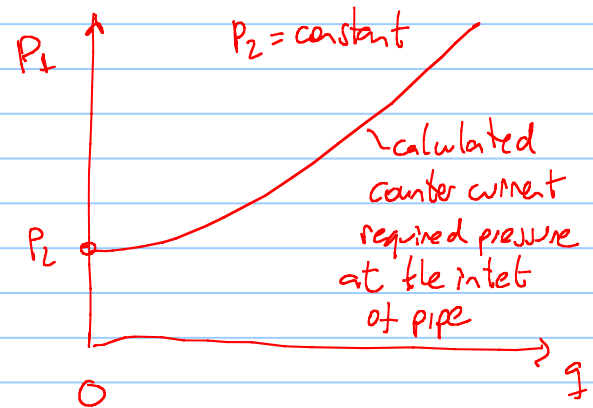


② Required pressure at the inlet of the pipe

provide  $P_2, q \rightarrow$  calculate  $P_1$

$$P_1 - P_2 = \Delta p$$

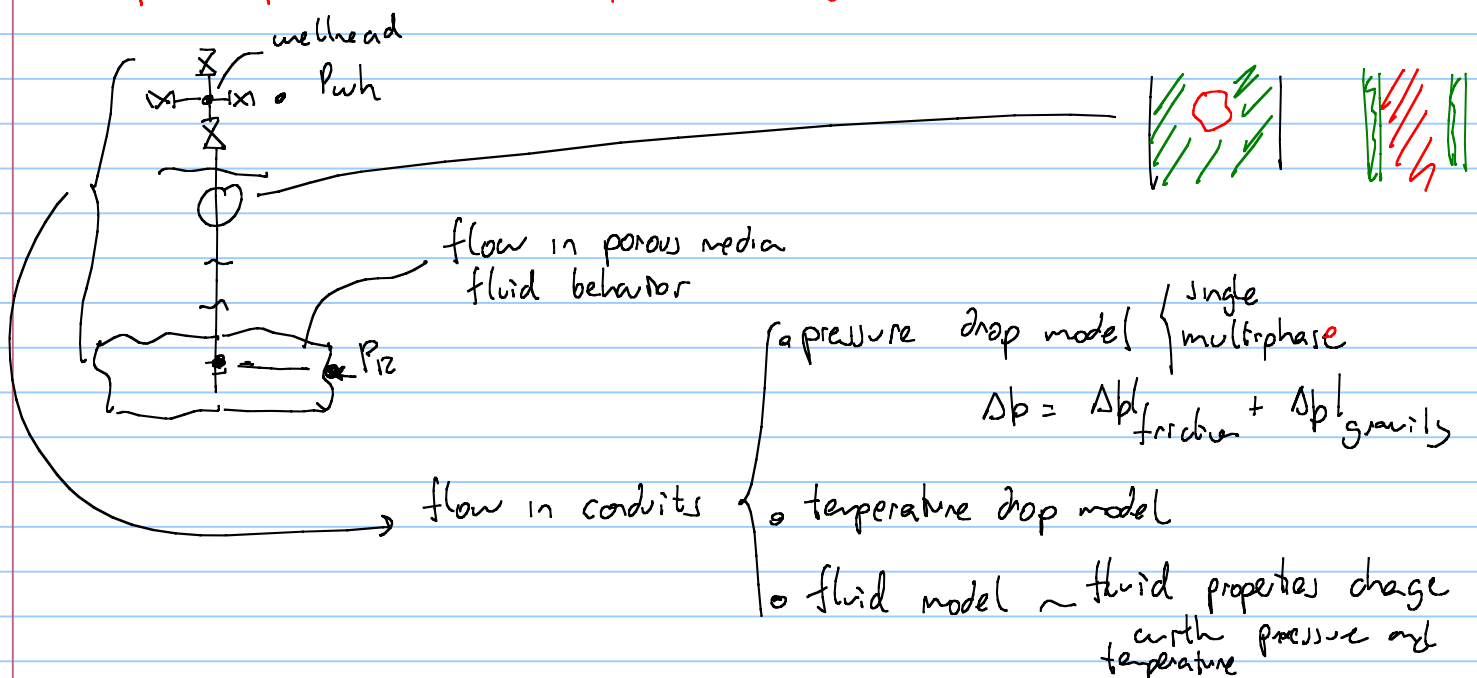
$$P_1 = P_2 + \Delta p$$

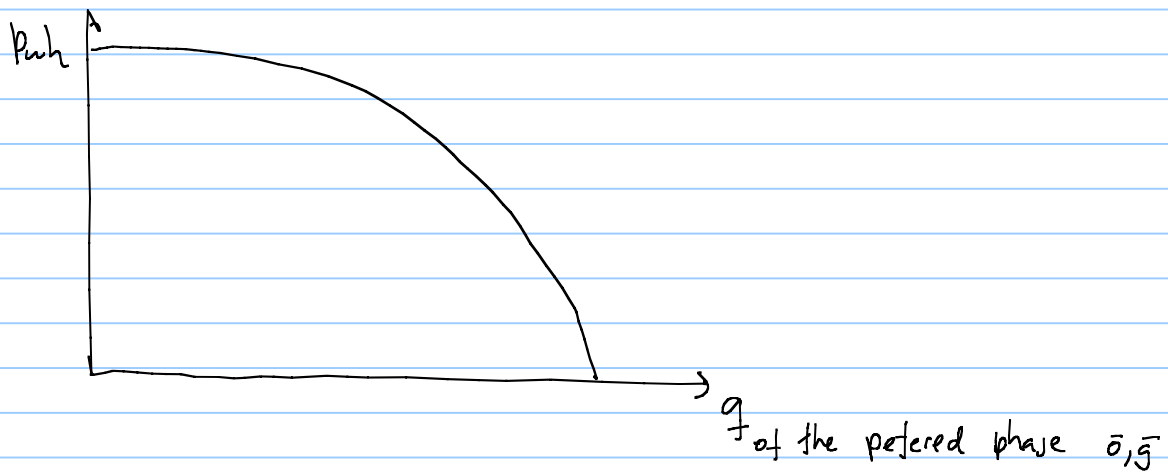


③ Calculate rate

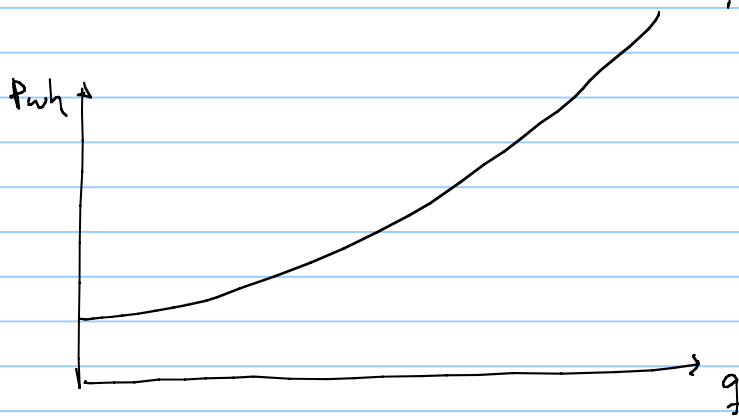
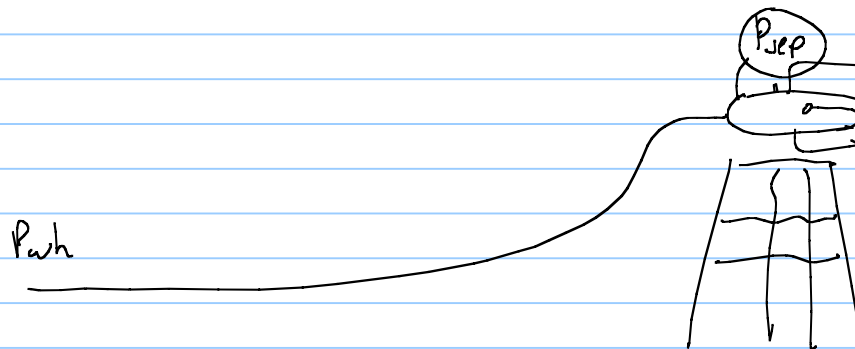
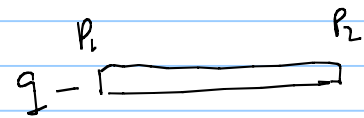
provide  $P_1, P_2 \rightarrow$  calculate  $q$

I can use available and required pressure curves to characterize complex parts of the production system

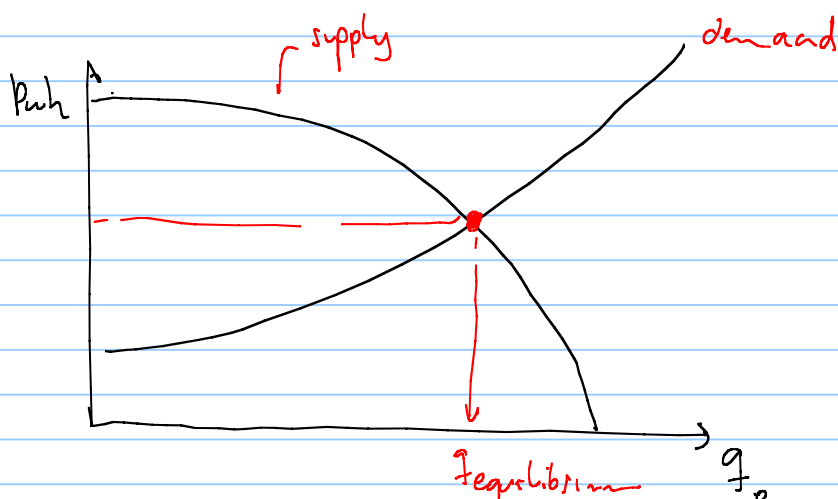




looking at the rest of the system



the only feasible operating rate is the intersection of both curves



one example with dry gas

$$\text{IPR} = q_g = C (p_R^2 - p_{wf}^2)^n$$

tubing =

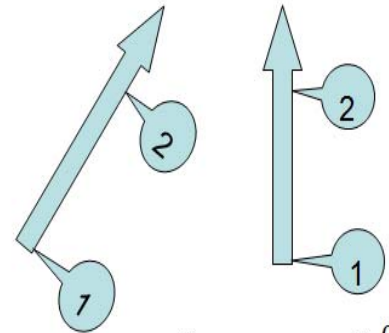
## Tubing flow Equation-Dry gas

remember pressure drop depends on the velocity.  $\frac{q_{\text{local}}}{A}$

$$q_{sc} = \left( \frac{\pi}{4} \right) \left( \frac{R}{M_{\text{air}}} \right)^{0.5} \left( \frac{T_{sc}}{P_{sc}} \right) \left[ \frac{D^5}{\gamma_g f_M (Z_{\text{av}} T_{\text{av}} L)} \right]^{0.5} \left( \frac{s e^s}{e^s - 1} \right)^{0.5} \left( \frac{p_1^2}{e^s} - p_2^2 \right)^{0.5}$$

$$\frac{s}{2} = \frac{M_g g}{Z_{\text{av}} R T_{\text{av}}} H = \frac{(28.97) \gamma_g g}{Z_{\text{av}} R T_{\text{av}}} H$$

$$q_{gsc} = C_T \left( \frac{p_1^2}{e^s} - p_2^2 \right)^{0.5}$$



$$p_{\text{inlet}} = p_1 = e^{s/2} \left( p_2^2 + \frac{q_g^2}{C_T^2} \right)^{0.5}$$

$$p_{\text{wh}} = p_2 = \left( \frac{p_1^2}{e^s} - \frac{q_g^2}{C_T^2} \right)^{0.5}$$

tubing equation  $q_g = C_T \left( \frac{p_1^2}{e^s} - p_2^2 \right)^{0.5}$

for dry gas, horizontal line

$$q_g = C_{FL} (p_1^2 - p_2^2)^{0.5}$$

let's find mathematically the equilibrium rate

Known  
blue

$$q_g = C (p_R^2 - p_{wf}^2)^n$$

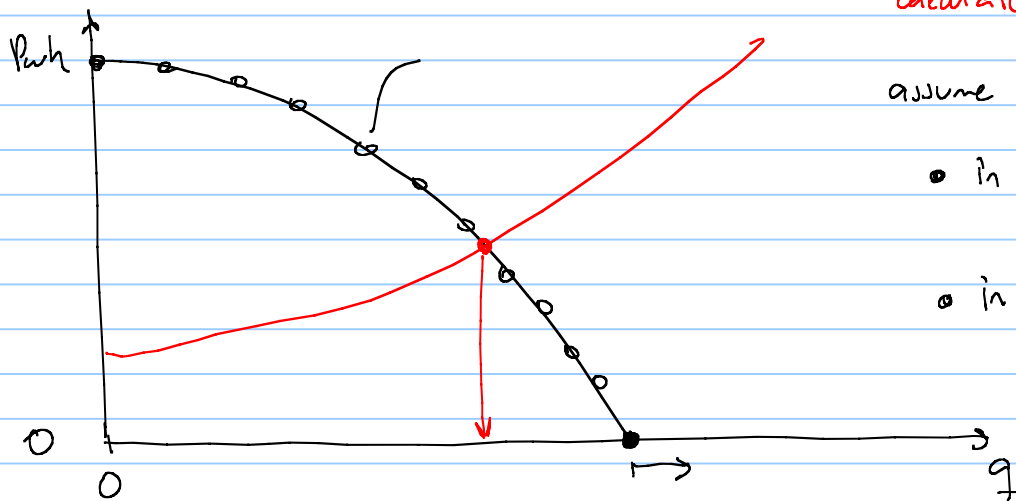
1 eq, 2 unknowns.

$$q_g = C_T \left( \frac{p_{wf}^2}{e^s} - p_{wh}^2 \right)^{0.5}$$

2 eq, 3 unknowns

$$q_g = C_{FL} (p_{wh}^2 - p_{sep}^2)^{0.5}$$

3 eq, 3 unknowns



calculate available pressure curve  
in the range

assume  $q_g^- (0 \rightarrow q_5^*)$

- in IPR eq. calculate  $P_{wf}$
  - in tubing equations calculate  $P_{wh}$
- repeat for other rates

$$q_{\text{FS}} = C_T \left( \frac{p_{\text{w}}^2}{e^5} - p_{\text{wh}}^2 \right)^{0.5}$$

$$P_{wh} = \sqrt{\frac{P_{wt}^2}{e^2} - \left(\frac{q}{5r}\right)^2}$$

calculate the required pressure curve

addition  $\mathbb{Z}_5 (0 \rightarrow \mathbb{Z}_5^*)$

use flowline equation

$$q_5 = C_{PL} (P_{inh}^2 - P_{sep}^2)^{0.5}$$

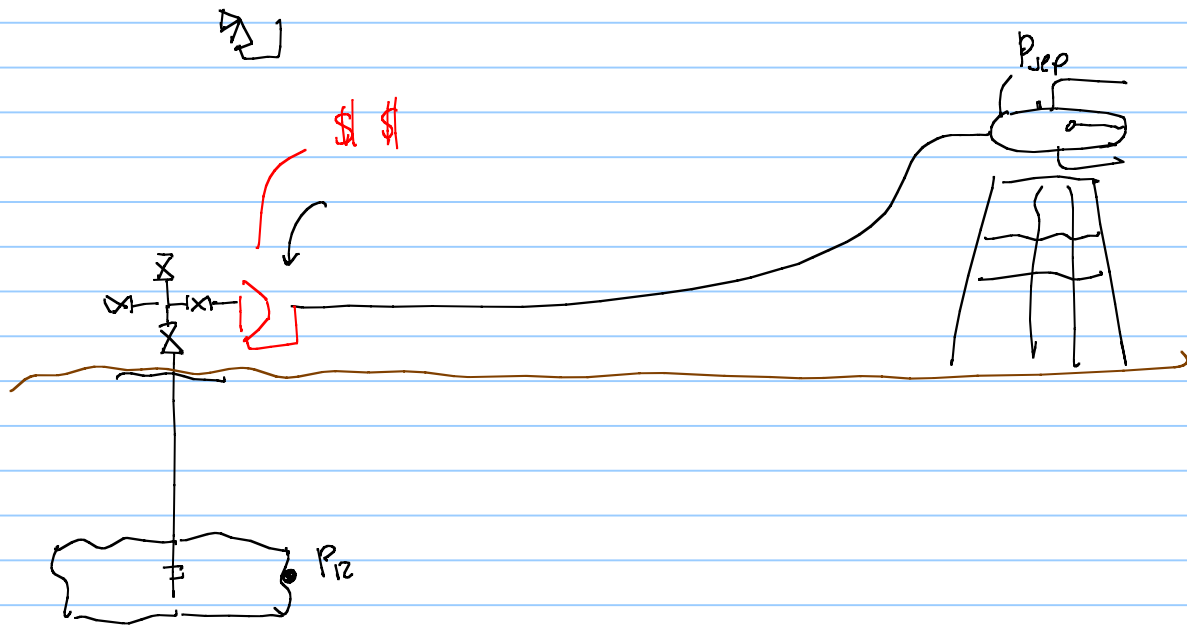
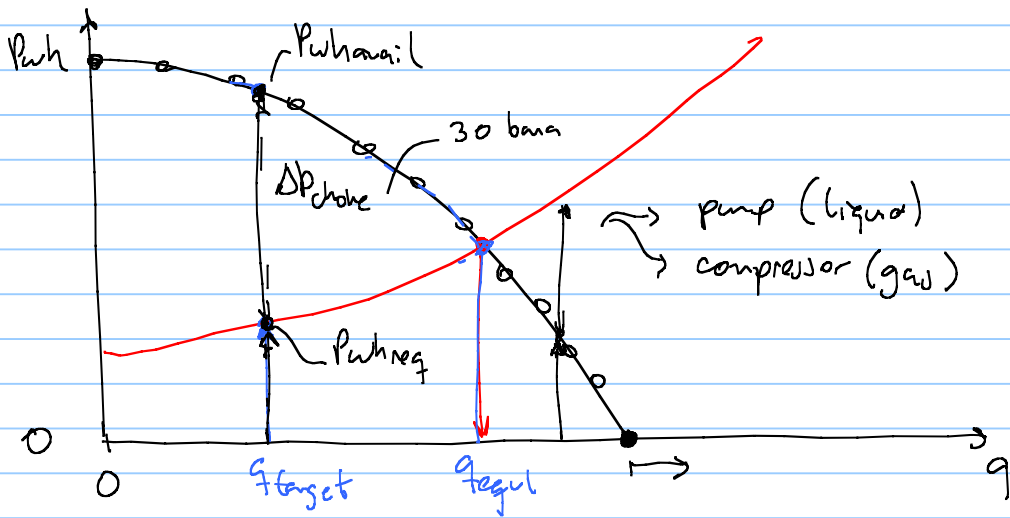
$$P_{wh} = P_{sep}^2 + \left( \frac{q}{C_{PV}} \right)^2$$

Diagram illustrating the relationship between time, performance, and cost:

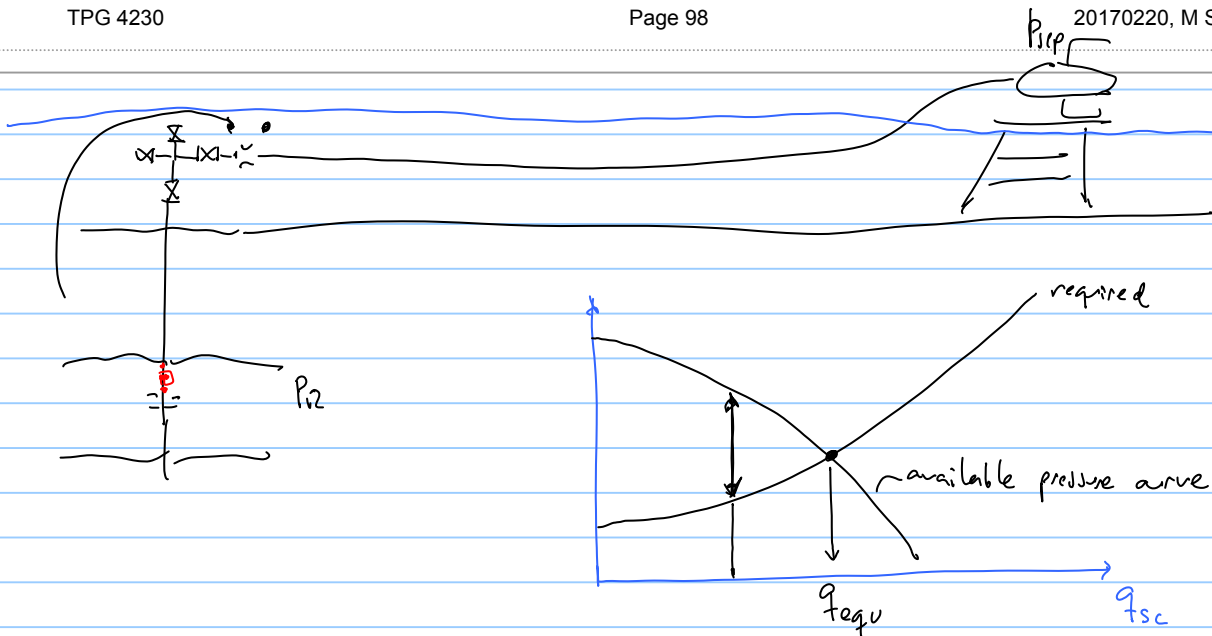
- Time axis (horizontal line).
- Performance axis (vertical line labeled  $P_R$ ).
- Cost axis (vertical line labeled  $q_s$  all-time, with a circled  $q_s$  below it).
- Performance axis (vertical line labeled  $P_R$ ).
- Performance axis (vertical line labeled  $P_R$ ).
- Performance axis (vertical line labeled  $P_{sep}$ ).
- Performance axis (vertical line labeled  $P_R$ ).
- Error axis (vertical line labeled Error  $(P_R - P_R)$ ).

Annotations:

- A blue arrow points from the  $q_s$  all-time section to the  $P_R$  section.
- A blue arrow points from the  $P_R$  section to the  $P_R$  section.
- A blue arrow points from the  $P_{sep}$  section to the  $P_R$  section.
- A blue arrow points from the  $P_R$  section to the Error axis.



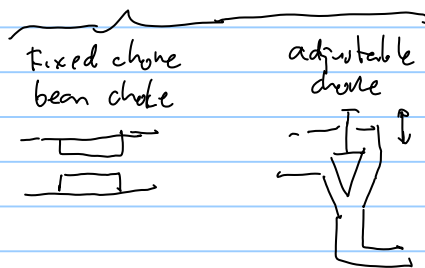




when we have adjustable elements in my production system:

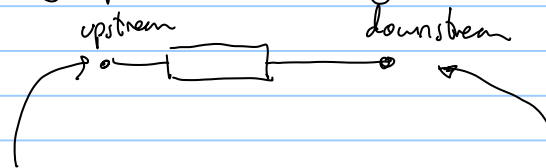
choke, pump (the rotational speed can be changed)

gas lift the gas lift injection rate can be changed:



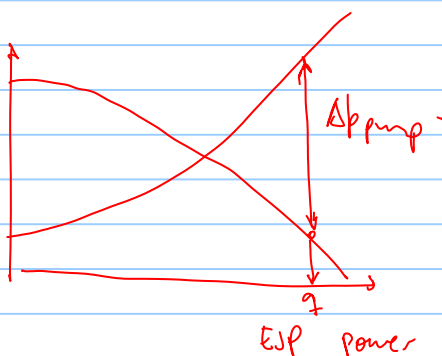
there are two ways to calculate equilibrium

1. Removing the component from the system and applying equilibrium exactly at that location



is useful for design. (when a new component will be acquired or replaced)  
when the numerical model is not available or is very uncertain and complex  
B.g. multiphase boosters  
multiphase chokes

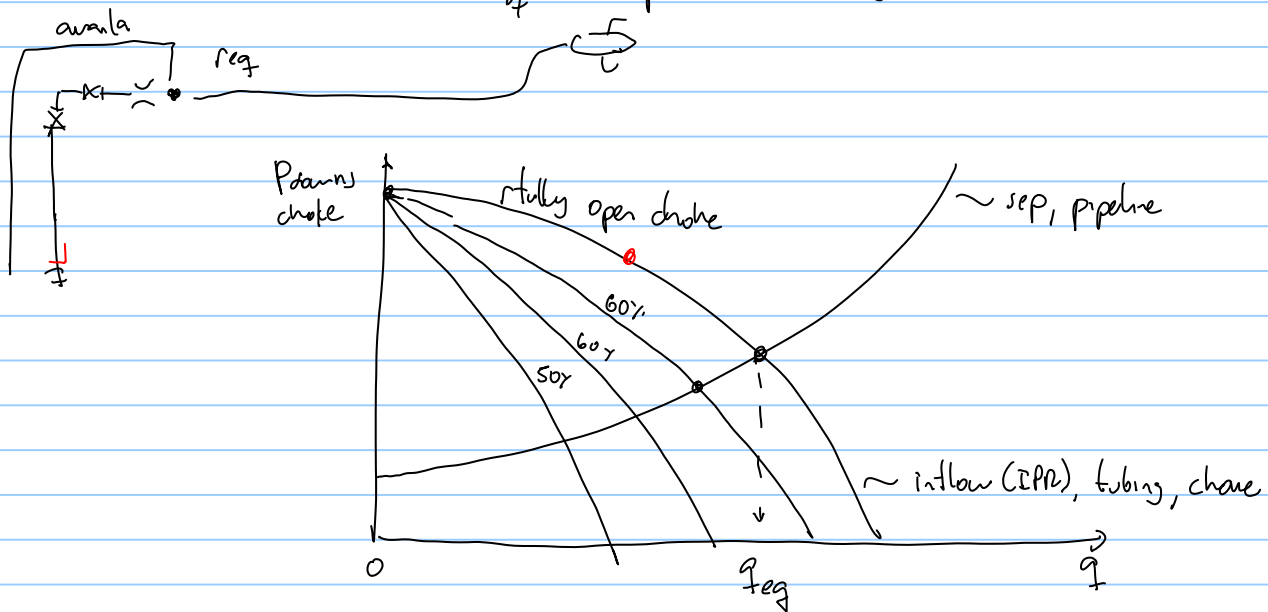
EOP design



300 hp  $\rightarrow$  2000 hp

the desired rate and  $\Delta p$  have to be verified against the equipment afterwards

2: including the component in the available or required pressure curves



if a particular model is available  
and an equation is also available

$$\text{exp} - \Delta p = a(f) q_{\text{act}}^2 + b(f) q_{\text{act}} + c(f)$$

$$\text{choke} \quad \Delta p = d \cdot q_{\text{act}}^2$$

↑ actual local volume  
rates at P, T  
at inlet of  
the component

commercial software use this mode  
PipeSim, gsp, prosper, Reo, pipephase

solving for a desired rate

$$q_{sc} = c_d A_2 p_1 \left( \frac{T_{sc}}{p_{sc}} \right) \sqrt{2 \frac{R}{M_g Z_1 T_1}} \sqrt{\left( \frac{k}{k-1} \right) \left[ \left( \frac{p_2}{p_1} \right)^{\frac{2}{k}} - \left( \frac{p_2}{p_1} \right)^{\frac{k+1}{k}} \right]}$$

for a dry gas well with a choke.

→ assume an opening.  
 calculate the intersection  $\sim \bar{q}^*$   
 check if  $\bar{q}^* = \bar{q}_{\text{desired}}$  ?  
 if yes  $\rightarrow$  high  
 if not

Newton method

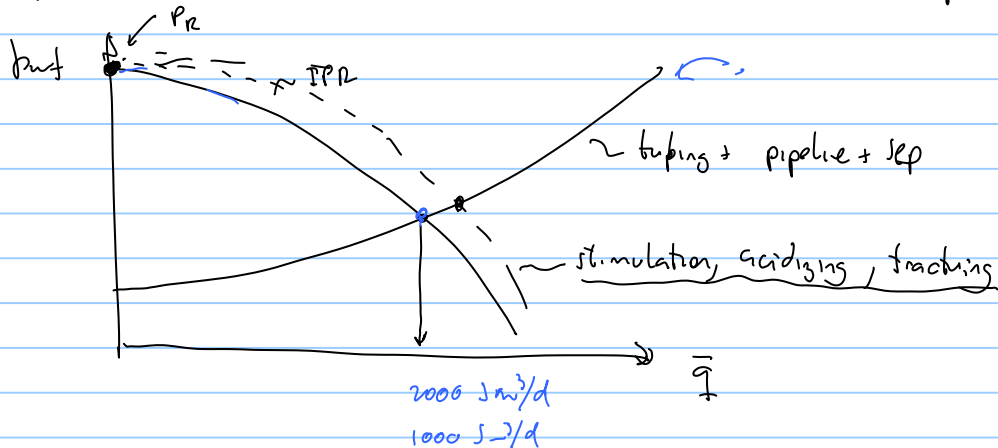
wrongly called  
optimization

in commercial  
 software

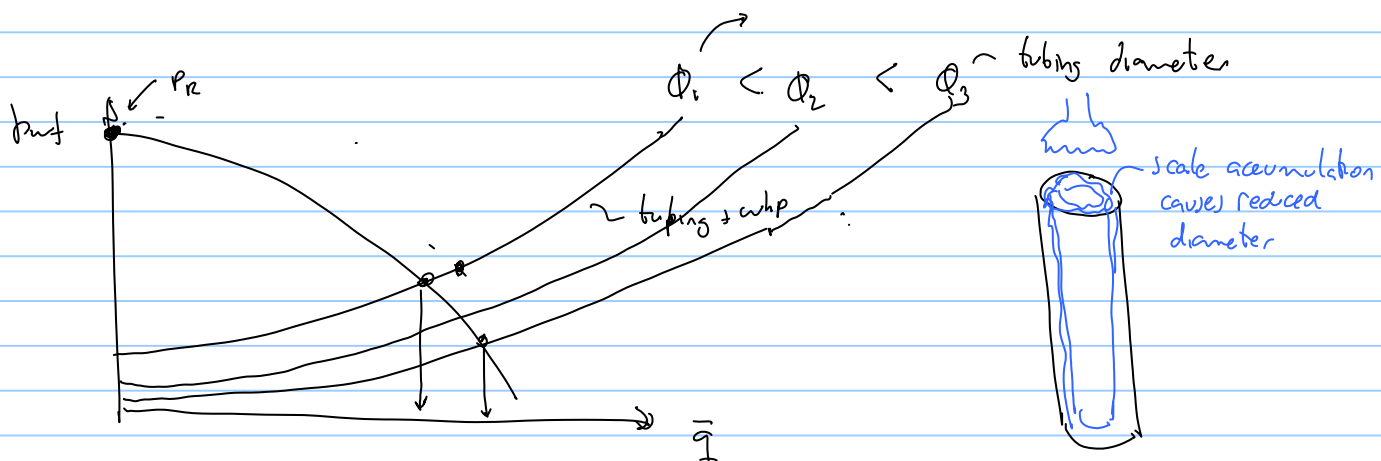
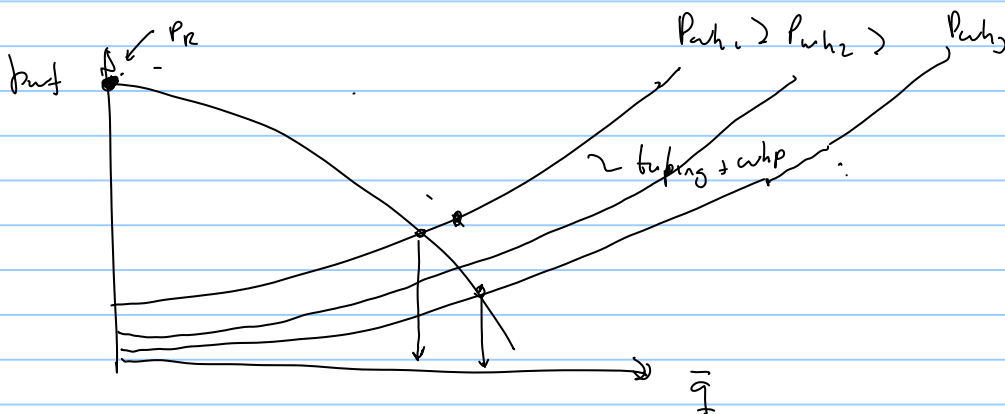
(-) the component model is usually  
 highly non-linear

(-) takes more time to evaluate

- the operator (engineer) can affect the available and required pressure curves



$$\bar{q} = C(p_R^2 - p_{wf})^n$$



Equilibrium analysis can be performed for diagnosis!

During the field design process

back and forth communication

① Reservoir engineers use reservoir simulator with pattern, target rate

Repeat simulation find optimum

Well, RF, max NPV

define for each well ( $q(t)$ )

when the production layout is defined!

② Production engineers, is that rate feasible?

the rate is not feasible!

the rate is feasible!!

Reservoir simulator + production simulator

coupling

what happens when we have multiphase flow? simultaneous flow of gas, oil and water in parts of the production system

IPR



$$q_o = q_{o, \text{GOR}}$$

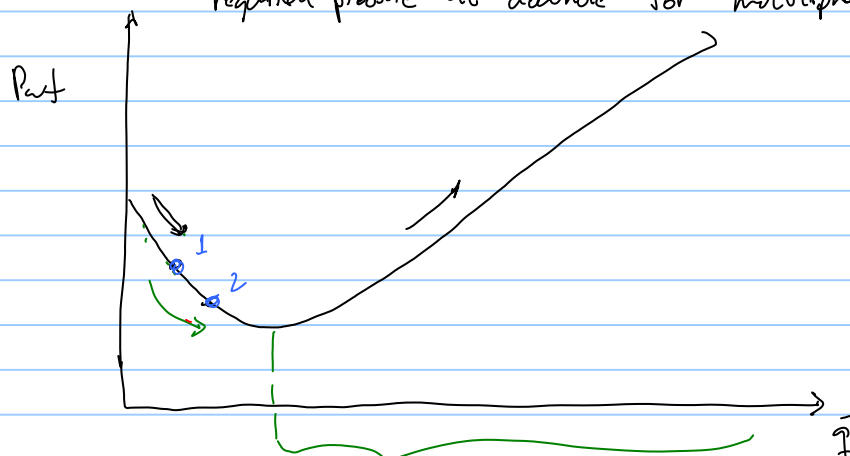
$$q_w = q_L \cdot w_c = (q_o + q_g) w_c$$

$$q_w = \frac{q_o w_c}{(1 - w_c)} \quad w_c \text{ is a fraction } (0-1)$$

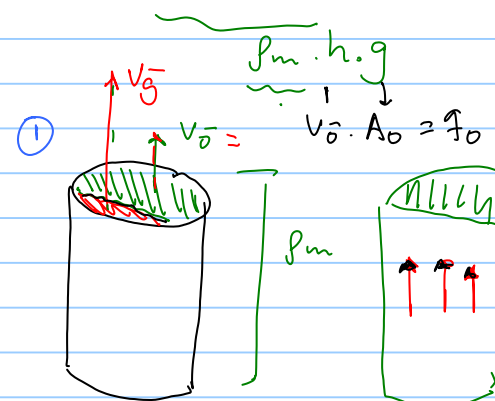
what happens with the flow in conduit?

required pressure at downhole for multiphase flow

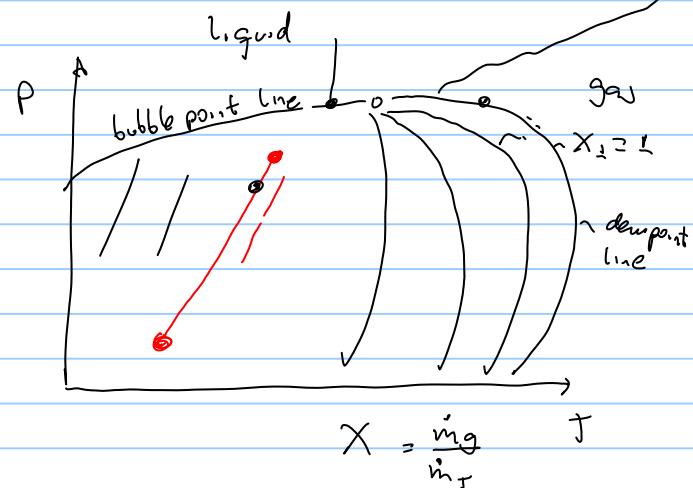
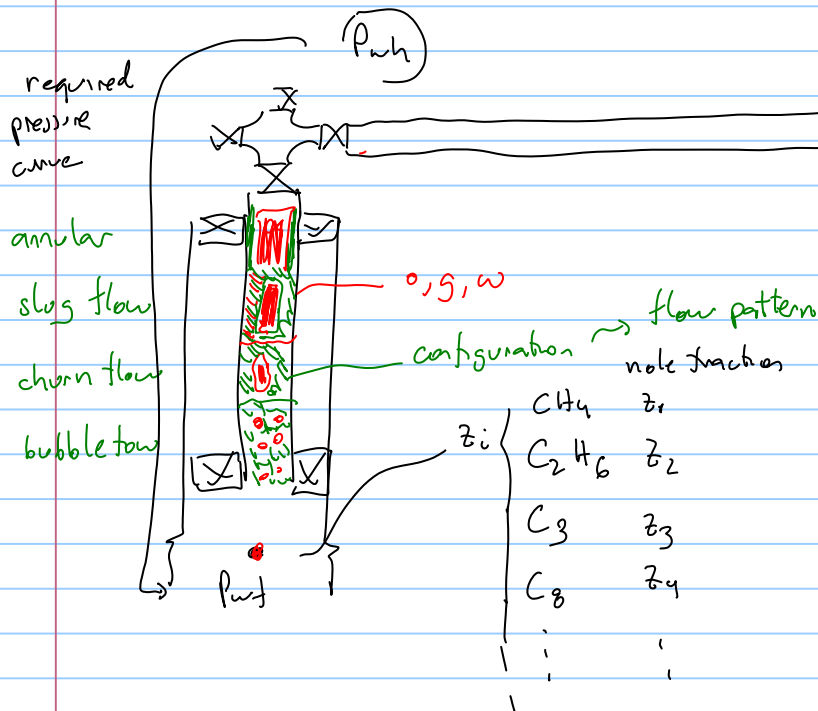
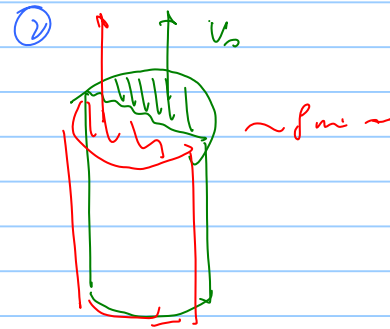
de Jager Nydal



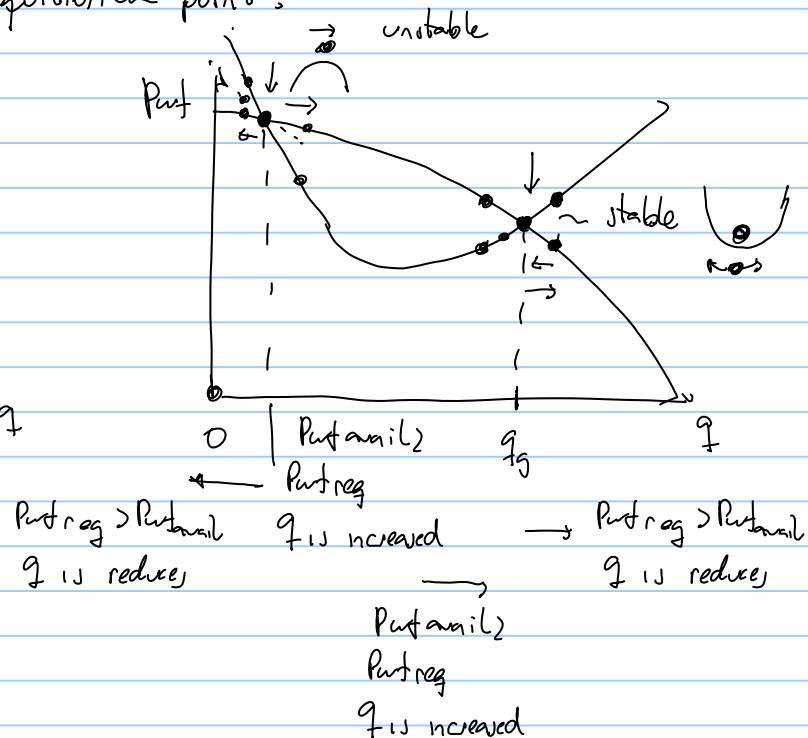
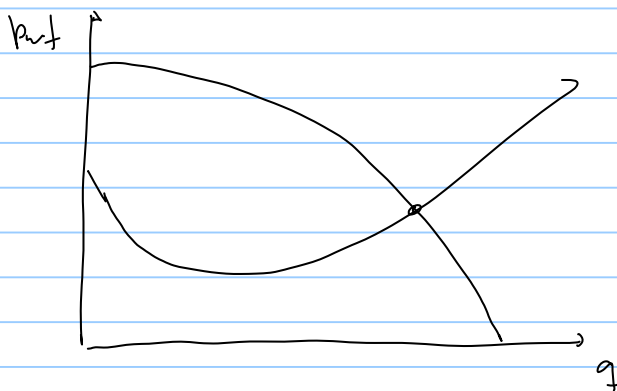
$$\Delta p_{\text{tubing}} = \Delta p_{\text{hydrostatic}} + \Delta p_{\text{friction}}(q)$$



the gas velocity  
 is high enough  
 such that it starts  
 pulling the liquid  
 up, reducing  
 the gas velocity  
 and increasing the  
 liquid velocity



what are the consequences for the equilibrium point?



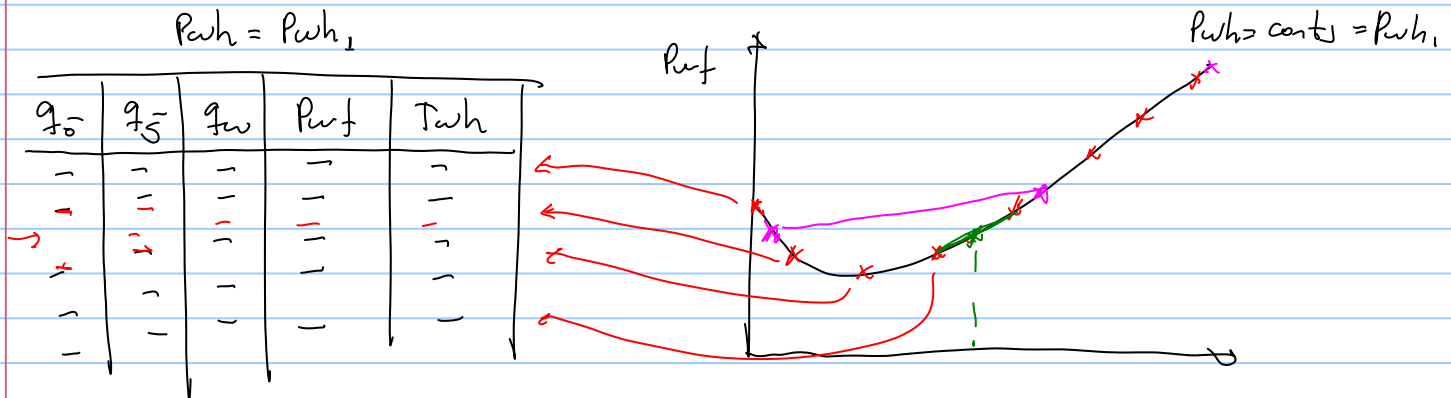
for multiphase flow pressure drop calculations are time consuming

stepwise manner  
 flow  $\rightarrow$  determining amount  
 of oil and gas  
 determine slip between phases  
 $\hookrightarrow$  calculate  $\Delta P$

to save time, TPR is pre-computed and  
 stored in tables beforehand

1
0.14
0.13
0.12
0.11
0

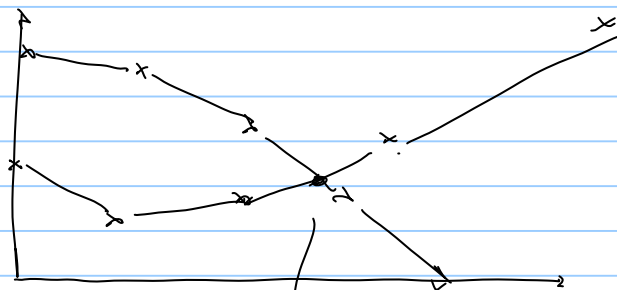
Tubing table VLP vertical lift performance  
 TT



later we use the table as our multiphase proxy.  
 perform interpolation on the table

there has to be an appropriate number of points on the table  
 such as  $P_{wf,interpolated} \approx P_{wf,calc}$

linear interpolation is fast and cheap (!!)



intersection of 2 straight  
 lines  $\approx$  computationally  
 cheaper than  
 non linear solver

there will be several tables for different wellhead pressure

$$P_{wh} = P_{wh_1}$$

$q_o$	$q_g$	$q_w$	$P_{wf}$	$T_{wh}$
-	-	-	-	-
-	-	-	-	-
-	-	-	-	-
-	-	-	-	-
-	-	-	-	-
-	-	-	-	-
-	-	-	-	-
-	-	-	-	-
-	-	-	-	-
-	-	-	-	-

$$P_{wh} = P_{wh_2}$$

$q_o$	$q_g$	$q_w$	$P_{wf}$	$T_{wh}$
-	-	-	-	-
-	-	-	-	-
-	-	-	-	-
-	-	-	-	-
-	-	-	-	-
-	-	-	-	-
-	-	-	-	-
-	-	-	-	-
-	-	-	-	-
-	-	-	-	-

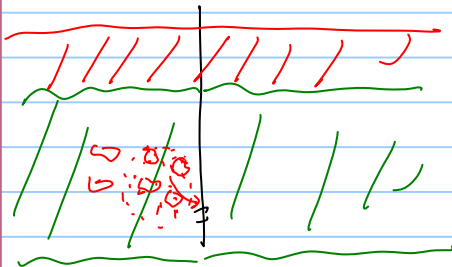
$$P_{wh} = P_{wh_3}$$

$q_o$	$q_g$	$q_w$	$P_{wf}$	$T_{wh}$
-	-	-	-	-
-	-	-	-	-
-	-	-	-	-
-	-	-	-	-
-	-	-	-	-
-	-	-	-	-
-	-	-	-	-
-	-	-	-	-
-	-	-	-	-
-	-	-	-	-

$$P_{wh} = P_{wh_4}$$

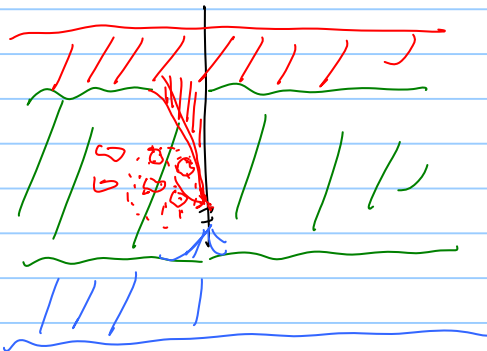
$q_o$	$q_g$	$q_w$	$P_{wf}$	$T_{wh}$
-	-	-	-	-
-	-	-	-	-
-	-	-	-	-
-	-	-	-	-
-	-	-	-	-
-	-	-	-	-
-	-	-	-	-
-	-	-	-	-
-	-	-	-	-
-	-	-	-	-

with time the well GOR changes, WC change



with the depletion

$S_g \uparrow K_{rg} \rightarrow$  more gas flow towards the wellbore the GOR  $\uparrow$



gas coning  
water coning

So usually it is necessary to build tables for different GORs and WCR



$$P_{wh} = P_{wh_1} \text{ GOR}_1 w_{C_1}$$

$q_{0-}$	$q_{5-}$	$q_{w-}$	$P_{wt}$	$T_{wh}$
-	-	-	-	-
-	-	-	-	-
-	-	-	-	-
-	-	-	-	-
-	-	-	-	-
-	-	-	-	-
-	-	-	-	-
-	-	-	-	-
-	-	-	-	-
-	-	-	-	-

$$P_{wh} = P_{wh_2} \text{ GOR}_1 w_{C_1}$$

$q_{0-}$	$q_{5-}$	$q_{w-}$	$P_{wt}$	$T_{wh}$
-	-	-	-	-
-	-	-	-	-
-	-	-	-	-
-	-	-	-	-
-	-	-	-	-
-	-	-	-	-
-	-	-	-	-
-	-	-	-	-
-	-	-	-	-
-	-	-	-	-

$$P_{wh} = P_{wh_3} \text{ GOR}_1 w_{C_1}$$

$q_{0-}$	$q_{5-}$	$q_{w-}$	$P_{wt}$	$T_{wh}$
-	-	-	-	-
-	-	-	-	-
-	-	-	-	-
-	-	-	-	-
-	-	-	-	-
-	-	-	-	-
-	-	-	-	-
-	-	-	-	-
-	-	-	-	-
-	-	-	-	-

$$P_{wh} = P_{wh_4} \text{ GOR}_1 w_{C_1}$$

$q_{0-}$	$q_{5-}$	$q_{w-}$	$P_{wt}$	$T_{wh}$
-	-	-	-	-
-	-	-	-	-
-	-	-	-	-
-	-	-	-	-
-	-	-	-	-
-	-	-	-	-
-	-	-	-	-
-	-	-	-	-
-	-	-	-	-
-	-	-	-	-

$$P_{wh} = P_{wh_1} \text{ GOR}_2 w_{C_1}$$

$q_{0-}$	$q_{5-}$	$q_{w-}$	$P_{wt}$	$T_{wh}$
-	-	-	-	-
-	-	-	-	-
-	-	-	-	-
-	-	-	-	-
-	-	-	-	-
-	-	-	-	-
-	-	-	-	-
-	-	-	-	-
-	-	-	-	-
-	-	-	-	-

$$P_{wh} = P_{wh_2} \text{ GOR}_2 w_{C_1}$$

$q_{0-}$	$q_{5-}$	$q_{w-}$	$P_{wt}$	$T_{wh}$
-	-	-	-	-
-	-	-	-	-
-	-	-	-	-
-	-	-	-	-
-	-	-	-	-
-	-	-	-	-
-	-	-	-	-
-	-	-	-	-
-	-	-	-	-
-	-	-	-	-

$$P_{wh} = P_{wh_3} \text{ GOR}_2 w_{C_1}$$

$q_{0-}$	$q_{5-}$	$q_{w-}$	$P_{wt}$	$T_{wh}$
-	-	-	-	-
-	-	-	-	-
-	-	-	-	-
-	-	-	-	-
-	-	-	-	-
-	-	-	-	-
-	-	-	-	-
-	-	-	-	-
-	-	-	-	-
-	-	-	-	-

$$P_{wh} = P_{wh_4} \text{ GOR}_2 w_{C_1}$$

$q_{0-}$	$q_{5-}$	$q_{w-}$	$P_{wt}$	$T_{wh}$
-	-	-	-	-
-	-	-	-	-
-	-	-	-	-
-	-	-	-	-
-	-	-	-	-
-	-	-	-	-
-	-	-	-	-
-	-	-	-	-
-	-	-	-	-
-	-	-	-	-

this increases the number of tables required significantly

$$N_{\text{points}} = N_{\text{rates}} \times N_{P_{wh}} \times N_{\text{GOR}_2} \times N_{w_{C_1}} = 1440 \text{ runs} \quad !$$

$\downarrow$                        $\downarrow$                        $\downarrow$                        $\downarrow$   
 typically                       $\sim 6$                        $\sim 8$                        $\sim 5$   
 $\sim 10$

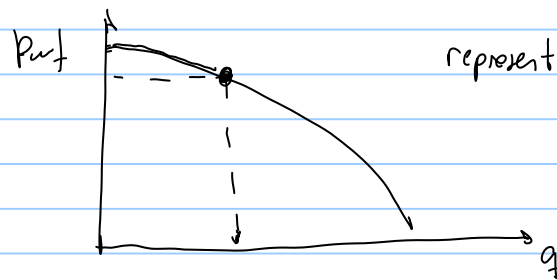
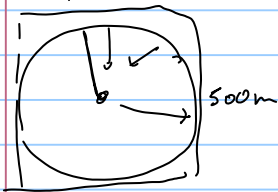
Inflow deliverability

## Inflow performance relationship:

for a given time, for a given  $P_R$ , for a given depletion state

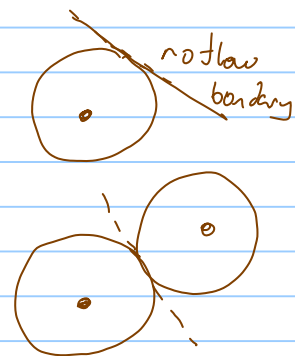
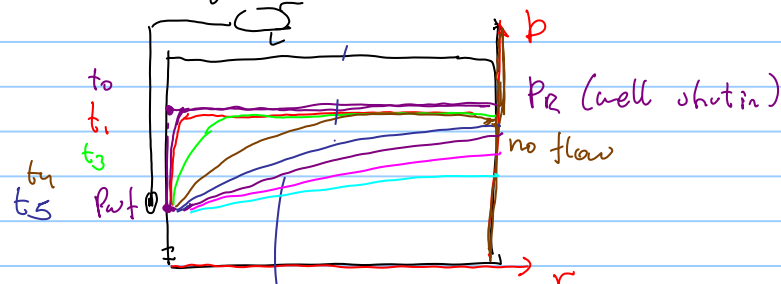


top view

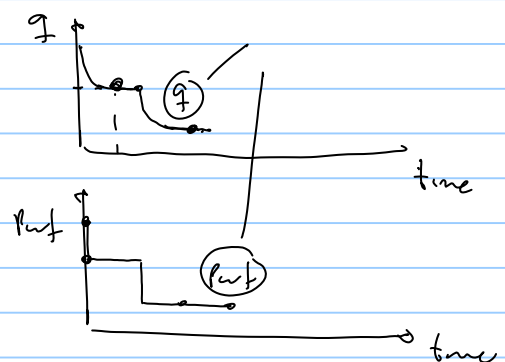
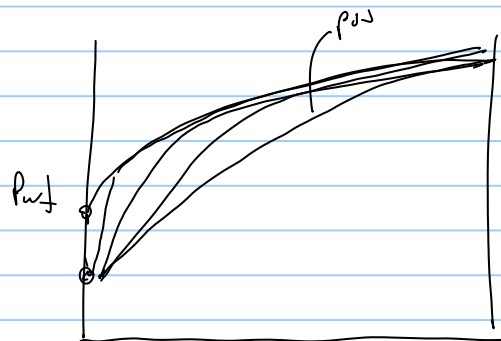


represents the flow behavior of the near wellbore formation

Reservoir engineers use reservoir simulator.

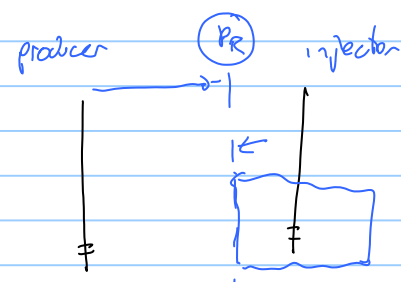


IPR applies usually for stabilized flow  
pss pseudo steady state



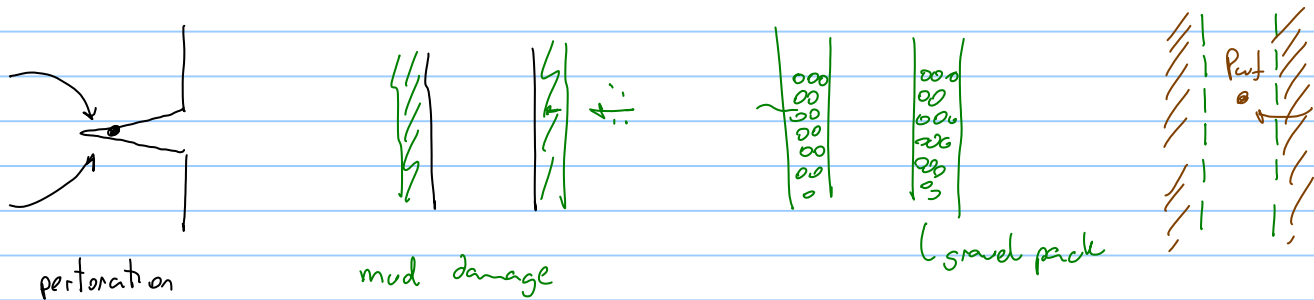
IPR: contains information about

- location and type of outer bound
  - no flow
  - constant pressure

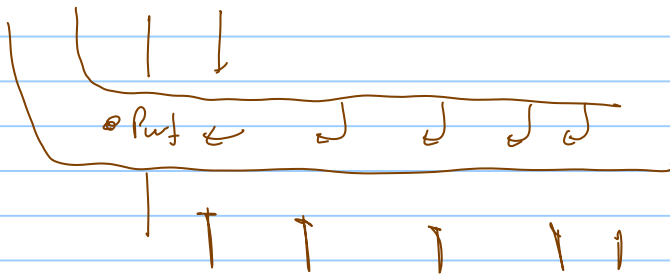


- permeability of formation (rock properties)  $K_z, K_x, K_y$
- fluid properties and their variation with  $p$ ,  $\sim \left( \frac{V}{\mu} \right) = \frac{\mu}{p} \frac{dp}{dr}$

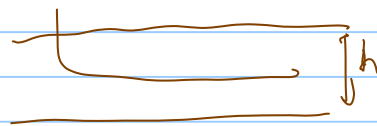
- oil, gas and water saturation in the drainage area  $\rightarrow K_{ro}, K_{rg}, K_{rw}$   
 $S_o, S_g, S_w$
- Restricted flow towards the wellbore



- for horizontal well, the IPR captures sometimes flow in the wellbore



- well radius
- formation thickness



- Volume average pressure of the drainage area ( $P_R$ )

- high velocity effect (non Darcy)

$$v = \frac{k}{\mu} \frac{dp}{dr}$$

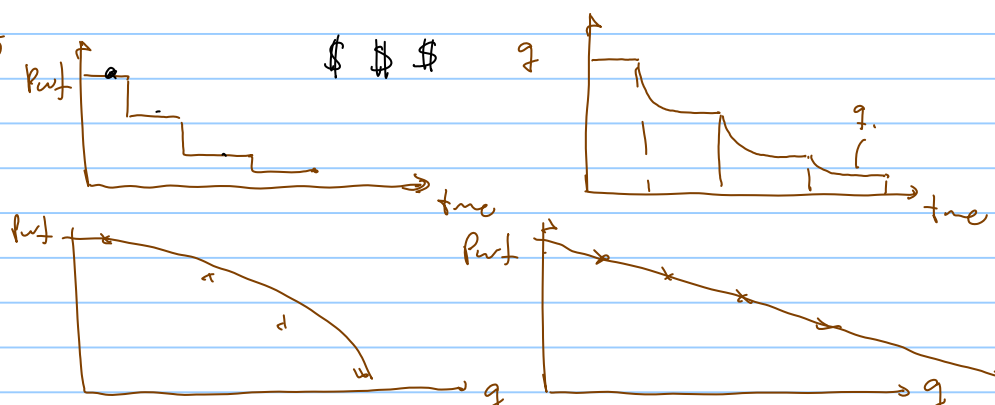
$$av + c(v)^2 = \frac{k}{\mu} \frac{dp}{dr}$$

- the convergence effect of the flow towards the wellbore



two methods to estimate IPR

- well test



Some equations typically used are

- Linear IPR  $\sim$  (undersaturated oil + water)

$$q_L = J (P_R - P_{wf})$$

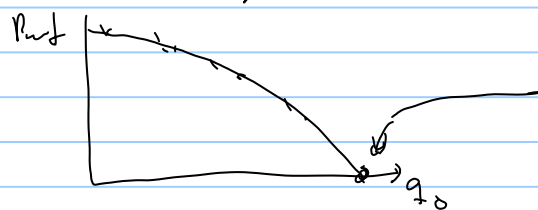
$$(q_o + q_w) = J (P_R - P_{wf})$$

- Backpressure equation (gas saturated oil)

$$q = C (P_R^2 - P_{wf}^2)^n$$

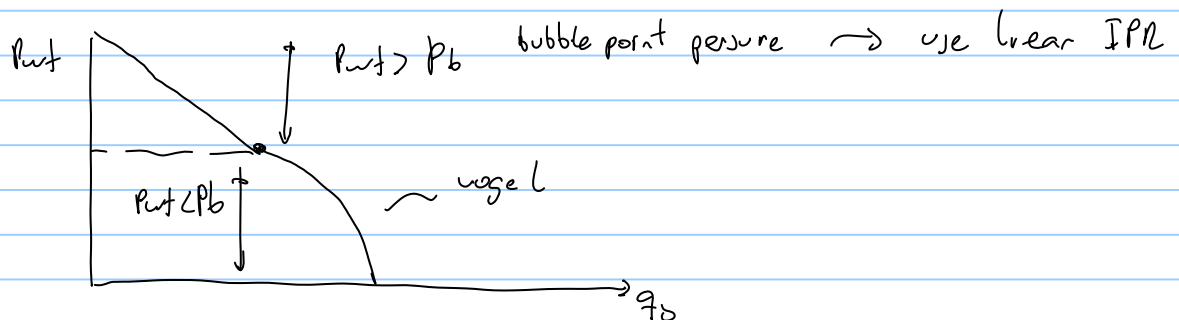
- Vogel equation (saturated oil)

$$q_o = \underbrace{q_{o \max}}_{q_o @ P_{wf} = 1 \text{ bar}} \cdot \left( 1 - 0.2 \frac{P_{wf}}{P_R} - 0.8 \left( \frac{P_{wf}}{P_R} \right)^2 \right)$$

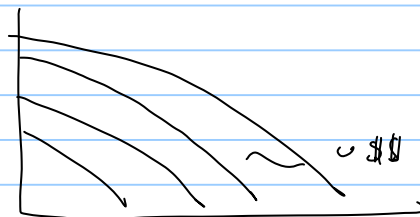


AOF: absolute open flow

- Composite IPR (saturated and undersaturated oil)



- with time the IPR changes  $\sim$  it is necessary to run well test again



- IPR can be also estimated analytically. useful for field design  $\nabla$   
(no test data is available)  $\oplus$

expression are derived from differential equations conservation of mass and

$$\frac{k}{\mu} 2\pi h \frac{\partial}{\partial r} \left( r \frac{\partial p}{\partial r} \right) = 2\pi h \phi c r \frac{\partial p}{\partial t}$$

customize the equation for each situation, well geometry, and solve it

some examples

for gas

$$q_g = \frac{\pi k h T_{sc} a}{T_p P_{sc} \left( \ln \left( \frac{r_e}{r_w} \right) - \frac{3}{4} + S \right)} \int_{P_{wf}}^{P_R} \left( \frac{2 p}{M_s z} \right) dp$$

unit conversion constant

for oil

$$q_o = \frac{2\pi k h a}{\ln \left( \frac{r_e}{r_w} \right) - \frac{3}{4} + S} \int_{P_{wf}}^{P_R} \frac{k_{ro}}{M_o B_o} dp$$

unit conversion constant

for under saturated oil

$$k_{ro} \leq 1 \text{ if you have create water}$$

$$\frac{k}{M_o B_o} = \text{constant with } P$$

$$k_{ro} = f(S_o)$$

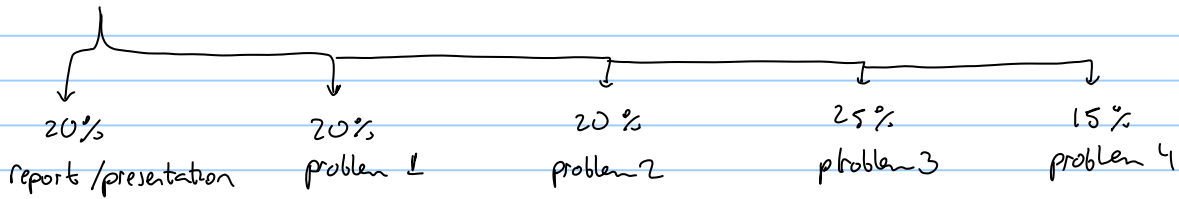
$$S_o = \text{constant}$$

$$k_{ro} = \text{value less than 1}$$

$$q_o = \frac{2\pi k h}{\underbrace{\left( \ln \left( \frac{r_e}{r_w} \right) - \frac{3}{4} + S \right)}_J} \left( \frac{1}{M_o B_o} \right) (P_e - P_{wf})$$

## Evaluation of exercise set 1:

### • 100%



for future deliveries 20% deduction for every day delivered late!

