

02.12.2019 ME683 Field development and operations

02.12-06.12 Prof Milan Stanko NTNU Norwegian University of science and Technology

09:00-14:00

3 breaks → 15 mins

Master program responsible: UDSM Joseph Kihed
NTNU: Ole Jørgen Nydal

Evaluation:

10% homework (2019)

2x15% Quizzes (2019, 2020)

60% Exam (2020)

Supporting prof. @ UDSM: Liberto Hauke

- Examination
- Exercises
- Quizzes

Students:

- Neema (petroleum)
- Wiffritus (chemical and process)
- Emmanuel (petroleum)
- Chrisostom (mechanical engineer)

course information:

<http://www.ipt.ntnu.no/~stanko/files/Courses/ME683/2019>

2018 previous
course material

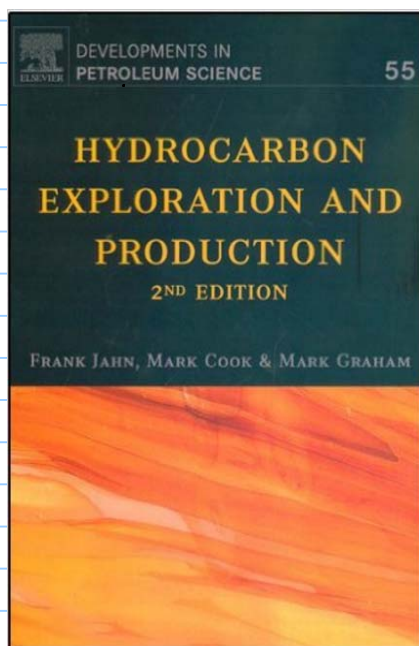
youtube channel:

<https://www.youtube.com/channel/UCWMfsCe1NQMGx4UZWrVvFgA>

↳ playlist:

ME683 - Field development and operation (2016)

Book:



Authors: Frank Jahn, Mark Cook, Mark Graham

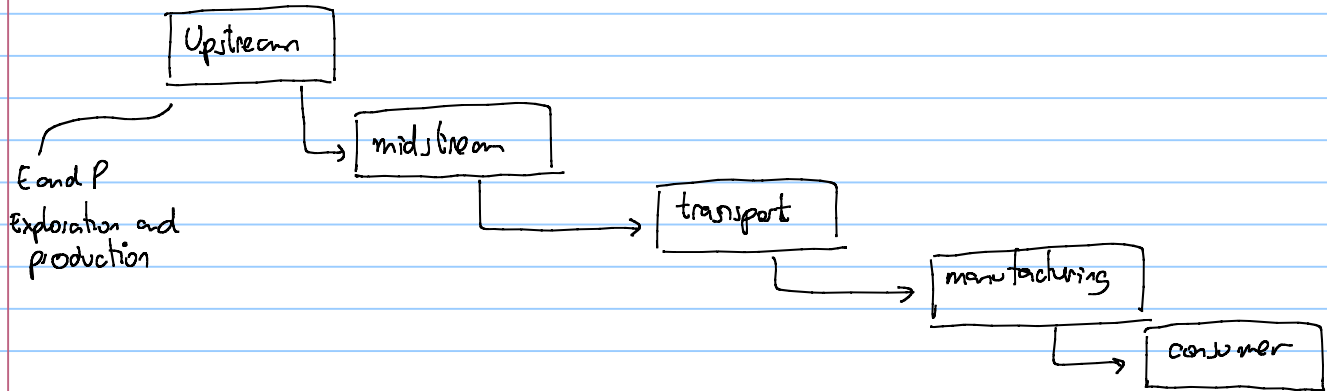
regular NTNU course:

<https://www.youtube.com/channel/UCWMfsCe1NQMGx4UZWrVvFgA>

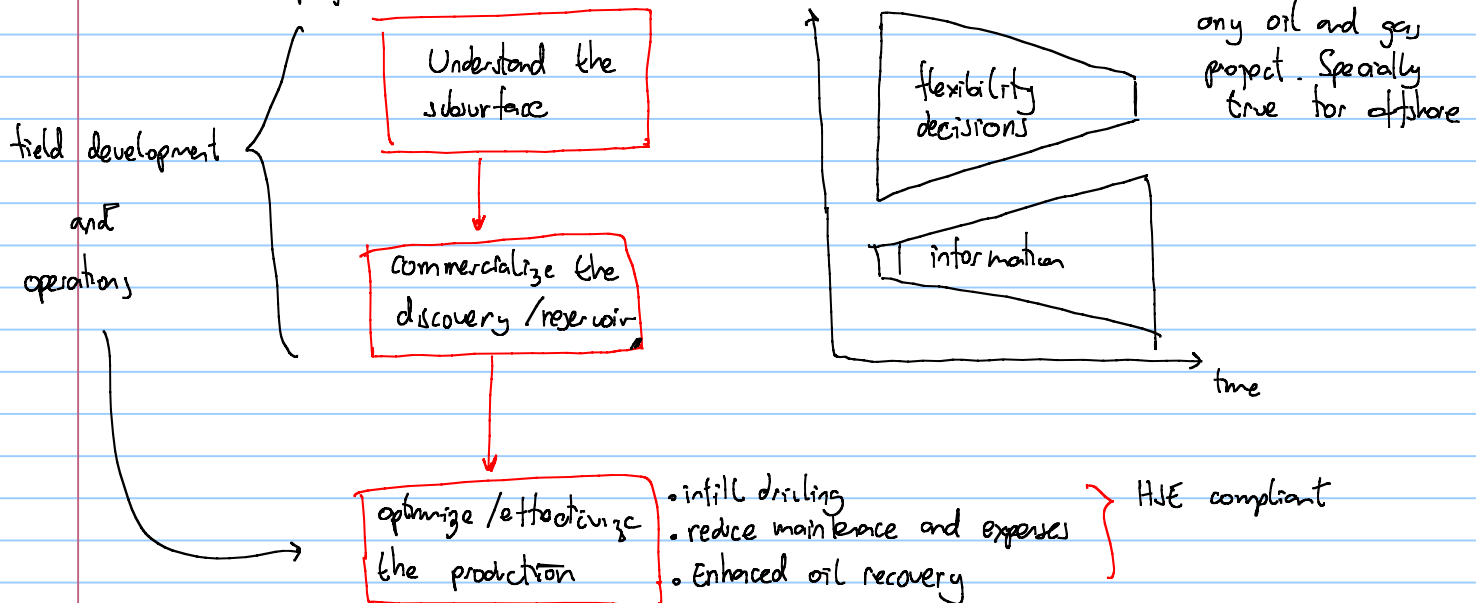
youtube channel:

playlist: TP64230 field development and operation (2019)

where are we?



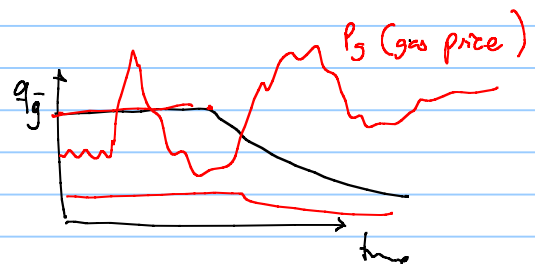
in E&P projects there are three distinct tasks:



topics to cover in the course

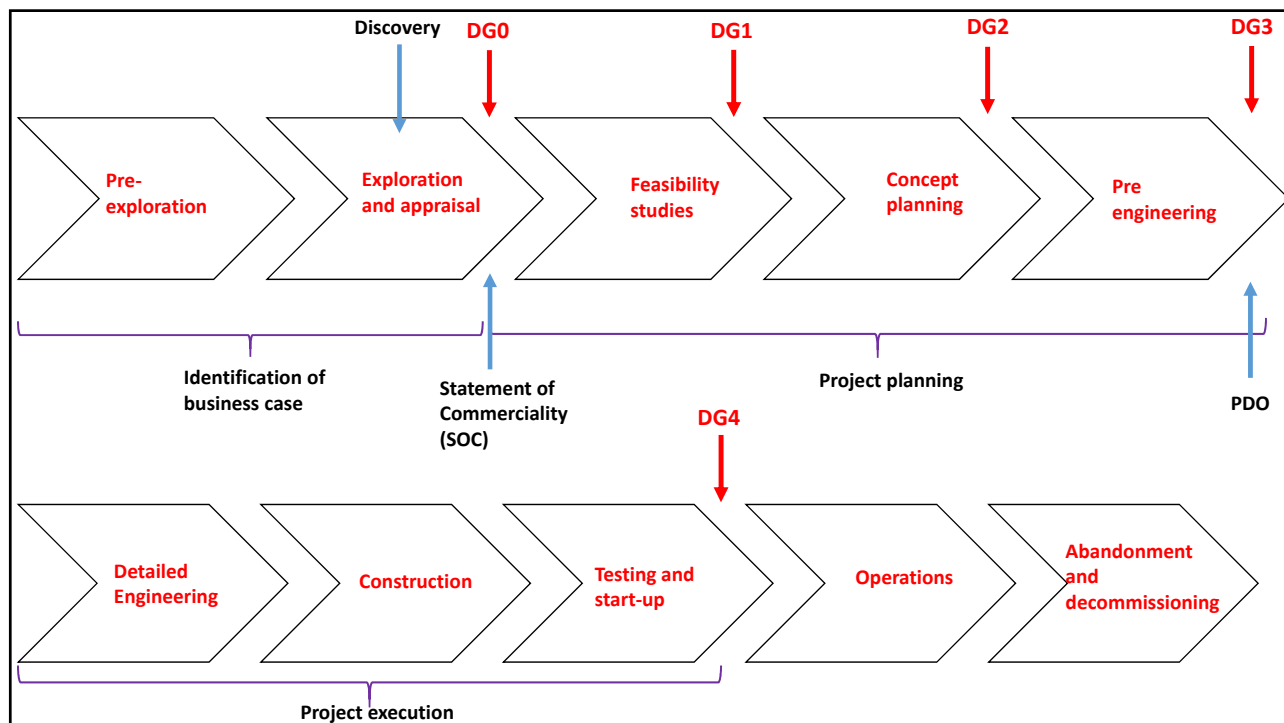
- Estimate and quantify reserve uncertainty
- Decision (probability) trees $\rightarrow$ appraisal
- flow assurance $\rightarrow$ hindrance to develop the field (multiphase transport Ole Tjørring Nydal)
(Corrosion, Roy Johnsen)
- offshore structure type and selection
- field production performance $\sim$ q_{field} vs time

allows to compute: Revenue
size of facilities $\rightarrow$ cost

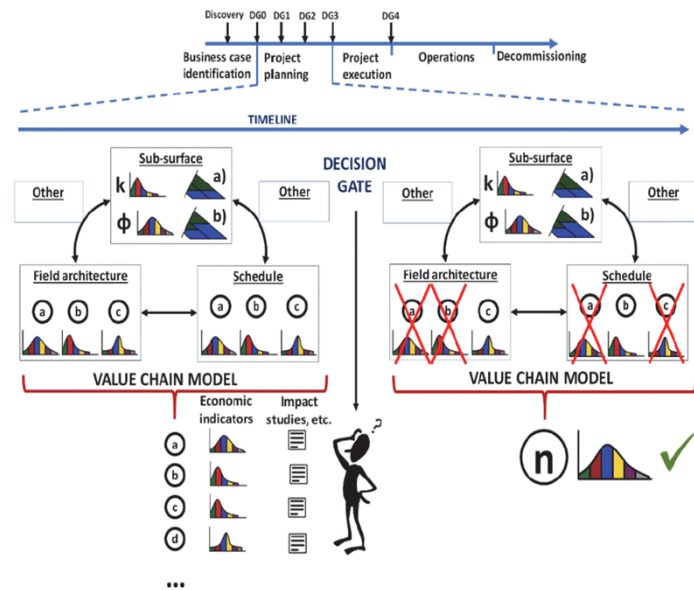


THE FIELD DEVELOPMENT PROCESS

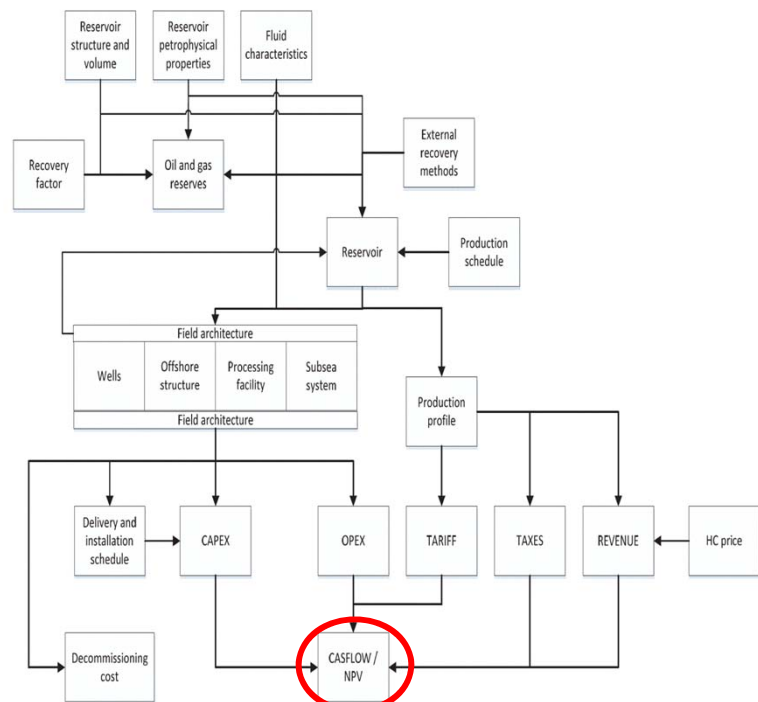
Prof. Milan Stanko (NTNU)

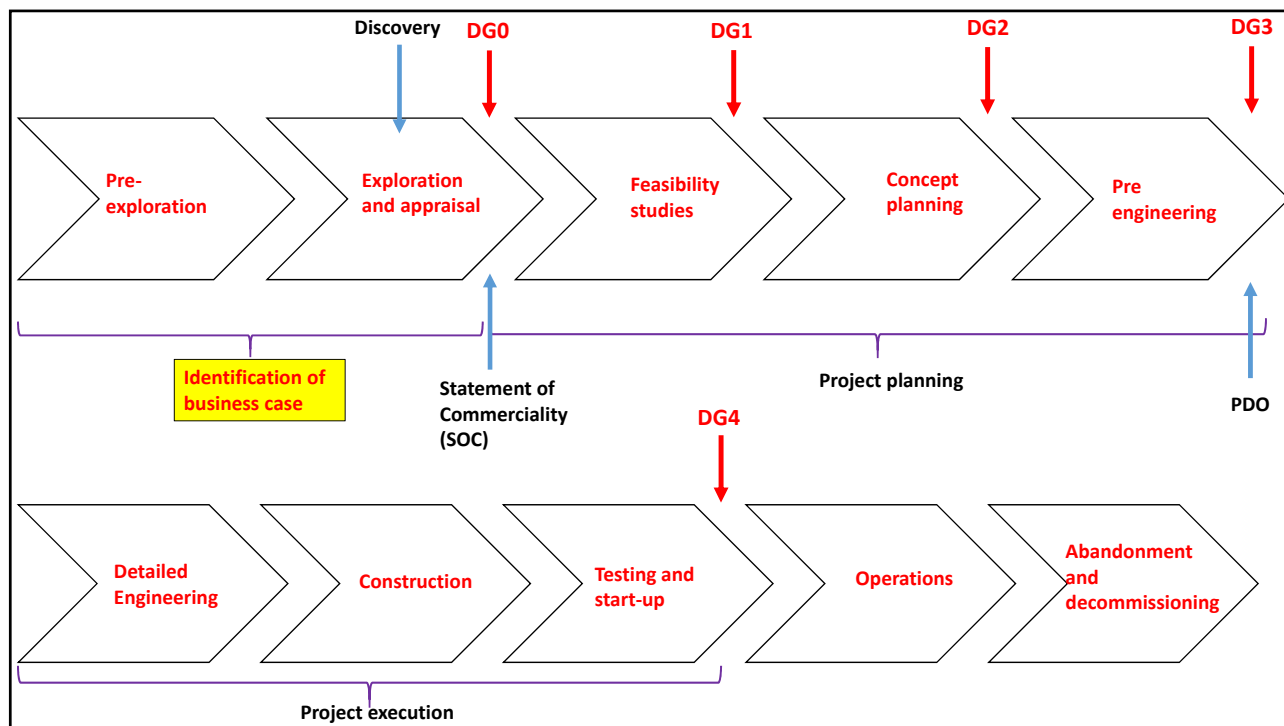


During the field development process a model of the value chain is made based on the disciplines involved and populated with information. Initially there are many alternatives and little information. As time progresses and decisions are taken, the model is expanded, there is more information but less flexibility.



Key performance indicators are computed with the value chain model and are used to take decisions in the decision gate process.





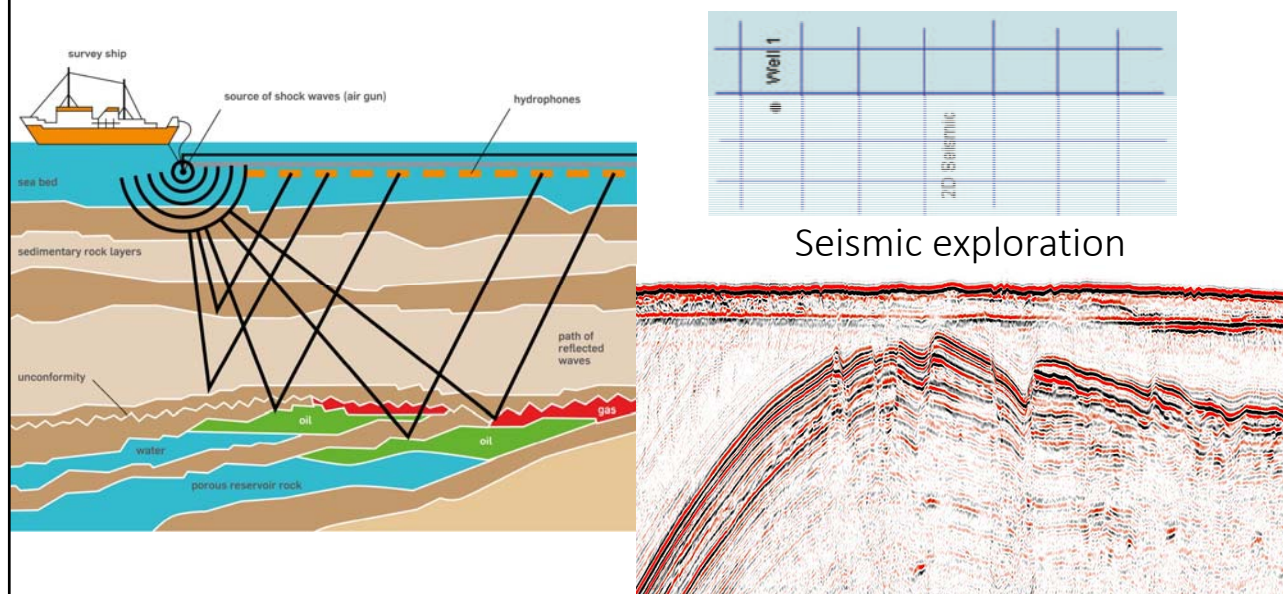
IDENTIFICATION OF BUSINESS CASE

The main goal of this stage is to prove economic potential of the discovery and quantify and reduce the uncertainty in the estimation of reserves.

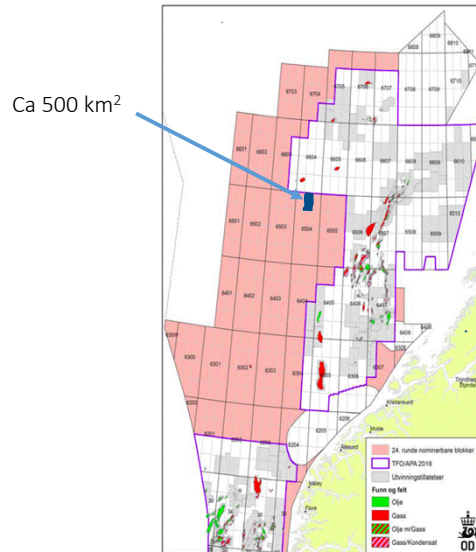
IDENTIFICATION OF BUSINESS CASE - TASKS

- Pre-exploration – scouting: collecting information on areas of interests. Technical, political, geological, geographical, social, environmental considerations are taken into account. E.g. expected size of reserves, political regime, government stability, technical challenges of the area, taxation regime, personnel security, environmental sensitivity, previous experience in the region, etc.
- Getting pre-exploration access – The exploration license (usually non-exclusive). In the NCS only seismic and shallow wells are allowed. This is usually done by specialized companies selling data to oil companies. Area: 500 Km²
- Identify prospects.

IDENTIFICATION OF BUSINESS CASE - TASKS



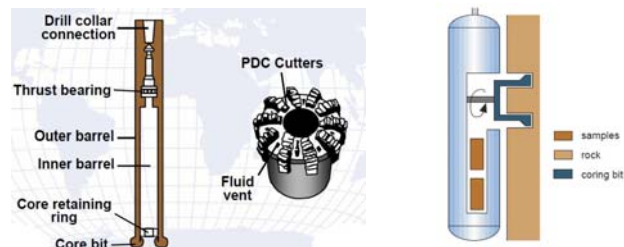
IDENTIFICATION OF BUSINESS CASE - TASKS



- Apply and obtain exclusive production license (6 years, possible to extend for 30 years). In the NCS: Licensing rounds (frontier areas) or Awards in predefined areas (APA). The current fees are 34 000 NOK/km² for the first year, 68 000 NOK/km² for the second year and 137 000 NOK/km² per year thereafter.

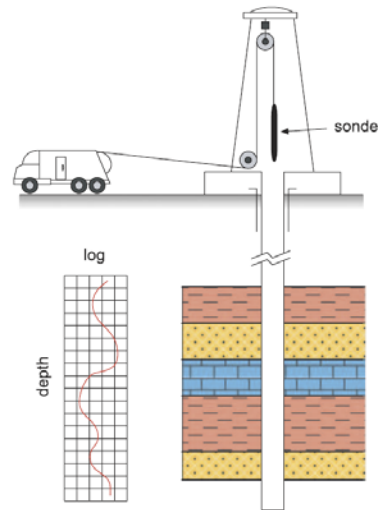
IDENTIFICATION OF BUSINESS CASE - TASKS

- Exploration. Perform geological studies, geophysical surveys, seismic, exploration drilling (Well cores, wall cores, cuttings samples, fluid samples, wireline logs, productivity test).
- Discovery!



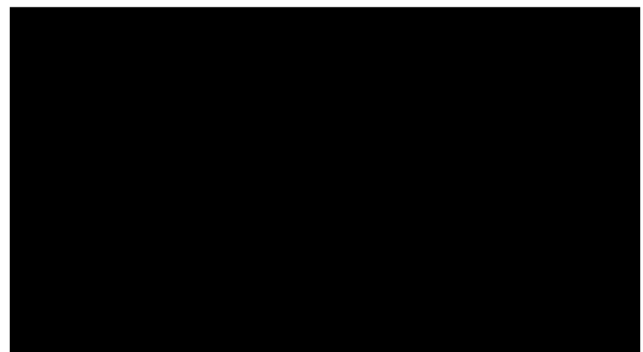
IDENTIFICATION OF BUSINESS CASE - TASKS

- Exploration. Perform geological studies, geophysical surveys, seismic, exploration drilling (Well cores, wall cores, cuttings samples, fluid samples, wireline logs, productivity test).
- **Discovery!**



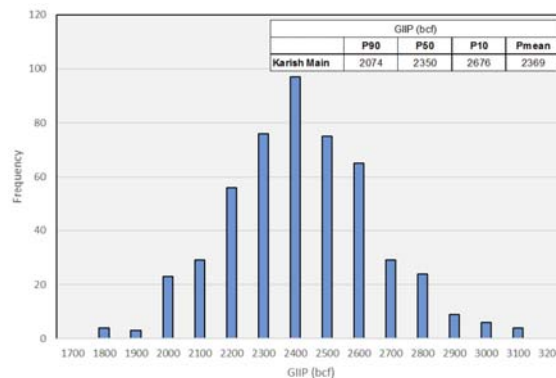
IDENTIFICATION OF BUSINESS CASE - TASKS

- Exploration. Perform geological studies, geophysical surveys, seismic, exploration drilling (Well cores, wall cores, cuttings samples, fluid samples, wireline logs, productivity test).
- **Discovery!**



IDENTIFICATION OF BUSINESS CASE - TASKS

- Assessment of the discovery and the associated uncertainty. Risk management:
 - o **Probabilistic reserve estimation.** Identify and assess additional segments.

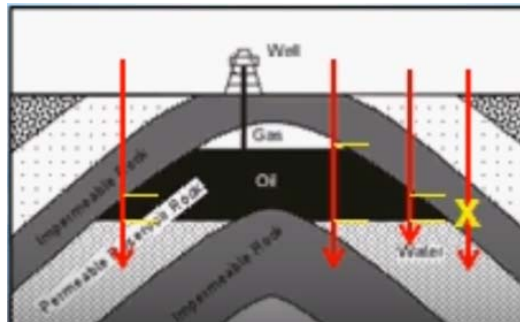


IDENTIFICATION OF BUSINESS CASE - TASKS

- Assessment of the discovery and the associated uncertainty. Risk management:
 - o **Probabilistic reserve estimation.** Identify and assess additional segments.
 - o Perform **simplified economic valuation** of the resources.
 - o Field **appraisal** to reduce uncertainty: more exploration wells and seismic to determine for example: fault communication, reservoir extent, aquifer behavior, location of water oil contact or gas oil contact.

