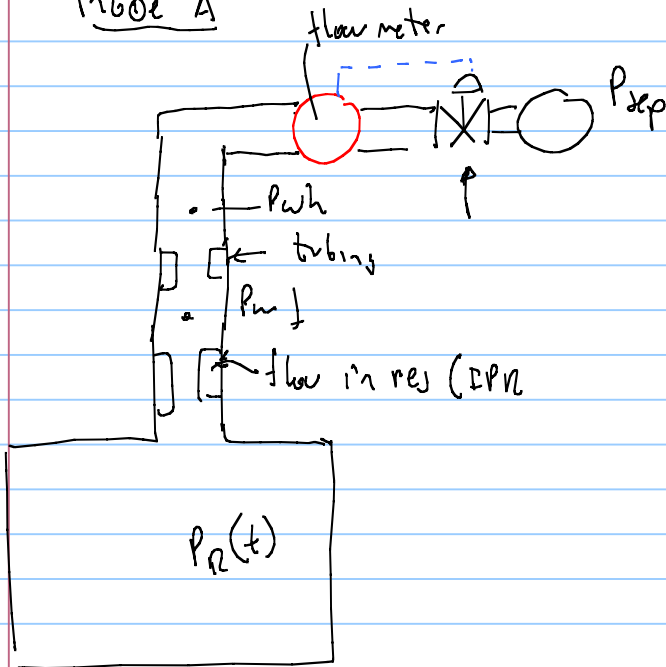
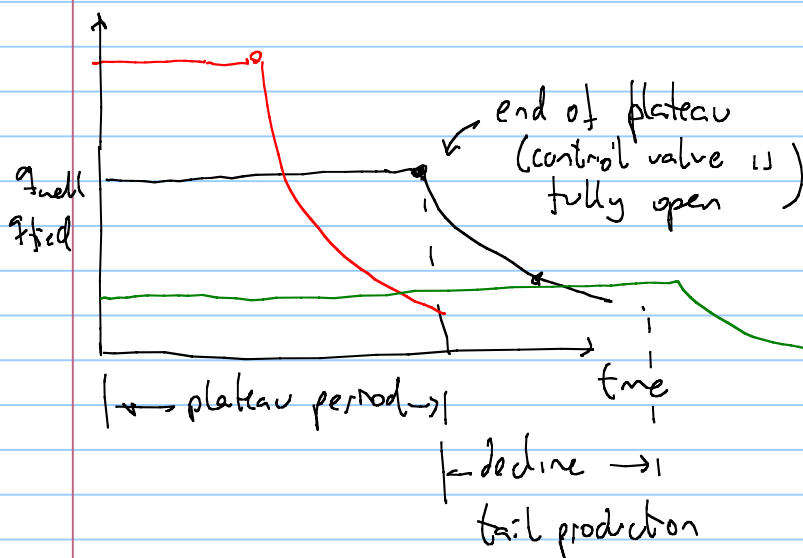


Week 2. Day 6:

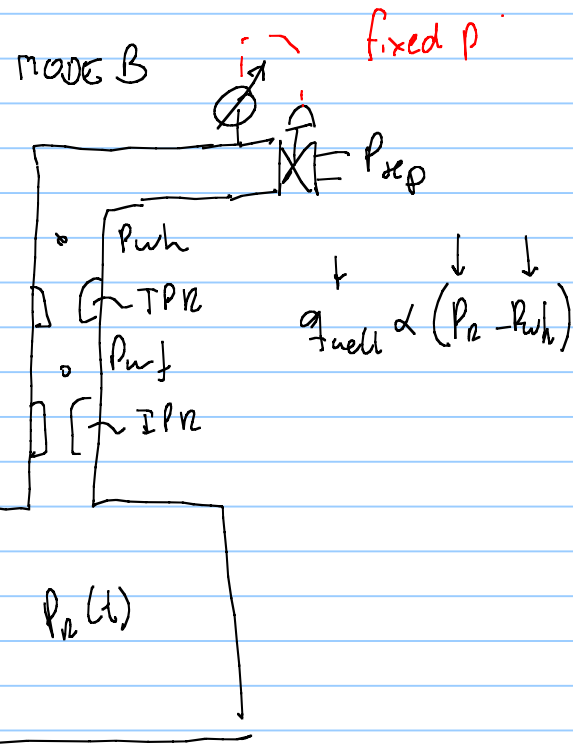
Production modes of wells and field

mode A

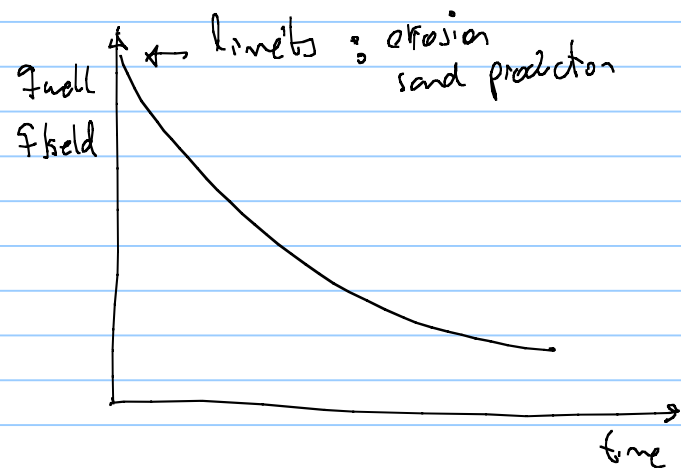
Constant production mode



- New development with standalone processing facilities
- Big size
- typically for gas (offshore), LNG predefined delivery contract
 ↓
 long term



constant pressure mode



- Produce as much as possible as early as possible
- Satellite fields (medium to small size)

the production is routed to existing processing facilities with spare capacity

Rule of thumb for defining plateau for oil reservoirs:

$$TRR = R.F. \cdot G$$

initial gas in place

R.F. = initial oil in place

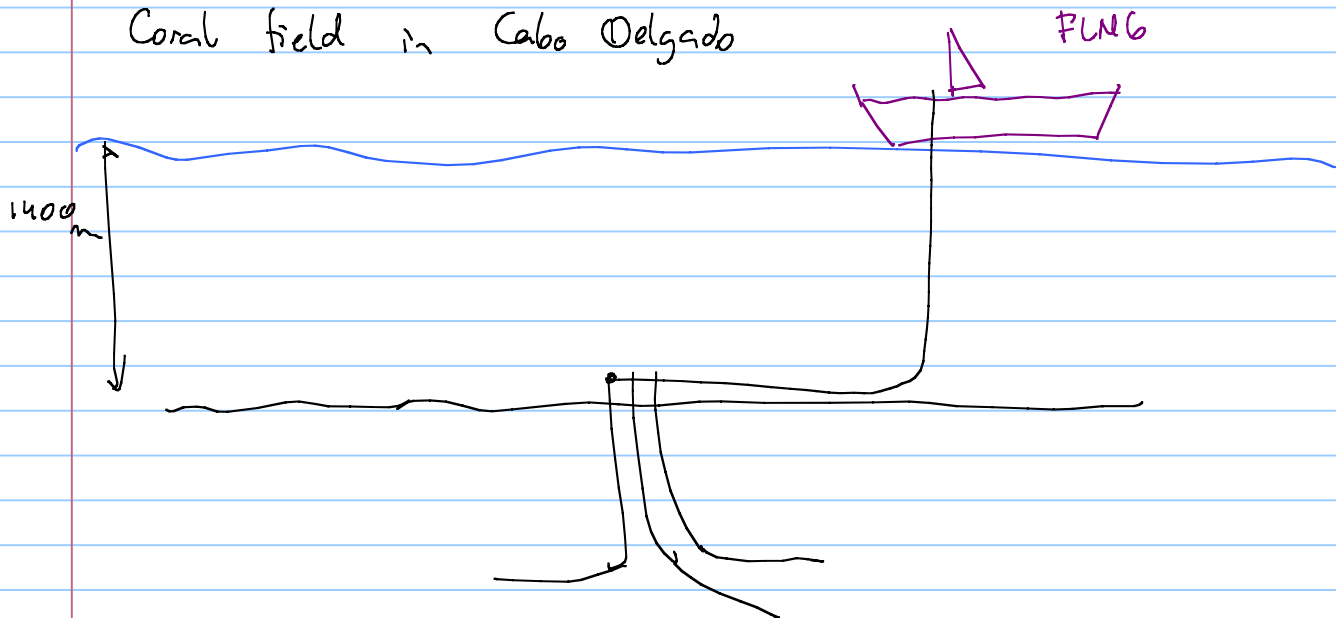
↑ recovery factor

$$q_{plateau} = \frac{0.1 \cdot TRR}{\text{Operational days per year}}$$

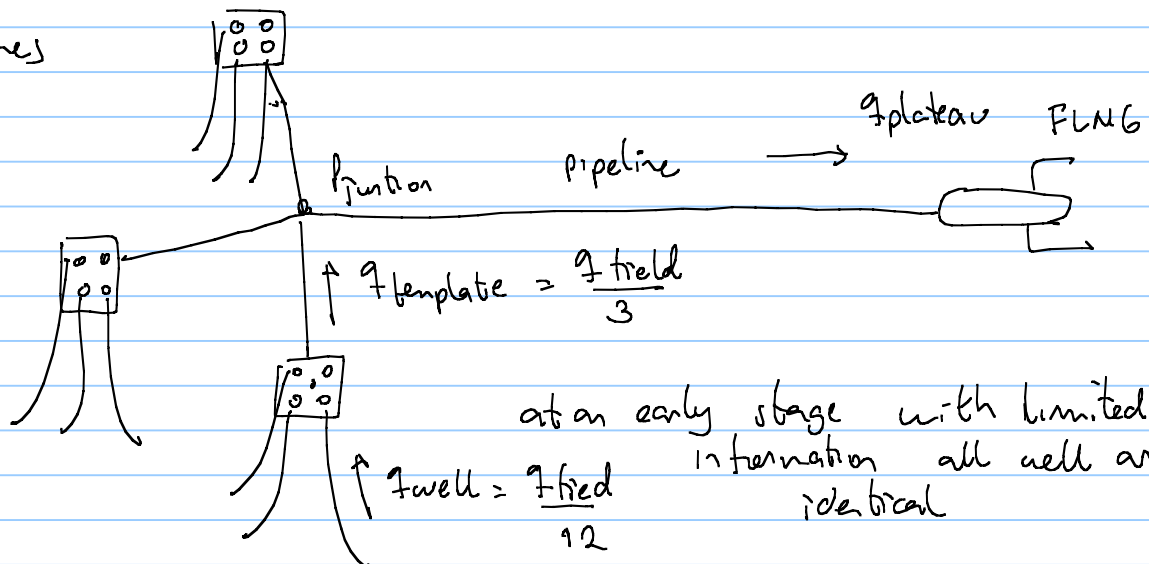
for gas

$$q_{plateau} = (0.03 - 0.05) TRR$$

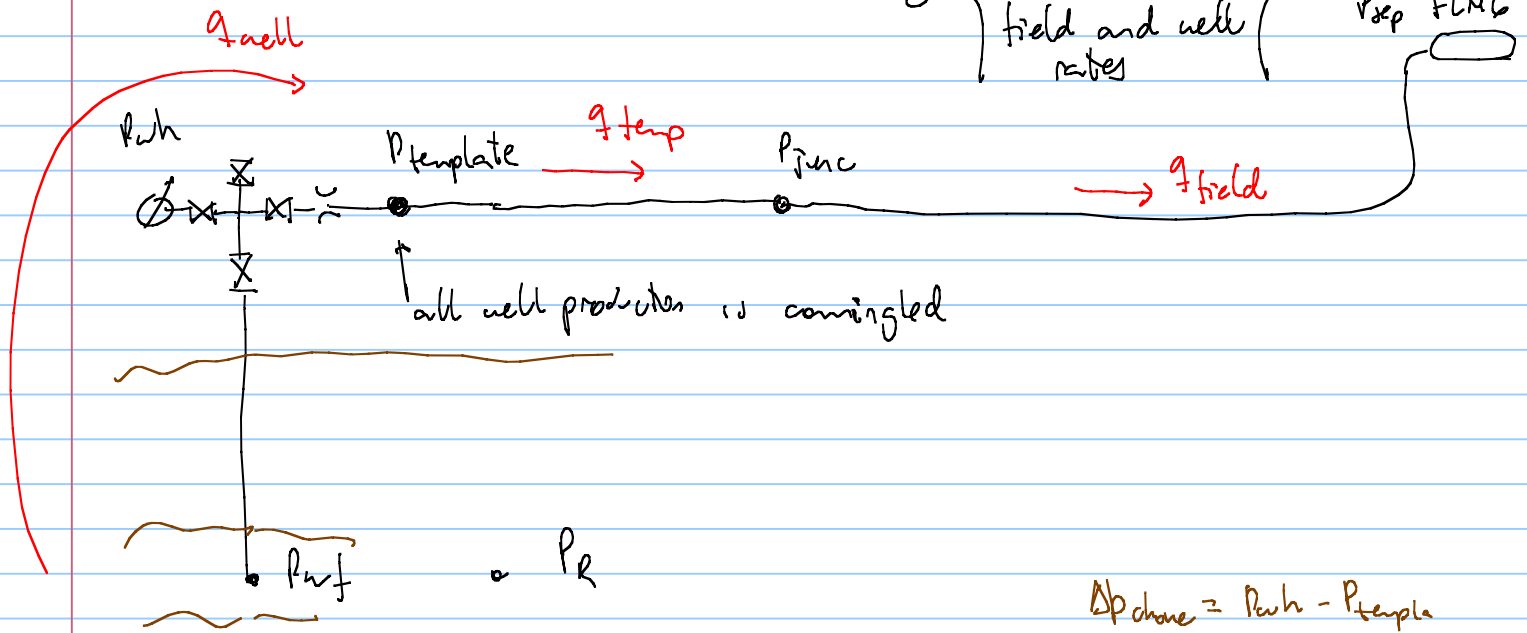
Coral field in Cabo Delgado



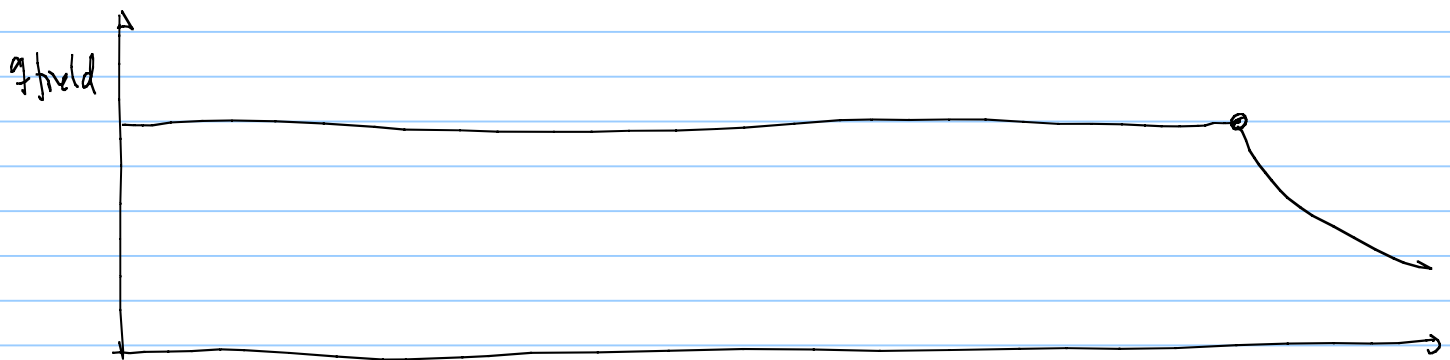
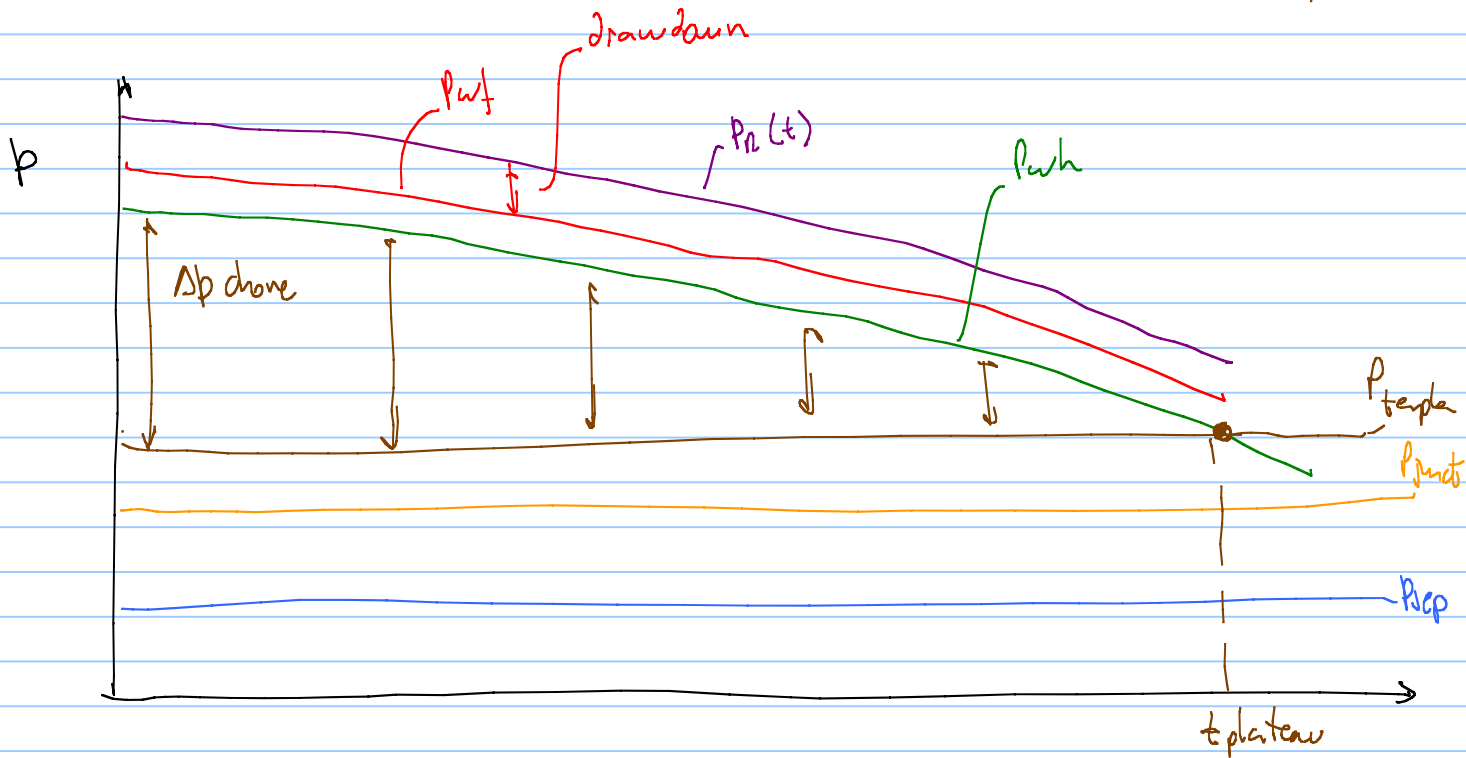
identical flowlines