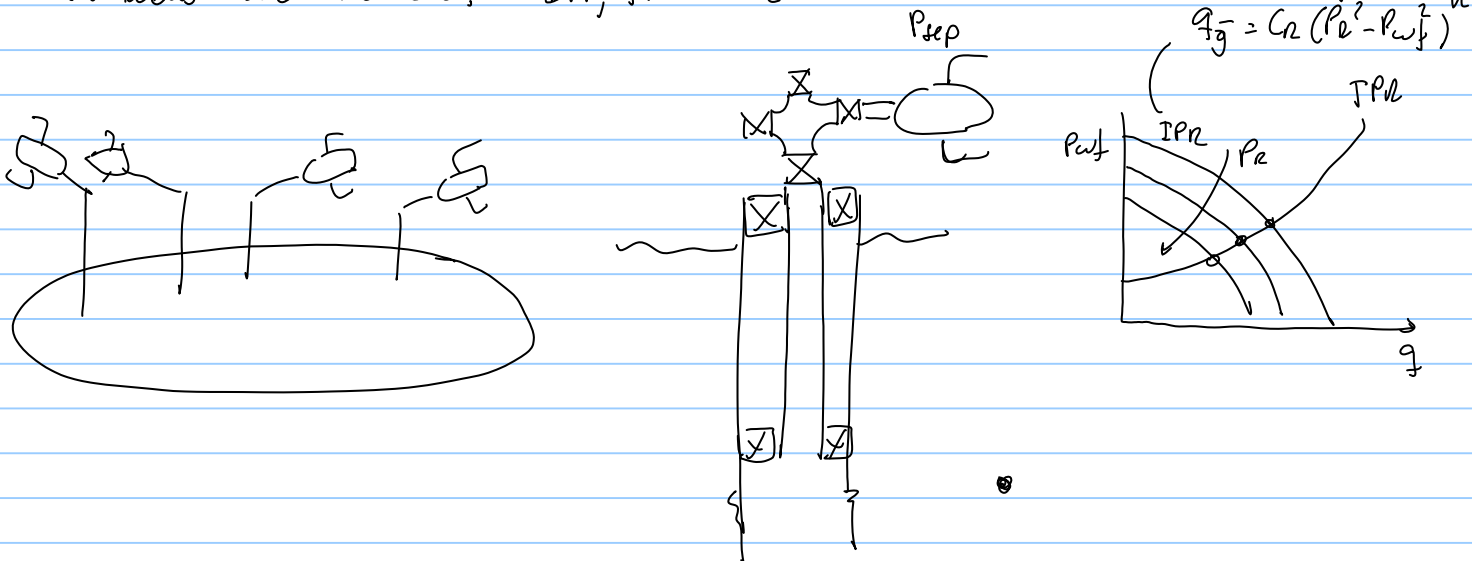
## Production potential

Dry gas reservoir  $\rightarrow$  uniform reservoir pressure

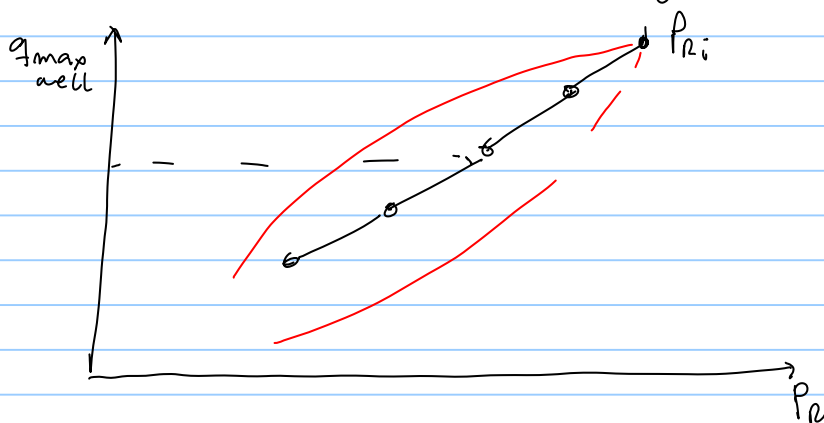
Standalone well  $\rightarrow$

N wells

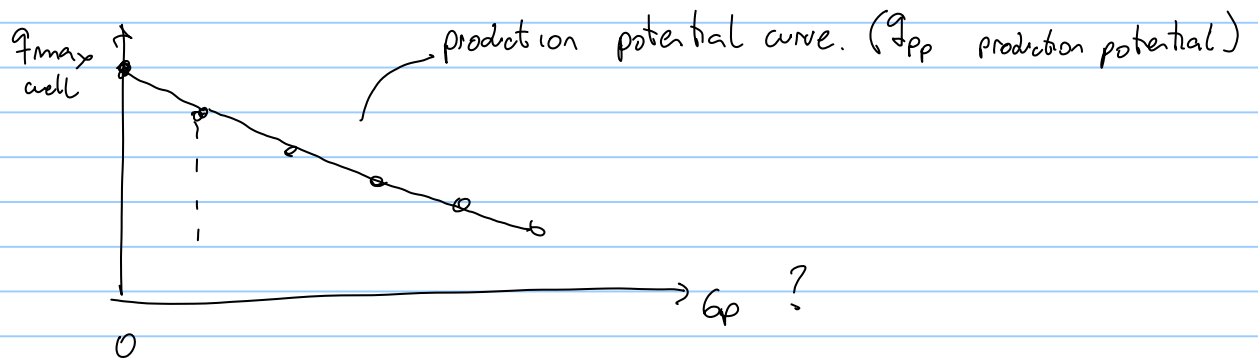
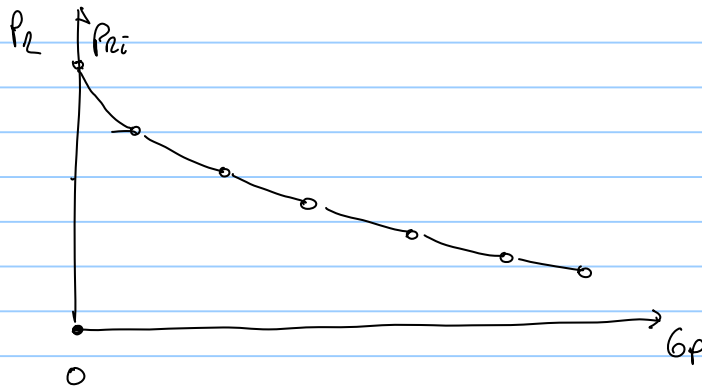
all wells are identical, IPR, JPR same



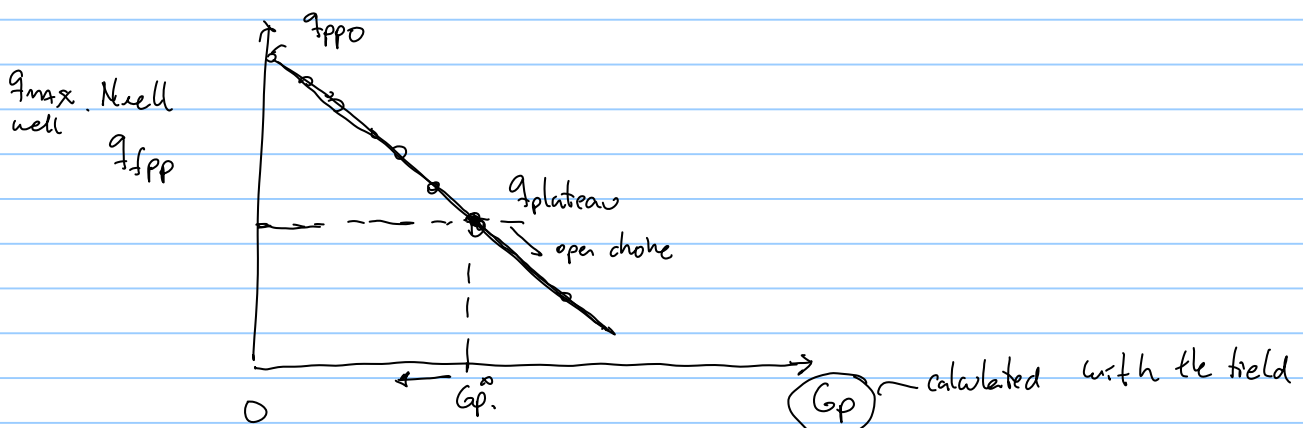
maximum rate from the well will go down with reservoir pressure



$p_r$  according to material balance  $p_r(t) = f(G_p)$   $G_p = \int_0^t q_{\bar{g}} dt$



for the field:



$G_p^*$  is the cumulative production at which the  $q_{fpp} = q_{plateau}$   
 $t_{plateau} = \left( \frac{G_p^*}{q_{plateau} \cdot N_{day/year}} \right)$

Until now, to find plateau length you perform a stepwise calculation in time

time	$q_{open\ choke}$	$q_{produce\ est}$	if $q_{open\ choke} > q_{produce\ est}$ then plateau
$t_1$			
$t_2$	-	-	-
$t_3$			
$t_4$			



Deriving the production profile using the production potential, always open choke

for dry gas  $\boxed{q_{fpp} = q_{ppo} - m G_p} \quad (1) \quad q_f = q_{fpp}$

$\boxed{G_p = \int_0^t q_f dt} \quad (2)$

$q_f = q_{ppo} - m \int_0^t q_f dt$  derive with respect to time

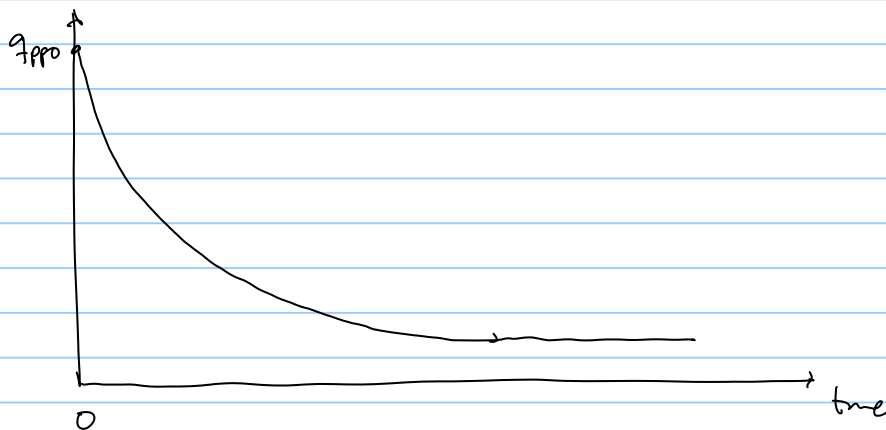
$\frac{dq_f}{dt} = -m q_f$

$\int_{q_{ppo}}^{q(t)} \frac{dq_f}{q_f} = \int_0^t -m dt$

production potential @  $t=0$ , @  $P_e = P_{ri}$

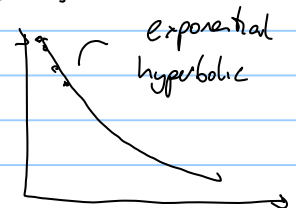
$\ln q_f \Big|_{q_{ppo}}^{q(t)} = -m(t-0)$

$\boxed{q_f = q_{ppo} \cdot e^{-mt}} \quad \text{eq (1)}$



material balance  
res simulator

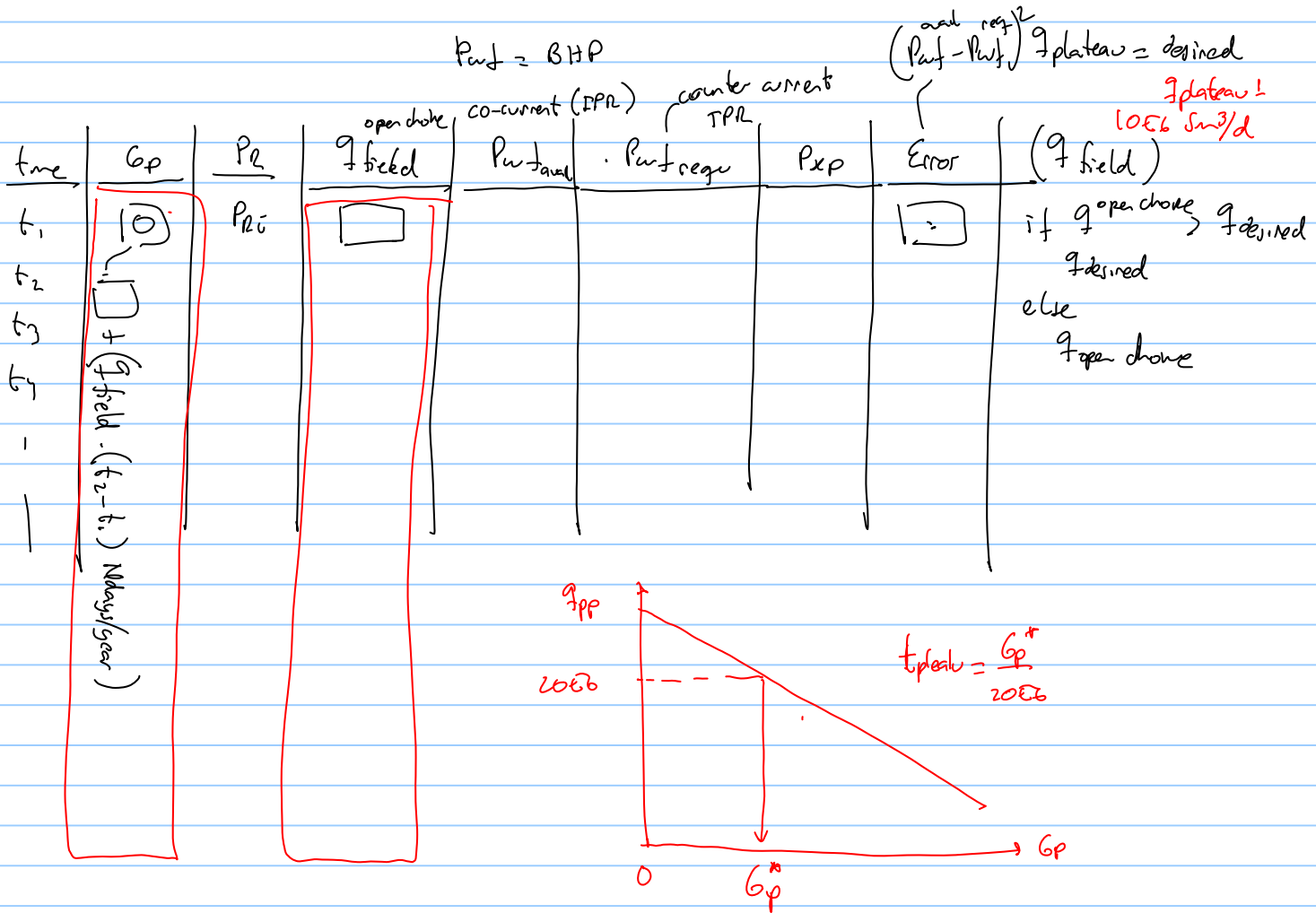
DCA



eq 1 gives you a decline shape for the rate

it can be applied for decline periods (producing at open choke) using appropriate bounds in the integral

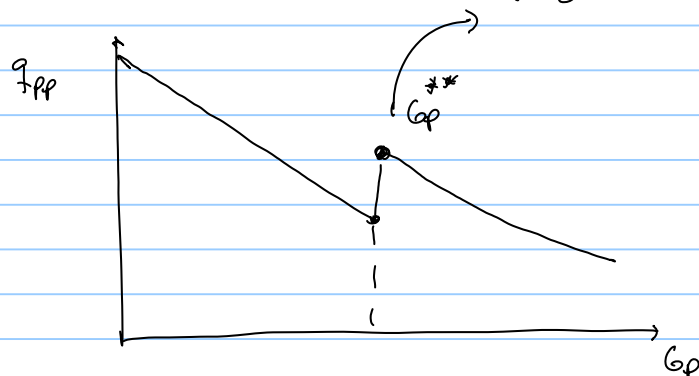
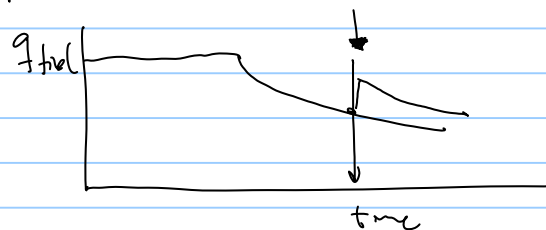
$\int_{q_{ppo}}^{q(t)} \frac{dq_f}{q_f} = \int_0^t -m dt$



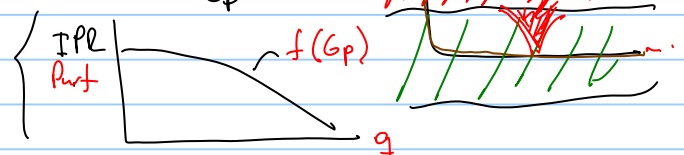
what happens if  $q_{plateau} = q_{plateau2}$  ( $20 \text{ E}6 \text{ Sm}^3/d$ )

what are the limitations?

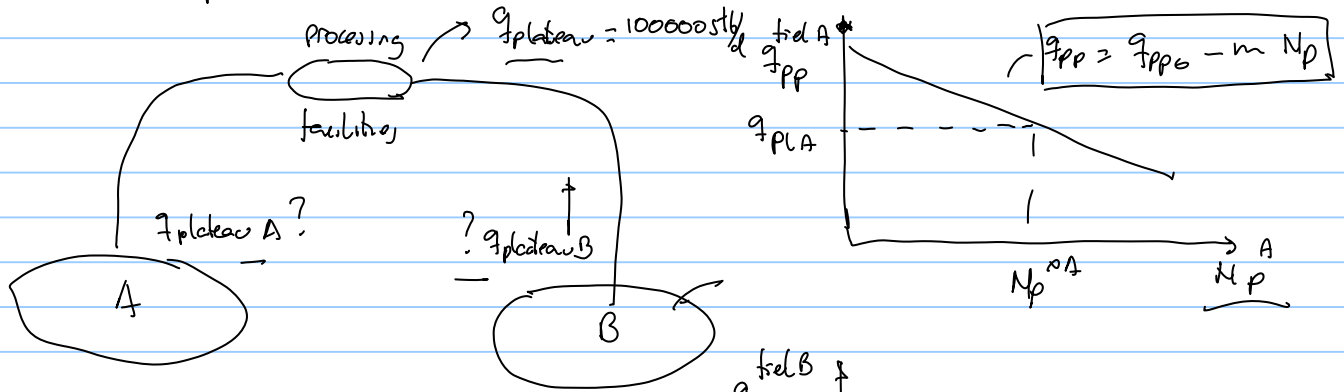
- changes in the production system  $\rightarrow$  change in well
- $G_p$  are applied at a particular day



- IPR  $f(P_{Ri}), f(G_p)$



take an example with two reservoirs



if  $q_{plateau}$  field is to be maximized  
then  $q_{plateau}^A = q_{plateau}^B$

iterative procedure

assume  $q_{plateau A}$

calculate  $q_{plateau B} = 100000 - q_{plateau A}$

go to the production potential curve  
read  $N_p^A, N_p^B$

calculate  $q_{plateau A}, q_{plateau B}$

$\rightarrow \frac{N_p^A}{q_{plateau A} \cdot N_{day/year}}$

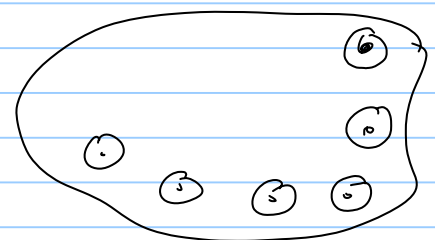
is  $q_{plateau A} = q_{plateau B}$  ? NO

YES

$q_{plateau A}, q_{plateau B}$  is the optimum solution

in big reservoirs  $q_{PPwell} \neq f(N_{pfield})$

$q_{PPwell} = f(N_{pwell})$



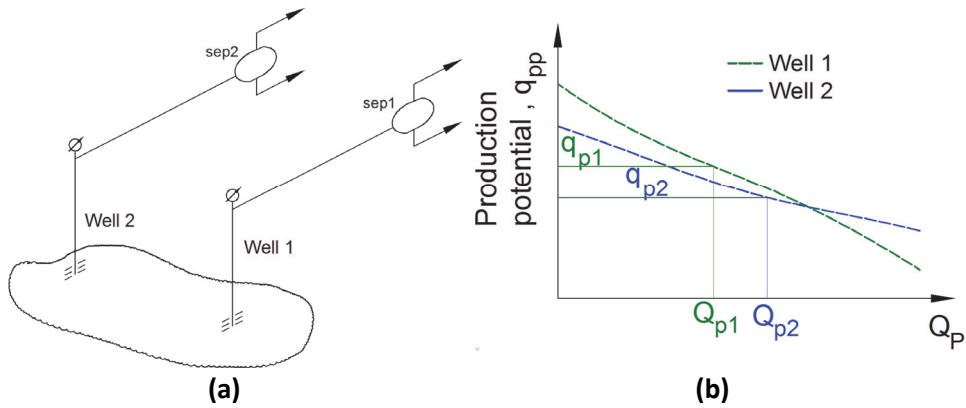
### Example 1: Production potential of a system with two standalone wells

Assume that there is a field with two (2) standalone wells, and that the production potential of each well can be expressed as a function of the cumulative production of each individual well:

$$q_{pp}^i = f(Q_P^i) \quad \text{Eq. 11}$$

In this case the production profile can be computed separately for each well from the production potential curve and then add them up to obtain the field production profile. Please note that the field production potential for a given field cumulative production is not unique. This is because there are different ways to achieve the same field cumulative production (e.g. in a two well system, produce more from well 1 than 2, produce equal, or produce more from well 2 than 1).

As an example, consider the production system with 2 standalone wells shown in Fig. 14.a. The production potential of each well is presented in Fig. 14.b. Wells will be produced at constant rate initially, with plateau rates  $q_{p1}$  and  $q_{p2}$  and, when the plateau rate is no longer feasible, they will be produced at the production potential.



**Fig. 14. Example case: 2 standalone wells**

The plateau duration of each well can be very easily calculated by intersecting the individual plateau rate with the production potential curve of each well. This yields a plateau duration of  $t_{p1} = Q_{p1}/q_{p1}$ , for well 1 and  $t_{p2} = Q_{p2}/q_{p2}$  for well 2. After the plateau ends, the production profile of each well follows the potential.

A typical reservoir management problem consists of how to define well rates to maximize field plateau duration when a fixed field rate is desired. If individual well plateau rates are to be kept constant, this can be achieved by finding the plateau rates for which the plateau end occurs at the same time. If the production potential curves are straight lines the following procedure is suitable:

The production potential curve for well 1:

$$q_{pp1} = -m_1 \cdot Q_{P1} + q_{ppo1} \quad \text{Eq. 12}$$

The cumulative production at which the production potential ( $q_{pp1}$ ) is equal to the plateau rate ( $q_{p1}$ ), i.e.  $Q_{pp1}$ , is:

$$Q_{p1} = \frac{q_{ppo1} - q_{p1}}{m_1} \quad \text{Eq. 13}$$

Similarly for well 2:

$$Q_{p2} = \frac{q_{ppo2} - q_{p2}}{m_2} \quad \text{Eq. 14}$$

Then the plateau duration has to be the same for both wells:

$$t_{p1} = \frac{Q_{p1}}{q_{p1}} = t_{p2} = \frac{Q_{p2}}{q_{p2}} \quad \text{Eq. 15}$$

Substituting Eq. 13 and 14 in Eq. 15:

$$\frac{q_{ppo1} - q_{p1}}{m_1 \cdot q_{p1}} = \frac{q_{ppo2} - q_{p2}}{m_2 \cdot q_{p2}} \quad \text{Eq. 16}$$

$$\frac{q_{ppo1}}{q_{p1}} - 1 = \frac{m_1}{m_2} \cdot \left( \frac{q_{ppo2}}{q_{p2}} - 1 \right) \quad \text{Eq. 17}$$

Eq. 17 has two unknowns, therefore one more equation is needed. Clearing  $q_{p2}$  from the expression of the total plateau rate:

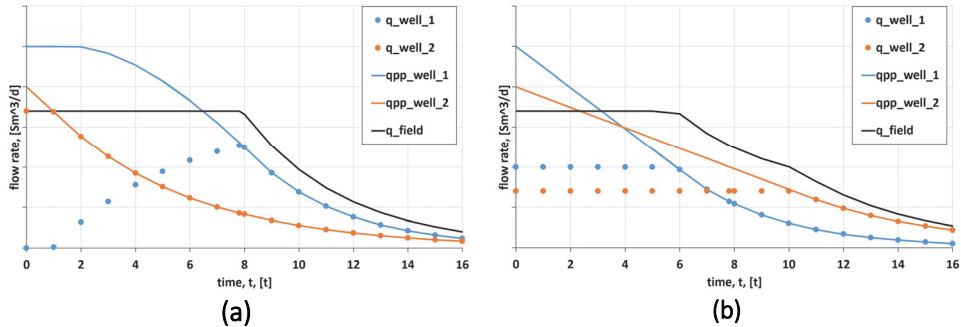
$$q_{p2} = q_p - q_{p1} \quad \text{Eq. 18}$$

Substituting Eq. 18 in Eq. 17 yields:

$$q_{p1}^2 \cdot (m_1 - m_2) + q_{p1} \cdot (q_{ppo1} \cdot m_2 + m_2 \cdot q_p - m_1 \cdot q_p + m_1 \cdot q_{ppo2}) - q_{ppo1} \cdot m_2 \cdot q_p = 0 \quad \text{Eq. 19}$$

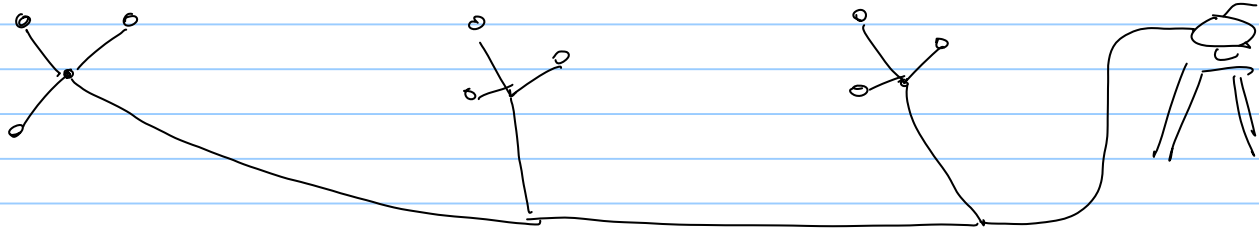
Eq. 19 can be solved with the quadratic formula to find  $q_{p1}$ .

Please note that there are infinite alternatives to produce the field at plateau rate as shown in Fig. 15. Each option will yield a different field plateau duration.

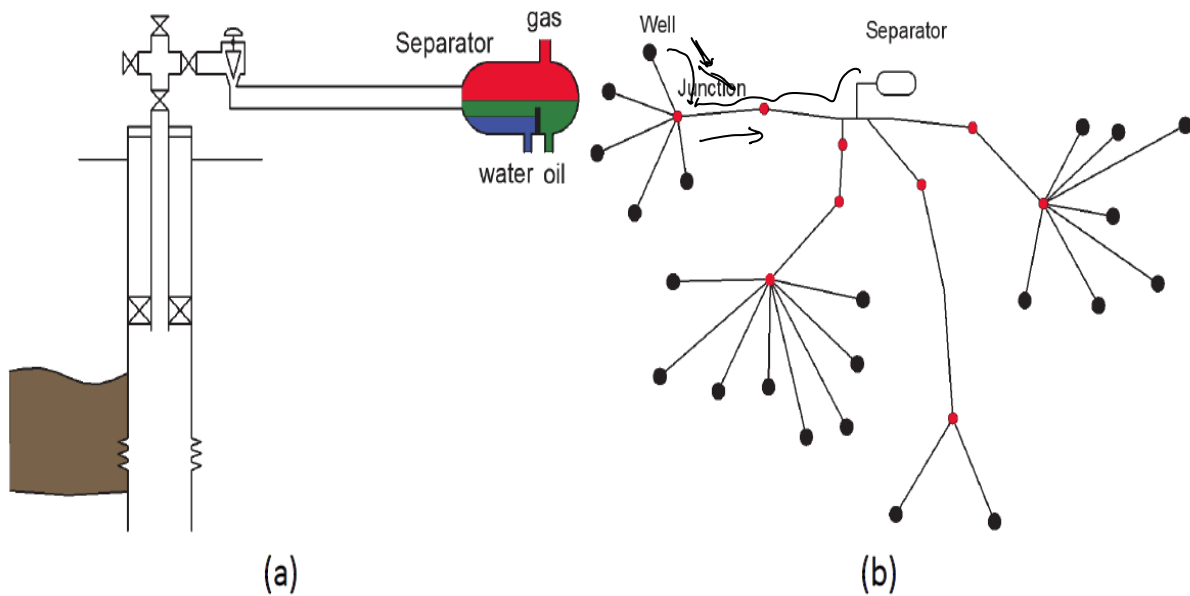


## Production networks

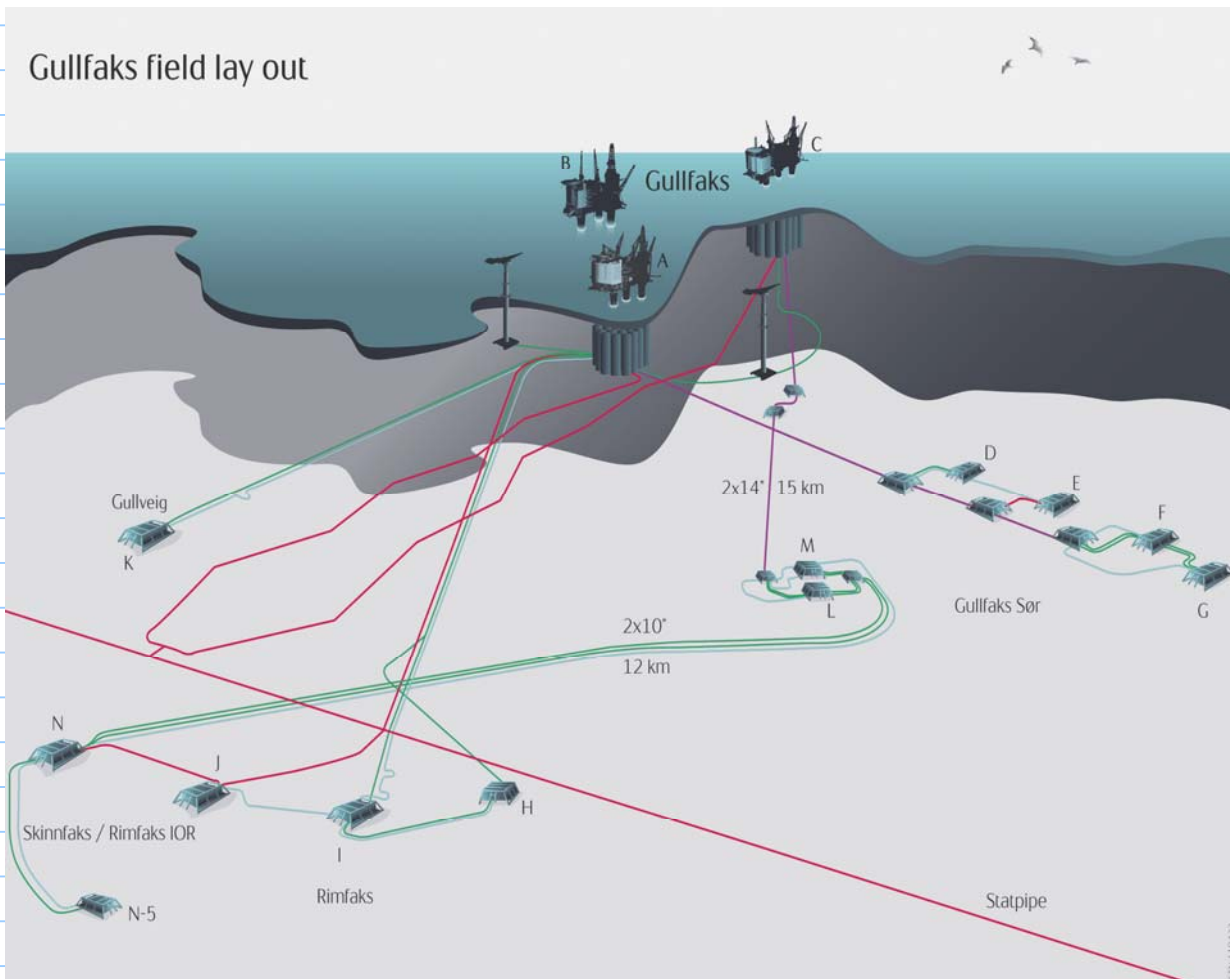
systems of flowlines that congregate the production from the individual well and take it to processing facilities



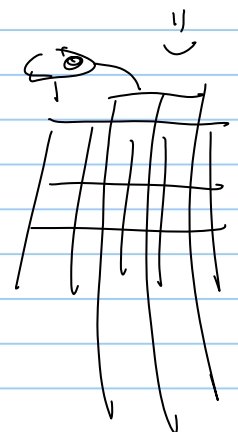
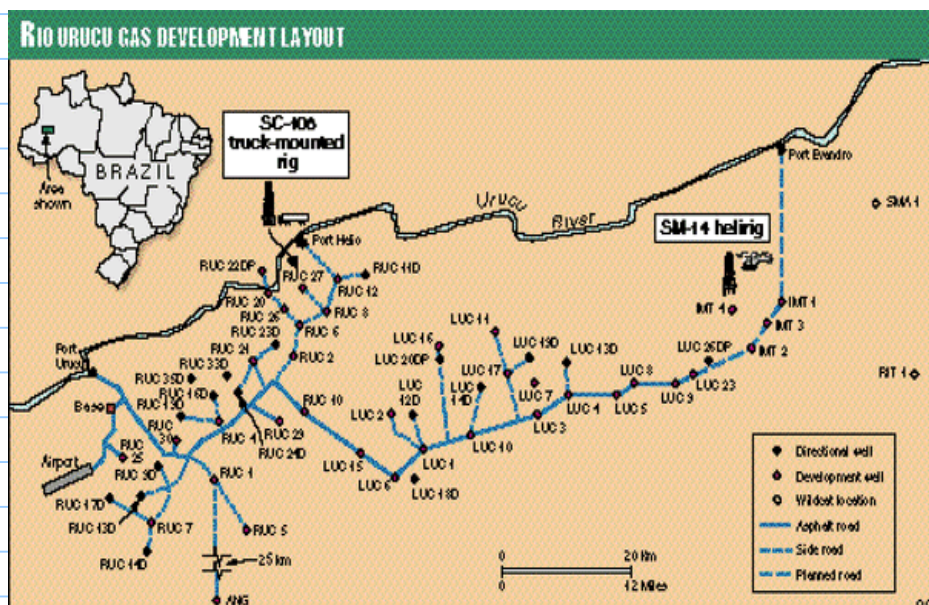
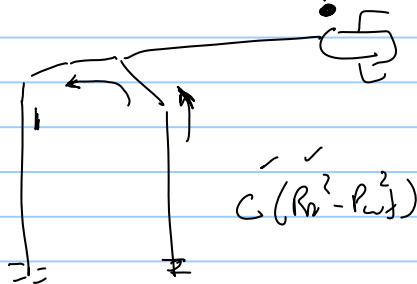
## Subsea wells







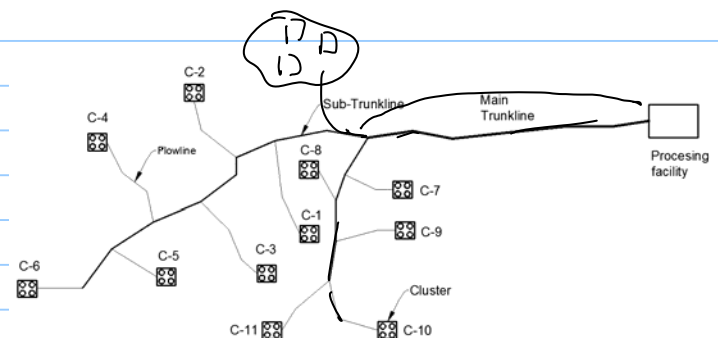
in networks there is interdependence between wells







Rubiales field





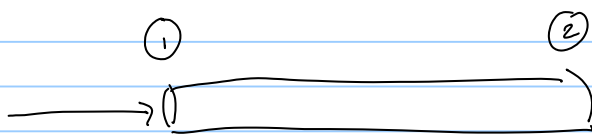


MENU FOR TODAY

- Work in groups on problem 1 exercise set Nr. 3.  $\rightarrow$  production scheduling using flow equilibrium

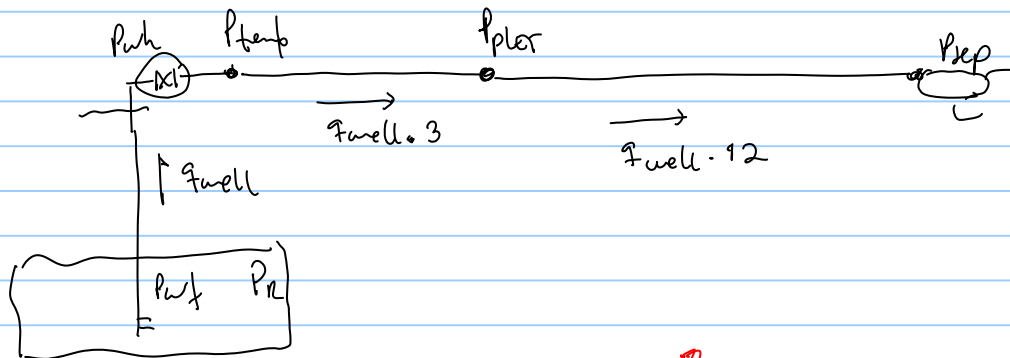
[http://folk.ntnu.no/stanko/Courses/TPG4230/2017/Exercises/Exercise\\_0/](http://folk.ntnu.no/stanko/Courses/TPG4230/2017/Exercises/Exercise_0/)

- Network solving  $\rightarrow$  flow equilibrium in networks  $\rightarrow$  theory
- Work in groups on problem 2 exercise set Nr. 3.  $\rightarrow$  using flow equilibrium



points ① and ② are defined by the flow direction. ① inlet, upstream  
② outlet, downstream.

i.e. our problem



Equilibrium point is the wellhead chose

### co-current calculation:

co-current from reservoir to wh  $\rightarrow$  IPR<sub>part</sub>, using  $P_i$  ( $P_r$ ) calculate  $P_z$  ( $P_{part}$ ) using  $q_{well}$

co-current from bottom-hole to wellhead  $\rightarrow$  tubing  $P_z$ , using  $P_i$  ( $P_{part}$ ) calculate  $P_z$  ( $P_{wh}$ ) using  $q_{well}$

### counter current calculation

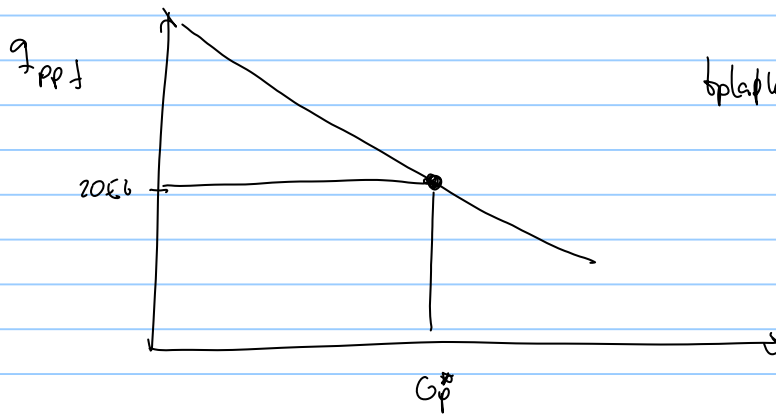
- counter current from sep to pplet, use tubing eq, tubing  $P_i$ , using  $P_z$  ( $P_{sep}$ ) calculate  $P_i$  ( $P_{plet}$ ) using  $q_{field}$ . (Remember to use  $C_{PL}$  and  $S_{PL}$  !)

- counter current from pplet to template. use line  $P_i$ , using  $P_z$  ( $P_{plet}$ ) calculate  $P_i$  ( $P_{temp}$ ) using  $q_{temp}$

---

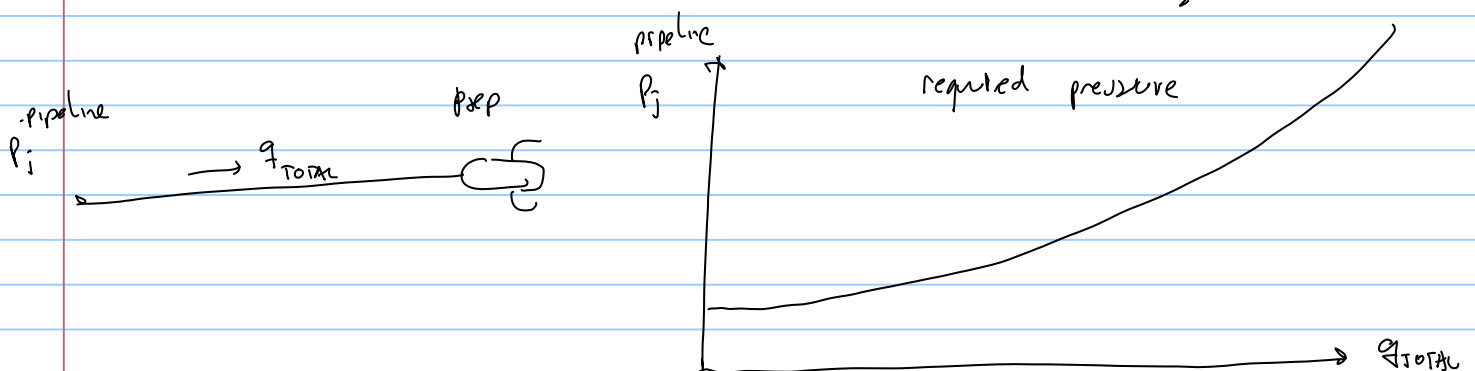
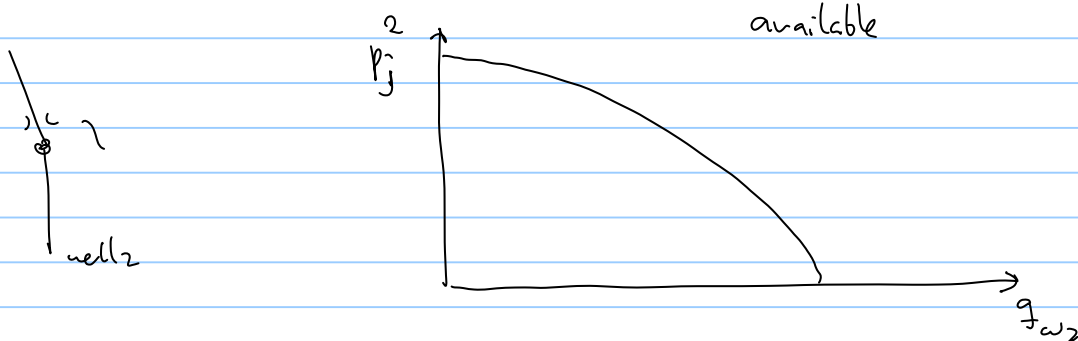
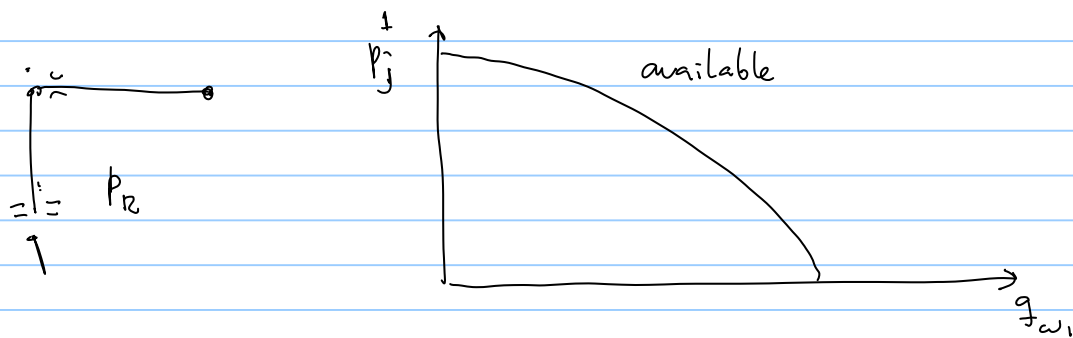
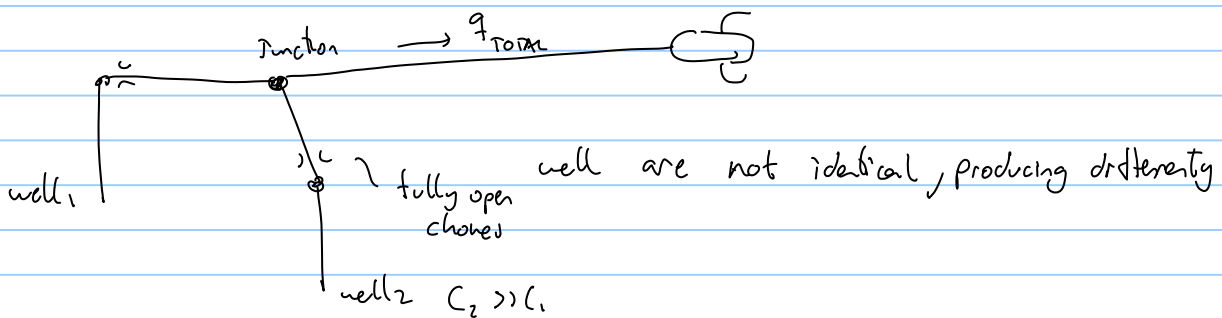

$$\Delta p_{chore} = P_{wh} - P_{temp}$$

TASK 2: comments



$$b_{plapka} = \frac{G_p^*}{20E6 \cdot 360}$$

flow equilibrium in production networks



- Assume a unique junction pressure  $p_j^*$
- from available pressure curve of well 1 calculate  $q_{w1}$



- from available pressure curve of well 2 calculate  $q_{w2}$



- from the required pressure curve of pipeline, calculate  $q_{total}$



- Verify mass conservation in the junction

$$i) \quad q_{total}^* = q_{w1}^* + q_{w2}^* \quad ? \quad \text{NO}$$

YES  
↓

$p_j^*, q_{w1}^*, q_{w2}^*, q_{total}^*$  are the equilibrium conditions

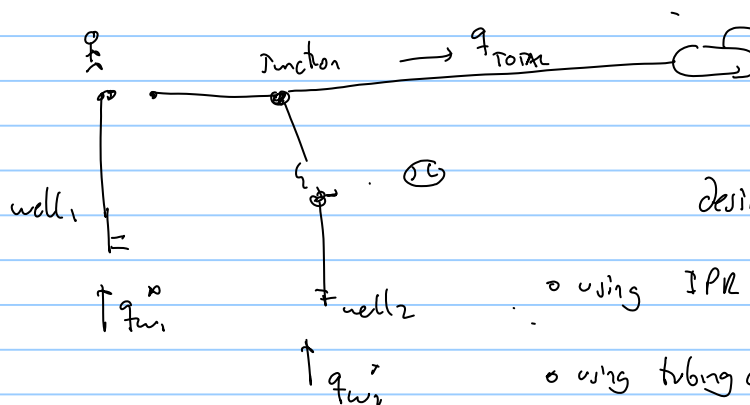


the equilibrium point is often calculated numerically, graphically is more difficult with increasing number of junctions.

equations	unknowns	Nr eqs	Nr unknowns
IPR eq 1, IPR eq 2	$q_{w1}, q_{w2}$ $p_{wf1}, p_{wf2}$	2	4
tubing eq 1, tubing eq 2	$p_{wh1}, p_{wh2}$	4	6
flowline 1, flowline 2	$p_j$	6	7
Pipeline eq	$q_{total}$	7	8
mass conservation in the junction $q_{total} = q_1 + q_2$		8	8



Fixed rate calculation method for networks.



desired rates  $q_{w1}^*, q_{w2}^*$

- using IPR and  $q_w^*$  calculate  $p_{wf1}, p_{wf2}$
- using tubing equation,  $p_{wf}, q_w$  calculate  $p_{wh1}, p_{wh2}$
- using pipeline equation,  $p_{sep}, q_{total}^* = q_{w1}^* + q_{w2}^*$   
calculate  $p_j$
- using flowline equations for each well,  $p_j, q_{w1}^*, q_{w2}^*$   
calculate  $p_{dc1}, p_{dc2}$  dc -- downstream of choke

verify if  $P_{wh1} > P_{dc1}$   
 $P_{wh2} > P_{dc2}$

if there are adjustable elements A network can be considered as a function that provides well rates with certain setting of the adjustable element

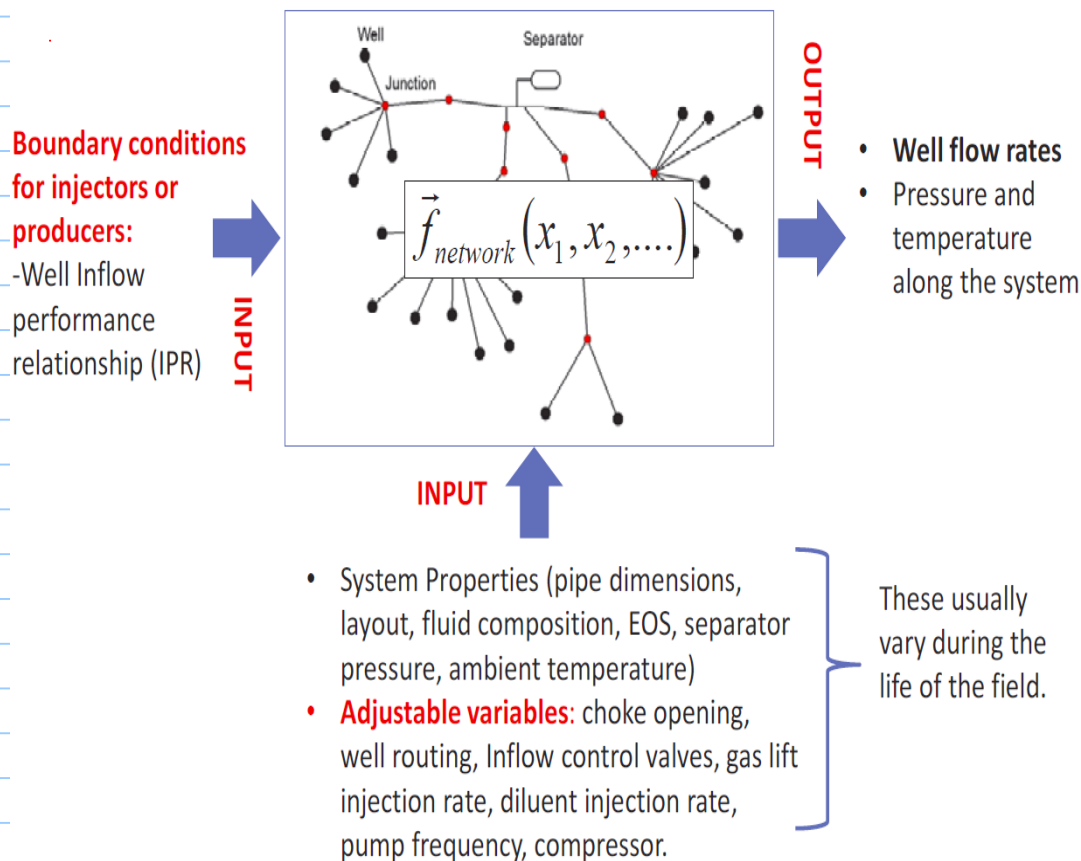
output

input

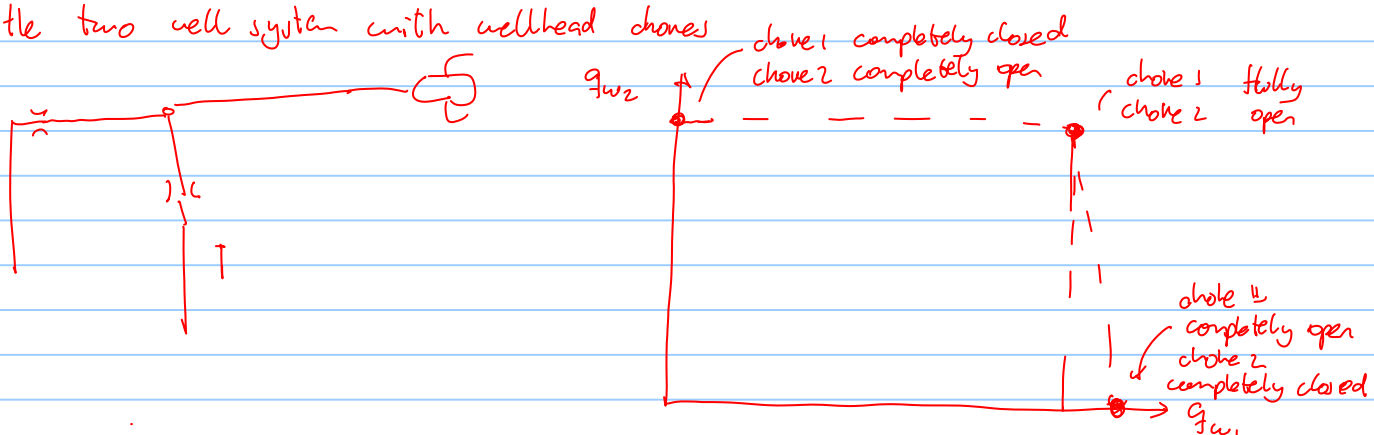
choke opening 1

choke opening 2

3.

