

Day 5:

- Class exercise. Calculate u_g vs TVD for the example we made yesterday

gas velocity

at p, T

TVD	T	p	z	B _g	q _g	u _g
[m]	[K]	[bara]	[-]			
0	360	40	z _{fact standing}	-		
⋮	⋮	⋮		⋮		
2834	300	85 bara		-		

$q_g \cdot B_g(p, T) = q_g$
 (at S.C.)
 volume rate at local conditions

velocity of gas
 $u_g = \frac{q_g}{A} = \frac{q_g}{\pi \phi^2}$

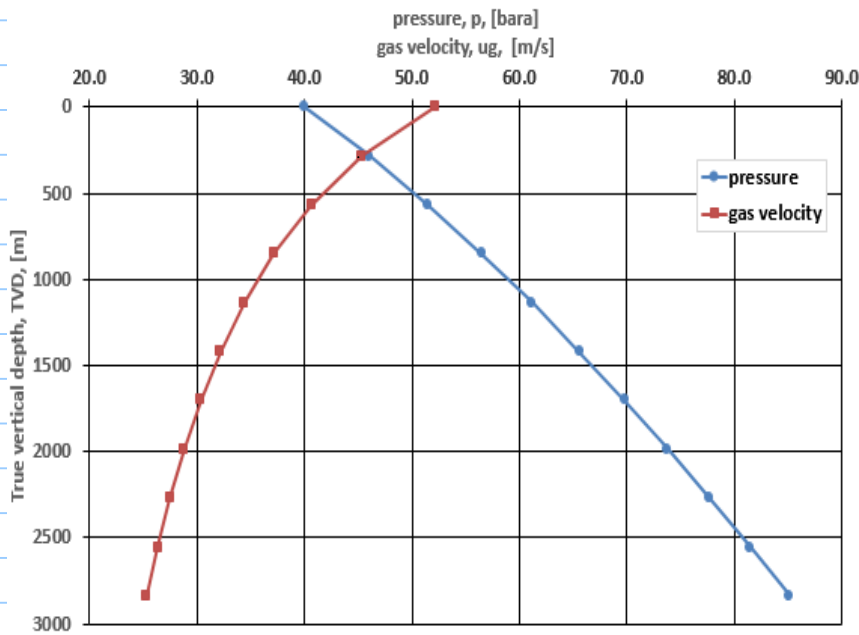
z

$\frac{m}{d} = \frac{24.3600 s}{\pi \phi^2}$

Tubing MD [m]	2837					
Tubing TVD [m]	2837					
Tubing ID [m]	0.157					
Tubing Cross section A [m ²]	0.019					
Wellhead pressure [bara]	40					
Gas gravity	0.55					
Twf [K]	378	104.85				
Twh [K]	360	86.85				
qg [Sm ³ /d]	2.85E+06					
liquid density [kg/m ³]	8.97E+02					
TVD	T	p	Z	B _g	qg _{local}	V _{local}
[m]	[K]	[bara]	[-]	[m ³ /Sm ³]	[m ³ /d]	[m/s]
0	360.0	40.0	0.9678	0.031	8.71E+04	52.1
284	361.8	46.0	0.9644	0.027	7.58E+04	45.3
567	363.6	51.5	0.9616	0.024	6.79E+04	40.6
851	365.4	56.5	0.9595	0.022	6.21E+04	37.1
1135	367.2	61.1	0.9577	0.020	5.75E+04	34.4
1418	369.0	65.6	0.9563	0.019	5.38E+04	32.2
1702	370.8	69.8	0.9552	0.018	5.08E+04	30.4
1986	372.6	73.8	0.9544	0.017	4.82E+04	28.8
2269	374.4	77.7	0.9537	0.016	4.60E+04	27.5
2553	376.2	81.4	0.9533	0.015	4.40E+04	26.3
2837	378.0	85.1	0.9531	0.015	4.23E+04	25.3

VBA func "z_{fact standing}"
 VBA func "B_g"
 $q_g \cdot B_g$
 $\frac{q_g}{A(24.3600)}$

checking if there is erosion in the tubing:



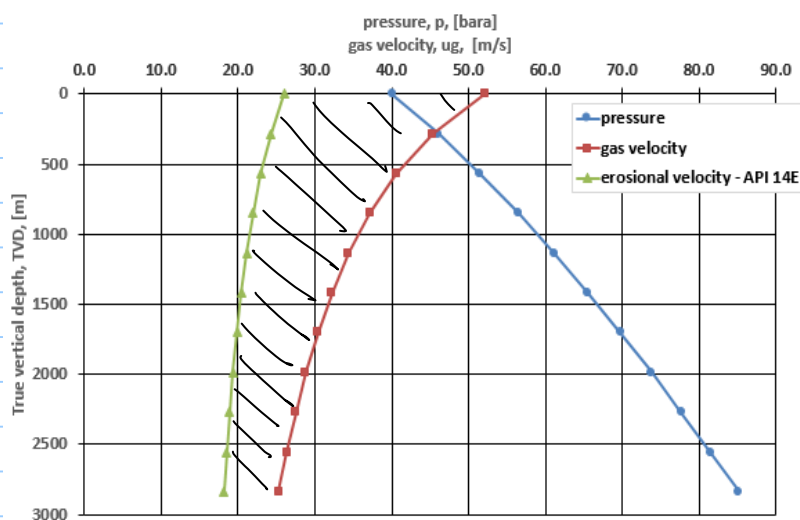
$$u_g \leq V_{\text{erosional}} = \frac{100}{\sqrt{\rho_g}}$$