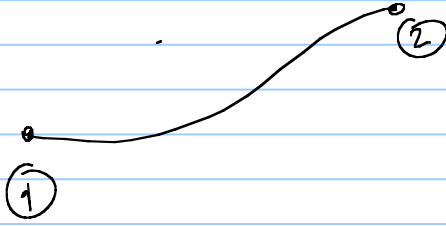
Production scheduling { define the field and well rates



$$\Delta p_{drawn} = P_{wh} - P_{temp}$$



Pressure drop for liquids: undersaturated oil + water



$$z_1 + \cancel{\frac{1}{2} \frac{v_1^2}{g}} + \frac{p_1}{\rho g} = \frac{p_2}{\rho g} + \cancel{z_2 + \frac{1}{2} \frac{v_2^2}{g}} + f \frac{L}{\phi} \frac{v^2}{2g}$$

↑

$$\text{ tubing } p_1 = f(p_2, q)$$

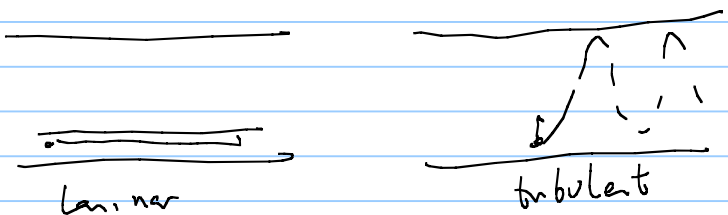
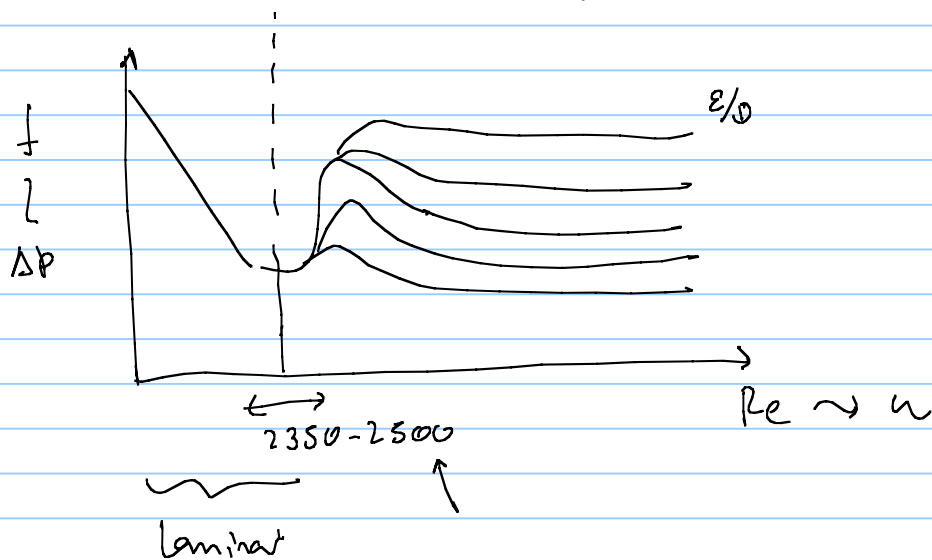
$$\text{ tubing } p_2 = f(p_1, q)$$

$$\text{ tubing } q = f(p_1, p_2)$$

$$q = V \cdot A = \frac{\pi \phi^2}{4} \cdot V$$

$$V = \left(\frac{q \cdot 4}{\pi \phi^2} \right)$$

$$v^2 = \frac{q^2 \cdot 16}{\pi \phi^2}$$



$$f_{\text{laminar}} = \frac{64}{Re}$$

$$f_{\text{turbulent}} =$$

Colebrook-White equation

$$\text{implicit} \rightarrow \frac{1}{\sqrt{f}} = -2 \log \left(\frac{\epsilon}{3.7 \phi} + \frac{2.51}{Re \sqrt{f}} \right)$$

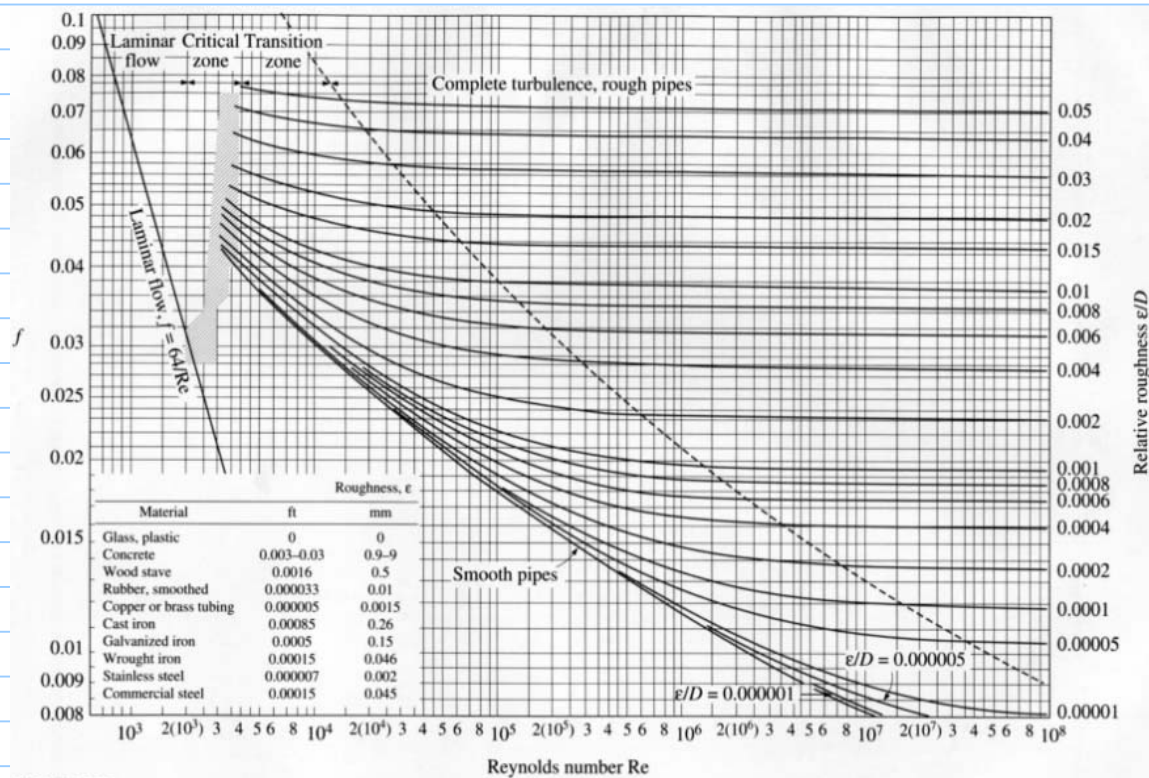


FIGURE A-27

The Moody chart for the friction factor for fully developed flow in circular tubes.