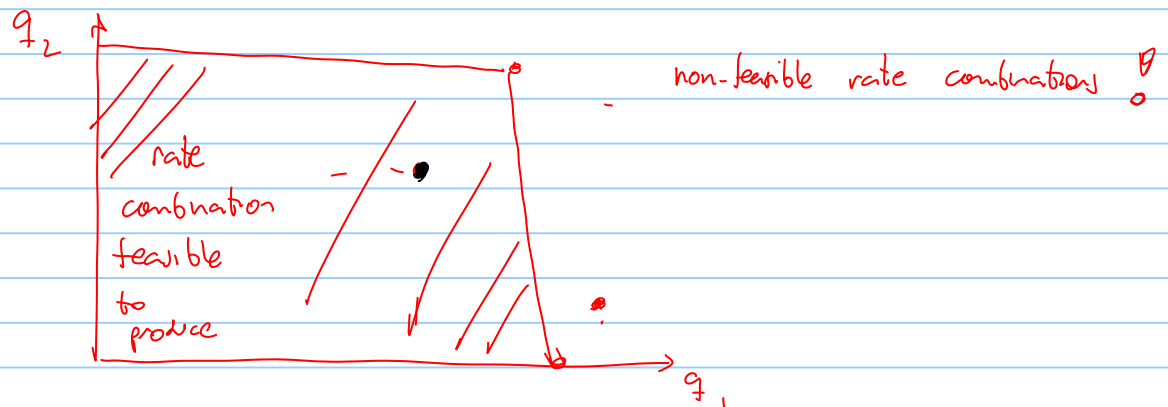


for the two well system with wellhead chokes



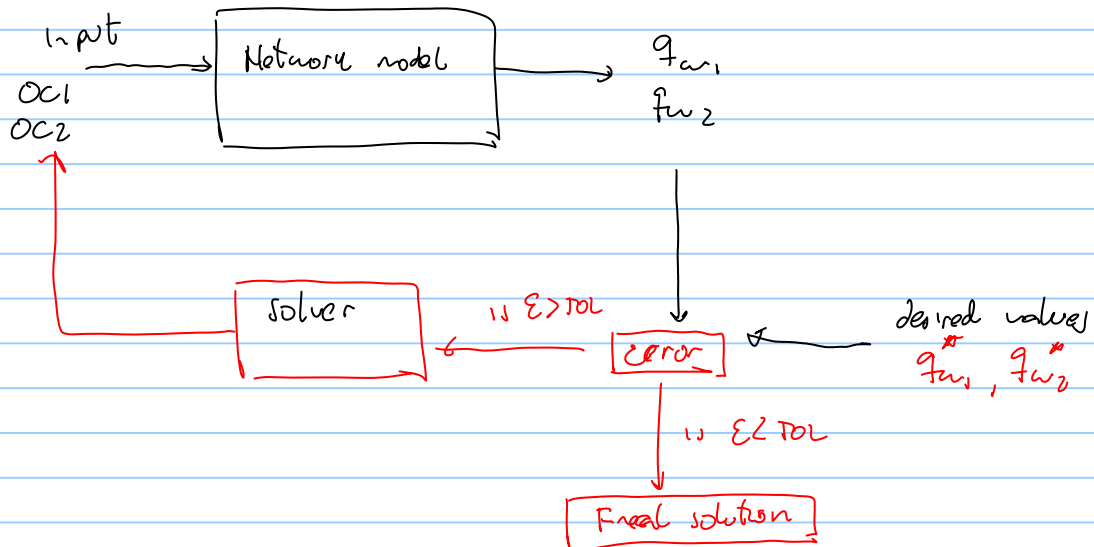


if I run my network with infinite combinations of choke points

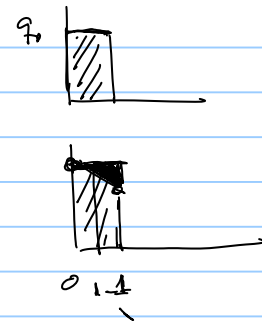
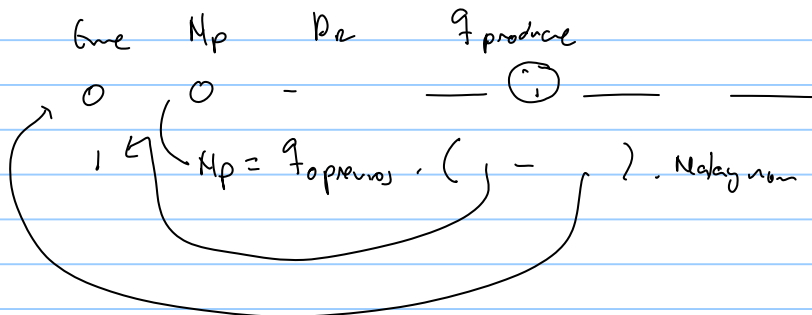


in commercial software the process of finding the settings of adjustable elements that give a certain rate combination  $(\vec{q}_w, \vec{q}_w)$  is wrongly called optimization. ⚠

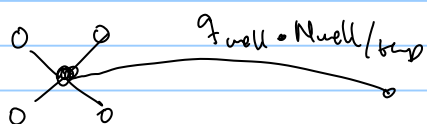
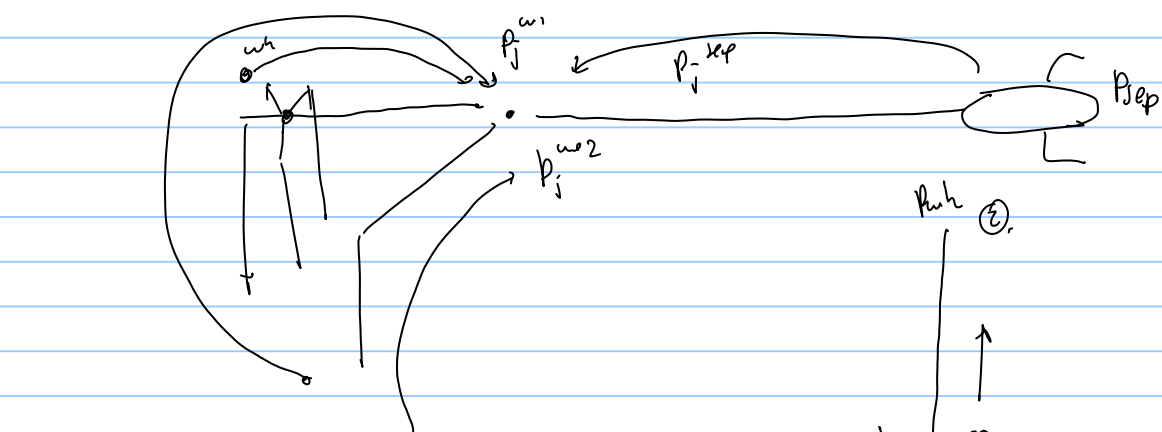
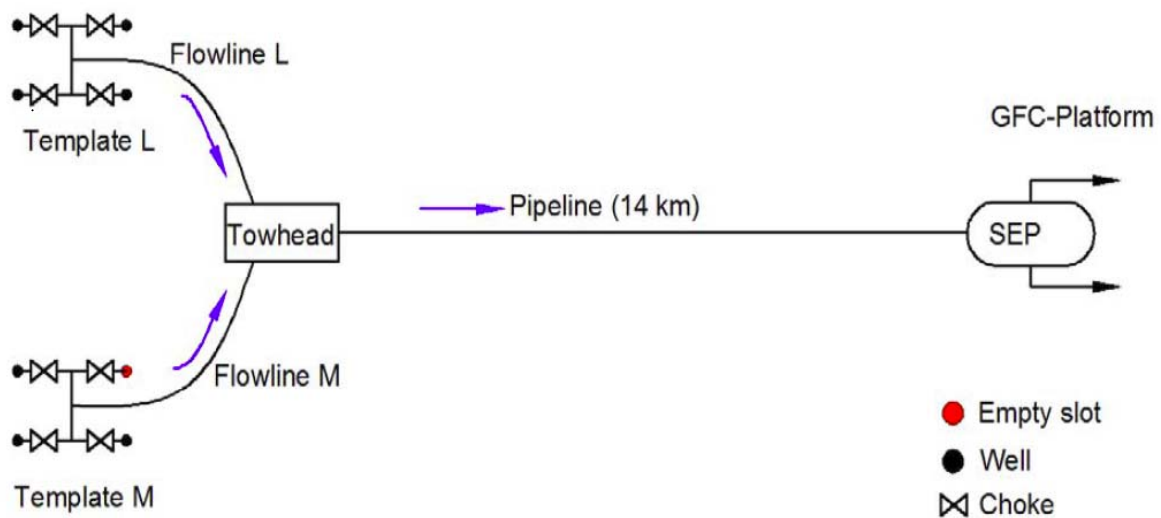
opening of choke OC







Topic for today: network solving - class exercise



$$p_i^{w1} + p_i^{w2} + p_i^{sep} = p_{av}$$

$$p_i^{w1} - p_{av} \rightarrow 0$$

TPG4230, Milan Stanko, 20170228														
Separator pressure, psep	60	bara												
	Nwells	pR [bara]	pwf [bara]	C [Sm <sup>3</sup> /bar <sup>2</sup> n]	n	qg [Sm <sup>3</sup> /d]	Ct [Sm <sup>3</sup> /bar]	S	pwh [bara]	qtemp [Sm <sup>3</sup> /d]	Cfl [Sm <sup>3</sup> /bar]	ptowhead[bara]	error [bara <sup>2</sup> ]	
Template L	4	145	99.6	1000	0.8	1.72E+06	38152	0.43	66.6	6.89E+06	1403054	66.5	0.0	
Template M	3	102	80.4	700	0.8	5.27E+05	41163	0.34	66.5	1.58E+06	1397663	66.5	0.0	
Pipeline									qfield [Sm <sup>3</sup> /d]=	8.47E+06	296439	66.5	0.0	
											average p, [bara]=	66.5	0.0	Error

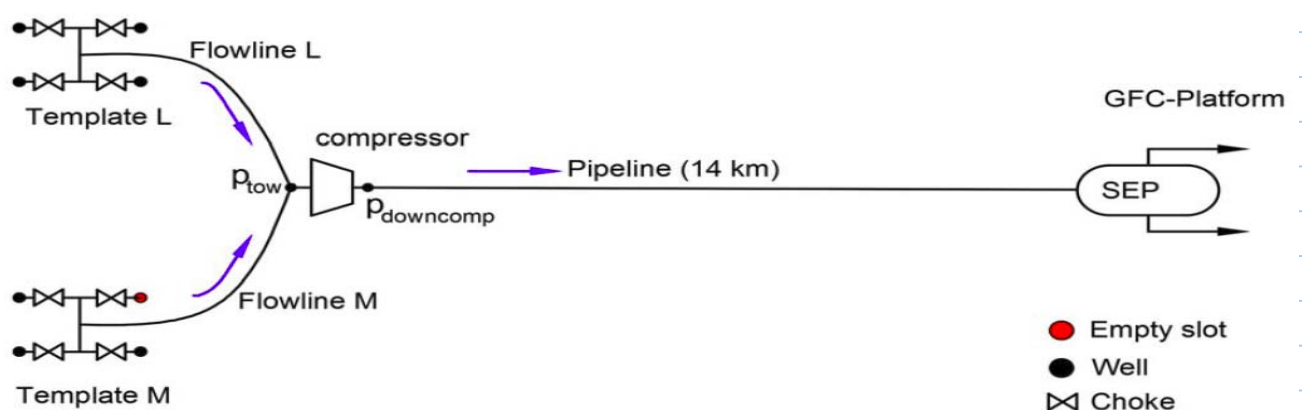
the reservoir engineer want to produce 1.5 EG from each well in template L  
 5 EG from " " " " " M  
 is that possible?

TPG4230, Milan Stanko, 20170228														
Separator pressure, psep	60	bara												
	Nwells	pR [bara]	pwf [bara]	C [Sm <sup>3</sup> /bar <sup>2</sup> n]	n	qg [Sm <sup>3</sup> /d]	Ct [Sm <sup>3</sup> /bar]	S	pwh [bara]	qtemp [Sm <sup>3</sup> /d]	Cfl [Sm <sup>3</sup> /bar]	ptowhead[bara]	ptemp[bara]	Deltapchoke[bar]
Template L	4	145	108.1	1000	0.8	1.50E+06	38152	0.43	78.0	6.00E+06	1403054		65.3	12.8
Template M	3	102	81.9	700	0.8	5.00E+05	41163	0.34	67.9	1.50E+06	1397663		65.1	2.8
Pipeline									qfield [Sm <sup>3</sup> /d]=	7.50E+06	296439	65.1		
											average p, [bara]=			

TENTATIVE PLAN

2<sup>nd</sup> exercise deadline is 06.03  
 3<sup>rd</sup> exercise deadline is 21.03  
 4<sup>th</sup> exercise deadline is 09.04 ± 90 days  
 5<sup>th</sup> exercise deadline is 05.05

task 2.



TPG4230, Milan Stanko, 20170228 Separator pressure, psep																
	60		bara													
Template L	Nwells	pR [bara]	pwf [bara]	C [Sm <sup>3</sup> /bar <sup>2</sup> n]	n	qg [Sm <sup>3</sup> /d]	Ct [Sm <sup>3</sup> /bar]	S	pwh [bara]	qtemp [Sm <sup>3</sup> /d]	Cfl [Sm <sup>3</sup> /bar]	ptowhead[bara]	error [bara^2]			
Template M	4	145	96.5	1000	0.8	1.80E+06	38152	0.43	62.2	7.19E+06	1403054	62.0	0.0			
Pipeline	3	102	75.7	700	0.8	6.04E+05	41163	0.34	62.0	1.81E+06	1397663	62.0	0.0			
										qfield, calc [Sm <sup>3</sup> /d]	AVERAGE ptow=	error - rate (calc-wanted)^2	sum error, tow press			
										9.00E+06	62.0	9.55E-09				
										qfield - wanted [Sm <sup>3</sup> /d]	Cfl [Sm <sup>3</sup> /bar]	pdowncomp[bara]				
										error-rate (calc-wanted)^2	296439	67.2				
											DP comp [bara]					

Problemløserparametre

Angi mål:

Til: ☐ Maks ☒ Min ☐ Verdi av:

Ved å endre variabelceller:  
SD55:SD56

Underlagt begrensningene:  

SKS10 = 0

Legg til

Endge

Slett

Tilbakestill alle

Last inn / lagre

☒ Gjør ubegrensede variabler ikke-negative

Vlg en løsningsmetode: 

Ikke-lineær GRG

Alternativer

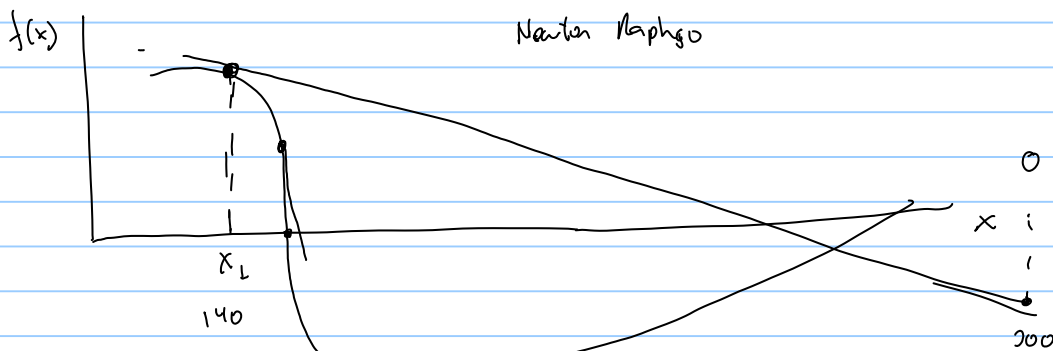
Løsningsmetode  
Velg ikke-lineær GRG for Problemløser-problemer som er jevne og ikke-lineære. Velg LP (simpleks) for lineære problemer, og velg Evolutionsør for problemer som er ujevne.

Hjelp

Løs

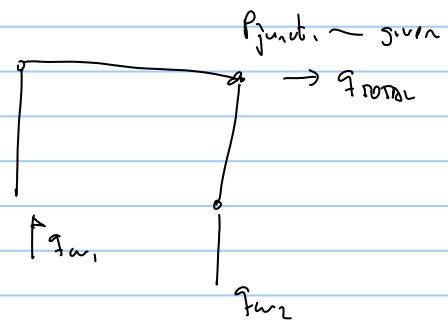
Lukk

This initial setup of the solver, although sounds logical, gives VALUE! errors problems and doesn't converge. some of the bottomhole pressures tried give a negative number inside the square root. Maybe it is related with the shape of the function:  
! Investigate this issue more in detail in the assignment!



An alternative approach is suggested, "Manual solution", analyzing and converging this problem separately:

provide pav at the towhead, and take out the field rate constraint out of the solver setting. Run for several values of pav at the towhead to find the one that gives exact 09E06 Sm<sup>3</sup>/d



TPG4230, Milan Stanko, 20170228														
Separator pressure, psep														
	60		bara											
Template L	Nwells	pR [bara]	pwf [bara]	C [Sm <sup>3</sup> /bar <sup>2</sup> n]	n	qg [Sm <sup>3</sup> /d]	Ct [Sm <sup>3</sup> /bar]	S	pwh [bara]	qtemp [Sm <sup>3</sup> /d]	Cfl [Sm <sup>3</sup> /bar]	ptowhead[bara]	error [bara <sup>2</sup> ]	
Template M	4	145	96.5	1000	0.8	1.80E+06	38152	0.43	62.2	7.19E+06	1403054	62.0	0.0	
Pipeline	3	102	75.7	700	0.8	6.04E+05	41163	0.34	62.0	1.81E+06	1397663	62.0	0.0	
										qfield, calc [Sm <sup>3</sup> /d]	AVERAGE ptow=	error - rate (calc-wanted)^2	sum error, tow press	
										9.00E+06	62.0	1.39E-08		
										qfield - wanted [Sm <sup>3</sup> /d]	Cfl [Sm <sup>3</sup> /bar]	pdowncomp[bara]		
										error-rate (calc-wanted)^2	296439	67.2		
											DP comp [bara]			

Problem-løserparametre

Angi mål:

Til: ☐ Maks ☒ Min ☐ Verdi av:

Ved å endre variabelceller:

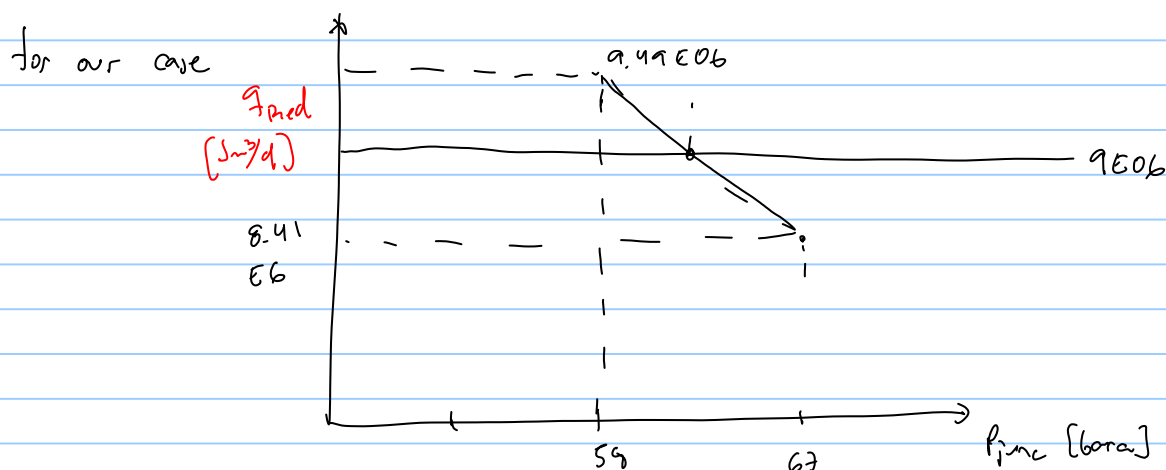
Underlagt begrensningene:

☒ Gjør ubegrensede variabler ikke-negative

Velg en løsningsmetode:

Løsningsmetode

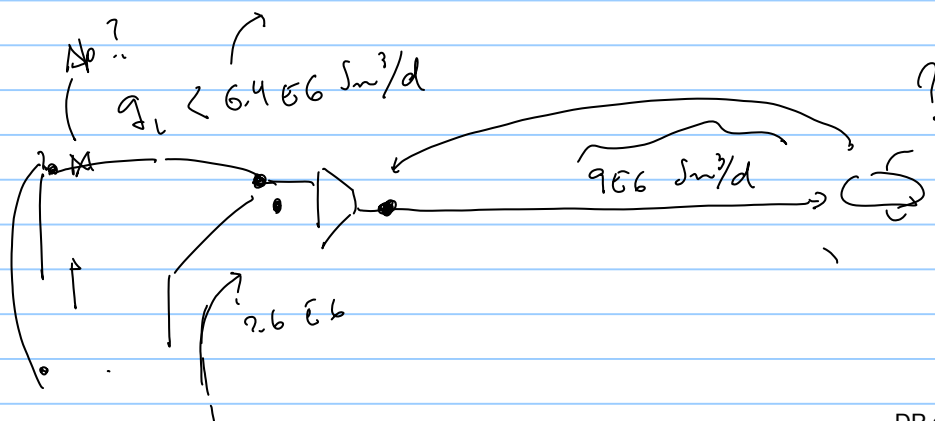
Velg ikke-lineær GRG for Problem-løser-problemer som er jevne og ikke-lineære. Velg LP (simpleks) for lineære problemer, og velg Evolusjonær for problemer som er ujevne.



task 3

One way of solving the problem is to fix the rates in the system,  $6.4 \text{ E}06 \text{ Sm}^3/\text{d}$  for template L,  $2.6 \text{ E}06 \text{ Sm}^3/\text{d}$  for template M and  $9 \text{ E}06 \text{ Sm}^3/\text{d}$  for the pipeline. Calculations are performed in the following way:

- Counter current calculation in pipeline from separator to compressor discharge.
- Co current calculations in template M from reservoir to suction of the compressor. Template M is NOT choked, thus we can perform calculations without problems.
- The DP of the choke in wells of template L is unknown. So, co-current calculations have to be carried from reservoir to wellhead, to find pressure upstream the choke and counter current calculations from the compressor suction (towards the template (downstream the choke) the difference in pressure is the choke pressure drop.



Co-current													
TPG4230, Milan Stanko, 20170228													
Separator pressure, psep	60	bara											
	Nwells	pR [bara]	pwh [bara]	C [Sm <sup>3</sup> /bar <sup>2</sup> n]	n	qg [Sm <sup>3</sup> /d]	Ct [Sm <sup>3</sup> /bar]	S	pwh [bara]	Ptemp [bara]	Deltapchoke [bara]	qtemp [Sm <sup>3</sup> /d]	Cfl [Sm <sup>3</sup> /bar]
Template L	4	145	104.4	1000	0.8	1.60E+06	38152	0.43	73.3	41.8	31.5	6.40E+06	1403054
Template M	3	102	55.3	700	0.8	8.67E+05	41163	0.34	41.6	41.6	0.0	2.60E+06	1397663
												AVERAGE ptow=	
												Cfl [Sm <sup>3</sup> /bar]	
Pipeline												qfield - wanted [Sm <sup>3</sup> /d]	296439
												error - rate	67.2
												DP comp [bara]	25.7

Co-current

counter-current

DP choke =  
pwh - ptemp

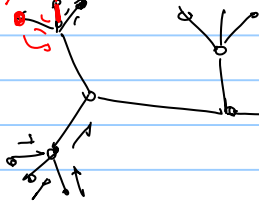
Counter-current

given

- Next class 09.03.2017 will be in P2. MBAL, PROSPER, GAP → networks (PETEX (petroleum experts))

10 Academic licenses available.

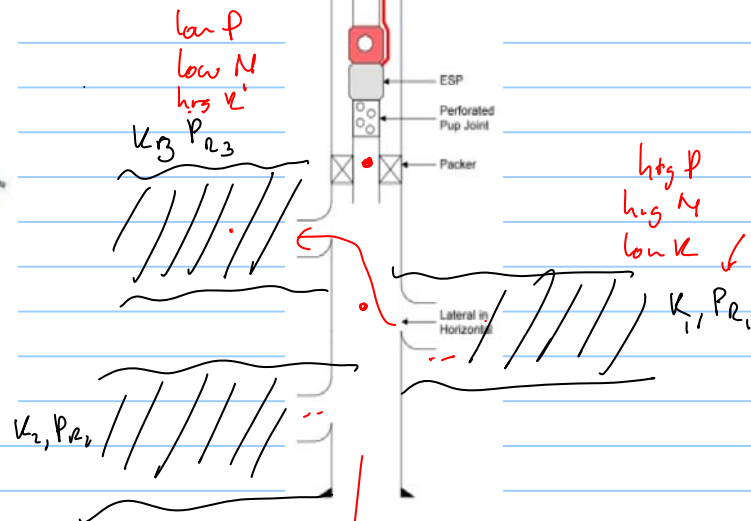
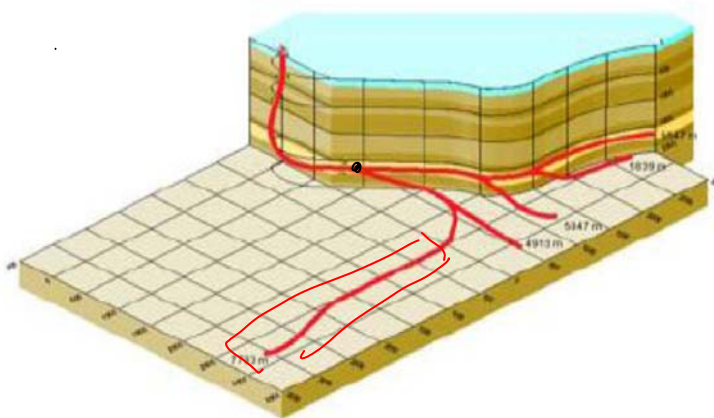
$P_{a,j}, P_{a,j}$



Pressure calculated counter-current and co-current is the same for a given point.

mass balance → surface rates should be conserved

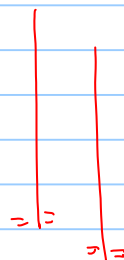
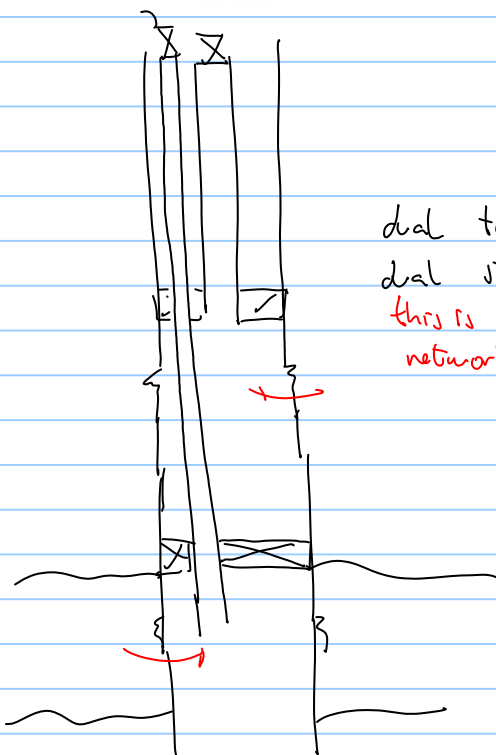
- We have downhole networks : multilateral wells



multilayer if  $P_{2i}$  are different are might have cross flow between formations

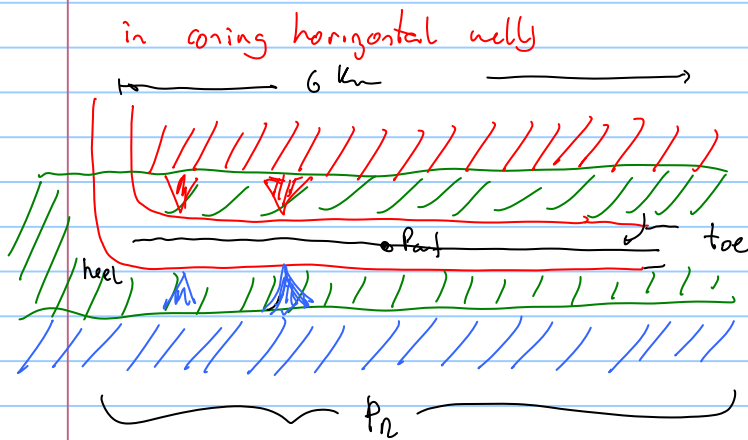
TP2 formation "charge" other formations.

dual tubing completions  
dual strings completion  
this is NOT a downhole network!



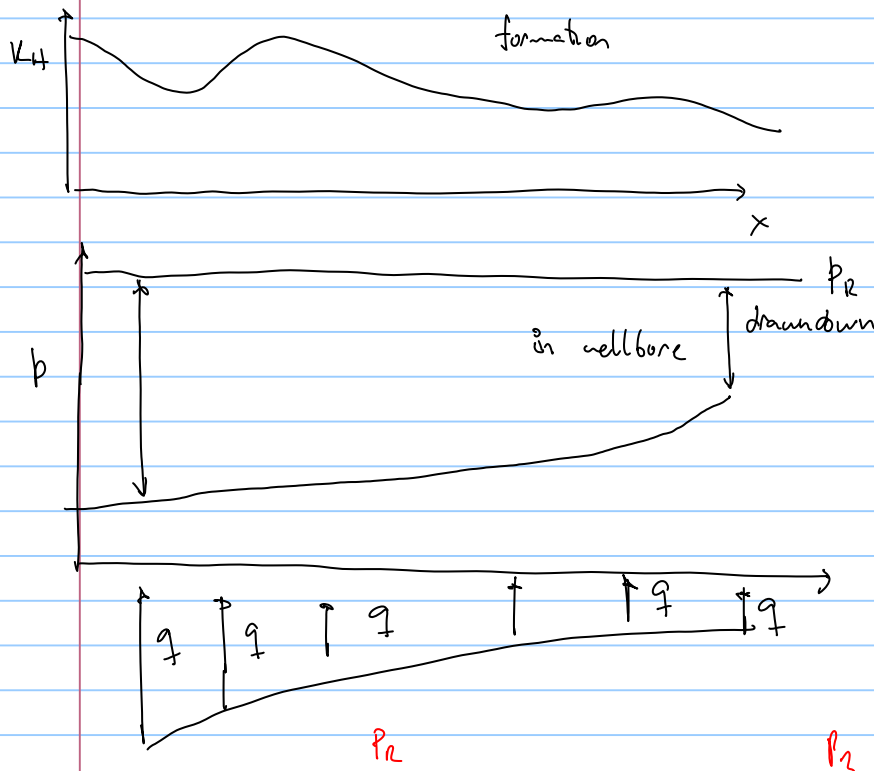


Inflow control devices (ICD) to control (passive or active) the rates coming out of a given formation, section)

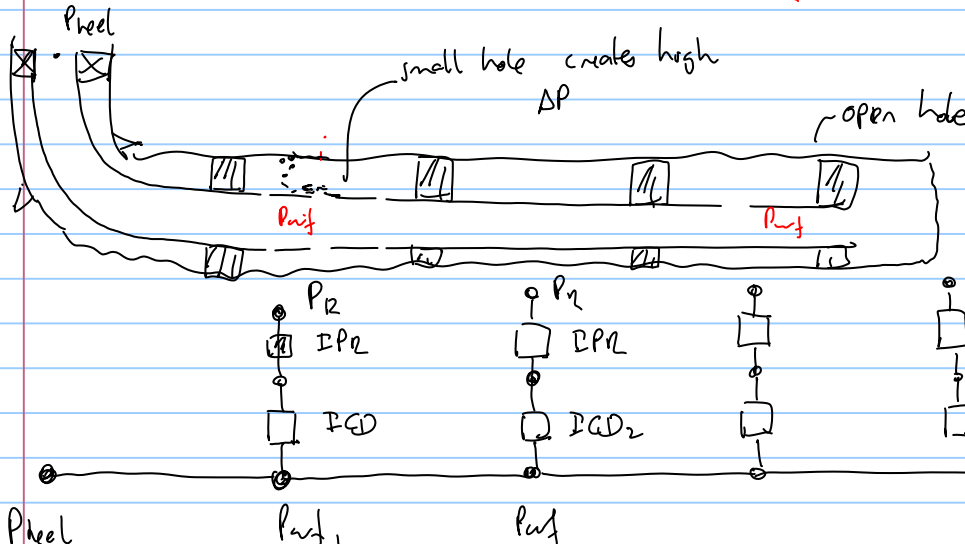


$$\frac{\Delta p}{\Delta x} \propto \frac{1}{k} \quad q = \frac{k}{\mu} \frac{\partial p}{\partial x}$$

M r



this causes an uneven distribution of inflow, of reservoir rates along the wellbore which can cause coning, uneven depletion, etc



→ slotted liner wire mesh

### Completion design

Design of ICD  
o determine the number of sections

• define the orifice diameter and number of orifices

Netool ~ Weatherford? commercial simulator to design completions.

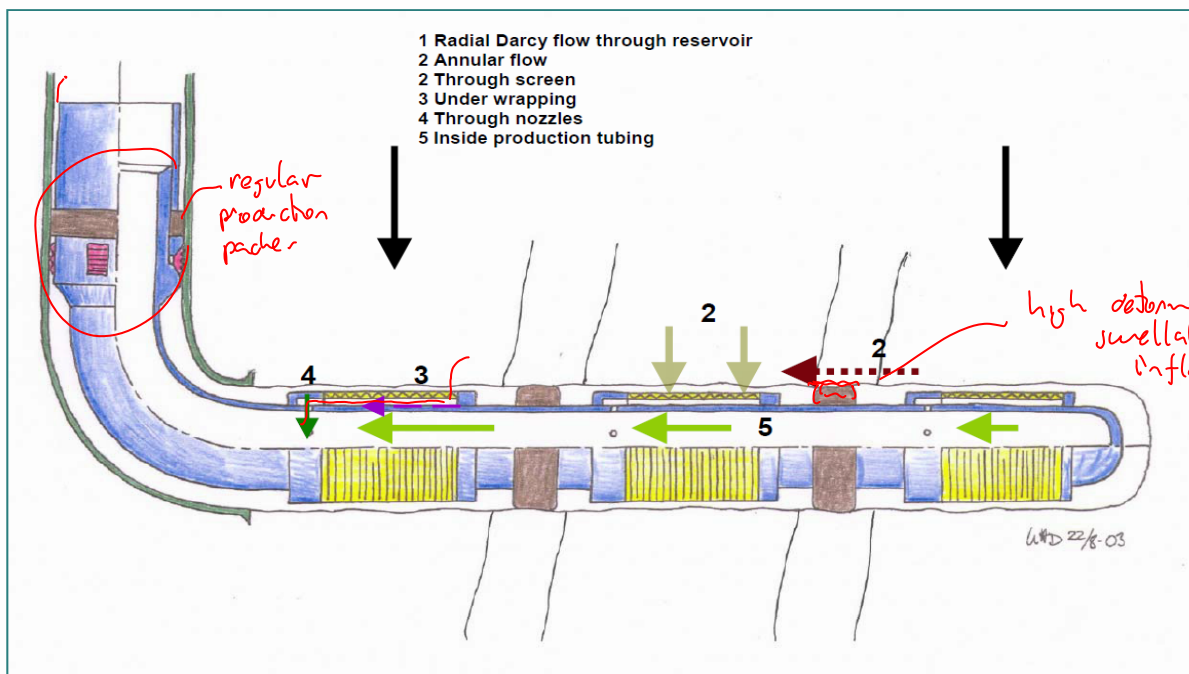
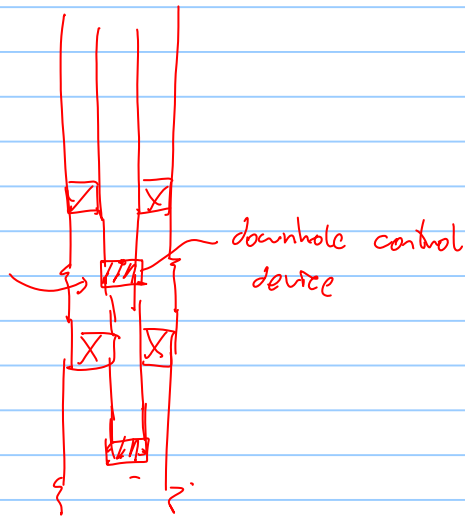


Figure-8 Functioning and interplay of an ICD completion architecture. Fluids enter the screen and flow between the axial wires and the un-perforated base pipe into the ICD housing, before passing through. Issues are properly analyzed and put in the right perspective to achieve

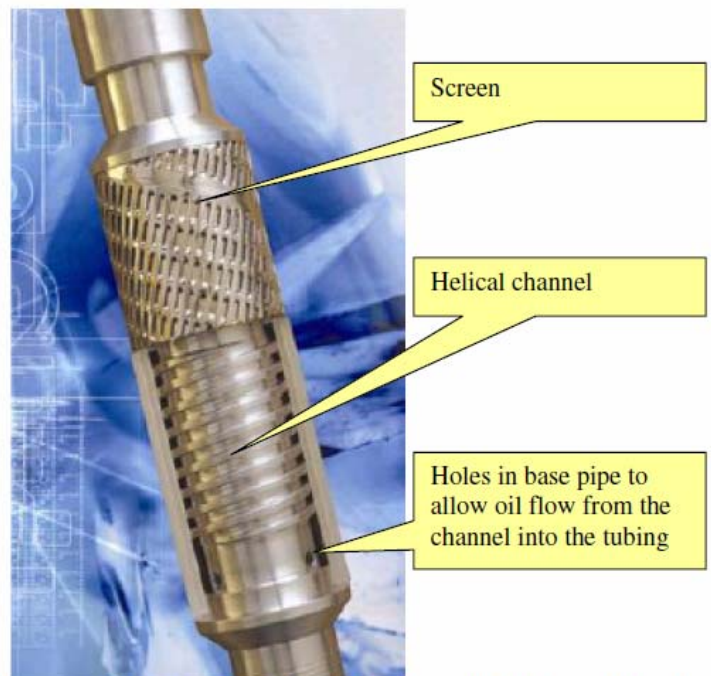
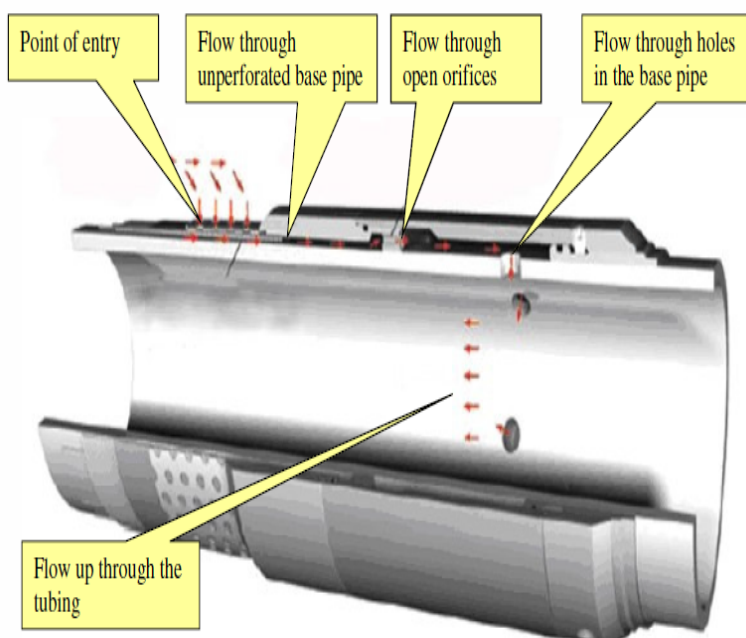
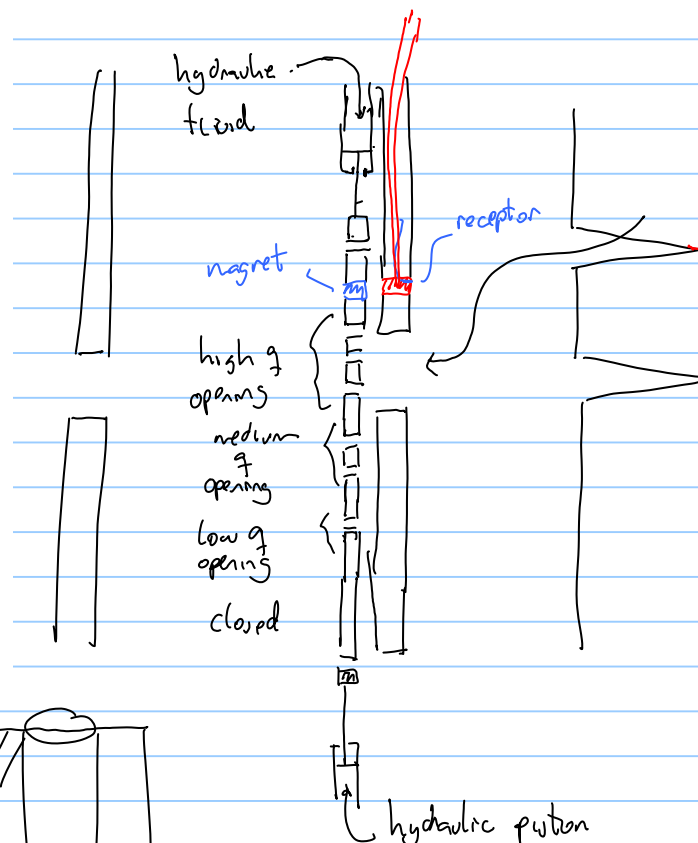
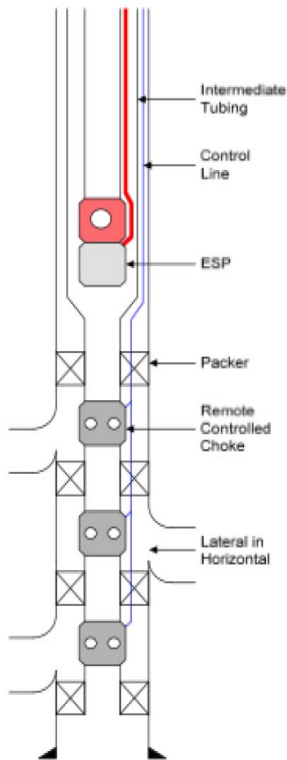
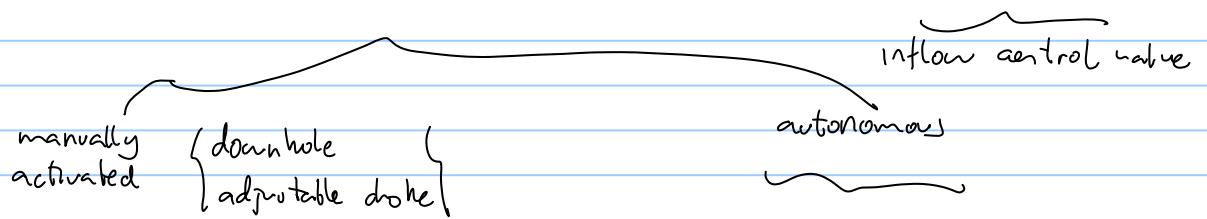


Figure 14 Helical channel type, Equalizer™, Baker Oil Tools [22]

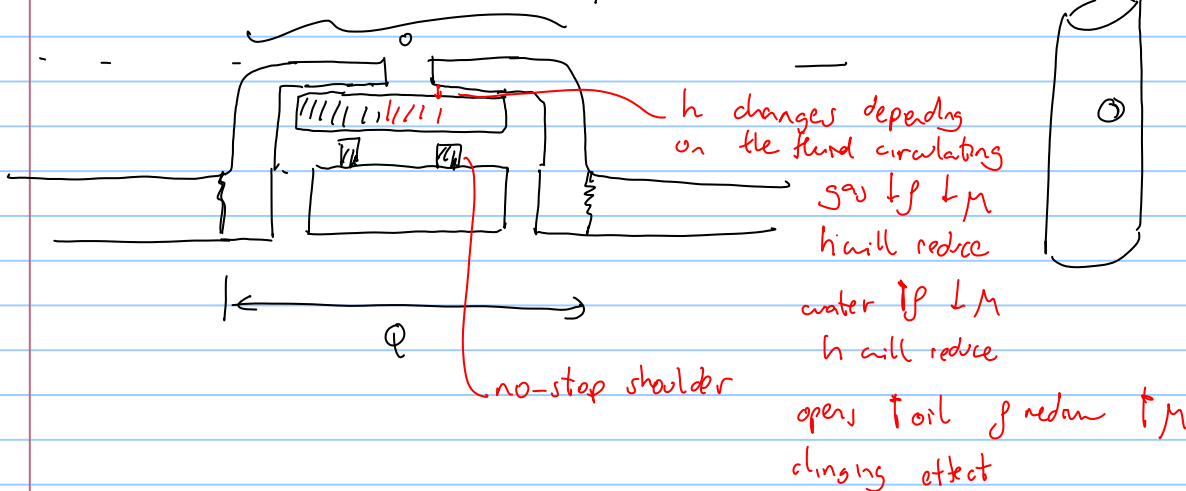
So far we have discussed passive inflow control devices

but we also have active inflow control devices (ICV)



• Autonomous,

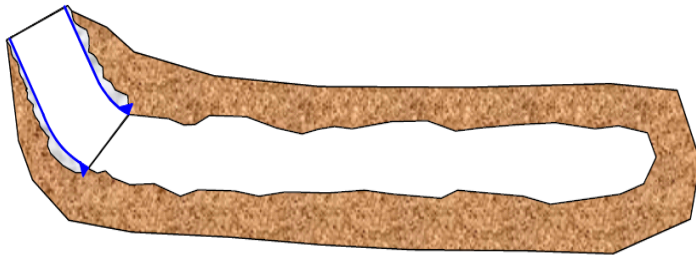
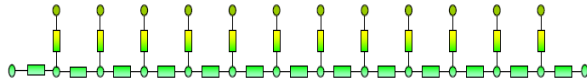
AICD, AICV



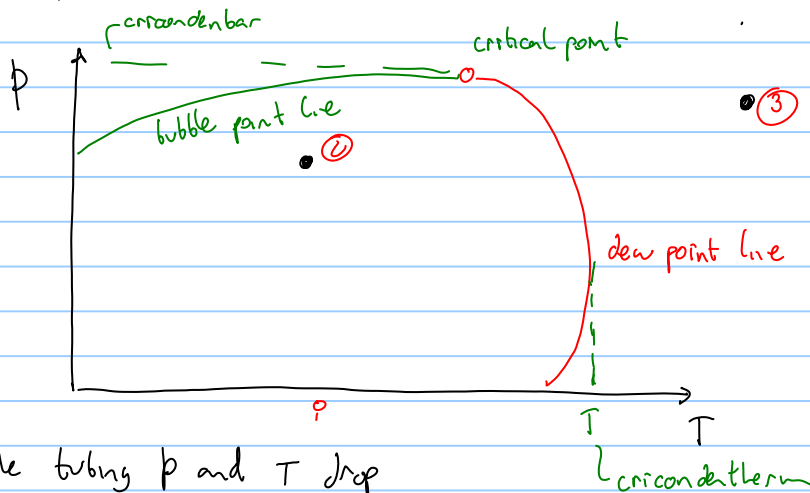
if there is a big variation of reservoir properties along the wellbore

it is also necessary to use network solving.

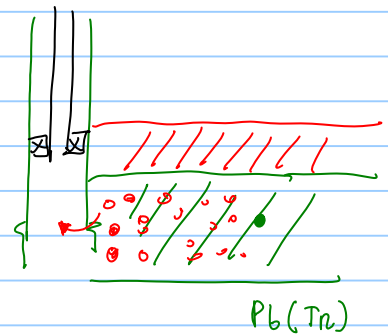
- Horizontal well with Open Hole completion  
- Including damage zone



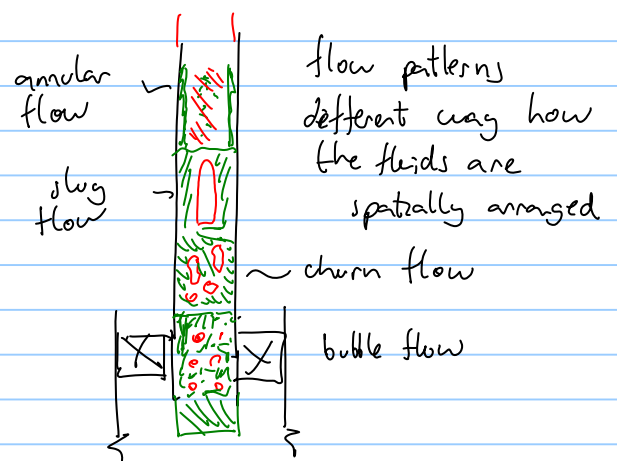
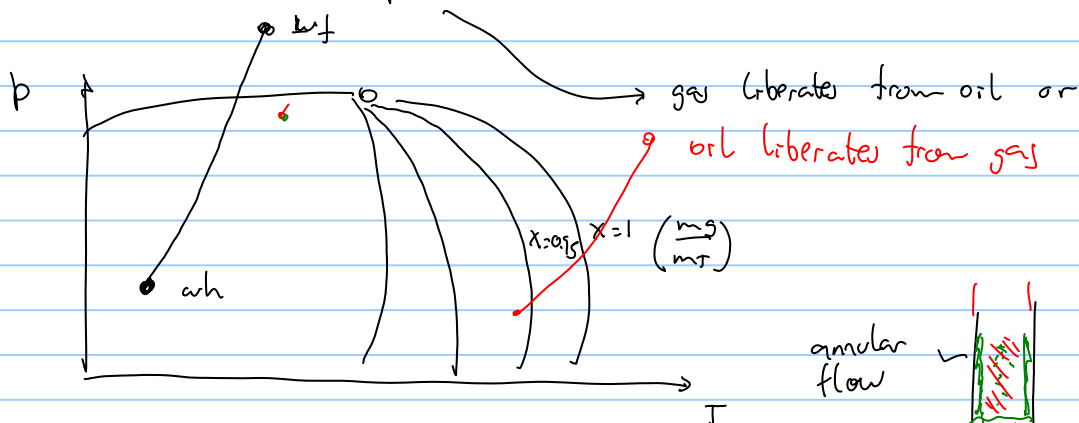
Multiphase flow:



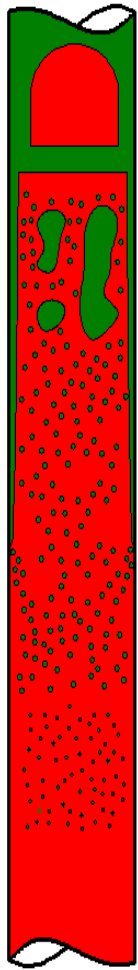
possible entry points to wellbore



in the tubing p and T drop



course on multiphase flow,  
TEP4250 Ole Jørgen Nydal {



slug flow

- be able to estimate  $\Delta p$ ,  $\Delta T$  with length

churn flow

- due to variation in  $p$ ,  $T$ , and the variation in flow patterns, the  $\Delta p$  calculation have to be made in a stepwise manner.

→ subdivide the tubing in segments!

- there are two ways to study multiphase flow

annular flow

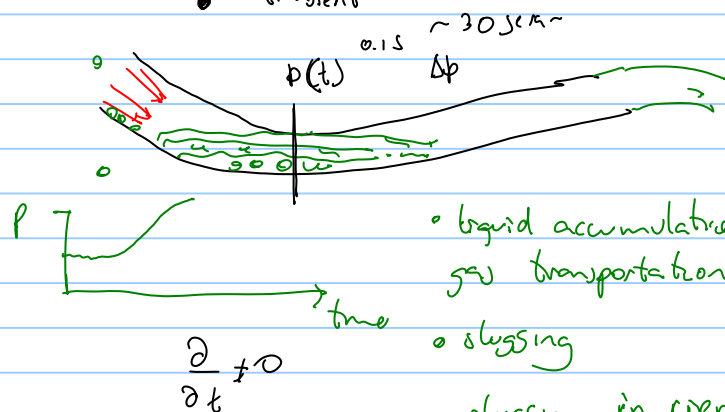
- steady state  $\left\{ \frac{\partial}{\partial t} = 0 \right.$

↳ pipes, pipeflow, PEO, prosper, gap

dense mist

- transient

mist flow



- liquid accumulation in gas transportation pipelines

- slugging

- slugging in rivers

commercial tools : OLGA, HedaFlow.

transient multiphase flow simulator

- there are two approaches to analyze multiphase flow

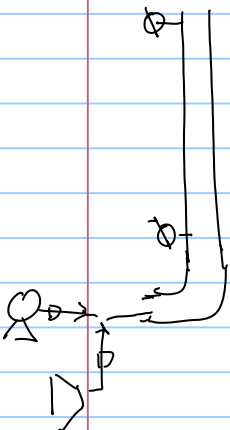
- correlation-based, Beggs and Brill, Orkiszewski, Ans and Roy, Hagedorn and Brown

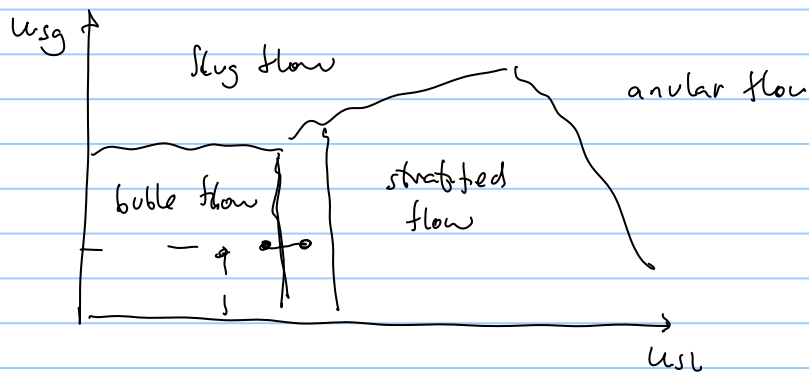
correlations develop based on experimental data, some physics and limited range of applicability

Superficial velocity  $v_{sl} = \frac{q_L}{A_p} \rightarrow m^3/s$

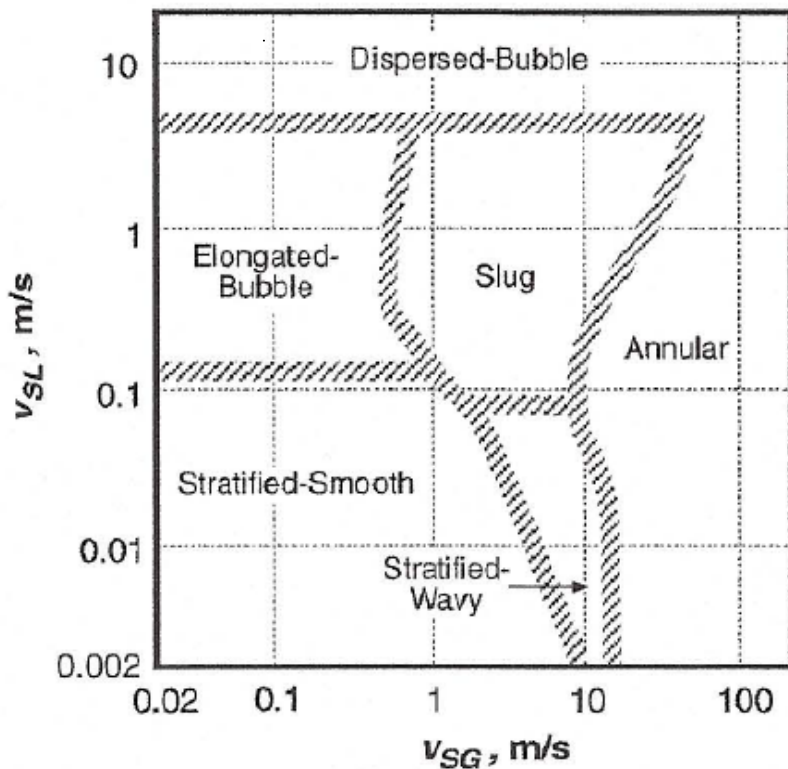
$A_p$  ~ cross section area of pipe ( $\pi r^2$ )

$$v_{sg} = \frac{q_g}{A_p}$$





this plot depends on fluid properties  $\left\{ \begin{array}{l} \rho_o, \rho_g \\ \mu_o, \mu_g \\ \sigma_{og} \end{array} \right.$   
inlet condition, pipe diameter

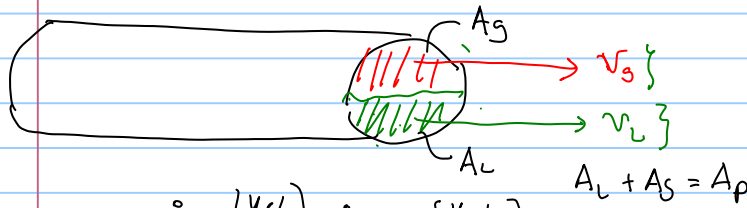
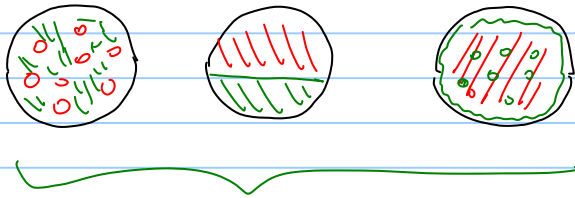


Fr and We

- mechanistic modeling  $\rightarrow$  applying  $\left\{ \begin{array}{l} \text{mass conservation for each phase} \\ \text{momentum conservation} \left\{ \begin{array}{l} \text{to each phase} \\ \text{to the mixture} \end{array} \right. \end{array} \right.$   
 $\rightarrow$  closure laws derived empirically (by exp)

$$-\frac{dp}{dL} = \underbrace{-\frac{dp}{dL}}_{\text{friction}} \underbrace{-\frac{dp}{dL}}_{\text{gravity}} \underbrace{-\frac{dp}{dL}}_{\text{acceleration}} \quad \text{momentum equation mixture}$$

$$-\frac{dp}{dL} = \frac{2}{d} f_{TP(F)} \rho_{TP} v_{TP}^2 + \underbrace{\rho_{TP}}_{\text{density of the mixture}} g \sin \theta + \rho_{TP} v_{TP} \frac{dv_{TP}}{dL}, \quad \left. \begin{array}{l} \text{momentum eq. for the mixture} \end{array} \right\}$$



if we assume  $v_g = v_L$

• homogeneous model

• no slip model

} bubble flow  
must flow

$$\dot{m}_g \left[ \frac{kg}{s} \right] \quad \dot{m}_L \left[ \frac{kg}{s} \right]$$

$$\rho_g \quad \rho_L \quad @ P, T$$

local flow rate  $q_g = \frac{\dot{m}_g}{\rho_g} \quad q_L = \frac{\dot{m}_L}{\rho_L}$

$$v_g = \frac{q_g}{A_g} \quad v_L = \frac{q_L}{A_L}$$


if homogeneous model

$$v_L = v_g \Rightarrow \frac{q_g}{A_g} = \frac{q_L}{A_L} \quad A_L = A_p - A_g$$

$$A_p - A_g = \frac{q_L}{q_g} A_g$$

$$A_p = \left( \frac{q_L}{q_g} A_g + A_g \right)$$

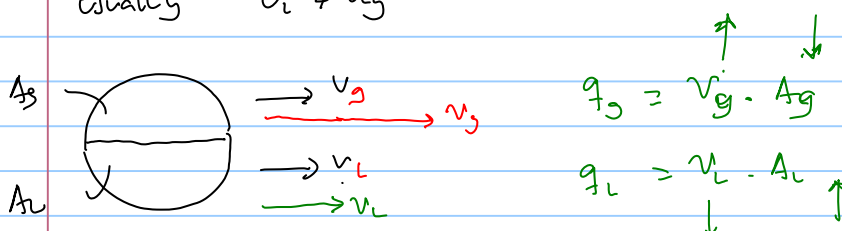
$$\frac{A_p}{A_g} = \left( \frac{q_L}{q_g} + 1 \right)$$

  $\left\{ \frac{A_g}{A_p} = \frac{1}{\frac{q_L}{q_g} + 1} = \left( \frac{q_g}{q_L + q_g} \right) \right. \sim \text{gas volume fraction } (\lambda_g)$

$$\rho_m = \lambda_g \rho_g + (1 - \lambda_g) \rho_L$$

$\lambda_L$

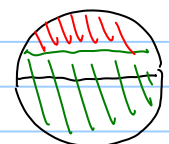
usually  $v_L \neq v_g$



$$q_g = v_g \cdot A_g$$

$$q_L = v_L \cdot A_L$$

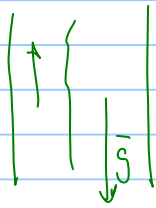
if the gas travels faster than liquid  
liquid holdup =  $h_L = \frac{A_L}{A_p}$  with slip





$$H_L \neq \lambda_L$$

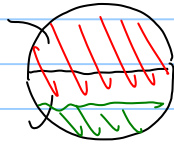
$$\rho_m = H_L \rho_L + (1 - H_L) \rho_g$$



in upwards flow gravity pulls liquid down, thus  $v_g > v_L$



in downwards flow gravity helps liquid down thus  $v_g < v_L$

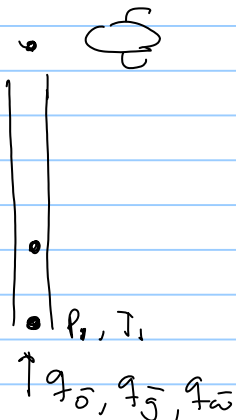


Calculating the real fluid velocities: 
$$v_L = \frac{q_L}{A_L} = \frac{q_L}{H_L A_p} = \left( \frac{u_{SL}}{H_L} \right)$$

$$v_g = \frac{q_g}{(1 - H_L) A_p} =$$

• How to perform multiphase calculation in conduits

① Depart from a point with known  $p, T$ , assume rate. calculate the rest with GOR, WC. (depth)



② Convert from sc to local conditions

Black oil

compute black oil properties  
from table, correlation

$$\begin{bmatrix} q_g \\ q_o \\ q_w \end{bmatrix} = \begin{bmatrix} \frac{B_g}{1 - R_s \cdot r_s} & \frac{-B_g \cdot R_s}{1 - R_s \cdot r_s} & 0 \\ \frac{-B_o \cdot r_s}{1 - R_s \cdot r_s} & \frac{B_o}{1 - R_s \cdot r_s} & 0 \\ 0 & 0 & B_w \end{bmatrix}_{(p,T)} \cdot \begin{bmatrix} q_{\bar{g}} \\ q_{\bar{o}} \\ q_{\bar{w}} \end{bmatrix}$$

(obtain  $q_g, q_o, q_w$ )

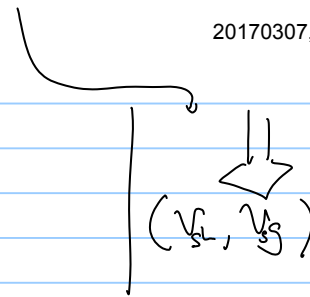
compositional model  
(EoS) Peng Robinson, SRK  
composition is available  
 $z_i \begin{cases} C_1 & z_{C1} \\ C_2 & z_{C2} \\ C_3 & z_{C3} \end{cases}$

calculate the mass fraction of oil and gas  
 $x_g = \frac{m_g}{m_t} @ p, T$

Calculate  $\dot{m}_g @ p, T$   
 $\dot{m}_L$

with  $\dot{m}_t$

• calculate  $q_g, q_o$  using properties  $\rho_g, \rho_o$



- with input  $V_{SL}, V_{SG}, \Phi$ , inclination,  $\varepsilon$ ,  $\rho_g, \rho_L, \mu_g, \mu_L, T_{og}, T_{ow}$   
 $\underbrace{\hspace{10em}}_{\text{roughness}} \quad \underbrace{\hspace{10em}}_{T_{gw}}$

multiphase experts

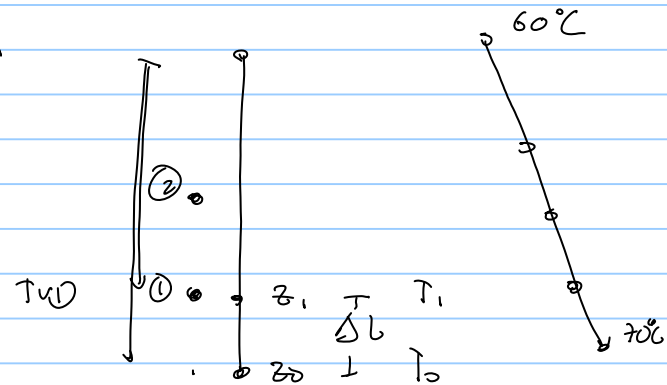
→ give me  $\left[ \frac{dP}{dz} \right]$