↑
API

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liquid density [kg/m ³]	8.97E+02								
TVD	T	p	Z	Bg	qg_local	V_local	deng	Verosional	
[m]	[K]	[bara]	[-]	[m ³ /Sm ³]	[m ³ /d]	[m/s]	[kg/m ³]	[m/s]	
0	360.0	40.0	0.9678	0.031	8.71E+04	52.1	22.0	26.01	
284	361.8	46.0	0.9644	0.027	7.58E+04	45.3	25.3	24.26	
567	363.6	51.5	0.9616	0.024	6.79E+04	40.6	28.2	22.97	
851	365.4	56.5	0.9595	0.022	6.21E+04	37.1	30.9	21.96	
1135	367.2	61.1	0.9577	0.020	5.75E+04	34.4	33.3	21.13	
1418	369.0	65.6	0.9563	0.019	5.38E+04	32.2	35.6	20.45	
1702	370.8	69.8	0.9552	0.018	5.08E+04	30.4	37.7	19.86	
1986	372.6	73.8	0.9544	0.017	4.82E+04	28.8	39.8	19.35	
2269	374.4	77.7	0.9537	0.016	4.60E+04	27.5	41.7	18.89	
2553	376.2	81.4	0.9533	0.015	4.40E+04	26.3	43.5	18.49	
2837	378.0	85.1	0.9531	0.015	4.23E+04	25.3	45.3	18.13	

VBA funct
VBA function "Verosional (ρ_g)"

deng (ρ, μ, Z, Bg)



Checking Turner criteria. Minimum gas velocity required to lift liquid droplet.

$$V = 5.46 \left[\frac{\sigma^{0.25} (P_L - P_g)^{0.25}}{\rho_s^{0.5}} \right] \quad \text{if } V_g > V_{\text{turner}}$$

~ constant

from correlation

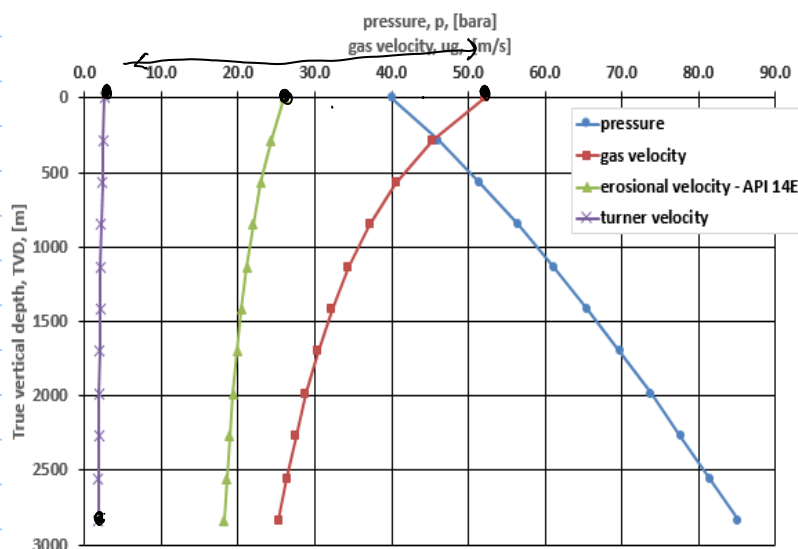
```

' Oil-Gas interfacial tension in N/m
Function STog(DenO, deng)
'Density of the oil, kg/m^3
'Density of the gas, kg/m^3

STog = (567 * (DenO - deng) * 0.001 / 213) ^ 4
STog = 0.001 * STog
End Function

