

for more detailed economical calculations → Petroleum Economics Tryave-Strøm (TPG5110)

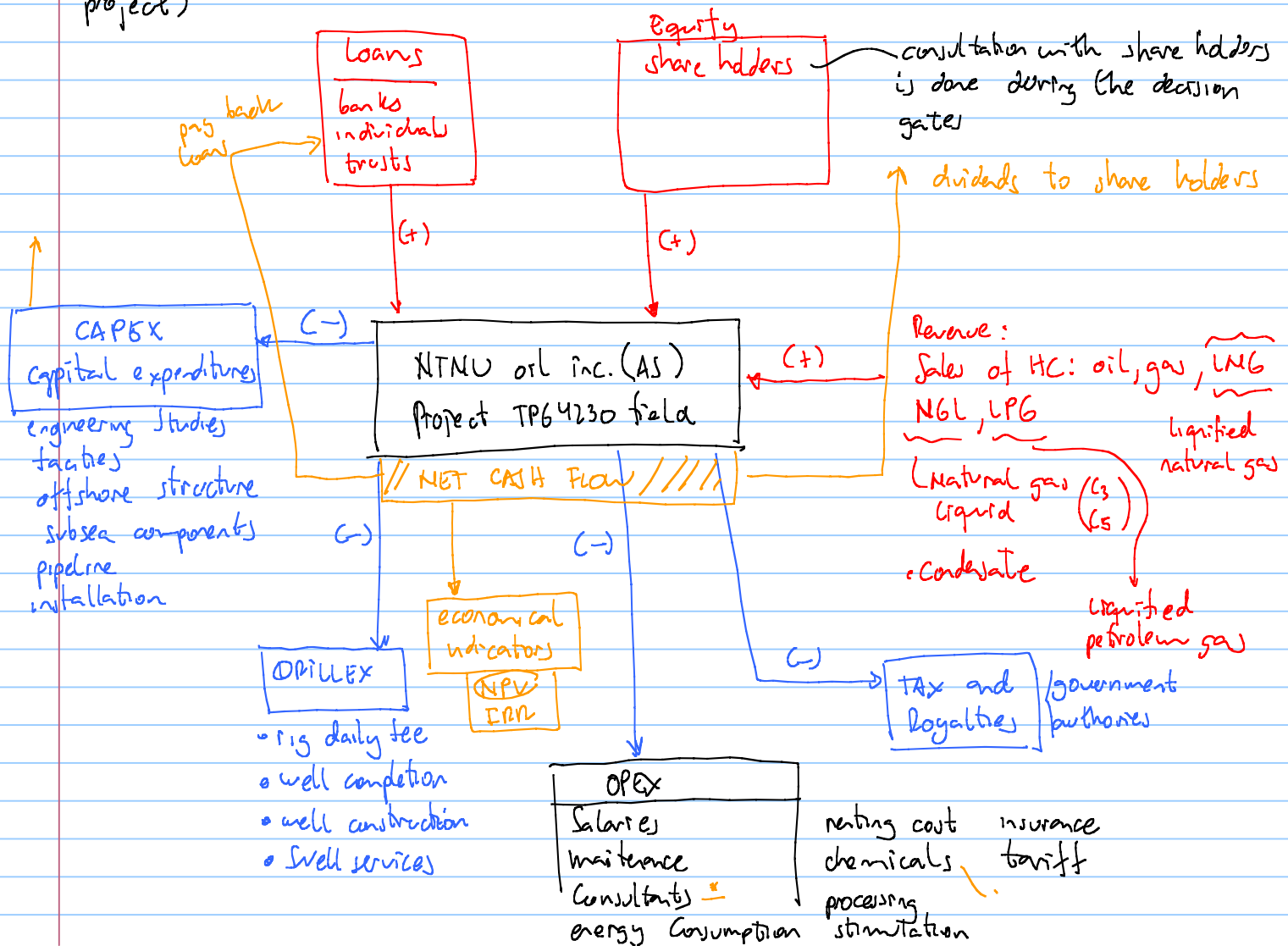
TRR [MMstb]	count	relative freq %
31	1	0.1
38	22	2.2
44	56	5.6
51	99	9.9
57	151	15.1
64	154	15.4
70	136	13.6
76	108	10.8
83	103	10.3
89	59	5.9
96	43	4.3
102	31	3.1
109	23	2.3
115	10	1
121	0	0
128	4	0.4

if I sum from bottom up

} probability that my TRR is equal or lower than 51

← probability that my TRR is equal or higher than

Cash flow and economic indicators of the project (Fried development project)