https://en.wikipedia.org/wiki/Darcy_friction_factor_formulae

all expressions for friction factor

Table of Colebrook equation approximations

Equation	Author	Year	Range	Ref
$f = .0055 \left[1 + \left(2 \times 10^4 \cdot \frac{\epsilon}{D} + \frac{10^6}{Re} \right)^{\frac{1}{4}} \right]$	Moody	1947	$Re = 4000 - 5 \cdot 10^8$ $\epsilon/D = 0 - 0.01$	
$f = .064 \left(\frac{\epsilon}{D} \right)^{.395} + 0.58 \left(\frac{\epsilon}{D} \right) + 88 \left(\frac{\epsilon}{D} \right)^{.44} \cdot Re^{-.9}$ where $\Psi = 1.62 \left(\frac{\epsilon}{D} \right)^{.136}$	Wood	1966	$Re = 4000 - 5 \cdot 10^7$ $\epsilon/D = 0.00001 - 0.04$	
$\frac{1}{\sqrt{f}} = -2 \log \left(\frac{\epsilon/D}{3.715} + \frac{15}{Re} \right)$	Eck	1973		
$\frac{1}{\sqrt{f}} = -2 \log \left(\frac{\epsilon/D}{3.7} + \frac{5.74}{Re^{0.9}} \right)$	Swamee and Jain	1976	$Re = 5000 - 10^8$ $\epsilon/D = 0.000001 - 0.05$	
$\frac{1}{\sqrt{f}} = -2 \log \left(\frac{\epsilon/D}{3.71} + \left(\frac{7}{Re} \right)^{.95} \right)$	Churchill	1973	Not specified	
$\frac{1}{\sqrt{f}} = -2 \log \left(\frac{\epsilon/D}{3.715} + \left(\frac{8.945}{Re} \right)^{.69} \right)$	Jain	1976		
$f = 8 \left[\left(\frac{8}{Re} \right)^{1.3} + \frac{1}{(\Theta_1 + \Theta_2)^{1.8}} \right]^{\frac{1}{2}}$ where $\Theta_1 = \left[-2.457 \ln \left(\left(\frac{7}{Re} \right)^{.95} + 0.27 \frac{\epsilon}{D} \right) \right]^{16}$ $\Theta_2 = \left(\frac{37530}{Re} \right)^{16}$	Churchill	1977		
$\frac{1}{\sqrt{f}} = -2 \log \left[\frac{\epsilon/D}{3.7055} - \frac{5.0452}{Re} \log \left(\frac{1}{2.8257} \left(\frac{\epsilon}{D} \right)^{1.1089} + \frac{5.8606}{Re^{0.44492}} \right) \right]$	Chen	1979	$Re = 4000 - 4 \cdot 10^8$	
$\frac{1}{\sqrt{f}} = 1.8 \log \left[\frac{Re}{0.135 Re (\epsilon/D) + 6.5} \right]$	Round	1980		
$\frac{1}{\sqrt{f}} = -2 \log \left(\frac{\epsilon/D}{3.7} + \frac{4.518 \log \left(\frac{Re}{7} \right)}{Re \left(1 + \frac{Re^{0.89}}{29} (\epsilon/D)^{0.7} \right)} \right)$	Barr	1981		
$\frac{1}{\sqrt{f}} = -2 \log \left[\frac{\epsilon/D}{3.7} - \frac{5.02}{Re} \log \left(\frac{\epsilon/D}{3.7} - \frac{5.02}{Re} \log \left(\frac{\epsilon/D}{3.7} + \frac{13}{Re} \right) \right) \right]$ or $\frac{1}{\sqrt{f}} = -2 \log \left[\frac{\epsilon/D}{3.7} - \frac{5.02}{Re} \log \left(\frac{\epsilon/D}{3.7} + \frac{13}{Re} \right) \right]$	Zigrang and Sylvester	1982		
$\frac{1}{\sqrt{f}} = -1.8 \log \left[\left(\frac{\epsilon/D}{3.7} \right)^{1.11} + \frac{6.9}{Re} \right]$	Haaland ^[2]	1983		
$\frac{1}{\sqrt{f}} = \Psi_1 - \frac{(\Psi_2 - \Psi_1)^2}{\Psi_2 - 2\Psi_1 + \Psi_1}$ or $\frac{1}{\sqrt{f}} = 4.781 - \frac{(\Psi_1 - 4.781)^2}{\Psi_2 - 2\Psi_1 + 4.781}$ where $\Psi_1 = -2 \log \left(\frac{\epsilon/D}{3.7} + \frac{12}{Re} \right)$	Bergides	1984		

$\Psi_1 = -2 \log \left(\frac{\epsilon/D}{3.7} + \frac{2.51 \Psi_2}{Re} \right)$ $\Psi_2 = -2 \log \left(\frac{\epsilon/D}{3.7} + \frac{2.51 \Psi_1}{Re} \right)$				
$A = 0.11 \left(\frac{68}{Re} + \epsilon \right)^{0.25}$ $\epsilon A \geq 0.018$ then $f = A$ and $\epsilon A < 0.018$ then $f = 0.0028 + 0.85A$	Tsai	1989		
$\frac{1}{\sqrt{f}} = -2 \log \left(\frac{\epsilon/D}{3.7} + \frac{95}{Re^{0.898}} - \frac{96.82}{Re} \right)$	Manandhi	1997	$Re = 4000 - 10^8$ $\epsilon/D = 0 - 0.06$	
$\frac{1}{\sqrt{f}} = -2 \log \left(\frac{\epsilon/D}{3.7065} - \frac{5.0272}{Re} \log \left[\frac{\epsilon/D}{3.827} - \frac{4.657}{Re} \log \left(\left(\frac{\epsilon/D}{7.7918} \right)^{0.8981} + \left(\frac{5.3236}{208.816 + Re} \right)^{0.8981} \right) \right] \right)$	Monzon, Romeo, Rojo	2002		
$\frac{1}{\sqrt{f}} = 0.8686 \ln \left[\frac{0.4587 Re}{(S - 0.31)^{0.75-0.64S}} \right]$ where: $S = 0.124 Re \frac{\epsilon}{D} + \ln(0.4587 Re)$	Goudar, Sonnad	2006		
$\frac{1}{\sqrt{f}} = 0.8686 \ln \left[\frac{0.4587 Re}{(S - 0.31)^{0.75-0.64S}} \right]$ where: $S = 0.124 Re \frac{\epsilon}{D} + \ln(0.4587 Re)$	Vahidkhah, Kouchaksazeh	2008		
$\frac{1}{\sqrt{f}} = \alpha - \frac{\alpha + 2 \log \left(\frac{Re}{B} \right)}{1 + \frac{Re}{B^{0.8}}}$ where: $\alpha = \frac{0.744 \ln(Re) - 1.41}{1 + 1.32 \sqrt{\epsilon/D}}$ $B = \frac{\epsilon/D}{3.7} Re + 2.51 \alpha$	Bussell	2008		
$f = \frac{6.4}{(\ln(Re) - \ln(1 + 0.01 Re \frac{\epsilon}{D} (1 + 10 \sqrt{\frac{\epsilon}{D}})))^{0.4}}$	Alici, Kargoz	2009		
$f = \frac{0.3479 - 0.0000947(7 - \log Re)^4}{\left(\log \left(\frac{\epsilon/D}{2.413} + \frac{1.888}{Re^{0.75}} \right) \right)^2}$	Eleonides, Papadimitriou, Timopoulos	2010		
$f = 1.618 \left[\ln \left(\frac{0.234e^{1.3007}}{Re^{1.1108}} + \frac{56.201}{Re^{0.0712}} \right) \right]^{-8}$	Fang	2011		
$f = \left[-2 \log \left(\frac{2.18\beta}{Re} + \frac{\epsilon}{3.71} \right) \right]^{-8}$, $\beta = \ln \left(\frac{1.186}{\ln(1 + 1.126\beta)} \right)$	Bric	2011		
$f = 1.325474505 \log_e (A - 0.8686068422 \beta \log_e (A - 0.8784893582 \beta \log_e (A + (1.6653680(35.2\beta)^{1.877307287})))^{-8}$ where: $A = \frac{\epsilon/D}{3.7065}$ $B = \frac{2.5228}{Re}$	Alshar	2012		

explicit

Haaland
Prof @ NTNU
~ 1983

$$\frac{1}{\sqrt{f}} = -1.6 \log \left[\left(\frac{\epsilon/D}{3.7} \right)^{1.11} + \left(\frac{6.9}{Re} \right) \right]$$

$$f = \left[-1.6 \log \left[\left(\frac{\epsilon/D}{3.7} \right)^{1.11} + \left(\frac{6.9}{Re} \right) \right] \right]^{-2}$$

friction factor

Beware !