```

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liquid density [kg/m^3]	8.97E+02											
TVD	T	p'	Z	Bg	qg_local	V_local	deng	Verosional	int_ten_o_g	Vturner		
[m]	[K]	[bara]	[-]	[m^3/Sm^3]	[m^3/d]	[m/s]	[kg/m^3]	[m/s]	[N/m]	[m/s]		
0	360.0	(40.0)	0.9678	0.031	8.71E+04	52.1	22.0	26.01	0.029	2.6		
284	361.8	46.0	0.9644	0.027	7.58E+04	45.3	25.3	24.26	0.029	2.4		
567	363.6	51.5	0.9616	0.024	6.79E+04	40.6	28.2	22.97	0.029	2.3		
851	365.4	56.5	0.9595	0.022	6.21E+04	37.1	30.9	21.96	0.028	2.2		
1135	367.2	61.1	0.9577	0.020	5.75E+04	34.4	33.3	21.13	0.028	2.1		
1418	369.0	65.6	0.9563	0.019	5.38E+04	32.2	35.6	20.45	0.028	2.0		
1702	370.8	69.8	0.9552	0.018	5.08E+04	30.4	37.7	19.86	0.027	2.0		
1986	372.6	73.8	0.9544	0.017	4.82E+04	28.8	39.8	19.35	0.027	1.9		
2269	374.4	77.7	0.9537	0.016	4.60E+04	27.5	41.7	18.89	0.027	1.9		
2553	376.2	81.4	0.9533	0.015	4.40E+04	26.3	43.5	18.49	0.027	1.8		
2837	378.0	85.1	0.9531	0.015	4.23E+04	25.3	45.3	18.13	0.026	1.8		



offshore gas well

typical production

3.66 Sm^3/d

30 mm scf/d

Production choke types $\left\{ \begin{array}{l} \text{Positive / bean choke} \\ \text{Adjustable} \end{array} \right.$

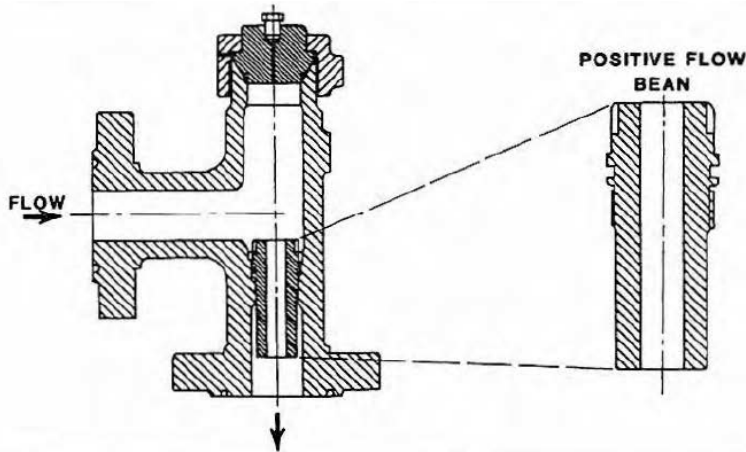
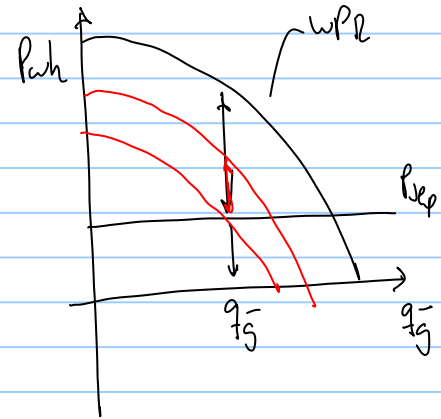
Bean