Cash flow with time

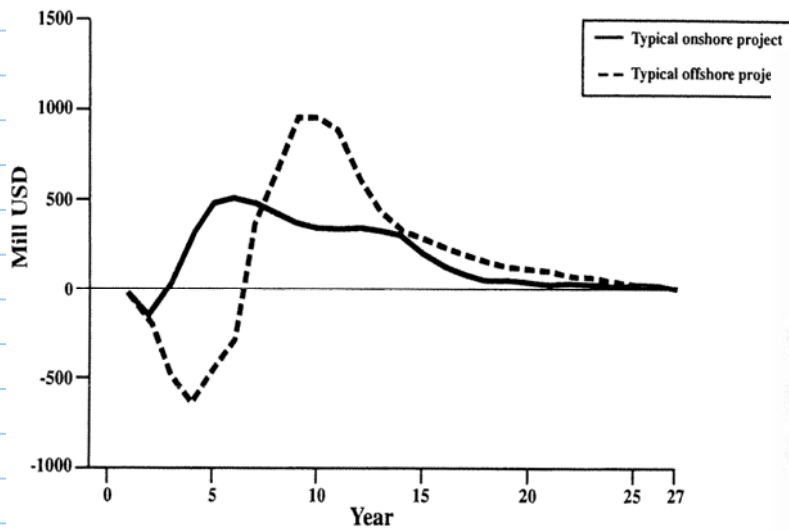
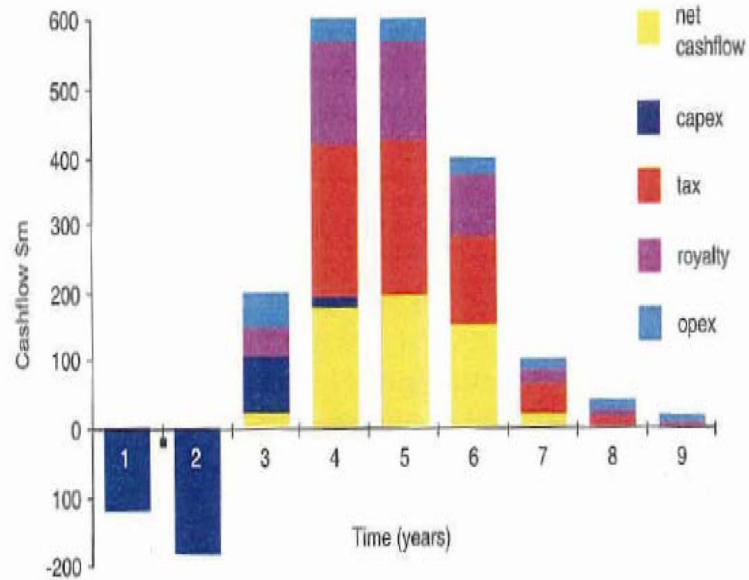


Fig. 9. Typical before tax cash flow profiles for offshore and onshore projects.



Cash flow is calculated on a yearly basis.

Year	CAPEX	OPEX	ROYALTY	TAX AND ROYALTIES	EXPENSES	Revenue	Cash flow	PV of cashflow
{0}	-	0	-	0	-	0	-	
1	-	0	-	0	-	0	-	
2	0	-	0	-	-	+	+	
3	0	-	0	-	-	+	+	

Present value: the current worth of a future sum of money

Present value

future value

$$V_p = V_f$$

$$\frac{1}{(1+i)^n}$$

interest, discount rate ~

(1+i) compound factor

$\left(\frac{1}{1+i}\right)$ ~ discount factor

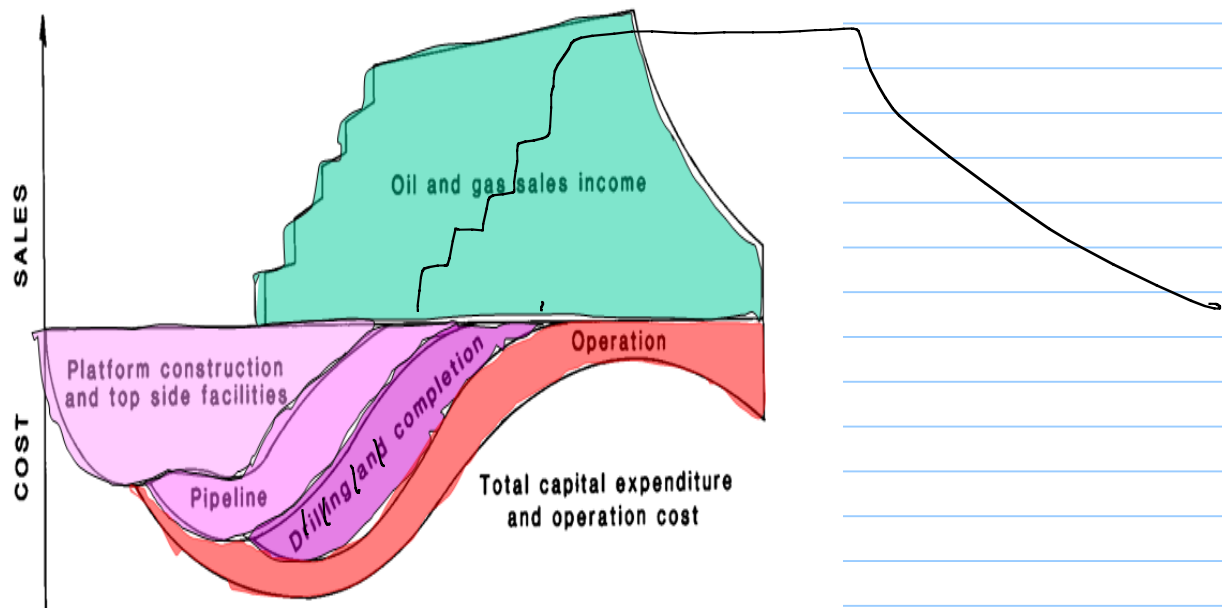
is the year were the future value is spent or gained

main economical indicator of the project

Net present value

has to be (+)