Darcy-Weisbach
 Fanning (American)

$$f = 4 \cdot f_{\text{FANNING}}$$

$$f_{\text{FANNING}} = \frac{\tau}{\frac{1}{2} \rho v^2}$$

$$f_{\text{DARCY}} = \frac{\tau}{\frac{1}{8} \rho v^2}$$

Class exercise IPR-TPR equilibrium for undersaturated oil well
(peregrino field, offshore Brazil).

[illegible]

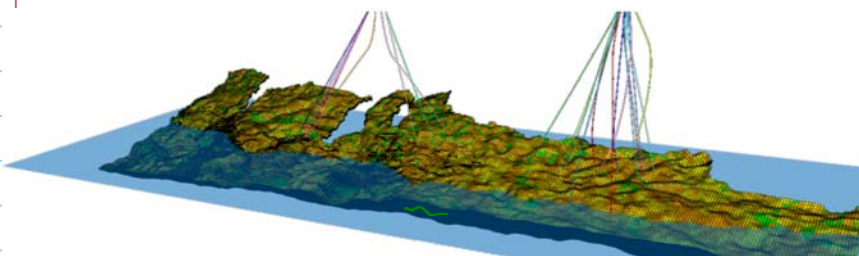
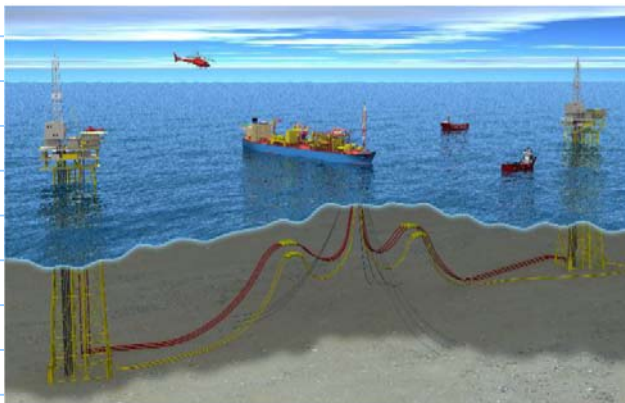
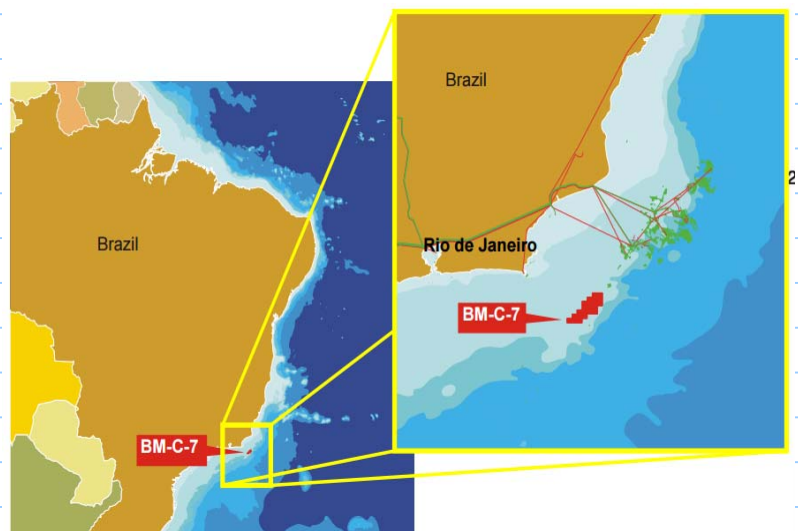
$$Q_o = J (P_e^{\leftarrow} - P_{wf})$$

~ pressure required at well bottom to flow against γ bore

Ø $P_{wh} = 7 \text{ bara}$

tubing P_1 ?

tubing P_2 ?

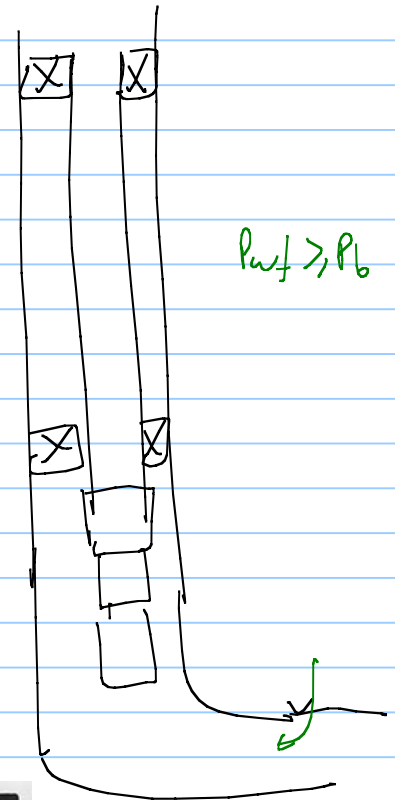
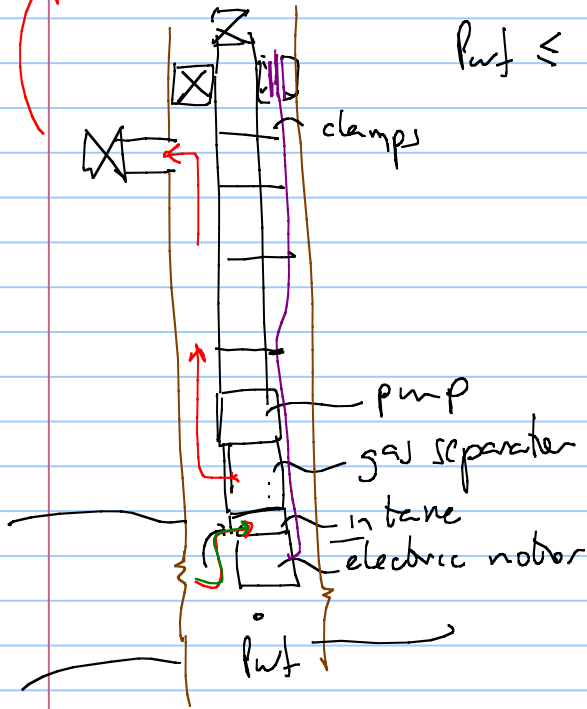


- LQ
- Drilling module
- Movable drill rig
- Electrical plant
- Wellheads
- Booster pumps
- Water Injection
- Uptime 99% bracket

