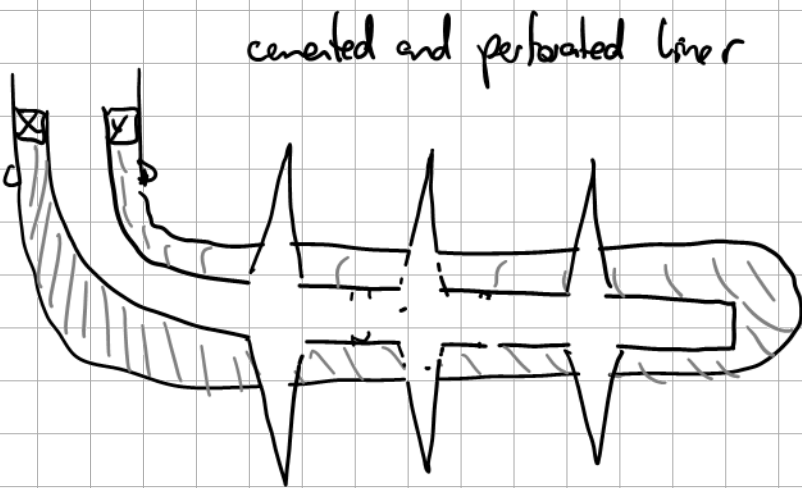
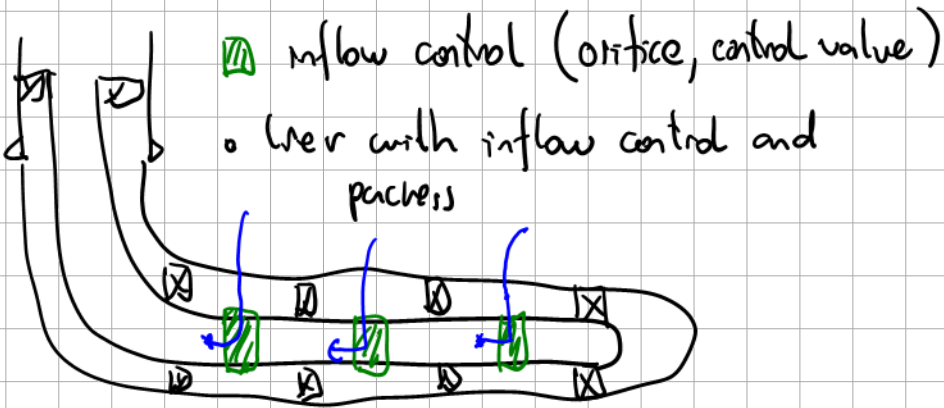
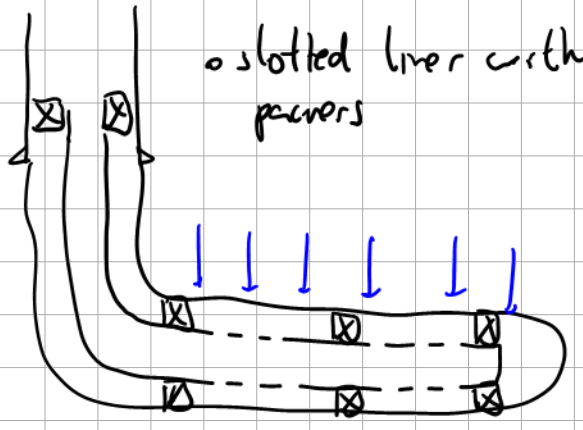
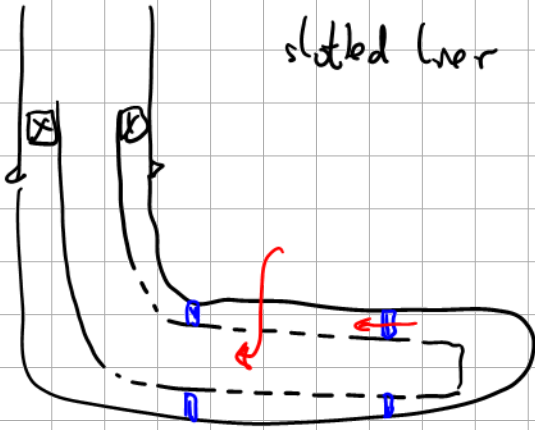