Revenue and Cost Profiles



The Ultimate driver in E&P operations

total number of years

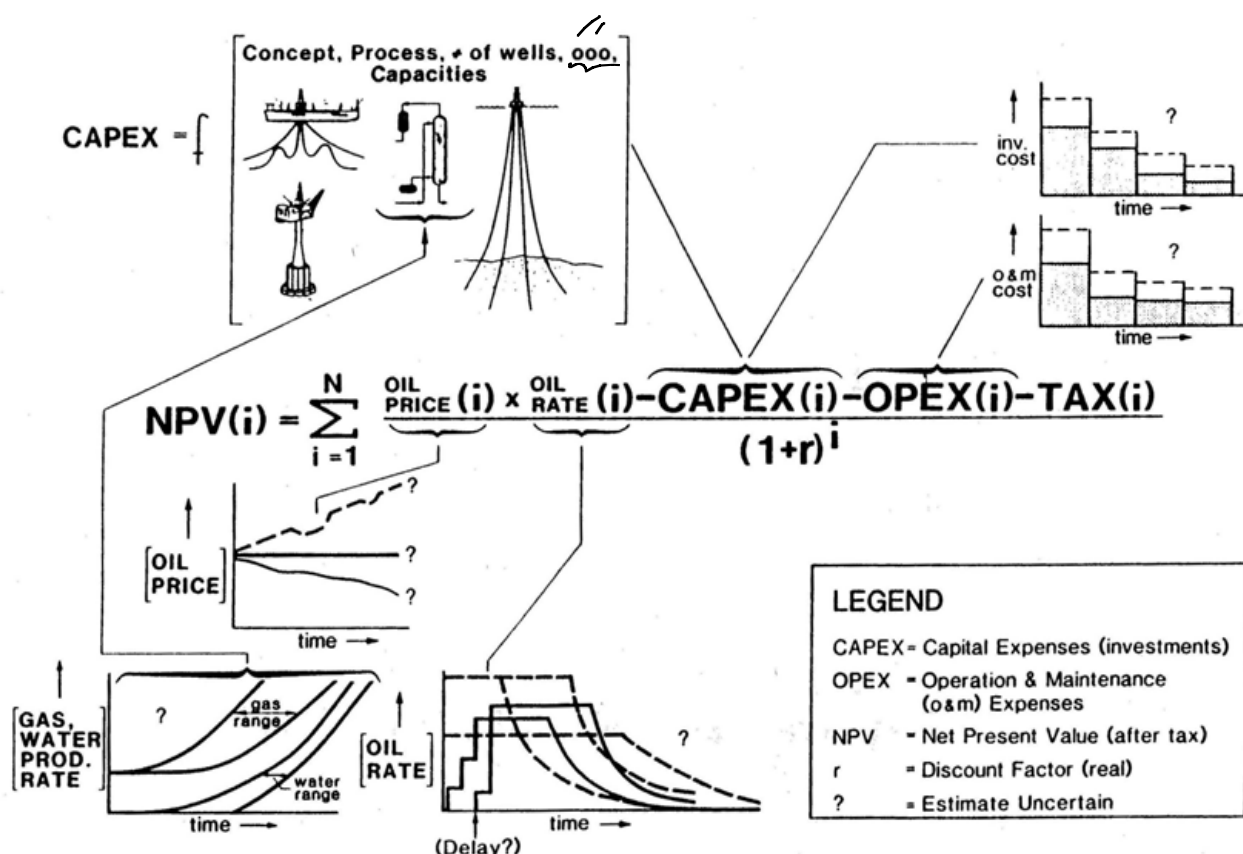
$$NPV = \sum_{i=0}^N \frac{\text{OIL PRICE}(i) \times \text{OIL PROD}(i) + \text{gas prod}(i) \times \text{gas price}(i) - \text{CAPEX}(i) - \text{OPEX}(i) - \text{TAX}(i)}{(1+r)^i}$$

year

interest, discount rate

neglected in this course

What can we control?



to get accurate estimates of cost values (and production rates) we need the input from the following specialists:

petroleum engineer : Reserves, location and nr wells,
production scheduling, fluids

Drilling engineer : Drilling and completion costs (Driller)

facilities engineer: production processing facilities
(processing) equipment required.
transportation