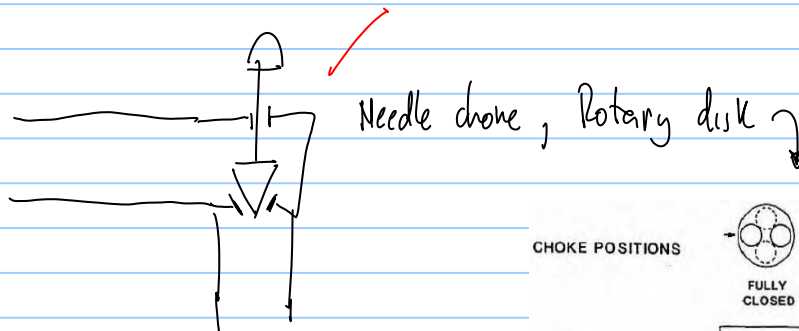
orifice size
 $\frac{1}{8}'' \sim 2''$

Steps $\frac{1}{64}''$

$\frac{8}{64}'' \rightarrow \frac{256}{64}''$

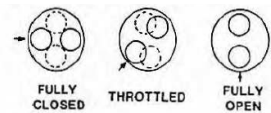


Adjustable

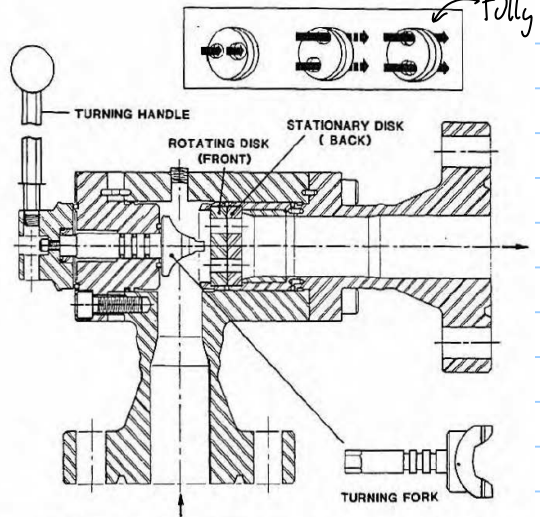


Needle choke, Rotary disk

CHOKE POSITIONS

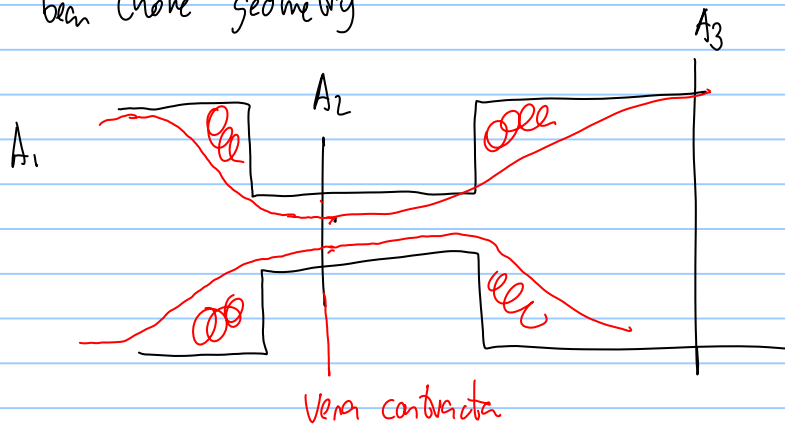


fully choked



Cage choke

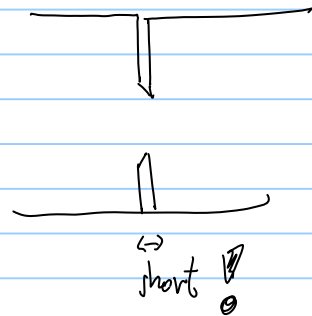
focusing on bean choke geometry



Different than

o

orifice for metering

main function of choke: dissipate a lot of energy in a concentrated place $\downarrow p$

control production

undesired consequences

p drops $\rightarrow$ in oil you get gas vaporization

$\rightarrow$ if gas you get liquid condensation

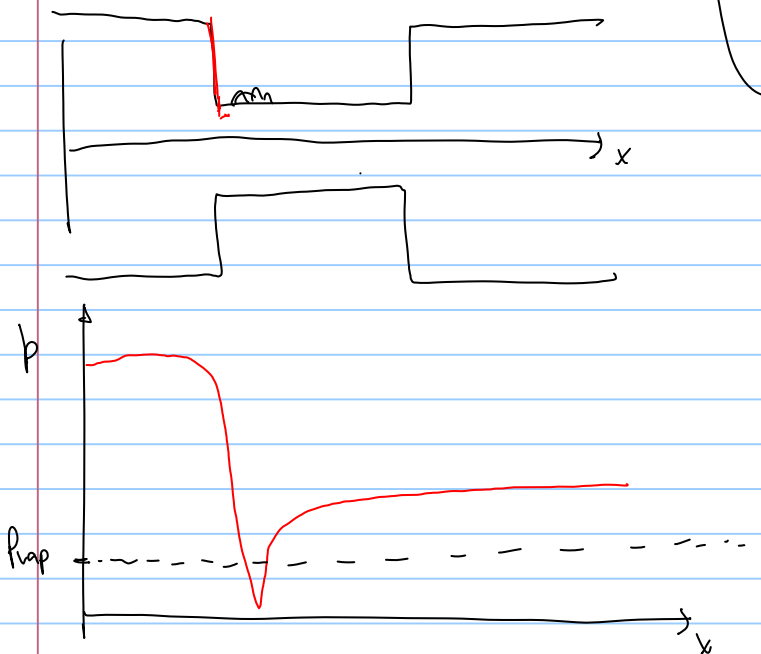
erosion $\rightarrow$ due to high velocities in chokes
sand - worsens the problem.