IDENTIFICATION OF BUSINESS CASE - TASKS

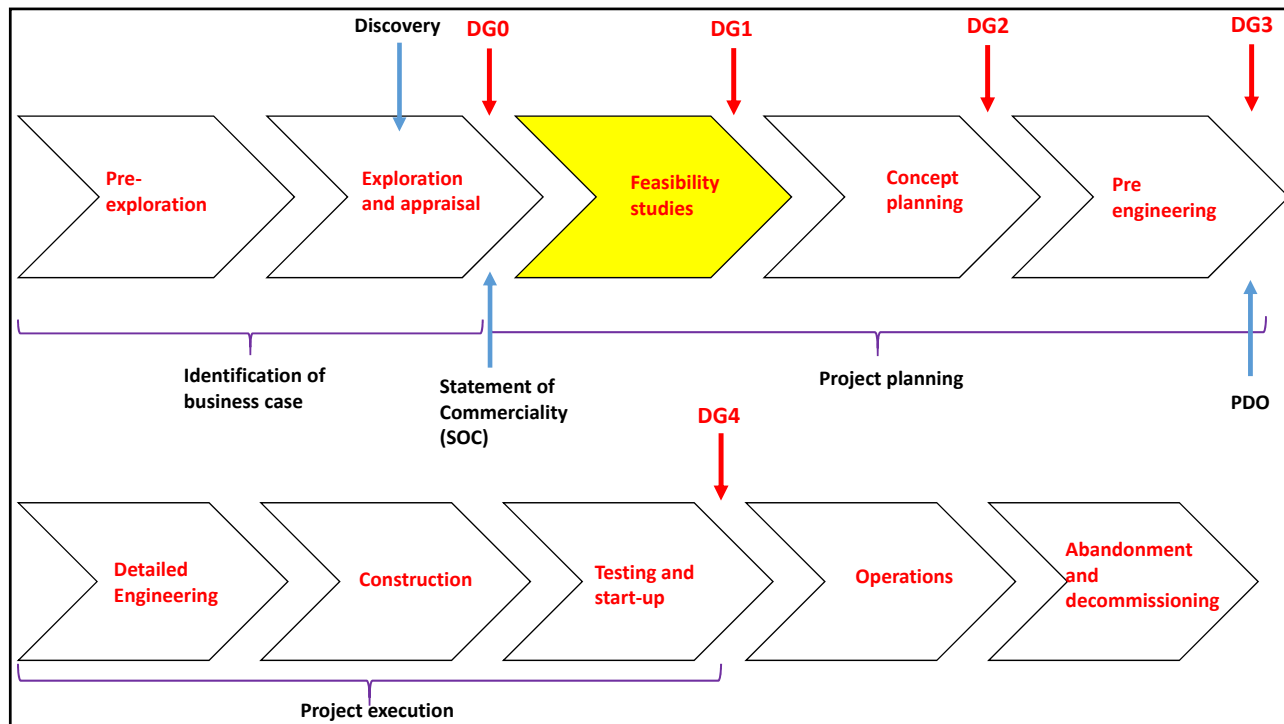
o Appraisal



IDENTIFICATION OF BUSINESS CASE - TASKS

DGO:

- Issue a SOC (Statement of Commerciality) and proceed with development.
- Continue with more appraisal
- Sell the discovery.
- Do nothing (wait)
- Relinquish to the government

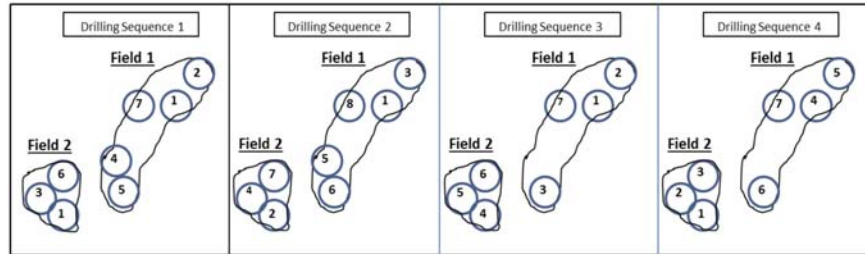


FEASIBILITY STUDIES - TASKS

OBJECTIVE: Justify further development of the project, finding one or more concepts that are technically, commercially and organizationally feasible

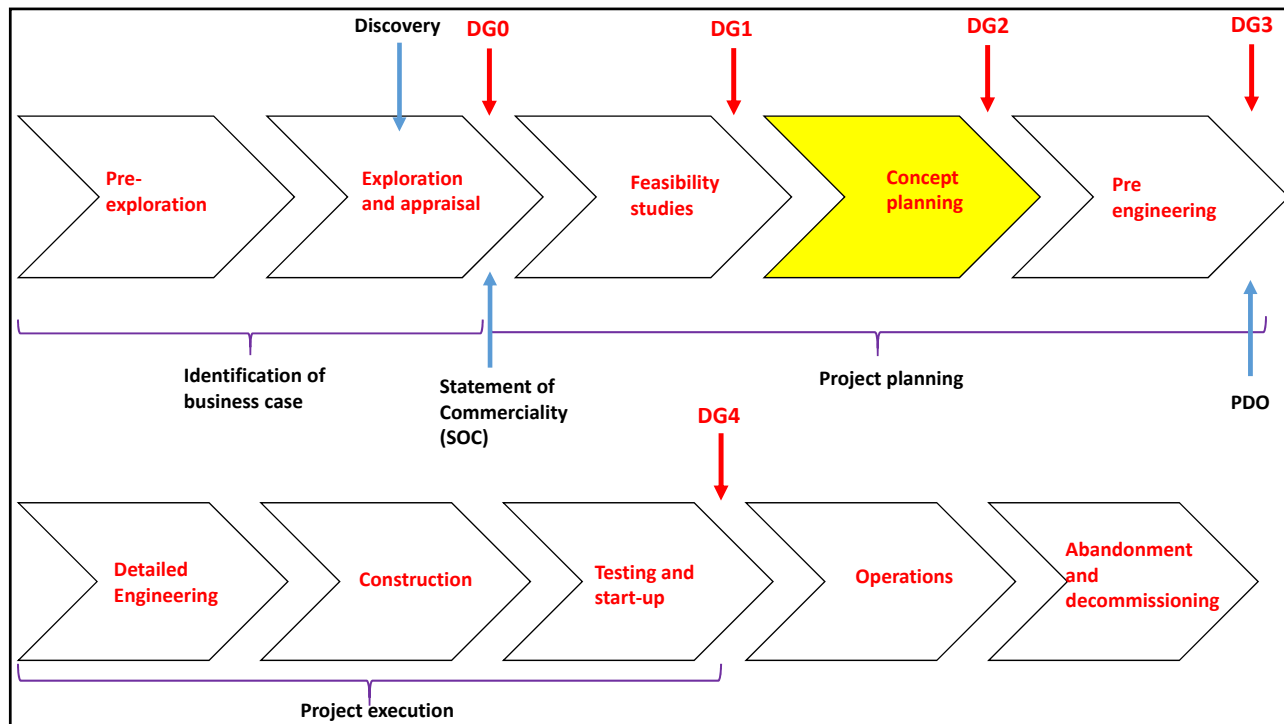
- Define objectives of the development in line with the corporate strategy.
- Establish feasible development scenarios.
- Create a project timeline and a workplan.

FEASIBILITY STUDIES - TASKS



FEASIBILITY STUDIES - TASKS

- Identify possible technology gaps and blockers.
- Identify the needs for new technology.
- Identify added value opportunities.
- Cost evaluation for all options (at this stage, cost figures are $\pm 40\%$ uncertain)



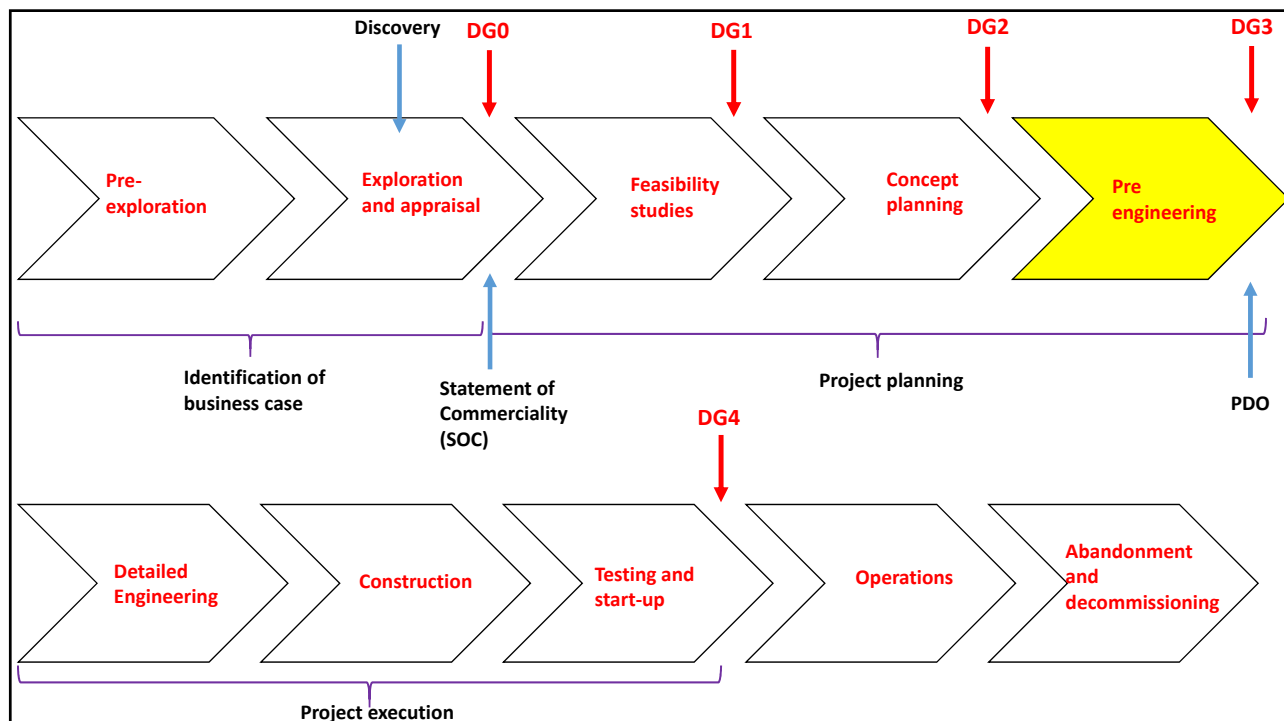
CONCEPT PLANNING - TASKS

OBJECTIVE: Identify development concepts, rank them and select and document a viable concept (Base Case Scenario).

- Evaluate and compare alternatives for development and screen out non-viable options.
- Elaborate a Project Execution Plan (PEP) which describes the project and management system.
- Define the commercial aspects, legislation, agreements, licensing, financing, marketing and supply, taxes.

CONCEPT PLANNING - TASKS

- Create and refine a static and a dynamic model of reservoir.
Define the depletion and production strategy.
- Define an HSE program
- **Flow assurance evaluation.** Identification of challenges related with fluid properties, multiphase handling and driving pressure.
- Drilling and well planning
- Pre-design of facilities
- Planning of operations, start-up and maintenance
- Cost and manpower estimates of the best viable concept.



PRE-ENGINEERING - TASKS

OBJECTIVE: Further mature, define and document the development solution based on the selected concept.

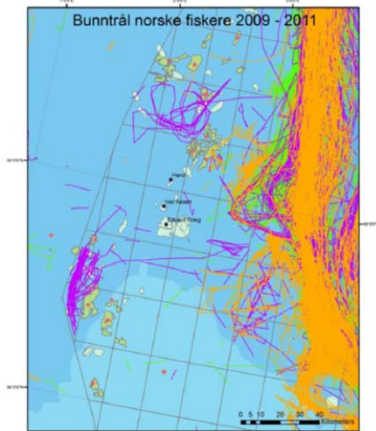
- Selection of the final technical solution. Decide and define all remaining critical technical alternatives.
- Execute Front End Engineering Design (FEED) Studies: determine technical requirements (arranged in packages) for the project based on the final solution chosen. Estimate cost of each package.
- Plan and prepare the execution phase.

PRE-ENGINEERING - TASKS

- Prepare for submission of the application to the authorities.
- Perform the Environmental impact assessment.
- Establish the basis for awarding contracts.
- Issue:
 - Plan for development and operations
 - Plan for installation and operations of facilities for transport and utilization of petroleum (PIO)
 - Impact assessment report

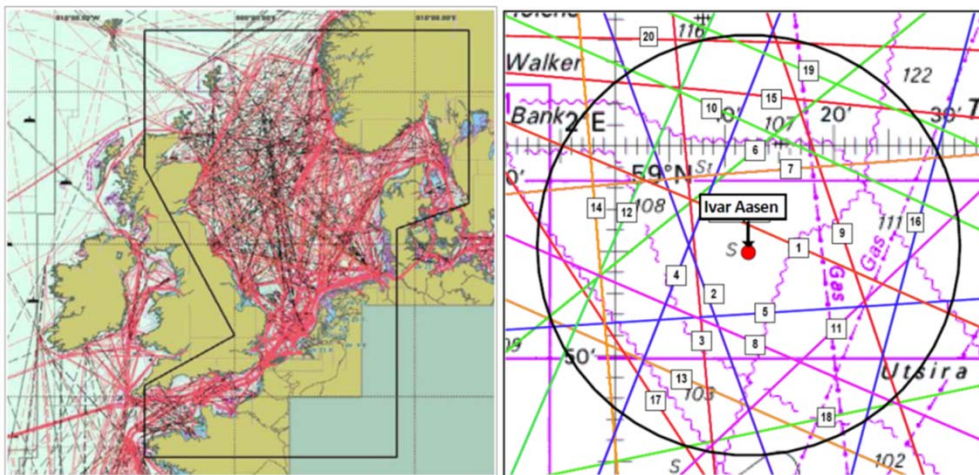


PRE-ENGINEERING - TASKS



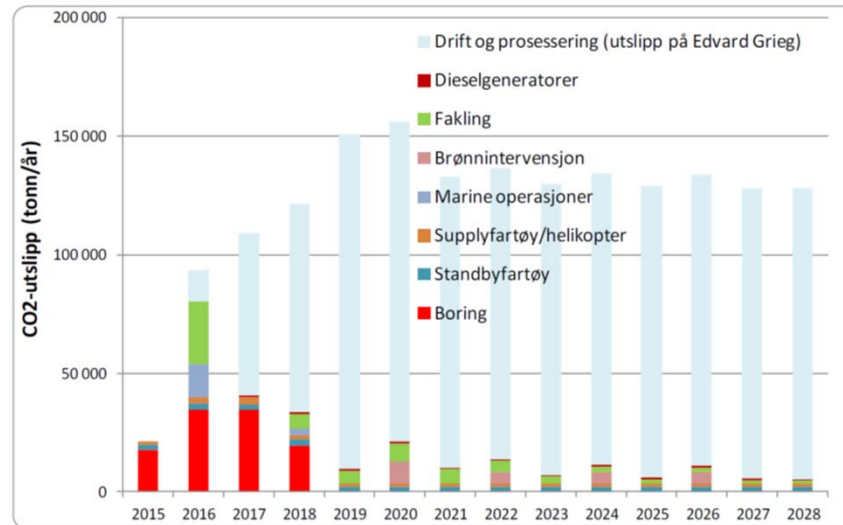
Figur 23. Registrert norsk fiskeriaktivitet med bunntål i området omkring Aasen i 2009 (grønn), 2010 (blått) og 2011 (oransje). Figur utarbeidet på grunnlag av data fra Fiskeridirektoratets satellittsporing av større fiskefartøyer

PRE-ENGINEERING - TASKS



Figur 24. Trafikkompleksitet i Nordsjøen (venstre) og skipsleder for handels- og offshorefartøyer innenfor en radius på 10 nautiske mil fra Aasen (høyre)

PRE-ENGINEERING - TASKS



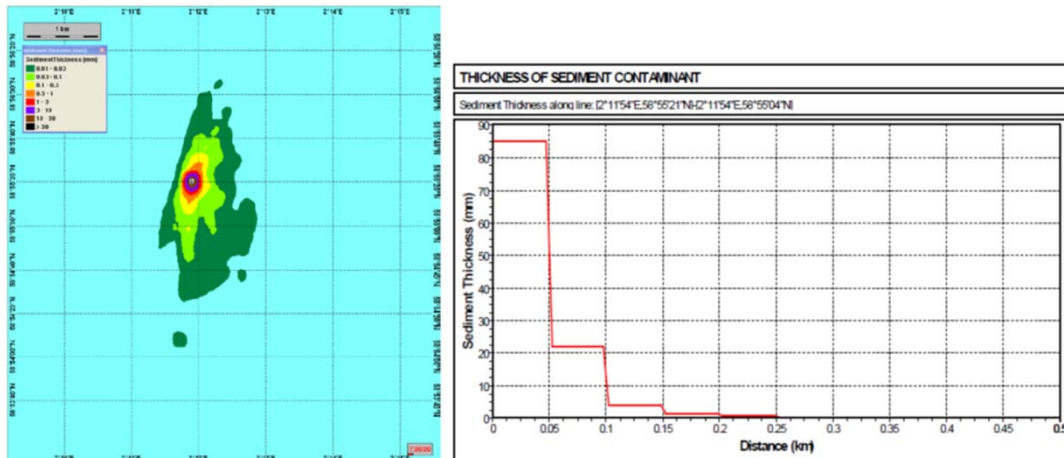
Figur 25. Samlede utslipp av CO₂ fra Aasenfeltet i perioden 2015 – 2028

PRE-ENGINEERING - TASKS

Tabell 5-1. Foreløpig oversikt over estimerte mengder kaks for typiske produksjonsbrønner på Aasen, West Cable og Hanz

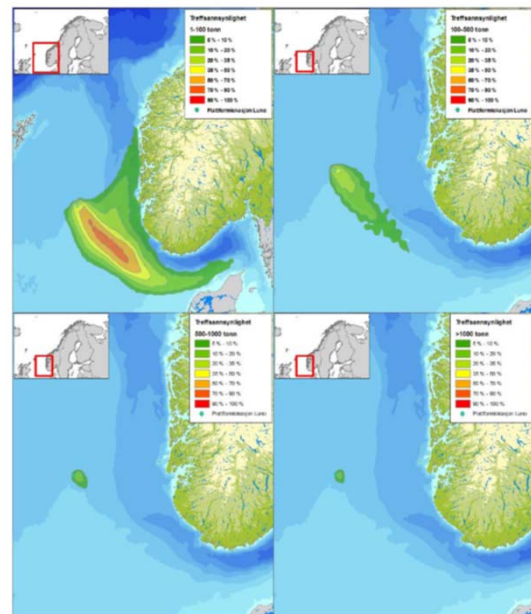
Seksjon	Borevæske	Boret lengde (m)			Mengde borekaks (tonn)		
		Aasen	West Cable	Hanz	Aasen	West Cable	Hanz
36"	WBM	88	88	86	70	70	70
26"	WBM	370	370	400	150	150	160
17 ½"	OBM	1 550	1 020	990	310	205	200
12 ¼"	OBM	860	3 890	1 700	90	390	170
8 ½"	OBM	1 390	1 530	90	70	80	5
SUM (avrundet)		4 300	6 900	3 300	690	895	605
SUM WBM kaks					220	220	230
SUM OBM kaks					470	675	375

PRE-ENGINEERING - TASKS



Figur 29. Sedimentering ved utslipp av vannbasert kaks ved havbunnen (sommersituasjon)

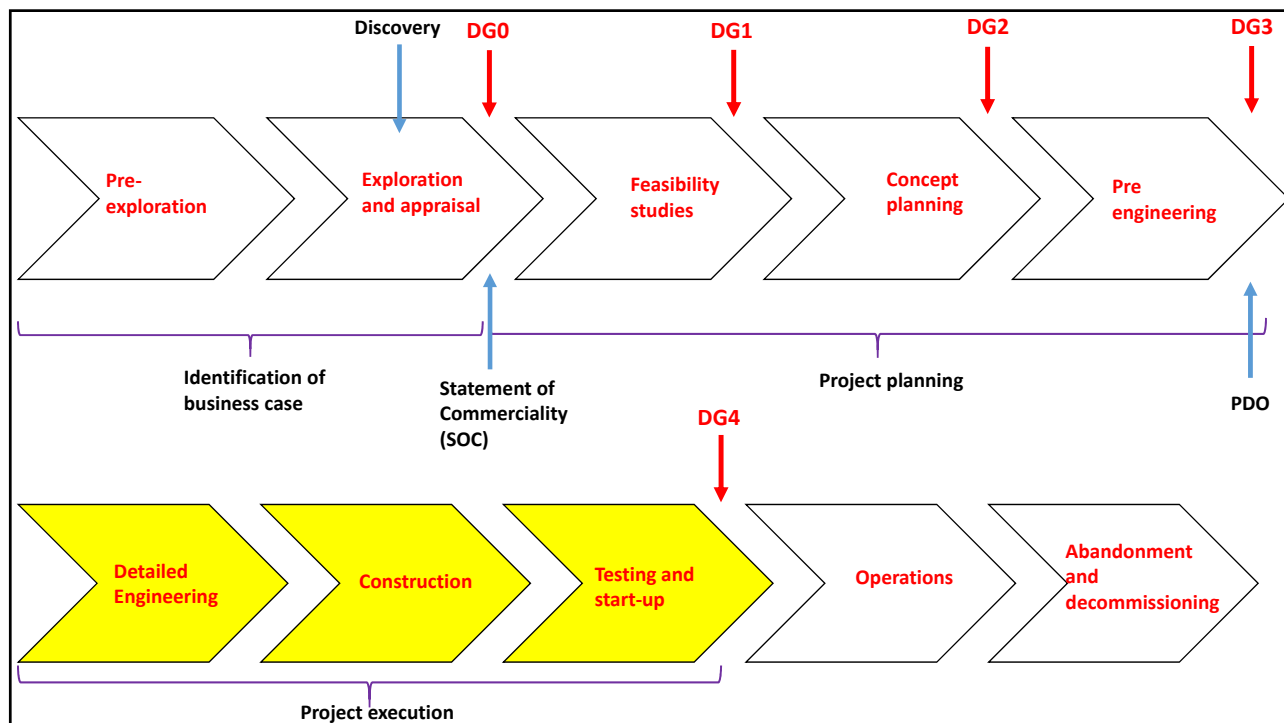
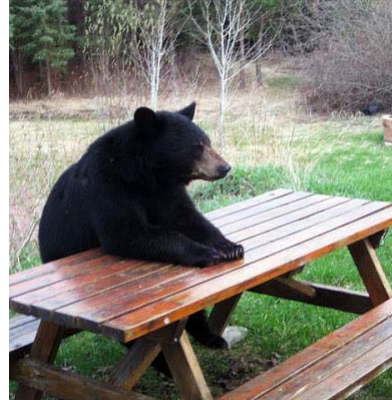
PRE-ENGINEERING - TASKS



Figur 37. Sannsynligheten for treff av ulike mengdekategorier av olje i 10 x 10 km ruter gitt en sjøbunnsutblåsning fra Aasen/Grieg (helårsstatistikk). Influensområdet er basert på alle utslippsrater og varigheter og deres individuelle sannsynligheter. Merk at det markerte området ikke viser omfanget av et enkelt oljeutslipp, men er det området som berøres i mer enn 5 % av enkeltsimuleringene av oljens drift og spredning (Lundin 2011).

PRE-ENGINEERING - TASKS

- Wait for the government to study the proposal



DETAILED ENGINEERING, CONSTRUCTION, TESTING AND STARTUP

OBJECTIVE: Detailed design, procurement of the construction materials, construction, installation and commissioning of the agreed facilities.

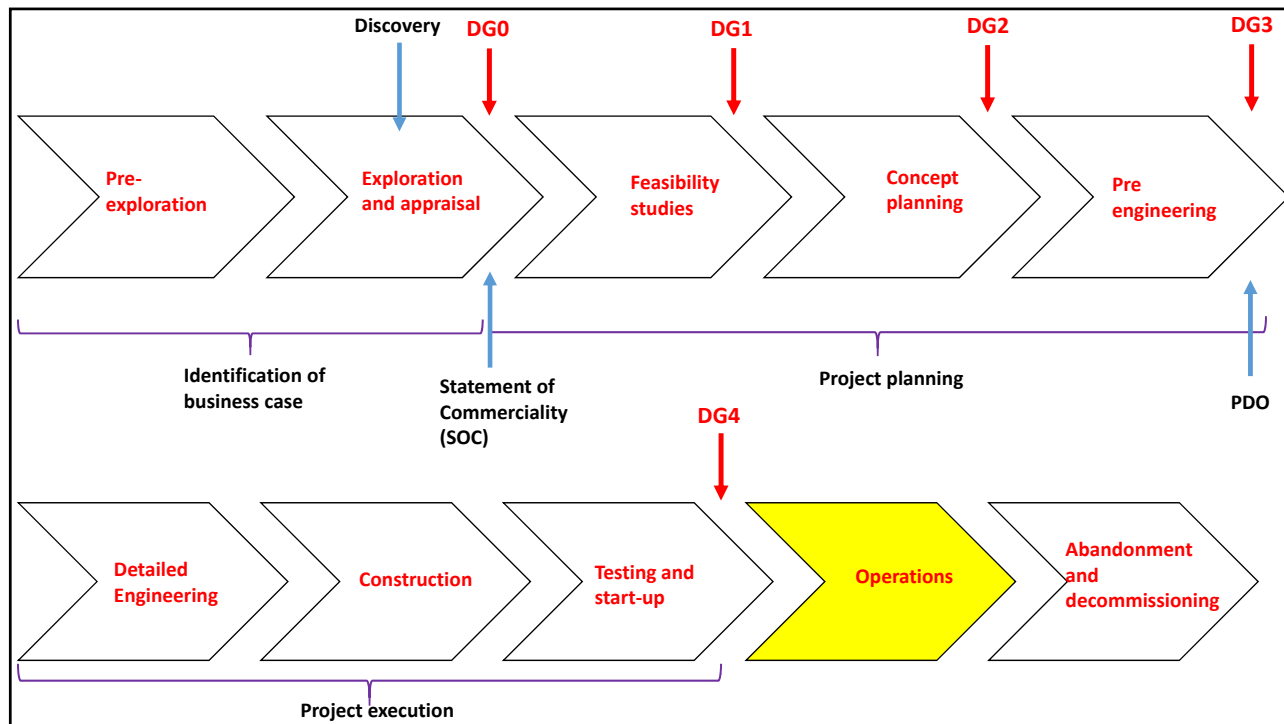
Individual contracts

Detailed engineering
Bids, contracts
Construction, fabrication
Installation
Commissioning (Cold or Hot)

EPCM (Engineering,
procurement,
construction, and
management contract)
with one main
contractor.

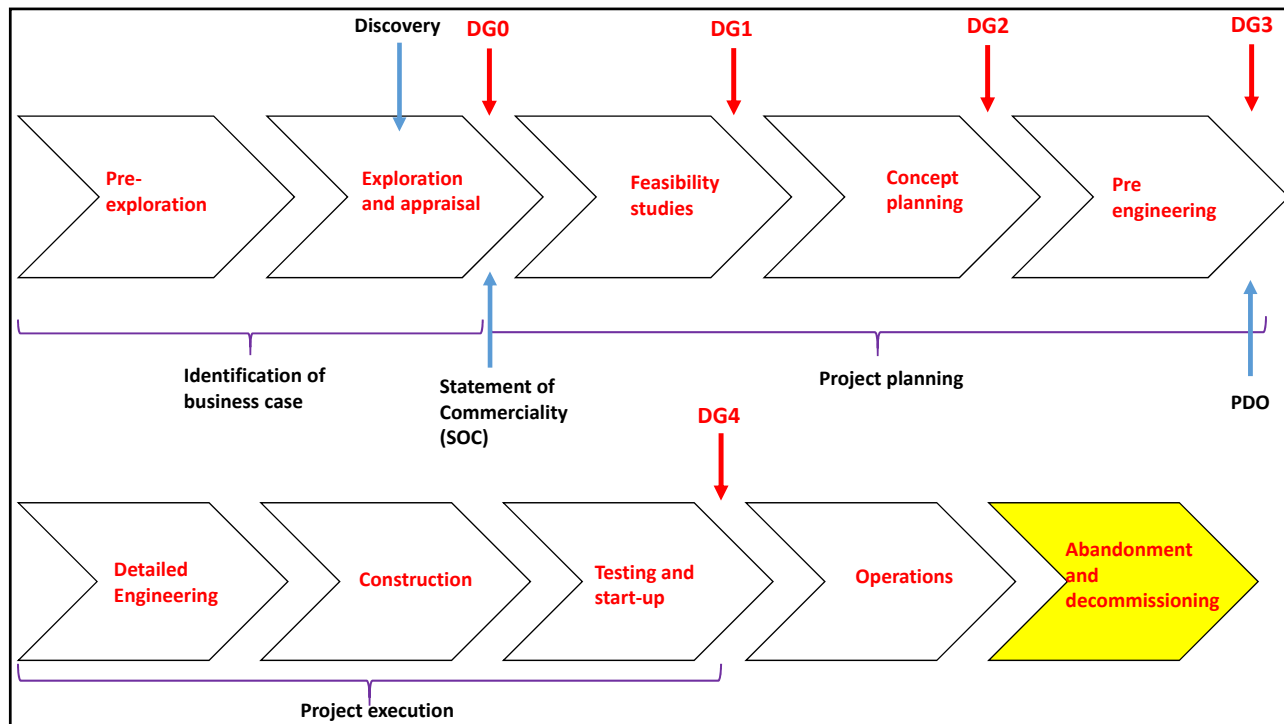
DETAILED ENGINEERING, CONSTRUCTION, TESTING AND STARTUP

- Constructing wells.
- Perform hand over to asset, operations
- Prepare for start-up, operation and maintenance



OPERATIONS

- Production startup, Build-up phase, Plateau phase, Decline phase, Tail production, Field shut-down.
- Maintenance.
- Planning Improved Oil recovery methods.
- Allocation and metering.
- De-bottlenecking.
- Troubleshooting.