producing gas through the annulus

$$P_{wf} \leq P_b(T_R)$$

bubble point pressure



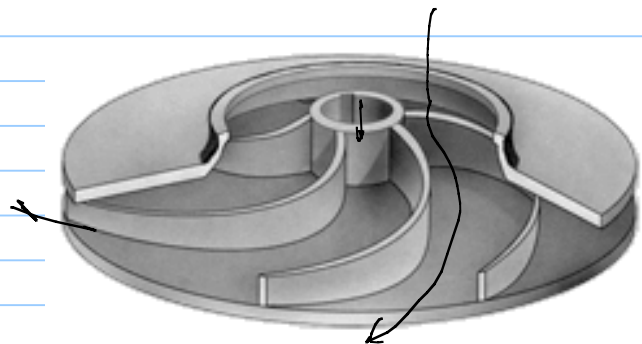
Armas

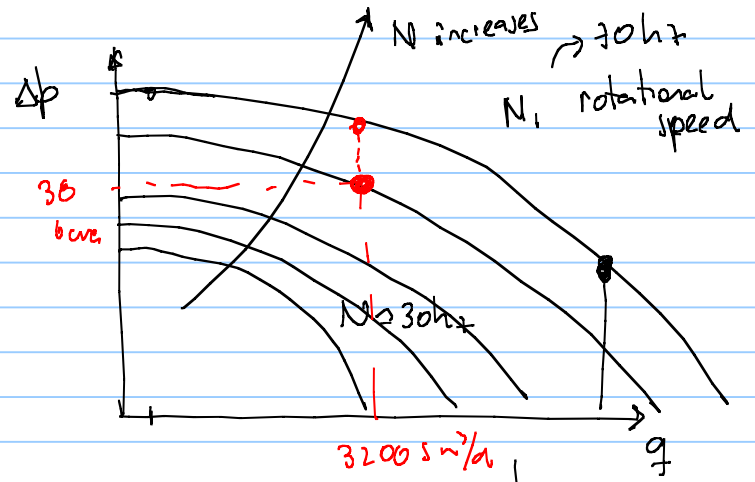
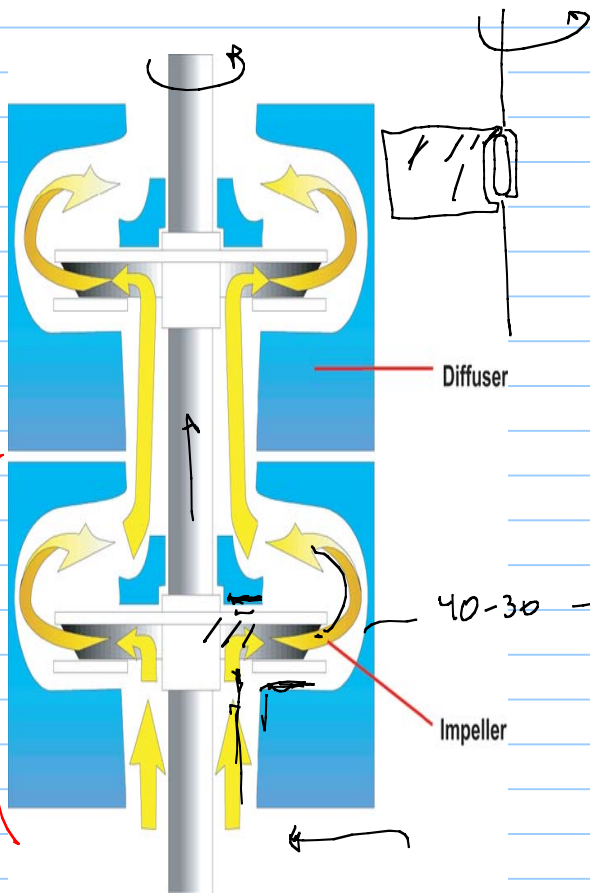
Aronutof ≈ 1930

Oklahoma

Reda pump

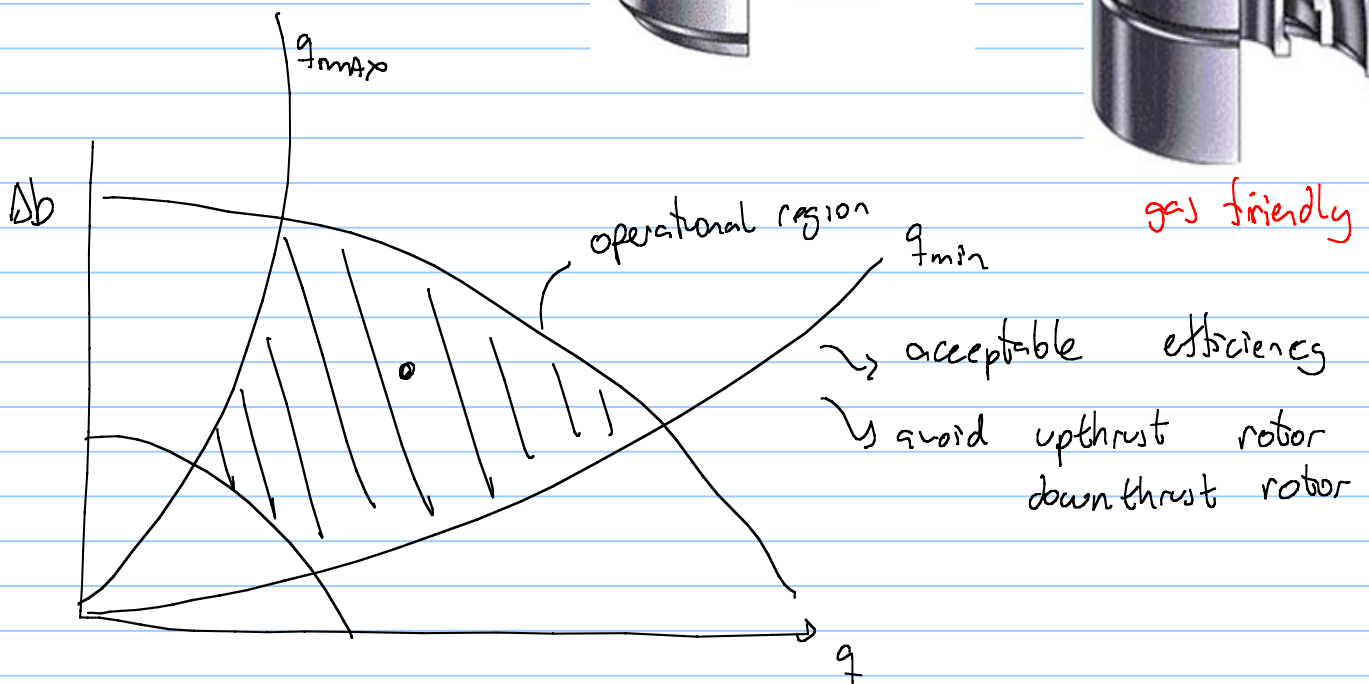
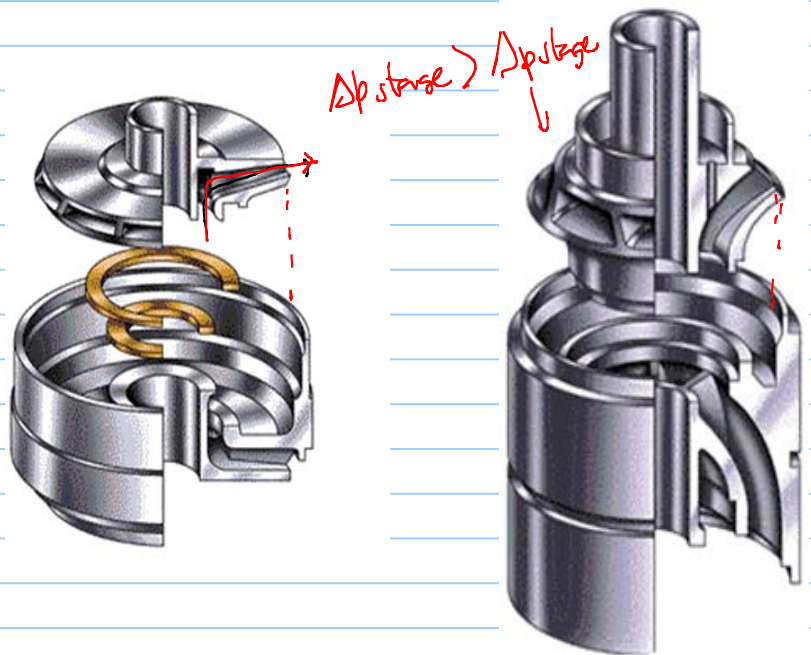
Schlumberger





