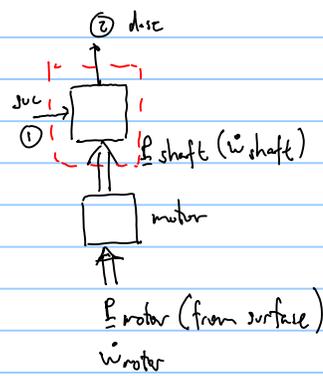
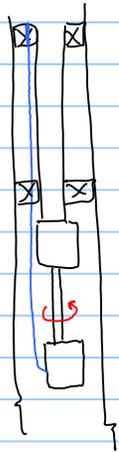


Hydraulic efficiency



$$\eta_H = \frac{P_{pump}}{P_{shaft}}$$

$$\eta_m = \frac{P_{shaft}}{P_{motor}} \approx 0.95 - 0.98$$

$$Q + \dot{w} + \dot{E}_1 - \dot{E}_2 = 0$$

$$\dot{w}_{shaft} = \dot{E}_2 - \dot{E}_1 = \dot{m} (e_2 - e_1)$$

$$e = \left(g \cdot z + \frac{V^2}{2} + h \right)$$

\downarrow \downarrow \downarrow
 0 0 $u + p \cdot v$

ideal pumping process $\Delta s = 0$ isentropic

$$\Delta h = 0 \quad u = f(T)$$

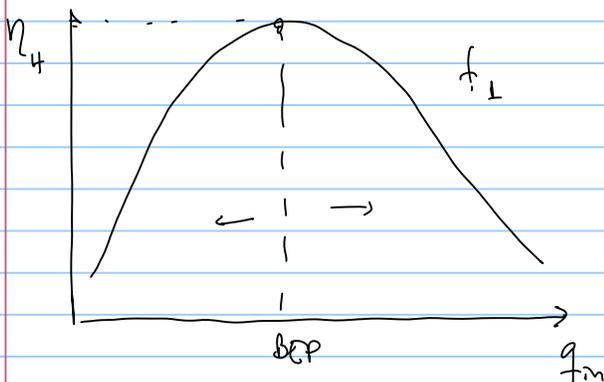
$$\dot{w}_{ideal} = \dot{m} (P_2 v_2 - P_1 v_1)$$

$$v = \text{constant} = \frac{1}{\rho}$$

$$\dot{w}_{ideal} = \dot{q} (P_2 - P_1)$$

$$\eta_H = \frac{\dot{q} (P_2 - P_1)}{P_{shaft}} \approx 0.4 - 0.8$$

- ↳ friction: vanes, base impeller
- ↳ volumetric: leakage in pump
- ↳ turbulence, recirculation



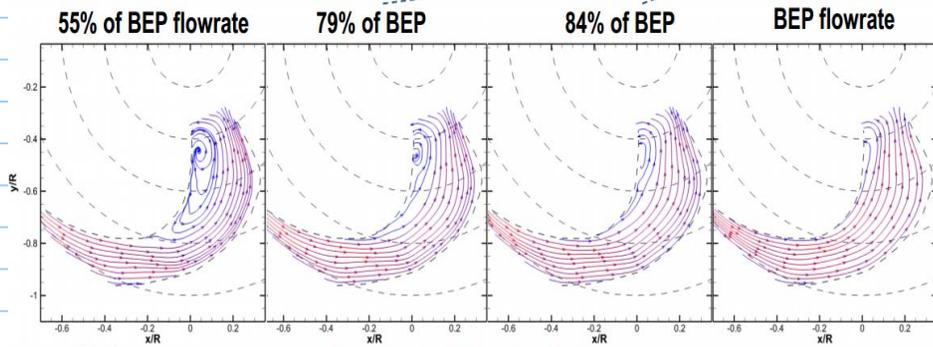
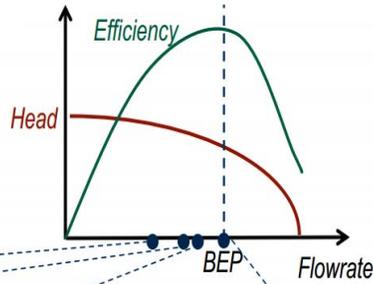
$$\eta_H = b_1 q^2 + b_2 q + b_3$$

$$\dot{w}_{shaft} = \frac{\Delta p \cdot \dot{q}}{\eta_H}$$

$$\dot{w}_{motor} = \frac{\dot{w}_{shaft}}{\eta_m}$$

PIV measurement in a radial flow stage

- Flow features in diffuser and impeller may be identified from measurements
- Flow misalignment and recirculations reduce efficiency