- numerical integration of ODE
  - explicit
    - Euler's method
    - Corrector predictor
    - Runge-Kutta etc
  - implicit

$$\left. \frac{dP}{dz} \right\} \text{ with starting point } P=P_0 \text{ @ } z=z_0$$

Euler's method

$$P_2 = P_0 + \Delta L \cdot \left. \frac{dP}{dz} \right|_{z_0}$$



for the next point one needs to have  $T_1$  beforehand

or if a Temperature drop model is available  $T = f(z)$

AND Repeat

### CLASS EXERCISE

fluid calculator to calculate  $X_o = \frac{m_o}{m_T}$ ,  $\rho_s, \rho_g$  need a fluid model, calculator

Compositional  $\left\{ \begin{array}{l} \text{HYSYS process simulator} \\ \text{DWSIM} \end{array} \right.$

SUM	=G4*1000*G11/(24*3600)																	
	A	B	C	D	E	F	G	H	I	J	K	L	M	N	O	P	Q	R
1	TPG4230, Prof. Milan Stanko, 20170307																	
2			Mole %	Mole frac														
3		Nitrogen	0.4	0.004		qo [Sm^3/d]	1000											
4		CO2	0.1	0.001		qg [E03 Sm^3/d]	200											
5		Methane	43.2	0.432		pwf [bara]	147											
6		Ethane	4.7	0.047		TR [C]	70											
7		Propane	3.0	0.03		ID [m]	0.12											
8		i-butane	1.5	0.015		Well TVD Depth [m]	2500											
9		n-butane	0.9	0.009		TwH [C]	60											
10		neo-pentane	0.0	0		Sc oil density [Kg/m^3]	850											
11		i-pentane	0.8	0.008		Sc gas density [Kg/m^3]	0.91											
12		n-pentane	0.5	0.005														
13		Hexanes	1.8	0.018														
14		Heptanes	4.1	0.041		mosc [kg/s]	9.8											
15		Octanes	5.0	0.05		mgsc [kg/s]	=G4*1000*G											
16		Nonanes	3.8	0.038		mt [kg/s]	11.9											
17		Decanes	30.1	0.301														
18																		
19																		
20																		
21																		
22																		
23																		
24						TVD	p	T	Liquid Mass fraction	mo	mg	deno	deng	qo	qg	vso	vsg	dp/dx
25						[m]	[bara]	[C]	[-]	[kg/s]	[kg/s]	[kg/m^3]	[kg/m^3]	[m^3/s]	[m^3/s]	[m/s]	[m/s]	[bara/m]
26					1	2500	147	70										
27					2	1000												
28					3	500												
29					4	0												

Object: MSTR-000

Status: Calculated (01.01.0001 00:00:00)

Linked to:

Connections:

Upstream:

Downstream:

Input Data: Compounds | Phase Properties | Annotations

Flash Spec: Temperature and Pressure (TP)

Temperature: 70.000000 C

Pressure: 147.000000 bar

Mass Flow: 1.000000 kg/h

Molar Flow: 0.014025 kmol/h

Volumetric Flow: 0.001998 m<sup>3</sup>/h

Specific Enthalpy: -222.862762 kJ/kg

Specific Entropy: -0.524852 kJ/[kg.K]

Phase Mole Fraction: 0.000000

Phase: ☒ Vapor ☐ Liquid ☐ Solid

Composition:

Basis: Mole Fractions

Solvent:

Compound	Amount
Nitrogen	0.004004
Carbon dioxide	0.001001
Methane	0.432432
Ethane	0.047047
Propane	0.030030
Isobutane	0.015015
N-butane	0.009009

Information

Date	Type	Message
07.03.2017 14:58:59	Tip	To view must
07.03.2017 14:58:59	Tip	Use the cursor
07.03.2017 14:58:59	Tip	Press
07.03.2017 14:58:59	Tip	Hold

Attach Utility

- Phase Envelope
- Binary Envelope (VLE/VLLE/SLE)
- Ternary Envelope (LLE)
- Petroleum Properties
- Natural Gas Hydrates
- True Critical Point

Connections:

Upstream:

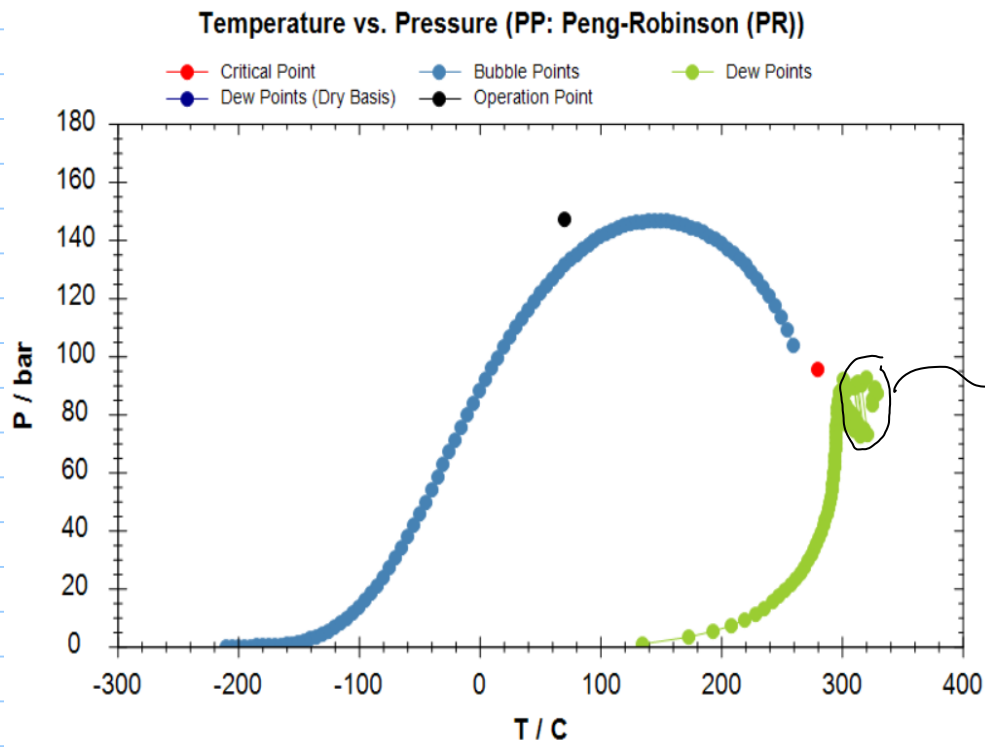
Downstream:

Input Data: Compounds | Phase Properties | Annotations

Mixture: Overall Liquid | Liquid 1

Property	Value	Units
Volumetric Flow Rate @ ...	0.001998	m <sup>3</sup> /h
Mass Flow Rate	1.000000	kg/h
Molar Flow Rate	0.014025	kmol/h
Phase Molar Fraction	1.000000	
Phase Mass Fraction	1.000000	
Compressibility Factor	0.000000	
Specific Enthalpy	-222.862762	kJ/kg
Molar Enthalpy	-15.890.055242	kJ/kmol
Specific Entropy	-0.524852	kJ/[kg.K]
Molar Entropy	-37.421787	kJ/[kmol.K]
Internal Energy	-26.356.625231	kJ/kg
Molar Internal Energy	-1.879.220.321...	kJ/kmol
Gibbs Free Energy	-42.759892	kJ/kg
Molar Gibbs Free Energy	-3.048.768867	kJ/kmol
Helmholtz Free Energy	-26.176.522361	kJ/kg
Molar Helmholtz Free Energy	-1.866.379.035...	kJ/kmol
Molecular Weight	71.299732	kg/kmol
Density	500.530625	kg/m <sup>3</sup>
Heat Capacity (Cp)	2.367538	kJ/[kg.K]
Heat Capacity Ratio (Cp/Cv)	1.170571	

100% liquid!



convergence  
error of the  
software  $\rightarrow$

[illegible]

Software suite from Petroleum Experts: UK, Edinburgh

IPM Integrated petroleum management

MBAL  $\rightarrow$  material balance

Prosper<sup>\*</sup>  $\rightarrow$  well modeling

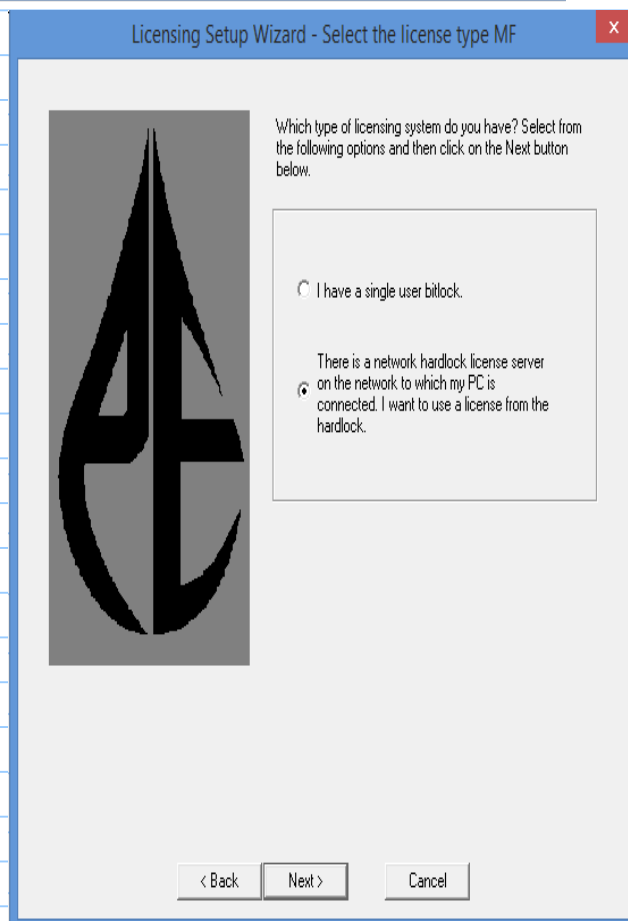
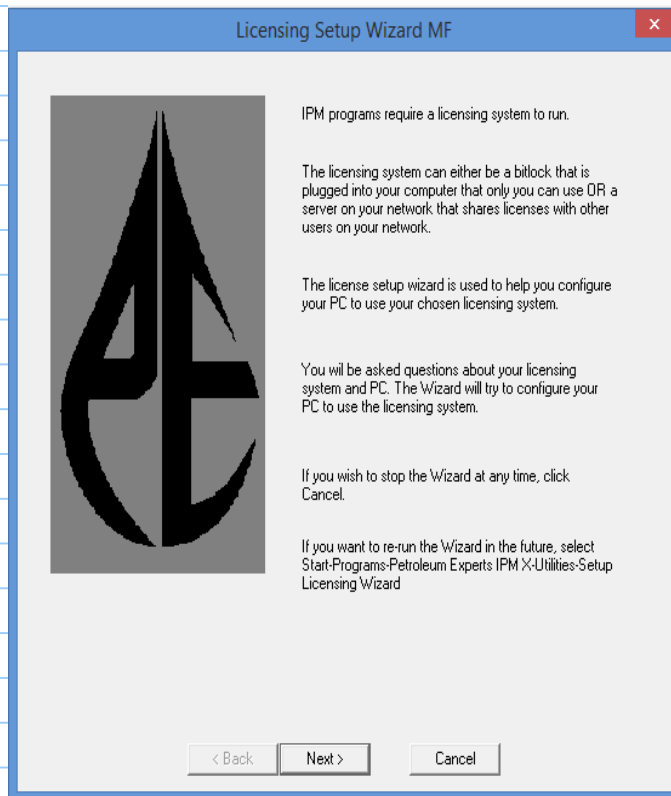
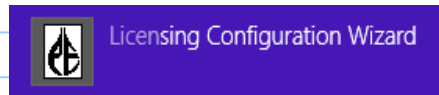
GAP<sup>\*</sup>  $\rightarrow$  networks and production systems (optimization)

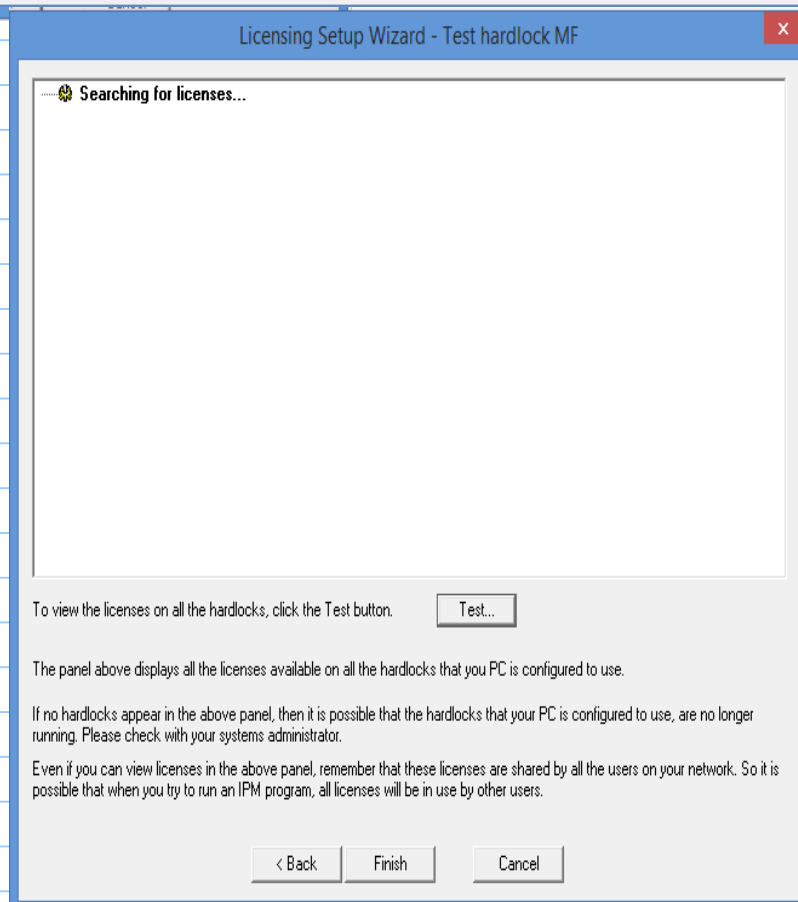
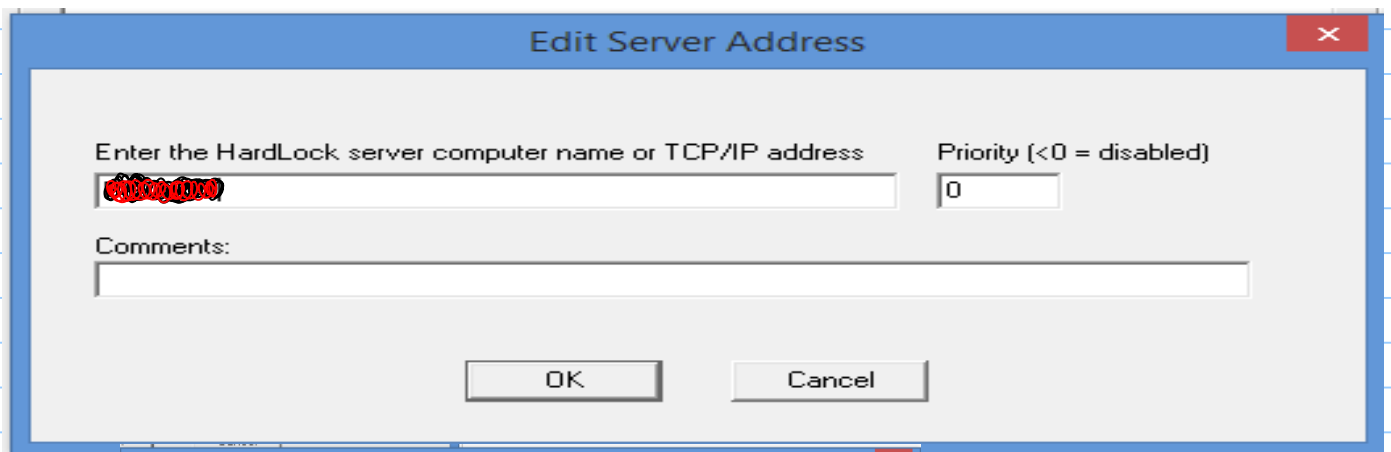
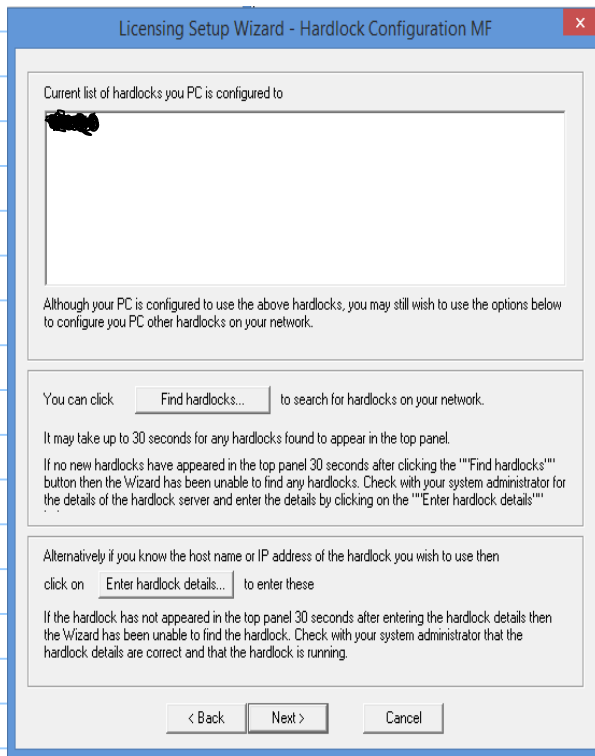
Reveal  $\rightarrow$  res. simulator

PVTP  $\rightarrow$  fluid analysis and modeling

Resolve  $\rightarrow$  coupling between reservoir + production system

IAM integrated asset modeling





**Exercise in Prosper and GAP, TPG4230, Milan Stanko, 20170309.****1. Subsea oil well modeling in Prosper****Fluid information:**

Use the black oil correlation of Glasø ( $p_b$ ,  $R_s$ ,  $B_o$ ) and Beal (viscosity) to model your PVT behavior.

Solution GOR = 142 Sm <sup>3</sup> /Sm <sup>3</sup>	Formation Water salinity = 23000 ppm
Producing GOR = 142 Sm <sup>3</sup> /Sm <sup>3</sup>	No H <sub>2</sub> S, CO <sub>2</sub> , N <sub>2</sub> .
Oil gravity = 30 API (876 Kg/m <sup>3</sup> )	Heat capacity of oil = 2.219 KJ/Kg/K
Gas gravity = 0.76	Heat capacity of gas = 2.1353 KJ/Kg/K
At initial conditions no water.	Heat capacity of water = 4.1868 KJ/Kg/K

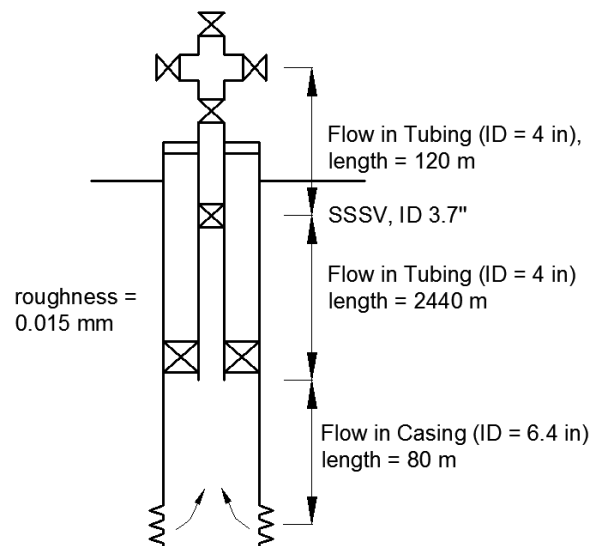
**Well layout:**

Deviation survey

MD [m]	TVD [m]
0	0
123	122
1059	1036
2164	2103
2640	2560

Geothermal gradient

MD [m]	T [C]
0	4
2640	100



**Overall heat transfer coefficient = 45 W/m<sup>2</sup> K**

**Reservoir info:**

Producing from a single layer  
 Reservoir pressure = 360 bara  
 Reservoir temperature = 100 C  
 Water cut = 0%



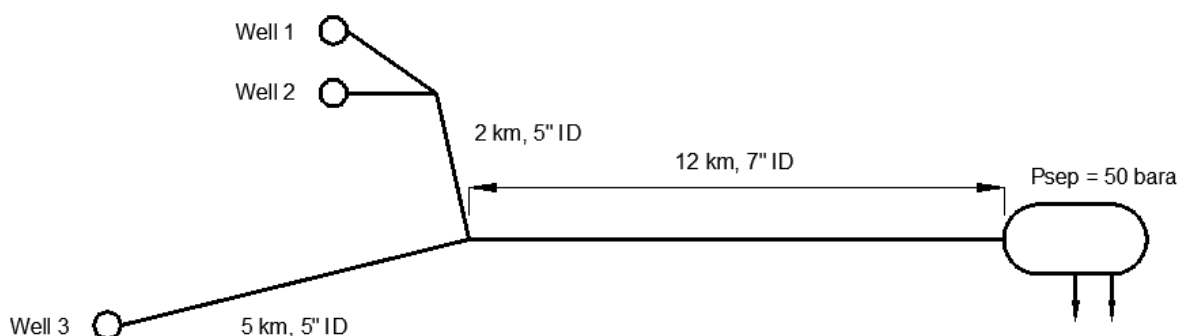
Productivity index =  $12 \text{ Sm}^3/\text{d}/\text{bara}$

### Tasks:

- Set up a prosper model of a subsea oil well.
- Report the bubble point pressure at reservoir temperature as predicted by the BO correlation.
- Estimate the producing rate using flow equilibrium assuming that the well is producing against a constant wellhead pressure of 100 bar. Is it correct to assume a linear productivity index?.
- Generate and export lift curves to be used in GAP (in the following exercise).  $p_{wh}$  range: 30-150 bara, GOR range: 141 – 500  $\text{Sm}^3/\text{Sm}^3$ . WC range: 0 – 50 %

### 2. Modeling of a subsea network with three oil wells in GAP

The layout of the production network layout is shown below. The S riser is not included in the figure. Assume that the water depth is 300 m, and the separator is 30 m above the sea level. The production riser is a lazy "S" riser with a total length of 700 m.



The wells have the same layout as the well created in the previous section, but with different GOR, WC and PI as specified in the table below:

Well	GOR [ $\text{Sm}^3/\text{Sm}^3$ ]	WC [%]	PI [ $\text{Sm}^3/\text{d}/\text{bara}$ ]
Well 1	142	0	12
Well 2	200	40	8
Well 3	250	20	15

### Tasks:

- Build the GAP model of three subsea wells producing to a FPSO.
- Calculate the natural equilibrium flow of the network. Report the flow potential of each well and calculate their split factor.
- Now, assume that the system has to be operated at a constant rate of  $2000 \text{ Sm}^3/\text{d}$ . Try the following methods:
  - Adding a constraint to the separator, add a choke pressure drop (controlled), and run an optimization.
  - Adding a constraint to the wells, and run an optimization

Exercise available here:

[http://folk.ntnu.no/stanko/Courses/TPG4230/2017/Class\\_files/20170309/Exercise\\_in\\_Prosper\\_and\\_GAP.pdf](http://folk.ntnu.no/stanko/Courses/TPG4230/2017/Class_files/20170309/Exercise_in_Prosper_and_GAP.pdf)

via Norwegian STI → PROSPER main interface

**Options Summary** (Box 1): general options

**PVT DATA** (Box 2): put model and calculations

**IPR DATA** (Box 3): IPR setup and model

**EQUIPMENT DATA** (Box 4): well components and architecture

**ANALYSIS SUMMARY** (Box 5): vlp exported for GAP

**Prosper (32bit) 13.0**  
IPM V9.0 - Build # 120 - Jul 4 2014

Petroleum Experts Limited  
Petex House  
10 Logie Mill  
Edinburgh, EH7 4HG  
United Kingdom  
Tel: +44 131 474 7030  
Fax: +44 131 474 7031  
Email: edinburgh@petex.com  
Web site: www.petex.com

C:\HD\NTNU\SEMESTER\Semester\_V\_2015\TPG4230\Notes\20150324\Prosper  
License Number : 04471  
File Format Version : 816  
Current File Version : Original=816 Current=816  
Memory - Load 44% Physical (4095/2047Mb) Virtual (4095/1781Mb)  
Windows (6.2) Build 9200 - 32-bit  
C:\Program Files (x86)\Petroleum Experts\IPM 9\prosper.exe  
\*\*\* Educational License - No Commercial Use Permitted \*\*\*

Prosper file structure

Oil Well	Anl	541 608 24.03.2015 09:38 -a-
Oil Well	Out	619 439 24.03.2015 09:38 -a-
Oil Well	Pvt	55 729 24.03.2015 09:38 -a-
Oil Well	Sin	179 870 24.03.2015 09:38 -a-
Oil Well	Tpd	9 973 24.03.2015 09:37 -a-
Oil Well	Op	93 183 24.03.2015 09:37 -a-

main prosper file

related with box 2

vlp exported for GAP

related with box 5

Double click to access each box:

- Remember to save your file.
- The first box has to be completed to input in the other boxes

System Summary (Oil\_Well.Out)

Done Cancel Report Export Help Datestamp

Fluid Description: Fluid: oil and water, Method: Black Oil

Separator: Single-Stage Separator

PVT Warnings: Disable Warning

Water Viscosity: Use Default Correlation

Water Vapour: No Calculations

Well: Flow Type: Tubing Flow, Well Type: Producer

Artificial Lift: Method: None

User Information: Company, Field, Location, Well, Platform, Analyst, Date: 24. mars 2015

Calculation Type: Predict: Pressure and Temperature (offshore), Model: Rough Approximation, Range: Full System

Well Completion: Type: Cased Hole, Sand Control: None

Reservoir: Inflow Type: Single Branch

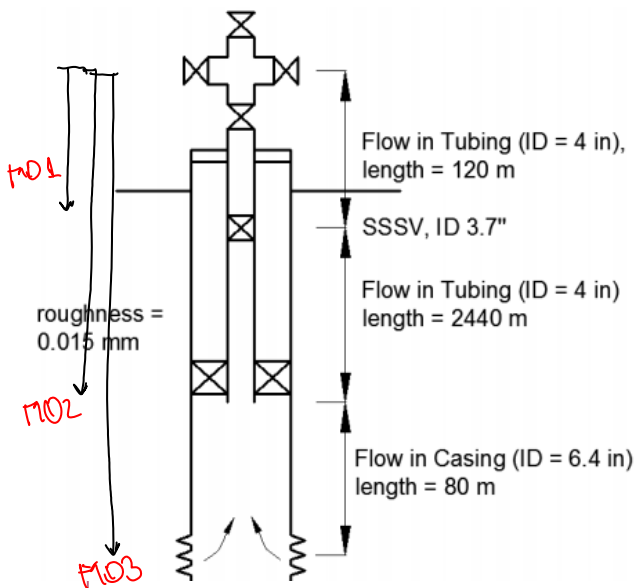
Comments (Ctrl-Enter for new line)

In proper the convention to input

downhole equipment is:

locate yourself at the wellhead (x-mas tree) and list, from top down, how many different sections do you observe: flow in tubing, flow in SSSV, flow in tubing and flow in casing.

- Introduce each one on the table. the measured depth is the depth of the end of the section measured from the wellhead.

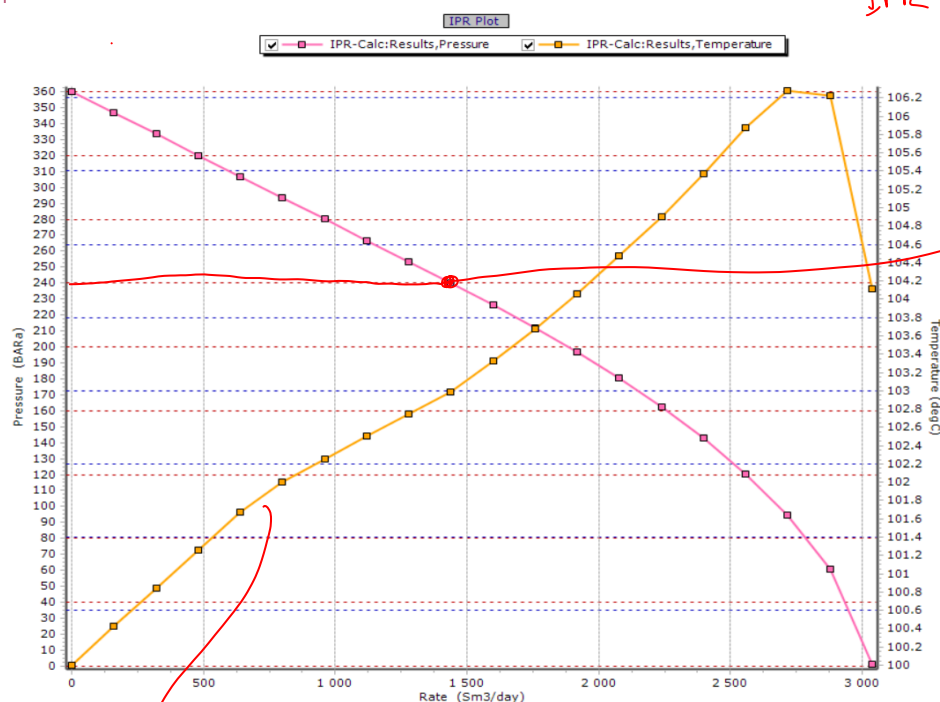


DOWNHOLE EQUIPMENT (Oil\_Well.Sin)

Point	Label	Type	Measured Depth (m)	Tubing Inside Diameter (m)	Tubing Inside Roughness (m)	Tubing Outside Diameter (m)	Tubing Outside Roughness (m)	Casing Inside Diameter (m)	Casing Inside Roughness (m)	Rate Multiplier
1		Xmas Tree	0							
2		Tubing	120	0.1	1.524e-5					1
3		SSSV		0.09						1
4		Tubing	2560	0.1	1.524e-5					1
5		Casing	2640					0.16	1.524e-5	1
6										
7										
8										
9										
10										
11										
12										
13										
14										
15										
16										
17										
18										

MD1  
MD1  
(we assume that the SSSV has no length)

MD2  
MD3



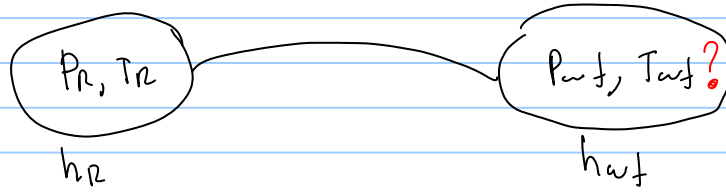
IPR Before leaving the IPR module remember to click "calculate". In that way the IPR is available for further calculations.

$P_b @ P_r$

below this part the curve will deviate from the straight line.

here, PROSPER assumes that  $P_r \neq P_{wf}$ . this is because the fluid experiences an expansion process from  $P_r \rightarrow P_{wf}$ .

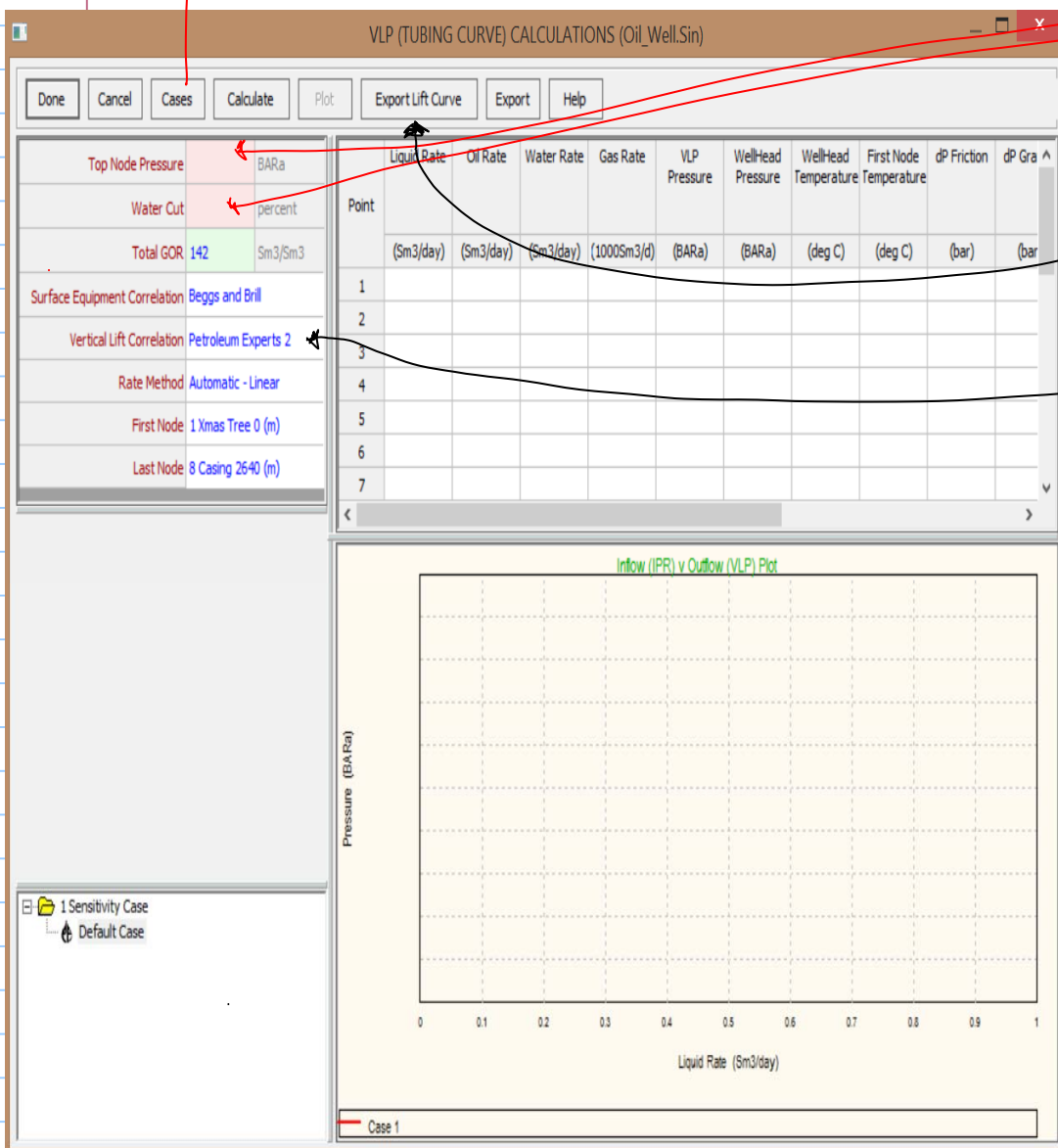
This expansion process is often modeled as isenthalpic, meaning  $h_g = h_{wf}$



with half and Perf it is possible to calculate Tuf.

VLP

→ in "cases", the expected variations of GOR, WC, Pwh are input. To be able to access it, make sure that you filled these two boxes:



to export the curves  
use:

→ multiphase "expert"

### 2.8.1.3.1 VLP Correlation Applications

**Fancher Brown** is a no-slip hold-up correlation that is provided for use as a quality control. It gives the lowest possible value of VLP since it neglects gas/liquid slip it should always predict a pressure, which is less than the measured value. Even if it gives a good match to the measured down hole pressures, Fancher Brown should not be used for quantitative work. Measured data falling to the left of Fancher Brown on the correlation comparison plot indicates a problem with fluid density (i.e. PVT) or field pressure data. **This is thus essentially, a correlation for quality control purposes.**

For oil wells, **Hagedorn Brown** performs well for slug flow at moderate to high production rates but well loading is poorly predicted. Hagedorn Brown should not be used for condensates and whenever mist flow is the main flow regime. Hagedorn Brown under predicts VLP at low rates and should not be used for predicting minimum stable rates.

**Duns and Ros Modified** The Duns and Ros Modified correlation is derived from the Duns and Ros Original correlation. The original correlation was modified by Petroleum Experts to overestimate the pressure drop in oil wells for the slug flow regime. This correlation should not be used for calculating the pressure drop in the wellbore or pipelines and hence should not be used for lift curve generation either. **This correlation should only be used for quality checking of the input well test data.**

**Duns and Ros Original** The Duns and Ros Original Correlation is derived from the original published method. In **PROSPER** the original Duns and Ros correlation has been enhanced and optimised for use with condensates. This correlation performs well in mist flow cases and may be used in high GOR oil wells and condensate wells.

**Petroleum Experts** correlation combines the best features of existing correlations. It uses the Gould et al flow map and the Hagedorn Brown correlation in slug flow, and Duns and Ros for mist flow. In the transition regime, a combination of slug and mist results is used.

**Petroleum Experts 2** includes the features of the PE correlation plus original work on predicting low-rate VLPs and well stability.

**Petroleum Experts 3** includes the features of the PE2 correlation plus original work for viscous, volatile and foamy oils.

**Petroleum Experts 4** is an advanced mechanistic model for any angled wells (including downhill flow) suitable for any fluid (including Retrograde Condensate).

**Petroleum Experts 5.** The PE5 mechanistic model is an advancement on the PE4 mechanistic model. PE4 showed some instabilities (just like other mechanistic models) that limited its use across the board. PE5 reduces the instabilities through a calculation that does not use flow regime maps as a starting point. PE5 is capable of modelling any fluid type over any well or pipe trajectory. This correlation accounts for fluid density changes for incline and decline trajectories. The stability of the well can also be verified with the use of PE5 when calculating the gradient traverse, allowing for liquid loading, slug frequency, etc. to be modelled.

**Petroleum Experts 6** includes the features of the PE3 correlation plus original work on the affects that water cut can have on a viscous oil.

**Orkiszewski** correlation often gives a good match to measured data. However, its formulation includes a discontinuity in its calculation method. The discontinuity can cause instability during the pressure matching process; therefore its use is not encouraged.

**Beggs and Brill** is primarily a pipeline correlation. It generally over-predicts pressure drops in vertical and deviated wells.

**Gray** correlation gives good results in gas wells for condensate ratios up to around 50 bbl/MMscf and high produced water ratios. Gray contains its own internal PVT model which over-rides **PROSPER**'s normal PVT calculations.

**Hydro 3P (internal)** is a mechanistic model and considers three phase flow.

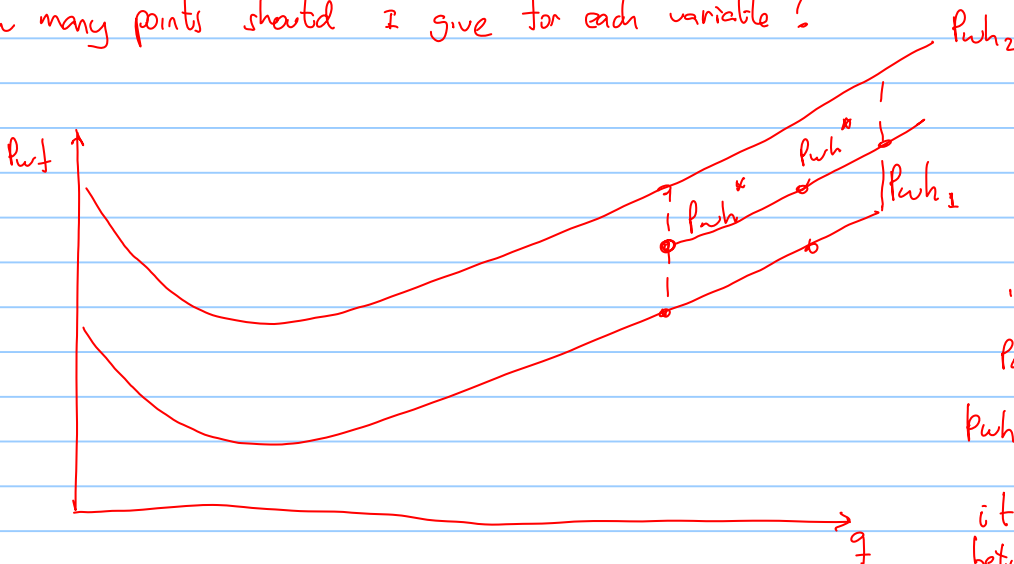


There is no universal rule for selecting the best flow correlation for a given application. It is recommended that the Correlation Comparison always be carried out. By inspecting the predicted flow regimes and pressure results, the User can select the correlation that best models the physical situation.

Further details can be found in the **PROSPER** Appendix B | Multiphase Flow Correlations.



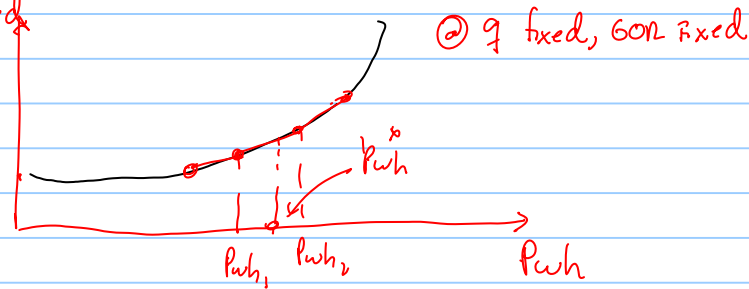
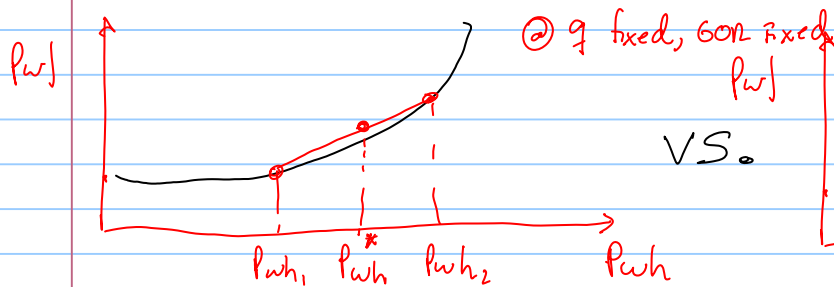
how many points should I give for each variable?



if I need  $P_{wf}$  for  $P_{wh}^*$  between  $P_{wh1} \leq P_{wh} \leq P_{wh2}$

it will interpolate between the two curves above

if  $P_{wh1}$  is relatively close to  $P_{wh2}$  the interpolation error will be small.



Prosper manual available here :

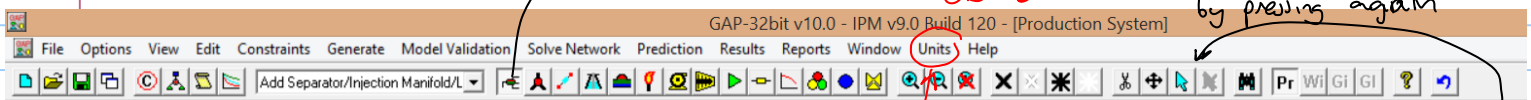
[C:\Program Files \(x86\)\Petroleum Experts\IPM 9\pdf\prosper](C:\Program Files (x86)\Petroleum Experts\IPM 9\pdf\prosper)

GAP network.

make the network layout

click on the element and click again in the canvas where you want to place it.

OBS! remember to unselect it by pressing again



! change units to Norwegian SI

the button or pressing here otherwise you might add the same component again by mistake



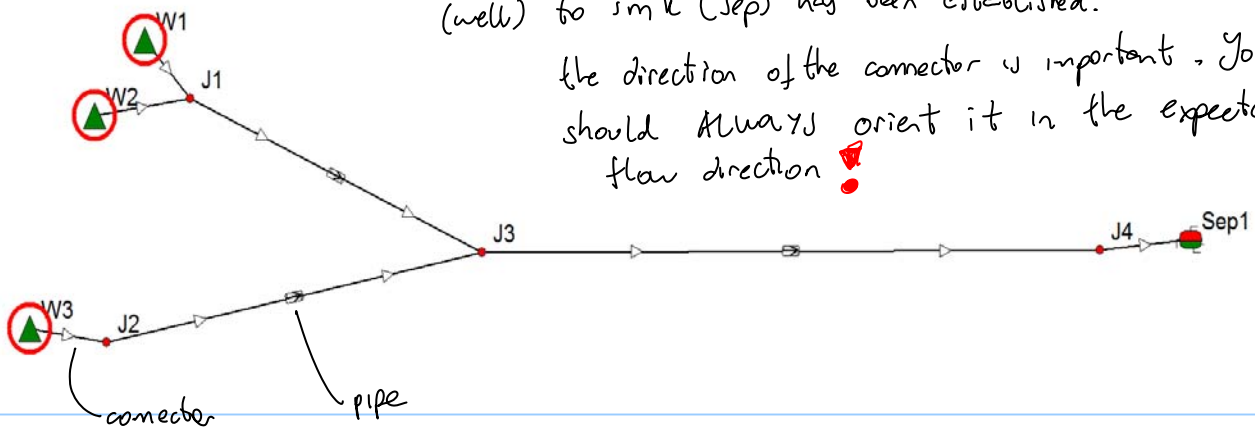
• pipe can only exist between two joints

• a connector between an element or a joint just means that the  $P_{wh}$  of  $W3$  is equal to  $P_{J2}$ , have the same water and conditions



the colors become bright when a full flow path from source (well) to sink (sep) has been established.

the direction of the connector is important. You should ALWAYS orient it in the expected flow direction!



Double click on the wells and link all of them to the proper file we just created

Well 'W1' - Summary

Label	Name	Mask
W1		Included in system

Comments

Well Type: Oil Producer (No lift) | Model: VLP / IPR intersection | Rate Model: Use volumes | ☐ Tight Oil

PROSPER File: C:\Users\Milan\Desktop\Oil\_Well.Out | Valid | Browse

Data Summary (click item to activate)

Tank Conns	OK	Controls	Not Set
IPR	Invalid	Downtime	None
VLP	Invalid	Coning	None
Constraints	None	Schedule	None

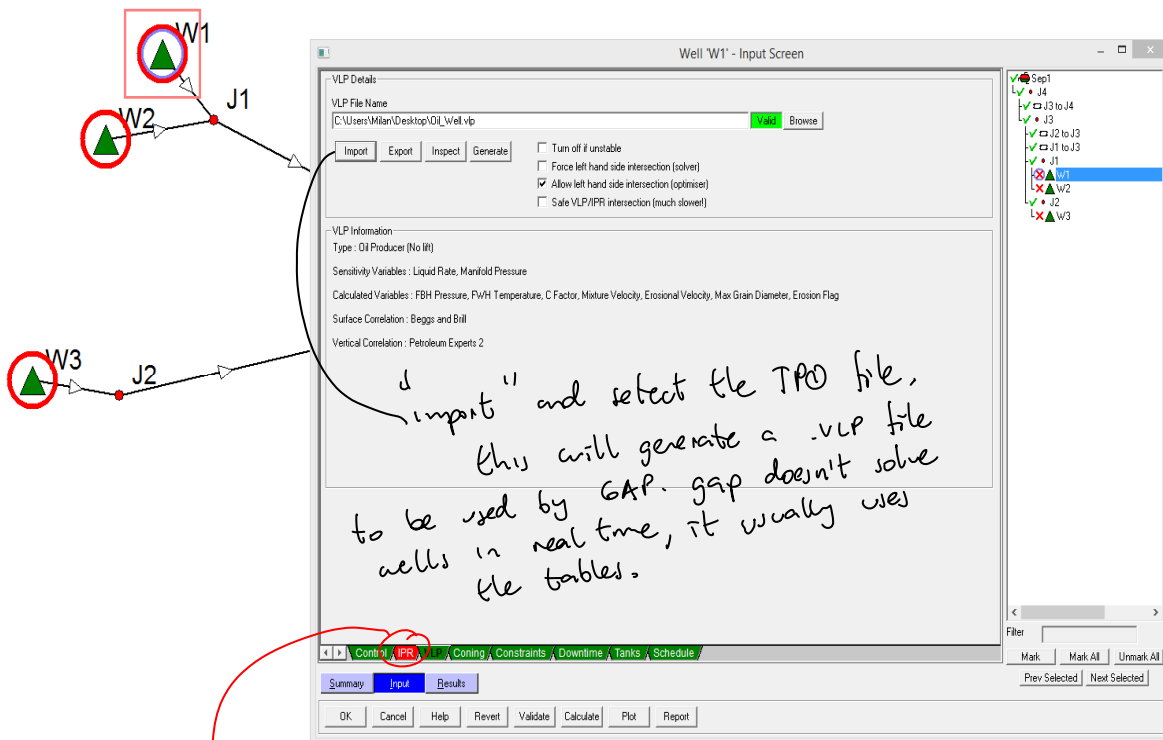
Summary | Input | Results

OK | Cancel | Help | Revert | Validate | Calculate | Plot | Report

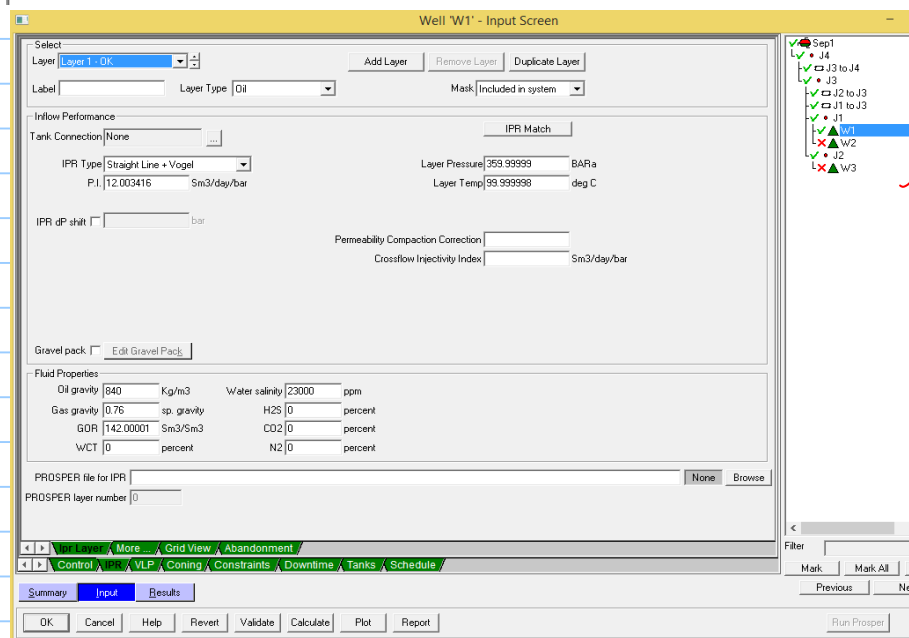
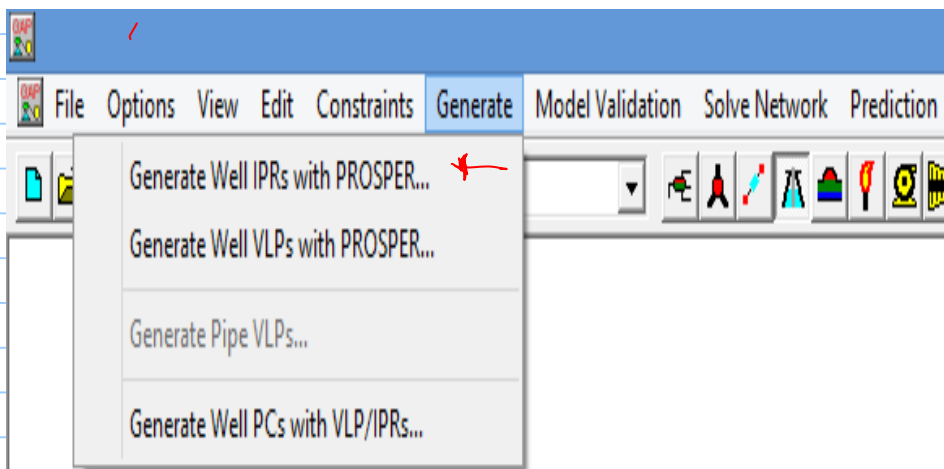
click here to assign the VLP.

we will assume that all wells have the same layout architecture.





IPR hasn't been defined. To transfer it from prosper to GAP go to "Generate IPR"



the IPR is transferred and then can be modified as defined in GAP

**Creating MBAL file, TPG4230, Milan Stanko, 20170314.****Fluid information:**

Use the black oil correlation of Glasø ( $p_b$ ,  $R_s$ ,  $B_o$ ) and Beal (viscosity) to model your PVT behavior.

Solution GOR = 142 Sm <sup>3</sup> /Sm <sup>3</sup> Producing GOR = 142 Sm <sup>3</sup> /Sm <sup>3</sup> Oil gravity = 30 API (876 Kg/m <sup>3</sup> ) Gas gravity = 0.76 At initial conditions no water.	Formation Water salinity = 23000 ppm No H <sub>2</sub> S, CO <sub>2</sub> , N <sub>2</sub> .
---	---

**Temperature:** 100 C

**Initial pressure:** 360 bara

**Porosity:** 0.3

**Connate water saturation:** 0.15

**Original oil in place:** 60 MSm<sup>3</sup>

**Start of production:** 01.04.2017

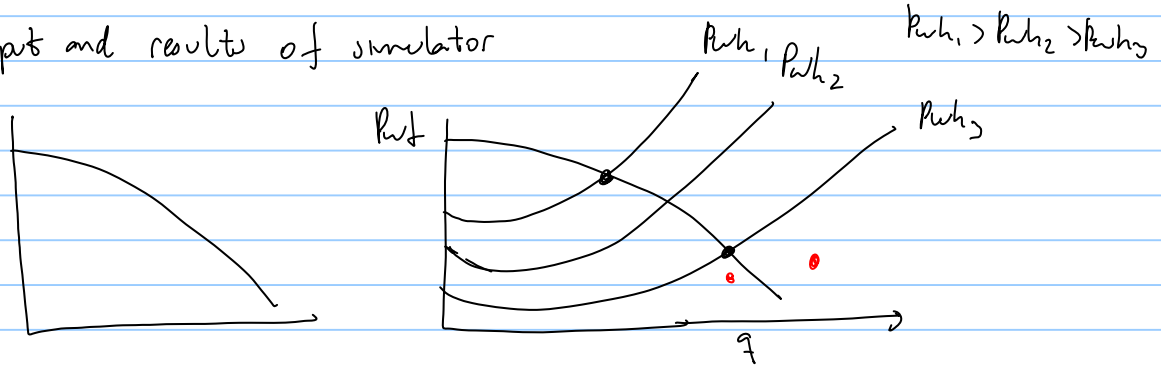
**Water influx:** Small Pot aquifer, 180 MSm<sup>3</sup>

**Rel Perm:** Corey Functions

	Residual Saturation	End Point	Exponent
	fraction	fraction	
K <sub>rw</sub>	0.15	1	1
K <sub>ro</sub>	0.15	0.8	1
K <sub>rg</sub>	0.01	0.9	1

## Some comments about the usage of commercial simulators:

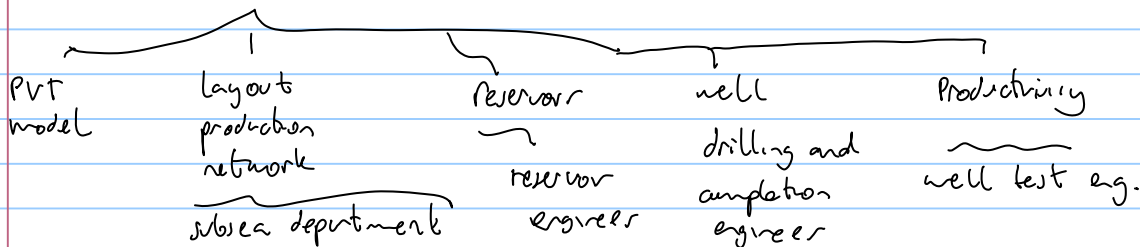
- QC input and results of simulator



- Garbage in → Garbage out.  
information.

USE THE MANUAL!!

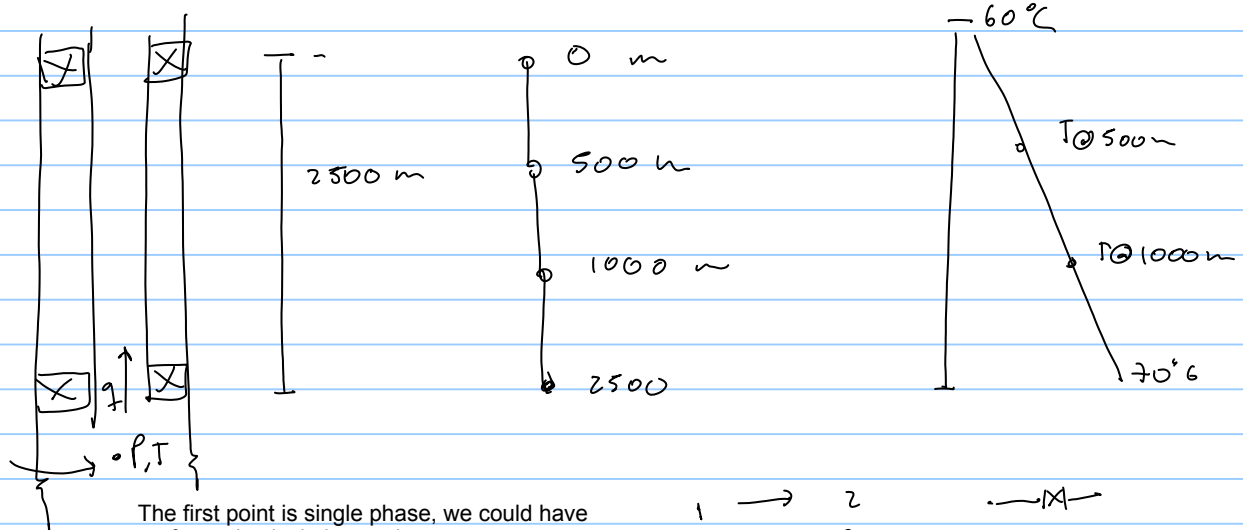
Information comes from many different sources



Extremely important for IAM integrated asset modeling.