size cost

operations and maintenance : maintenance costs, manpower requirements

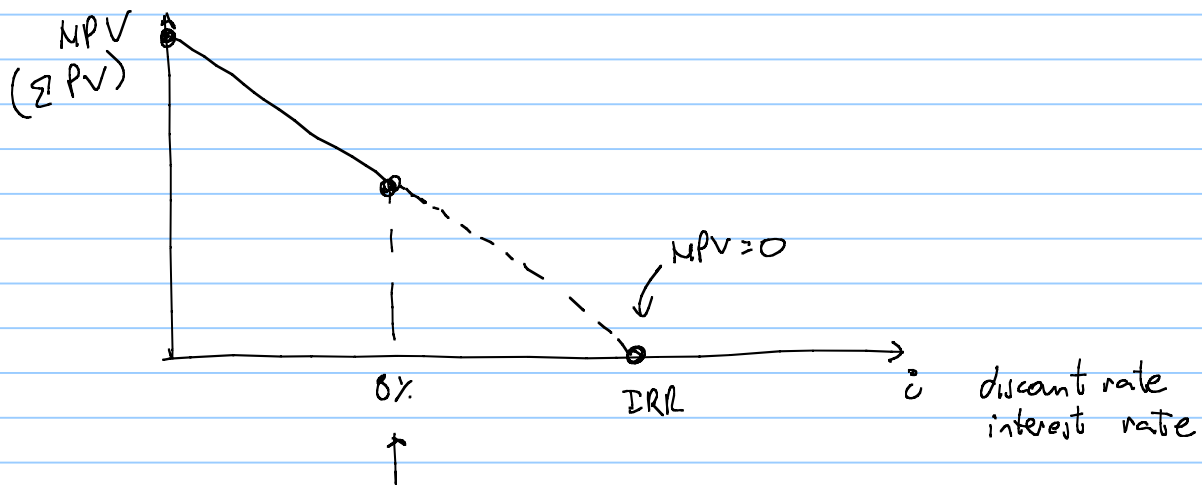
Offshore engineer : offshore structure, layout of the system

Project manager. tax, royalties

Human resources; Fiscal system expert, corporate planner

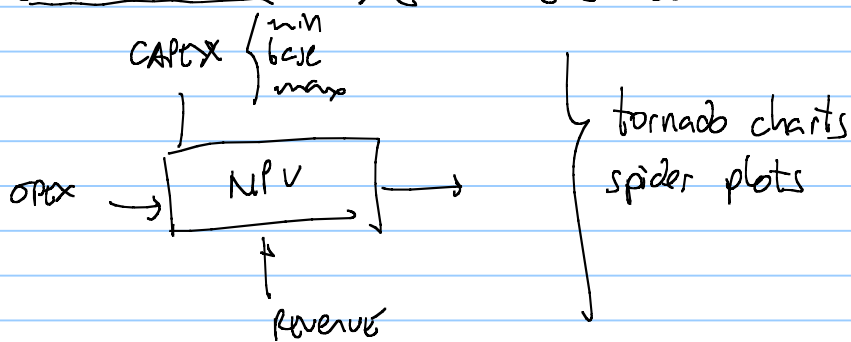
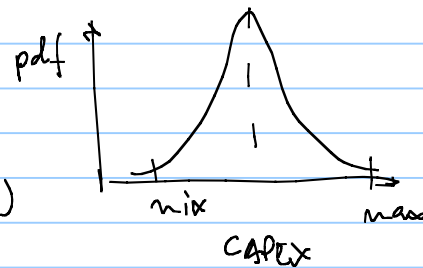
Another indicator of economical health of the project. IRR

internal rate of return: the interest rate that makes the project $NPV = 0$



how do we quantify the effect of uncertainty in the NPV?

Sensitivity studies using the principle of "Ceteris Paribus" $\rightarrow$ (all others same)

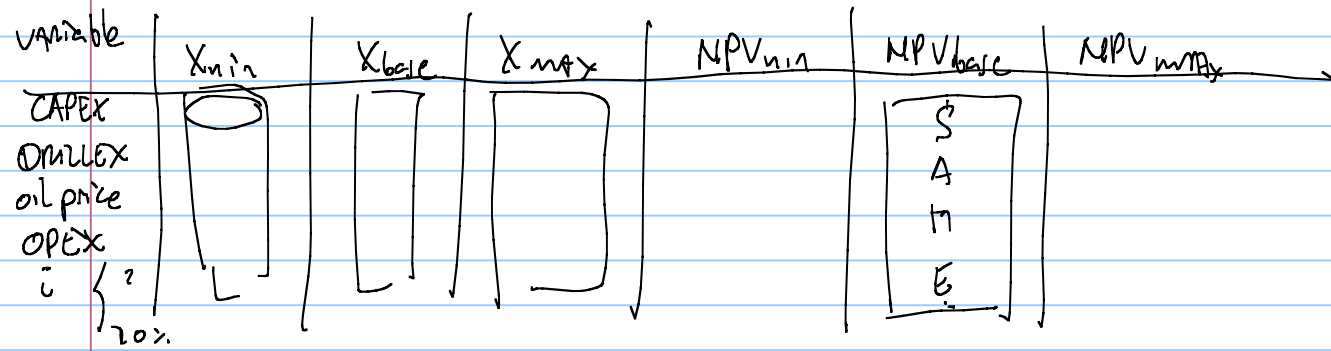


- ① Define a base case scenario base value for $\left\{ \begin{array}{l} \text{oil price} \\ \text{CAPEX} \\ \text{opex, etc} \end{array} \right.$
- ② Define a range for each variable. E.g. oil price $\left\{ \begin{array}{l} \text{min} \\ \text{base} \\ \text{max} \end{array} \right.$
- ③ Calculate value of interest (economic indicator NPV) changing (one at a time) the variables (while keeping all other variables at their base value)