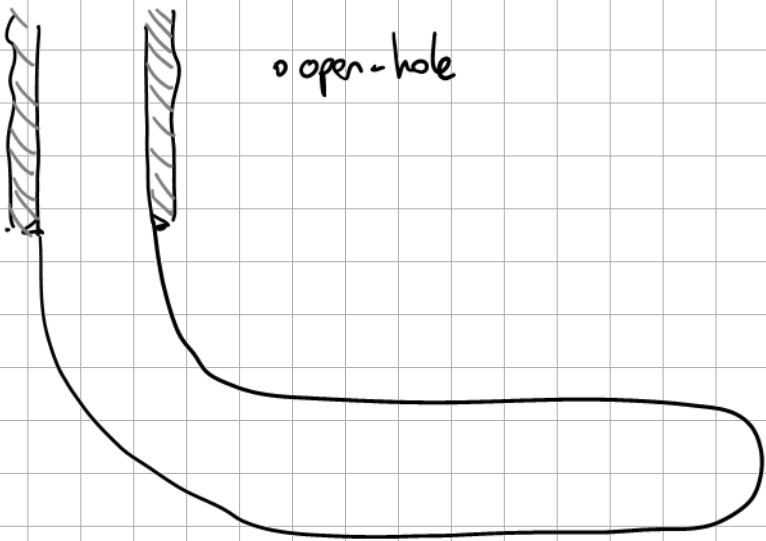
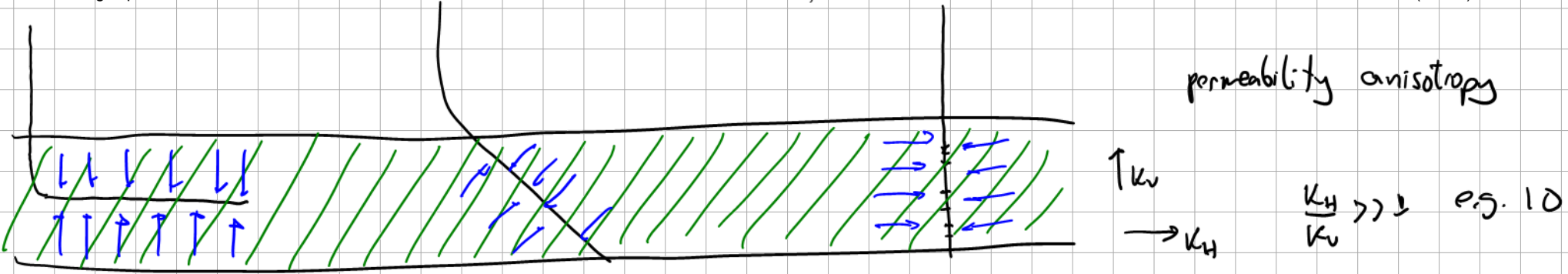
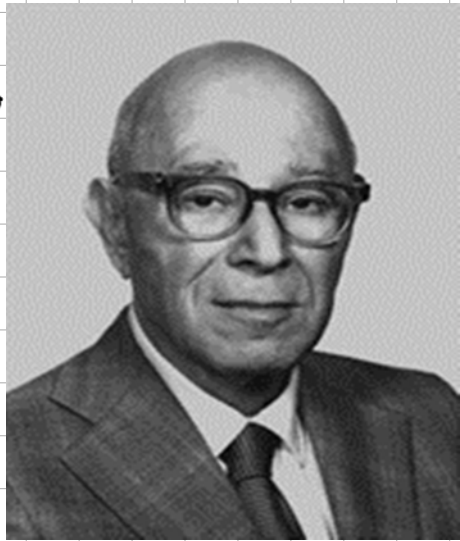