- Have up-to-date information
- QC information

- (class exercise about pressure drop calculations in conduits with multiphase flow



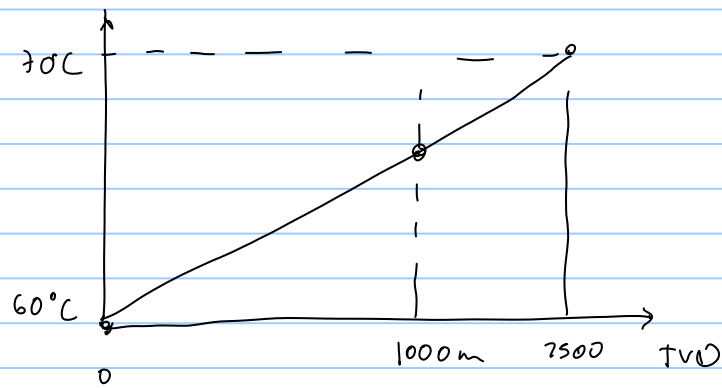
The first point is single phase, we could have performed calculations using:

$$h_1 = h_2$$

$$\frac{P_1}{\rho_1 g} + z_1 + \frac{V_1^2}{2g} = \frac{P_2}{\rho_2 g} + z_2 + \frac{V_2^2}{2g} + h_f$$

Bernoulli conservation equation for incompressible fluid

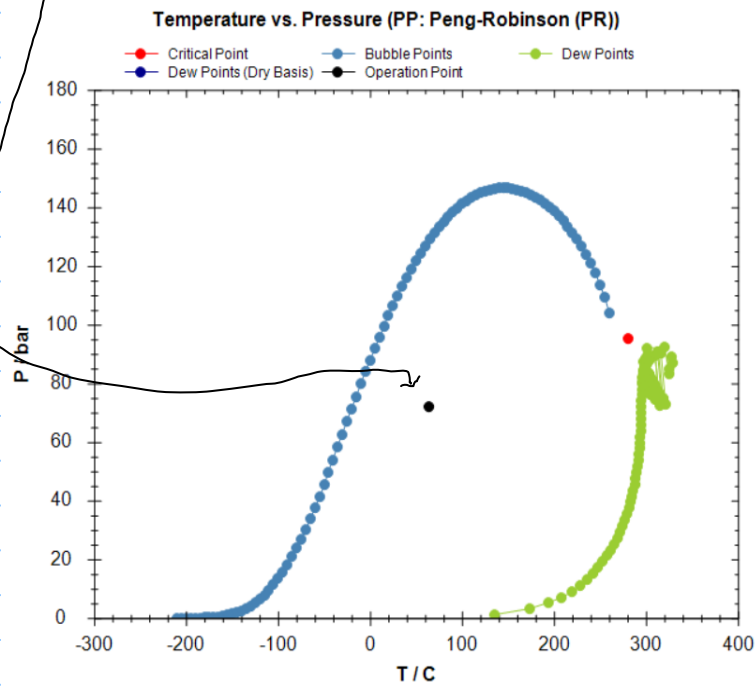
$$h_f = f \frac{L}{D} \frac{V^2}{2g} \quad h_{ac} = K \frac{V^2}{2g}$$



$$\left( \frac{70 - 60}{2500 - 0} \right) = \left( \frac{70 - T}{2500 - 1000} \right)$$

$$\begin{aligned} &T \\ &1500 \quad f = 1600 \text{ kg/m}^3 \\ &1500 \cdot 1000 \cdot \frac{9.81}{10} \\ &\left\{ \begin{array}{l} 150 \text{ kg/m}^3 \\ 150 - 200 \\ 150 \end{array} \right\} \\ &\frac{150}{5} \\ &30 \text{ bar} \end{aligned}$$

	TVD	p	T	Liquid Mass fraction	m <sub>o</sub>	m <sub>g</sub>	deno	deng	q <sub>o</sub>	q <sub>g</sub>	v <sub>so</sub>	v <sub>sg</sub>	dp/dx
	[m]	[bara]	[C]	[-]	[kg/s]	[kg/s]	[kg/m <sup>3</sup> ]	[kg/m <sup>3</sup> ]	[m <sup>3</sup> /s]	[m <sup>3</sup> /s]	[m/s]	[m/s]	[bara/m]
1	2500	147	70	1	11.9	0.0	500.5	-	0.024	0.000	2.11	0.00	0.050285
2	1000	72	64	0.933	11.1	0.8	578.4	52.9	0.019	0.015	1.70	1.34	0.032234
3	500	55											
4	0												



## Chapter 8: Flow assurance management in production systems

Flow assurance consists in ensuring uninterrupted flow of hydrocarbon streams from the reservoir to the point of sale according to production plan. Flow assurance is particularly relevant for deep subsea systems with relatively long transportation distances (5-150 km) and low surrounding temperatures. In this type of systems if there is a problem intervention and remediation has to be done remotely and it is usually time consuming and very expensive.

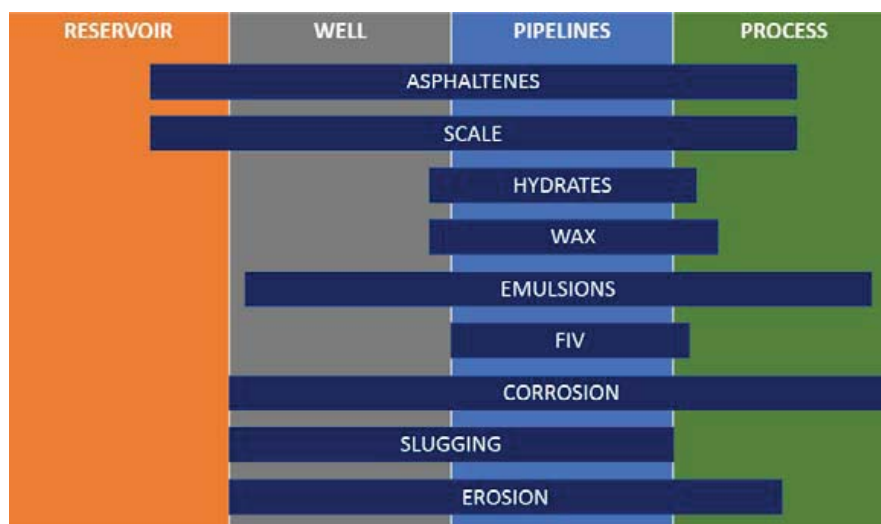
Flow assurance focuses on three main aspects:

1. Avoid flow restrictions (excessive pressure drop, blockage or intermittent production).
2. Safeguard the structural integrity of parts of the production system from damages caused by internal flow.
3. Maintain the functionality and operability of components in the production system.

There are multiple issues that are typically addressed in flow assurance:

- Formation and deposition of wax.
- Formation of hydrates.
- Formation and accumulation of scale
- Flow induced vibrations (FIV)
- Asphaltene formation and deposition
- Slugging
- Erosion
- Emulsion
- Corrosion
- Pressure surges during shutdown and startup.

Fig. 1 shows where these issues usually occur in the production system.



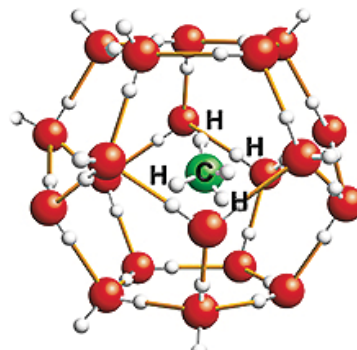
**Fig. 1. Flow assurance problems and their typical location in the production system**

### HYDRATES

Hydrates are solid substances where water molecules (in liquid phase) form a cage-like structure that hosts small ( $< 9 \text{ \AA}$  diameter) molecules (Fig. 2). The small molecules are usually methane, ethane, propane, butane, carbon dioxide, nitrogen. The cage-type structure is formed due to hydrogen bonding of water molecules (the water molecule tends to spatially create two positives and a negative pole).



(a)



(b)

**Fig. 2. A) appearance of a hydrate plug, b) molecular structure of a methane hydrate**

Hydrates contains a much higher proportion of water than the hydrocarbon component. For example a methane hydrate (called methane clathrate) with molecular formula  $4\text{CH}_4 \cdot 23\text{H}_2\text{O}$  (MW = 478) has a molar proportion of 85% (23/27) water and 15% (4/27) methane.

However, this doesn't necessarily indicate that they contain small amounts of gas. For example one cubic meter of methane clathrate (of an approximate density of  $900 \text{ kg/m}^3$ ) contains 1.88 ( $900/478$ ) kmols of hydrate, of which there are 7.53 ( $1.88 \cdot 4$ ) kmols of methane. 7.53 kmols of methane at standard conditions correspond to 178.4

$Sm^3!$  ( $V_{SC} = n_{moles} \cdot R \cdot T_{SC} / p_{SC}$ ). For a cubic meter to contain the same amount of gaseous methane at standard temperature, it would have to be compressed at 180.4 bara ( $p = 7.53 \text{ kmol} \cdot R \cdot T_{SC} / 1 \text{ m}^3$ ).

Hydrates form only if **ALL** following ingredients are present:

- Free water (in liquid phase)
- Small hydrocarbon molecules
- Particular range of pressure and temperature.

An example of the hydrate formation region is shown in Fig. 3. The actual line depends mainly on the fluid composition, but, as a rule of thumb, it happens at high pressure and low temperatures. For example at a pressure of 12 bar, the hydrate formation temperature is 4 C.

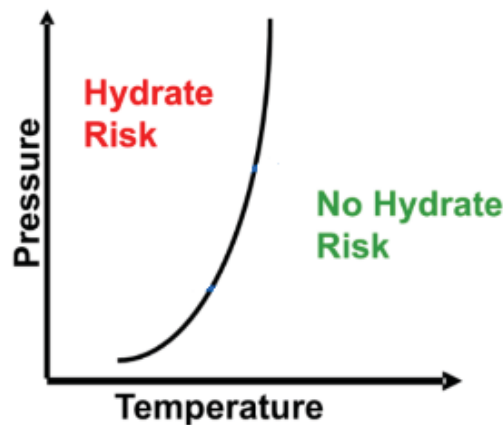


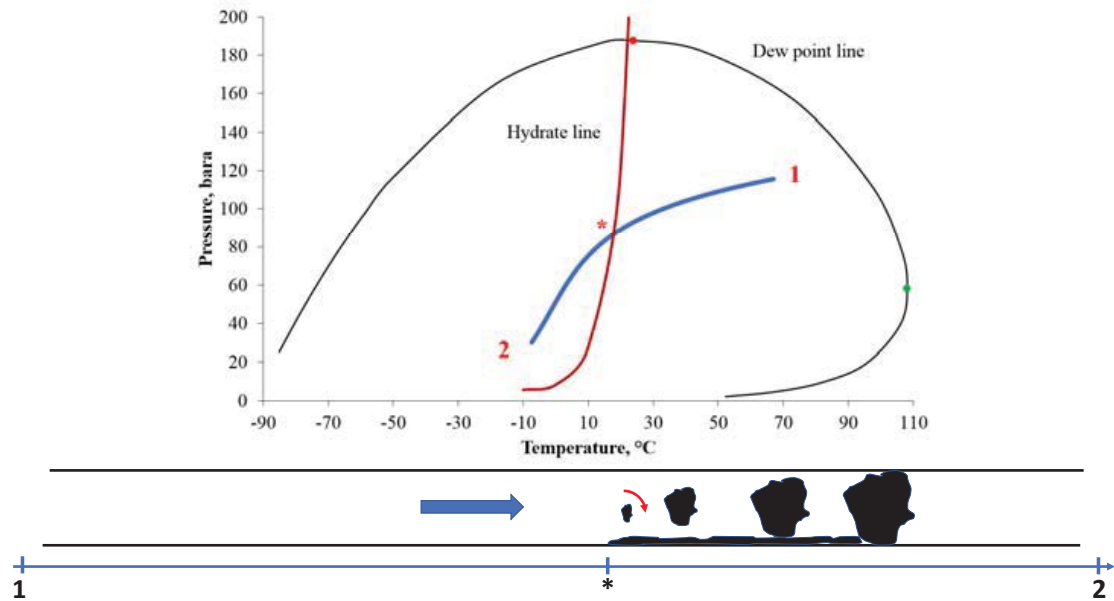
Fig. 3. Hydrate formation region

The hydrate formation line can be predicted by empirical expressions (that are a function of the specific gravity of the gas), or using equilibrium calculations with an Equation of State. Hydrate equilibrium calculations resemble to Vapor Liquid equilibria by finding  $p$  and temperature conditions that make equal the chemical energy of the component in the hydrate phase and liquid and gas phases.

### Consequences of hydrates for flow assurance

If the pressure and temperature of the fluid flowing along the production system falls inside the hydrate formation region, hydrates will start to form. Hydrates usually form at the liquid-gas interphase where free water and small hydrocarbon molecules are in contact. The mixing and turbulence of the flow further increases the contact between the two thus causing the formation of more hydrates. Hydrates then start to agglomerate until they eventually plug the pipe (Fig. 4).





**Fig. 4. Evolution of p and T of the fluid when flowing along the production system**

Hydrates can also form when the production is stopped and the stagnant fluid begins to cool by transferring heat with the environment.

### Management

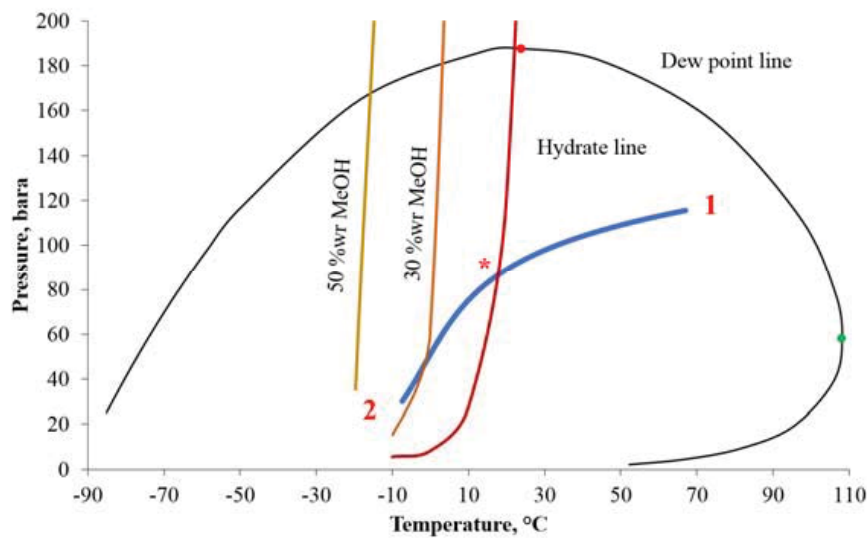
The traditional strategy to manage hydrates is to avoid their formation. There are two main techniques commonly used to prevent the formation of hydrates:

- **Keep the fluid conditions out of the hydrate formation region.** This is done mainly by reducing the rate of temperature drop of the fluid (reducing the lateral spread of the blue line in Fig. 4). This is achieved in practice by two methods: better insulation or electrical heating of the pipe.

Please note that insulation works effectively for a flowing system, but when production is stopped, usually some other control method must be used as the fluid will eventually cool down during a long period.

Electrical heating is usually not cost effective for long transportation distances.

- **Reduce the hydrate formation region.** The equilibrium pressure and temperature of hydrate formation can be affected by adding liquid inhibitors (typically Mono-ethylene-glycol MEG, Tri-ethylene-glycol TEG or methanol MEOH) to the water phase. Inhibitors interfere with the formation of hydrogen bonds by keeping water molecules apart. As a consequence, the hydrate formation line will be shifted to the left (as shown in Fig. 5).



**Fig. 5. Effect of inhibitor injection on the hydrate line**

Typical concentrations of inhibitors used are 30-60 in weight %. For example the Snøhvit field has a Water Gas ratio of  $6 \text{ E-6 Sm}^3/\text{Sm}^3$ . The plateau production of the field is  $20 \text{ MSm}^3/\text{d}$ , thus it produces around  $120 \text{ Sm}^3/\text{d}$  of water, or, equivalently,  $120\,000 \text{ kg/d}$  of water. If we assume that the inhibitor concentration used is 50 in weight %, then this gives  $120\,000 \text{ kg/d}$  of MEG that must be continuously injected on the field. MEG is usually reclaimed in the processing facilities. Otherwise, it will represent a daily cost of  $60\,000 - 180\,000 \text{ USD}$  (assuming a MEG cost between  $0.5 - 1.5 \text{ USD/kg}$ ).

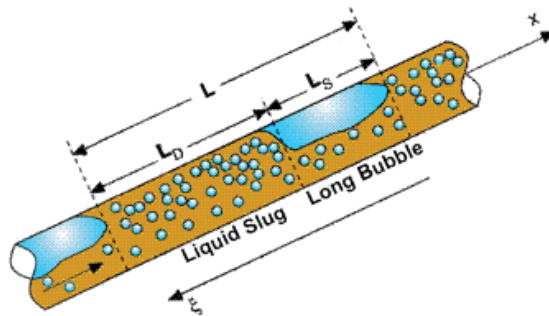
Please note that the inhibitor must be present in the water phase for it to be effective, thus evaporation to the gas phase has to be taken into account when estimating the required amounts of inhibitor.

Inhibitors are also injected when preparing to shut down production, to make sure hydrates will not form due to the cooling of the fluid.

During the last years, many experts have proposed to use a less conservative hydrate control strategy where we allow hydrates to form, but impede their agglomeration and carry the slurry together with the production fluids. This can be performed by injecting special types of chemicals, or by using cold flow. However, up to date there are limited field cases where this type of management is performed.

## SLUGGING

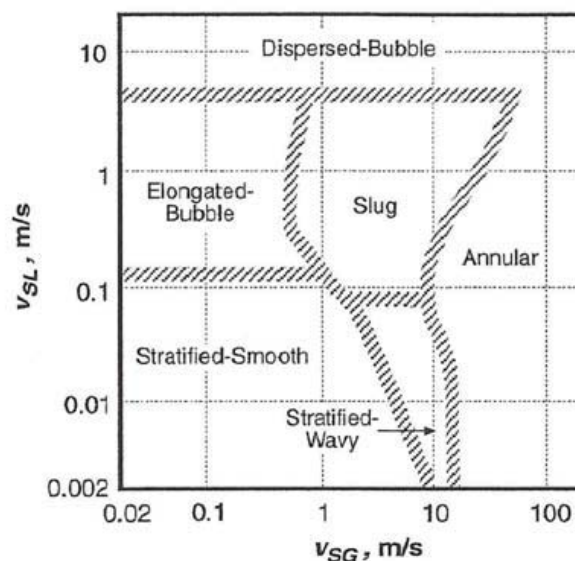
Slugging consists on intermittent flow of gas and liquid in the production system (Fig. 6).



**Fig. 6. Slug in a pipe section**

There are two main types of slugging:

- Hydrodynamic slugging: It occurs spontaneously at a particular combination of flow velocities of liquid and gas and it depends strongly on the fluid properties and pipe inclination. As an example, Fig. 7 shows the flow pattern map for a horizontal pipe and certain fluid properties. There is a particular combination of operational velocities where the flow will arrange itself in a slug flow configuration.



**Fig. 7. Flow pattern map for an horizontal pipe (After Mandhane et al. 1974)**

- Terrain slugging: Terrain slugging is mainly due to cyclic accumulation of liquid in the production system (especially in lower points). This happens in undulating well trajectories, transportation flowlines with varying topology of the seabed and in risers.

An example of slugging in a s-shaped production riser is shown in Fig. 8. Liquid accumulates in the lowest pipe section and blocks the flow of gas (a). The liquid level

starts increasing and the gas pressure in the horizontal line also increases (b). Eventually, the liquid floods the second floor of the riser (c). Gas pressure increases until it is sufficient to flush out almost all the liquid in the riser (d).



**Fig. 8. Stages of severe slugging in an S-shaped riser.**

### Consequences of slugging

The main consequence of slugging is that production rates and pressures will fluctuate in time which is often detrimental to the proper operation of the downstream processing facilities. In gravity separators for example, a sudden inlet of liquid might increase significantly the liquid level, causing liquid carryover, activating the warnings for high liquid level and even triggering a shutdown alarm.

Slugging also causes vibration in flowlines, manifolds, risers which can develop in structural damages due to elevated stress levels and fatigue.

### Management

Slugging can be, to some extent, predicted during the design phase of the field using commercial multiphase flow simulators such as Leda, Olga and FlowManager. If it is detected and it has high severity (long slug lengths, frequencies that coincide with the natural frequency of the structure, relevant pressure fluctuations), potential solutions are to change the routing of the flowline, refill or dig some sections of the seabed that can cause liquid accumulation or changing the pipe diameter. Smaller pipe diameters increase the gas velocity, increasing the drag of the gas on the liquid thus reducing the liquid deposition. However, too small pipe diameters also cause higher pressure drops that reduce overall production rates.

If slugging is occurring in an existing production system, some approaches that have been used successfully in the past are to apply gas lift in the riser base or to use the topside choke to change dynamically the backpressure on the line and “control” the slug.

### SCALING

Scaling is the precipitation of minerals compounds (constituted by Na, K, Mg, Ca, Ba, Sr, Fe, Cl) **from the produced water** and their deposition on pipe walls. Scale occurs when the solubility of the minerals in the water decreases due to changes in pressure and temperature, due to mixing of waters of different sources, injection of CO<sub>2</sub>. Minerals

usually deposit on surface areas that are rough or have irregularities (e.g. valve components).



**Fig. 9. Scale accumulation in a a) pipe, b) choke**

There are two main types of scales that usually occur in production systems:

- **Carbonate scales.** These scales are formed when  $\text{CO}_2$  dissolved in the water disassociates in carbonate ions  $\text{CO}_3^{-2}$  and join with some of the aforementioned minerals (typically calcite  $\text{CaCO}_3$ , Iron carbonate  $\text{FeCO}_3$ ). Their precipitation is mainly due to reduction in pressure (due to flow in restrictions, valves, chokes) or increases in temperature. This type of scale can be removed with acid.
- **Sulphate scales:** These scales are formed by the sulphate ion  $\text{SO}_4^{-2}$  that is present in seawater (Barite  $\text{BaSO}_4$ , Gypsum  $\text{CaSO}_4 \cdot 2\text{H}_2\text{O}$ , Anhydrite  $\text{CaSO}_4$ , Celestite  $\text{SrSO}_4$ ). It precipitates out of solution when waters from different sources are mixed (e.g. seawater used for injection and production water from the aquifer or formation). The pressure has little influence in the precipitation, but the increase in temperature can reduce further the solubility. This type of scale **must be** removed mechanically.

### Consequences

Scaling causes gradual blockage of the flow path and loss of functionality in production equipment (Subsurface safety valves, chokes).

### Management

Studies are usually performed on the produced water to determine if it will be prone to form scale at the pressure and temperature conditions encountered in the production system. Moreover, special attention must be paid to situations where there is mixing of water from different sources,  $\text{CO}_2$  injection.

Scaling is usually avoided by using chemicals (scale inhibitors) that attach themselves to the scale ions and impede growth. Coating can help to prevent deposition on the surfaces but when damaged (e.g. due to erosion) their effectivity is reduced dramatically.

If scale forms in a component of the production system, the removal technique depends on the type of scale. Carbonates can be removed by acid injection and sulphates can only be removed mechanically.

### **EROSION**

Erosion is the gradual damage and loss of material from the wall of components of the production system (valves, pipes, bends, etc. Fig. 10) due to the repeated impingement of solid particles (sand) or droplets at high velocity.



**Fig. 10. Erosion damage in a cage-type choke.**

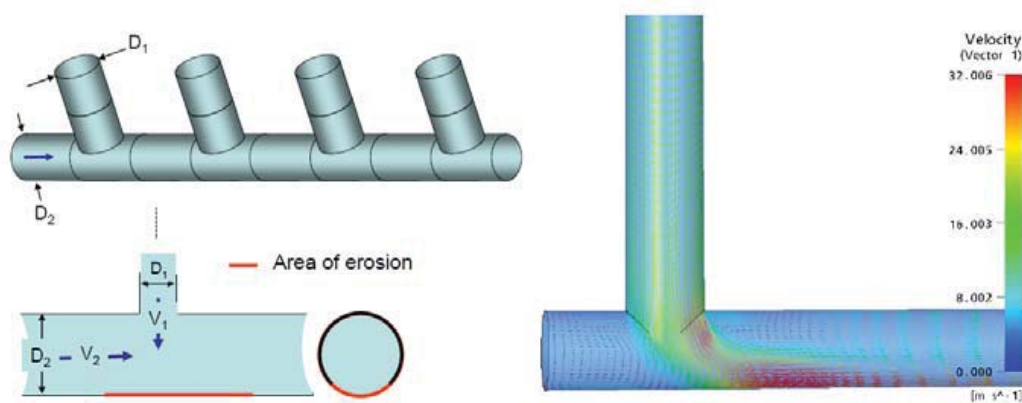
### **Consequences**

Structural damage, vibration, leaks and corrosion (due to the removal of the protective coating).

### **Management**

Erosion is usually accounted for in the field design phase. The design process sizes the equipment such that the velocities are below certain limit value that gives an acceptable erosional rate. These calculations usually consider the velocity of impingement, the angle of impingement, the amount of solid particles and the wear resistance of the material.

There are some standards that give guidelines how to estimate erosive wear for common pipe components (e.g. DNV Recommended Practice RP O501). However, complex geometries usually require in-depth studies (e.g. using computational fluid dynamics, CFD) to estimate erosion prone areas, fluid velocities, angle of impingement, etc. An example is shown in Fig. 11.

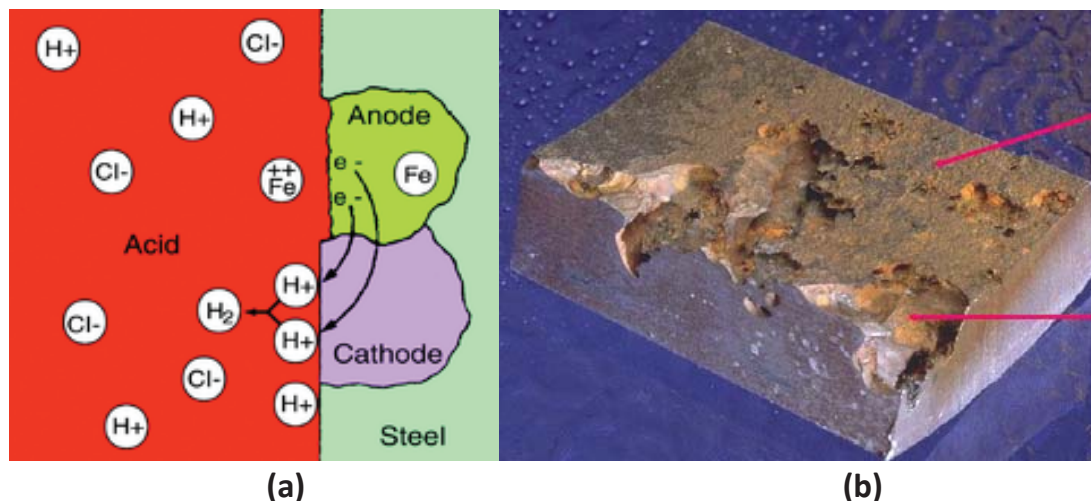


**Fig. 11. CFD simulation of erosion in a production header**

If erosion is detected in an existing production system then, when possible, components might be reevaluated and replaced with geometries that are less susceptible to erosion. Alternatively, if corrosion is due to excessive sand production from the reservoir, the only alternative is then reduce the well rate to limit sand production.

## CORROSION

Corrosion is an electrochemical reaction where steel is converted to rust and occurs when metal is in contact with water. Two locations are established in the metal, a cathode and an anode. In the anode, iron loses electrons and becomes a positively charged ion. This ion further reacts with water and oxygen in the surrounding media to form rust. The cathode receives the electrons of the anode and generates by-products (such as hydrogen  $H_2$ ) with other ions.

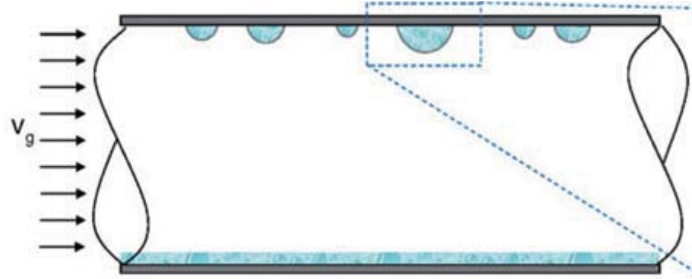


**Fig. 12. a) Illustration of a corrosion reaction b) corrosion on the tubing surface**

Corrosion can occur virtually anywhere in the production system where water is in contact with metal (casing, tubing, flowlines, pipelines, tanks, pumps, etc.). In



transportation pipes, corrosion usually occurs at the pipe bottom where water is transported, in low pipe sections where water accumulates or at the top of the pipe due to splashing and condensation of water droplets (also known as TLC, Top of line corrosion).



**Fig. 13. Wet gas flow in a horizontal flowline depicting top of line condensation**

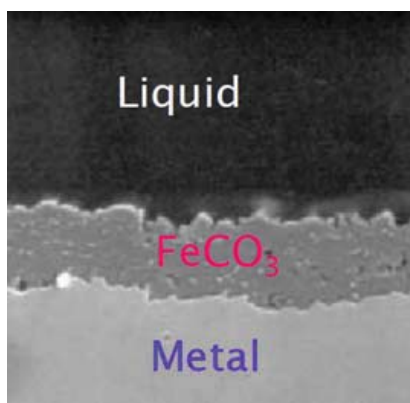
### Consequences

Corrosion on an unprotected pipe can cause losses of 1-20 mm of pipe thickness per year, leading ultimately to structural damage and leakages. Rust particles can also travel downstream and cause problems such as plugging other components.

### Management

The measures to mitigate corrosion can be divided into two main principles:

- Eliminate the contact between water from steel. This can be done by applying a protective layer on the steel surface, for example with coating (which might be eventually damaged due to sand erosion), creating a layer of protective oxide on the steel (Fig. 14 a) or by using inhibitors (Fig. 14 b).



**(a)**



**(b)**

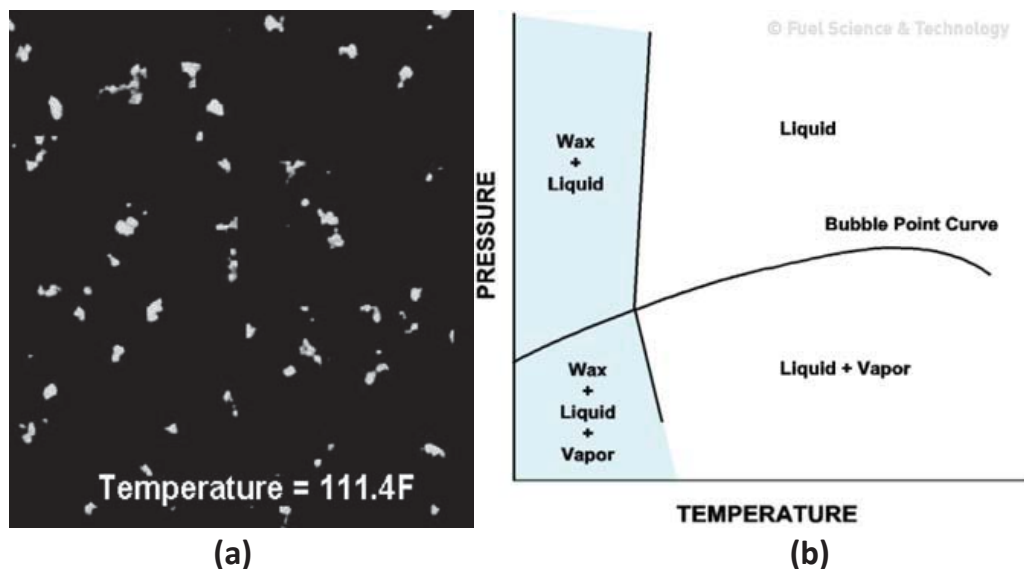
**Fig. 14. Protective layer of FeCO<sub>3</sub> formed on the metal surface b) inhibitors attached to the metal surface**

- Use steel materials with higher resistance to corrosion. For example alloy steels. This is usually feasible for wells, but it becomes too expensive for flowlines and pipelines.

## WAX DEPOSITION

Wax deposition occurs when long alkane chains (C18+) precipitate out of solution from the oil, agglomerate and deposit on the pipe walls.

In a waxy crude, when temperature is reduced down to a certain value (for North sea crudes this happens around 30-40 C), some wax crystals will start to precipitate and become visible. The temperature when this occurs is called cloud point or WAT (wax appearance temperature).



**Fig. 15. a) Wax crystals visible in a crude at WAT, b) WATs at different pressures in the phase diagram**

The WAT depends on oil composition, type and molar amounts of alkanes, pressure, cooling rate. Wax crystals typically attach to nucleating agents present in the oil (asphaltenes<sup>6</sup>, fine sand, clay, water, salt), form wax “clusters” and grow.

If the temperature is reduced further down to the pour point, the oil becomes solid-like and stops flowing.

<sup>6</sup> Asphaltenes are coal-like solids that also have the tendency to precipitate out of the crude. They are high molecular weight compounds containing poly-aromatic carbon rings with nitrogen, sulphur, oxygen and heavy metals such as vanadium and nickel.



**Fig. 16. Crude oil not flowing once the pour point is reached**

Wax deposition occurs when **ALL** the following ingredients are present:

- Wax-prone components in the oil composition (long alkane chains).
- Temperature below WAT.
- Pipe wall colder than the fluid such that there is a temperature profile in the fluid reducing towards the pipe wall (temperature gradient).
- Irregularities on the wall where wax clusters attach.

Wax deposits age with time and become more rigid (thus more difficult to remove).

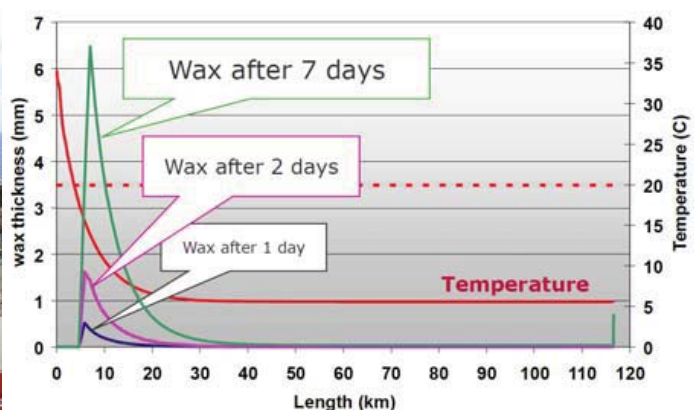
### Consequences

In flowlines and pipelines:

- Increases pressure drop due to the increase in pipe roughness.
- Reduction of cross section area.
- Pipe blockage.



(a)



(b)

**Fig. 17. a) wax plug retrieved topside (Statfjord B), b) evolution of the wax thickness in a pipeline with time.**

- The presence of wax crystals in the fluids changes its rheology (e.g. making it non Newtonian or with a higher effective viscosity).
- During shut-downs, the temperature of the fluid can reach the pour point of the crude, causing it not to flow (gelling).

## Management

The first step in developing a wax management strategy is to test the crude oil in the laboratory and measure and quantify all of its properties relevant for deposition.

A common management method for wax is to perform frequent pigging. Pigging consists in sending a device (pig) inside the pipe that scraps the wax deposits and pushes them forward. Pigs are usually sent and received from the processing facilities thus two pipelines must be installed. There are also subsea pig launchers, but this is economic only for systems with very low pigging frequency.

Pigging frequency is usually estimated by performing numerical simulations to compute the profile of deposited wax along the flowline with time. With this, the total amount of wax deposited in the system at any given time is estimated. There is a maximum length and weight of wax that can be pushed through the pipe, given by the maximum allowable pressure that the pipe can tolerate. The required pigging frequency is given by the time at which that wax amount is reached.

Other techniques used are keeping the fluid outside of the wax formation region. This is done by thermal insulation or electrical heating. However, for long flowlines, electrical heating is usually very expensive and insulation alone is not enough to keep temperature high. Thus in most cases insulation or electrical heating are often used to reduce wax deposition rates together with pigging.

Chemical inhibitors that are also often injected. Chemical inhibitors work by reducing the cloud point of the crude or by preventing further agglomeration of wax crystals. As with insulation, in many systems this doesn't eliminate completely the problem but it helps slowing down the deposition rate. Please note that chemical inhibitors are expensive.

If the seabed temperature is below or equal the pour point of the oil, then it is necessary to inject chemical inhibitors before shutting down the system to avoid gelling.

In recent years pipe coating has been proposed as a technique to avoid wax attaching to pipe walls. However it is not yet field tested.

In systems with wax-prone oils the pressure drop between end points of flowlines should be closely monitored. Any unexplained increase might indicate wax deposition and must be immediately addressed.

## OIL-WATER EMULSIONS

Oil-water emulsions are fine and stable dispersions of oil droplets in water or water droplets in oil (Fig. 18). The formation of emulsions depends on a variety of factors such as the dynamics of multiphase flow, the properties of oil and water such as viscosity and interfacial tension, the shear stress (mixing) experienced by the mixture, chemical compounds present in the oil-water interface. In production systems, the mixing is typically generated when commingling production from different sources, due to the violent expansion across the choke, flow through multiphase pumps, etc.

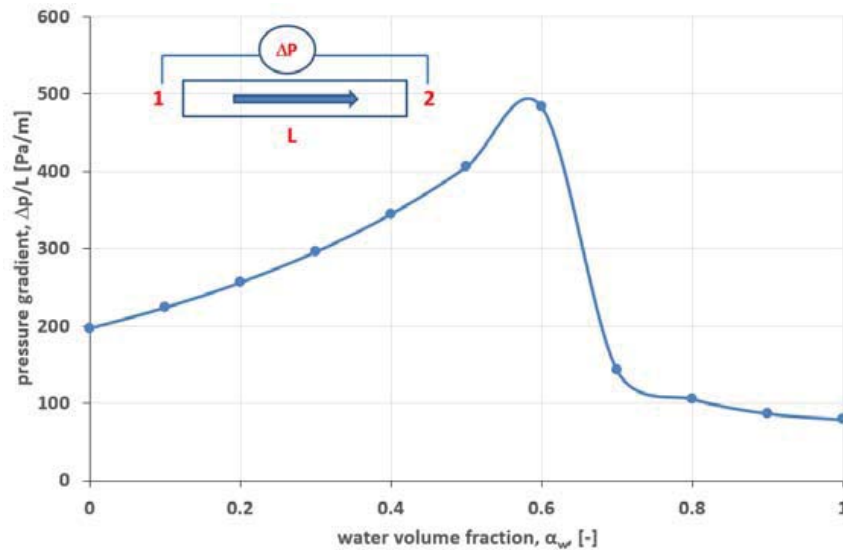


**Fig. 18. a) oil (red) and water (White) originally separated, b) oil and water emulsion after vigorous stirring in a blender**

## Consequences

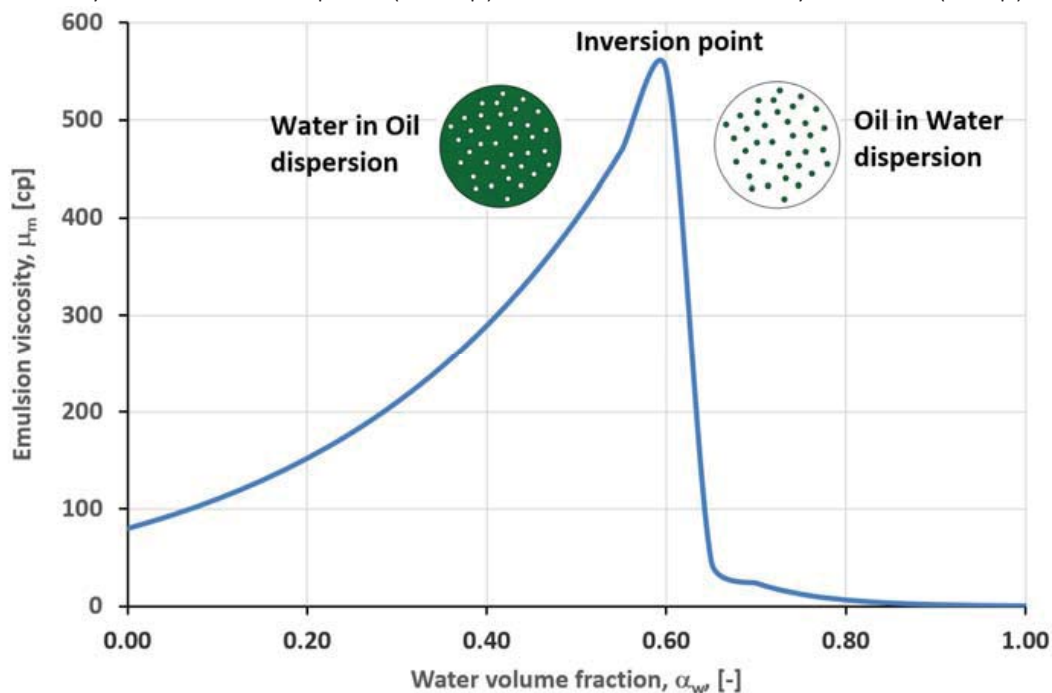
In pipe flow, emulsions often exhibit the behavior presented in Fig. 19. For a fixed volumetric rate of the mixture ( $q_o + q_w$ ), if one measures the pressure drop along a pipe segment for several water volume fractions, it will increase with water volume fraction until a maximum is reached and then it will decline abruptly. The water volume fraction that has the highest pressure gradient is called the inversion point. Please note that the increase in pressure drop is significant (more 2.5 times the one for pure oil in the figure).

When increasing the water fraction, at the inversion point the dispersion changes from an oil in water dispersion to a water in oil dispersion.



**Fig. 19. Measured pressure drop in a horizontal pipe keeping the total flow rate constant and changing water volume fraction,  $q_w/(q_w+q_o)$**

Using an homogeneous model (single fluid with average properties) one can back-calculate the effective mixture or “emulsion” viscosity that the mixture should have to provide the pressure drop measured (Fig. 20). For the particular case, the emulsion viscosity at the inversion point (570 cp) is 7.1 times the viscosity of the oil (80 cp).



**Fig. 20. Mixture viscosity behavior versus water volume fraction exhibited by the oil water mixture**

There are many expressions used to represent the behavior shown in Fig. 20 that are later used in emulsion pressure drop models. Most of them require data measured in the lab to tune their coefficients. As an example, the Richarson model is shown below.

For oil continuous

$$\mu_m = \mu_o \cdot e^{n_o \cdot \alpha_w}$$

For water continuous

$$\mu_m = \mu_w \cdot e^{n_w \cdot (1 - \alpha_w)}$$

Eq. 1.

### Consequences

Emulsions can cause excessive pressure drops in pipe segments and components, which can reduce dramatically production rates, pumping capacity of electric submersible pumps, etc. Moreover, stable emulsions are difficult to separate in processing facilities thus creating bottlenecks and fluid disposal problems.

### Management

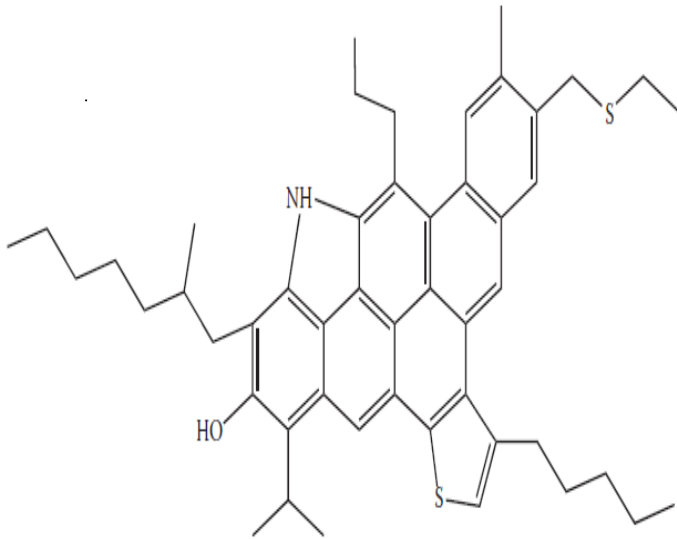
During the field design phase, the capacity oil and water system to form emulsions can be somewhat studied with laboratory tests (shaking bottle tests). However, these results have sometimes limited applicability partly because the shear magnitudes (mixing) applied in the laboratory conditions are very different from the mixing experienced in the field.

When there is mixing of streams with different water cut, the inversion point must be avoided.

Often, chemical substances such as demulsifiers and light oils (diluent) are injected into the stream to reduce the stability of the emulsion. Light oils reduce the viscosity of the formation oil, thus helping separation. Demulsifiers are chemicals that attach themselves to the interface between oil and water promoting separation.

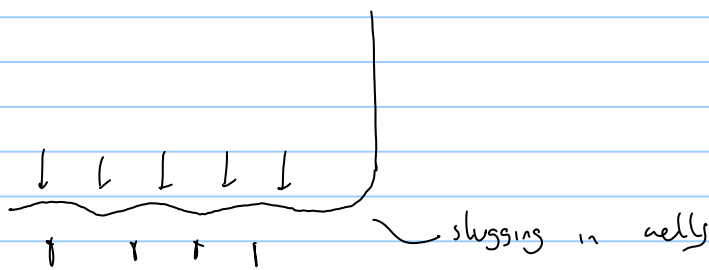
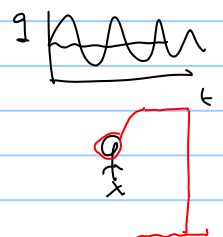
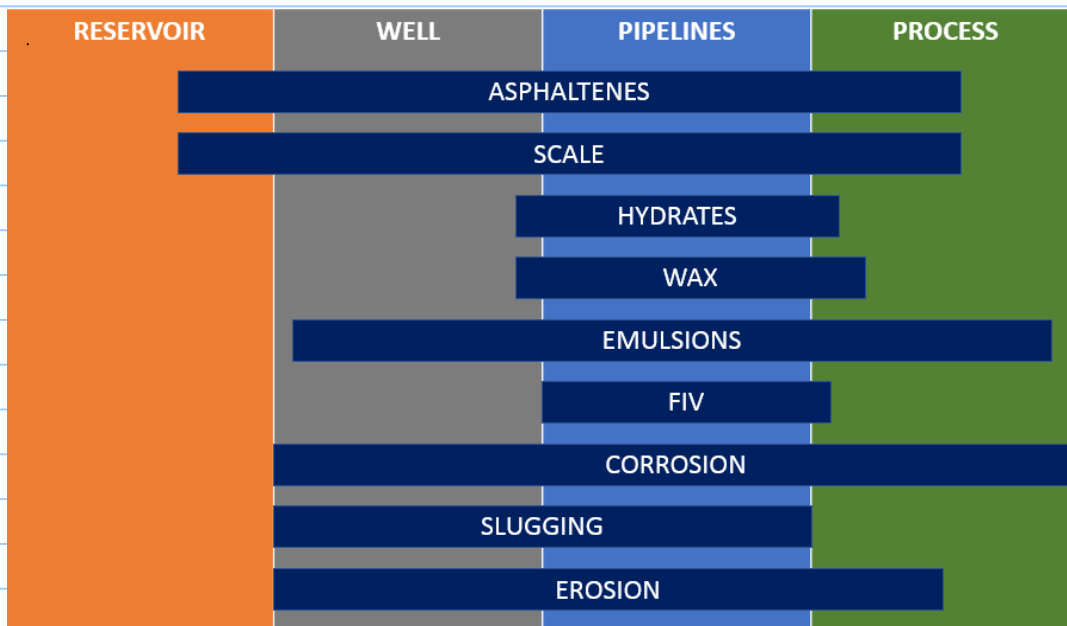
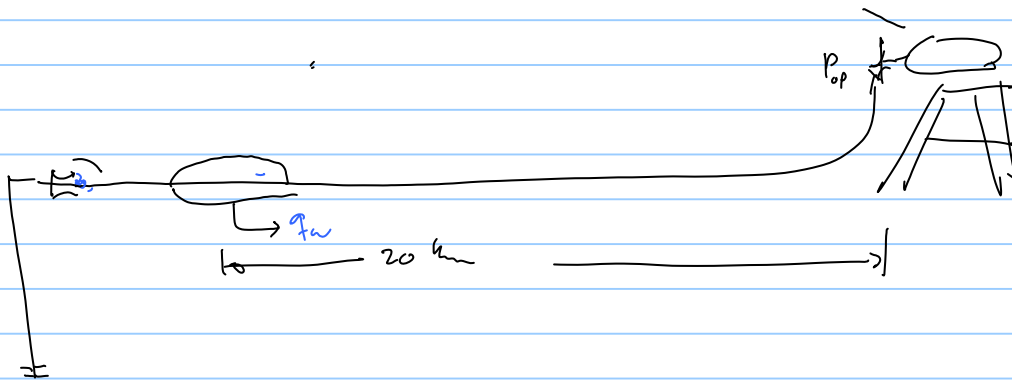


asphaltene molecule



emulsion

$$p_{mix} = p_w d_w + (1 - d_w) p_o$$

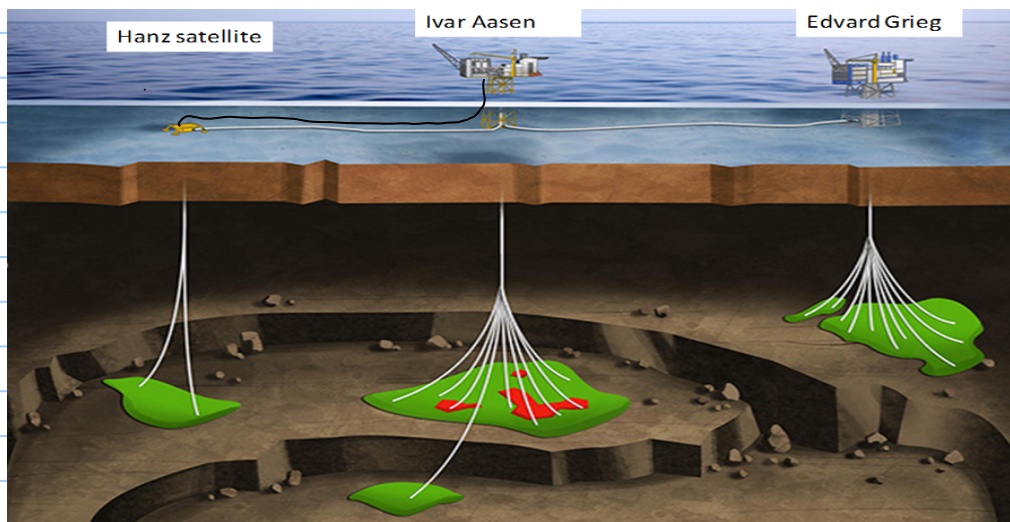


- Others issues to consider are
  - bacteria (biocide)
    - against  $O_2$ ,  $H_2S$  (scavengers for  $O_2$   $H_2S$  sequestration) corrosion
  - anti foamers liquid + gas
  - DRA ~ Drag reducing agent  $\rightarrow$  reduce  $\Delta p$  in pipe

Production chemicals  $\rightarrow$  cost  
 $\rightarrow$  compatibility  
 $\rightarrow$  environmental impact

EOR processes  $\sim$  polymers  
 $\sim$  nanoparticles

$\rightarrow$  many of production chemicals will end up in liquid phase  $\rightarrow$  oil  
 better for environ  
 band for water recovery  
 $\rightarrow$  injection  
 $\rightarrow$  disposal to sea  
 under allowable concentration



Ivar Aasen Consequence study

Tabell 5-2. Foreløpig oversikt over kjemikalietyper

Type kjemikalie	Konsentrasjon (ppm vol.)	Tilsettes i	Frekvens
Avleiringshemmer A	50	Produsert vann	Kontinuerlig
Avleiringshemmer B	20-50	Sjøvann	Kontinuerlig
Korrosjonshemmer	50	Produsert vann	Kontinuerlig
Emulsjonsbryter	50	Total væske 1)	Kontinuerlig ved behov
Skumdemper	5	Total væske	Periodisk
Flokkulant	10	Produsert vann	Kontinuerlig
Vokshemmer	150	Total væske 1)	Periodisk
Biocid	80	Total væske 1)	Kontinuerlig
Oksygenfjerner	5	Sjøvann	Kontinuerlig
H <sub>2</sub> S fjerner	150	Produsert vann	Kontinuerlig ved behov
MEG	Batch	Brønnstrøm	Ved behov

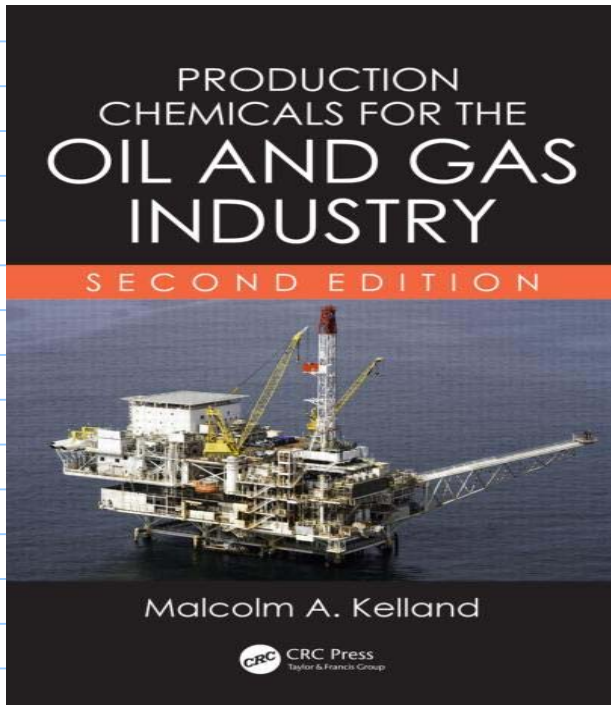
1) Olje og produsert vann.

hemmer : inhibitor

- continuous
  - periodic
  - as required.  $\rightarrow$  during shutdown period
- to remove scale deposits  
 hydrate  
 wax

scale  
 detritus  
 flocculant  
 wax

most of these chemicals are not recovered, reclaimed  
 except  $\left. \begin{array}{l} \text{MEG} \\ \text{MEOH} \\ \text{TEG} \end{array} \right\}$



- ① increased  $\Delta p$ , flow restrictions  
blockage
- ② integrity problems
- ③ loss in functionality of components

Summary table

flow assurance issue	consequence	corrective measures
slugging	①, ②, ③	selection of $\phi$ , trajectory of pipeline, filling or digging the seabed, control scheme. slug catcher $\rightarrow$ 1 <sup>st</sup> stage separator
wax	①	insulation design, heat tracing requirement of pigging loop chemical inhibitor $\rightarrow$ amounts to inject $\rightarrow$ distribution system
hydrate	①, ③	insulation design, heat tracing, chemical inhibitor $\rightarrow$ amounts $\rightarrow$ distribution system
scale	①, ③	chemical inhibitor $\rightarrow$ amounts in well injection $\rightarrow$ distribution system

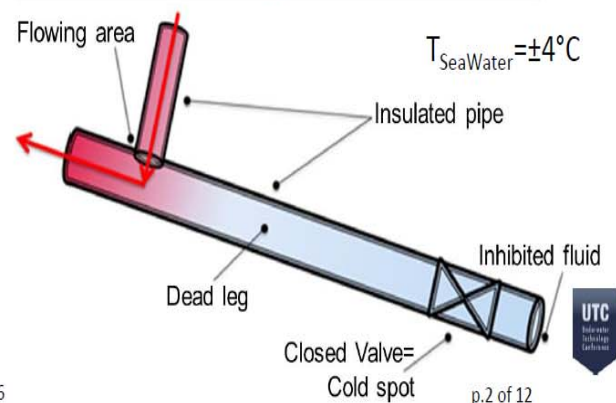
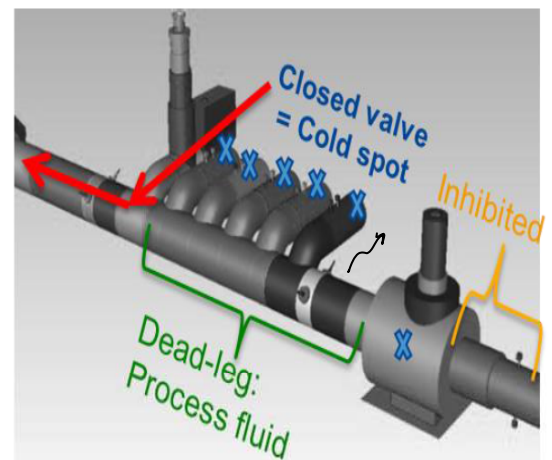
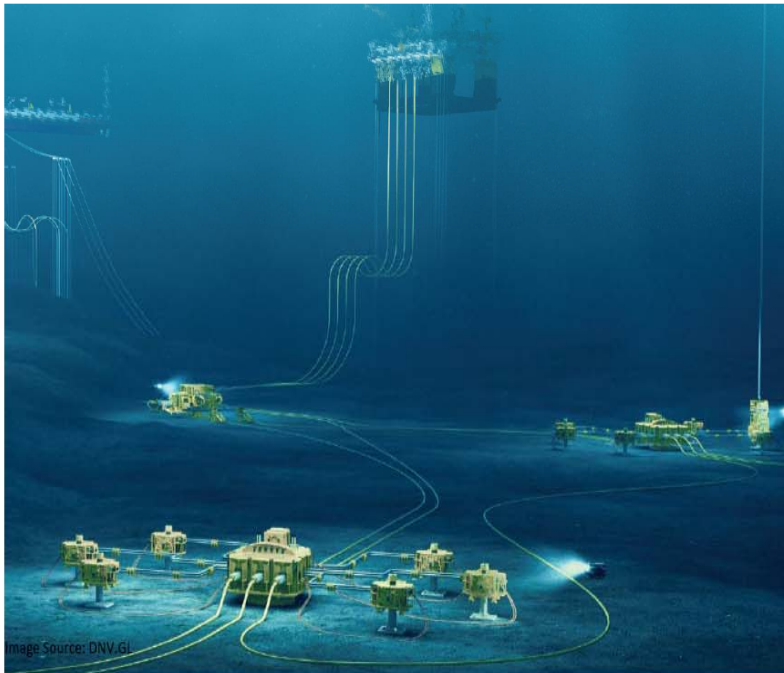
Erosion	②, ③	<ul style="list-style-type: none"> <li>• pipe size and diameter</li> <li>• flange dimensioning</li> <li>• component dimensioning</li> </ul>
Corrosion	②	chemical inhibitor $\rightarrow$ amounts $\swarrow$ well injection $\nwarrow$ distribution system
Erosion	①	chemical inhibitor $\rightarrow$ amounts $\swarrow$ well injection $\nwarrow$ distribution system

design and study of flow assurance problems in dead legs is also important

places where there is no flow during normal operations

## Subsea manifold and dead-leg geometry

- Dead-legs are inherently present



## Considerations during field development:

Early studies  $\rightarrow$  many development options

$\hookrightarrow$  detect potential showstoppers  $\left\{ \begin{array}{l} \rightarrow$  slugging \\  $\rightarrow$  wax \\  $\rightarrow$  hydrate \end{array} \right.

Front End Engineering design

$\hookrightarrow$  FEED  $\rightarrow$  (

a specific alternative selected

$\hookrightarrow$  in detail study  $\rightarrow$  hydrate management plan

$\hookrightarrow$  wax management plan

$\hookrightarrow$  detailed pipeline design

$\hookrightarrow$  prediction of temperature  
velocity  
pressure

n. components

dead legs

erosion

cold spots

FIV

$\hookrightarrow$  EPC Engineering Procurement Construction

## Tools used for analysis

Multiphase flow simulator  $\left\{ \begin{array}{l} \text{hydro} \text{ gap, pipeline} \end{array} \right\}$   
transient flow simulators  $\left\{ \begin{array}{l} \text{oiga, leda} \\ \text{Flow manager} \end{array} \right\}$

$\hookrightarrow$  predict  $\{ P, T, \alpha_o, \alpha_s, \alpha_w \}$  along the pipe for different times.

PVT analysis

$\left\{ \begin{array}{l} \bullet \text{ Lab test} \\ \bullet \text{ develop a EOS that represents} \\ \text{with an acceptable accuracy} \\ \text{my fluid} \\ \text{wax (WAT), hydrate, scale} \\ \text{emulsion} \end{array} \right.$

Lab test  $\rightarrow$  predict erosion rates

CFD computational fluid dynamics  $\left\{ \begin{array}{l} U_x, U_y, U_z \\ P, T \\ \text{in a 3D domain} \end{array} \right.$

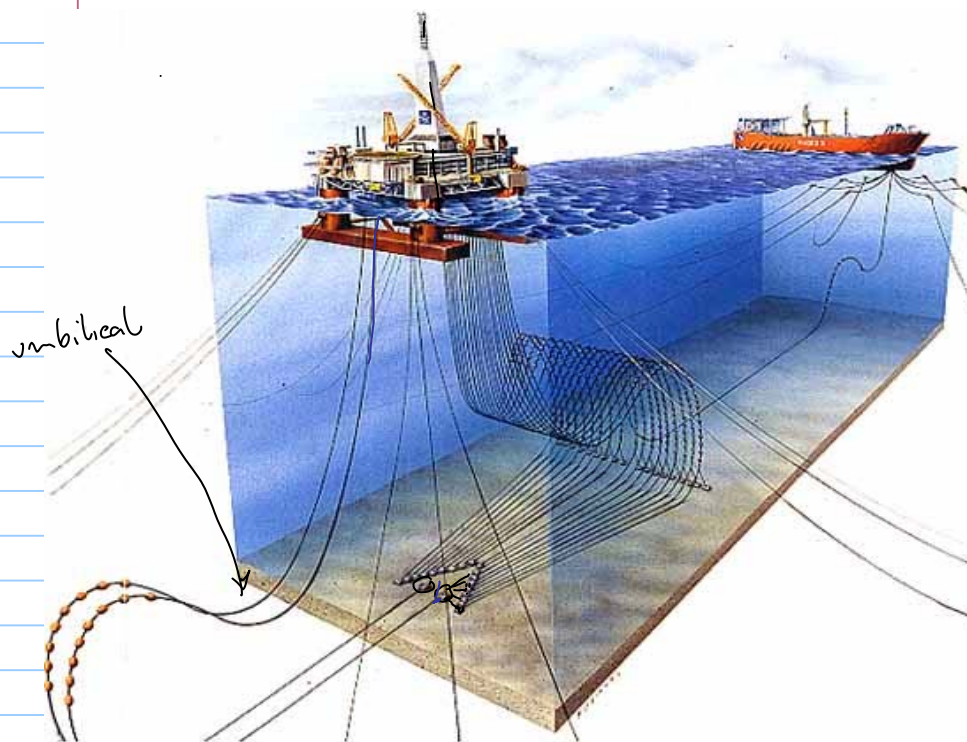
FEA Finite element analysis

$\left\{ \begin{array}{l} \text{displacement} \\ \text{stresses in a} \\ \text{3D geometry} \end{array} \right.$

Standards  $\sim$  cookbook, Recommended practice.