min price $\rightarrow$ calculate NPV

base oil price $\rightarrow$ NPV

max oil price $\rightarrow$ NPV



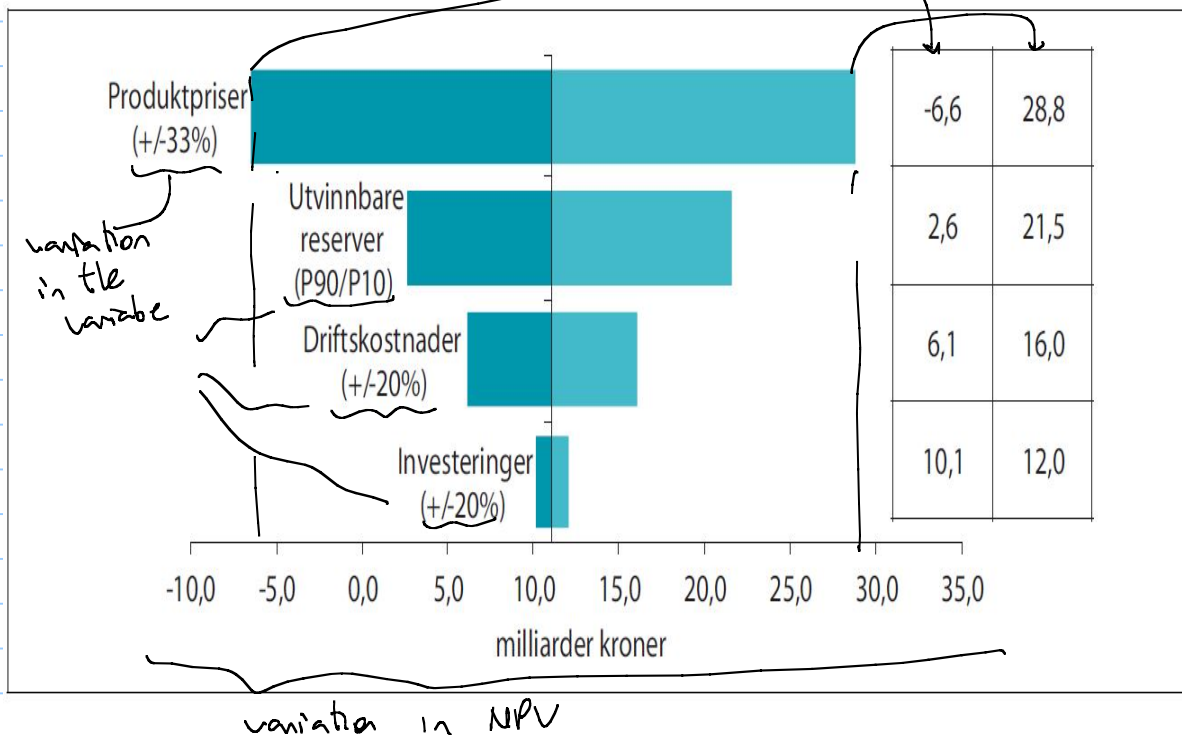
apply normalization

X_{min} normalized X_{base} normalize X_{max}

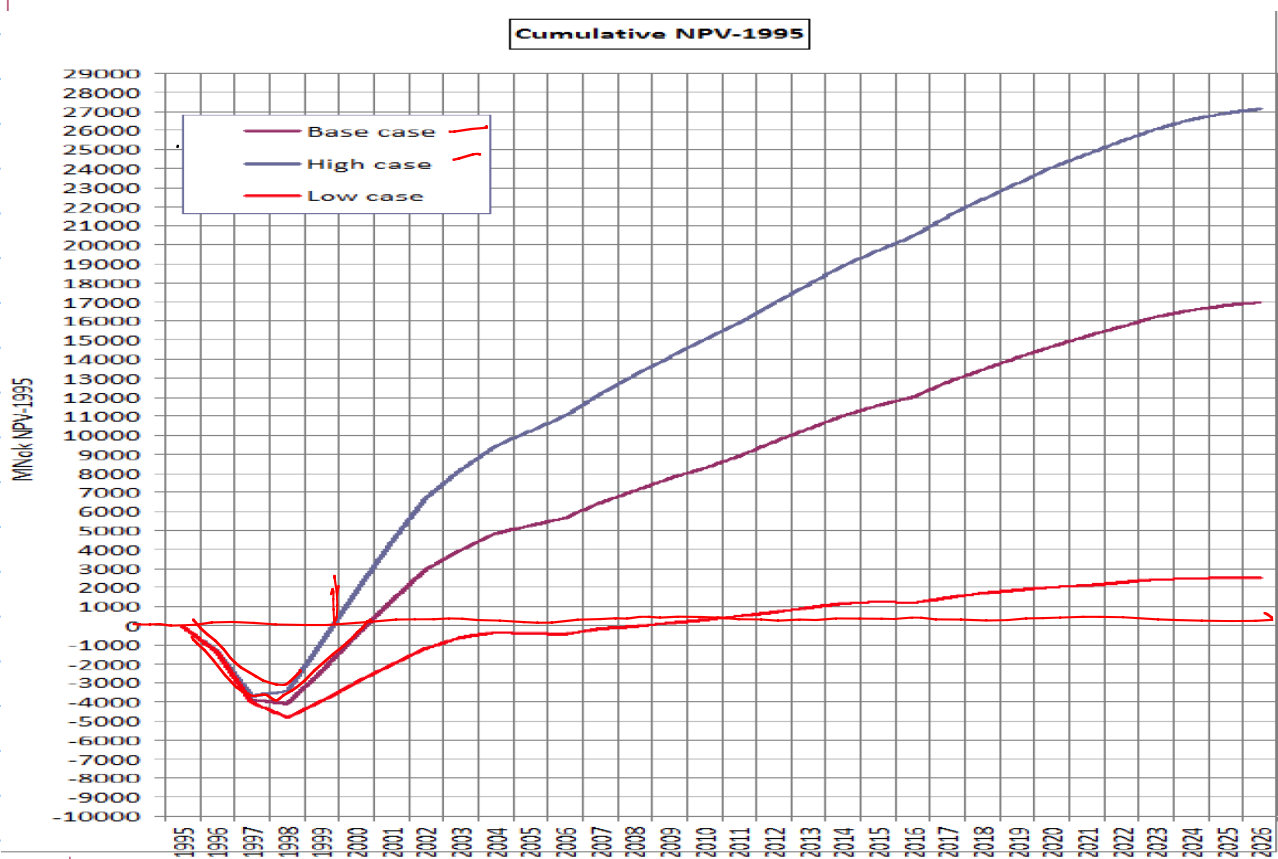