Example of stall region in diffuser passage (measured)

SPE-14MEAL-14017-PP-MS • Measurement and Unsteady Simulation of Internal Flows within Stages • J Dusting

analytical

$$Q_B = Q_A \cdot \frac{n_B}{n_A}$$

$$H_B = H_A \cdot \left(\frac{n_B}{n_A}\right)^2$$

$$P_B = P_A \cdot \left(\frac{n_B}{n_A}\right)^3$$

Similarity law

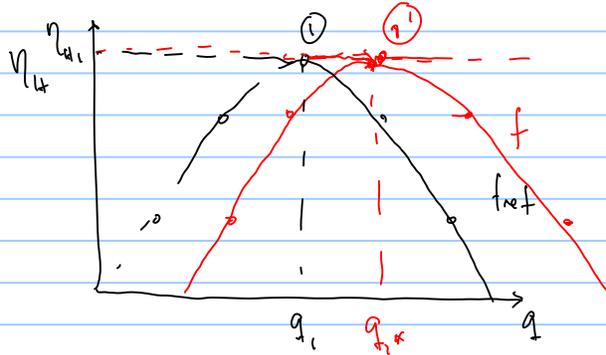
$$\eta_{Href} = \frac{q_{ref} \cdot \Delta h_{ref}}{P_{shaft ref}}$$

$$\eta_{Hof} = \frac{q \Delta h}{P_{shaft}}$$

$$\eta_{Hof} = \frac{q_{ref} \frac{f}{f_{ref}} \Delta h_{ref} \left(\frac{f}{f_{ref}}\right)^2}{P_{shaft ref} \left(\frac{f}{f_{ref}}\right)^3}$$

W shaft

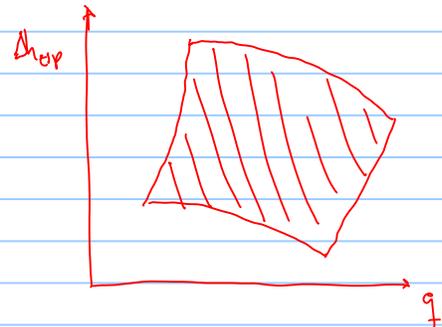
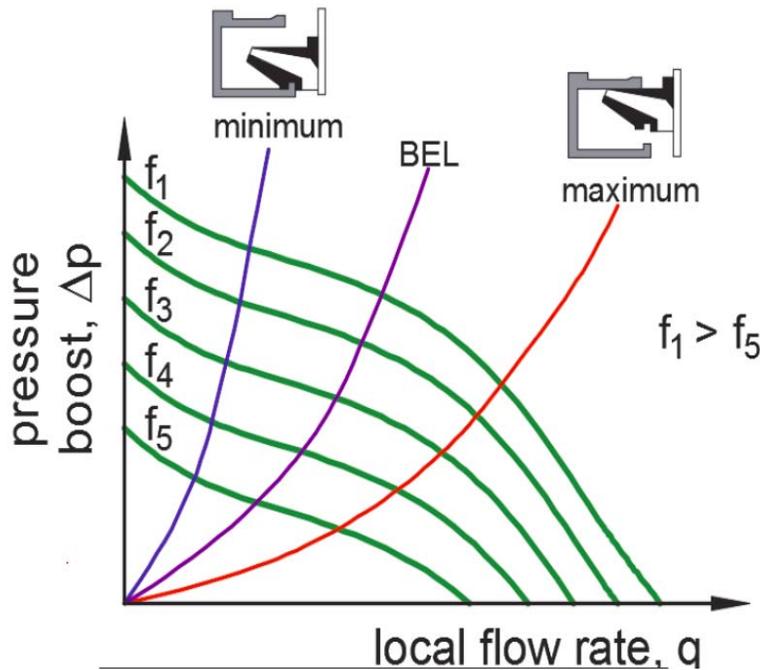
$$\eta_{Hof} = \eta_{Hof ref}$$