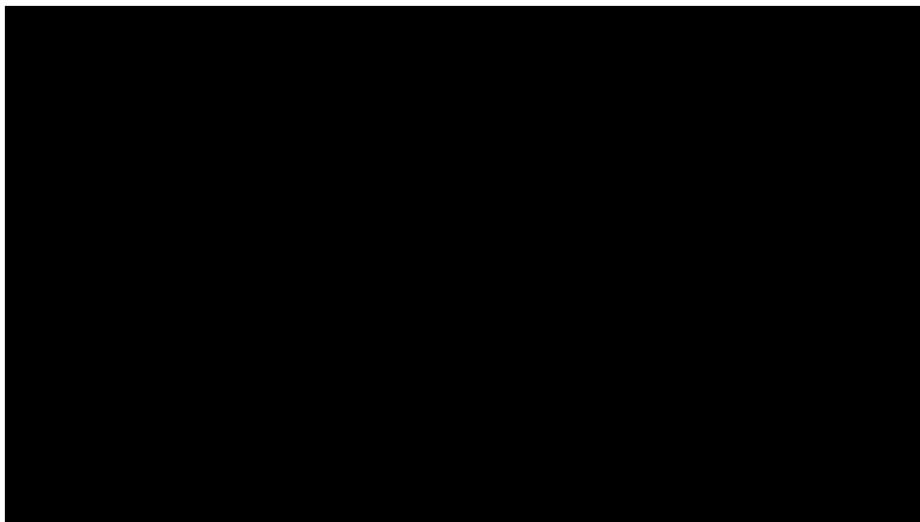
DECOMMISSIONING AND ABANDONMENT

- Engineering “down and clean”: flushing and cleaning tanks, processing equipment, piping.
- Coordinate with relevant environmental and governmental authorities.
- Well plugging and abandonment (P&A)
- Cut and remove well conductor and casing.
- Remove topside equipment.

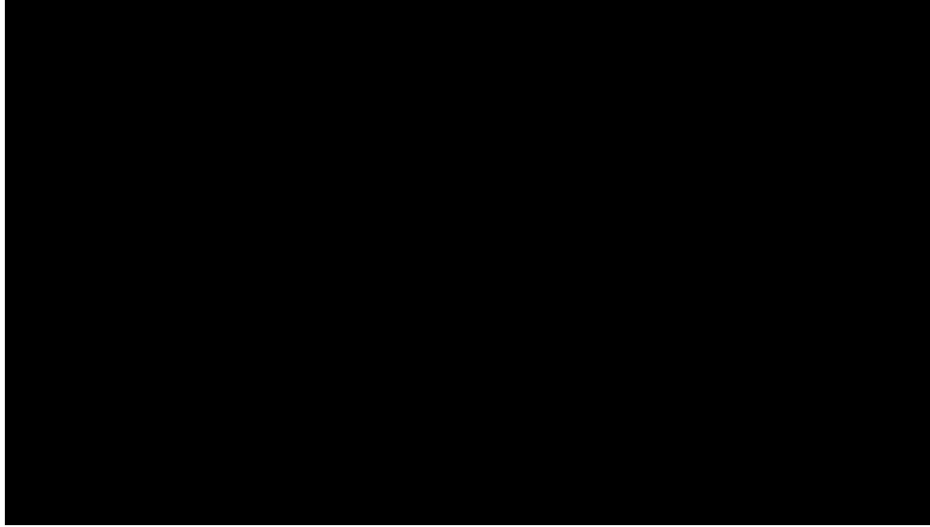
DECOMISSIONING AND ABANDONMENT

- Removal of the offshore structure: Lifting operations and transport
- Remove or bury subsea pipelines
- Mark and register leftover installations on marine maps
- Monitoring
- Recovery of material: Scrap (steel) and recycling equipment (Gas turbines, separators, heat exchangers, pumps, processing equipment)
- Disposal of residues

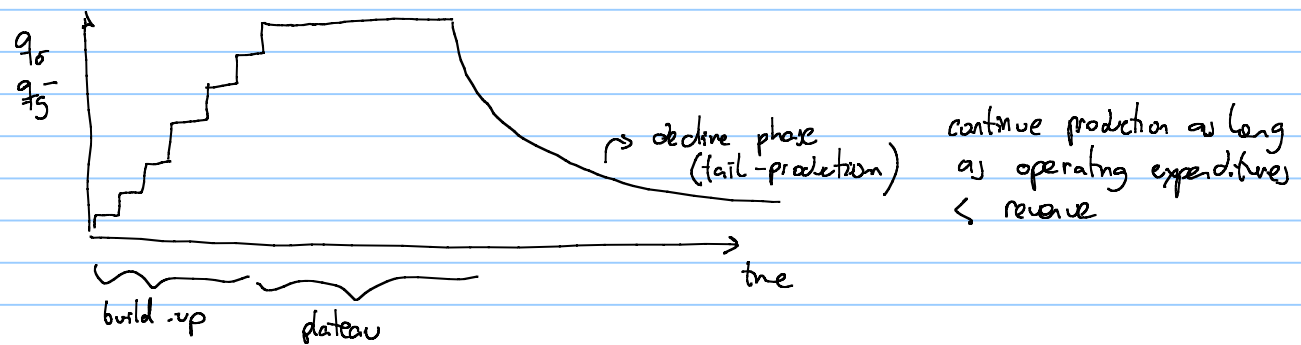
DECOMISSIONING AND ABANDONMENT



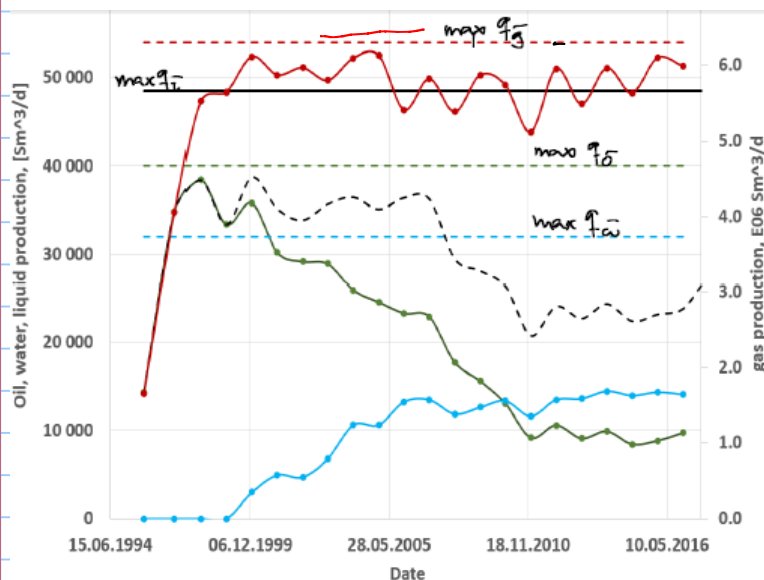
DECOMISSIONING AND ABANDONMENT



typical production profile (phases) of a field:



as short as possible (pre-drilled wells, platform wells versus subsea wells)



bottlenecked? (gas capacity)

for oil field

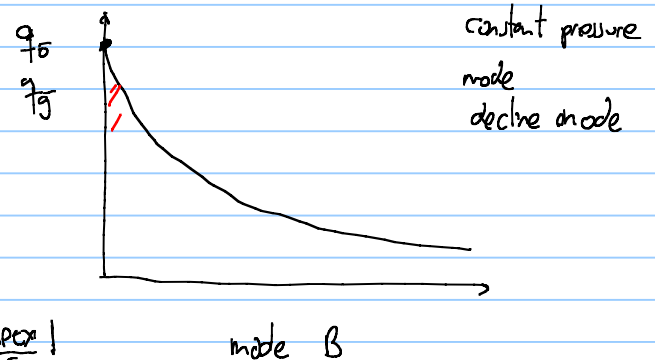
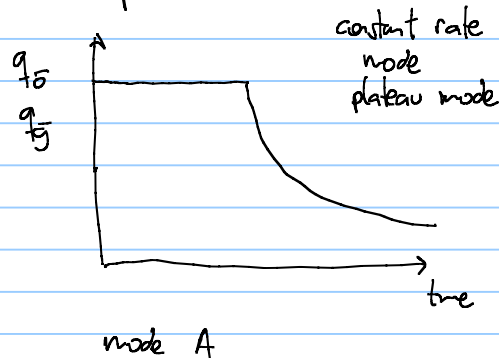
q_o

$$q_g = \text{GOR} \cdot q_o$$

GOR changes with time

Predicting and quantifying field production performance

two production modes



$$NPV = \frac{\frac{q_o \cdot P_o}{P_o - CAPEX}}{(1+i)^t}$$

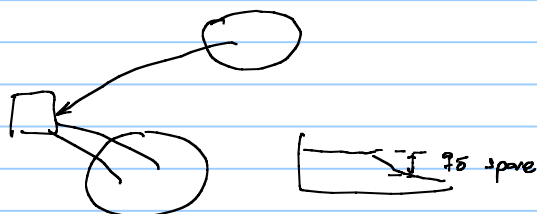
years discount rate

Used for:

- standalone fields that require new infrastructure to be built from scratch
- medium to large fields

Used for

- satellite fields that can be tied in to existing infrastructure (medium-small size)



why not to produce as much as possible as early as possible?

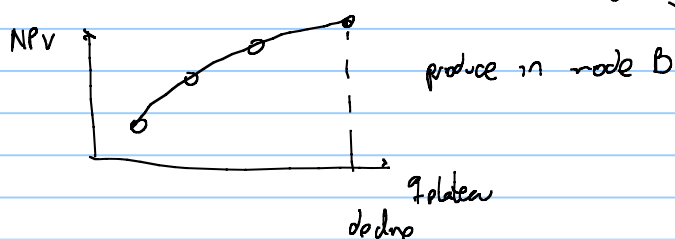
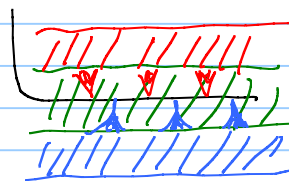
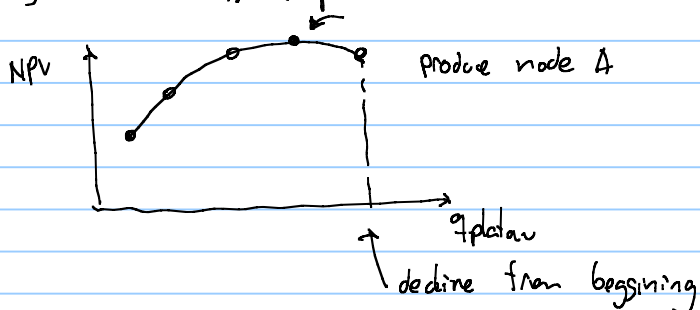
- trade off / balance between CAPEX and revenue.

higher plateau rate gives $\uparrow$ revenue

higher plateau rates give $\uparrow$ capital expenses $\rightarrow$ bigger processing facilities

$\rightarrow$ bigger offshore structure
 $\rightarrow$ drill more wells (to avoid sand production, formation damage, gas coning or water cusping)

to study this dependency, we typically run analysis with different plateau rates

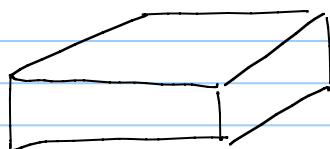


rule of thumb to define plateau rates for standalone fields:

for oil $\sim 10\%$ of TRR per year
 $\rightarrow$ total recoverable reserves

only oil and water

N - OOIP original oil in place



V_R

$$N = \underbrace{V_R}_{V_{\text{fluid}}} \cdot \phi \cdot \frac{S_{oi}}{B_o} = \frac{V_R \cdot \phi \cdot (1 - S_{wc})}{B_{oi} \phi_{i,T_i}} \quad \text{m}^3 - \text{bbls}$$

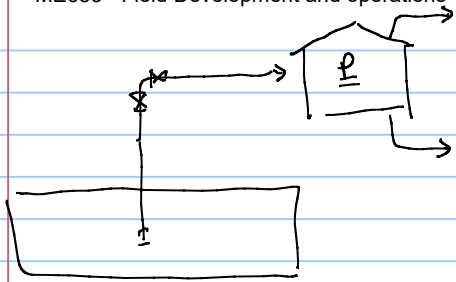
$$\phi = \frac{\text{pore volume}}{\text{rock volume}}$$



$$S_o = \frac{V_o}{V_{\text{pore}}}$$

$$S_w = \frac{V_w}{V_{\text{pore}}}$$

connate water
 S_{wc}



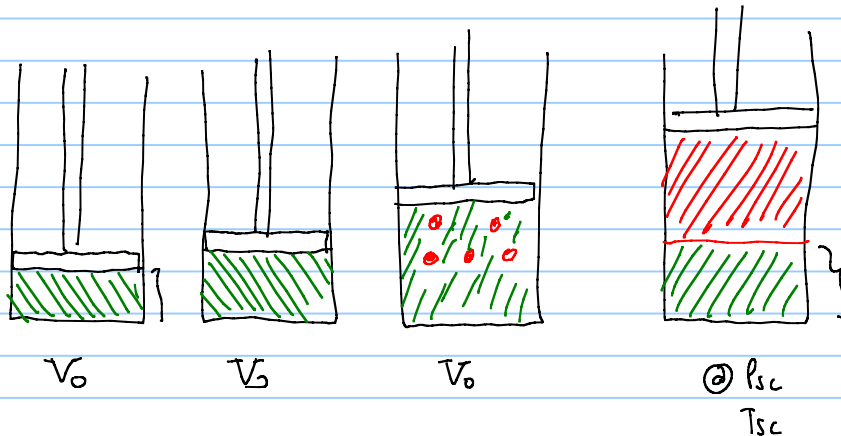
oil volume factor $B_o = \frac{V_o @ p_r \text{ [m}^3\text{]}}{V_o @ p_{sc}, T_{sc} \text{ [m}^3\text{]}}$

greater than 1
1 - 1.7
light oil
heavy oil low GOR
high GOR

standard conditions depend

$$p_r = 1.01325 \text{ bara}$$

$$T_{sc} = 15.56 \text{ } ^\circ\text{C}$$



$$TRR = N_{pu} = RF_u \cdot N = V_R \Phi \frac{(1 - S_{wc})}{B_o} \cdot RF_u$$

ultimate cumulative production

ultimate recovery factor

for gas (0.5 - 0.8)
for oil (0.2 - 0.6)

an example - a field with

$$N = 100\,000\,000 \text{ stb}$$

10% of TRR in every year

$$\text{assume } RF_u = 0.4$$

$$TRR = N_{pu} = 40\,000\,000 \text{ stb}$$

$$q_{\text{plateau}} = \frac{0.1 \cdot N_{pu}}{365} = \frac{0.1 \cdot 40\,000\,000}{365} \text{ stb}$$

$$q_{\text{plateau}} = 10958 \text{ stb/day}$$

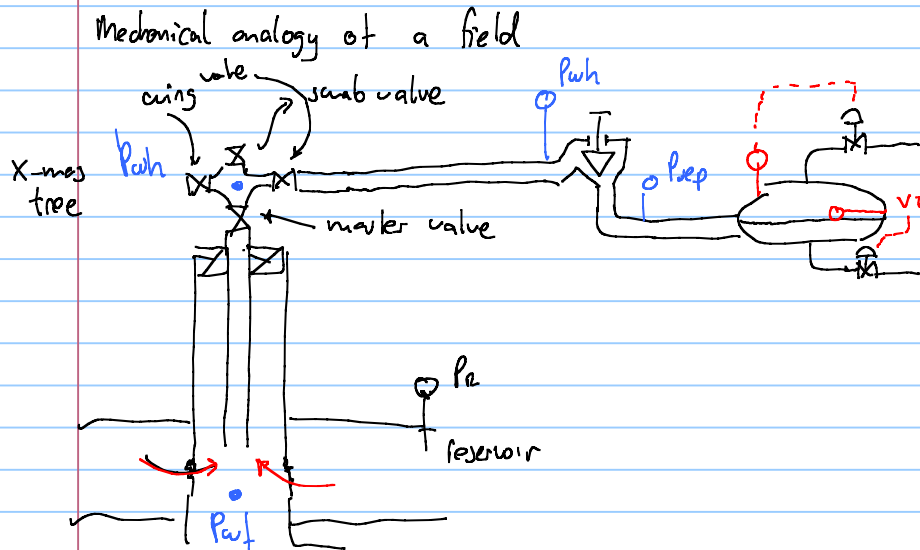
for gas IGIP, G 2x - 5x of TRR per year

differences between oil and gas production:

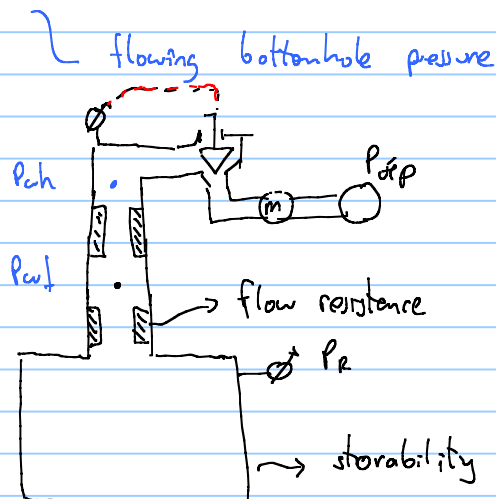
- oil can be sold in the spot market, with tanker. gas must be sold to a customer with a pre-existing contract, infrastructure
- Gas contracts are typically long term, they specify a plateau rate swing factor

because of this, plateau duration of gas fields is much longer than oil fields (1-5 years) (5-30 years)

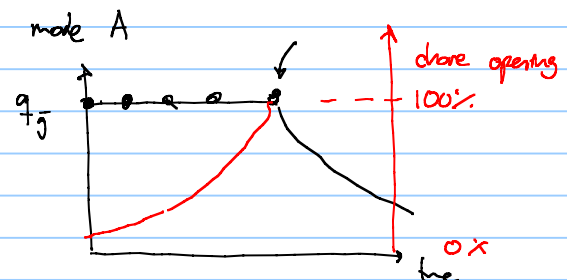
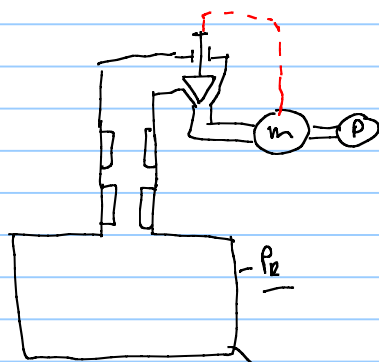
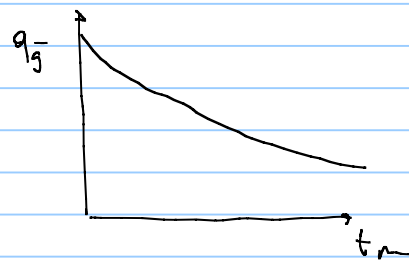
LNG Liquefied natural gas CH_4 C_2H_6
methane ethane $\xrightarrow{-160^\circ\text{C}}$ liquid



always P_{sep} is constant
no matter the rate
 q_o, q_g, q_w

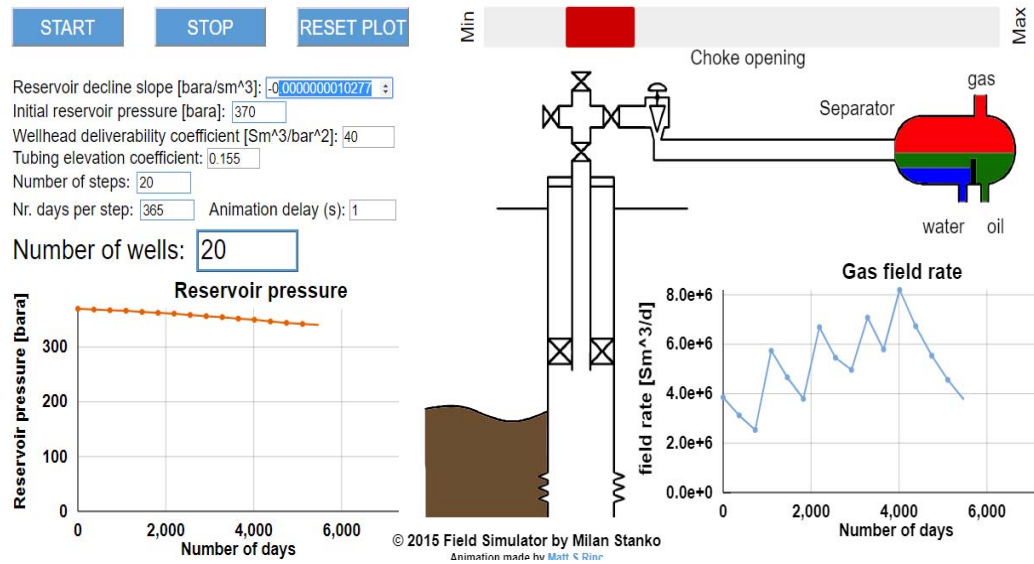


mode B (decline mode)
keep the choke opening fixed



$$q \propto (P_R - P_{sep})$$

P_R vs G_p



Dry gas →

material balance

$$P_R = f(G_p)$$

cumulative production

$$G_p = \int_0^t q_g dt$$

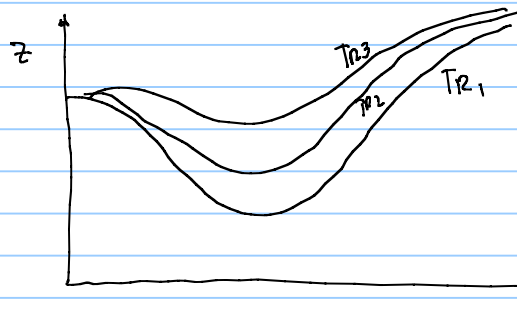
initial pressure

$$P_R = p_i \frac{z_R}{z_i} \left(1 - \frac{G_p}{G} \right)$$

initial gas in place
 gas deviation factor $P_R = z_R T$

$$RF = \frac{G_p}{G} \quad (0 \rightarrow RF_w)$$

$$P_{c,1c} = f(R_g)$$

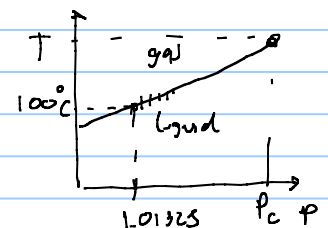


$$P_{wf} = f(P_R, q_g)$$

Inflow performance relationship (IPR)

$$P_{wh} = f(P_{wf}, q_g)$$

tubing performance relationship (TPR)



$\frac{P}{P_c}$ critical pressure gas

$$P_R = P_i \frac{z_R}{z_i} \left(1 - \frac{G_p}{G} \right)$$

$$z_R = f \left(\frac{P_R}{P_c}, \frac{T_R}{T_c} \right)$$

1: Assume P_R

z_R from chart, read z_R with $\frac{P_R}{P_c}, \frac{T_R}{T_c}$

3: verify

$$\overset{\text{assumed}}{P_R} - P_i \frac{\overset{\text{assumed}}{z_R}}{z_i} \left(1 - \frac{G_p}{G} \right) = 0 \quad ?$$

if not

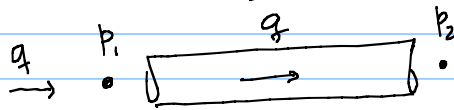
if yes

P_R is the solution !

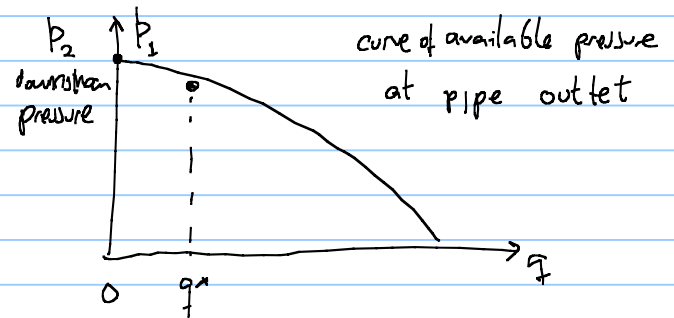
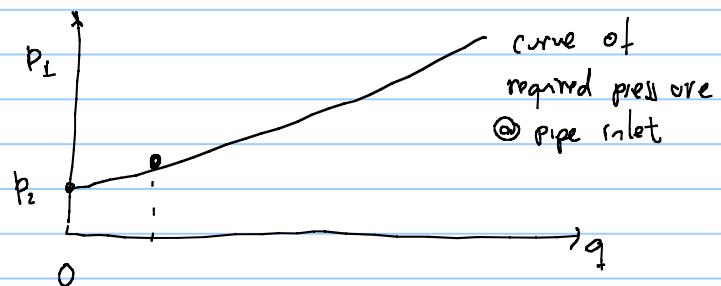
Day 2 03.12.2019

flow equilibrium

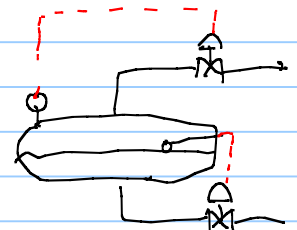
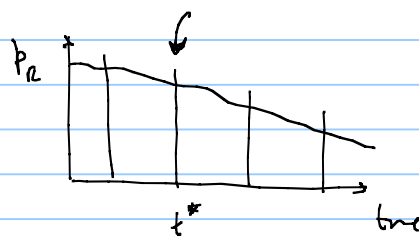
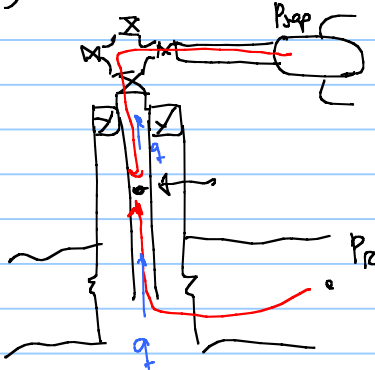
horizontal pipe



$$\Delta p_f = f \frac{L}{\phi} \frac{v^2}{25}$$

1) fixed upstream pressure, p_1 , change q 2) fixed downstream pressure p_2 , vary the rate

looking back at our production system



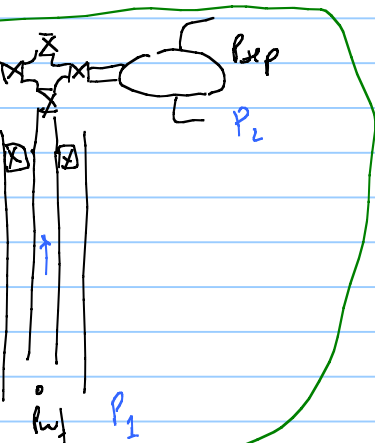
to determine flow rate of petroleum systems we usually use equilibrium analysis

- select an equilibrium point (wellhead p_{wh} bottom-hole p_{wf})
- changes
- pumps

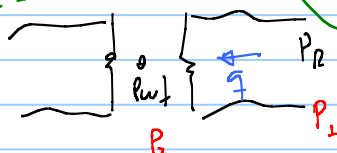
- plot the available pressure curve calculated from the upstream boundary with constant pressure

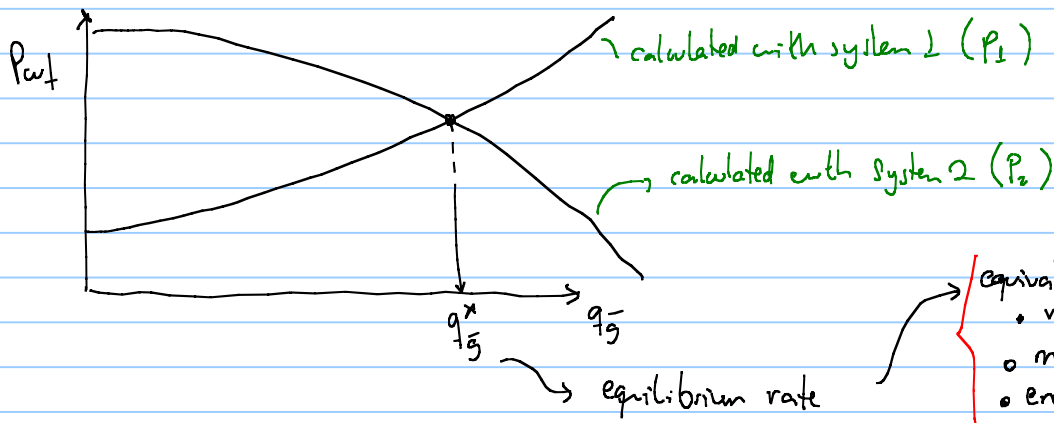
- plot the curve of required pressure from the downstream boundary with constant pressure