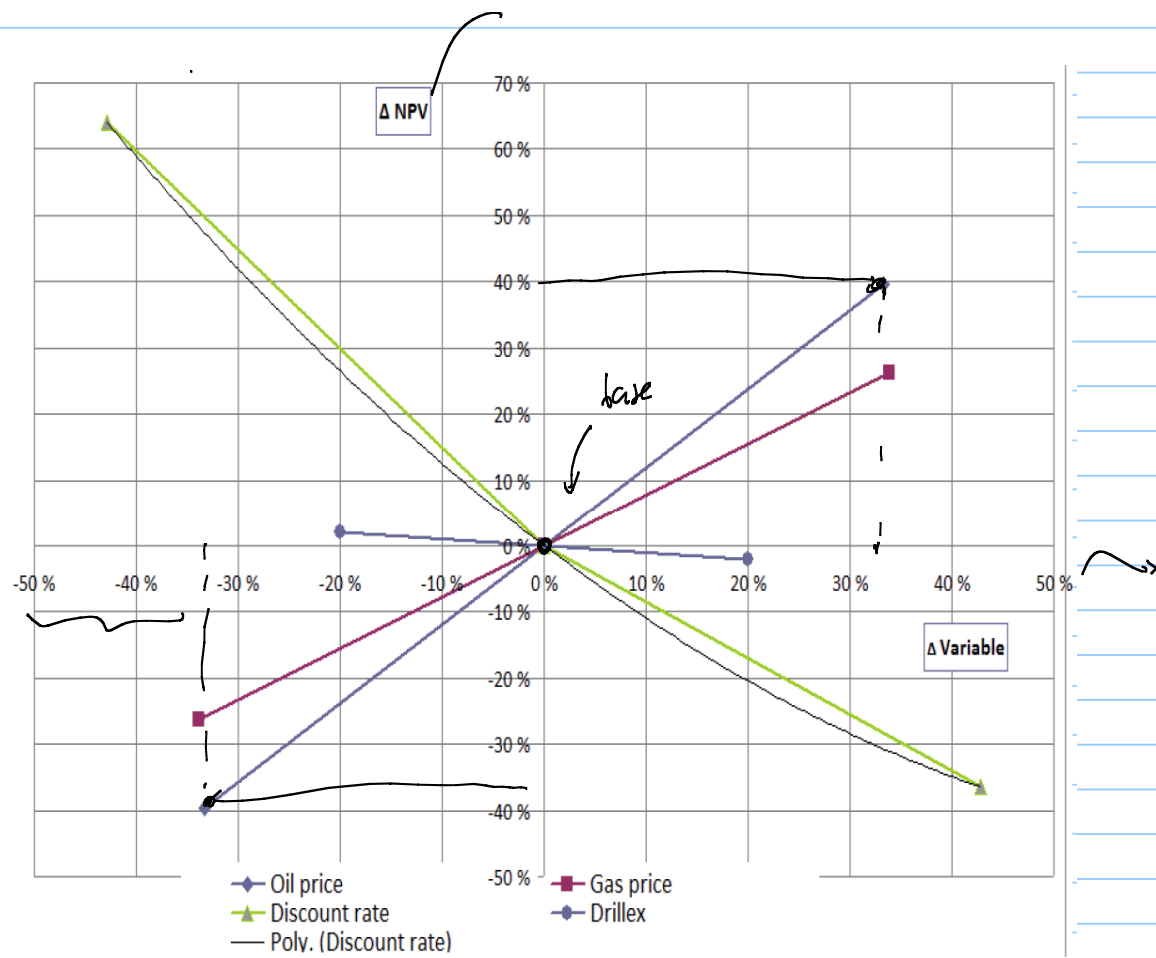
% NPV
normalize

CAPEX	$\frac{X_{min} - X_{base}}{X_{base}} \cdot 100$	0%	$\frac{X_{max} - X_{base}}{X_{base}} \cdot 100$	$\frac{NPV_{min} - NPV_{base}}{NPV_{base}} \cdot 100$
OMUPEX	11	0%	11	
oil price	11	0%	11	