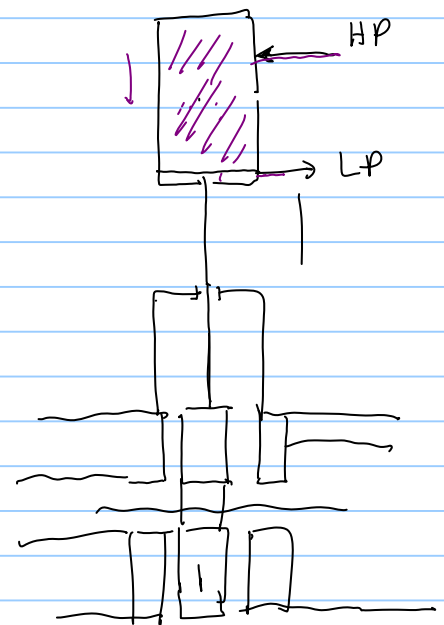
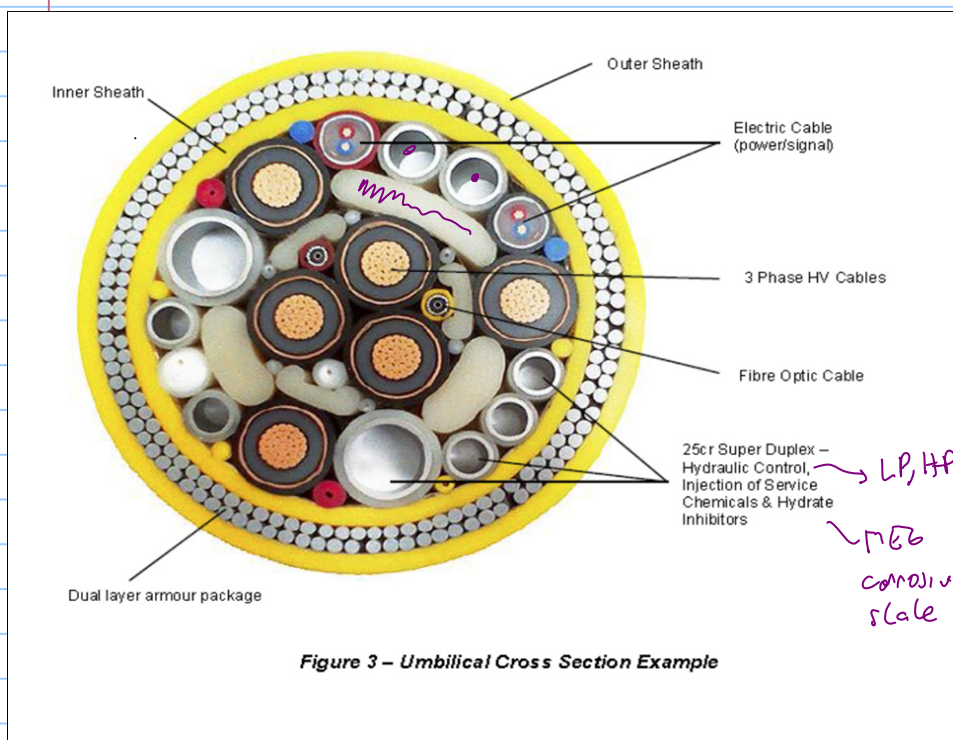


delivery system for production chemicals:

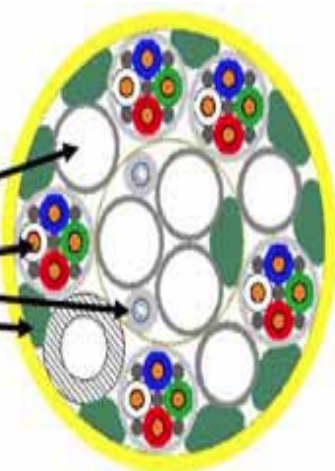


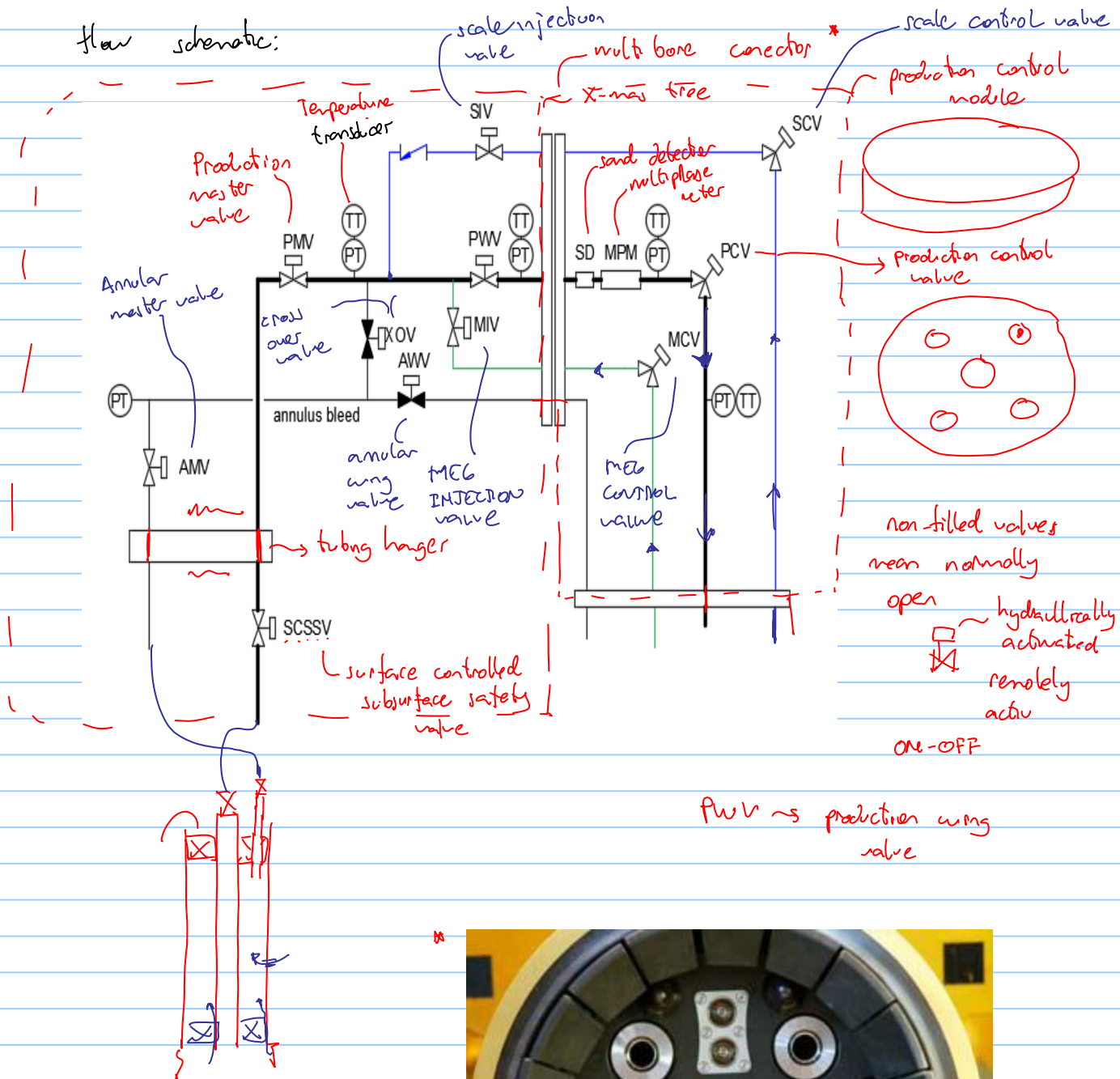
Njord

CDU  
control distribution unit  
SDU  
subsea distribution unit

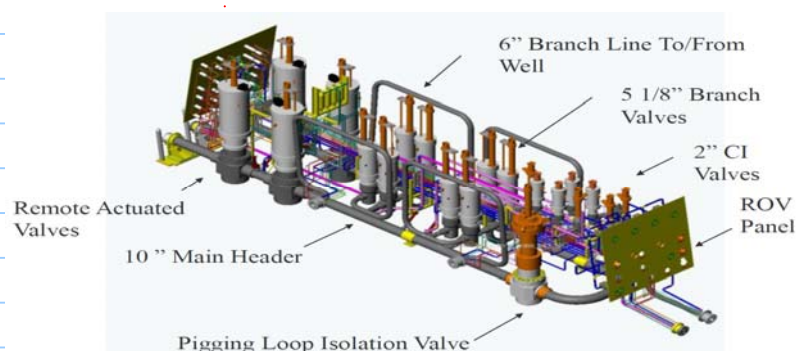
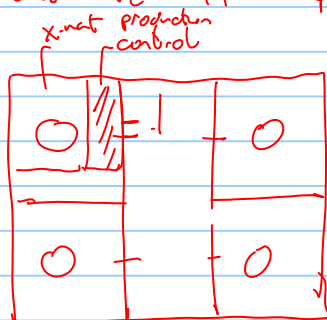


HP hydraulic supply lines  
LP hydraulic supply lines  
Hydraulic return line  
Electric power / signal cables  
Fibre Optical cables  
Fillers (fill empty room)



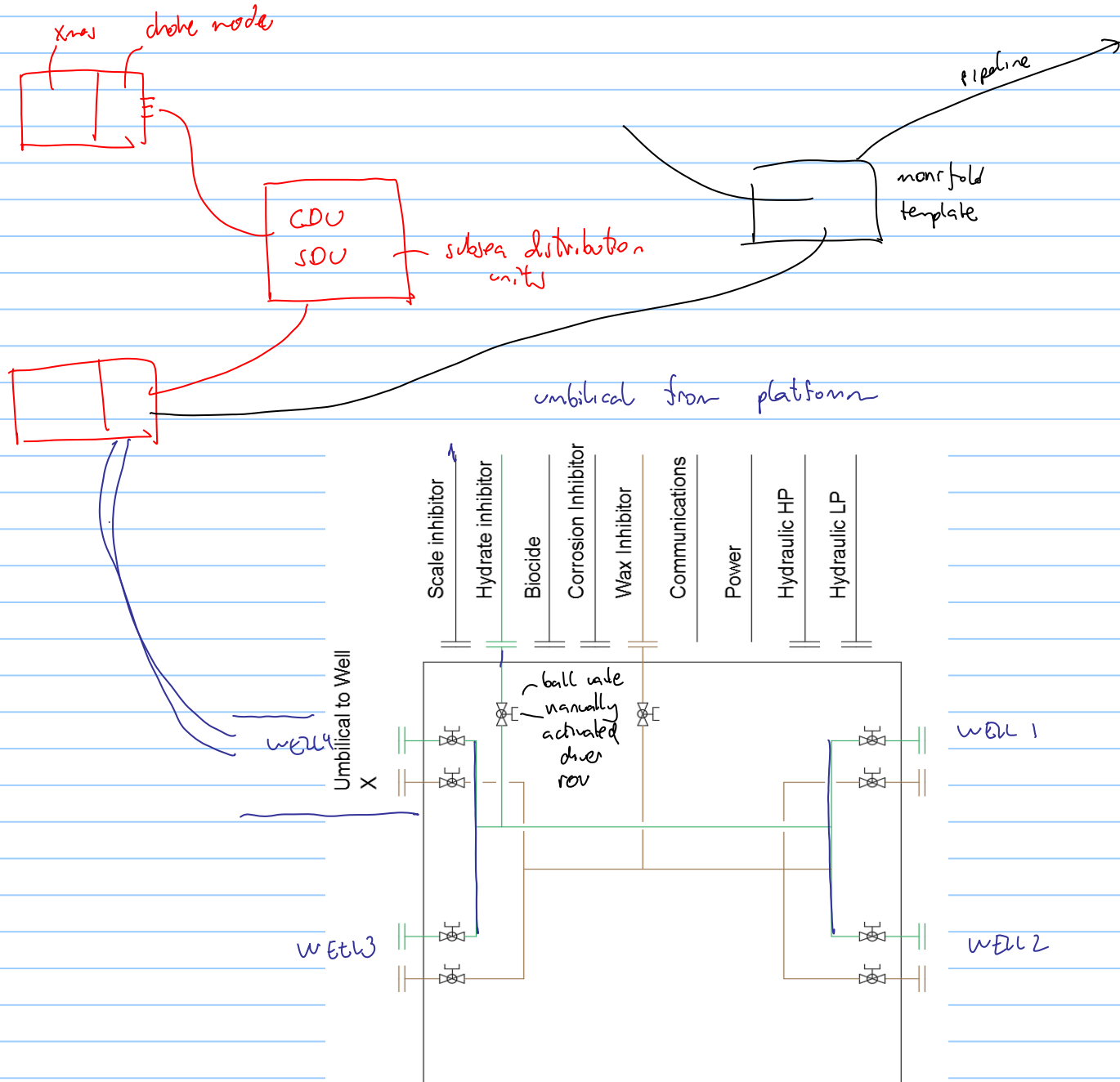


if the wells are in templates

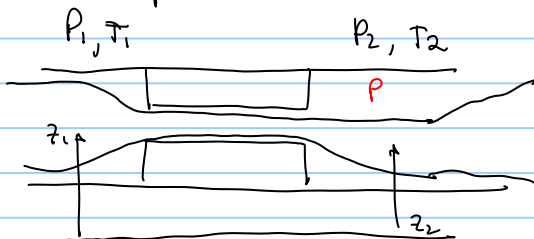




if well are satellite



fluid cooling due to expansion in chokes

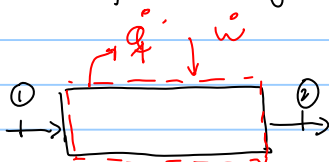


$$\Delta p = p_1 - p_2$$

$$T_1 \approx T_R$$

$T_2$  might be very different from  $T_1$ , specially if mainly gas

1<sup>st</sup> law of thermodynamics for open systems



$$\dot{q} - \dot{w} = \dot{m} \left( u_2 + \frac{p_2}{\rho_2} + z_2 g + \frac{v_2^2}{2} - u_1 + \frac{p_1}{\rho_1} + z_1 g + \frac{v_1^2}{2} \right)$$

for chokes  $\dot{q} = 0$   
 $\dot{w} = 0$

$$z_1 \approx z_2 \quad v_1 \approx v_2$$

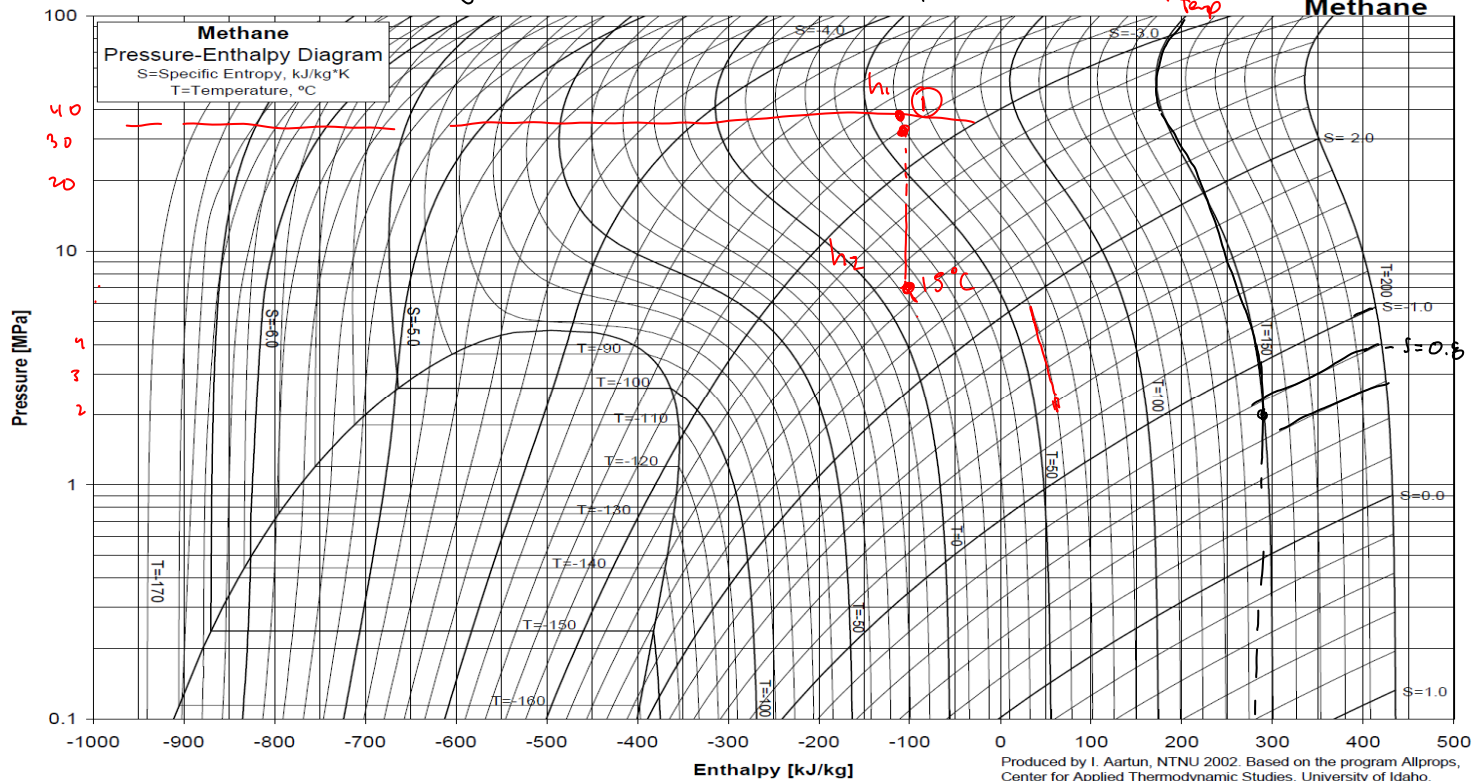
$h$  enthalpy  
 $h = u + p v$   $v = \frac{1}{\rho}$   
 $\downarrow$  internal energy

for valves  $h_1 = h_2$  use thalpac

$T_1 = 20^\circ\text{C}$   
 $p_{\text{wh}} = 34.3 \text{ bara}$

$\Delta P = 26.7 \text{ bara}$   
 chose

$P_2 = 7.7 \text{ bar}$   $7.7 \text{ MPa}$



temperature drop in pipe - conduction

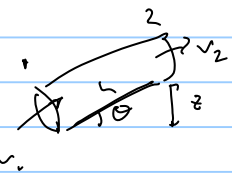
$$\dot{q} - \dot{q}_0 = \dot{m} \left( u_2 + \frac{p_2}{\rho_2} + z_2 g + \frac{v_2^2}{2} - u_1 + \frac{p_1}{\rho_1} + z_1 g + \frac{v_1^2}{2} \right)$$

$$d\dot{q} = \dot{m} (dh + dzg + v dv) \text{ divide by } dL$$

$$\frac{d\dot{q}}{dL} = \dot{m} \left( \frac{dh}{dL} + \frac{dz}{dL} g + v \frac{dv}{dL} \right)$$

$$\frac{dz}{dL} = \sin(\theta)$$

pipe inclination

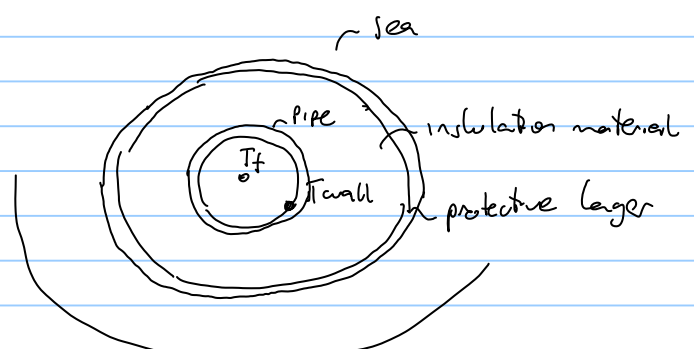
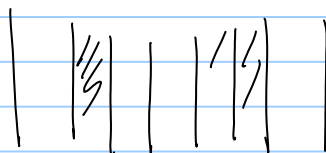


$$\frac{d\dot{q}}{dL} = \dot{m} \left( \frac{dh}{dL} + \sin \theta g + v \frac{dv}{dL} \right)$$

fluid model  
 $h = f(p, T)$

• Tamb

the cross section of a pipe segment

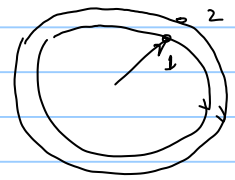


heat transfer

in solids conduction

$$\dot{q} = 2\pi L \cdot K \left( \frac{T_1 - T_2}{\ln\left(\frac{r_2}{r_1}\right)} \right)$$

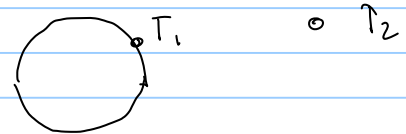
conductivity  
of material



{ pipe wall  
 { insulation material  
 { sock.

in liquid convection  $\begin{matrix} \nearrow \text{free} \\ \searrow \text{forced convection} \end{matrix}$

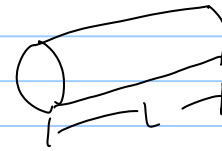
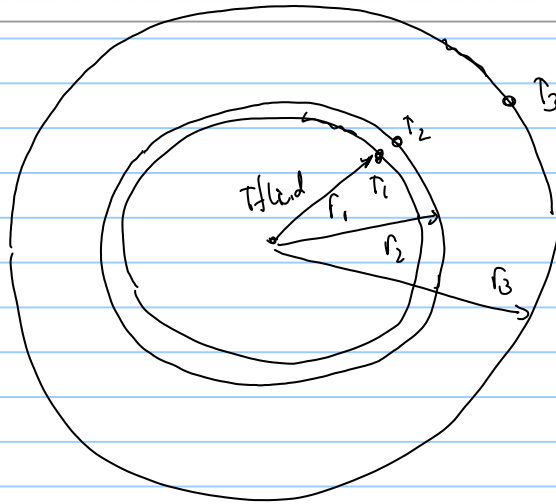
$$\dot{q} = 2\pi r L h (T_1 - T_2)$$



$$(T_f - T_{wall}) = \frac{\dot{q}}{2\pi r L h_{int}}$$

$$(T_{wall, in} - T_{wall, out}) = \frac{\dot{q}}{2\pi r L K} \ln\left(\frac{r_2}{r_1}\right)$$

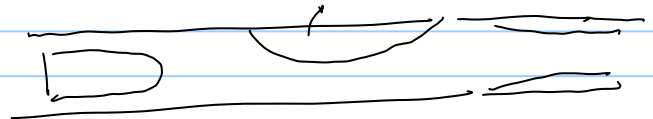
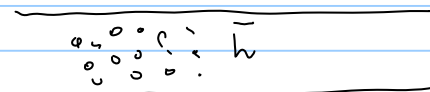
$$(T_f - T_{amb}) = \dot{q} \left( \overset{con}{\quad} + \overset{cond1}{\quad} \overset{cond2}{\quad} \overset{con3}{\quad} \overset{con4}{\quad} \right)$$



Sea bed • Tamb

- forced convection on internal flow

$$\dot{q} = 2\pi r_1 L \underbrace{h_{int}}_{\text{forced convection}} (T_f - T_1)$$



- Conduction in pipe wall

$$\dot{q} = 2\pi L k_{pipe} \frac{(T_1 - T_2)}{\ln\left(\frac{r_2}{r_1}\right)}$$

- Conduction in insulating layer

$$\dot{q} = 2\pi L K_{insulation} \cdot \frac{(T_2 - T_3)}{\ln\left(\frac{r_3}{r_2}\right)}$$

$$\dot{q} = A \cdot h (\Delta T)$$

$$\Delta T = \frac{\dot{q}}{A \cdot h}$$

- Convection in sea

$$\dot{q} = 2\pi r_3 h_{out} L (T_3 - T_{amb})$$

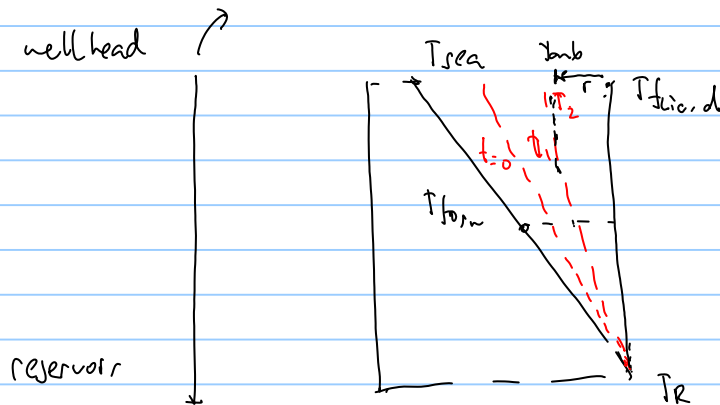
in these equations dec the Temperature differences and sum them up:

$$(T_f - T_1) + (T_1 - T_2) + (T_2 - T_3) + (T_3 - T_{amb}) = \dot{q} \left( \frac{1}{2\pi r_1 L h_{int}} + \frac{\ln\left(\frac{r_2}{r_1}\right)}{2\pi k_{pipe} L} + \frac{\ln\left(\frac{r_3}{r_2}\right)}{2\pi K_{insulation} L} + \frac{1}{2\pi r_3 L h_{out}} \right)$$

$$(T_f - T_{amb}) = \dot{q} \underbrace{\frac{1}{U \cdot 2\pi r_3 L}}_{\text{overall heat transfer coefficient}} = \dot{q} \left( \frac{1}{2\pi r_1 L h_{int}} + \frac{\ln\left(\frac{r_2}{r_1}\right)}{2\pi k_{pipe} L} + \frac{\ln\left(\frac{r_3}{r_2}\right)}{2\pi K_{insulation} L} + \frac{1}{2\pi r_3 L h_{out}} \right)$$

$$\frac{1}{U} = \left[ \frac{1}{h_{in} \left( \frac{r_1}{r_3} \right)} + \frac{\ln \left( \frac{r_2}{r_1} \right) r_3}{k_{pipe}} + \frac{r_3 \ln \frac{r_3}{r_2}}{k_w} + \frac{1}{h_{out}} \right]$$

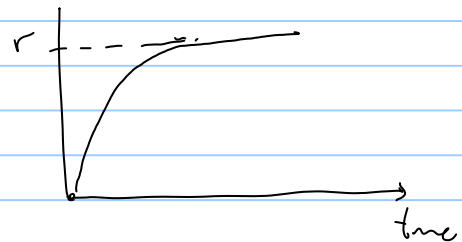
(overall heat transfer coefficient referred for outer area)



$$\frac{\partial}{\partial t} \neq 0$$

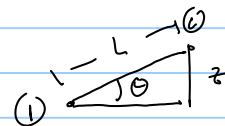
$T_{amb}$  will be located at an position  $r$  that varies with time.

Ramey - Stanford (1956)



Energy equation in the fluid:

$$\frac{d\dot{q}}{dl} = \dot{m} \left( \frac{dh}{dl} + v \frac{dv}{dl} + \frac{dz}{dl} g \right)$$



$$\frac{z}{L} = \sin(\theta)$$

$$\frac{d\dot{q}}{dl} = \dot{m} \left( \frac{dh}{dl} + v \frac{dv}{dl} + \sin(\theta) g \right)$$

(p, T)  
EoS  
correlation

• neglecting velocity changes along the pipe  $\rightarrow$  heavy oil + water

if liquid  
•  $dh = C_p(T) dT$

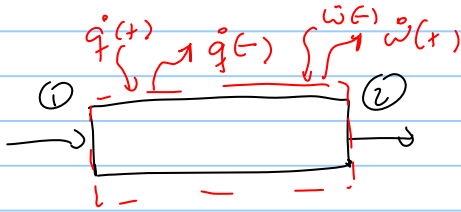
for gas, compressible fluid, Joule Thompson

$$dh = C_p(T) dT + \frac{1}{\rho} dp$$

neglect

$$\frac{d\dot{q}}{dl} = \dot{m} \left( C_p \frac{dT}{dl} + \sin \theta g \right)$$

$$\dot{q} = 2\pi r_{out} L U_{out} (T_f - T_{amb})$$



$$-2\pi \text{Lat } U_{\text{out}} (T - T_{\text{amb}}) = \dot{m} c_p \frac{dT}{dL} + \dot{m} g \sin \theta$$

$$\frac{dy}{dx} + ay = C$$

$$\frac{dT}{dL} + T \cdot \frac{1}{A} - \frac{T_{\text{amb}}}{A} - \frac{\sin(\theta) \cdot g}{c_p} = 0$$

$$u \cdot \frac{dT}{dL} + u \cdot T \cdot \frac{1}{A} = u \cdot \left( \frac{T_{\text{amb}}}{A} + \frac{\sin(\theta) \cdot g}{c_p} \right)$$

$$u = e^{\frac{x}{A}}$$

$$e^{\frac{x}{A}} \cdot \frac{dT}{dL} + e^{\frac{x}{A}} \cdot T \cdot \frac{1}{A} = e^{\frac{x}{A}} \cdot \left( \frac{T_{\text{amb}}}{A} + \frac{\sin(\theta) \cdot g}{c_p} \right)$$

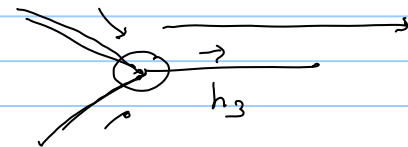
$$\frac{d\left(e^{\frac{x}{A}} \cdot T\right)}{dL} = e^{\frac{x}{A}} \cdot \left( \frac{T_{\text{amb}}}{A} + \frac{\sin(\theta) \cdot g}{c_p} \right)$$

$$e^{\frac{x}{A}} \cdot T \Big|_{T_0}^{T(x)} = \left( \frac{T_{\text{amb}}}{A} + \frac{\sin(\theta) \cdot g}{c_p} \right) \cdot A \cdot e^{\frac{x}{A}} \Big|_0^x$$

$$e^{\frac{x}{A}} \cdot T(x) - T_0 = \left( \frac{T_{\text{amb}}}{A} + \frac{\sin(\theta) \cdot g}{c_p} \right) \cdot A \cdot \left( e^{\frac{x}{A}} - 1 \right)$$

$$T(x) = T_0 \cdot e^{-\frac{x}{A}} + \left( \frac{T_{\text{amb}}}{A} + \frac{\sin(\theta) \cdot g}{c_p} \right) \cdot A \cdot \left( 1 - e^{-\frac{x}{A}} \right)$$

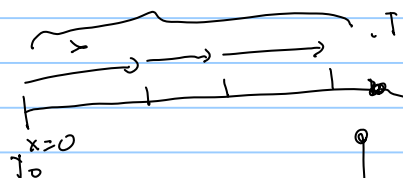
$$A = \frac{\dot{m} c_p}{2\pi \text{Lat} \cdot U}$$



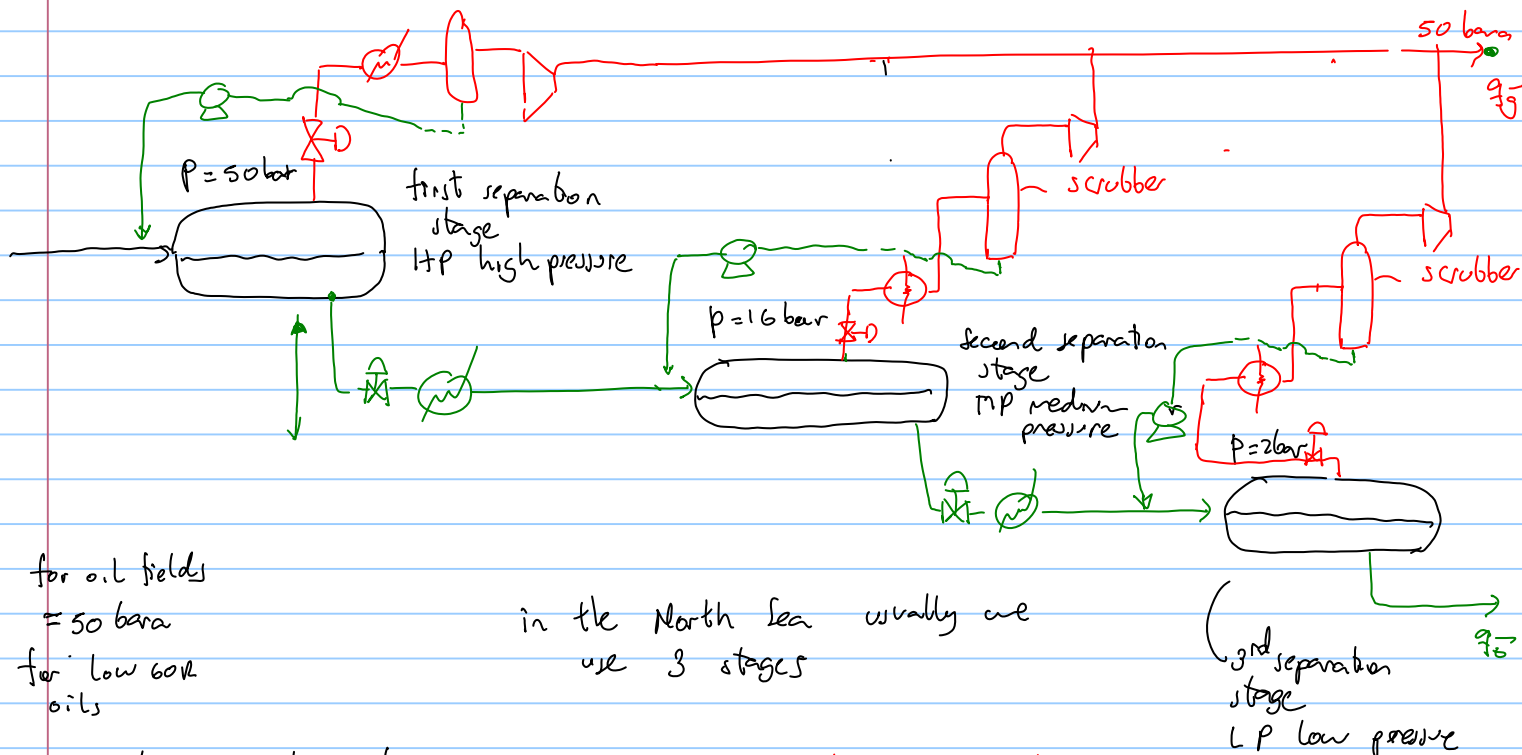
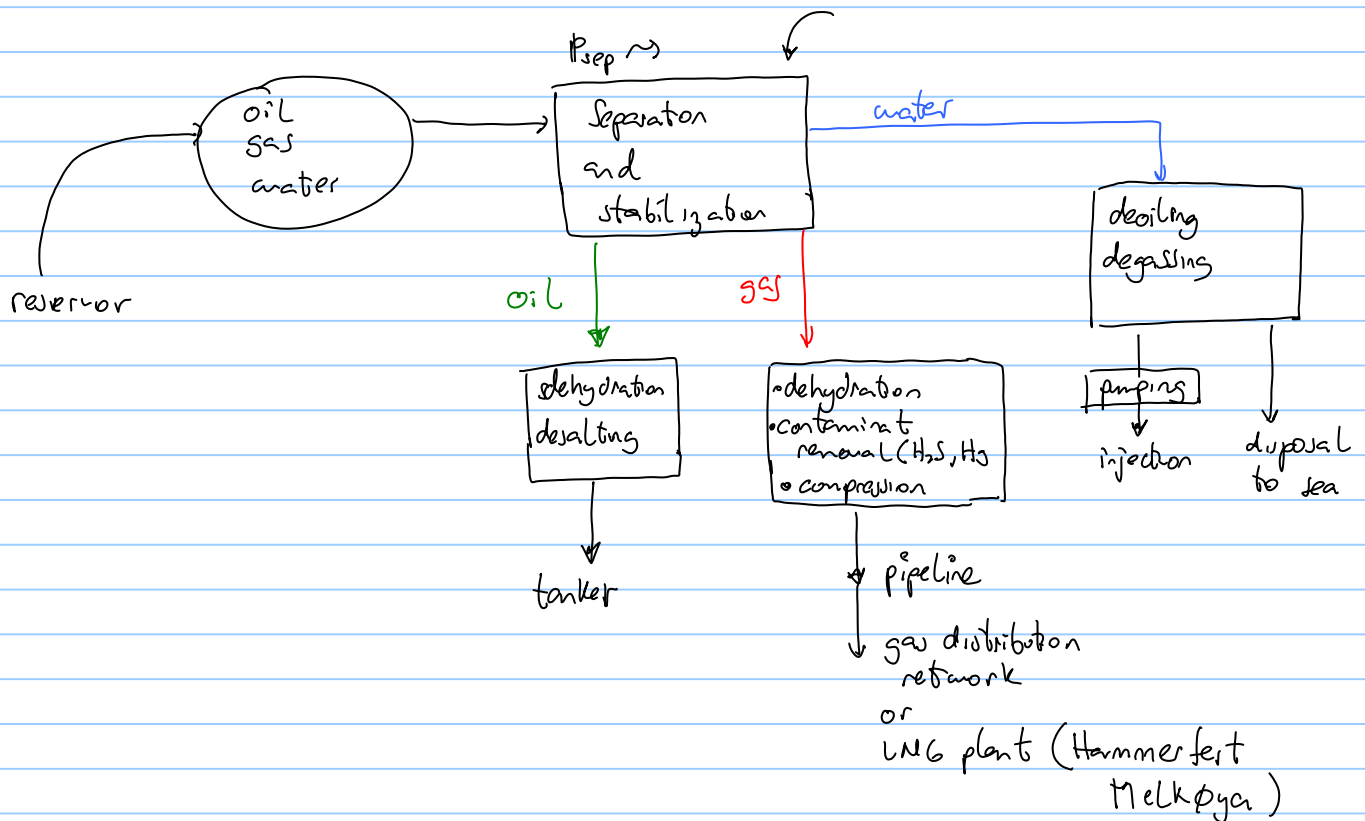
$$\dot{m}_1 h_1 + \dot{m}_2 h_2 = \dot{m}_3 h_3$$

this equation applies for a given pipe segment when  $U, c_p, \theta, \dot{m}, \text{Lat},$  remain constant.

$x$  is distance ALONG pipe.



# Processing of hydrocarbon fluids $\rightarrow$ equipment on platform

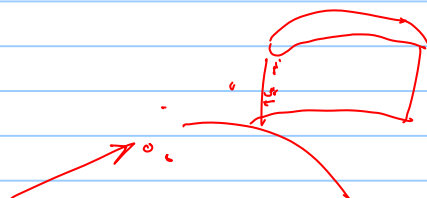


for oil fields  
 $\approx 50$  bara  
 for low 60%  
 oils

it can be down to 20 bara  
 for gas  
 higher than 50 bara

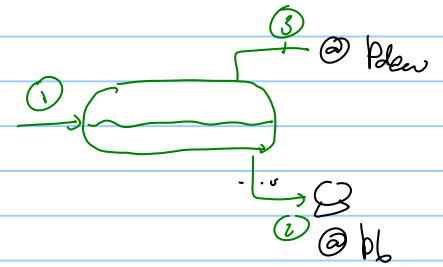
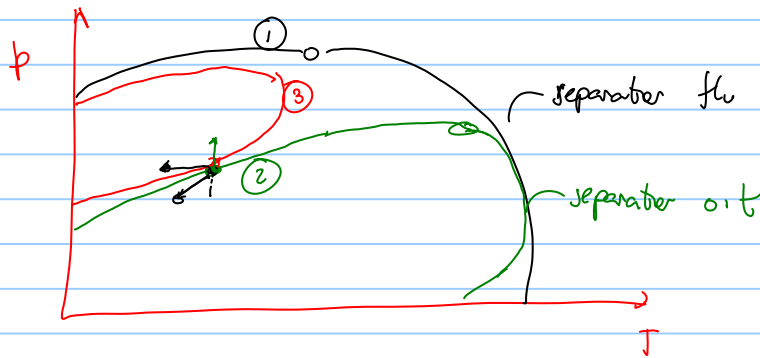
in the North Sea usually we  
 use 3 stages

compressor can only work with  
 gas (dry)



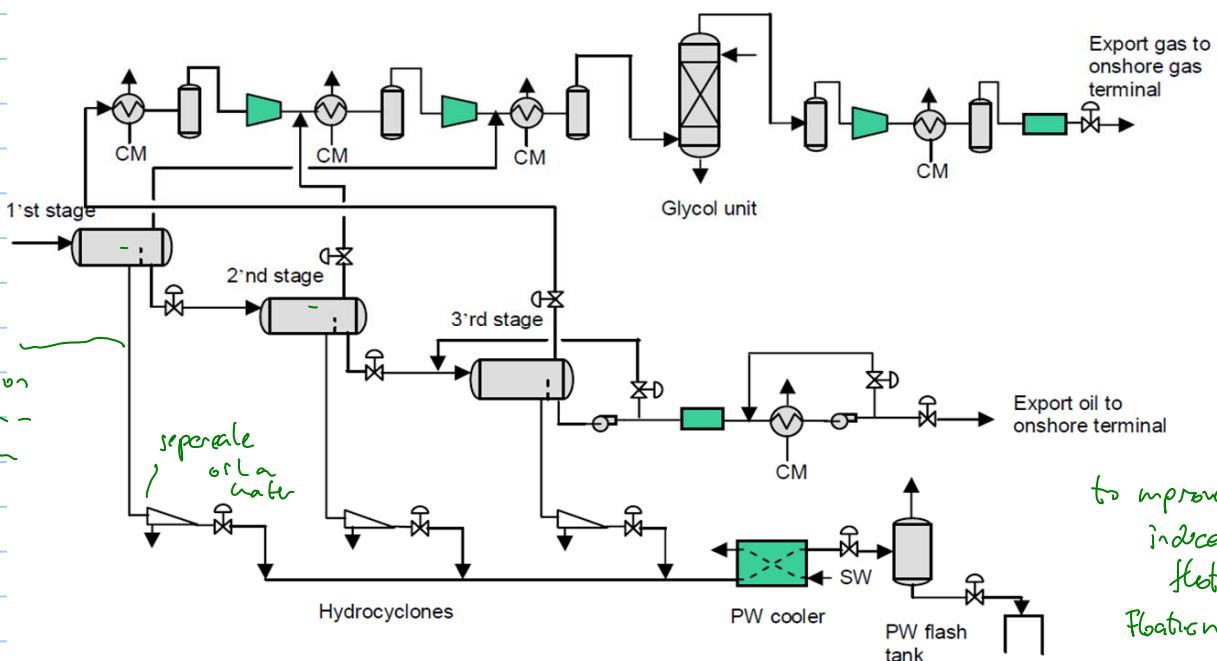
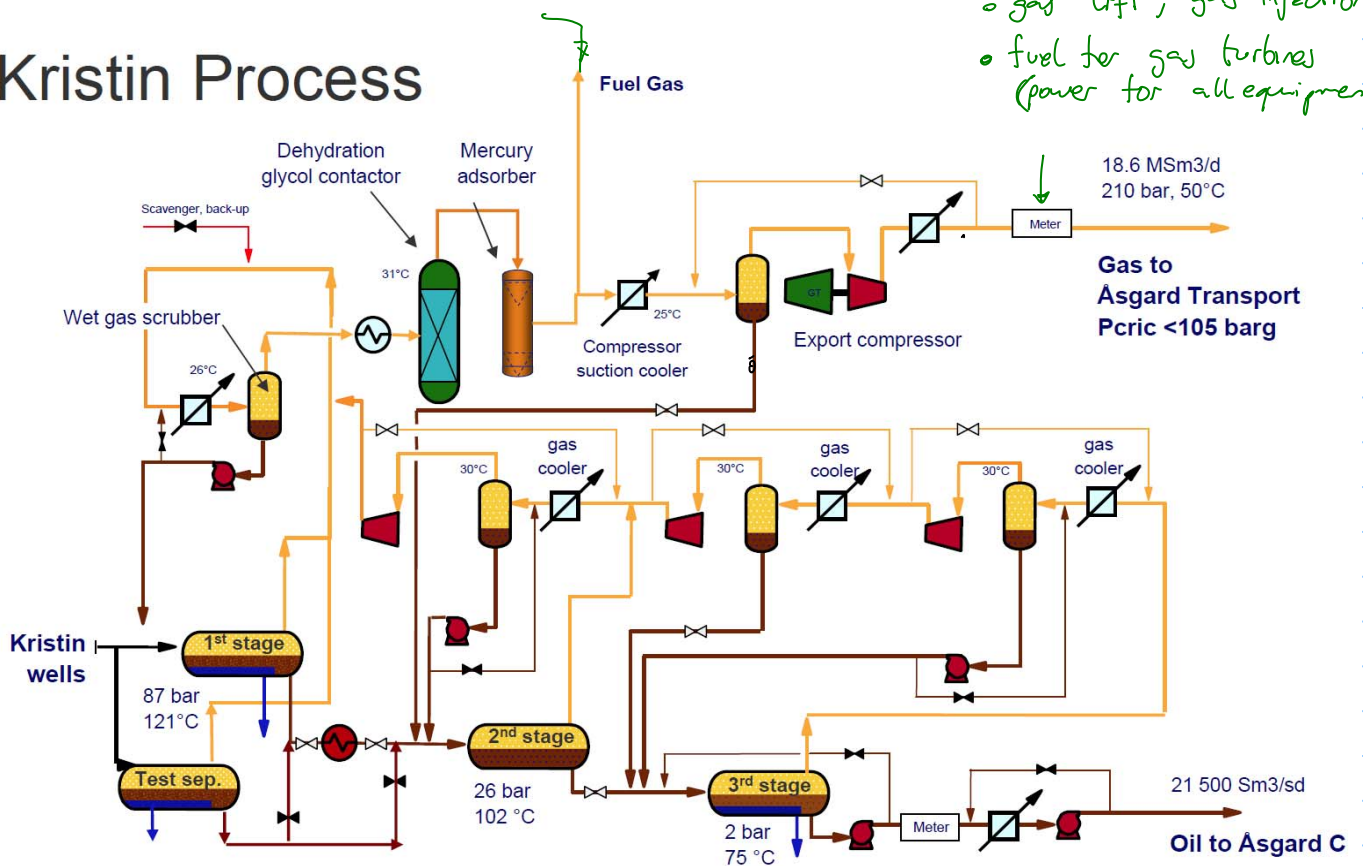


in every separation stage



gas can be used for  
 • gas lift, gas injection  
 • fuel for gas turbines (power for all equipment)

# Kristin Process



Oil concentration  
 1000ppm -  
 500ppm

separate  
 oil & water

to improve separation  
 induced gas  
 flotation  
 Flotation tanks

typical processing capacities:  
of an oil field

$$q_o : 8000 \text{ m}^3/\text{d} - 50000 \text{ m}^3/\text{d}$$

$$q_g = 1.5 - 8.5 \text{ Eb m}^3/\text{d}$$

$$p_{HP} \approx 50 \text{ bara}$$

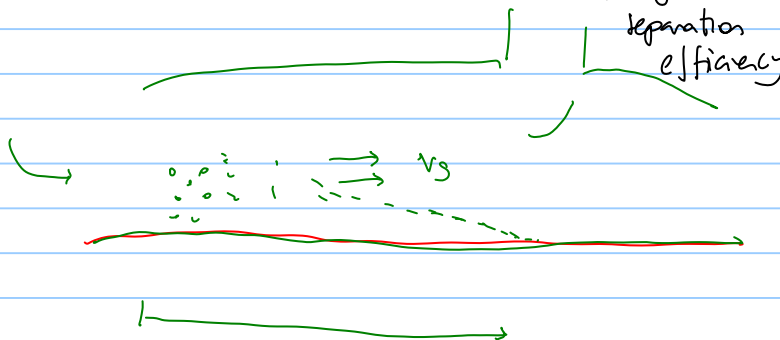
number of stages : 3

number of trains : 1-2

How processing facilities affect the field design process?

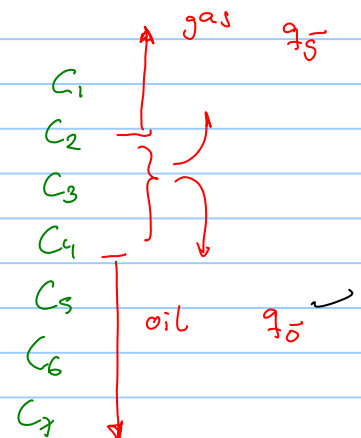
- Pressure of 1<sup>st</sup> stage separator

- high pressure gives better liquid recovery
- high pressure reduce production rates from reservoir
- high pressure  $\rightarrow$  gas occupies less volume  
 $v_g$  are less  $\rightarrow$  less  $\Delta p$   
 $\rightarrow$  higher separation efficiency

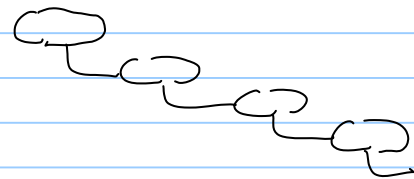


Usually for oil  $p_{HP}$  is 50 bara or less

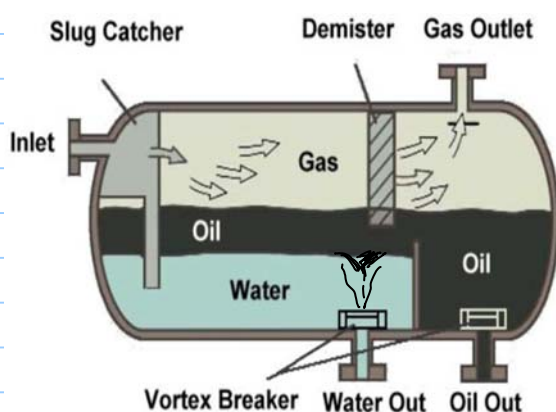
Usually for gas  $p_{HP}$  can be higher 50 bara



more separation stages  
also improve liquid  
recovery



Separators are three phase separator (most of the water is separated in the first stage)



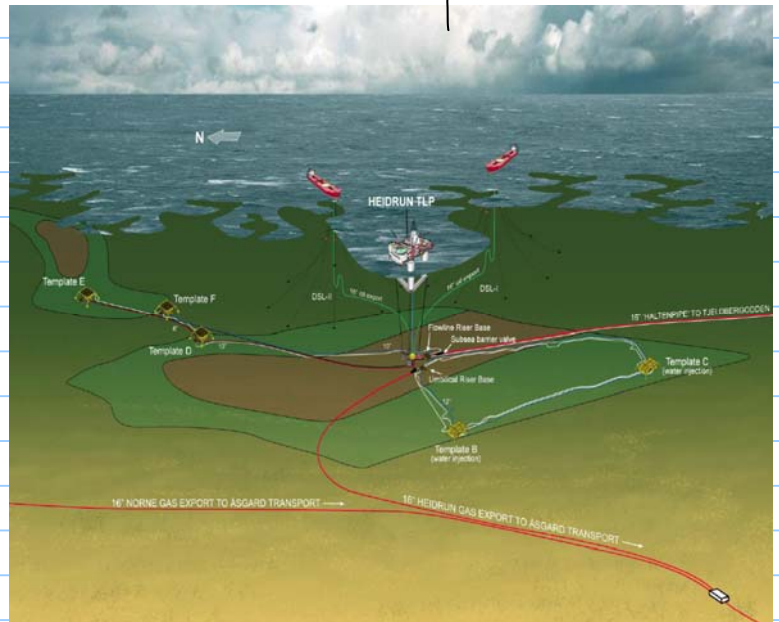
facilities have maximums of : processing capacity of gas { dehydration unit  
compressor

If at any point in time, i reach one of these capacities,  
there is no choice but to choke back production!

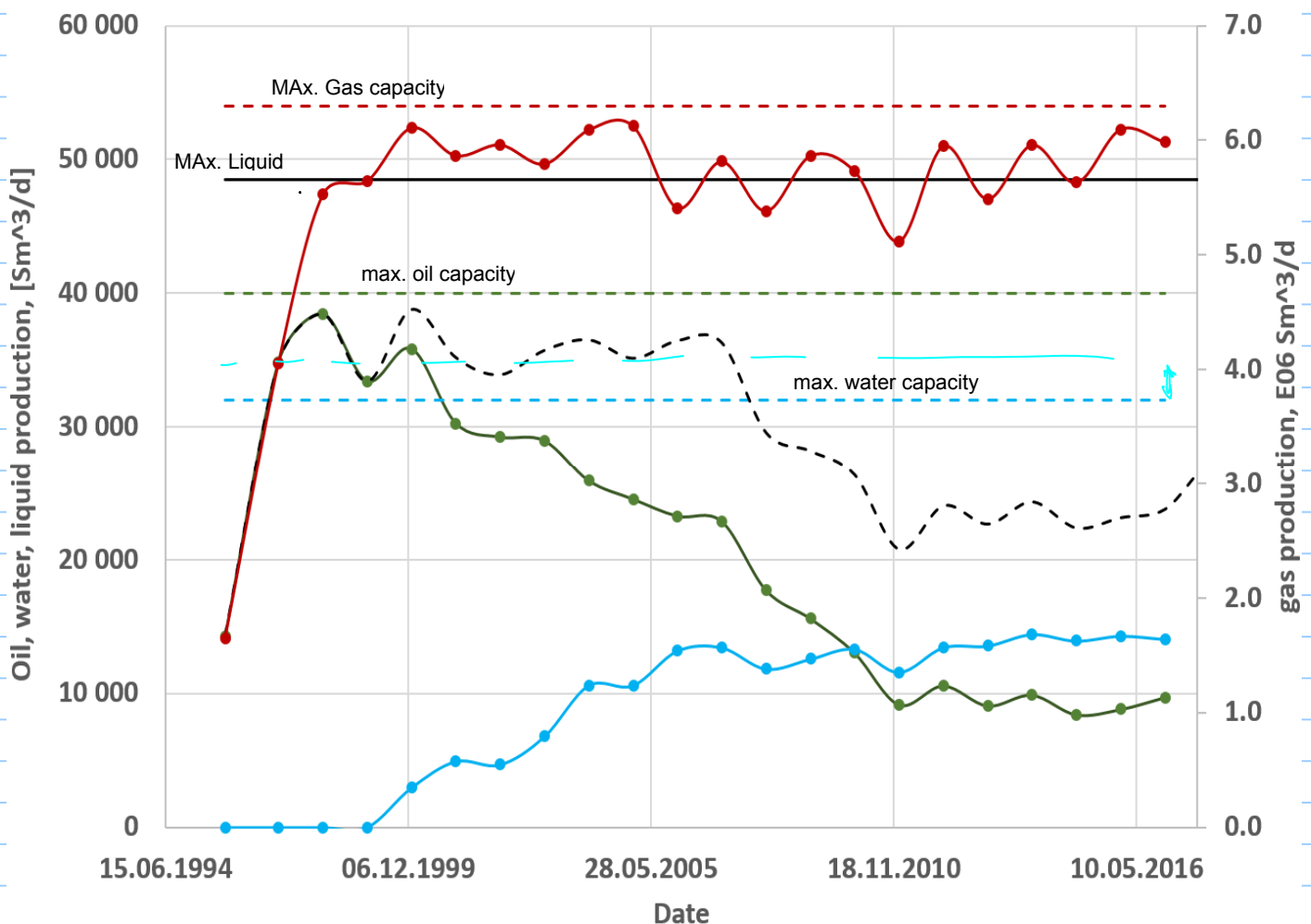
processing capacity of water { cyclones

processing capacity of liquid { separator capacity  
separator level

Let's look at the production profile of Heidrun:

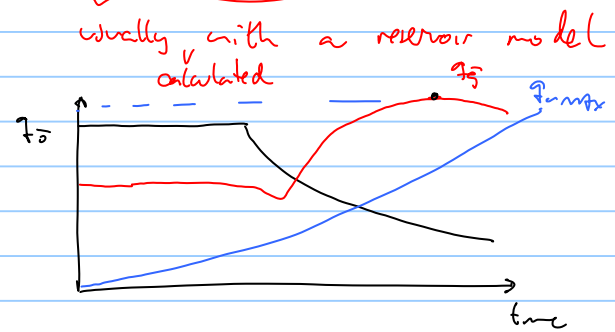


In Heidrun it looks like gas is at its maximum capacity, thus it might indicate that the production of the field had to be choked back.



Increasing the capacity of the processing facilities costs money, bigger capacity, bigger size, more weight and more space on the platform. The optimal capacity should be studied using an economic analysis to choose capacity values that do not increase significantly capex but still give high NPV.

CAPEX of topside processing facilities:  $f(q_o(t), q_g(t), q_w(t))$



during production actual profiles can be different than the profiles predicted during the design phase  $\rightarrow$  GOR, WC

Be sure  $q_{g \text{ fixed}} \leq q_{g \text{ max}}$  processing facilities

$$q_{w \text{ fixed}} \leq q_{w \text{ max}}$$

$$q_{i \text{ fixed}} \leq q_{i \text{ max}}$$

$q_{w \text{ max}}$  occupies space that could potentially be used for oil.

the only way to ensure this is choosing production.

we could use optimization for this.  
Ranking method

well usually have different GOR  
WC  
choosing which well to choke and  
which well to produce.

Determining optimum P of second stage separator to increase liquid recovery.

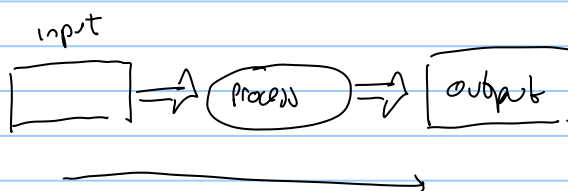
Hysys  $\rightarrow$  simulating processes  $\rightarrow$  processing facilities

compositional simulator EOS { Peng Robinson  
SRK  
Aspentech

Honeywell  $\rightarrow$  UNISIM (same source code as Hysys but developed by another company).

Class exercise.