cooling $\rightarrow$ for gas Joule-Thomson effect

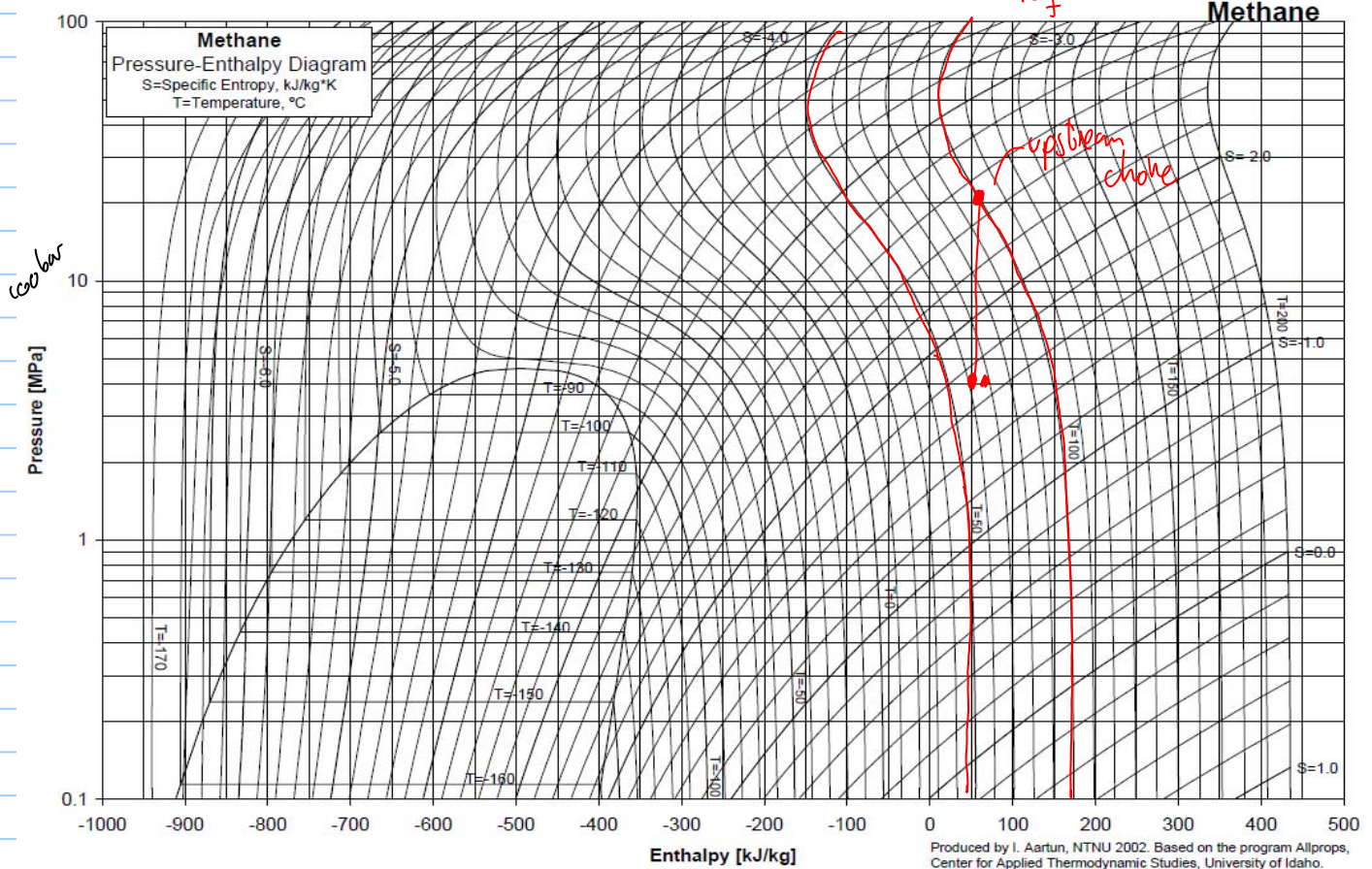
$\rightarrow$ more liquid condensation

$\rightarrow$ free water + low $T \rightarrow$ ice block!

cavitation.



p vs. h diagram



the process in the choke is isenthalpic (no $\dot{q}$ or $\dot{w}$ transferred out of the control volume)

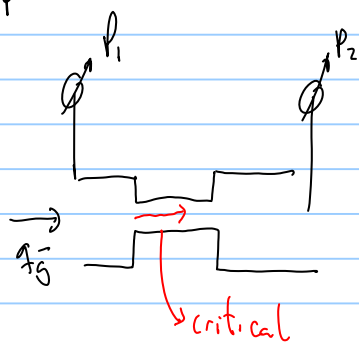
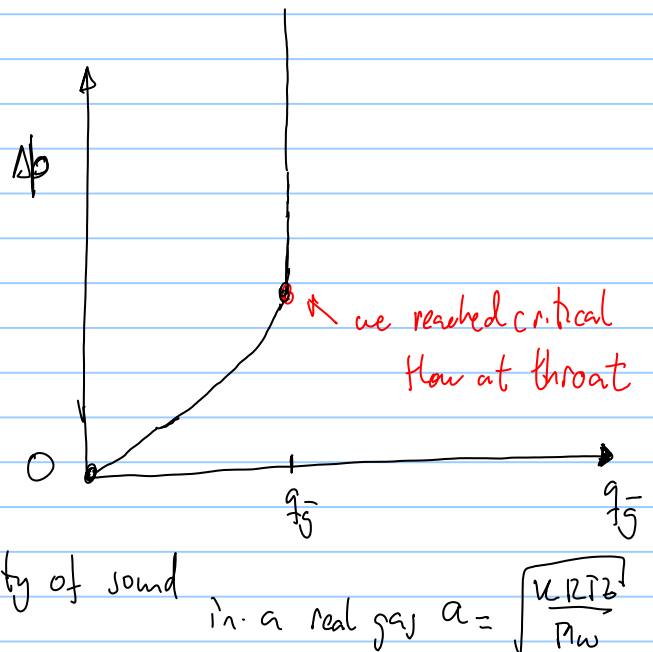
1st law of thermodynamics for open systems