System 2



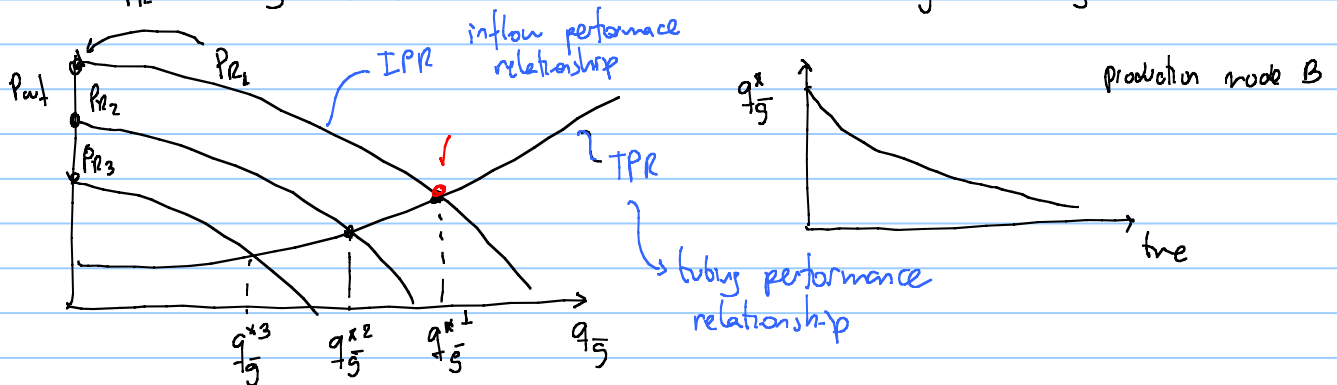
System 1



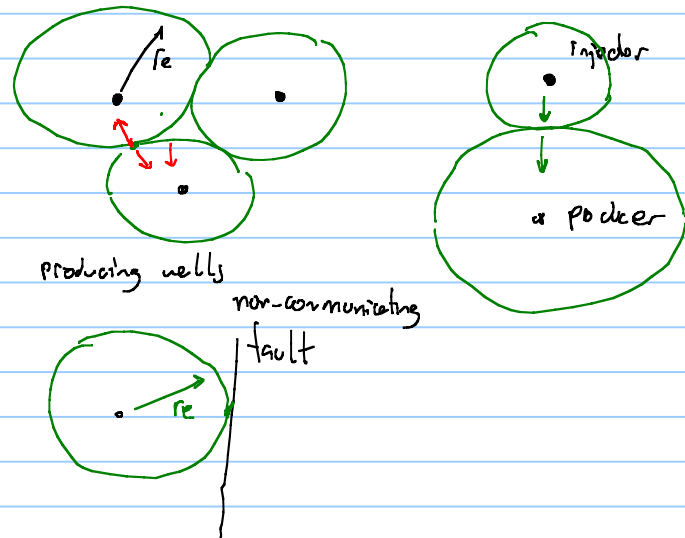
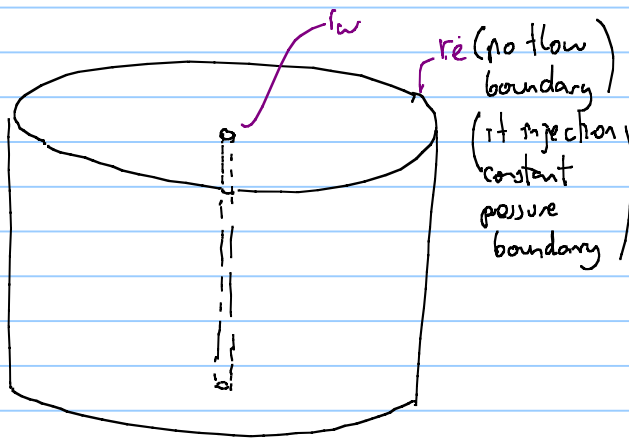


- equivalent to solve:
- mass conservation eq
 - momentum conservation eq
 - energy conservation eq

in time P_R usually declines. how does the intersection change? q_g^*



IPR:



so at time $t=0$

$$p(r=r_w) = P_{wf \text{ const}}$$

@ t_3 the pressure change reaches the boundary

two distinct regimes

$t=0 \rightarrow t_3$ "infinite acting" transient

$t_3 \rightarrow$ forward PSS

pseudo steady state

for PSS, IPR equations can be written as a function of q_g , P_R , P_{wf} only

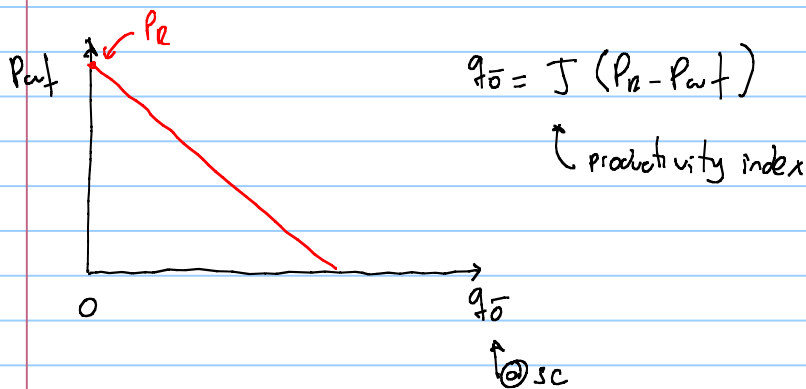
for II, IPR equations must be a function of time, q_g , P_{R2} , P_{wf}

① for conventional reservoirs where K (permeability) is medium-high, the infinite acting $t=0 \rightarrow t_3$ is very short (hours $\rightarrow$ days). therefore, most of the production occurs in PSS

$\rightarrow$ we will work with PSS equations in class

② However for unconventional reservoirs tight reservoir, shale reservoir, K low to super low, the infinite acting period $t=0 \rightarrow t_3$ might take months $\rightarrow$ years. therefore most of the production occurs in II $\hookrightarrow$ IPR must consider time

PSS IPRs for oil, Gas, oil+gas



$$J = \frac{2\pi \cdot k \cdot h}{\mu_o \cdot B_o \cdot \left[\ln\left(\frac{r_e}{r_w}\right) - 0.75 \right]}$$

height of reservoir layer

undersaturated oil

for dry gas

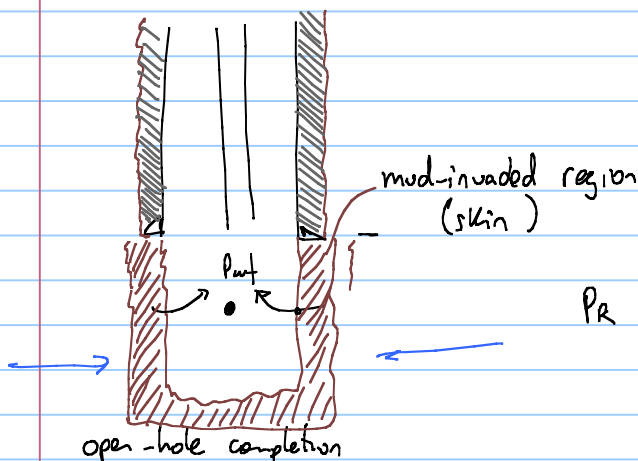


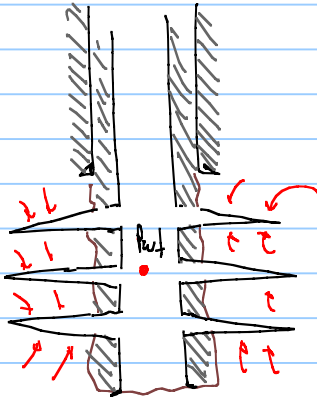
dry gas back pressure equation for medium-low pressure

to capture the effect of skin, a factor S is included in the IPR. for example, for liquid

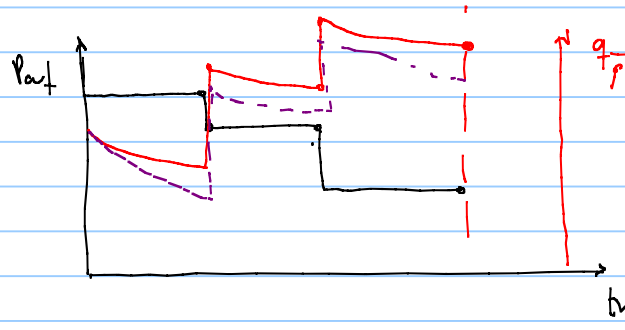
$$J = \frac{2\pi k h}{B_o \mu_o \left(\ln \frac{r_e}{r_w} - 0.75 + S \right)}$$

$q = J (P_R - P_{wf})$ usually consider near well flow impairment "restrictions".



well testing

cased and perforated completion



in program $q_g = f(t, P_{ri}, K, \phi, \mu_o, P_{wf}, h, r_e)$

$$q_{g, \text{measured}} \neq q_{g, \text{simulated}}$$

find reservoir properties (h, K, ϕ) such that

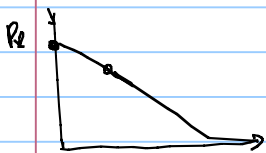
$$q_{g, \text{measured}} = q_{g, \text{simulated}}$$

$$q_g = \frac{2\pi kh}{\left[\ln \frac{r_e}{r_w} - 0.75 + S \right]} \frac{T_{sc}}{T_R P_{sc}} \left(\frac{1}{M^2} \right) \frac{1}{2} (P_{ri}^2 - P_{wf}^2)$$

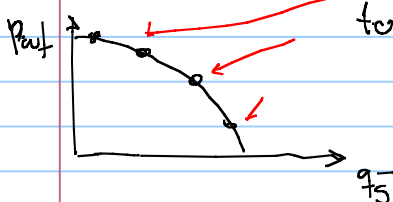
C , backpressure coefficient

IPR's can be estimated from analytical equations derived for simple cases or can be derived from stabilized well tests

$$q = J(P_{ri} - P_{wf})$$



$$q = C(P_{ri}^2 - P_{wf}^2)^n$$

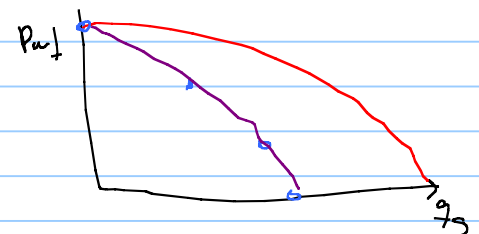


find C and n to reproduce test results

C ☐

n ☐

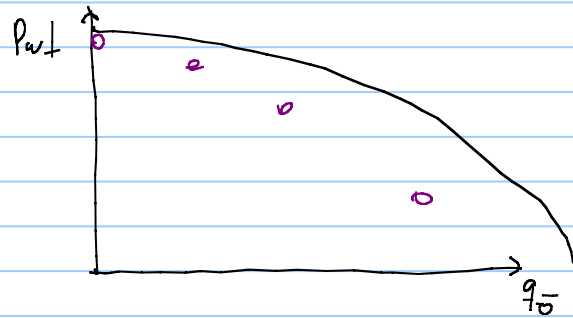
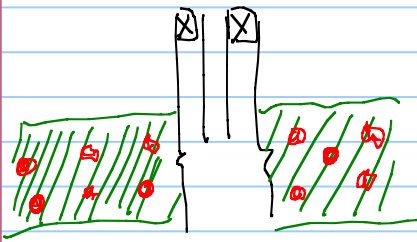
P_{wf}	q_g
☐	☐
☐	☐
☐	☐



change C, n until passes through $\bullet$

depending on reservoir mins $\rightarrow$ hrs $\rightarrow$ days

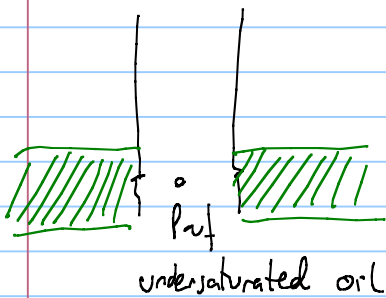
Saturated oil (simultaneous flow of oil and gas near wellbore)



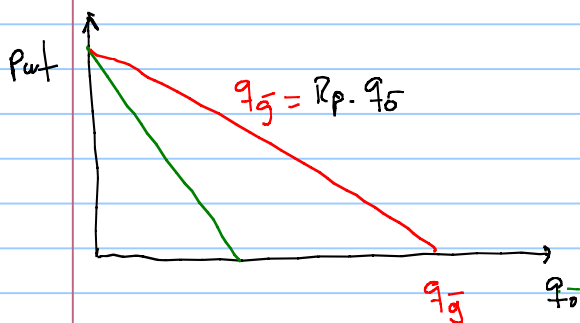
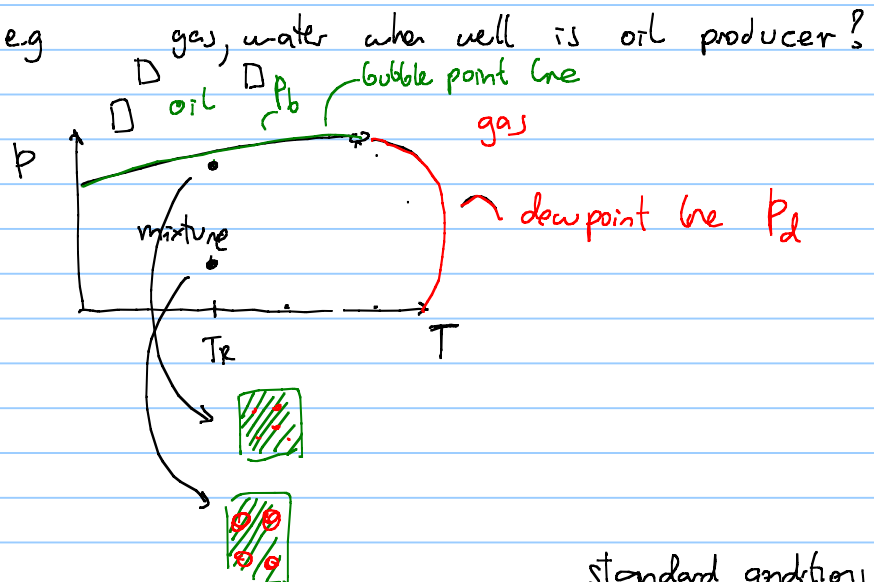
analytical expressions are more complex, but people typically use Vogel

$$\frac{q_o}{q_{o,max}} = 1 - 0.2 \frac{P_{wf}}{P_R} - \frac{P_{wf}^2}{P_R^2} \quad \text{tune } q_{o,max} \text{ to measurements}$$

How to compute other phases? e.g.



$$P_{wf} > P_b @ T_R$$



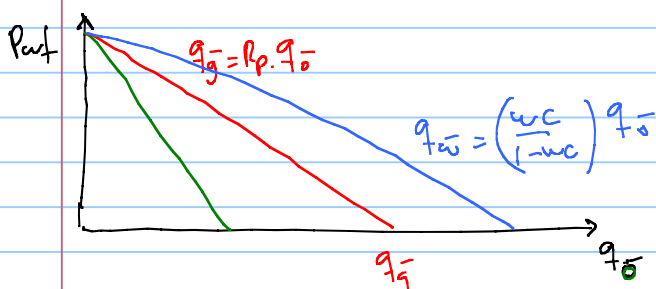
standard conditions P_{sc}, T_{sc}



$$R_p = \frac{V_g}{V_o} \quad \text{GOR,}$$

$$WC = \frac{q_w}{q_o + q_w} \Rightarrow q_w (1 - WC) = q_o WC$$

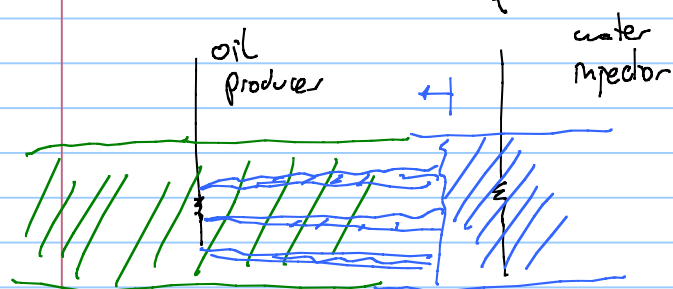
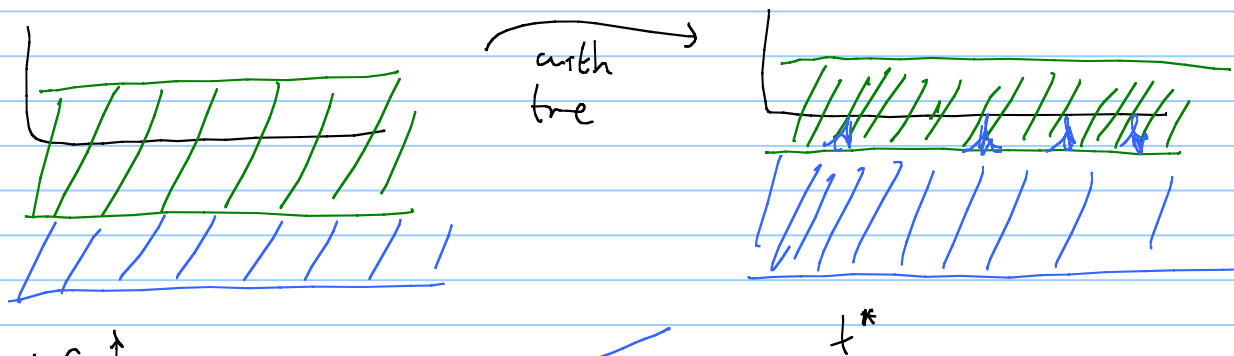
$$q_w = q_o \left(\frac{WC}{1 - WC} \right)$$



R_p and WC might change with time!

for example

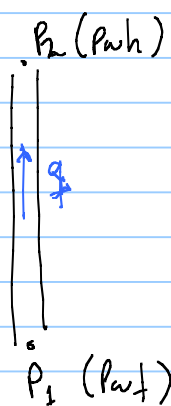
for example WC might change with water cusping



"Available" curve (IPR) ✓

required curve (TPR)

tubing performance relationship



$$q_j = C_T \left(\frac{P_1^2}{e^j} - P_2^2 \right)^{0.5}$$

tubing coefficient

elevation coefficient (NOT skin)

$$P_1 = \left[\left(\frac{q_j}{C_T} \right)^2 + P_2^2 \right] e^j$$

$$P_2 = \sqrt{\frac{P_1^2}{e^j} - \left(\frac{q_j}{C_T} \right)^2}$$

Tubing flow Equation-Dry gas

universal gas constant
 $R = 8.314 \frac{\text{J}}{\text{mol K}}$

$$q_{sc} = \left(\frac{\pi}{4} \right) \left(\frac{R}{M_{air}} \right)^{0.5} \left(\frac{T_{sc}}{P_{sc}} \right) \left[\frac{D^5}{\gamma_g f_M Z_{av} T_{av} L} \right]^{0.5} \left(\frac{se^s}{e^s - 1} \right)^{0.5} \left(\frac{p_1^2}{e^s} - p_2^2 \right)^{0.5}$$

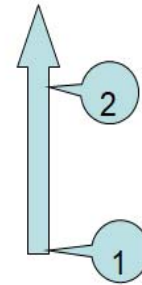
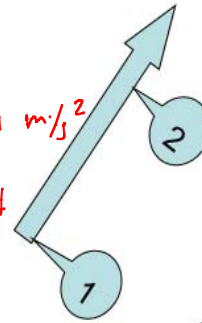
$M = \text{molecular weight}$
 $M_{air} = 28.97$

$$\frac{s}{2} = \frac{M_g g}{Z_{av} R T_{av}} H = \frac{(28.97) \gamma_g g}{Z_{av} R T_{av}} H$$

height difference

$$q_{gsc} = C_T \left(\frac{p_1^2}{e^s} - p_2^2 \right)^{0.5}$$

$\frac{T_{wh} + T_{inlet}}{2}$



$Z_{av} = \frac{Z_{wh} + Z_{inlet}}{2}$

γ_g gas specific gravity

$$\gamma_g = \frac{M_{wg}}{M_{Wair}}$$

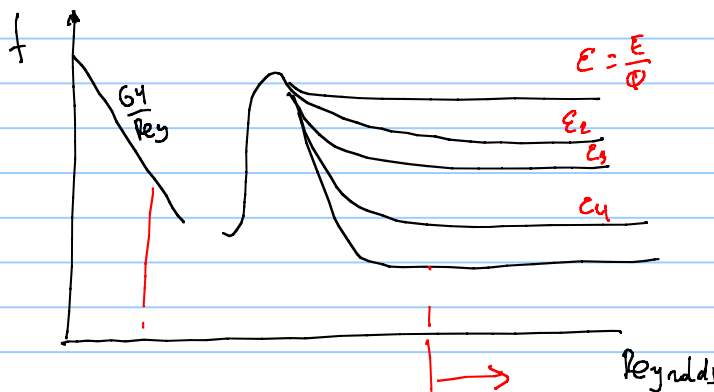
$\text{CH}_4 \quad 12 + 4 = 16$

$$\gamma_{\text{CH}_4} = \frac{16}{28.97}$$

$$\gamma_{\text{CH}_4} = 0.55$$

$$p_{inlet} = p_1 = e^{s/2} \left(p_2^2 + \frac{q_g^2}{C_T^2} \right)^{0.5}$$

$$p_{wh} = p_2 = \left(\frac{p_1^2}{e^s} - \frac{q_g^2}{C_T^2} \right)^{0.5}$$



$$Re = \frac{v \rho \phi}{\eta}$$

Re are usually very high
 v are high

M are very low

liquid 10^{-3} Pa.s

gas 10^{-5} Pa.s

gas is usually in the turbulent fully region

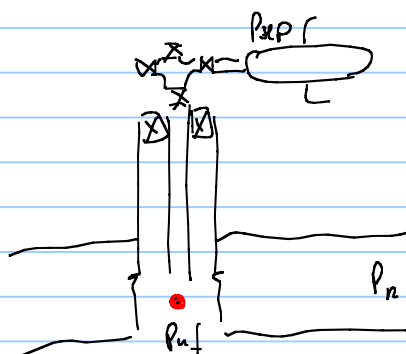
$$f \neq F(Re)$$

$$f = f(\epsilon)$$

$$\epsilon = f(\phi)$$

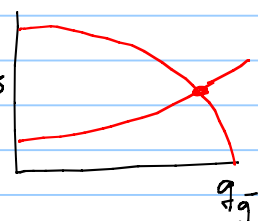
$$f_M = \frac{0.01748}{D^{0.224} \cdot \left(|1 \text{ m}| \cdot \left| \frac{39.37 \text{ in}}{1 \text{ m}} \right| \right)^{0.224}} = \frac{0.0077}{D^{0.224}}$$

Class exercise



$$q_g = C_R (p_R^2 - p_{wf}^2)^\eta$$

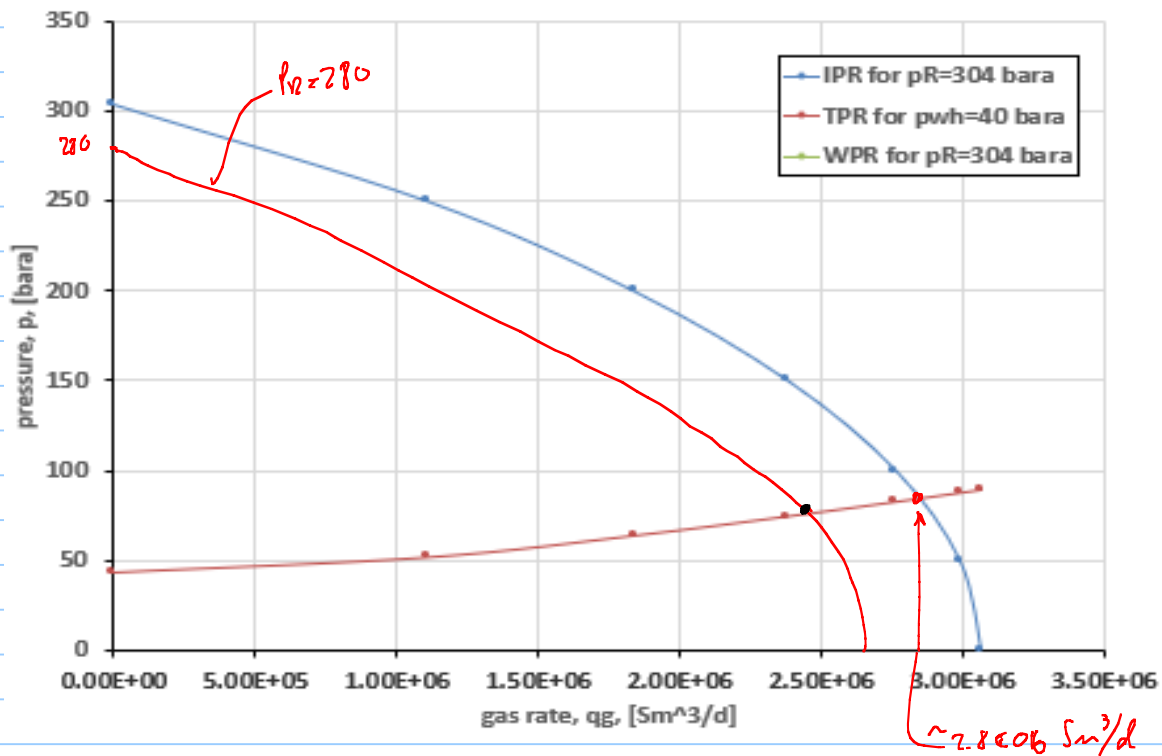
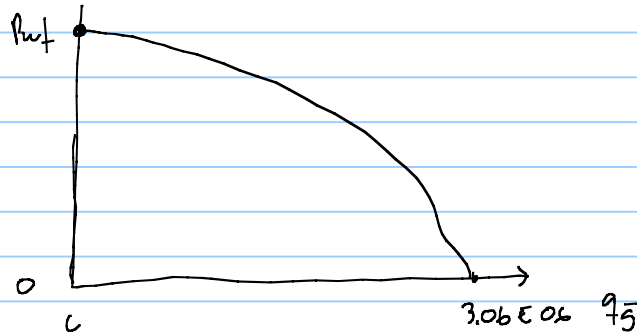
$$p_{wf} = \left(p_R^2 - \left(\frac{q_g}{C_R} \right)^{1/\eta} \right)^{1/2}$$



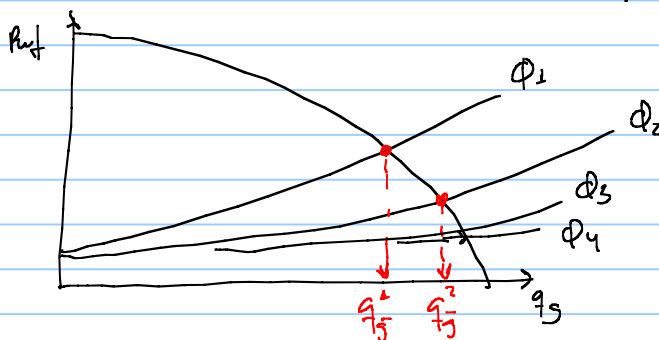
from $p_{wp} \rightarrow p_{wf}$

$$p_{wf} = \left[\left(\frac{q_g}{c_r} \right)^2 + p_{wh}^2 \right] e^S \quad \checkmark$$

p _{wf} _avail [bara]	IPR q _g [Sm ³ /d]
304	0.00E+00
250	1.11E+06
200	1.84E+06
150	2.38E+06
100	2.76E+06
50	2.99E+06
0	3.06E+06



How do we decide on tubing size (Φ) **NOT POROSITY!**
 $\Phi \uparrow$



$$\Phi_2 > \Phi_1$$

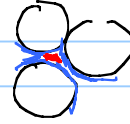
$\Phi \uparrow$ also costs more

Φ_3 and Φ_4 don't give a substantial increment in rate

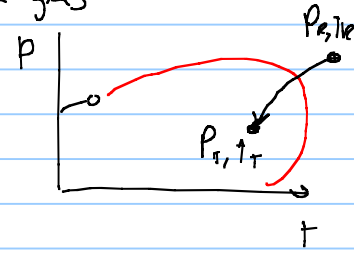
Usually wells produce not only gas, but liquid $\rightarrow$ oil condensing from gas