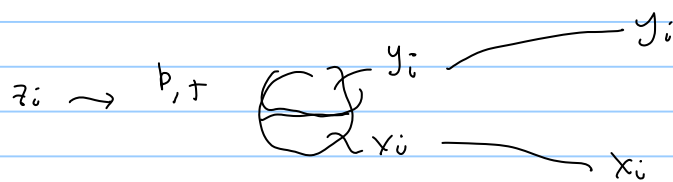
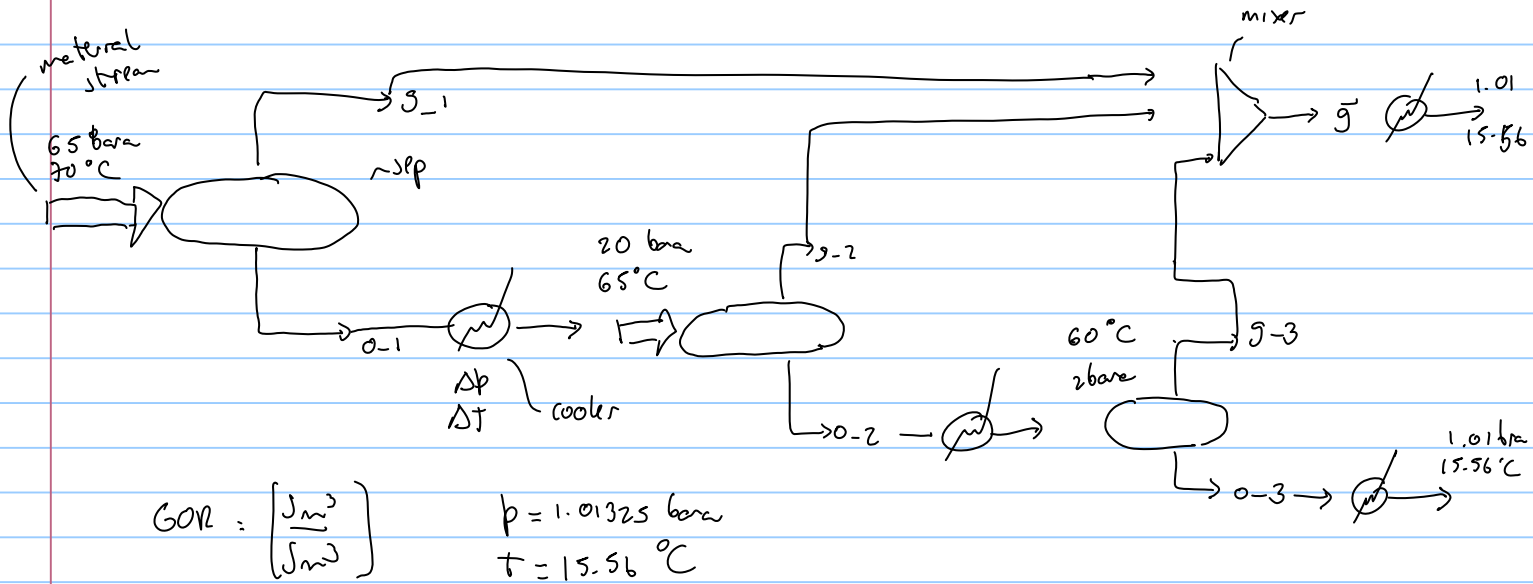
[http://folk.ntnu.no/stanko/Courses/TPG4230/2017/Class\\_files/20170328/](http://folk.ntnu.no/stanko/Courses/TPG4230/2017/Class_files/20170328/)



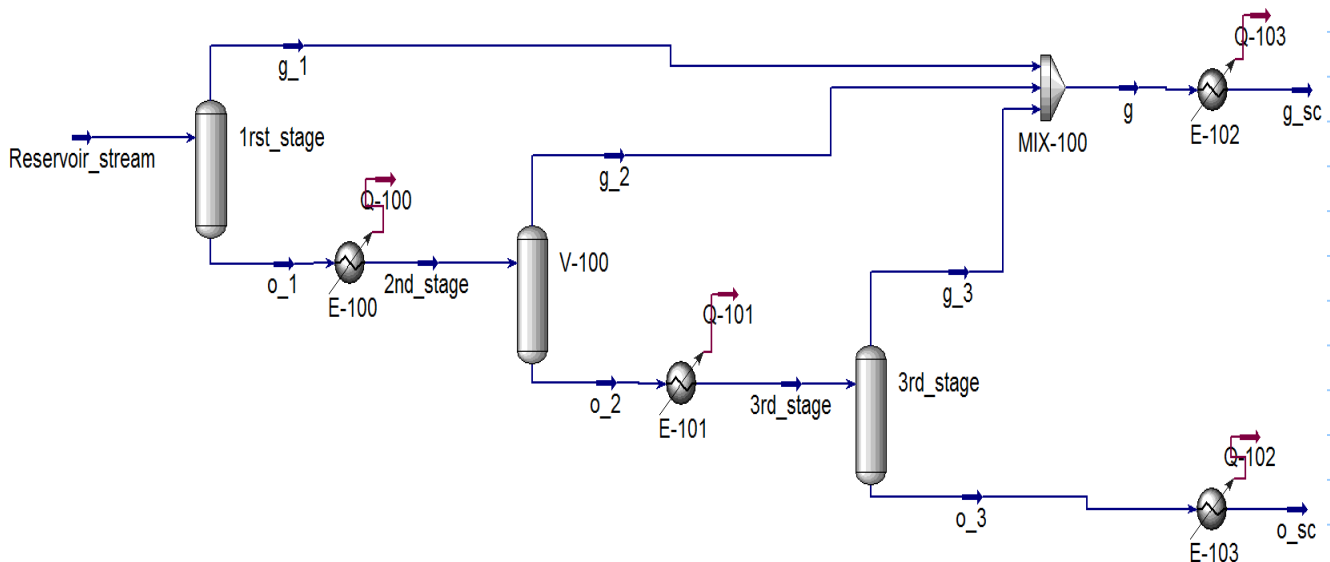
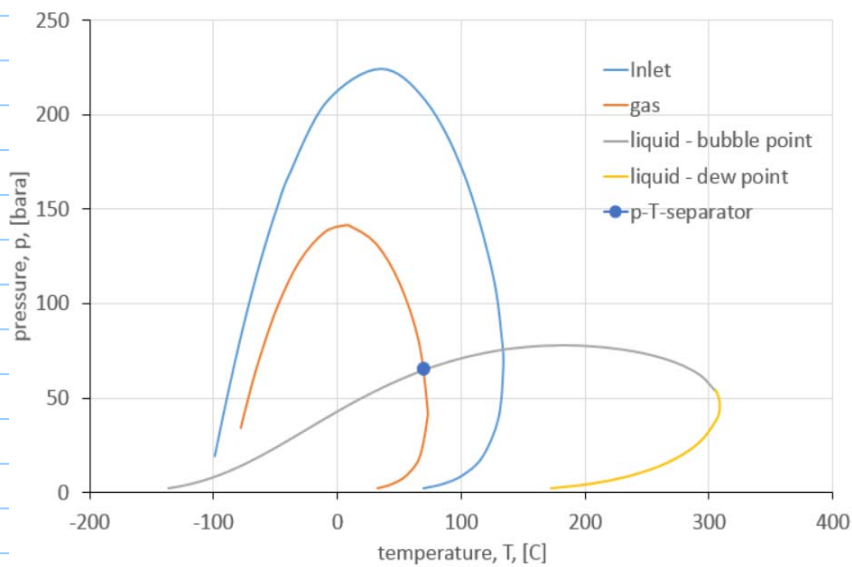
co-current

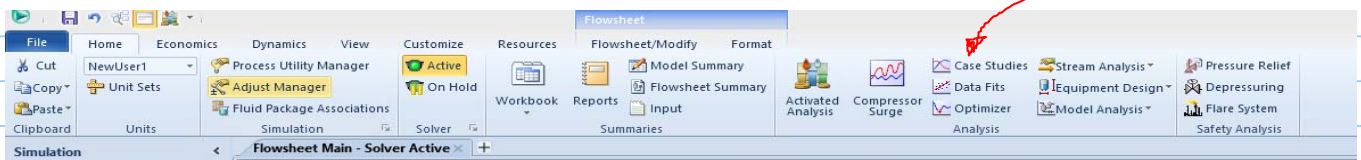
always downstream

always along the direction of flow



First stage separator, GFC

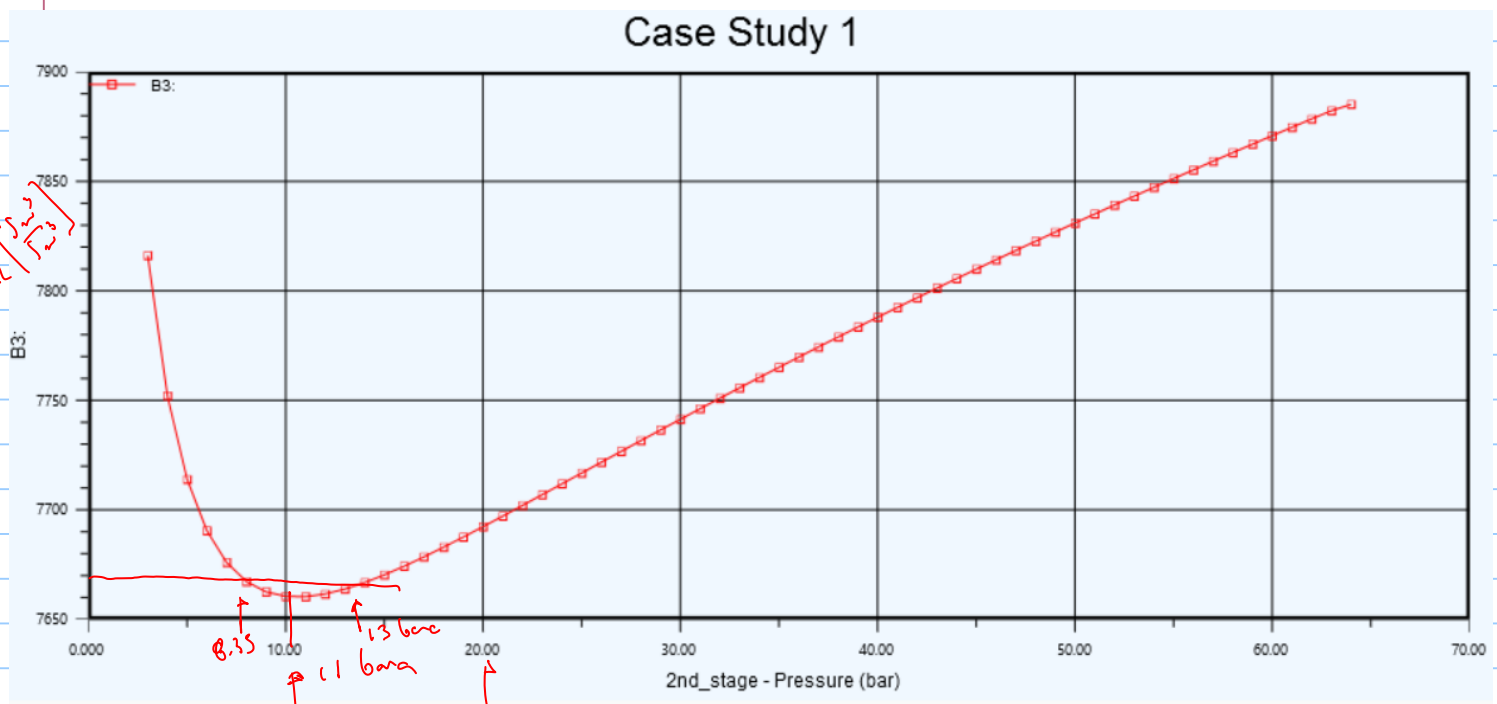




## Case studies

Object	Variable	Independent	Include
2nd_stage	Pressure	Yes	<input checked="" type="checkbox"/>
SPRDSHT-1	B3:	No	<input checked="" type="checkbox"/>

$x$   $y$   
 $y = f(x)$   
 $GOR = f(P_{sep})$



$GOR = 7692 \text{ S}_m^3/\text{S}_m^3$   
 $GOR = 7660 \text{ S}_m^3/\text{S}_m^3$

if  $75 \text{ liq} = 756 \text{ S}_m^3/\text{d}$

$P_{sep} = 20 \text{ bara}$

$7_{liquid} = 910.04 \text{ S}_m^3/\text{d}$

$P_{sep} = 11 \text{ bara}$

$7_{liquid} = 913.83 \text{ S}_m^3/\text{d}$

$3.8 \text{ S}_m^3/\text{d}$

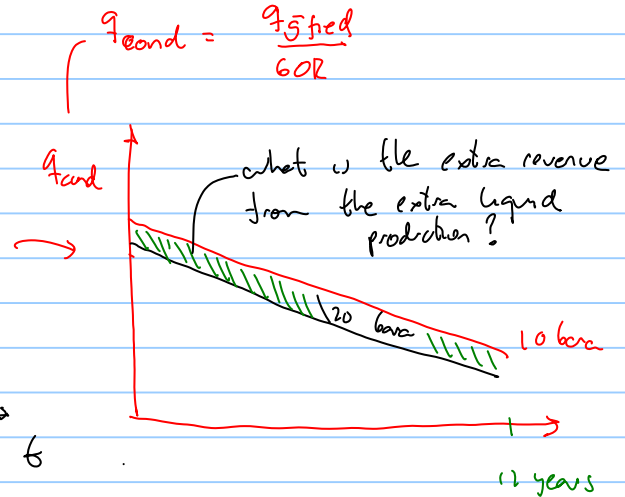
$24 \text{ Stb/d}$

@  $50 \text{ w/d}$   
 $\frac{661}{661} \approx 1200 \text{ w/d/d}$



to compare the two options  $P_{2nd\ stage} = 20\ \text{bar}$  vs.  $10\ \text{bar}$

Compute GOR for all years



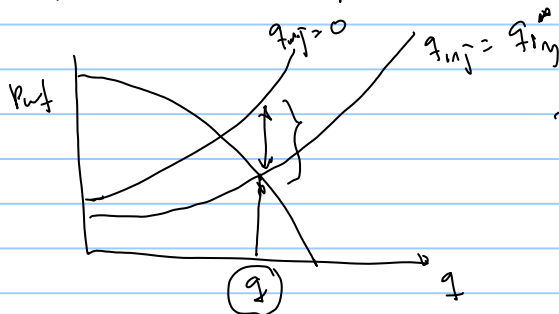
$$q_{\text{cond}} = \frac{q_{\text{liquid}}}{\text{GOR}}$$

Other Hysys tricks

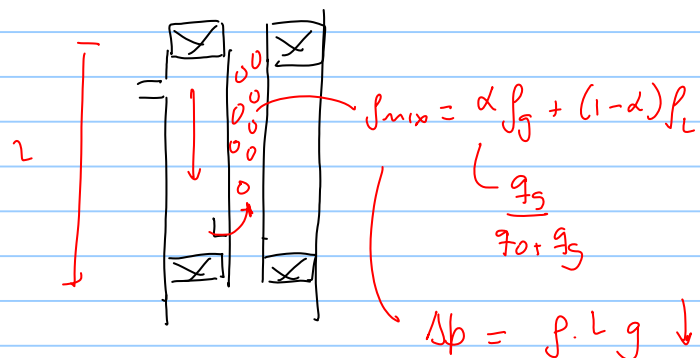


calculates everything all the time  
doesn't calculate

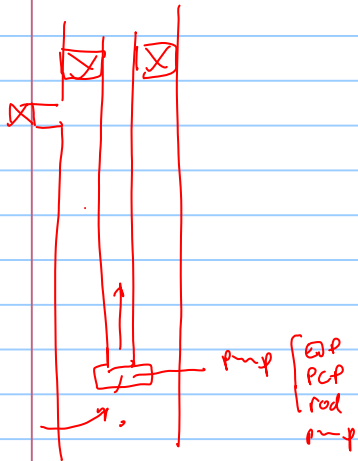
Artificial lift: methods deployed in well to increase production and natural flow



gas lift  
reduce the density of the flowing mixture in the tubing by injecting gas

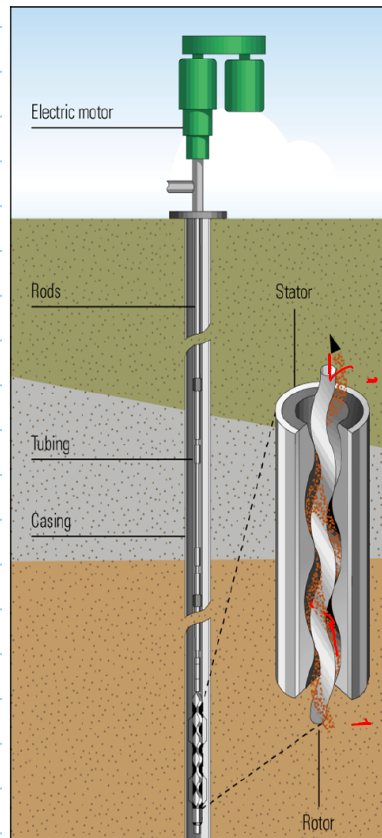


• PCP Progressive cavity pump



if  $P_{wt} \leq P_b$   
then gas  
should be  
produced through  
annulus

if  $P_{wt} > P_b$   
single phase oil  
pump section



• rod pumping

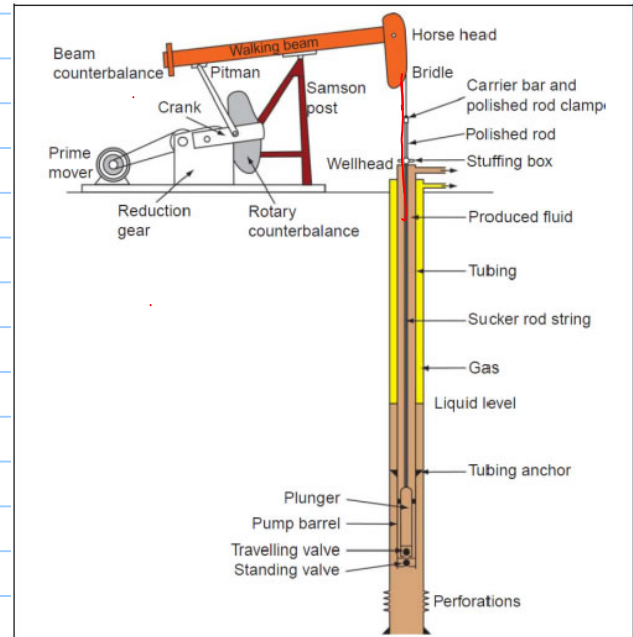
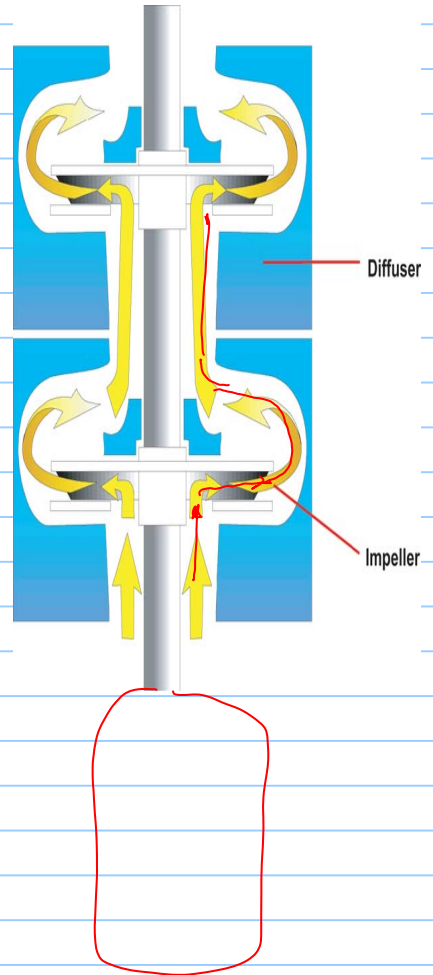
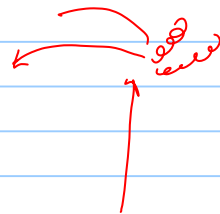
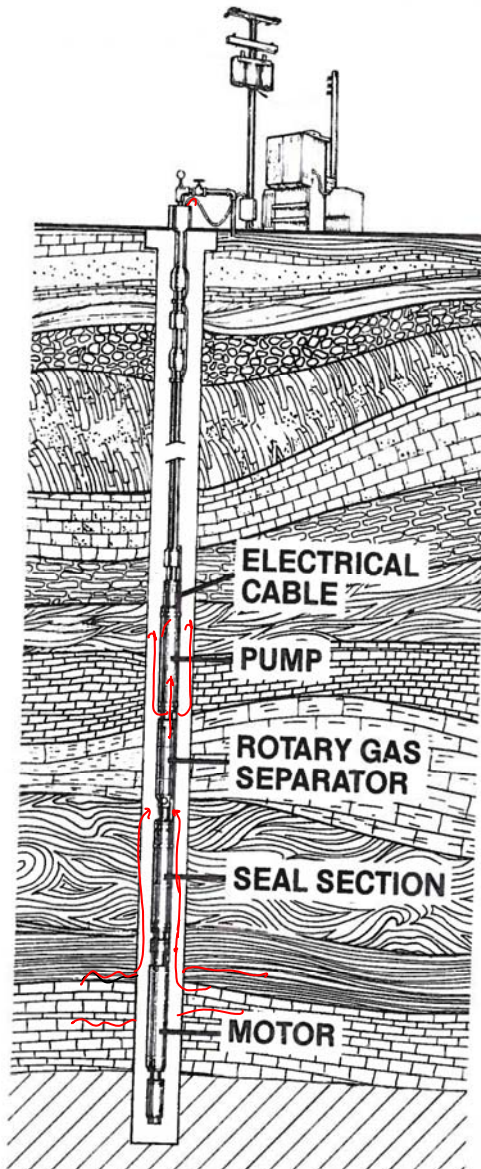


Figure 2. Typical configuration of a sucker rod pump (Bellarby, 2009).

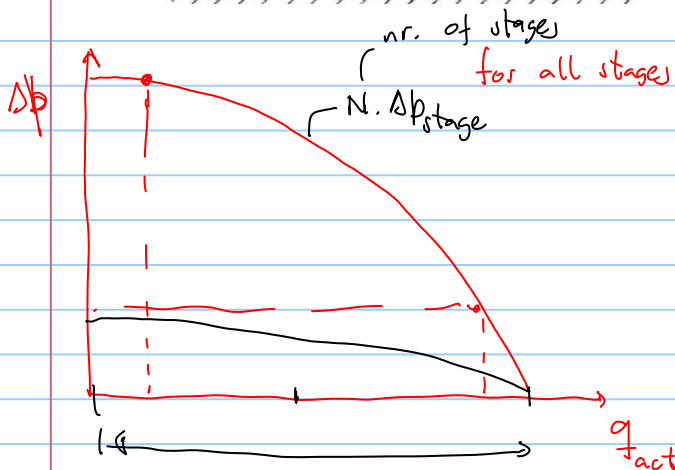
- ESP Electric submersible pump • Russian engineer (Armais Arutunoff)
- centrifugal pump installed in the wellbore  
driving electrical motor is also in the wellbore



50 - 100 stages



$p_{wf} < p_b$



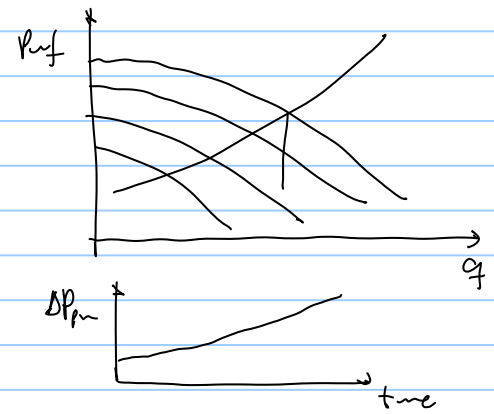
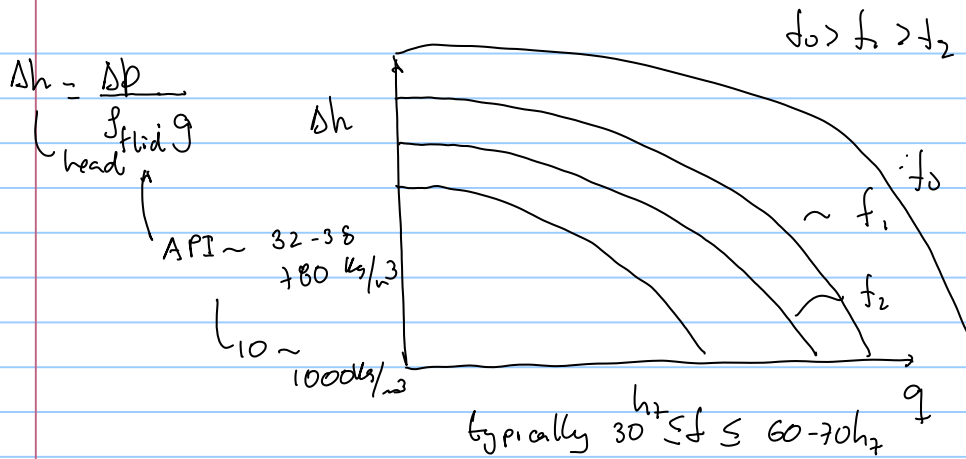
with  $q_{required}$  and  $\Delta p_{required}$

the

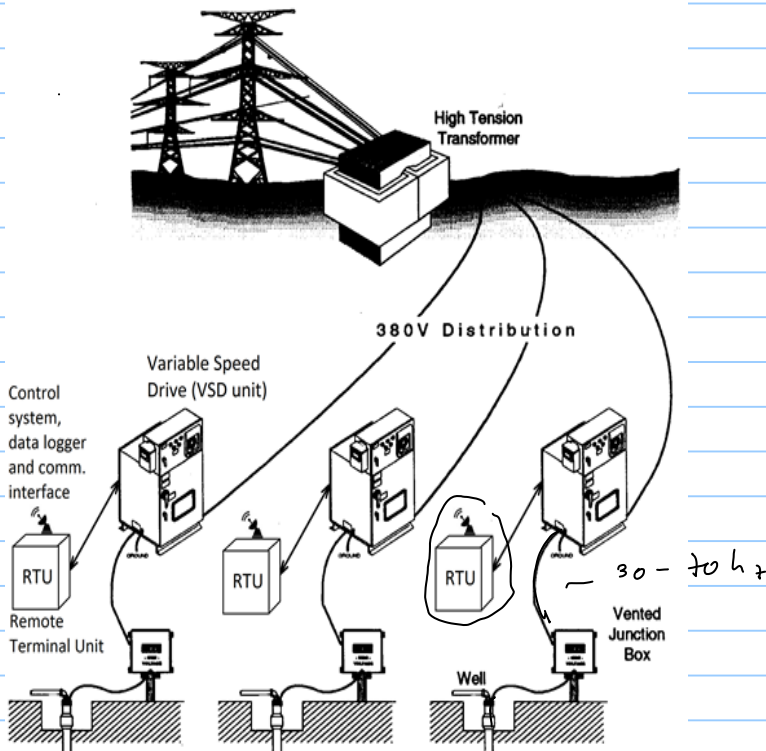
$$N_{stages} = \frac{\Delta p_{required}}{\Delta p_{stage}} \cdot F$$

$F$   
performance factors

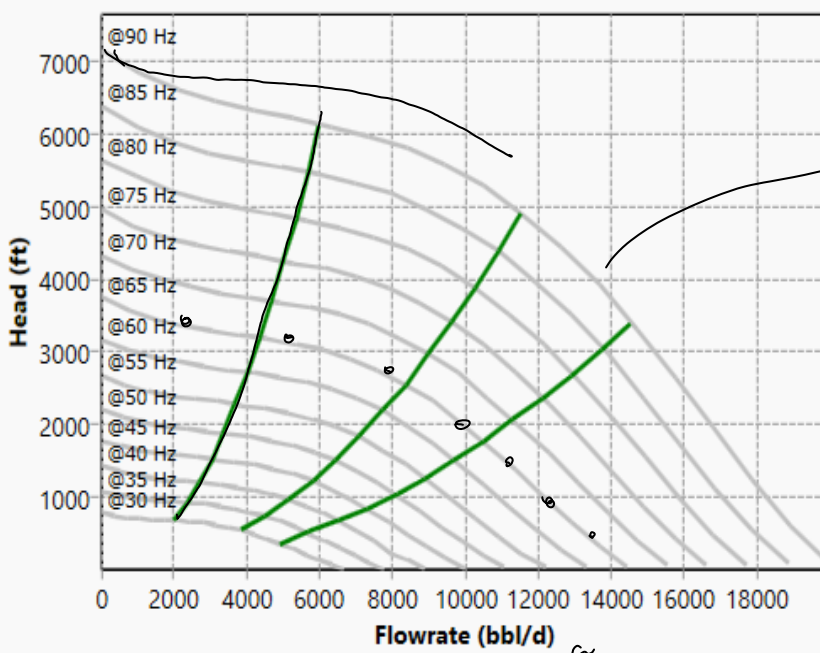




change the rotational speed of pump



WoodGroup TE7000\_Imported  
50 Stages



usually represented with a  
polynome

$$\Delta h = a q^4 + b q^3 + c q^2 + d q + e$$

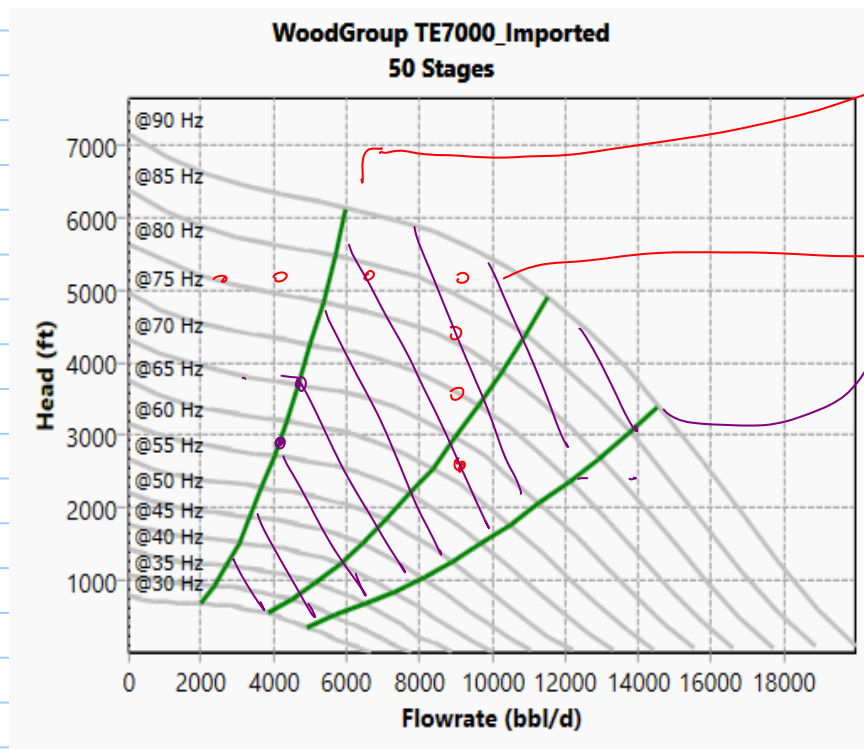
the  $a, b, c, d, e$  to  
measured data @ reference  
frequency {60 Hz  
for another speed one use  
similarity law. ~ 60 Hz

$$\frac{\Delta h @ f_1}{\Delta h @ f_2} = \left( \frac{f_1}{f_2} \right)^2$$

calculated for 60 hz

$$\Delta H = \left( a_4 \cdot \left( \frac{60 \text{ hz}}{f} \right)^4 + a_3 \cdot \left( \frac{60 \text{ hz}}{f} \right)^3 + a_2 \cdot \left( \frac{60 \text{ hz}}{f} \right)^2 + a_1 \cdot \left( \frac{60 \text{ hz}}{f} \right) + a_0 \right) \cdot \left( \frac{f}{60 \text{ hz}} \right)^2$$

$$\frac{q_{@f_1}}{q_{@f_2}} = \left( \frac{f_2}{f_1} \right)$$



minimum flow rate line  
maximum flow rate line

line	q	Δb
1	q <sub>1</sub>	Δb <sub>1</sub>
2	q <sub>2</sub>	Δb <sub>2</sub>
3	q <sub>3</sub>	Δb <sub>3</sub>
4		
5		

$q_{min}(t) \leq q \leq q_{max}(t)$  for  
every frequency

if not pump life is reduced  
dramatically !

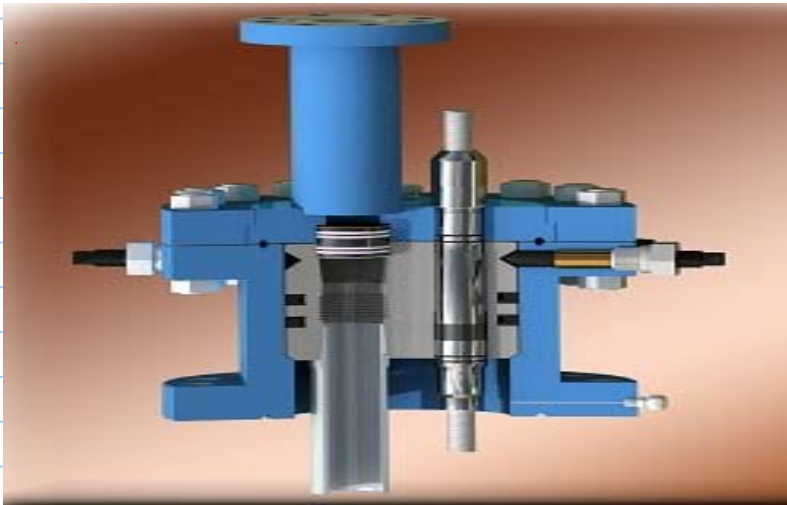
typical pump life  $\approx$  2 years  
5 years

not favorite for subsea installations  
due to increased maintenance  
frequency !

typical intervention time in  
subsea systems is 5 years.



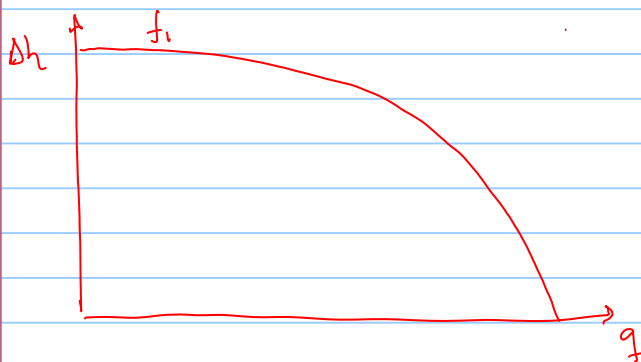
04.04.2017 . Multiphase subsea boosting  
 06.04.2017 . Production optimization  
 20.04.2017 . Course wrap-up



operational limitations of ESP's  
 so far

$$30\text{Hz} \leq f \leq 70\text{Hz}$$

$$P_{suc} > f \cdot P_b$$



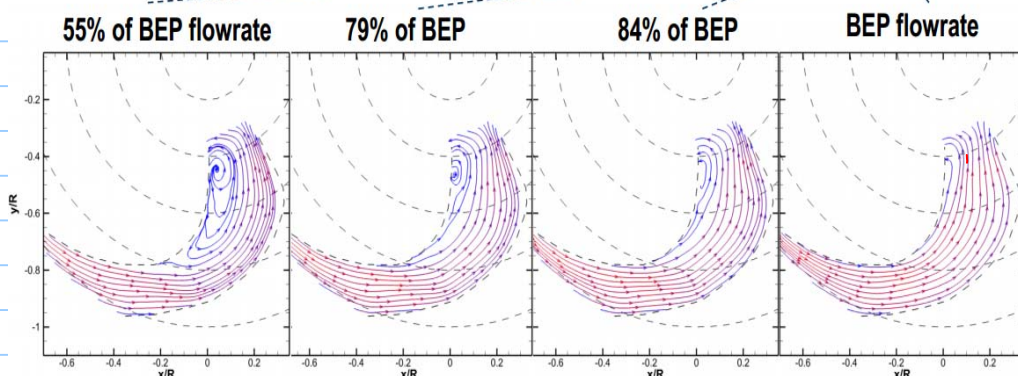
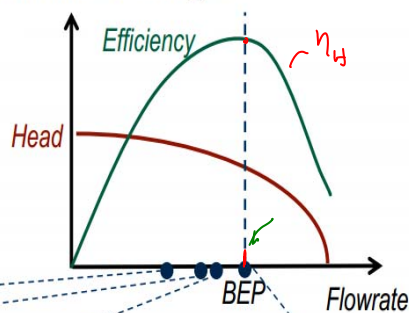
$$P_{pump} = \frac{(P_{dis} - P_{suc}) \cdot q}{\eta_H \cdot \eta_{mech}}$$

local conditions

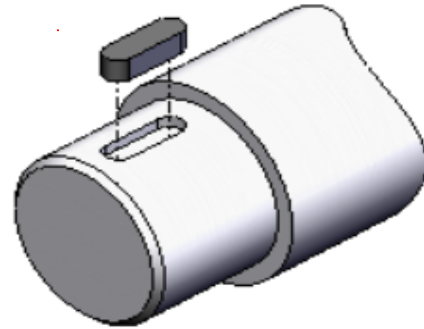
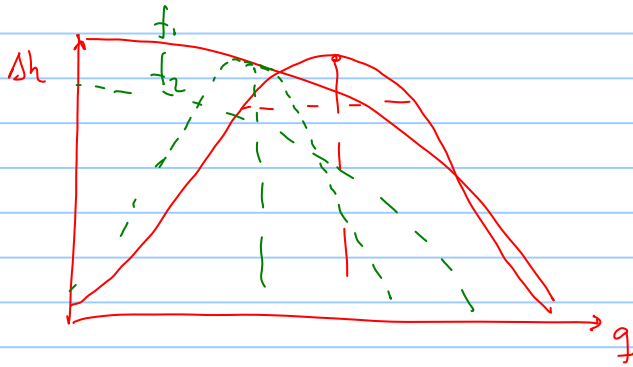
fluid friction

### PIV measurement in a radial flow stage

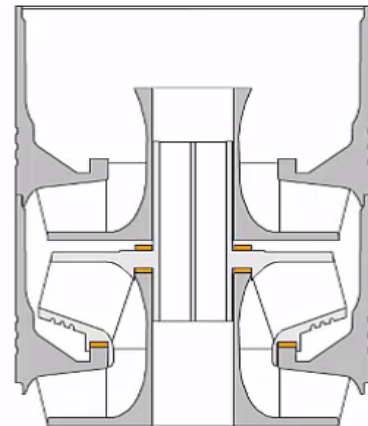
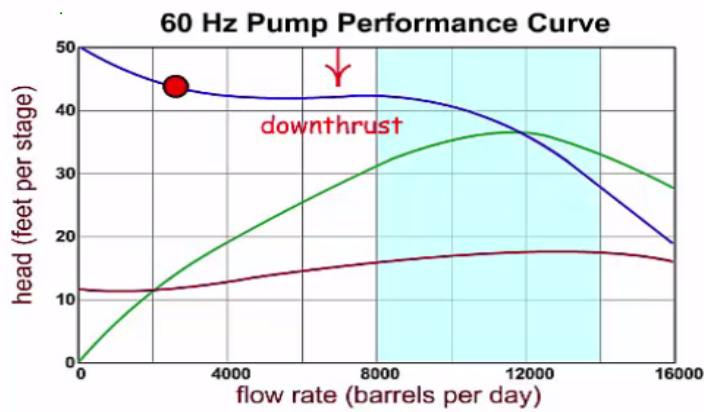
- Flow features in diffuser and impeller may be identified from measurements
- Flow misalignment and recirculations reduce efficiency



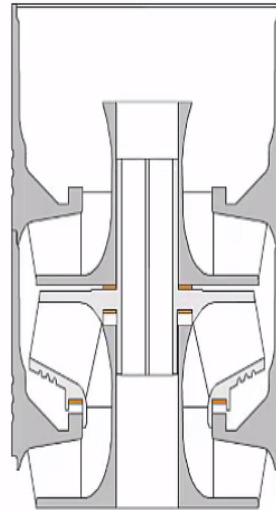
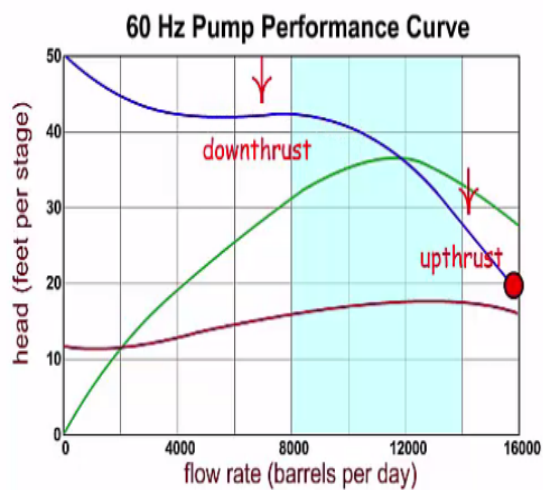
Example of stall region in diffuser passage (measured)



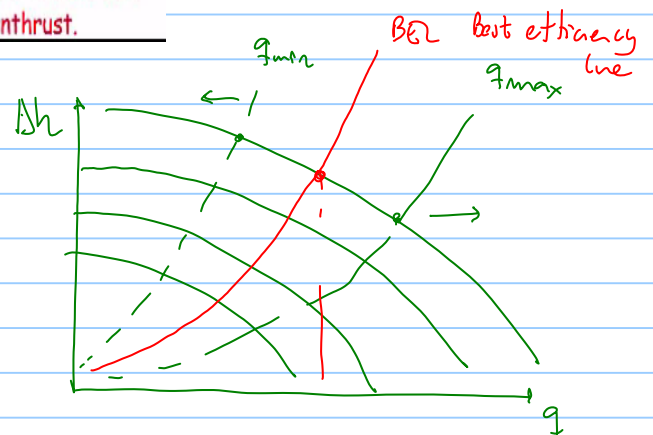
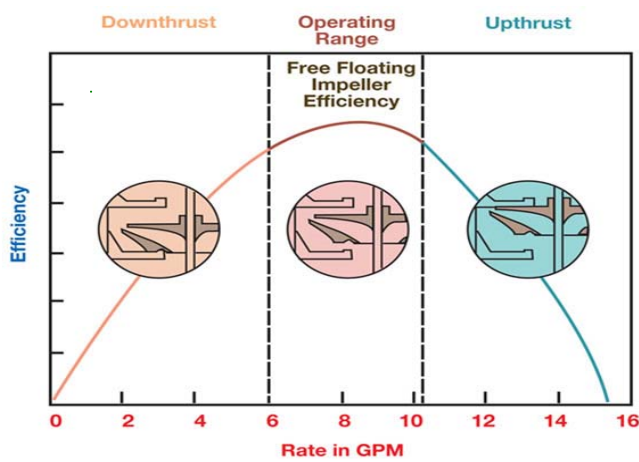
In mechanical engineering, a key is a machine element used to connect a rotating machine element to a shaft.



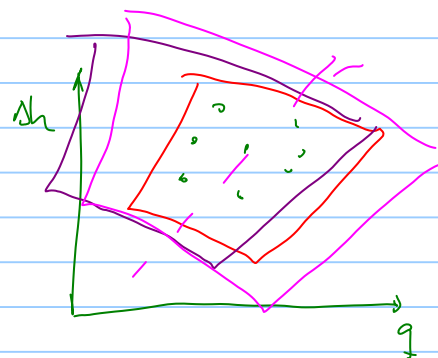
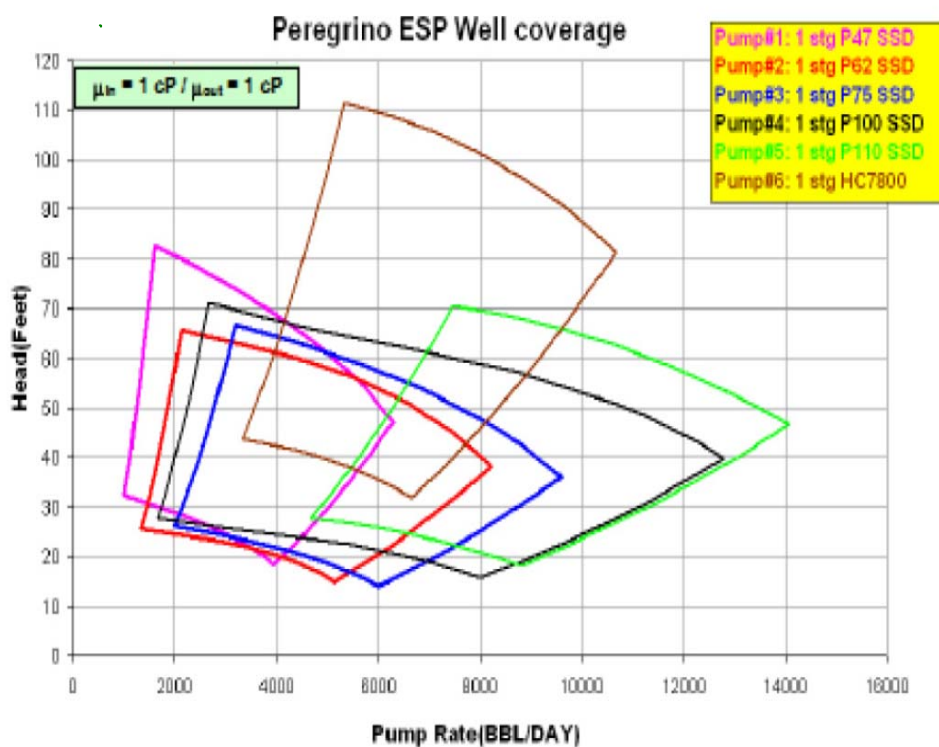
Until it reaches a certain point on the curve where it goes in to downthrust.



It will not go into upthrust at the same point it went into downthrust.



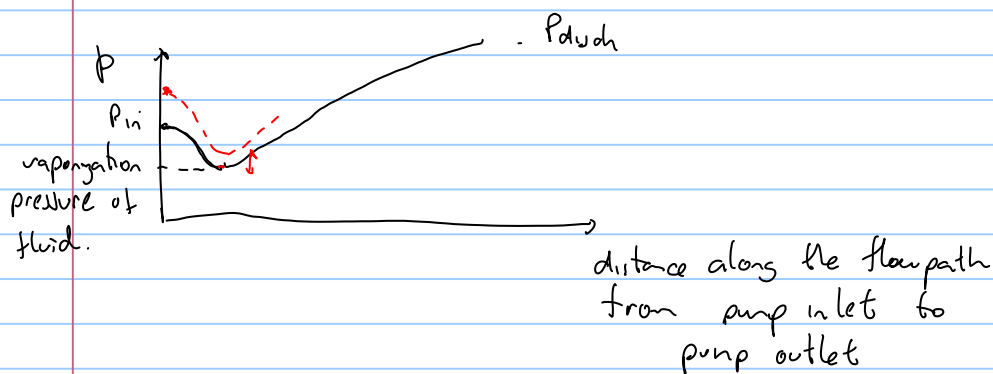




- maximum power capacity of motor (100 hp  $\sim$  1600 hp)

$$P = \frac{\Delta p \cdot q}{\eta_H \eta_m} \leq \text{Power installed}$$

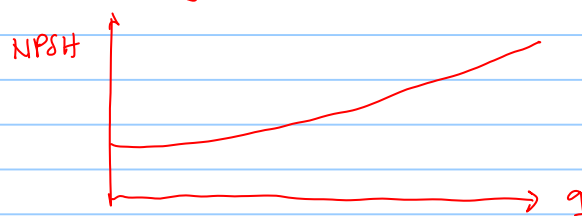
- Cavitation

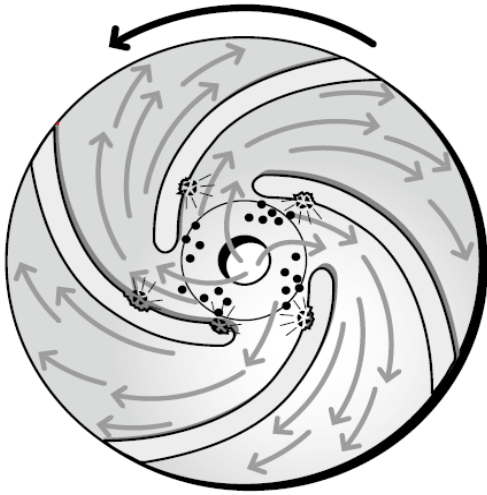


$P_{out} > \text{that } P_{limit}$

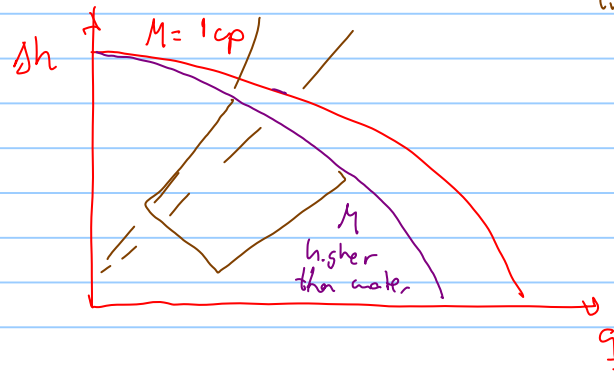
NPSH net positive suction head [m]

(with  $\Delta p$  change to bara)





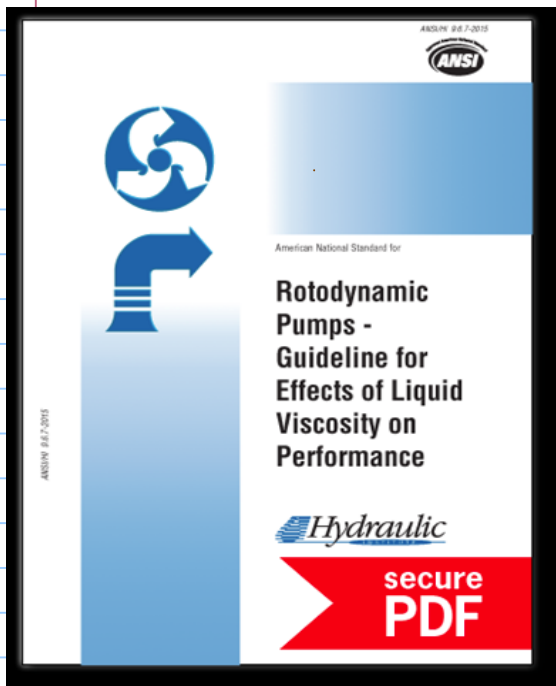
Effect of viscosity

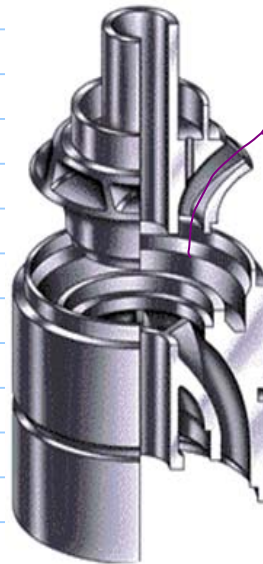
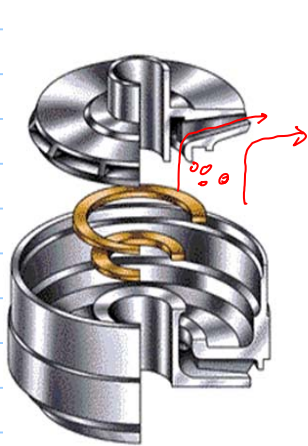


viscosity reduces the operational envelope of pump.!

how to estimate pump performance with viscosity

↳ lab testing  
↳ hydraulic institute method not 100% accurate!



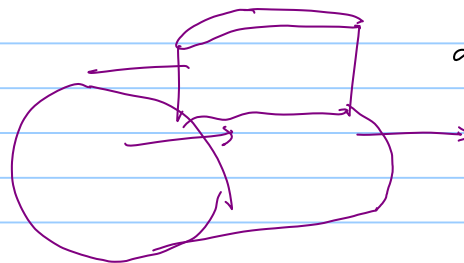
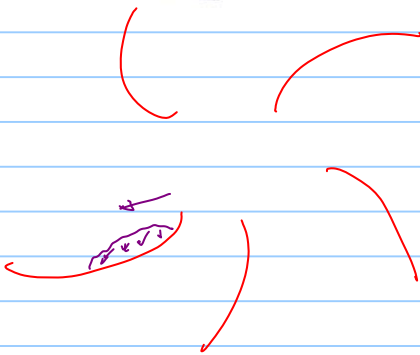


mixed flow  
↳ axial  
radial

$\Delta p$  per stage is  
usually.

very tolerant to gas

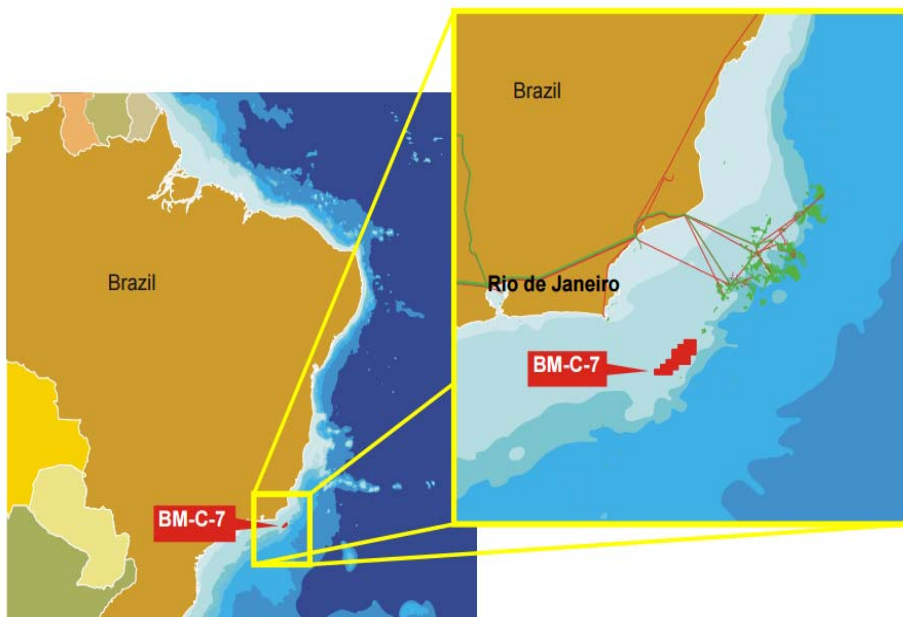
$GVF \approx 10\%$   
gas volume fraction  
↳ actual cond.  
local cond

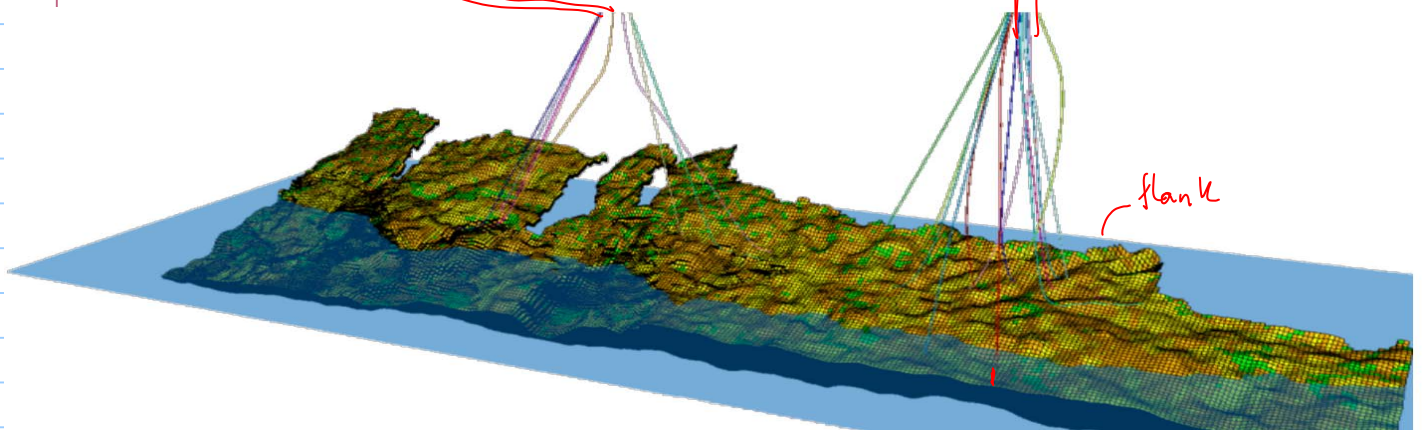
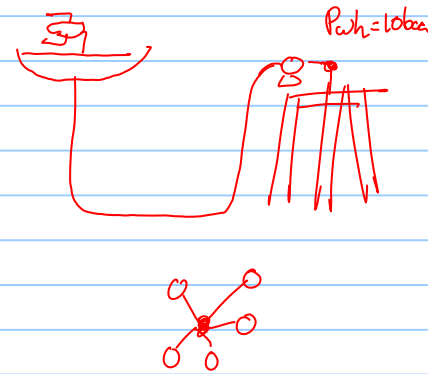
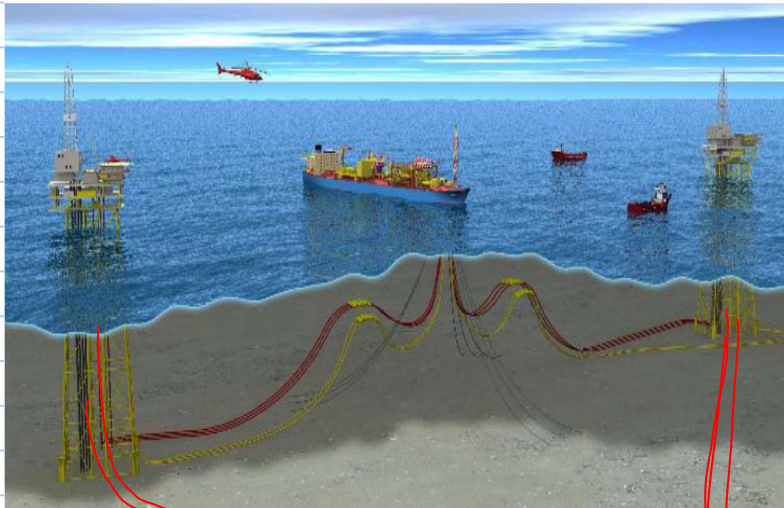


axial impeller, not used  
in ESRs.