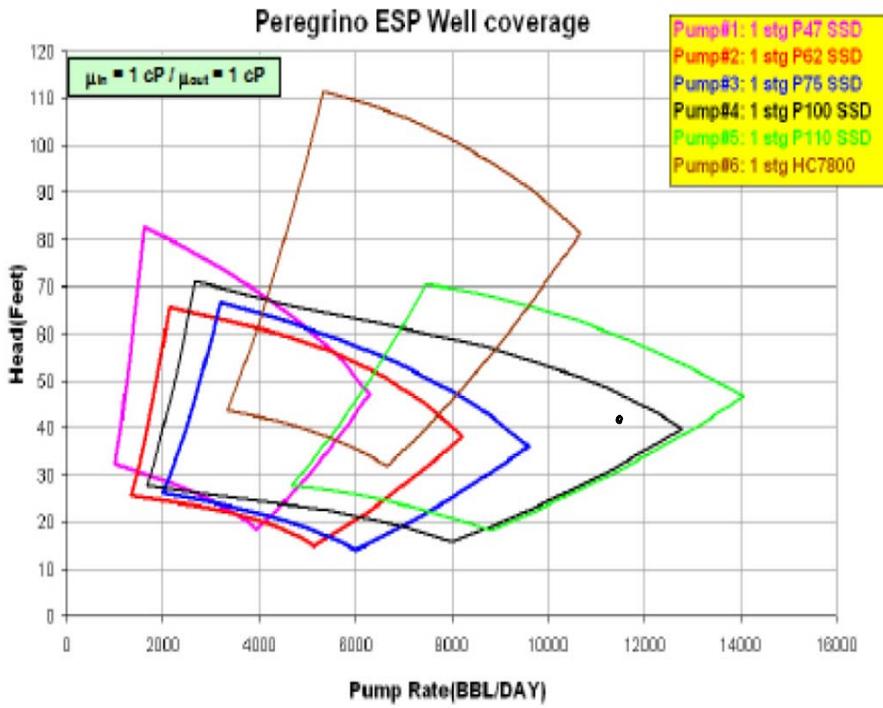


$$\eta_{H, ref of} = \eta_{H, of ref}$$

$$q_{1, of ref}$$

$$q_{1, of} = q_{1, of ref} \cdot \frac{f}{f_{ref}}$$



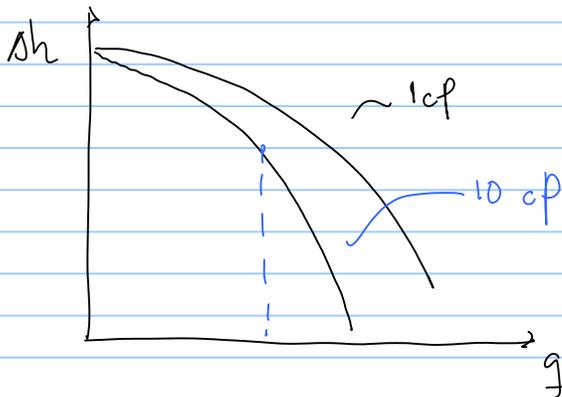


SPE-173948-MS

ESP Application on Heavy Oil in Peregrino Field

Vinicius Castro, and Daniela Leite, Statoil; Daniel Lemos, Jean Marins, Rui Pessoa, and João Magalhães, Baker Hughes

the viscosity of fluid also affects the performance of pump



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American National Standard (Guideline) for
**Effects of Liquid Viscosity on
Rotodynamic (Centrifugal and Vertical)
Pump Performance**