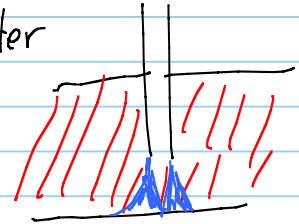
$\rightarrow$ water condensing out of gas



$\rightarrow$ coning from aquifer



the gas must evacuate the liquid from well
gas velocity v_g must be high enough to
drag liquid out of well



$\uparrow \Phi$ $v_g \downarrow$ then liquid dragging capacity will be reduced $\Rightarrow$ liquid loading

choose a diameter that assures liquid is carried to surface

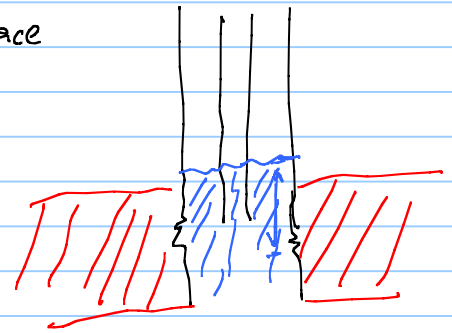
v_g should be high enough

F_d Buoyancy



liquid droplet

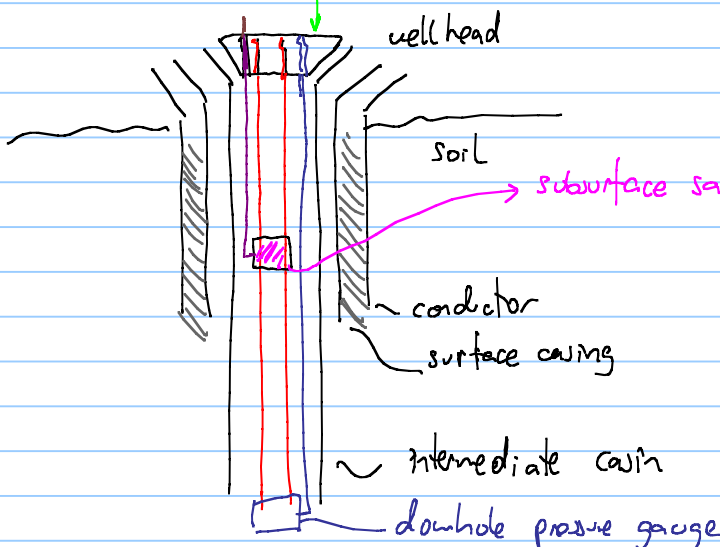
$$F_d + F_B = F_{\text{weight}} \Rightarrow v_g \text{ runner}$$



- Erosion usually wells produce particles and liquid, if Φ is too small this can cause erosion.

$$v_g < v_{\text{erosional}} \rightarrow \text{API 14E}$$

- tubing hanger



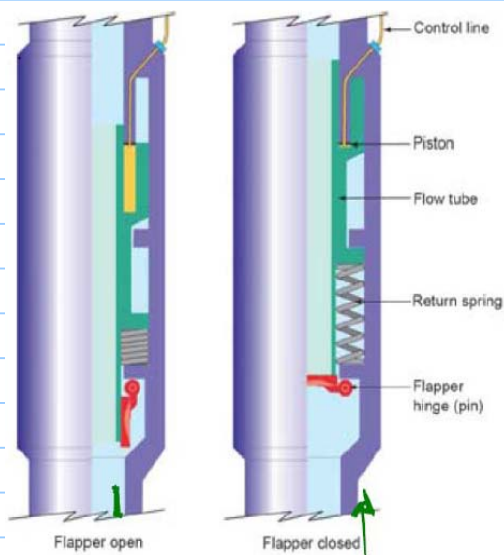
leave enough space in the hanger

$\rightarrow$ subsurface safety valve SSSV

conductor
surface casing

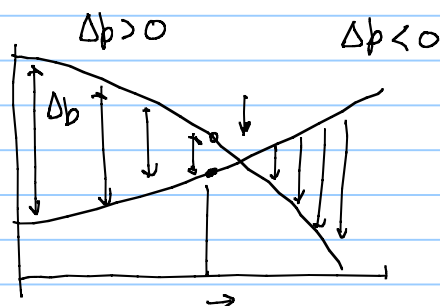
intermediate casing

downhole pressure gauge



how to find the equilibrium point

find x^* such that $f_1(x^*) = f_2(x^*)$
 $f_1(x)$
 $f_2(x)$
 $f_3 = f_1 - f_2$ find x^* such that $f_3(x^*) = 0$
 root finding



	IPR	TPR	
pwf_avail	qg	pwf_req	pwf_avail - pwf_req
[bara]	[Sm ³ /d]	[bara]	[bara]
304	0.00E+00	43.2	260.8
250	1.11E+06	51.6	198.4
200	1.84E+06	63.7	136.3
150	2.38E+06	74.4	75.6
100	2.76E+06	82.5	17.5
50	2.99E+06	87.4	-37.4
0	3.06E+06	89.1	-89.1

the solution is between these two. When $P_{wf_avail} - P_{wf_req}$ equals zero

	IPR	TPR	
pwf_avail	qg	pwf_req	pwf_avail - pwf_req
[bara]	[Sm ³ /d]	[bara]	[bara]
304	0.00E+00	43.2	260.8
250	1.11E+06	51.6	198.4
200	1.84E+06	63.7	136.3
150	2.38E+06	74.4	75.6
84.3784	2.85E+06	84.4	0.0
50	2.99E+06	87.4	-37.4
0	3.06E+06	89.1	-89.1

Goal seek

equilibrium rate $q_g = 1.85 \times 10^6 \text{ Sm}^3/\text{d}$

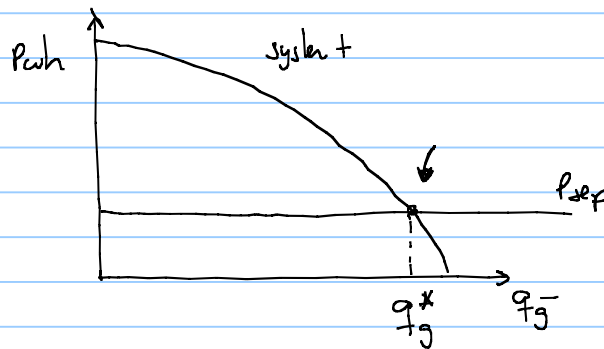
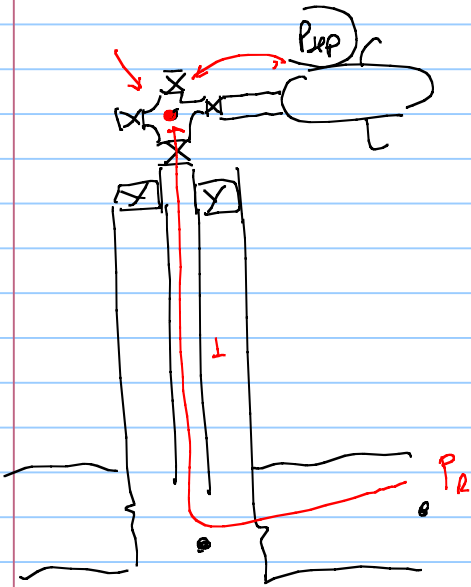
$P_{wf} = 84.37 \text{ bara}$

$$q_g = C_R (P_a^2 - P_{wf}^2)^n$$

$$q_g = C_T \left(\frac{P_{wf}^2}{e^{\frac{2}{\alpha}}} - P_{wh}^2 \right)^{0.5}$$

two equations with two unknowns

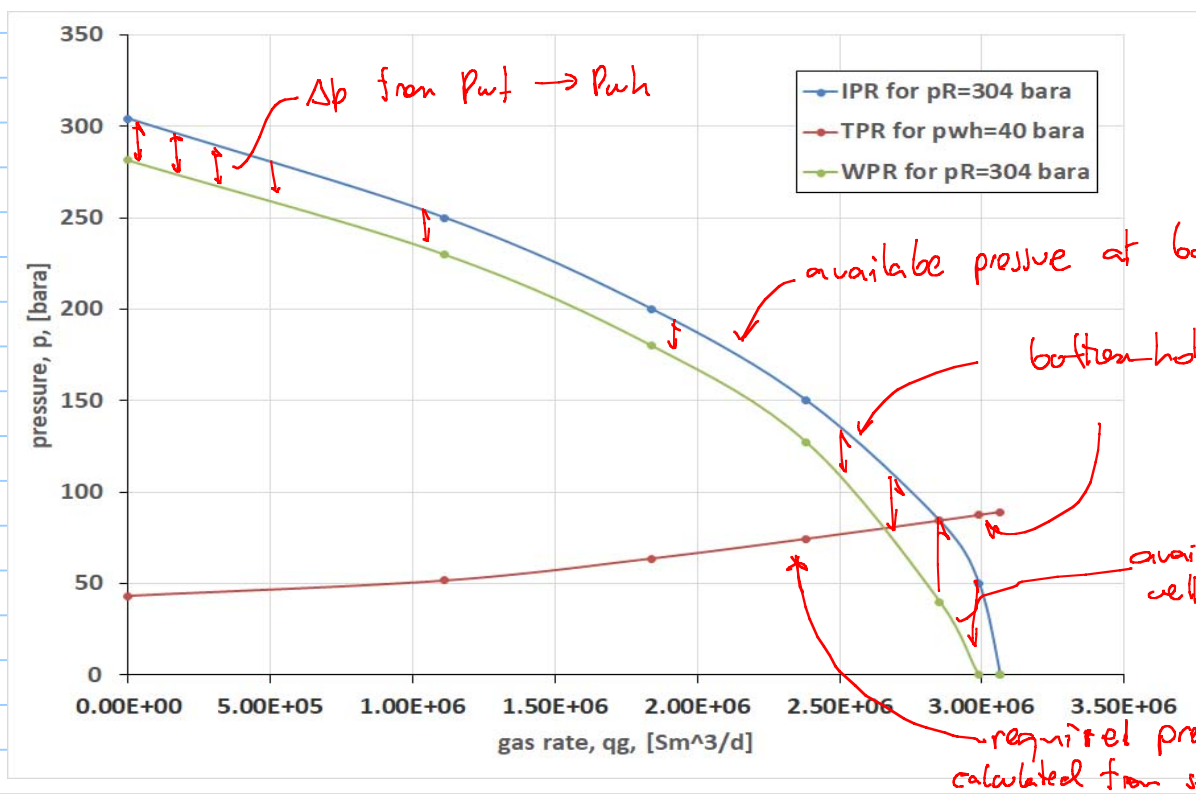
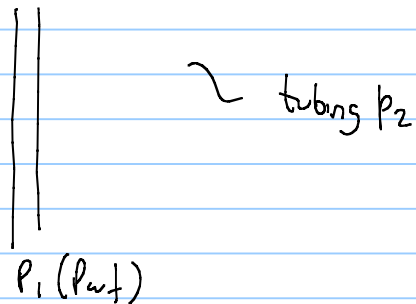
- change equilibrium point $\rightarrow$ at well head

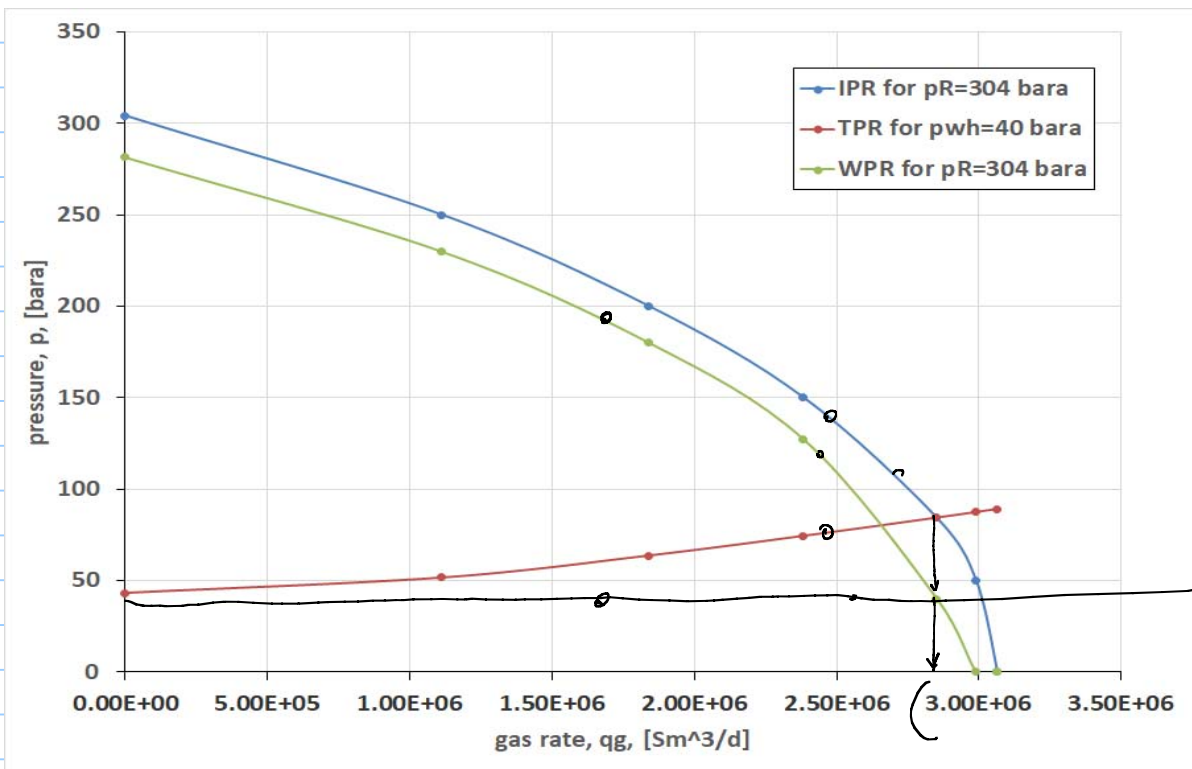


very close to wellhead, therefore friction of flowline is neglected

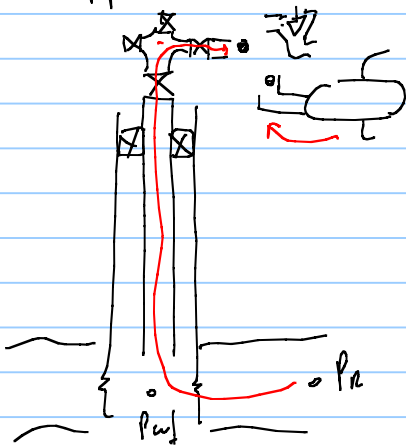
$\rightarrow 2.85 \text{ E}06 \text{ Sm}^3/\text{d}$ same system!
the system is the same regardless of equilibrium point

map from $P_{wh} \rightarrow P_{wh}$
 $\rightarrow P_L(P_{wh})$

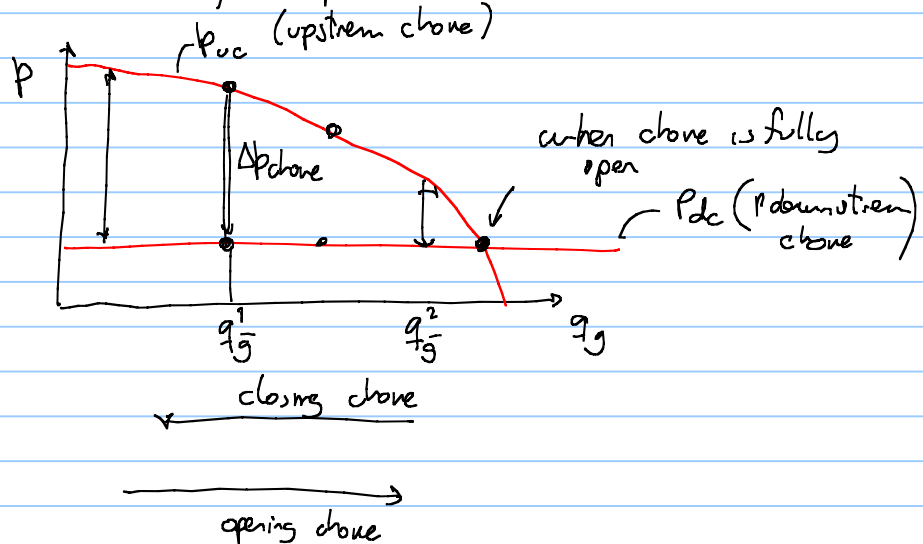


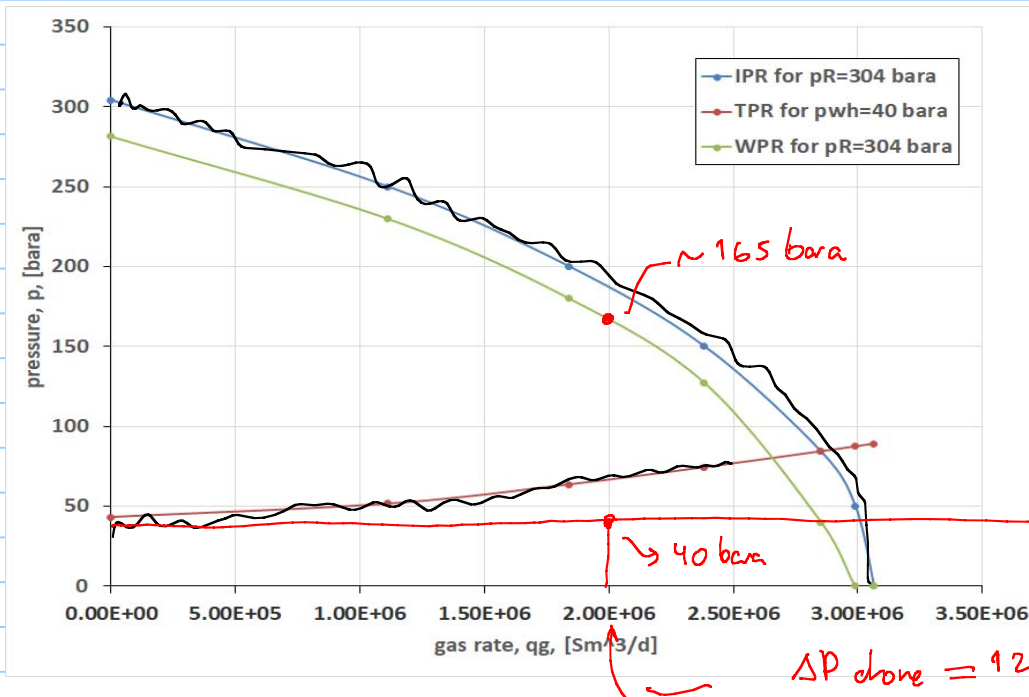


what happens when there is a choke?

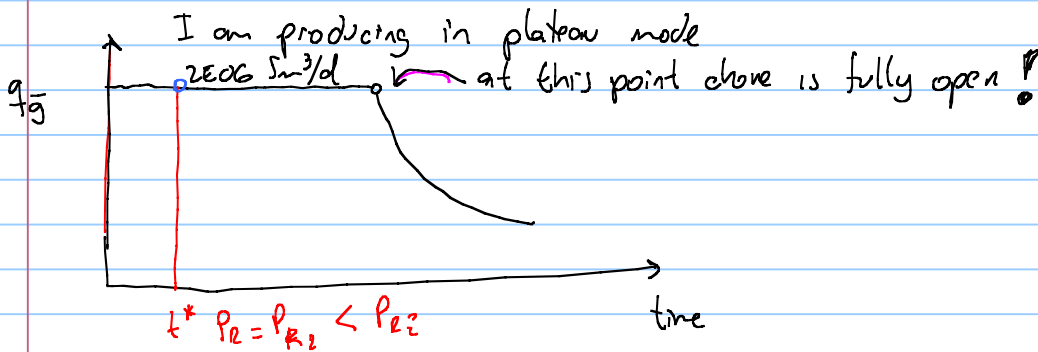


- remove choke
- compute available pressure at choke inlet and required pressure at choke outlet

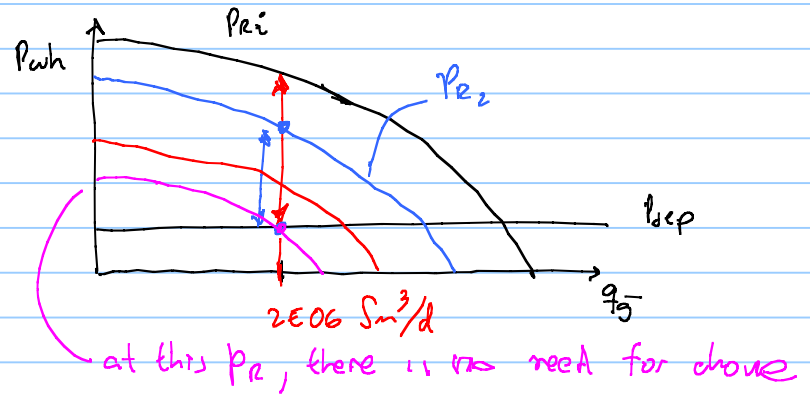
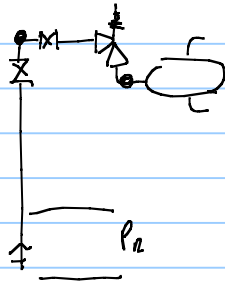




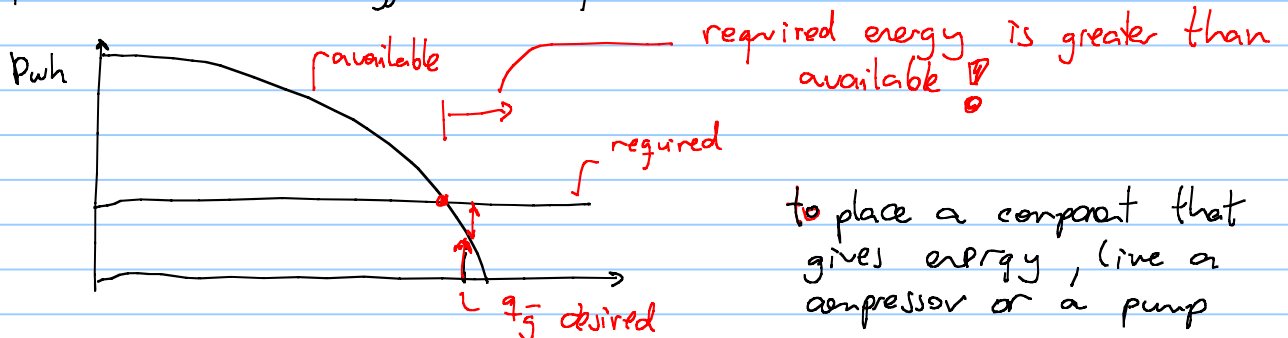
what chore Δp is needed to produce $q_g = 2.00 \times 10^6$ Sm³/d?

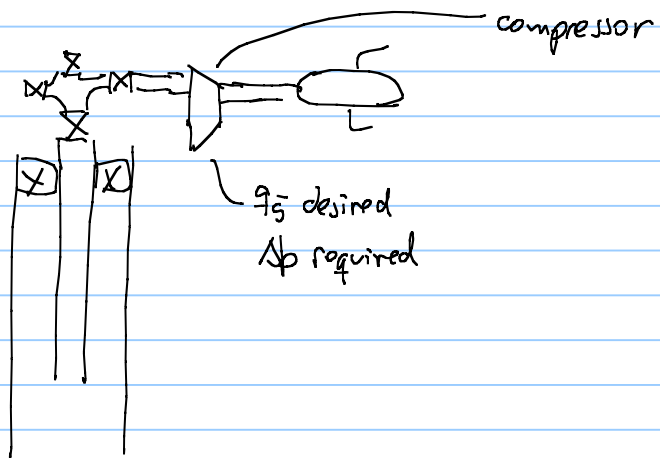


$$\Delta p_{chore2} < \Delta p_{chore}^i$$



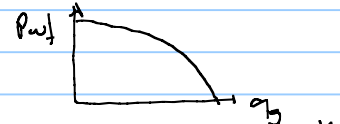
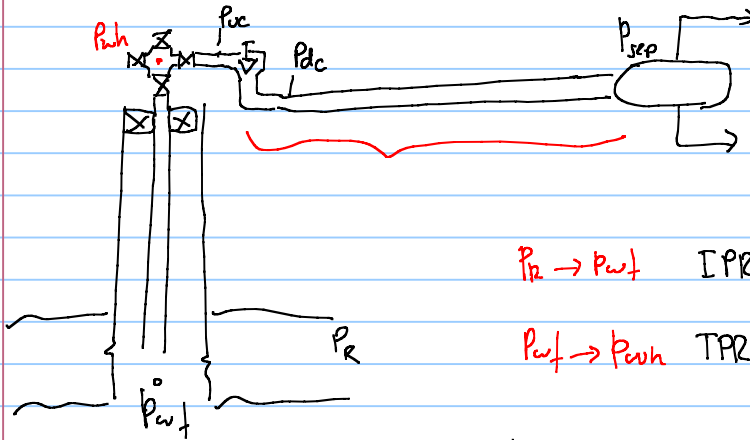
what if i need a rate bigger than equilibrium rate?