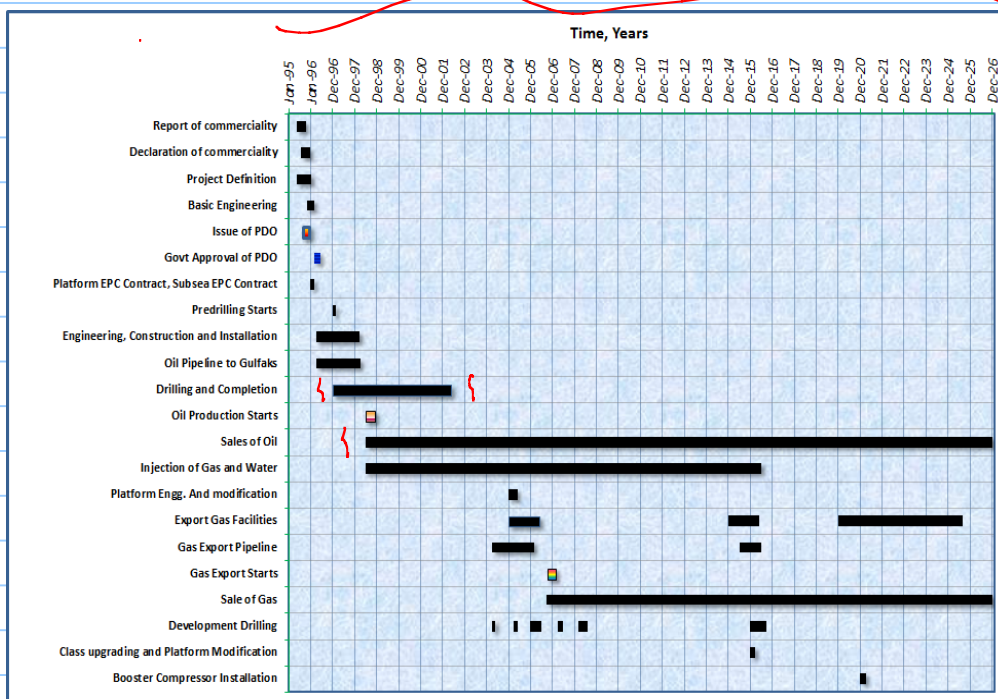
ternario chart



Sprider plot



Gantt diagrams Special chart diagram used in project management that shows when and the duration of important events in the design and construction of the field



Henry Gantt (1861-1919), a mechanical engineer, management consultant, and industrial advisor developed Gantt charts in the 1910's. Not as commonplace as they are today, Gantt charts were innovative and new during the 1920's, where Gantt charts were used on large construction projects like the Hoover Dam started in 1931 and the Eisenhower National Defense Interstate Highway System started in 1956.



Henry Gantt

Every time we, in our project management careers, go through the rigmarole of our projects, trying to meet and beat our own-set goals, a silent word of gratitude goes to the heavens for Henry Gantt for conceiving this intuitive diagram for charting project timelines, for the Gantt Diagram allows us to excel in this chosen career.

<https://www.smartsheet.com/blog/gantt-chart-excel>

useful for exercise.

How to deal with uncertainty in decisions or with integer variables

variables {

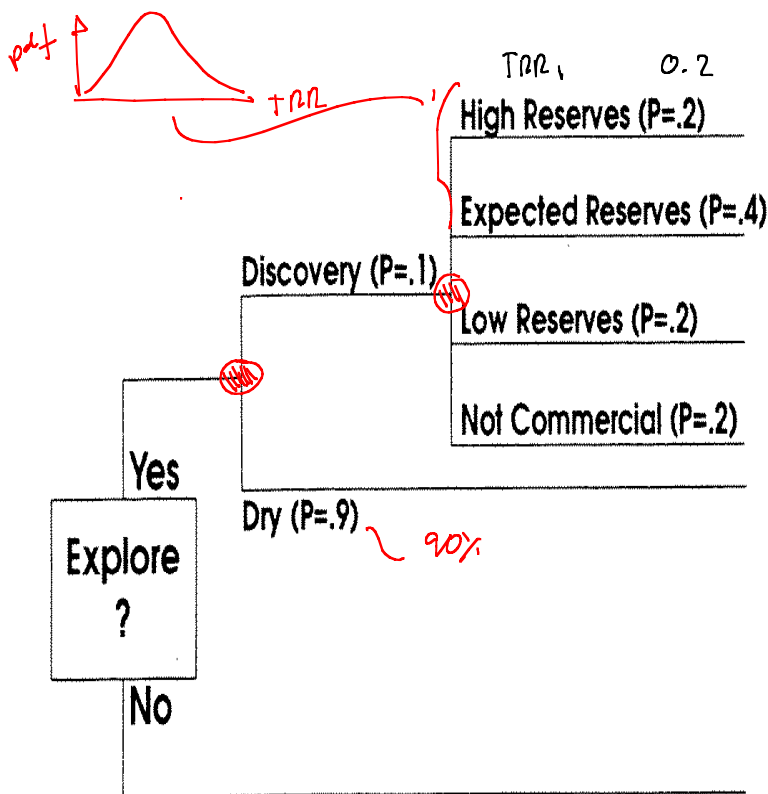
- decisions
- development options {
 - platform
 - subject to beach
 - FPSO

Decision trees allow to deal with integer variables (not continuous)