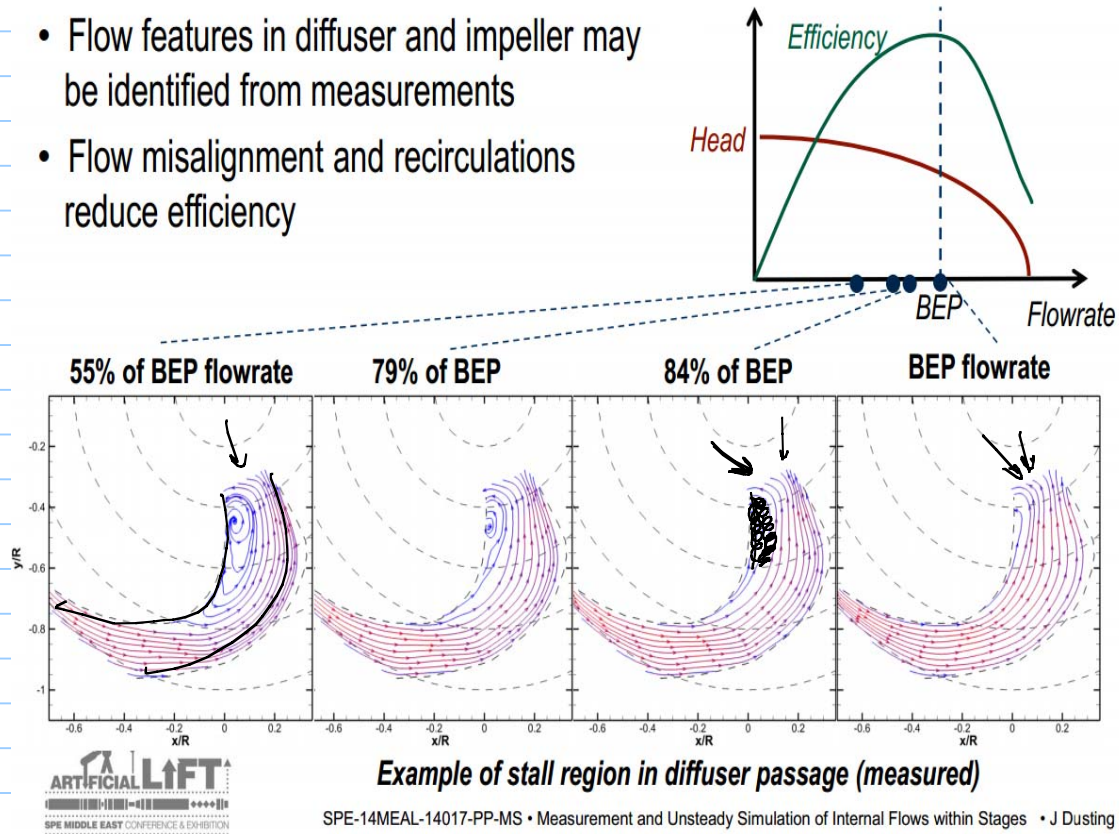
$$\text{Power} = q \Delta p$$

40-30 \rightarrow 100 stb

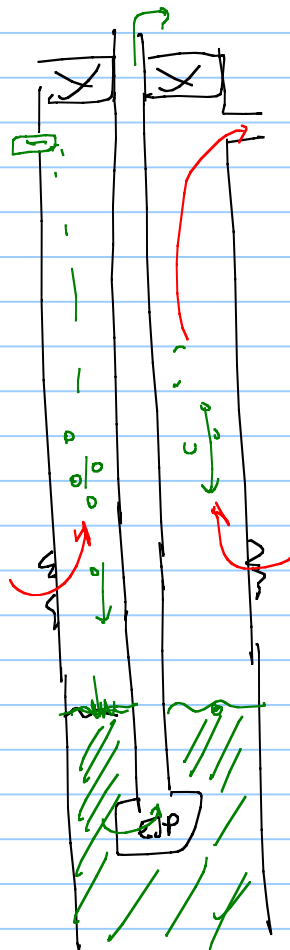


PIV measurement in a radial flow stage

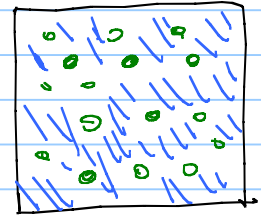
- Flow features in diffuser and impeller may be identified from measurements
- Flow misalignment and recirculations reduce efficiency



ESP are also used to drain liquid accumulated in gas wellbores



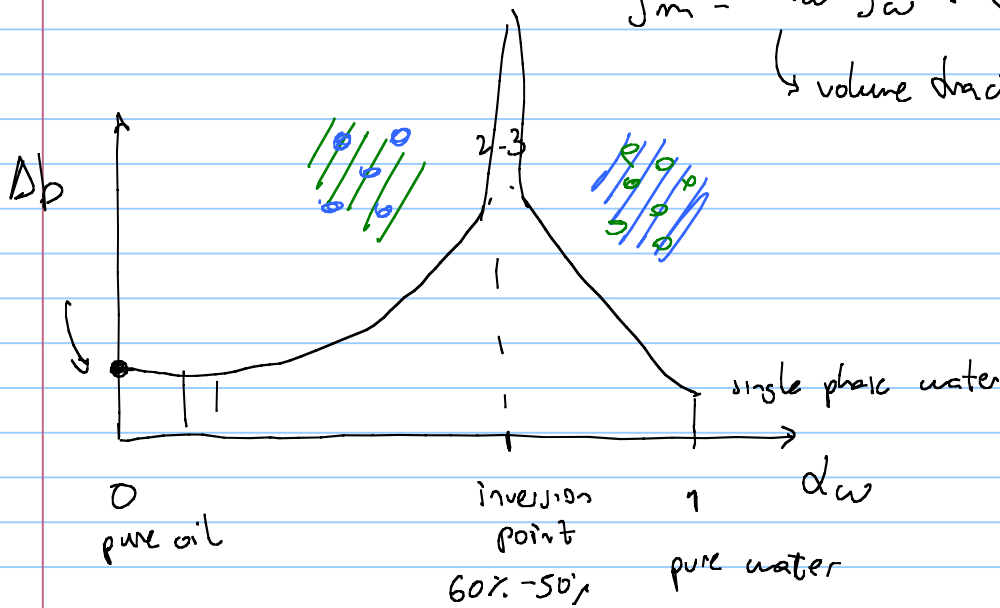
Pressure drop expressions for liquid are also useful to deal with
oil + water emulsions \rightarrow stable dispersion \rightarrow oil in water
water in oil



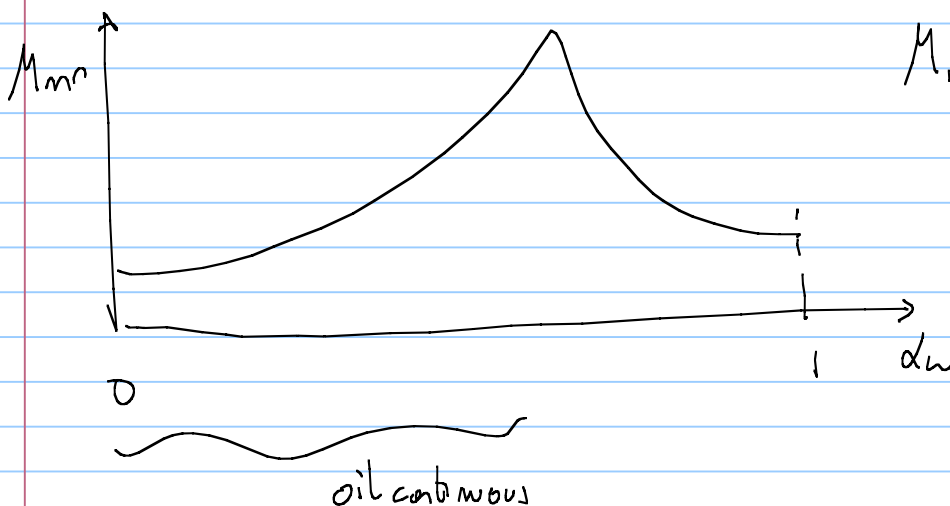
$$\frac{p_1}{\rho g} + z_1 + = \frac{p_2}{\rho g} + z_2 + \frac{f L}{D} \frac{V^2}{2g} \quad \leftarrow M_{\text{mixture}}$$

$$\rho_m = \alpha_w \rho_w + (1 - \alpha_w) \rho_o$$

\rightarrow volume fraction of water $\frac{q_w}{q_o + q_w} = \frac{10}{40} = 0.25$



oil continuous



$$\mu_m = \mu_o e^{\alpha_w}$$

water continuous

$$\mu_m = \mu_w e^{\alpha_o}$$

$$u_{fluid} = \frac{q}{\pi \phi^2} \leftarrow m^3/d \quad q_o \quad m^3/d$$



$$V_o(p, t) \rightarrow V_g(p_{sc}, T_{sc})$$

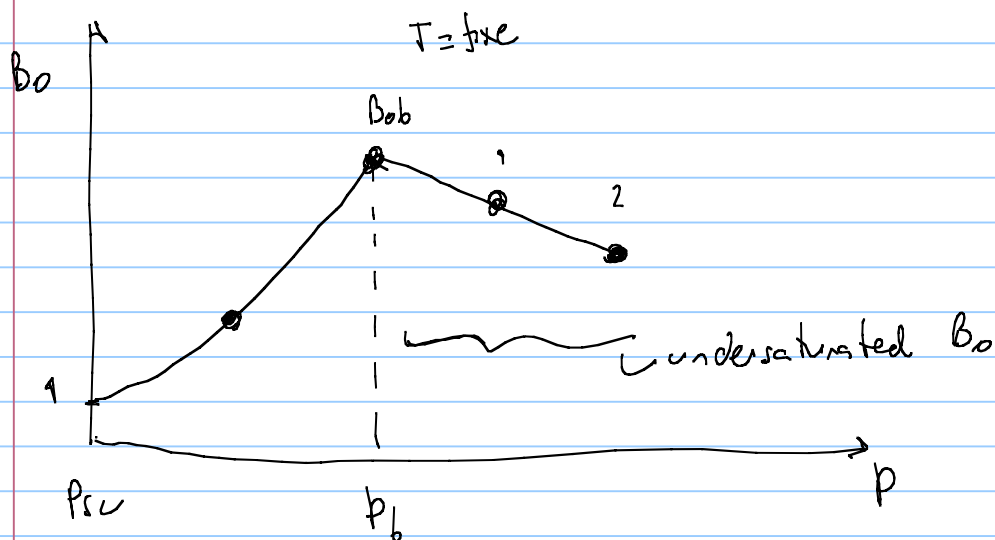
$$b_g = \frac{q_g(p, t)}{q_g(p_{sc}, T_{sc})} \ll 1$$