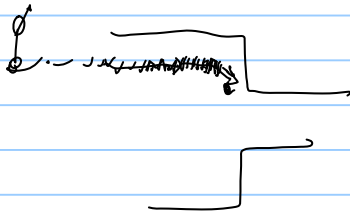
$$\dot{m}(h_2 - h_1) = \dot{q} - \dot{w}$$

0 0

$h_2 = h_1$!

Experiment

 P_1 is fixed



$$K = \frac{C_p}{C_v}$$

$$a \quad K=1.6$$

$$R=8314.3$$

$$T=80+273.15$$

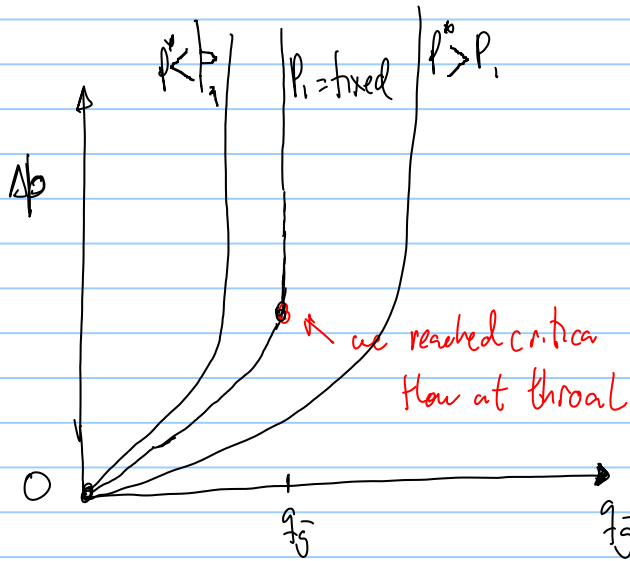
$$n=1.6$$

as a rule of thumb critical pressure ratio 1)

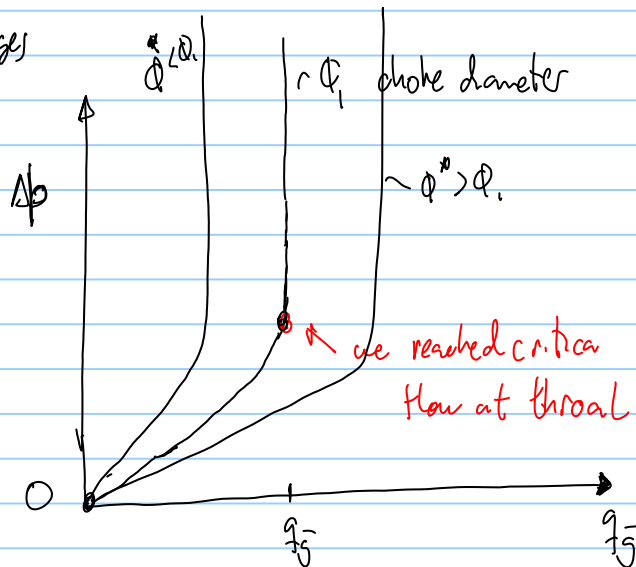
$$a \approx 542 \text{ m/s}$$

$$\frac{P_2}{P_1} \approx 0.5 \quad \checkmark$$

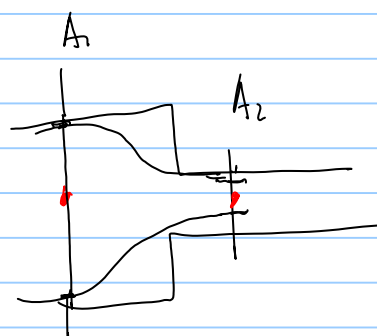
$$\text{in gas} \quad \left(\frac{P_2}{P_1} \right)_c = \left(\frac{2}{K+1} \right)^{\frac{K}{K-1}}$$



if the orifice changes



Choke equation for liquid:



$$dp + \frac{\rho}{2} u du + f \frac{L}{D} \frac{\rho u^2}{2} = 0$$

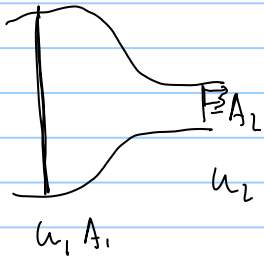
distance short no frictional losses

$$\int_1^2 \frac{dp}{\rho} + \int_1^2 u du = 0$$

$$p_2 - p_1 = \rho_L \cdot 0.5 \cdot (u_1^2 - u_2^2)$$

q_{sc} vs Δp

mass balance



$$u_2 \cdot A_2 = u_1 \cdot A_1$$

$$(u_1)^2 = \left(\frac{d_2^2}{d_1^2} u_2 \right)^2$$

$$\beta = \frac{d_2}{d_1}$$

$$A_1 = \frac{\pi \cdot d_1^2}{4}$$

$$A_2 = \frac{\pi \cdot d_2^2}{4}$$

$$u_1^2 = \beta^4 u_2^2$$

$$p_2 - p_1 = \rho_L \cdot 0.5 (\beta^4 u_2^2 - u_2^2)$$

$$\frac{\Delta p}{\rho_L (1 - \beta^4)} = u_2^2$$

$$u_2 = \sqrt{\frac{\Delta p \cdot 2}{\rho_L (1 - \beta^4)}}$$

$$q_{sc} = u_2 \cdot A_2 \cdot C_d$$

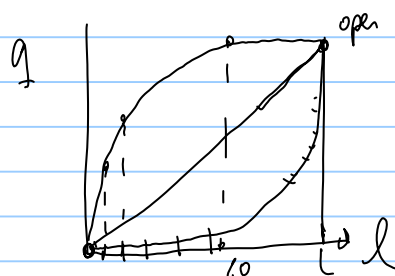
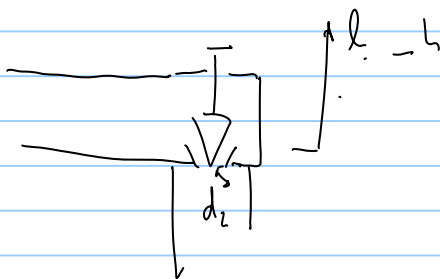
↑ flow coefficient

to account for
vena contraction

$$q = A_2 C_d \sqrt{\frac{\Delta p \cdot 2}{\rho_L (1 - \beta^4)}}$$

in adjustable chokes d_2 is changing

$$q = f(l) \cdot C_d \sqrt{\frac{\Delta p \cdot 2}{\rho}}$$



if Δp is fixed

Derivation of chone equation for gas $\rightarrow$ orifice

$$\int_1^2 \frac{dp}{\rho} + \int_1^2 u du$$

$$\int_1^2 \frac{dp}{\rho} = 0.5 (u_1^2 - u_2^2)$$

$$u_2 \gg u_1 \quad u_2^2 \gg u_1^2$$

$$\rho = \frac{p M_w}{R T}$$

$$u_2^2 - u_1^2 \approx u_2^2$$

$$p v^n = \text{constant}$$

$$n = \kappa$$

adiabatic: $p \frac{1}{\rho^\kappa} = \text{constant} = C$ $\rho = \frac{p^{1/\kappa}}{C}$

$$C^{1/\kappa} \int_1^2 \frac{dp}{p^{1/\kappa}} = C^{1/\kappa} \left(\frac{\kappa}{\kappa-1} \right) \left(p_2^{\frac{\kappa-1}{\kappa}} - p_1^{\frac{\kappa-1}{\kappa}} \right)$$

$$C^{1/\kappa} \frac{\kappa}{\kappa-1} p_1^{\frac{\kappa-1}{\kappa}} \left(\left(\frac{p_2}{p_1} \right)^{\frac{\kappa-1}{\kappa}} - 1 \right) \quad y = \frac{p_2}{p_1}$$

$$C^{1/\kappa} = \frac{p_1^{1/\kappa}}{\rho_1^{1/\kappa}}$$

$$-u_2^2 = 2 \frac{p_1}{\rho_1} \frac{\kappa}{\kappa-1} \left(y^{\frac{\kappa-1}{\kappa}} - 1 \right) \quad \rho_1 = \frac{p_1 M_w}{R T_1}$$

$$u_2 = \sqrt{2 \frac{p_1}{\rho_1} \frac{\kappa}{\kappa-1} \left(y^{\frac{\kappa-1}{\kappa}} - 1 \right)}$$

$$u_2 = \frac{\dot{m}}{\rho_2 \cdot C_d A_2}$$

$$p \rho^\kappa = \text{Constant}$$

$$p_1 \rho_1^\kappa = p_2 \rho_2^\kappa$$

$$\rho_1 = \frac{p_1 M_w}{R T_1}$$

$$\rho_2 = \left(\frac{p_1}{p_2} \right)^{1/\kappa} \rho_1$$

$$\dot{m} = q_{sc} \cdot f_{sc}$$

$$\frac{p_{sc} M}{T_{sc} \sqrt{g}} \cdot R$$

$$q_{sc} = c_d A_2 p_1 \left(\frac{T_{sc}}{p_{sc}} \right) \sqrt{2 \frac{R}{M_g Z_1 T_1}} \sqrt{\left(\frac{k}{k-1} \right) \left[(y)^{\frac{2}{k}} - (y)^{\frac{k+1}{k}} \right]}$$