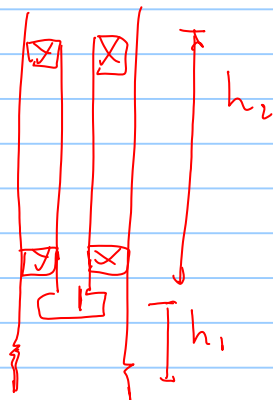
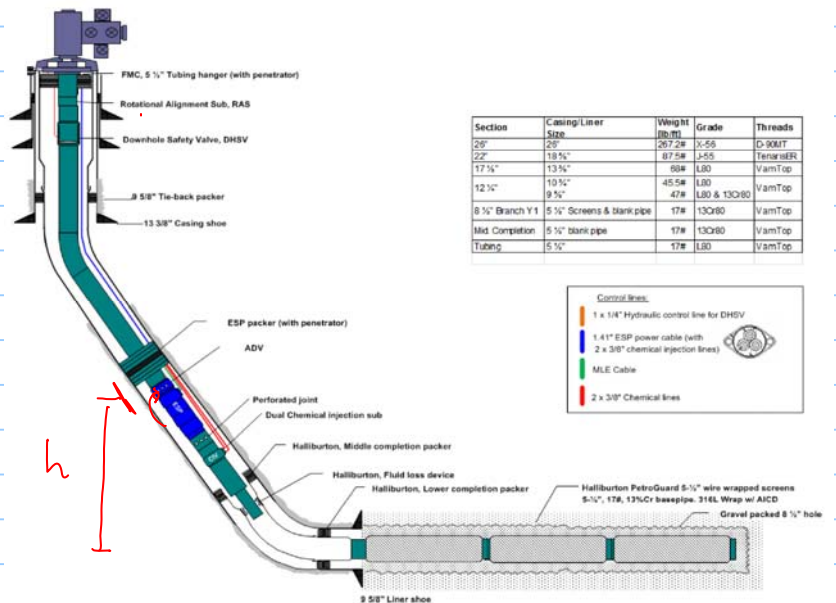
Class exercise  
the Peregrino field:

[http://folk.ntnu.no/stanko/Courses/TPG4230/2017/Class\\_files/20170330/](http://folk.ntnu.no/stanko/Courses/TPG4230/2017/Class_files/20170330/)

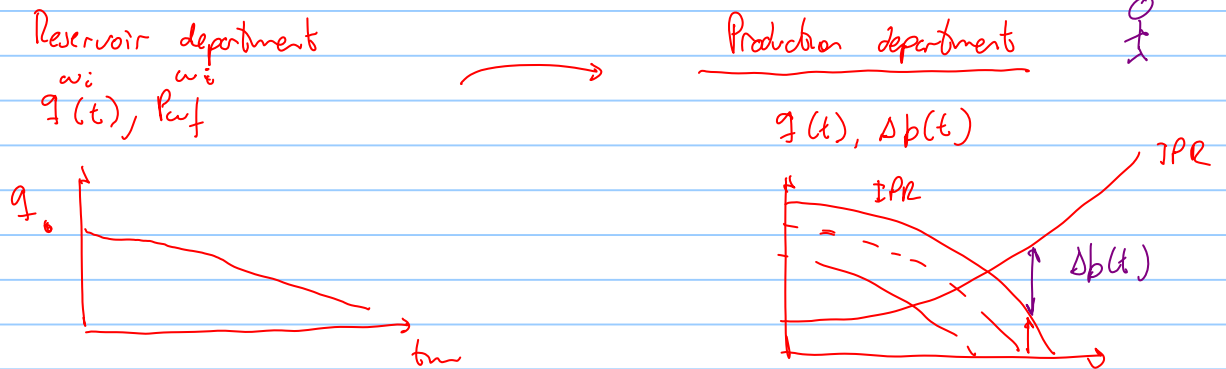




- LQ *living quarters*
- Drilling module
- Movable drill rig
- Electrical plant
- Wellheads
- Booster pumps
- Water Injection
- Uptime 99% bracket



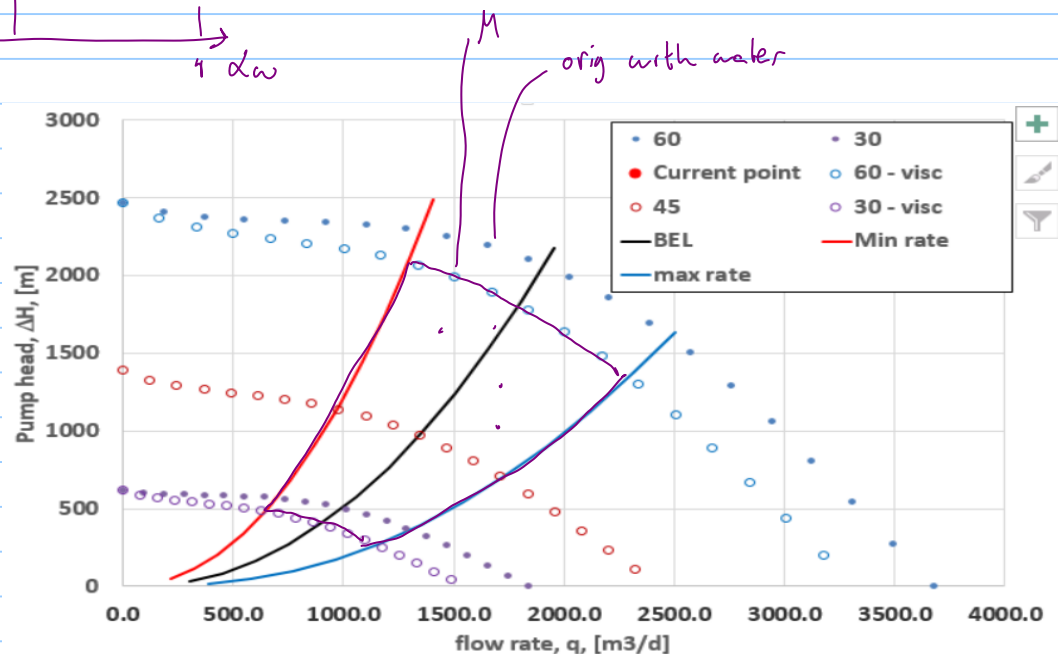
# Design process of ESP for the field lifetime



Find an equipment such that covers  $\Delta p, q(t)$  for most of lifetime with high efficiency not gas at inlet at affordable price

you select an ESP model to produce  $t_1 - t_2$  but you cannot produce in this interval  $t_3 - t_5$

Evolution





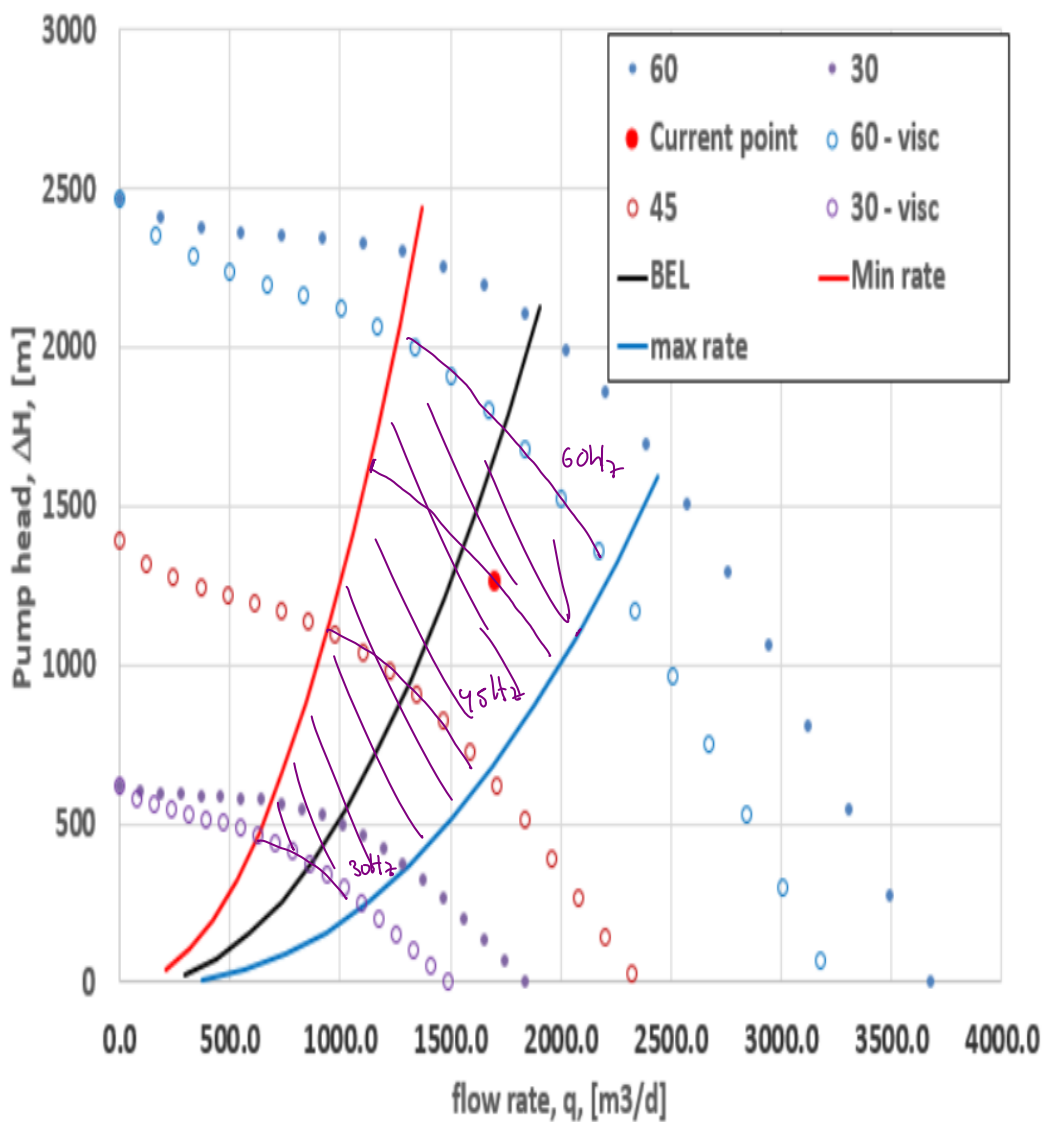
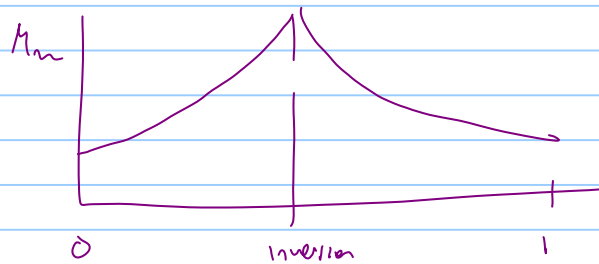
$$f_s = f_o \quad \text{no dissolved gas}$$

$$f_w = f_w$$

$$\frac{f_w}{f_o + f_w} = \frac{f_w}{f_o + f_w}$$

$$f_m = \alpha_w f_w + (1 - \alpha_w) f_o$$

$$M_m = M_{\text{conbre}} e^{c \cdot \alpha_{\text{dispersed}}}$$



$$q = 1700 \text{ m}^3/\text{d}$$

$$\Delta p = 111 \text{ bara}$$

$$\mu = 0.138 \text{ Pa} \cdot \text{s}$$

$$\rho = 910 \text{ kg/m}^3$$

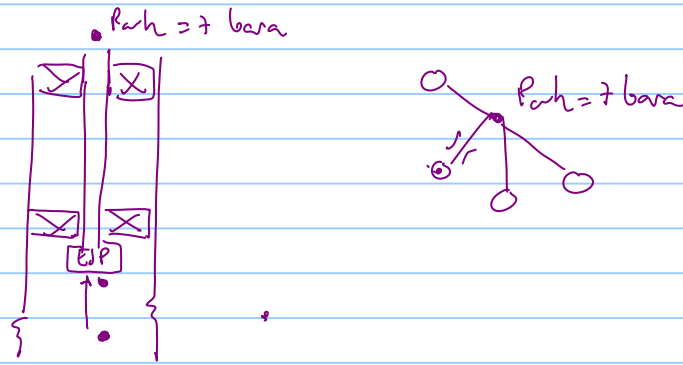
$$f \approx 52.5 \text{ Hz}$$

$$P = \frac{\Delta p \cdot q}{\eta_H \eta_{\text{mech}}}$$





[http://folk.ntnu.no/stanko/Courses/TPG4230/2017/Class\\_files/20170404/](http://folk.ntnu.no/stanko/Courses/TPG4230/2017/Class_files/20170404/)

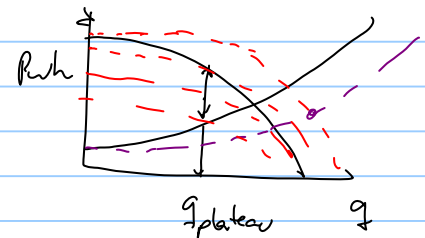


30 [bara]		Required pressure at pump intake										36												Max power [hp]		950	
P <sub>R</sub>	WC	Average density	Effective viscosity	Q <sub>tot</sub>	P <sub>wf</sub>	Q <sub>o</sub>	Q <sub>w</sub>	P <sub>suc</sub>	f	P <sub>disc</sub>	ΔP <sub>ESP</sub>	Δh <sub>ESP</sub>	P <sub>wh calc</sub>	P <sub>wh given</sub>	Hydraulic Effic	Pump power	q <sub>min</sub>	q <sub>max</sub>									
bara	[-]	kg/m <sup>3</sup>	Pa s	Sm <sup>3</sup> /d	bara	Sm <sup>3</sup> /d	Sm <sup>3</sup> /d	bara	[Hz]	bara	bara	m	bara	bara	[-]	[hp]	[m <sup>3</sup> /d]	[m <sup>3</sup> /d]									
231	0.10	910	0.138	1700	110	1530	170	75.7	53.0	188	113	1264	7.0	7	0.452	658.6	1121	1994									
215	0.10	910	0.138	1700	94	1530	170	59.6	55.3	188	129	1445	7.0	7	0.455	748.5	1169	2079									
200	0.10	910	0.138	1700	79	1530	170	44.6	57.4	188	144	1613	7.0	7	0.456	833.4	1213	2156									
175	0.10	910	0.138	1470	70	1323	147	36.0	56.5	187	151	1693	7.0	7	0.438	786.6	1194	2124									
150	0.10	910	0.138	1120	70	1008	112	36.0	54.1	185	149	1673	7.0	7	0.401	647.4	1144	2033									
125	0.10	910	0.138	771	70	694	77	36.0	52.5	184	148	1656	7.0	7	0.344	513.3	1110	1973									

Singh, B2 Tanzania what can we do to prolong plateau?

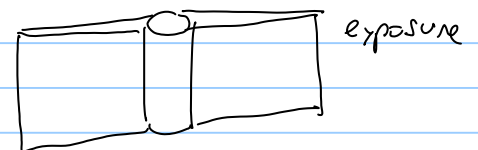
- increase available pressure  $P_{wh avail}$
- decrease required pressure  $P_{wh req}$

methods to increase available pressure:



•  $q = \frac{C_R}{2\pi} (P_R^2 - P_{wf}^2)^n$  Increase reservoir deliverability: acidizing  
injecting chemical to improve permeability of near wellbore region

• Fracturing. increase wellbore formation exposure



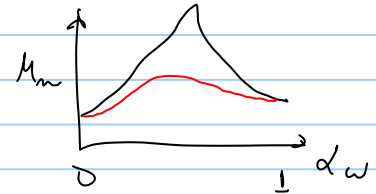
• multi-laterals  
• multi-layer (activate in another segment)

• Inflow control devices.  
reduce the flow of other phases that affect the flow of the main phase

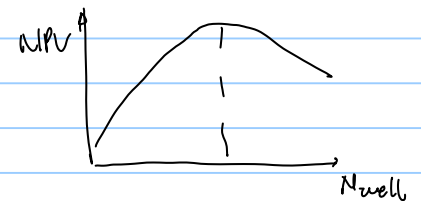
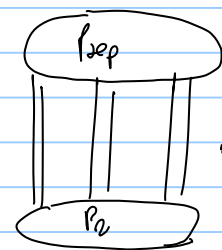
- pressure support in reservoir: water injection, gas injection \$

- tubing:
  - increase tubing ID
  - install artificial lift
    - ESP
    - PCP
    - jet pump

- reduce  $\mu$  of fluid  $\rightarrow$  demulsifiers
  - ↘ solvent
  - ↘ lister API
  - oil

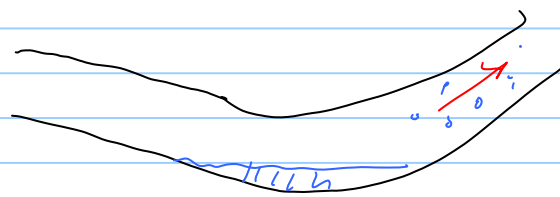


- increase the number of wells



reducing required pressure

- changing size (ID) of transportation flowlines and pipelines  $\uparrow ID \uparrow \$$



WARNING! Be careful with liquid accumulation in gas/liquid flow.

- a parallel pipeline !
- reduce  $\mu_m \rightarrow$  inject demulsifier solvent.

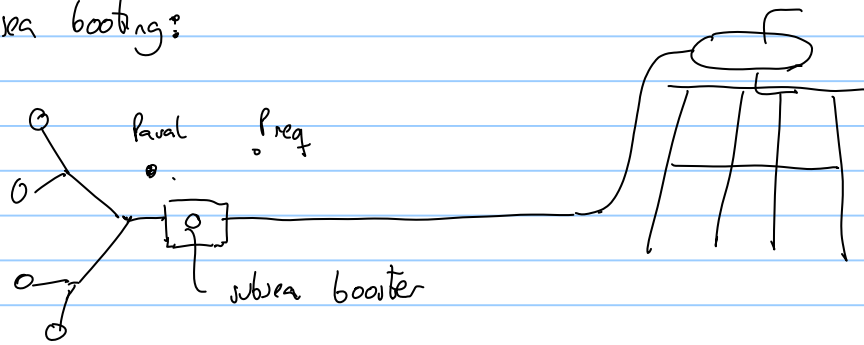
- reduce separator pressure



Change  
~ big change in topside / processing facilities

- subsea processing: separation of oil, gas, water to avoid unnecessary transportation losses. from seabed to topside

## • Subsea boosting:



2 types of booster : • single phase liquid, gas  $\rightarrow$  requires separation before  
• multiphase  $\rightarrow$  oil, gas, water

## two types of boosting principles

### Positive displacement

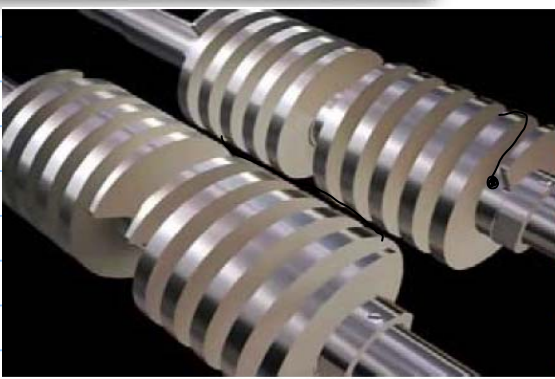
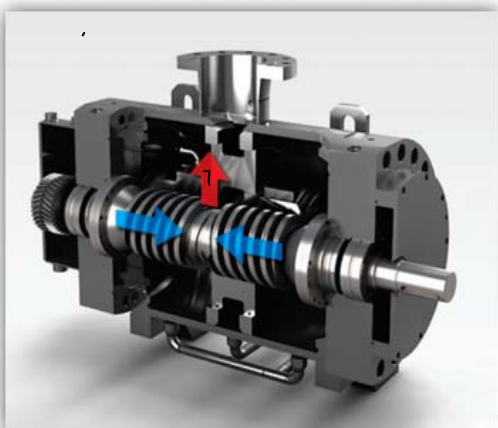
- gives higher  $\Delta P$
- don't tolerate solids
- lower rates

### Rotodynamic

- gives medium  $\rightarrow$  low  $\Delta P$
- have some tolerance to solids.
- medium and high rates.

## multi-phase boosters

### twin screw pump



### HAP helico-axial pump.

Framo. OneSubsea



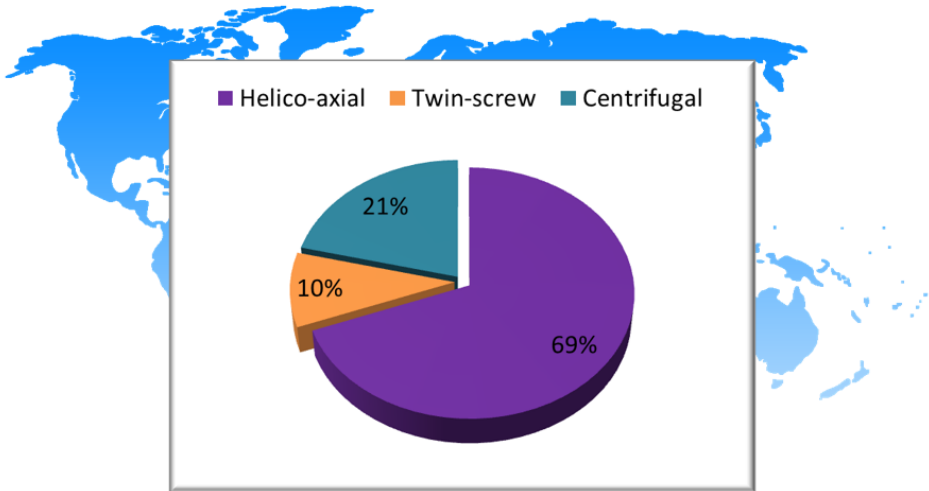
(a) Impeller



(b) Diffuser

# Subsea multiphase boosting around the world

52 subsea pumps in 23 locations in the World



From <http://www.offshore-mag.com/>

Wet gas compressor  $\rightarrow$  lots of gas with some liquid.   
*gas-liquid mixture is possible to model it as a single fluid with average properties.*   
*counter-rotating wet gas compressor.*

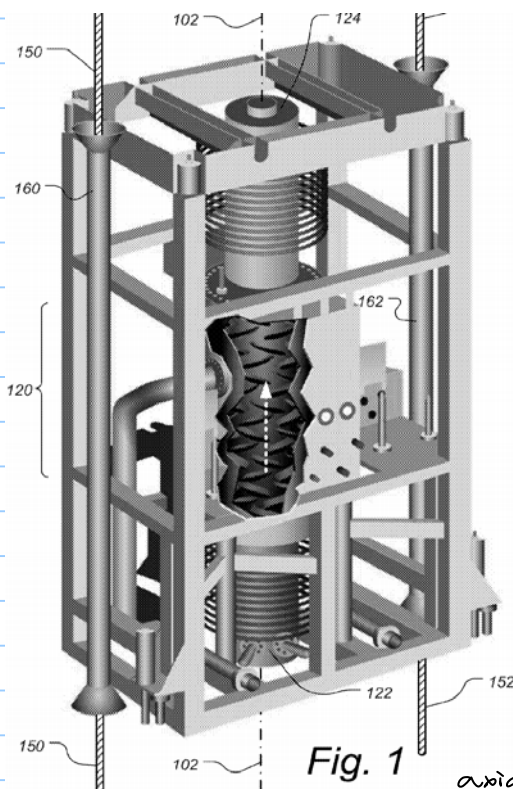
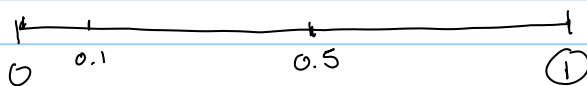


Fig. 1

axial impellers { HAP  
WGC

mixed flow



radial centrifugal impellers  $\rightarrow$  high  $\Delta P$

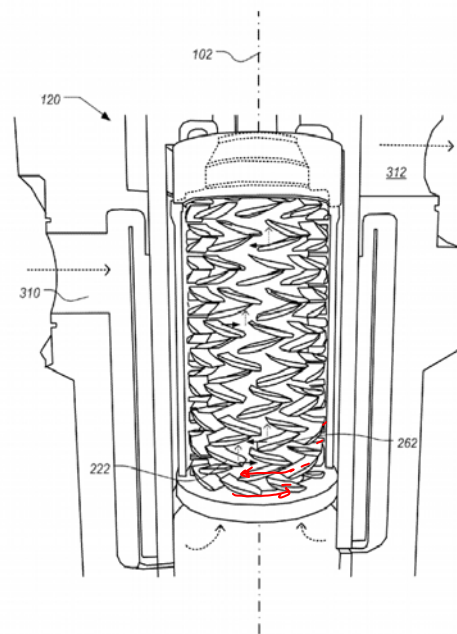


Fig. 3A

gives a lower  $\Delta P$

*usually requires more stages than centrifugal for same  $\Delta p$*

GVF gas volume fraction

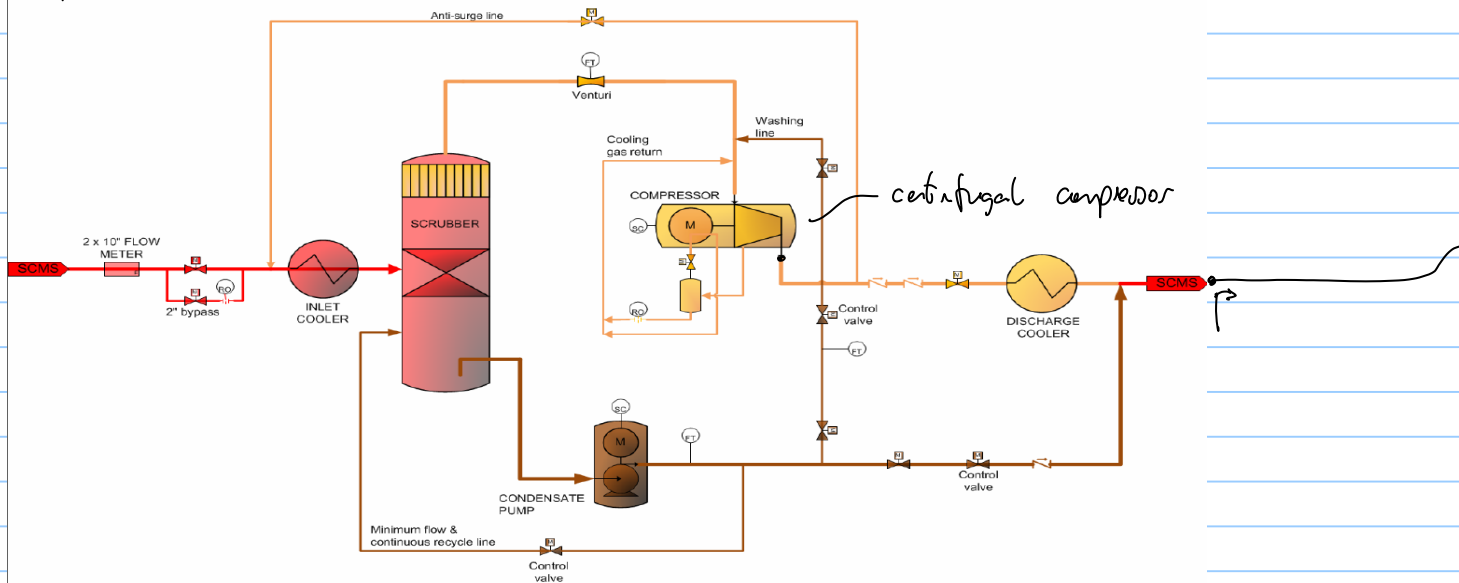
$$g_g$$

$$g_o + g_w + g_g$$

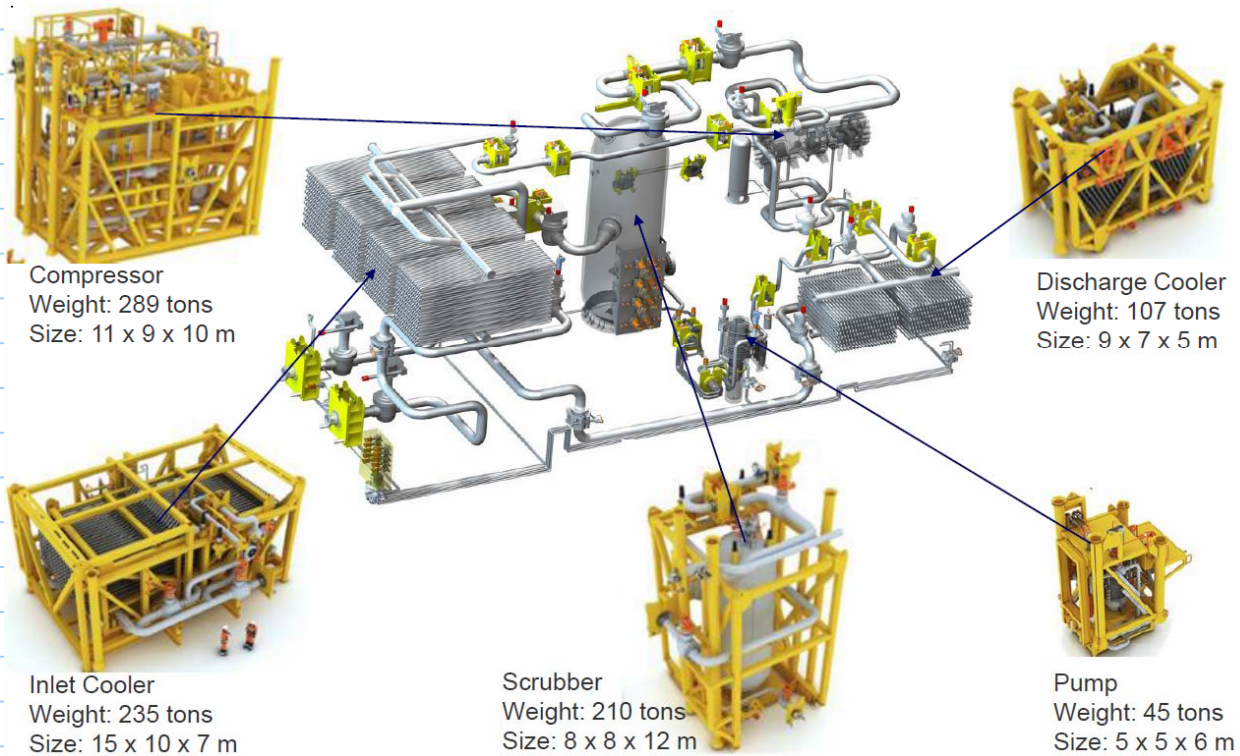
@ local conditions better inlet

Single phase subsea boosters → separation before! Aasgard subsea compression dry compressor + separation station

## Process Flow Diagram



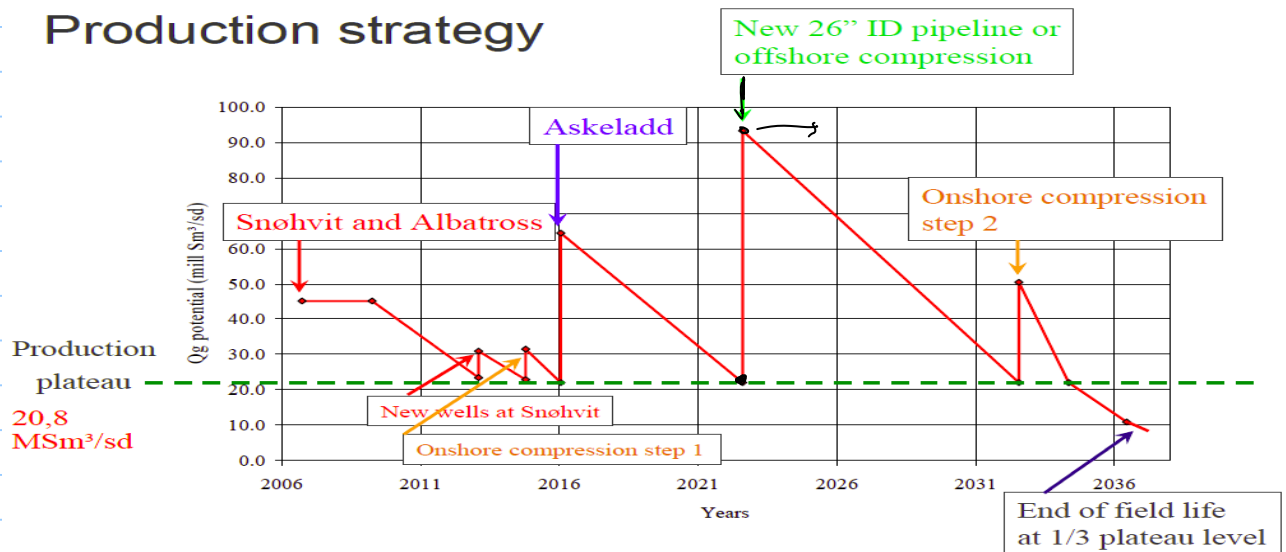
## Process Modules- Sizes and Dry Weights



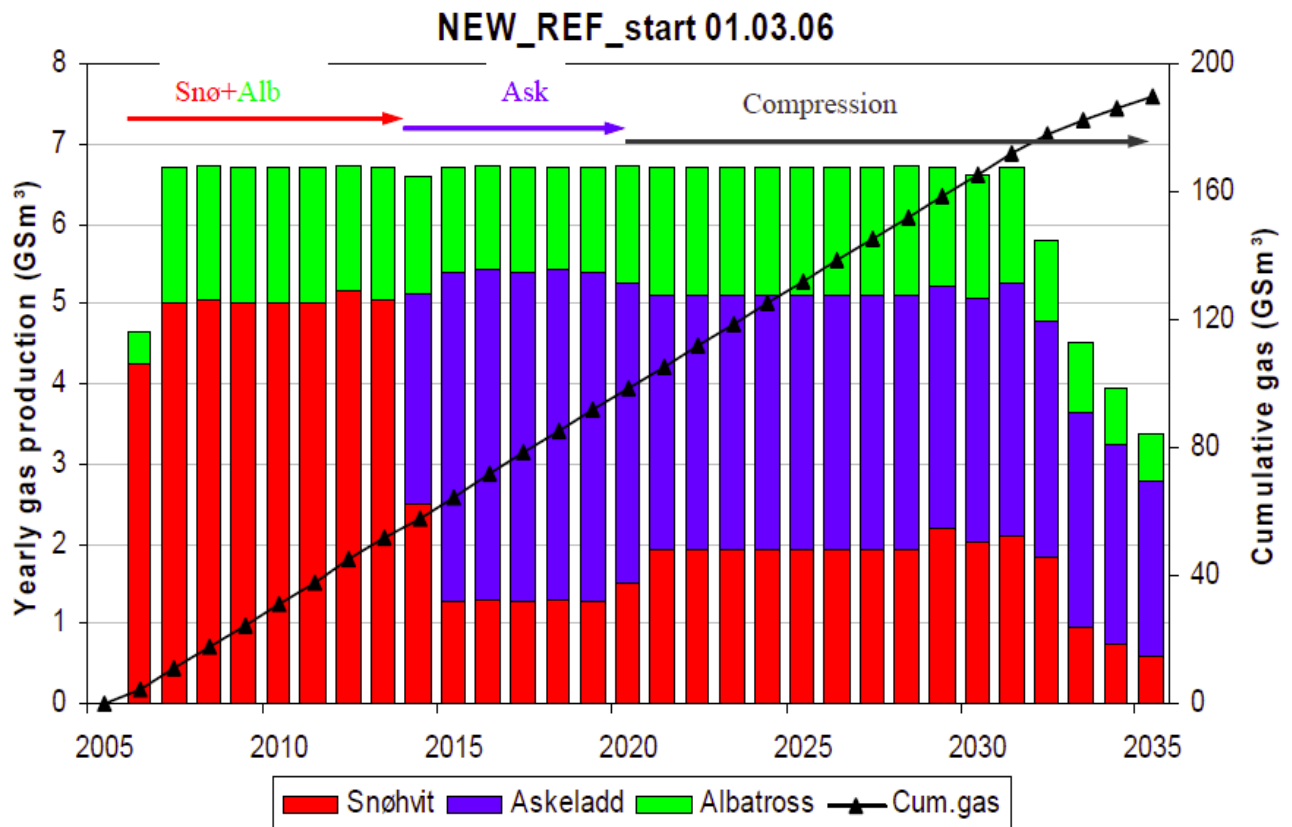


In particular, the Snøhvit field:

## Production strategy



## Production profile (20,8mill. Sm³/sd – 6,7 GSm³/år)

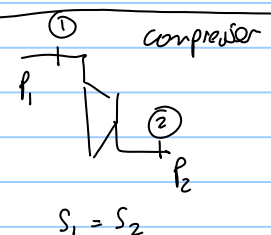


Refreshment in compressors

if I compress ideally:

$$\tilde{T}_{2s} = \left( \frac{p_2}{p_1} \right)^{\frac{\kappa-1}{\kappa}} = r_p^{\left( \frac{\kappa-1}{\kappa} \right)}$$

$$\kappa = \frac{C_p(T)}{C_v(T)} = \kappa f(T)$$



in reality the process is not isentropic!

the compression process is represented using a polytropic expansion

$$\frac{T_2}{T_1} = \left(\frac{P_2}{P_1}\right)^{\frac{n-1}{n}}$$

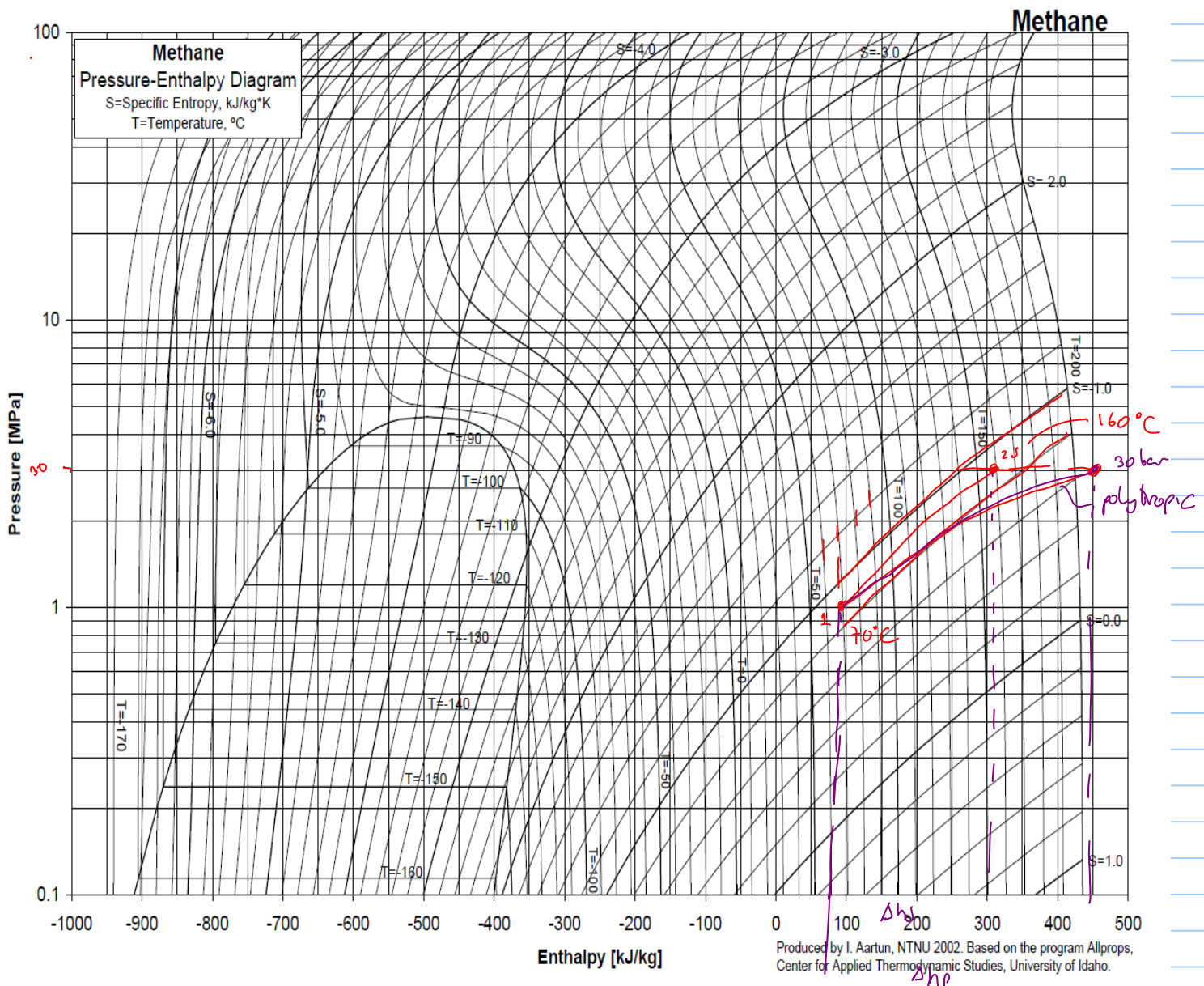
$$P V^n = \text{const}$$

polytropic exponent

the real compression power required is given by:

$$2 \phi \underbrace{(T_2 - T_1)}_{\text{for liquids}} = h_2 - h_1$$

$$P_{\text{comp}} = \frac{\dot{m}' \Delta h_p}{\underbrace{\eta_p \eta_m}_{\left(\frac{n-1}{n}\right) = \left(\frac{\kappa-1}{\kappa} \eta_p\right)}} = \frac{\dot{m}}{\eta_p \eta_m} \cdot \underbrace{z_{\text{av}} \cdot \bar{R} \cdot \frac{n}{n-1} \left(\left(\frac{P_2}{P_1}\right)^{\frac{n-1}{n}} - 1\right) T_1}_{\substack{\Delta h_p \rightarrow \bar{R} = \frac{R_u}{M_{\text{gas}} \\ z_1 + z_2 \\ 2}}}$$

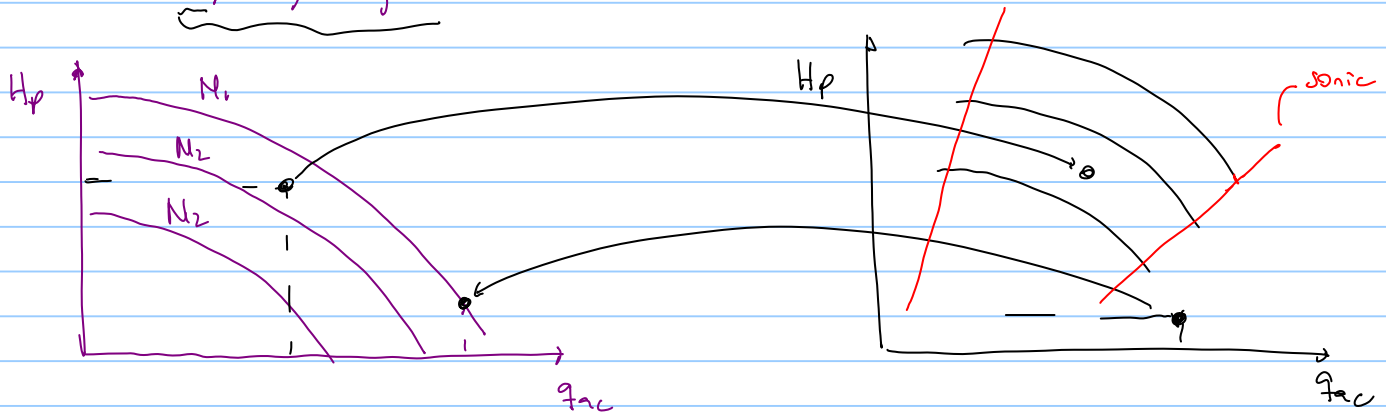




$$H_p = \frac{\Delta h_p}{g} \approx \text{polytropic head}$$

$$\text{for } P_1^*, T_1^*, \dot{m}_w^*, k^*$$

test the compressor at  $P_1 = 1.01325 \text{ bar}$   
 $T_1 = 15.56^\circ\text{C}$   
 $\dot{m}_w = 20.97$   
 $k = 1.3$ ?



to calculate compressor performance for other conditions different than test  
 apply the following corrections:

$$q_{act} = q_{test} \sqrt{\frac{k_{ac}}{k_{tes}}} \cdot \sqrt{\frac{\dot{m}_{w,tes}}{\dot{m}_{w,ac}}} \cdot \sqrt{\frac{T_{ac}}{T_{test}}} \quad q_{test}$$

$$H_p^{corrected} = \frac{\dot{m}_{w,tes}}{\dot{m}_w} \cdot \frac{T_1}{T_{1,tes}} \cdot \frac{k}{k_{tes}} \cdot H_p^{test}$$

Compressors constraints:

- discharge  $T \leq 150^\circ\text{C}$ 
  - integrity pipeline
  - avoid vaporization glycol hydrate inhibitor
  - avoid damaging compressor seals

another assumption

$$\eta_p = \text{const} \approx 0.7$$

in reality

$$\eta_p = f(q_{act})$$

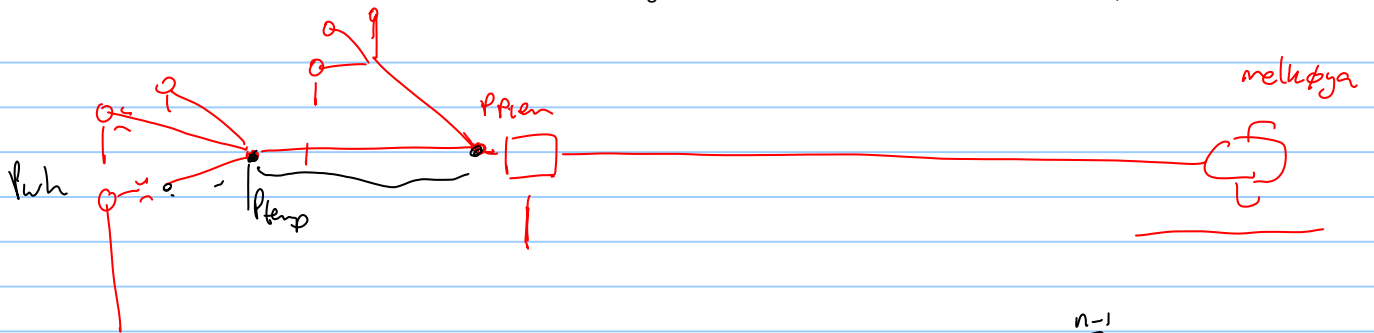
$$\text{Power} \leq P_{max} (11 \text{ MW})$$

- $P_{suc} \geq 10 \text{ bar}$ 
  - to activate seals
- operational speed 9350 - 6800 rpm

$$q_{min} \leq q \leq q_{max}$$

surge.  $\left\{ \begin{array}{l} \text{flow} \\ \text{back and forth} \\ \text{in machine} \\ \text{(unstable)} \end{array} \right.$

$\rightarrow$  sonic velocity in machine passages  $M = 1$



estimate  $T_{outlet}$   $\frac{T_2}{T_1} = r_p^{\frac{n-1}{n}}$

estimate  $\Delta h_p = c_{p,air} \cdot \bar{R} \cdot \frac{n}{n-1} \left( r_p^{\frac{n-1}{n}} - 1 \right) \dot{T}_1$

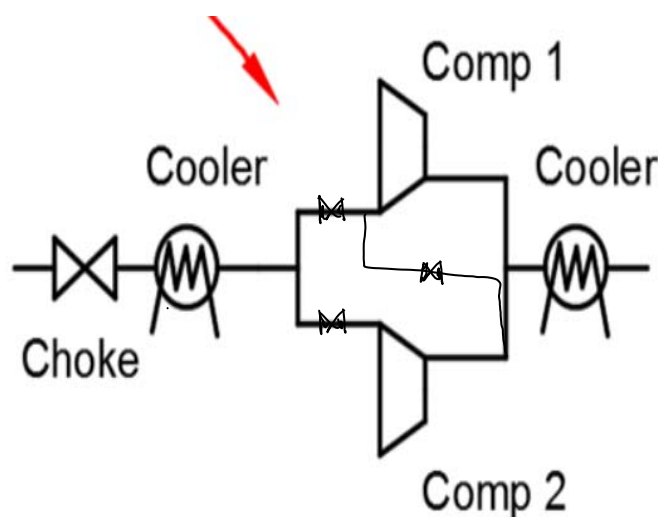
calculate  $H_p = \frac{\Delta h_p}{g}$   $\frac{8314 \text{ J}}{\text{kg} \cdot \text{K}} \cdot \frac{\text{K}}{\text{kg} \cdot \text{K}} \cdot \text{K}$

calculate  $q_{act} = B_0(P,T) \cdot T_{sc}$   $\frac{\text{J}}{\text{kg}}$

$B_0 = z \frac{T}{T_{sc}} \frac{P_{sc}}{P}$

$H_p, q_{act} \rightarrow$  convert to test conditions  
plot in compressor map.

- chane at inlet reduce even more available pressure
- cool fluid upstream ( $30^{\circ}\text{C } \Delta T$ )
- cool fluid downstream ( $30^{\circ}\text{C } \Delta T$ )
- decide to use single or two compressors
- To reduce ratio

[illegible]

- Production optimization :
  - increase oil or gas production
  - Reduce cost
  - by using cost effective measures

In the industry, typical activities performed in optimization are:

- Detect pipe section, component with high  $\Delta p$ .  $\left\{ \begin{array}{l} \text{too small size} \\ \text{blockage} \end{array} \right.$
- Verify design conditions of equipment vs actual operating conditions.
- Study and analyze maintenance, installation, testing logistics, detect deficiencies, problems and take measures.
- Identify sources with non attractive characteristics ( $H_2S$ ,  $wC$ ), and limit their production
- Review failure data and detect patterns
- Identification <sup>and address</sup> of operational constraints or bottleneck.
- calibration of instrumentation
- identifying and monitoring KPIs  
key performance indicators



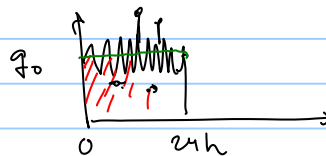
- ① → • find settings of adjustable elements that give the maximum revenue and satisfy the multiple operational constraints.

mathematical procedure that can guarantee optimality.

tools used to perform optimization: • historic data (reported)

> 1000 sensors

- look at more frequent data



- instrumentation
- experience from field operators.
- numerical models.

Formal-mathematical  $\rightarrow$  Production optimization

short term

• min  $\rightarrow$  weeks(is neglects time)  
effect, steady state

• real-time production optimization

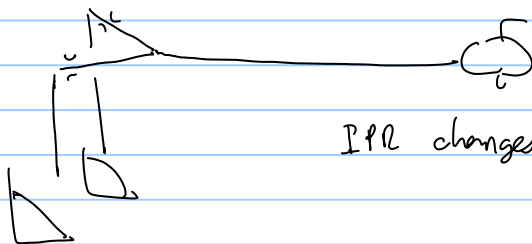
• gas-lift allocation  $\leftarrow$  gas lift rate• routing  $\leftarrow$  open or close valve• ESP systems  
(chase +)

• processing opt.

long-term

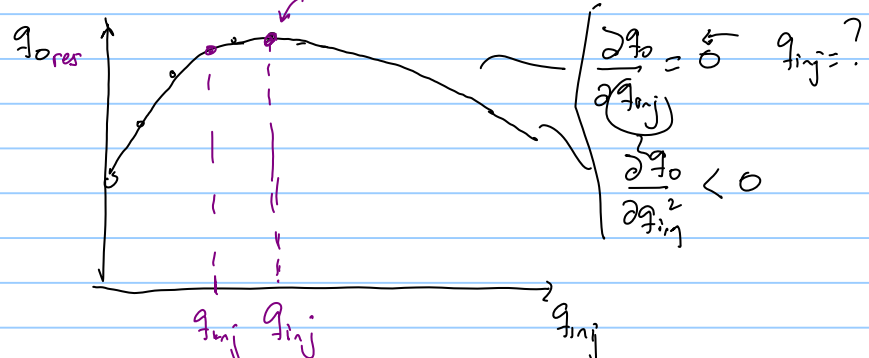
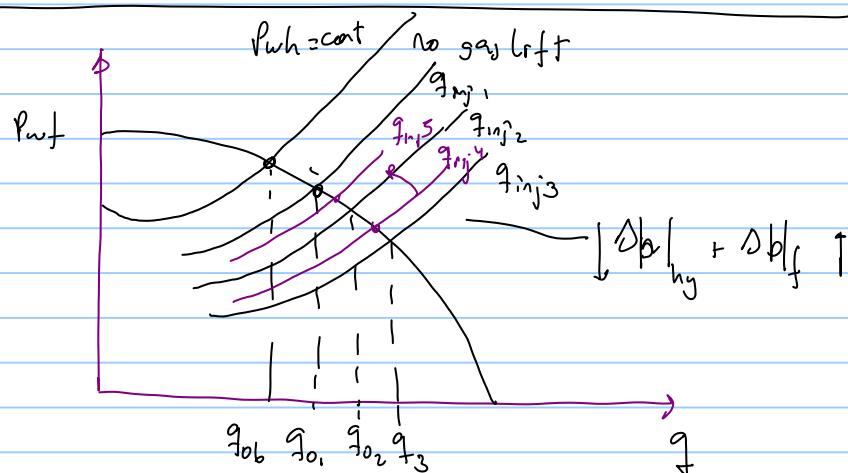
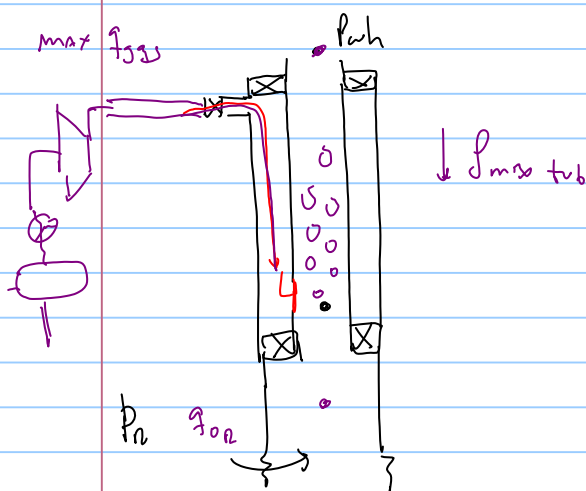
month  $\rightarrow$  years $i$  - nr well• reservoir  
controlfind  $q_o(t)$ that gives max NPV  
max RFconsidering the time  
effect in a long  
time scale

• well placement



IPR changes with time

//

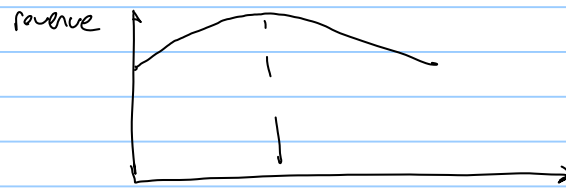
operational constraints have to be  
taken into account when performing  
optimization

- gas capacity
- water processing capacity
- gas processing capacity

maximize this optimization on revenue

- gas coning
- water coning
- sand production
- power consumption
- erosion

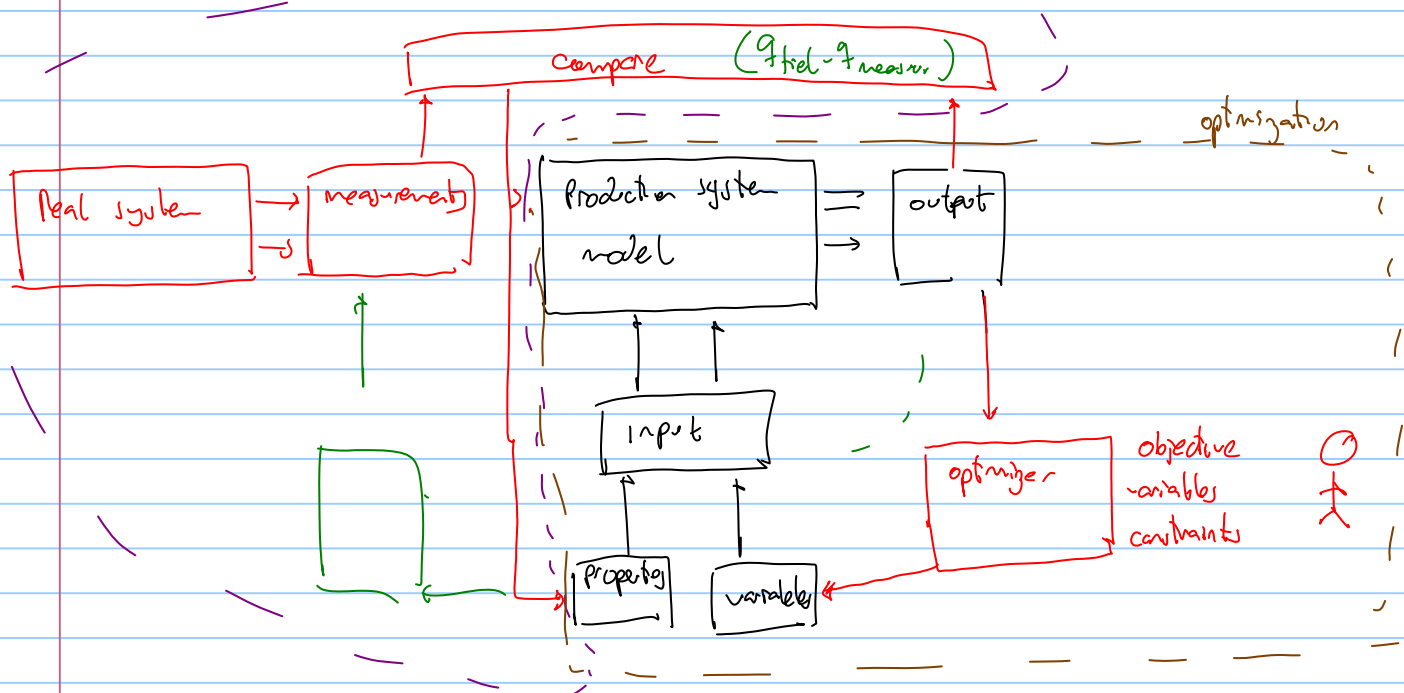
$$\text{revenue} = q_o \cdot P_o - q_g \cdot P_w \quad \text{or} \quad \text{revenue} = q_o \cdot P_o - \frac{\text{cost} \cdot \text{power}}{\text{eff}}$$



An optimization problem consists on 3 things

- objective  $\rightarrow \begin{cases} \text{max} \rightarrow q_o, q_g, RF, MPV \\ \text{min} \rightarrow \text{cost}, q_w, \text{downtime}, \text{etc} \end{cases}$
- variable  $\left\{ \begin{array}{l} \text{chose position, well placement} \\ \text{gas lift rate} \\ \text{pump frequency} \\ \text{well rating} \end{array} \right\}$  only the essential
- constraint  $\left\{ \right.$

for optimization we use numerical models  
data assimilation



How is optimization performed?

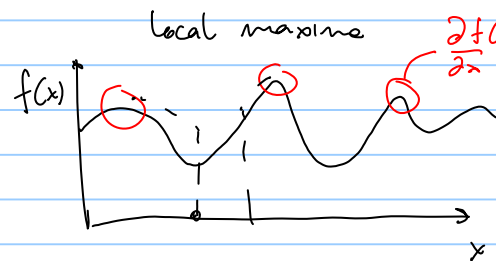
- perform single or multiple evaluations of model for different input conditions
- estimating the next set of input conditions that you want to evaluate (algorithm).
- checking if the stopping criteria is met.

there are different types of optimization problems

- variable type  $\rightarrow$  continuous  
 $\rightarrow$  integer

- constraints: constrained  
or unconstrained

- linear vs non linear



run multiple starting points and verify that the solution doesn't change.

there are different methods to perform optimization:

- gradient based (derivative based)

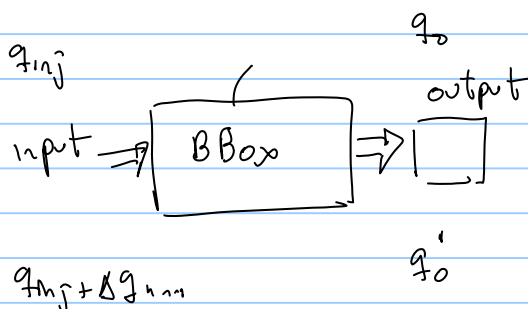


- move in the direction of gradient

Newton-Raphson type method

$$\left\{ \frac{\partial f}{\partial x} \right\} \quad \left\{ \frac{\partial^2 f}{\partial x^2} \right\}$$

$$F(x_1, x_2, x_3, \dots, x_n)$$



for black box models  $\frac{\partial f}{\partial x}$  is estimated numerically  
no access to equations

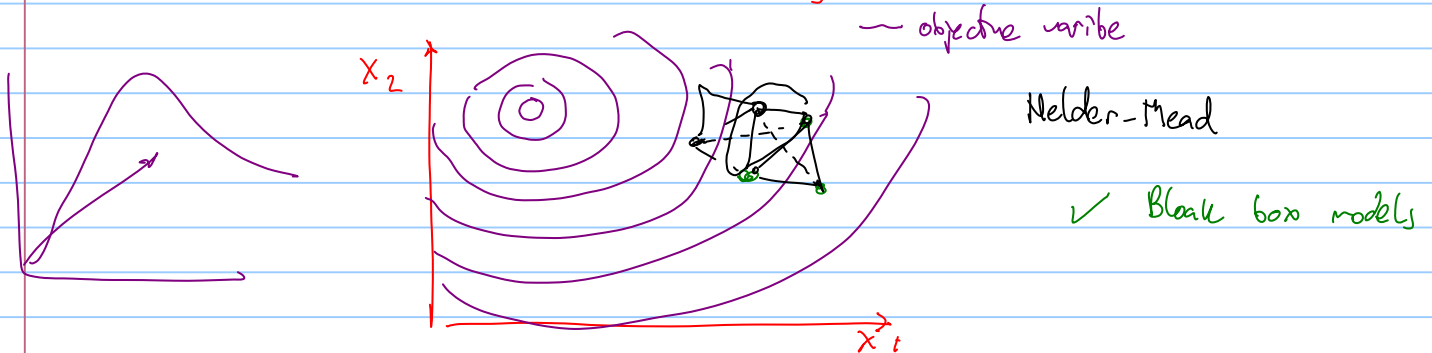
$$\frac{\partial f}{\partial x} \approx \frac{f(x + \Delta x) - f(x)}{\Delta x}$$

- for many variables is a prohibitive approach

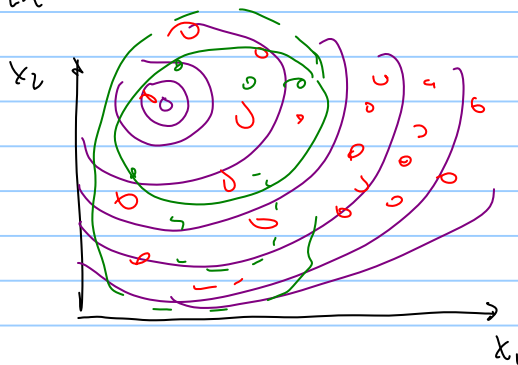


- quick convergence

- heuristic methods. Some logic to chose the next point from the existing evaluations



- Evolutionary methods. evaluate a group of individuals. Select those who performed best and estimate new set of individuals
- genetic algorithm



to evaluate a whole population.

last class 20.04.2017 !

Life cycle of a hydrocarbon field	Appreciation	NO	-	-
Field development workflow - Probabilistic reserve estimation - Cost estimation and NPV calculations	Appreciation/ configuration/ design	YES	Gant chart, NPV calculations, Spider plot, decision trees, Monte Carlo simulation, basic probability, tornado chart	Excel VBA
Offshore (and some onshore) field architectures and layout of production systems - Production manifold - Pigging facilities	Configuration	YES	Engineering diagrams and drawings.	-
Offshore structures for oil and gas production - Wave statistics - Loads	Configuration/ design	YES	Fast Fourier Transform for signal analysis. Probability distributions.	Excel VBA
Reservoir depletion and field performance - Production potential - Production scheduling - Flow equilibrium in production systems, choking and boosting - Flow performance of surface and downhole production networks	Design	YES	Flow in porous media. Material balance. Single and multiphase flow in conduits. Flow equilibrium	Excel VBA, Gap, Prosper, Mbal
Production Processing - Overview	Appreciation, Design	YES	Flash calculations and PVT behavior	Hysys, Excel VBA
Flow assurance - Modeling of gas and condensate transport in pipeline and hydrate formation - Simplified modeling of oil and water emulsions	Appreciation, Design	YES	Pressure and temperature drop in flowlines and pipelines	Hysys, Excel VBA
ESP fundamentals, design and plan for the field life	Design	YES	Pump performance. Operational constraints.. Production system analysis	Excel VBA
Early subsea boosting planning	Design	YES	Compressor performance. Operational constraints.	Excel VBA
Data management and allocation	Appreciation/ design	YES	Data analysis, filtering, QC, averaging, aggregating.	Excel VBA
Production optimization.	Design	YES	Basics on practical and mathematical optimization.	Excel VBA
Integrated asset modeling	Appreciation	NO	-	-
Generic skills exercised			Modeling, Analysis, Problem solving, critical thinking, Excel skills, Excel etiquette, programming	
Additional skills gained by home and class exercises			Group work. Develop written and oral engineering communication skills.	

1.

solver  
solver

Spring	Written examination	60/100	C	2017-05-15	09:00	13:00
Spring	Work	40/100				

ex 1      60  
• 40 exercise       $\frac{60 \cdot 8}{100} +$   
• 60 exam

Content

- covered in class !
- topics covered in the exercises !, class exercises !
- additional material
  - Compendium
  - offshore structures write-up
  - FD of Arta Hamskeen field