□ ~ decision nodes

○ ~ chance nodes

◁ ~ end node



multiplication of all probabilities (chance nodes) of that particular branch

i	Prob _i	NPV _i	Prob _i x NPV _i	
1	0.02	A	(.02) A	Σ P _i x NPV _i
2	0.04	B	(.04) B	
3	0.02	C	0.02 (.02) C	
4	0.02	D	(.02) D	
5	0.90	E	(.90) E	
6	1.00	0	0	=

EPV

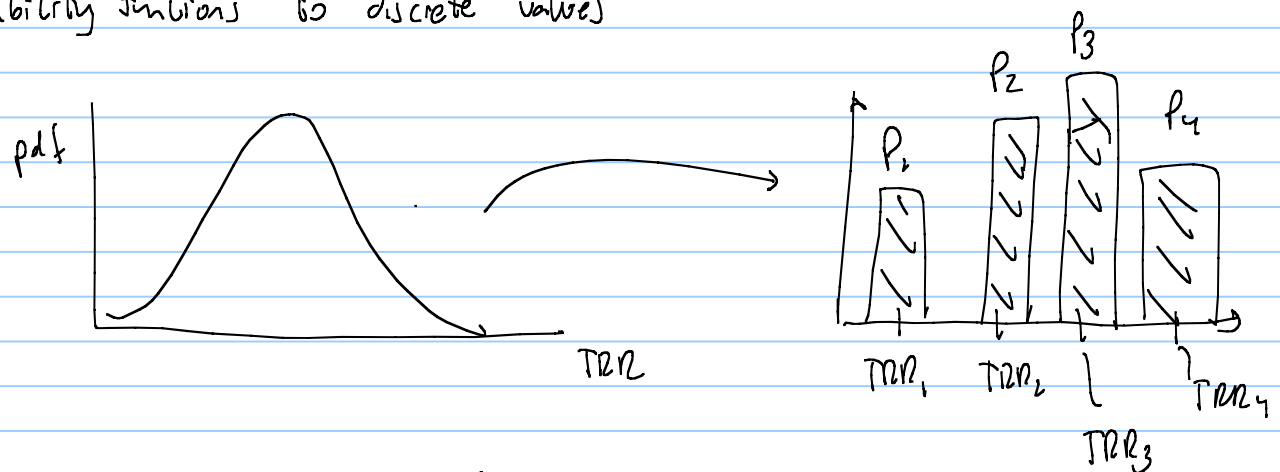
(NPV)

E negative (+)

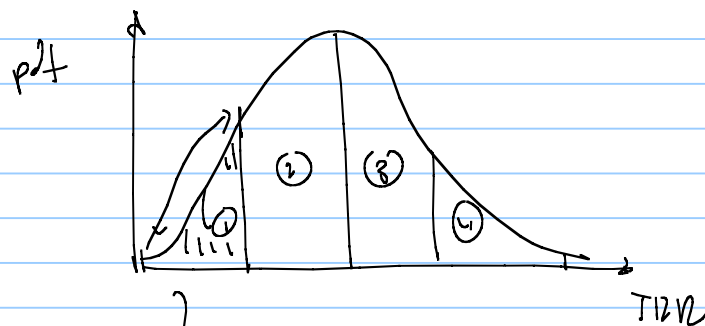
A) B) C) D)

- Weighted AVG. NPV ('Yes-Branch') = $\sum_{i=1}^5 (\text{Prob}_i) \times \text{NPV}_i = G$
- NPV ('No-Branch') = 0
- IF $G > 0$, Explore!
- A-E; Shows the spread in NPV-Outcome for this venture

in decision trees we sometimes have to convert - continuous probability functions to discrete values



one way to do it is the following:
divide the pdf in sections



area under the curve provides the probability of the section

for the value TRR_1 calculate the most probable value in the section (mode of each section)

Price \$/Bbl.	Initial Investment \$MM	Reserves MM Bbls.	Case	Prob.	NPV	NPV x Prob.
10 P = .70	50 P = .30	50 P = .20	1	.042	60	2.52
10 P = .70	50 P = .30	30 P = .70	2	.147	15	2.21
10 P = .70	50 P = .30	20 P = .10	3	.021	-10	-0.21
10 P = .70	60 P = .40	50 P = .20	4	.056	53	2.97
10 P = .70	60 P = .40	30 P = .70	5	.196	8	1.57
10 P = .70	60 P = .40	20 P = .10	6	.028	-17	-0.48
8 P = .30	50 P = .30	50 P = .20	7	.042	46	1.93
8 P = .30	50 P = .30	30 P = .70	8	.147	1	0.15
8 P = .30	50 P = .30	20 P = .10	9	.021	-24	-0.50
8 P = .30	60 P = .40	50 P = .20	10	.018	35	0.63
8 P = .30	60 P = .40	30 P = .70	11	.063	0	0.00
8 P = .30	60 P = .40	20 P = .10	12	.009	-20	-0.18
8 P = .30	50 P = .30	50 P = .20	13	.024	28	0.67
8 P = .30	50 P = .30	30 P = .70	14	.084	-7	-0.59
8 P = .30	50 P = .30	20 P = .10	15	.012	-27	-0.32
8 P = .30	60 P = .40	50 P = .20	16	.018	21	-0.38
8 P = .30	60 P = .40	30 P = .70	17	.063	-14	-0.88
8 P = .30	60 P = .40	20 P = .10	18	.009	-35	-0.32
Weighted Avg. NPV				9.55		

MEV mean expected value