$$A_2 = \frac{\pi d_2^2}{4}$$

if $y > y_c (\approx 0.5)$

then use this equation

if $y \leq y_c$

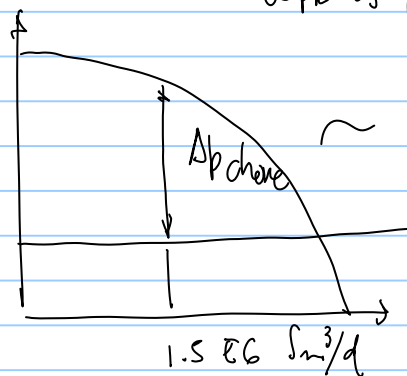
then use this equation with

$$y = y_c$$

Exercise

I performed

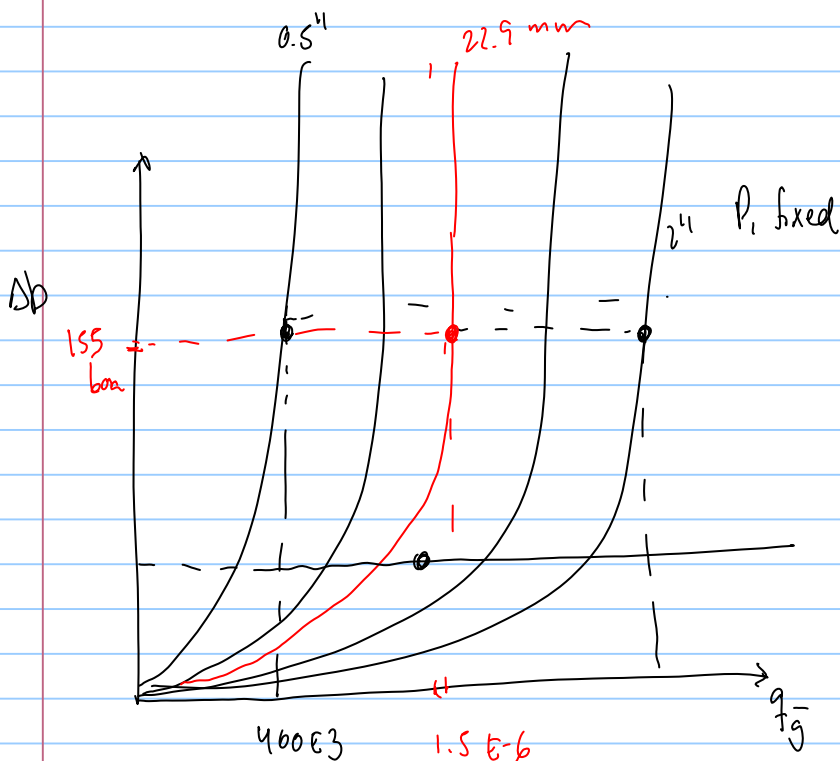
w PR vs P dep



$p_{h, avail} = 205 \text{ bara}$

$p_{h, req} = 40 \text{ bara}$

$\Delta p = 155 \text{ bara}$



Excel Solver dialog box for the Choke Performance Equation - Dry Gas -Metric.

Set Objective: \$E\$16

To: ☐ Max ☐ Min ☒ Value Of: 1.5e6

By Changing Variable Cells: \$C\$13

Subject to the Constraints:

☒ Make Unconstrained Variables Non-Negative

Select a Solving Method: GRG Nonlinear

Solving Method: Select the GRG Nonlinear engine for Solver Problems that are smooth nonlinear. Select the LP Simplex engine for linear Solver Problems, and select the Evolutionary engine for Solver problems that are non-smooth.

Solve button is highlighted.

Choke Performance Equation - Dry Gas -Metric					
C _D Discharge Coefficient		0.865			
C _s		1.6259			
p _{sc} , Standard conditions pressure		101.325 kPa			
T _{sc} , Standard conditions temp		288.71 °K			
C _n		4.0075			
k, Adiabatic Constant		1.300			
Gas Gravity, Gamma		0.55	Air=1.0		
T _i , choke temperature		86.85 C		360 °K	
y _c Critical Ratio		0.546			
p ₂ , Downstream pressure		40 bara		4000 kPa	
d, ChokeDiameter	mm	12.5			
	p1	p1	y	Z1	q _{sc}
	bara	kPa	[]	[]	Sm ³ /d
	205.0	20500	0.195	0.9281	446.8E+3

Home exercise

Using the same data shown before $P_1 = 205 \text{ bara}$

$P_2 = 40 \text{ bara}$

$d_2 = 22.9 \text{ mm}$

make the following plot