Day 3 04.12.2019

(B2 Tanzania)

 $P_R \rightarrow P_{wh}$ IPR equation

$$q_g = C_R (P_R^2 - P_{wh}^2)^n$$

 $P_{wh} \rightarrow P_{wh}$ TPR equation

$$q_g = C_T \left(\frac{P_{wh}^2}{e^s} - P_{wh}^2 \right)^{0.5}$$

$P_{vc} \rightarrow P_{dc}$ no equation, simply fix the rate and calculate available pressure upstream and required pressure downstream

$P_{dc} \rightarrow P_{sep}$ FPR (flowline performance relationship)
assuming horizontal flowline $H=0$

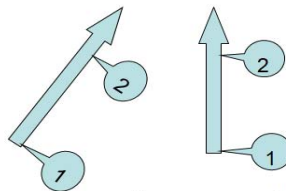
if $H=0$ $S=0$

Tubing flow Equation-Dry gas

$$q_{sc} = \left(\frac{\pi}{4} \right) \left(\frac{R}{M_{air}} \right)^{0.5} \left(\frac{T_{sc}}{P_{sc}} \right) \left[\frac{D^5}{\gamma_g f_M Z_{av} T_{av} L} \right]^{0.5} \left(\frac{s e^s}{e^s - 1} \right)^{0.5} \left(\frac{P_1^2}{e^s} - P_2^2 \right)^{0.5}$$

$$\frac{s}{2} = \frac{M_g g}{Z_{av} R T_{av}} H = \frac{(28.97) \gamma_g g}{Z_{av} R T_{av}} H$$

$$q_{gsc} = C_T \left(\frac{P_1^2}{e^s} - P_2^2 \right)^{0.5}$$



$$P_{inlet} = P_1 = e^{s/2} \left(P_2^2 + \frac{q_g^2}{C_T^2} \right)^{0.5}$$

$$P_{wh} = P_2 = \left(\frac{P_1^2}{e^s} - \frac{q_g^2}{C_T^2} \right)^{0.5}$$

$$e^s \quad e^0 = 1$$

$$\left(\frac{s e^s}{e^s - 1} \right)^{0.5} \quad s \rightarrow 0 ?$$

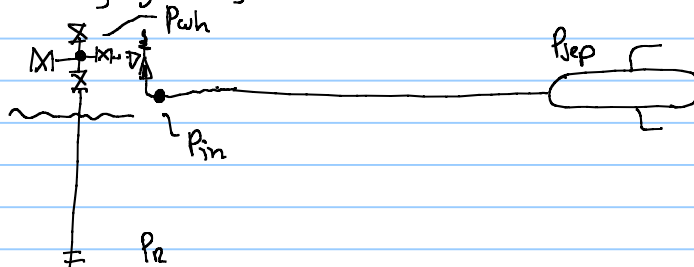
$$\frac{0.1}{1-1} \rightarrow \frac{0}{0} \quad \text{L'Hopital}$$

$$\lim_{s \rightarrow 0} \frac{s \cdot e^s}{e^s - 1} = \frac{e^s + e^s \cdot s}{e^s}$$

$$\text{if } s=0 \quad \frac{1+0}{1} = 1$$

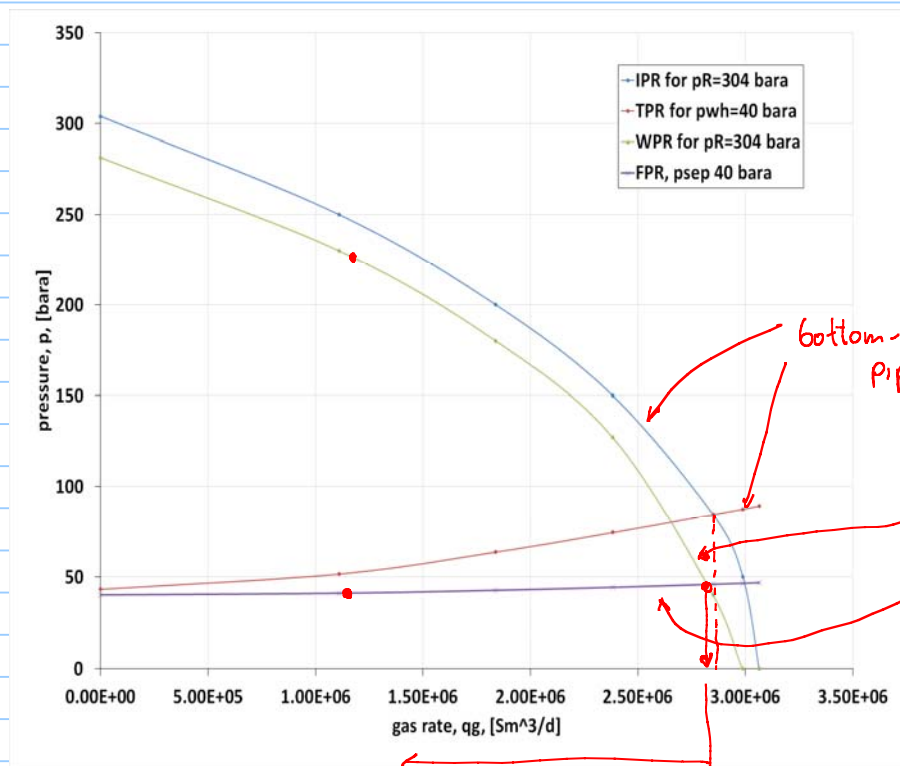
$$\text{for horizontal flowline} \quad q_g = C_{F2} (P_1^2 - P_2^2)^{0.5}$$

Revisiting yesterday's exercise

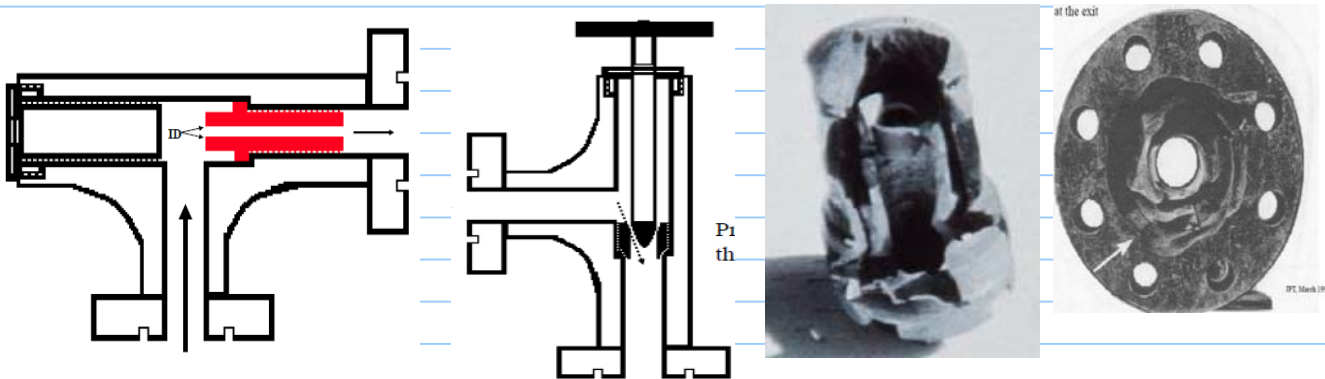


$P_R \rightarrow P_{wh} \rightarrow P_{wh}$ available pressure at wellhead

$P_{sep} \rightarrow P_{in}$ required pressure at flowline inlet



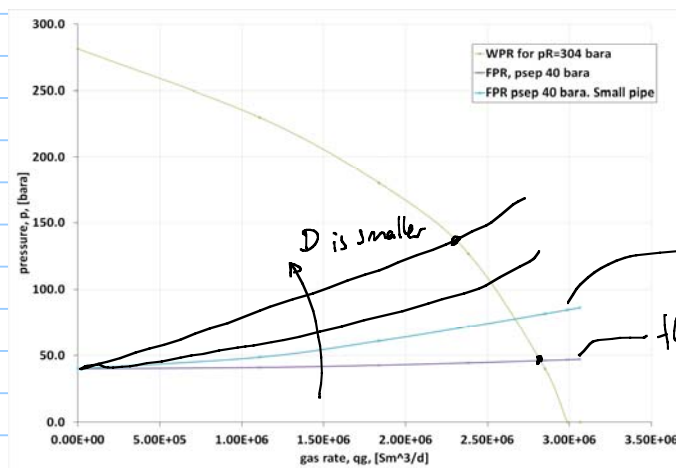
with a choke, p_{wh} is at the upstream and p_{in} is at downstream therefore, I can obtain all rates to the left



it is challenging to operate the choke with high $\Delta p \rightarrow$ high velocities $\rightarrow$ high erosion



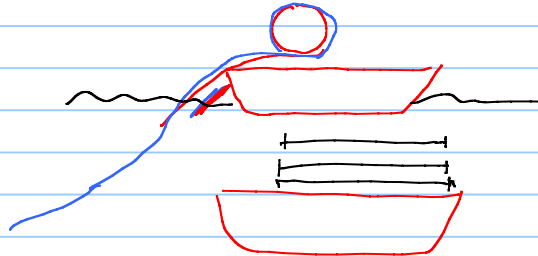
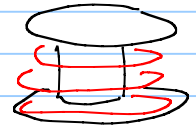
"newer" design to avoid excessive erosion



how to decide on flowline diameter?

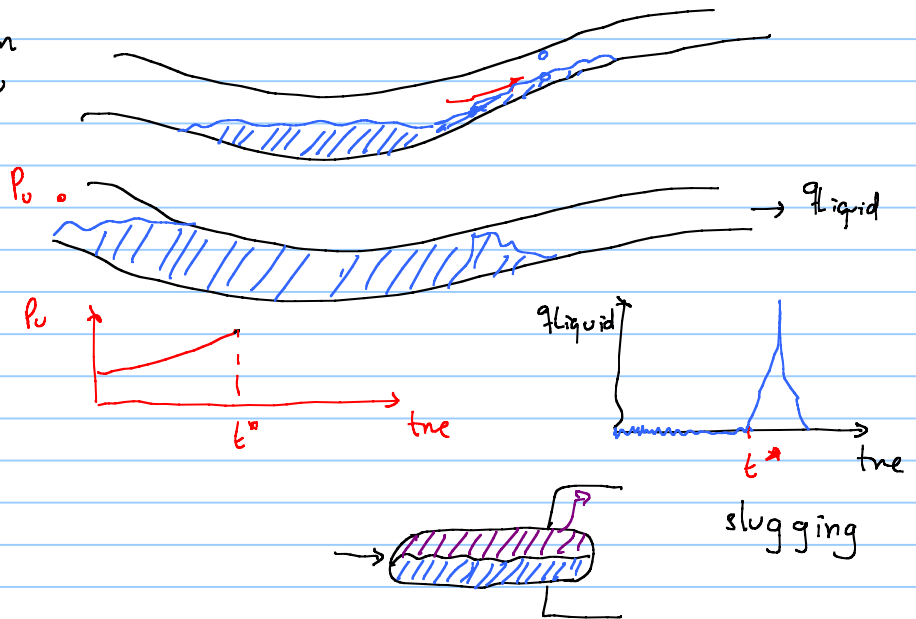
- provide desired rate $\rightarrow$ minimize pressure drop
- minimize pipe cost $\rightarrow$ large pipe is more costly to manufacture to transport to install

small diameter pipe can be reeled



- avoid erosion
- avoid liquid accumulation
increase N_g reducing ϕ

if slugging cannot be avoided a different type of separator is needed (slugcatcher)



- avoid excessive cooling

big diameter increases surface area, increases heat transfer

$$\dot{q} = U A (T_f - T_{amb})$$

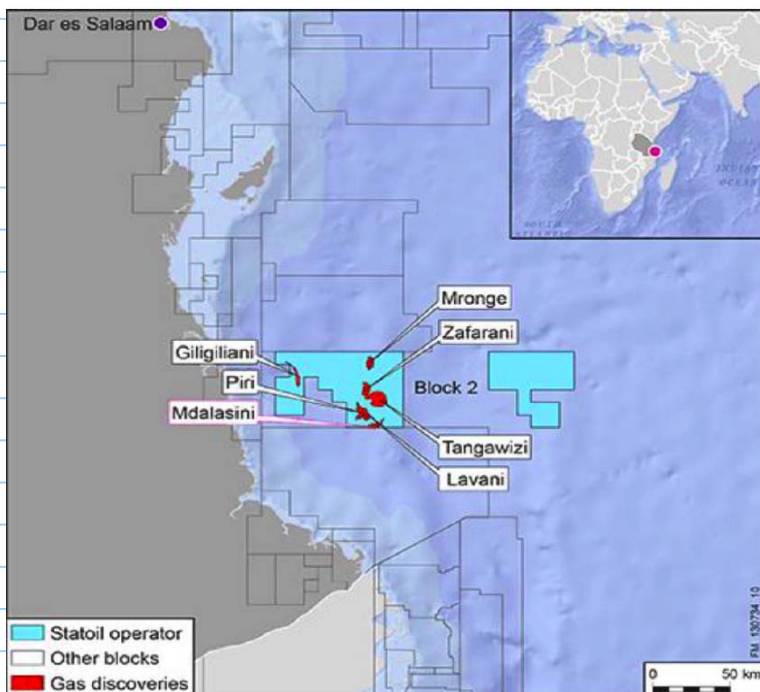
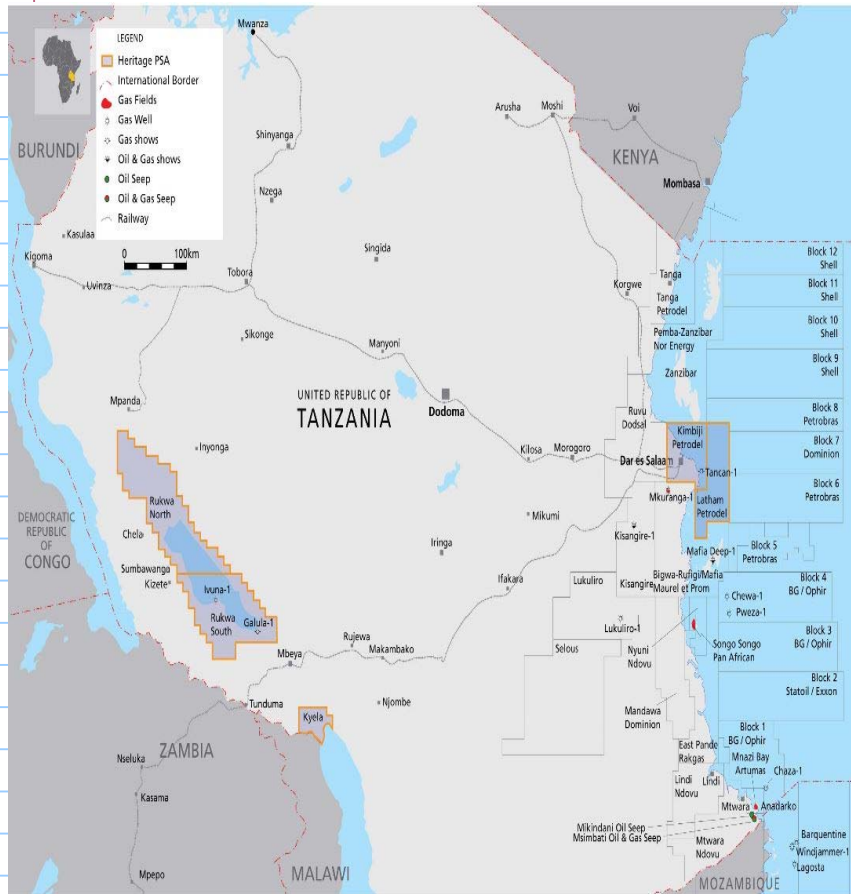
$\downarrow$ heat $\downarrow$ universal heat transfer coefficient $\downarrow$ fluid

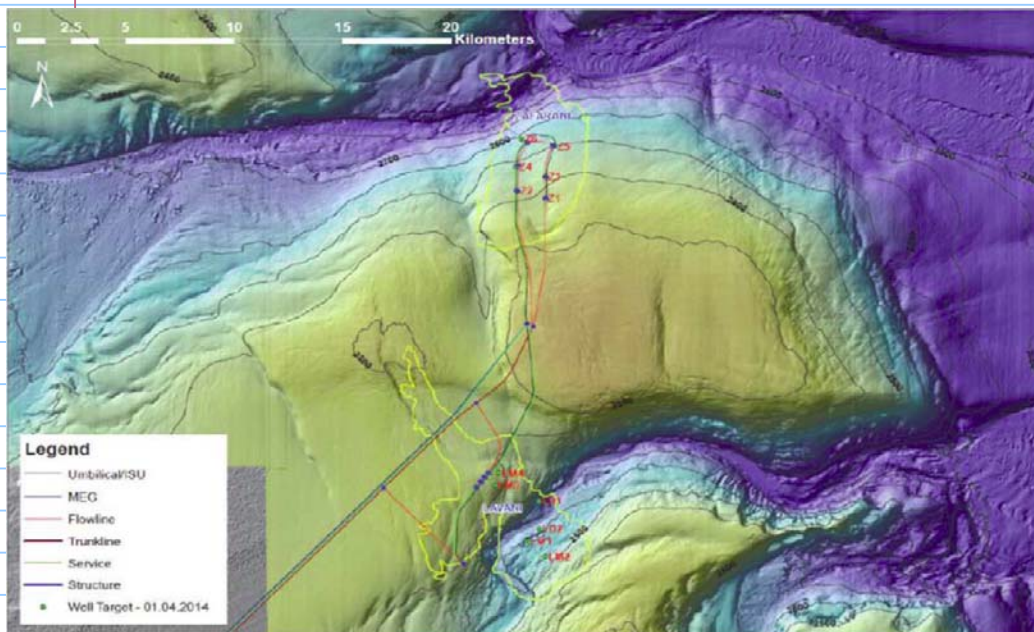
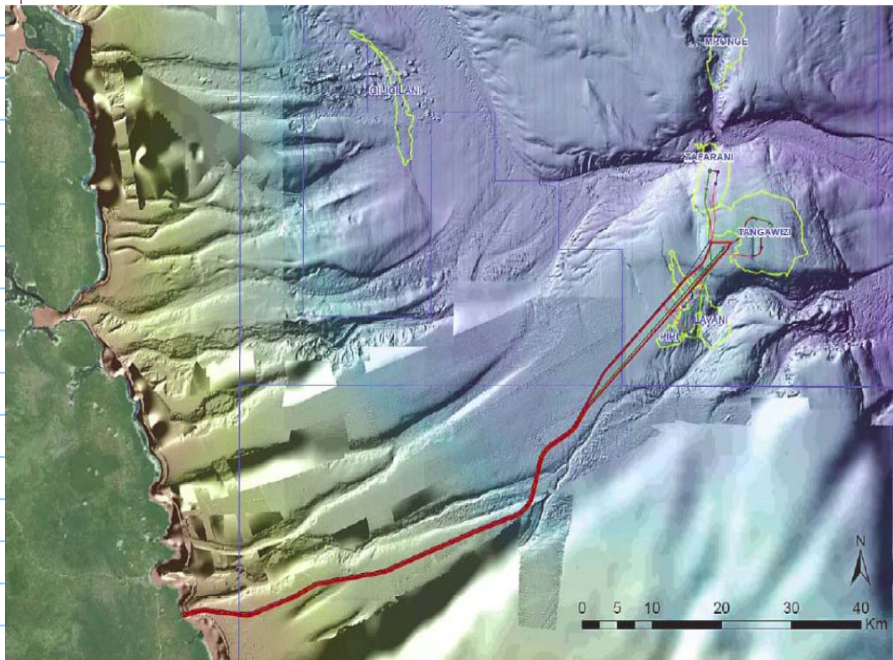
cooling and low temperatures can lead to hydrates, wax

Production scheduling calculations for offshore gas field

estimating q_{field} vs time (very important for revenue calculations
cost estimation
NPV calculations)

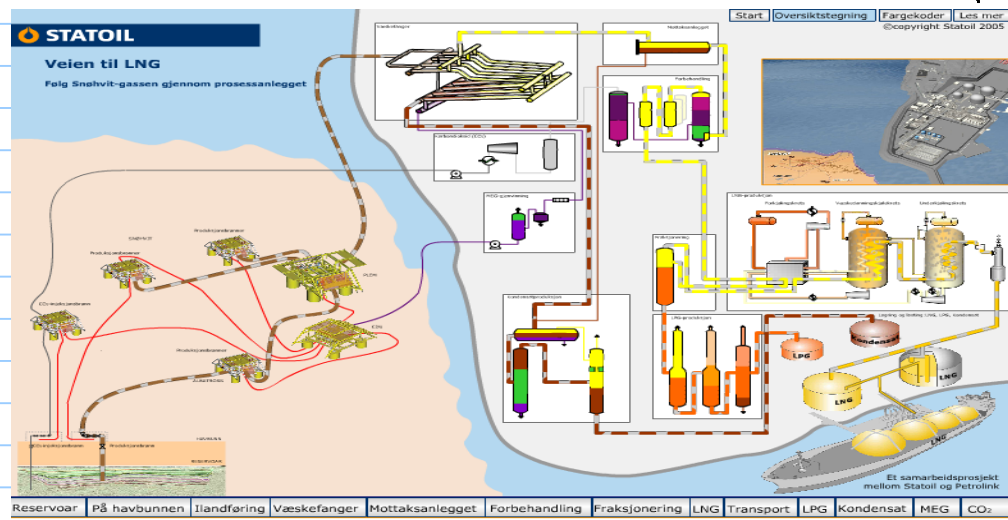
Case: Block 2 offshore Tanzania

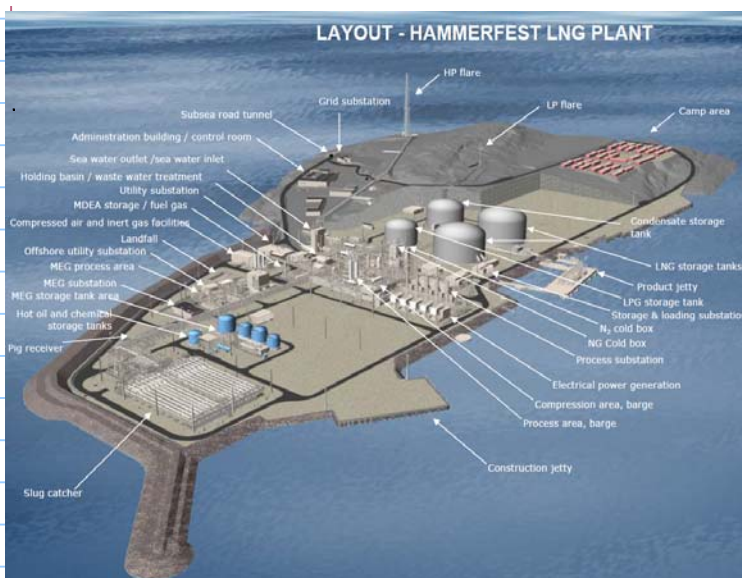
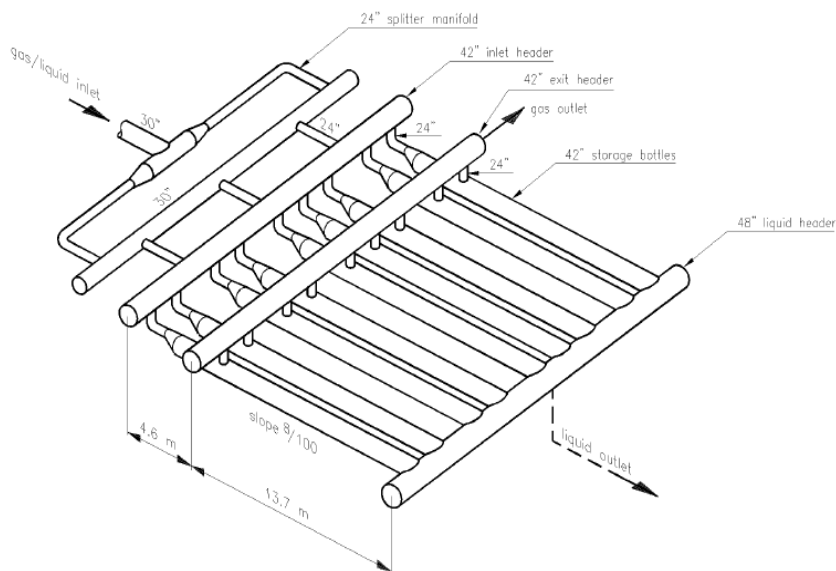




in Norway there is a field very similar to B2, Snøhvit (Snowhite)

Subsea to beach : subsea wells, no platform, no offshore structure and a long transportation pipeline to shore





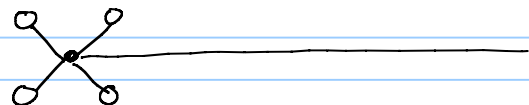
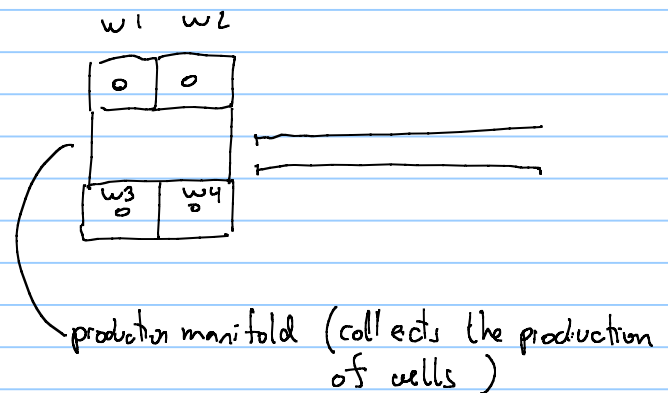
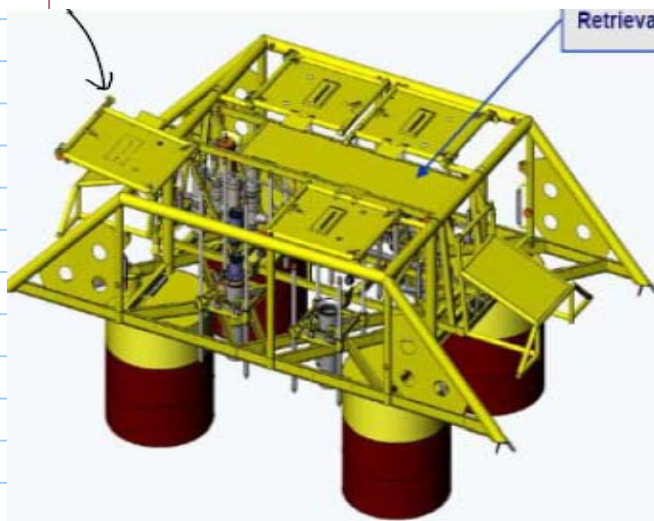
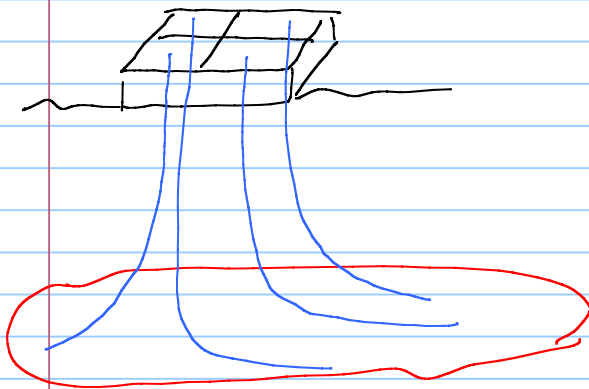
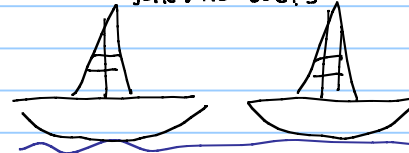
Subsea layout

typically, wells are arranged in templates

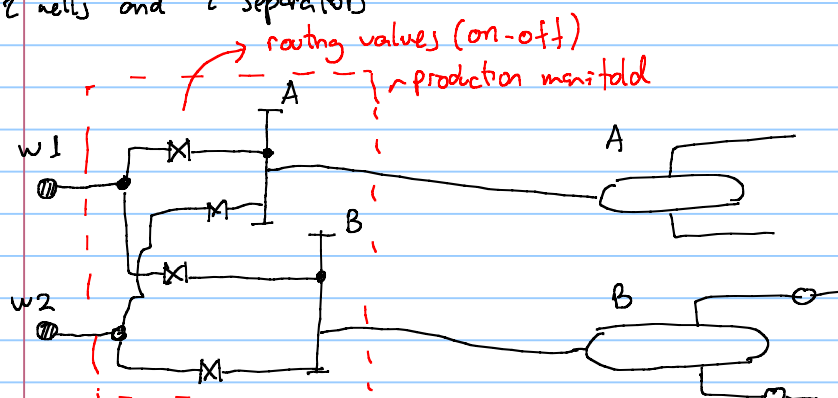
4-slot template



satellite wells



2 wells and 2 separators



to have the option to send production from w1 to A or to B

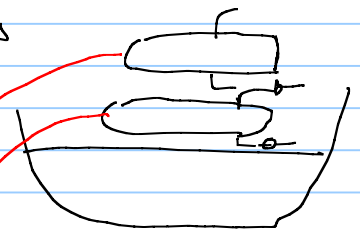
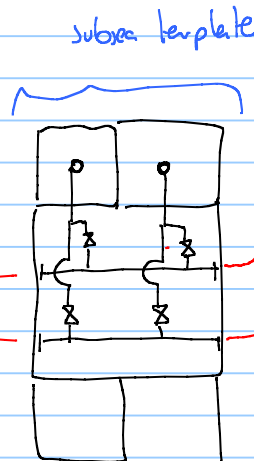
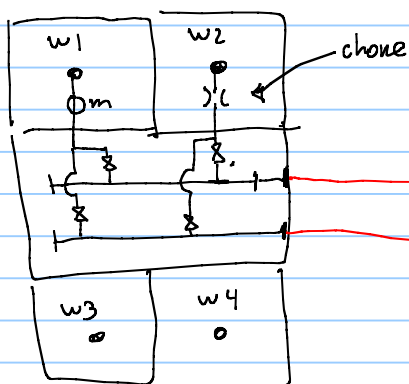
include a header for each destination

Reasons to use a production manifold : for well testing (allocation)

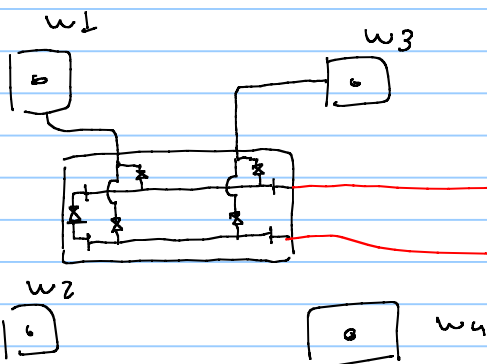
↳ to find out how much is the well producing and split production and revenue among partners
to improve models (production
(reservoir
history matching)



subsea, we have the same arrangement of headers, routing valves, and pipes for template wells



what happens when you have satellite wells?