$$GOR = \frac{\bar{V}_g}{\bar{V}_o}$$

$$B_o = \frac{q_o(p, t)}{q_o(p_{sc}, T_{sc})}$$

oil volume factor
formation volume factor

oil
1.3-1.5 "Normal" $\rightarrow 600-900 \text{ scf/stb}$
1. $\rightarrow 1.05$ "low" $\rightarrow 5-150 \text{ scf/stb}$
1.7 $\rightarrow 2$ "high" $\rightarrow 2500 \rightarrow$



oil compressibility

$$C_o = -\frac{1}{V_o} \frac{\partial V_o}{\partial p} \quad \left\{ \begin{array}{l} \text{thermodynamic} \\ \text{definition} \end{array} \right.$$

$$V_o = B_o \cdot V_{sc}$$

$$C_o = -\frac{1}{V_{sc} B_o} \frac{\partial (B_o V_{sc})}{\partial p}$$

$$C_o = - \frac{1}{B_o} \frac{\partial B_o}{\partial p}$$

$$\int_{P_b}^{p > P_b} C_o \partial p = \int_{B_{ob}}^{B_o} - \frac{\partial B_o}{B_o}$$

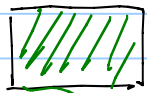
check

$$B_o = B_{ob} e^{C_o(P_b - p)}$$

$$f(SG_g, SG_o, GOR, p, T)$$

Black oil correlations

(P, T)

 P_{sc}, T_{sc} 

s.c

$$\frac{q}{A} \checkmark B_o$$

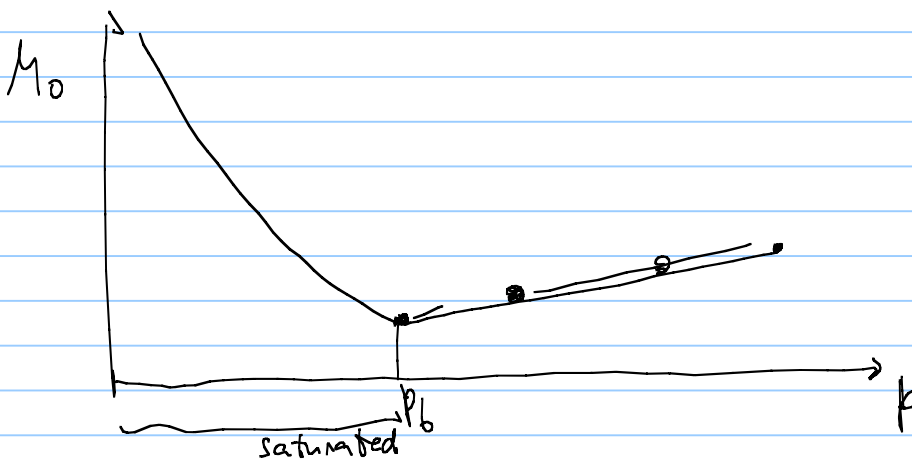
$$\rho_o = \frac{M_o}{V_o} = \frac{V_g \cdot \rho_g + V_o \cdot \rho_o}{V_o}$$

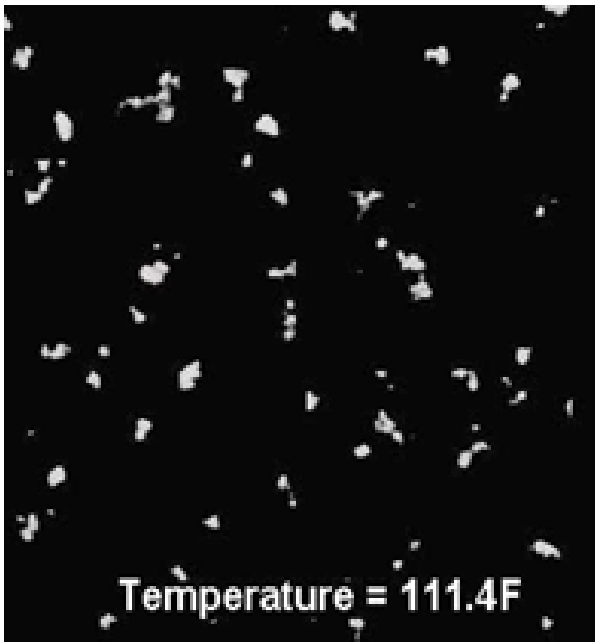
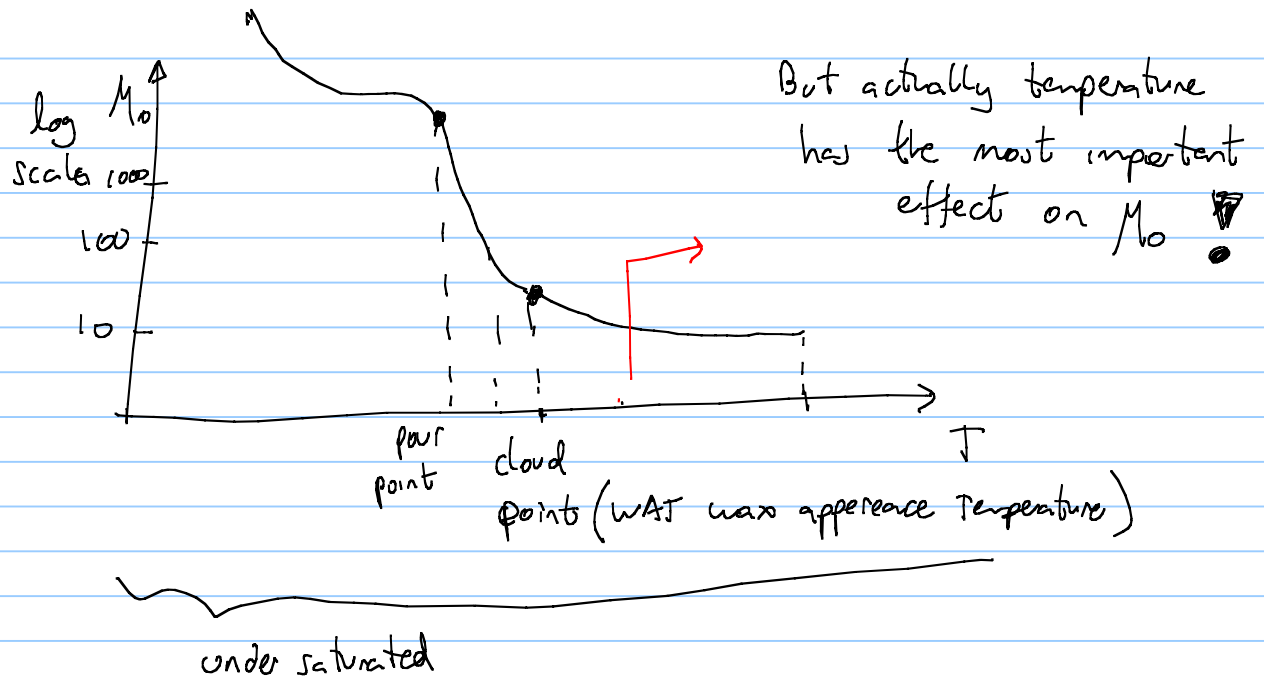
$$V_g = GOR \cdot V_o$$

$$Re = \frac{v \cdot \phi \cdot f}{\mu}$$

$$\rho_o = \frac{SG_g \cdot 1.224 \cdot GOR \cdot V_o + V_o \cdot SG_o \cdot 1000}{V_o}$$

$$\rho_o(p, T) = \frac{SG_g \cdot 1.224 \cdot GOR + SG_o \cdot 1000}{B_o}$$





cloud point



pour point (no flow)