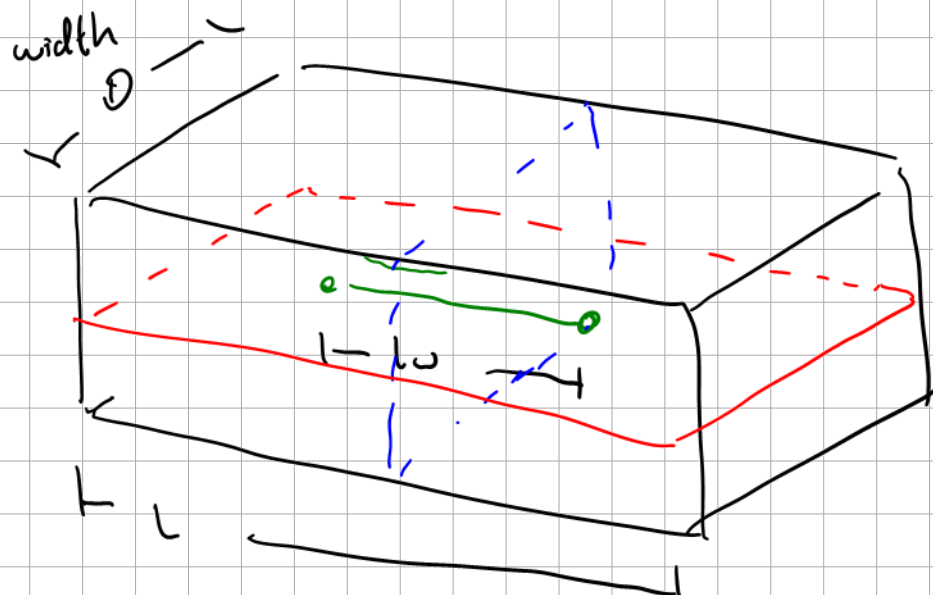


- 1937 - Muskat (1937) (Gulf oil)
- 1958 - Merkulov
- 1964 - Borisov
- 1974 - Gringarten (Imperial College), Ramey (Stanford)
- 1983 - Giger (IFP)
- 1988 - Joshi
- 1989 - Babuh, Odeh (Mobil)
- 1991 - Renard, Dupuy (IFP)
- 1994 - Buttler
- Harald Asheim (NTNU)

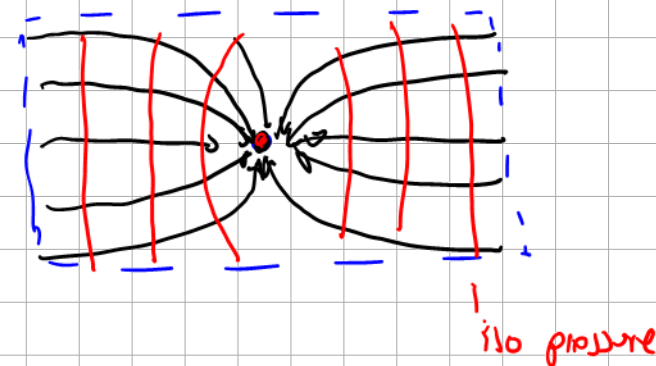
Morris



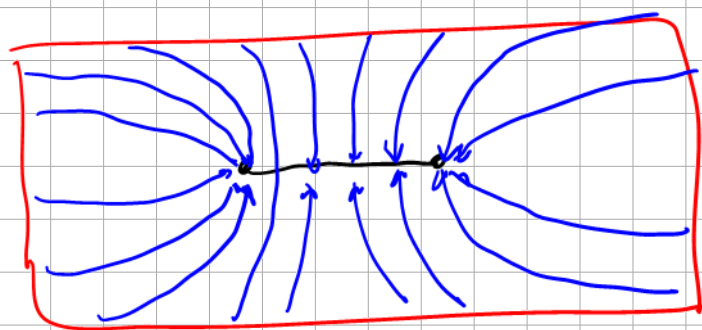
<http://www.ipt.ntnu.no/~asheim/prodbr.html>



k_v
 $\rightarrow k_h$



$$p = f(x)$$

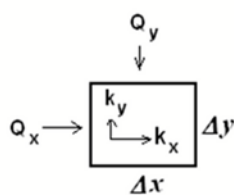


$$p = f(x)$$

Superposition

Strategy to deal with permeability anisotropy

- Actual reservoir element



- Homogenous equivalent:

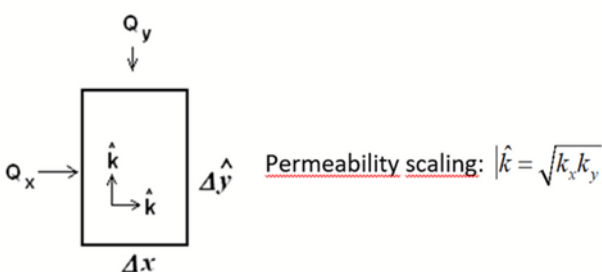
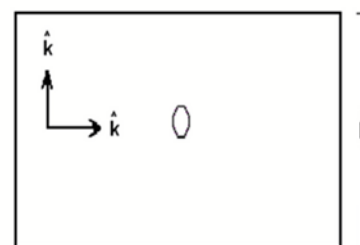