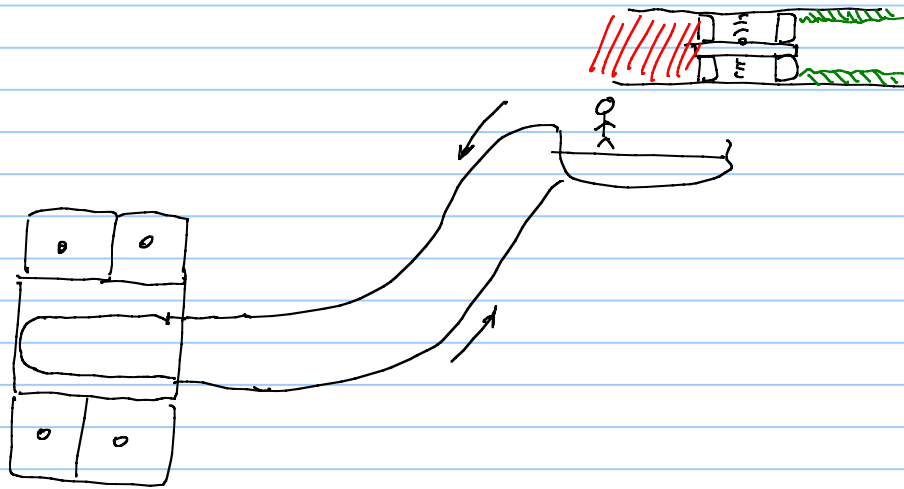


some reasons to have two flowlines :

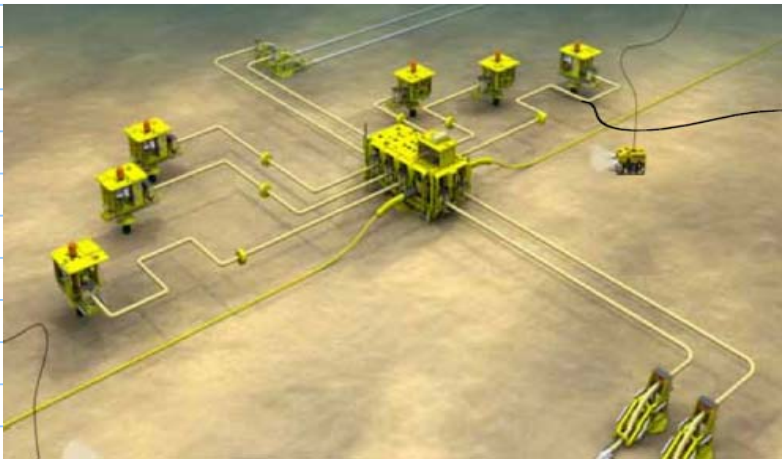
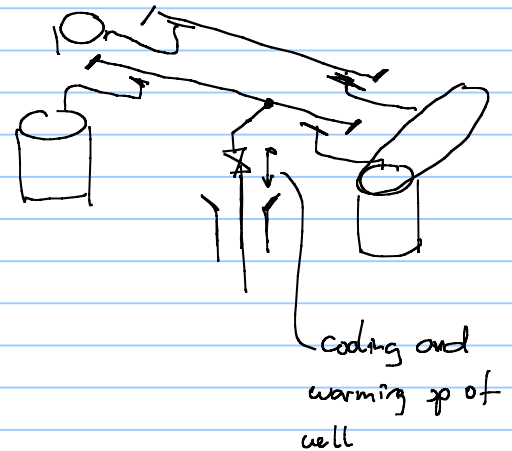
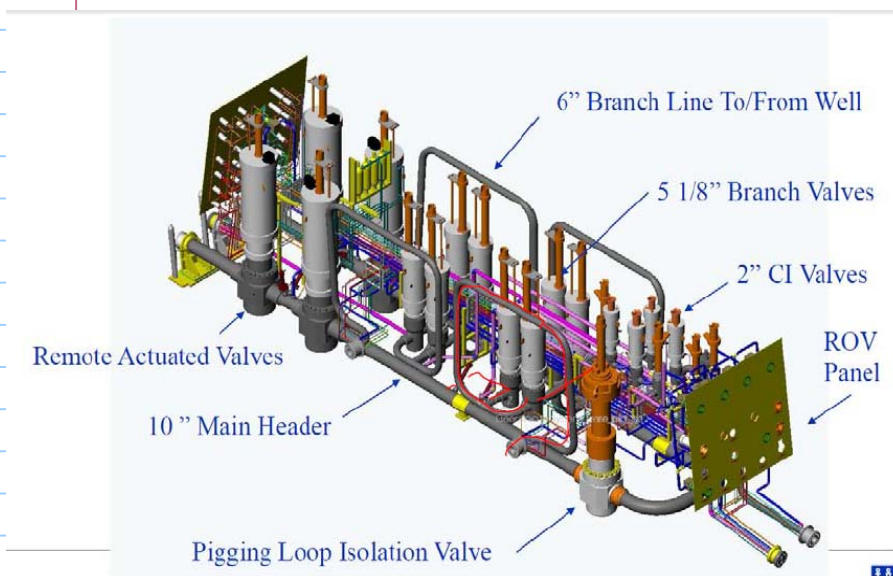
- to meter rates topside (test separator)
- to use 2 separators and smaller pipelines (operational flexibility)

- to perform pigging.

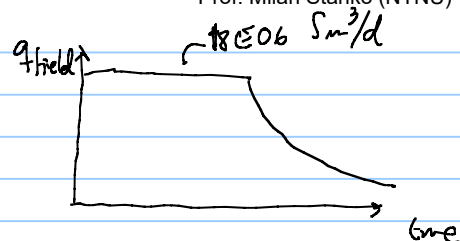
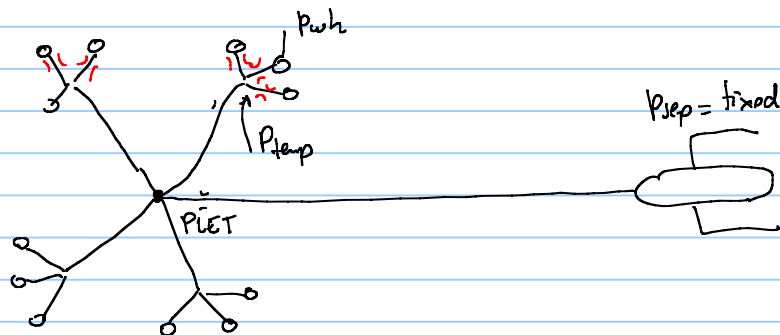
- inspection and monitoring pipe thickness
- evacuate liquid e.g. used hydrostatic pressure test
- remove wax accumulation



manifold module of 4 well subsea template



B2 problem (12 wells)



a long term gas contract
produced mode A

$$G = 311 \text{E}9 \text{ Sm}^3$$

set equilibrium point = choke

- All well are identical
- All template are identical
- All template are located symmetrical and same distance from PLET

2-5% of TRR produced annually

$$\text{TRR} = \frac{G \cdot R_{Fo}}{0.8} = \frac{311 \cdot 0.8 \cdot 1 \text{E}09}{0.8} = 248 \text{E}09$$

$$\text{calculate } q_w = \frac{q_{\text{field}}}{N_w}$$

$$q_{\text{plateau}} = \frac{\text{TRR} \cdot 0.02}{N_{\text{day in year}}} = \frac{248 \cdot 109.002}{365}$$

compute available pressure at Pwh

$P_R - P_{wf}$ IPR equation with q_w

$P_{wf} \rightarrow P_{wh}$ TPR equation with q_w

compute required pressure downstream the choke (P_{temp})

$P_{sep} \rightarrow P_{PLET} \rightarrow$ pipeline equation with q_{field}

$P_{PLET} \rightarrow P_{temp} \rightarrow$ flowline equation with $q_{temp} = \frac{q_{\text{field}}}{N_{temp}}$

• verify $P_{wh} > P_{temp}$?
 if yes production is possible by chosing
 if not production is not possible, rate must be reduced

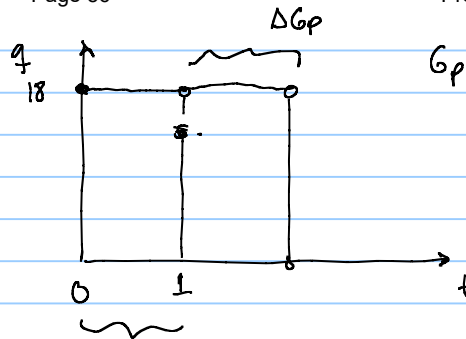
	IPR		TPR		FPR	PPR (pipeline performance relationship)	
time	P_R	P_{wf}	P_{wh}	P_{temp}	P_{PLET}	P_{sep}	
→ 0							
1							

time 0 years means first day of year 1

time 1 years means first day of year 2

$$P_R = P_{Ri} \frac{z_{Ri}}{z_{Rf}} \left(1 - \frac{G_p}{G} \right)$$

to calculate G_p for $t=1$ i assume production remained constant from $t=0 \rightarrow t=1$



$$G_{p2} = \Delta G_{p1} + \Delta G_{p2}$$

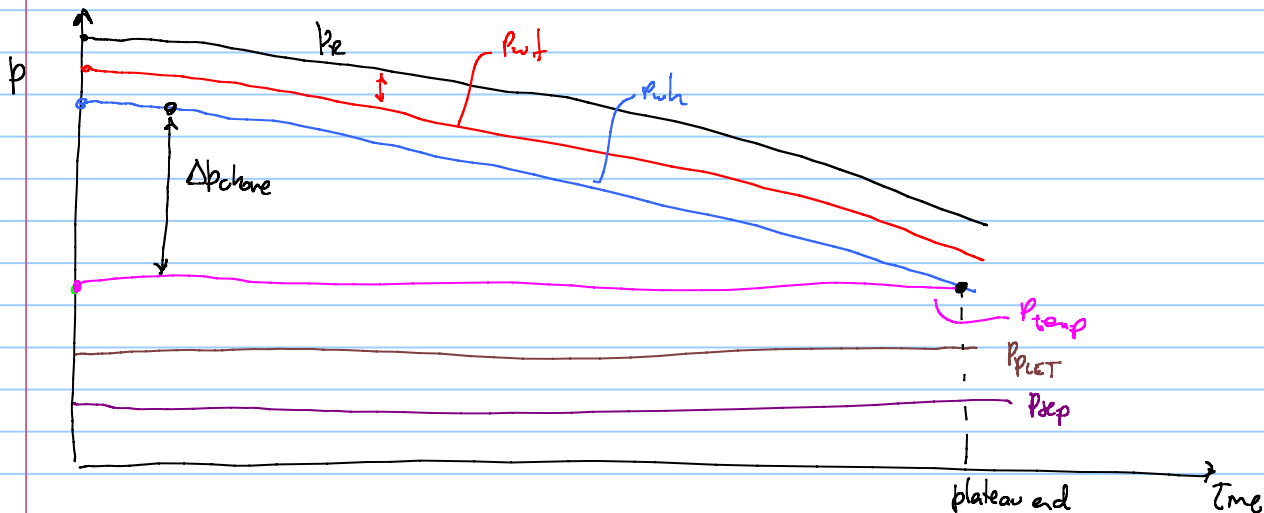
$$\Delta G_p = q_{\text{field}}(t=0) \cdot \Delta t \quad \text{Nday/year}$$

$$[\text{Sm}^3/\text{d}] \quad [\text{year}] \quad [\text{d/year}]$$

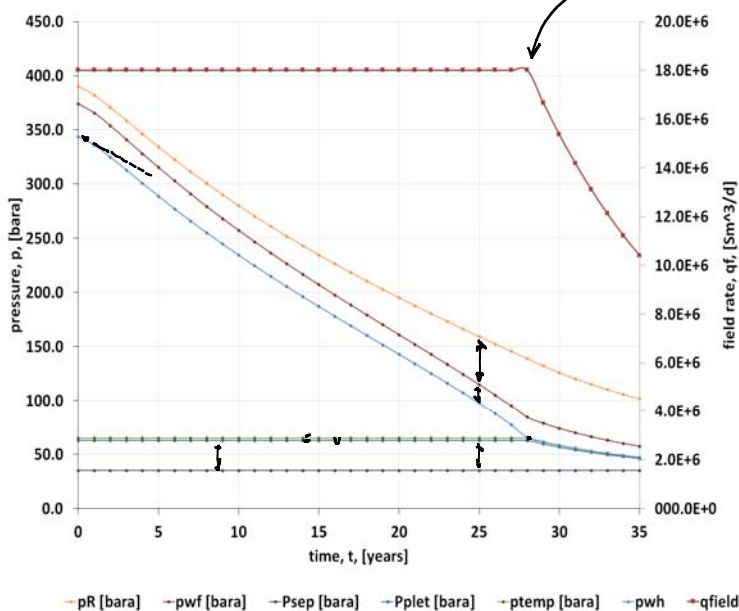
$$G_p = \sum_{i=0}^N \Delta G_p$$

usually the company
doesn't operate all
day in year

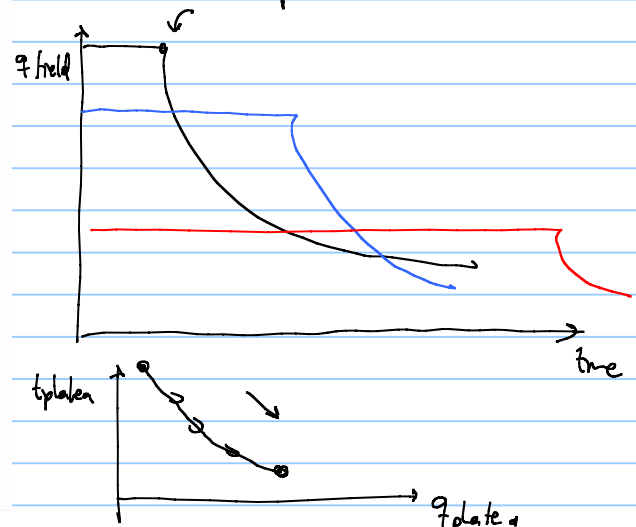
$$\text{uptime} = \text{N. producing days in a year} < 365$$



$t_{\text{plateau}} \sim 28 \text{ years}$



usually the higher the plateau rate,
the shorter the plateau



How to extend the plateau?

- make available pressure higher or make it decline "slower"

- $P_R \sim$ pressure support to reservoir injection?

- "enhance" IPR

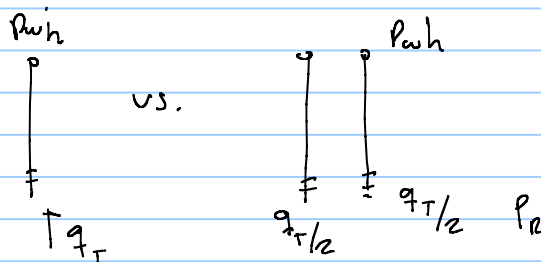


for oil water/gas
for gas not feasible

stimulation
fracturing
acidizing (cleaning pores)

- Increase tubing size . if oil reservoir { pumping in well artificial lift
gas lift

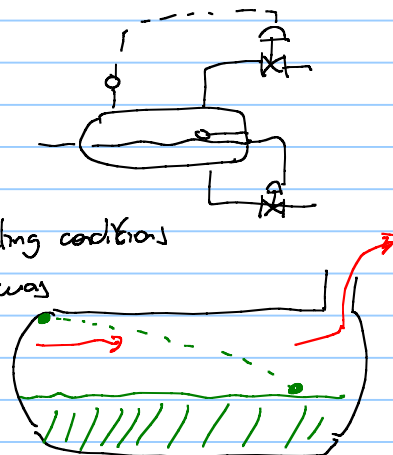
- Increase $N_w \rightarrow$ lower rate per well, lower pressure drop in formation and in tubing therefore higher P_{wh}



- making required pressure lower plateau?

- lower $P_{sep} \rightarrow$ change separator set

might not be desirable
because it changes operating conditions
for which equipment was
designed



if P_{sep} is reduced $v_g \uparrow$

high pressure low pressure

$$\dot{m}_g = \dot{m}_g$$

$$\rho_g q_g = \rho_g \cdot q_g$$

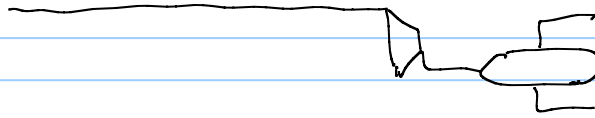
$\downarrow$
 P is high ρ is also high

$\downarrow$
 P is low, ρ_g is low

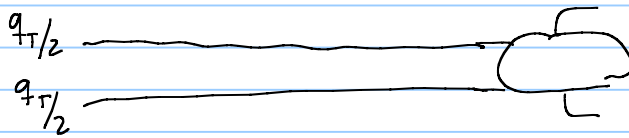
q_g for low pressure is higher
than q_g for high pressure

$$v_g = \frac{q_g}{A_{sep}}$$

- add a compressor before separator

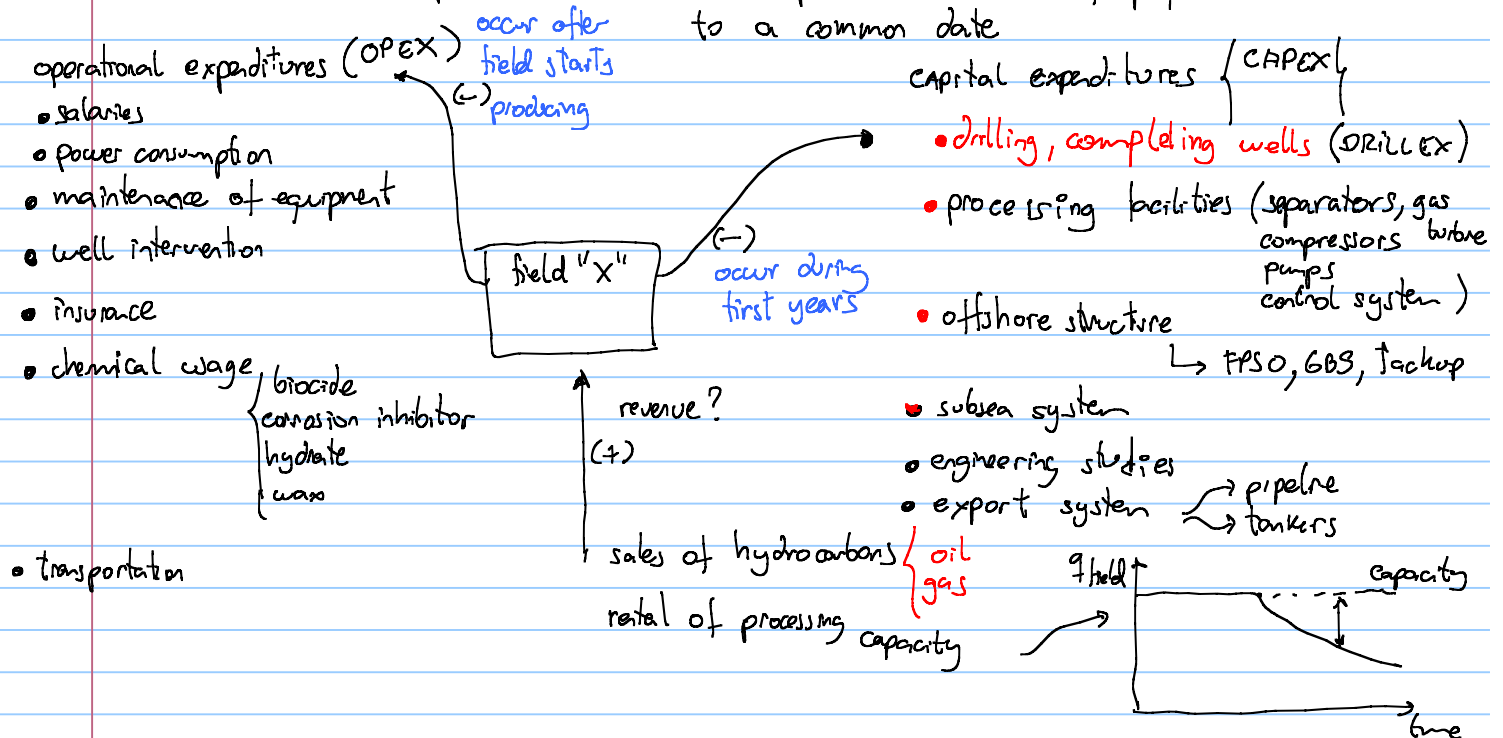


- increase pipeline diameter
- increase flowline diameter
- add another pipeline



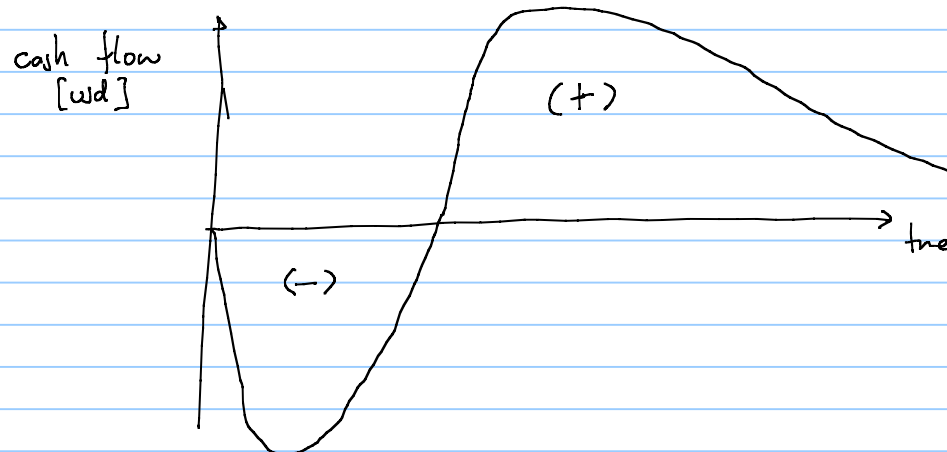
- homework repeat calculations for plateau rate of $25 \times 10^6 \text{ Sm}^3/\text{d}$

NPV calculations (Net present value): Sum expenses and revenue of project and refer all to a common date



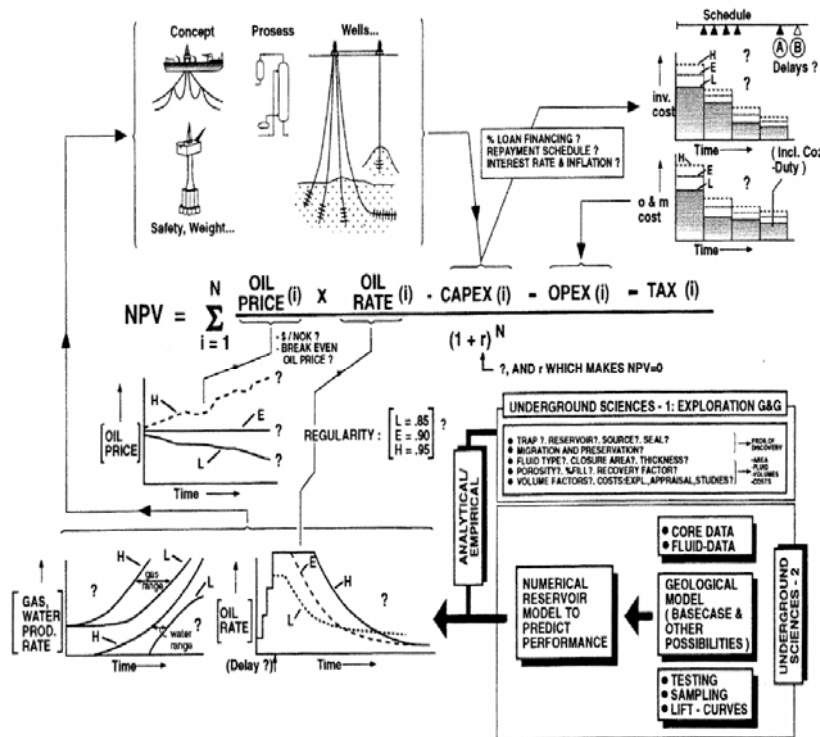
Cash flow calculation

time	CAPEX	DRILL EX	OPEX	Revenue [USD]	Cash flow
0	-	0	0	0	$\Sigma (+) (-)$
1	-	-	0	0	
2	-	-	0	0	
3	-	-	0	0	
4	-	-	0	0	
5	0	0	-	+	
	0	0	-	+	
	0	0	-	+	
	0	0	-	+	



Day 4 05.12.2019

NPV calculations
 Reserve estimation
 probability/decision trees



- Usually royalties and taxes must be considered in NPV calculations.
 fixed amount(%) of revenue (%) of net profit

- Other costs such as EXPEX (exploration expenditures)
 ABEX (Abandonment costs)

might be included in NPV calculations

will be covered more
 in detail in petroleum
 economics course
 (Trygve Strøm)

$$NPV = \sum_{i=1}^N \frac{\text{Revenue}(i) - \text{expenses}(i)}{(1+dc)^i} = \frac{P_o(i) \cdot \Delta N_p(i) + P_g(i) \cdot \Delta G_p(i) - \text{CAPEX}(i) - \text{OPEX}(i)}{(1+dc)^i}$$

year
 counter

dc discount factor $\sim$ (6% $\sim$ 12%)

$$\left(\frac{1}{1+dc}\right)^i$$

for year 1 : $\frac{1}{(1.06)^1} = 0.94$
 6%

for year 10 : $\frac{1}{(1.06)^{10}} = 0.56$
 6%

class exercise

CAPEX + DRILLEX + OPEX

discounted cash flow

time	ΔG_p	Revenue	CAPEX	DRILLEX	OPEX	Expenses	Cash flow	DCF
1	0	0	(-)	(-)	0	(-)	Revenue - Expenses	$\frac{CF}{(1+dc)^t}$
2	0	0	(-)	(-)	0	(-)		
3	0	0	(-)	(-)	0	(-)		
4	0	0	(-)	(-)	0	(-)		
5	0	0	(-)	(-)	0	(-)		
6	ΔG_{p6}	$\Delta G_p \cdot P_g$	0	0	(-)	(-)		
7	ΔG_{p7}	"	0	0	(-)	(-)		
8	"	"	0	0	(-)	(-)		
9	"	"	0	0	(-)	(-)		
10	"	"	0	0	(-)	(-)		
11	"	"	0	0	(-)	(-)		

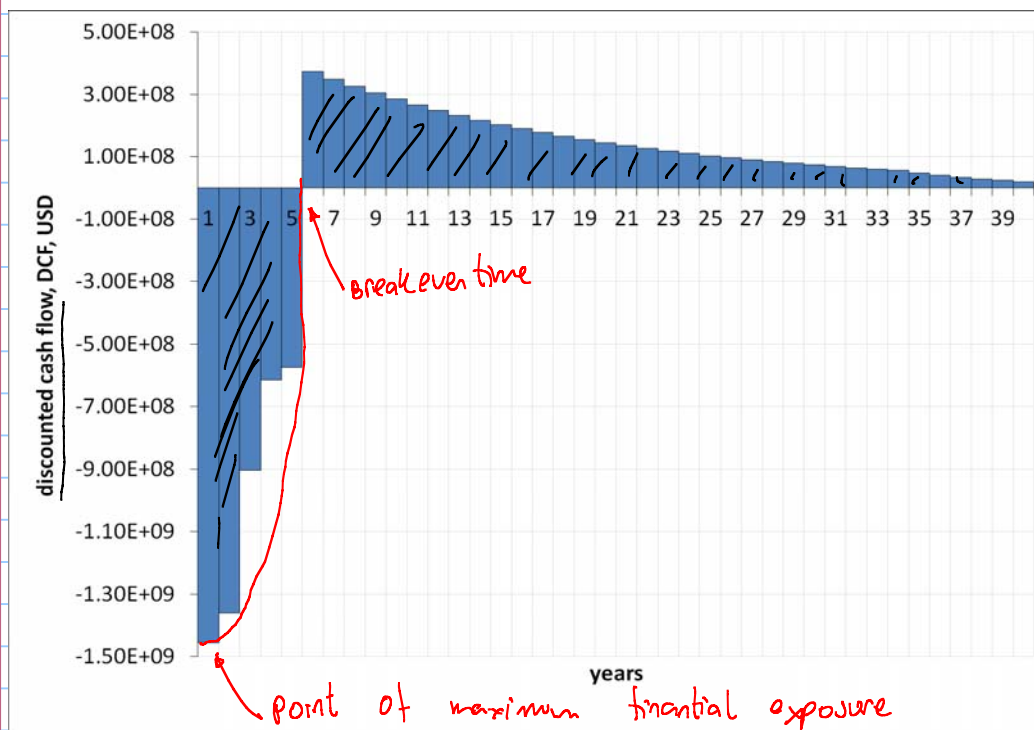
$\sum \frac{CF}{(1+dc)^t} = NPV$

B2 example

Well drilling cost	150	[1E6 USD]	Observations:
water depth	2500	[m]	Maximum 5 wells can be drilled per year
Discount rate	0.07	[-]	all CAPEX is invested evenly during the first 5 years
Uptime	360	days/year	
OPEX	1.20E+08	USD/year	
Gas price	0.11	[USD/Sm ³]	
CAPEX _{LING}	3.48E+09	USD	
CAPEX _{SUBSEA}	5.58E+08	USD	