Figure 3.10 Anisotropic reservoir

$$k_H \frac{\partial^2 p}{\partial x^2} + k_V \frac{\partial^2 p}{\partial y^2} = \phi \mu c \frac{\partial p}{\partial t}$$

$$\frac{\partial^2 p}{\partial x^2} + \frac{\partial^2 p}{\partial (\sqrt{k_H / k_V} y)^2} = \frac{\phi \mu c}{k_H} \frac{\partial p}{\partial t}$$



$$\frac{\partial^2 p}{\partial x^2} + \frac{\partial^2 p}{\partial \hat{y}^2} = 0$$

$$\hat{y} = (k_H / k_V)^{0.5} y$$

$$\text{Height scaling: } \hat{h} = (k_H / k_V)^{0.5} h$$

Harald Asheim's IPR equation

- undersaturated oil
- horizontal well
- ps
- scaling due to anisotropy

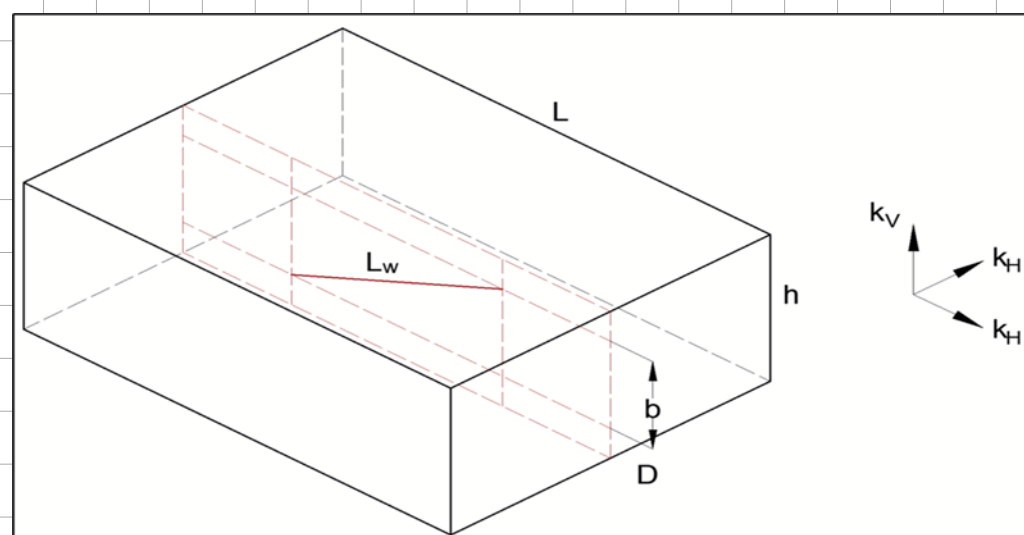
$$q_o = \frac{k_H \cdot h}{6.22 \cdot (\mu_o \cdot B_o)_{@p_{av}} \cdot \left[\frac{\pi \cdot D \cdot \hat{f}_a}{2 \cdot \bar{L}_w} + \frac{3 \cdot h \cdot \beta}{\bar{L}_w} \cdot \left(\ln \left(\frac{h \cdot \beta}{2 \cdot \pi \cdot \hat{r}_w} \right) + s_b \right) \right]} [p_R - p_{wf}]$$

function of PVT, fluid properties

$$\beta = \sqrt{\frac{k_H}{k_V}}$$

$$\hat{L}_w = L_w \cdot \sqrt{1 - \left(\frac{b}{L_w} \right)^2 \cdot (\beta^2 - 1)}$$

$$\bar{L}_w = L_w \cdot \sqrt{1 - \left(\frac{b}{L_w} \right)^2}$$



$$\hat{r}_w = r_w \cdot \frac{1 + \sqrt{1 + (\beta^2 - 1) \cdot \left(\frac{\bar{L}_w}{L_w}\right)^2}}{2}$$

$$\hat{f}_a = \frac{\bar{L}_w}{L} \cdot \left[1 + \left(0.53 \cdot \left(\frac{L}{D}\right)^2 + 1.15 \cdot \left(\frac{L}{D}\right) + 0.164 \right) \cdot \left(\frac{1 - \left(\frac{\bar{L}_w}{L}\right)}{0.45 + \left(\frac{\bar{L}_w}{L}\right)} \right) \right]$$

well completed partially in the interval

$$\hat{s}_b = \begin{cases} 0.69 & \text{if } O(b) = O(h) \\ 0 & \text{if } b = 0 \end{cases} \sim \text{skin factor, 'shielding' effect from top and bottom walls}$$