Time	Gas production in year	Revenue	DRILLEX	CAPEX _{SUBSEA}	CAPEX _{LING}	OPEX	Total Cost	Cash Flow	Discounted Cash Flow: PV(i)
end of year	[Sm ³]	USD	USD	USD	USD	USD	USD	USD	USD
1	0	0.00E+00	7.50E+08	1.12E+08	6.95E+08	0	1.56E+09	-1.56E+09	-1.46E+09
2	0	0.00E+00	7.50E+08	1.12E+08	6.95E+08	0	1.56E+09	-1.56E+09	-1.36E+09
3	0	0.00E+00	3.00E+08	1.12E+08	6.95E+08	0	1.11E+09	-1.11E+09	-9.04E+08
4	0	0.00E+00	0.00E+00	1.12E+08	6.95E+08	0.00E+00	8.07E+08	-8.07E+08	-6.16E+08
5	0	0.00E+00	0.00E+00	1.12E+08	6.95E+08	0.00E+00	8.07E+08	-8.07E+08	-5.75E+08
6	6.5E+9	6.80E+08	0.00E+00	0.00E+00	0.00E+00	1.20E+08	1.20E+08	5.60E+08	3.73E+08
7	6.5E+9	6.80E+08	0.00E+00	0.00E+00	0.00E+00	1.20E+08	1.20E+08	5.60E+08	3.49E+08
8	6.5E+9	6.80E+08	0.00E+00	0.00E+00	0.00E+00	1.20E+08	1.20E+08	5.60E+08	3.26E+08
9	6.5E+9	6.80E+08	0.00E+00	0.00E+00	0.00E+00	1.20E+08	1.20E+08	5.60E+08	3.05E+08
10	6.5E+9	6.80E+08	0.00E+00	0.00E+00	0.00E+00	1.20E+08	1.20E+08	5.60E+08	2.85E+08
11	6.5E+9	6.80E+08	0.00E+00	0.00E+00	0.00E+00	1.20E+08	1.20E+08	5.60E+08	2.66E+08
12	6.5E+9	6.80E+08	0.00E+00	0.00E+00	0.00E+00	1.20E+08	1.20E+08	5.60E+08	2.49E+08
13	6.5E+9	6.80E+08	0.00E+00	0.00E+00	0.00E+00	1.20E+08	1.20E+08	5.60E+08	2.33E+08
14	6.5E+9	6.80E+08	0.00E+00	0.00E+00	0.00E+00	1.20E+08	1.20E+08	5.60E+08	2.17E+08
15	6.5E+9	6.80E+08	0.00E+00	0.00E+00	0.00E+00	1.20E+08	1.20E+08	5.60E+08	2.03E+08
16	6.5E+9	6.80E+08	0.00E+00	0.00E+00	0.00E+00	1.20E+08	1.20E+08	5.60E+08	1.90E+08
17	6.5E+9	6.80E+08	0.00E+00	0.00E+00	0.00E+00	1.20E+08	1.20E+08	5.60E+08	1.77E+08
18	6.5E+9	6.80E+08	0.00E+00	0.00E+00	0.00E+00	1.20E+08	1.20E+08	5.60E+08	1.66E+08
19	6.5E+9	6.80E+08	0.00E+00	0.00E+00	0.00E+00	1.20E+08	1.20E+08	5.60E+08	1.55E+08
20	6.5E+9	6.80E+08	0.00E+00	0.00E+00	0.00E+00	1.20E+08	1.20E+08	5.60E+08	1.45E+08
21	6.5E+9	6.80E+08	0.00E+00	0.00E+00	0.00E+00	1.20E+08	1.20E+08	5.60E+08	1.35E+08
22	6.5E+9	6.80E+08	0.00E+00	0.00E+00	0.00E+00	1.20E+08	1.20E+08	5.60E+08	1.26E+08
23	6.5E+9	6.80E+08	0.00E+00	0.00E+00	0.00E+00	1.20E+08	1.20E+08	5.60E+08	1.18E+08
24	6.5E+9	6.80E+08	0.00E+00	0.00E+00	0.00E+00	1.20E+08	1.20E+08	5.60E+08	1.10E+08
25	6.5E+9	6.80E+08	0.00E+00	0.00E+00	0.00E+00	1.20E+08	1.20E+08	5.60E+08	1.03E+08
26	6.5E+9	6.80E+08	0.00E+00	0.00E+00	0.00E+00	1.20E+08	1.20E+08	5.60E+08	9.65E+07
27	6.5E+9	6.80E+08	0.00E+00	0.00E+00	0.00E+00	1.20E+08	1.20E+08	5.60E+08	9.02E+07
28	6.5E+9	6.80E+08	0.00E+00	0.00E+00	0.00E+00	1.20E+08	1.20E+08	5.60E+08	8.43E+07
29	6.5E+9	6.80E+08	0.00E+00	0.00E+00	0.00E+00	1.20E+08	1.20E+08	5.60E+08	7.88E+07
30	6.5E+9	6.80E+08	0.00E+00	0.00E+00	0.00E+00	1.20E+08	1.20E+08	5.60E+08	7.36E+07
31	6.5E+9	6.80E+08	0.00E+00	0.00E+00	0.00E+00	1.20E+08	1.20E+08	5.60E+08	6.88E+07
32	6.5E+9	6.80E+08	0.00E+00	0.00E+00	0.00E+00	1.20E+08	1.20E+08	5.60E+08	6.43E+07
33	6.5E+9	6.80E+08	0.00E+00	0.00E+00	0.00E+00	1.20E+08	1.20E+08	5.60E+08	6.01E+07
34	6.5E+9	6.80E+08	0.00E+00	0.00E+00	0.00E+00	1.20E+08	1.20E+08	5.60E+08	5.62E+07
35	6.0E+9	6.30E+08	0.00E+00	0.00E+00	0.00E+00	1.20E+08	1.20E+08	5.10E+08	4.78E+07
36	5.5E+9	5.81E+08	0.00E+00	0.00E+00	0.00E+00	1.20E+08	1.20E+08	4.61E+08	4.03E+07
37	5.1E+9	5.36E+08	0.00E+00	0.00E+00	0.00E+00	1.20E+08	1.20E+08	4.16E+08	3.40E+07
38	4.7E+9	4.95E+08	0.00E+00	0.00E+00	0.00E+00	1.20E+08	1.20E+08	3.75E+08	2.87E+07
39	4.4E+9	4.58E+08	0.00E+00	0.00E+00	0.00E+00	1.20E+08	1.20E+08	3.38E+08	2.42E+07
40	4.0E+9	4.24E+08	0.00E+00	0.00E+00	0.00E+00	1.20E+08	1.20E+08	3.04E+08	2.03E+07
							NPV		1.92E+08

① Homework: repeat NPV calculation for $q_{plateau} = 25 \text{ EOG Sm}^3/\text{d}$



Revenue and Cost Profiles

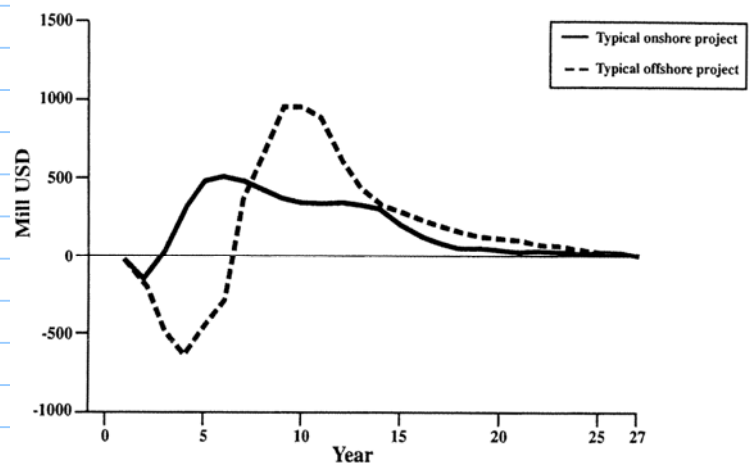
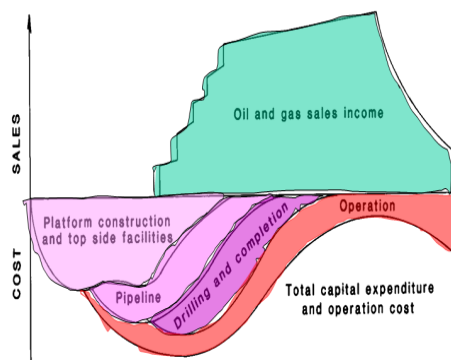


Fig. 9. Typical before tax cash flow profiles for offshore and onshore projects.

we should always evaluate the effect of uncertainty

Sensitivity analysis

P_g, P_o
 Cost figures
 production rates

→ change one variable at the time while keeping all others fixed

for gas price $P_g \rightarrow 1.2 P_g (+20)\%$

$\rightarrow 0.8 P_g (-20)\%$

for our problem, evaluate the effect of uncertainty :

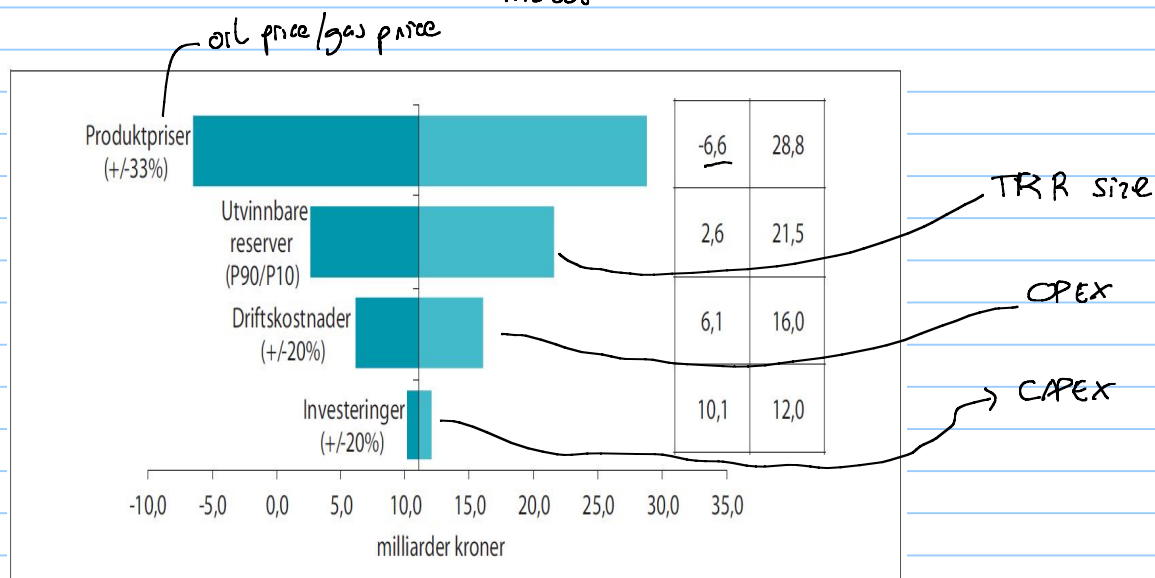
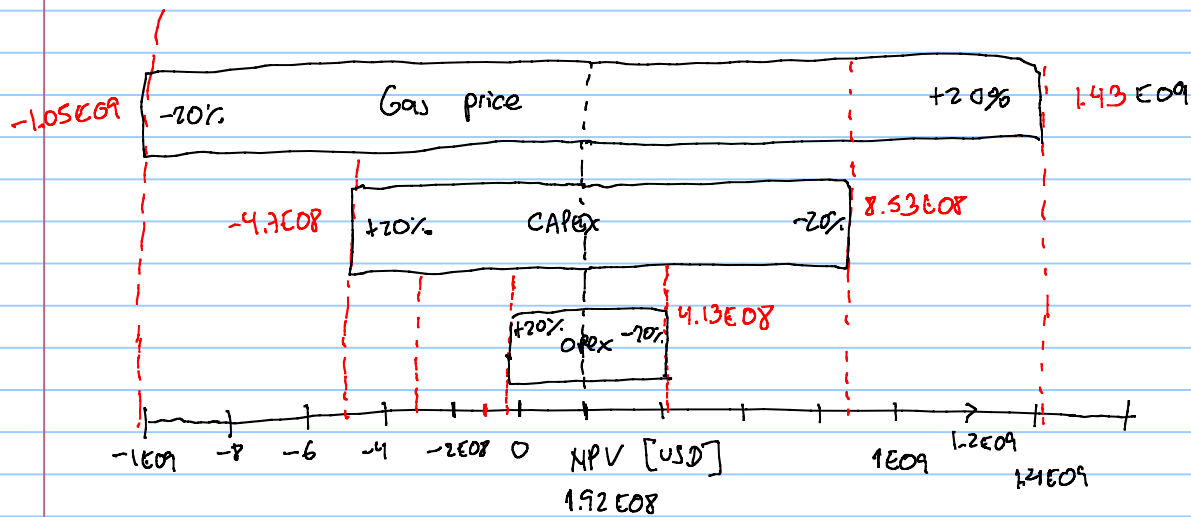
$\pm 20\%$ gas price
 $\pm 20\%$ Capex values
 $\pm 20\%$ OPEX

1) • change $P_g \rightarrow P_g \cdot 1.2 \rightarrow$ Compute NPV $\rightarrow$ return to P_g

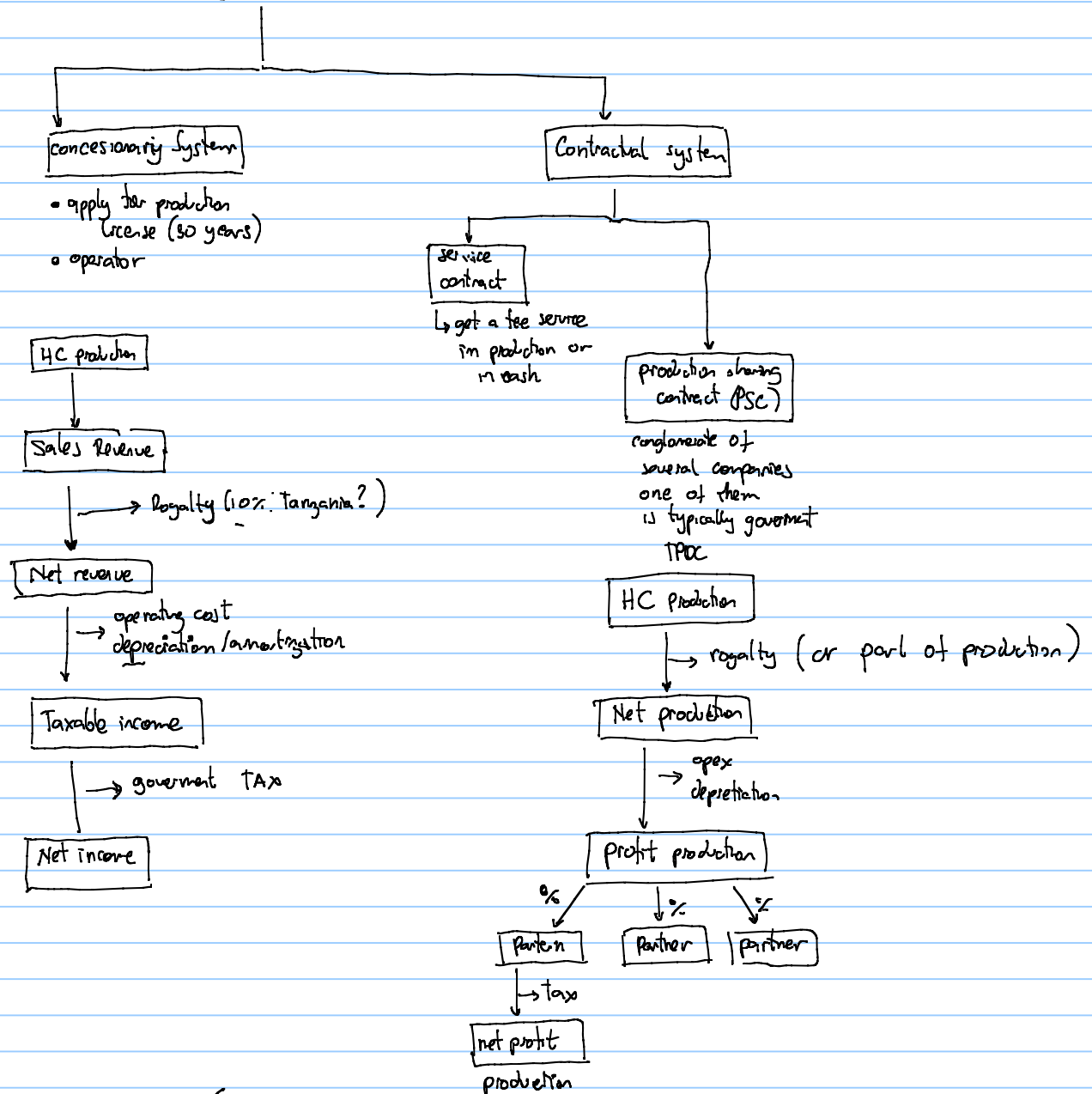
2) • change $P_g \rightarrow P_g \cdot 0.8 \rightarrow$ Compute NPV $\rightarrow$ return to P_g

Variable	NPV		
	-20%	BASE CASE	+20%
gas price	-1.05E9	1.92E8	1.43E09
CAPEX	8.53E08	1.92E8	-4.7E8
OPEX	4.13E08	1.92E8	-3E07

tornado chart



Petroleum fiscal systems

Reserve estimation (060, 061, 062)

→ estimating $N, G \rightarrow N_{pu}, G_{pu}$

$$N_{pu} = N \cdot F_{ru}$$

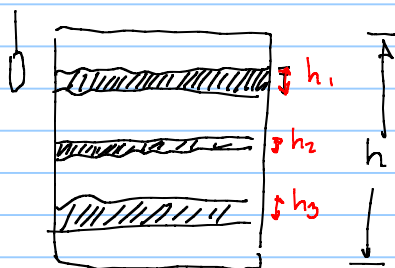
$$G_{pu} = G \cdot F_{ru}$$

ultimate recovery factor

$$N = \frac{\overbrace{V_R} \cdot \overbrace{\phi} \cdot \overbrace{S_o} \cdot \overbrace{N_{Tc}}}{\underbrace{B_o}}$$



N_{TG} --- Net to gross



reservoir rock layers which are not "clean" not "hydrocarbon-bearing" rock

$$N_{TG} = \frac{\sum h_i}{h} = \frac{h_1 + h_2 + h_3}{h}$$

is a multiplier to the total rock volume, to account for the presence of non productive layers.

$$N_{pu} = N_{FGU} = \frac{V_R \cdot \Phi \cdot S_o \cdot N_{TG} \cdot F_{RU}}{B_o}$$

The input to this equation is not a single number!

$\Phi \rightarrow$

$V_R \rightarrow$

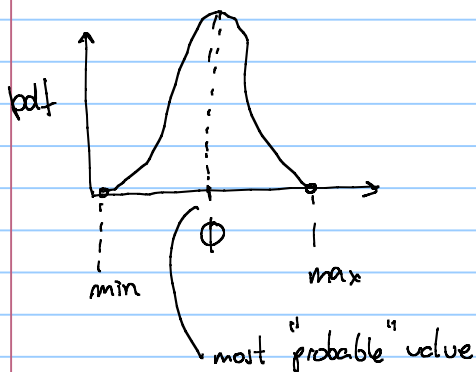
$S_o \rightarrow$

$B_o \rightarrow$

$N_{TG} \rightarrow$

$F_{RU} \rightarrow$

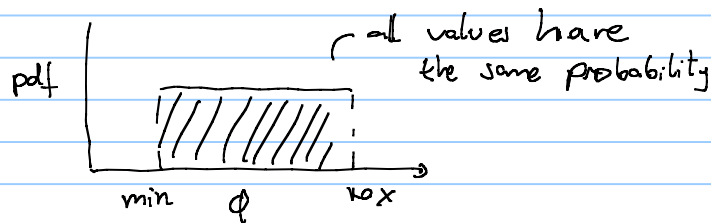
we are also interested in computing N_{pu} as a range, with associated probabilities



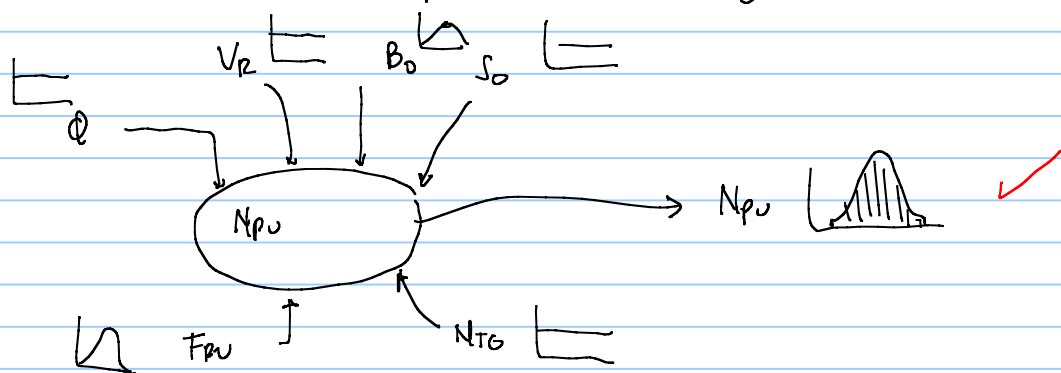
pdf probability density function

pdf probability distribution function

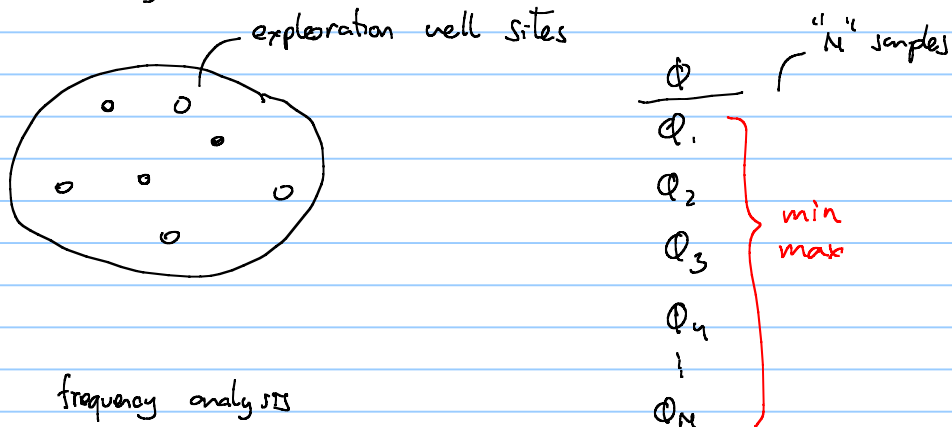
if i have no prior information



what i am interested in computing is the resulting distribution for N_{pu}



estimating probability distribution using measured data



frequency analysis

Φ $\leftarrow$ "N" samples

$\left. \begin{array}{l} Q_1 \\ Q_2 \\ Q_3 \\ Q_4 \\ \vdots \\ Q_N \end{array} \right\} \begin{array}{l} \text{min} \\ \text{max} \end{array}$

min
max

make

- define certain number of bins n
 n should be much less than N (number of samples)
- determine minimum and maximum values of sample

n should be much less than N (number of samples)

- determine minimum and maximum values of sample

 Φ_{mir}

$$\Delta\phi_z = \frac{\phi_{max} - \phi_{min}}{n-1}$$

$$Q_{max}$$

- generate bins

bins

Qmiz

$$\phi_1 = \phi_{min} + \Delta\phi$$

$$\Phi_2 = \Phi_1 + \Delta\Phi$$

1001

$$\Phi_{max} = \Phi_{i-1} + \Delta\Phi$$

Qmiz

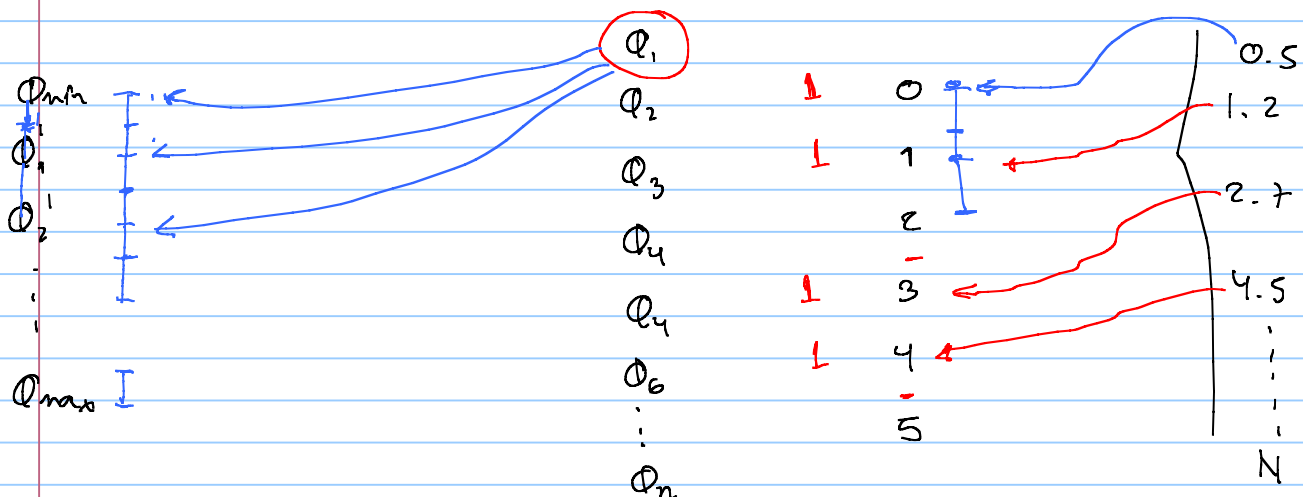
$$\Delta\phi = \frac{\phi_{\max} - \phi_{\min}}{2}$$

$Q_1 -$

$$Q_{max}$$

$$\phi_i = \phi_{min} + \frac{(\phi_{max} - \phi_{min})}{2} =$$

- look at each value in sample and assign it to a bin

 Q_2

Q₃

 Φ_4

Q_c

 O_6

1

 Φ_n 

1

2

3

4

5

Q.5

1. 2

2.7

4 -

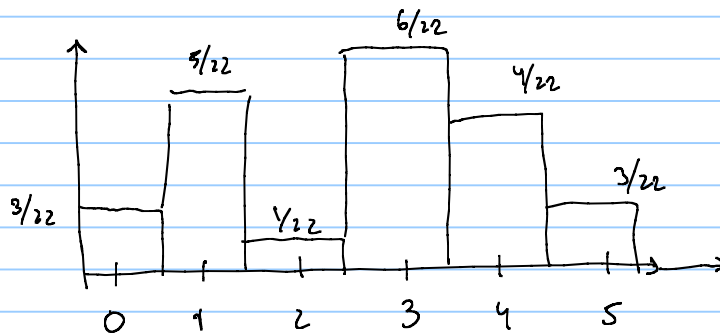
1

- count the number of samples assigned to each bin and probability

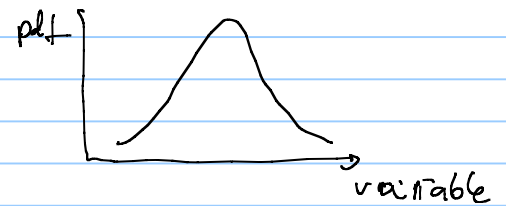
$n = 6$

bin	Count	frequency
0	3	$3/22$
1	5	$5/22$
2	1	$1/22$
3	6	$6/22$
4	4	$4/22$
5	3	$3/22$

$N = 22$

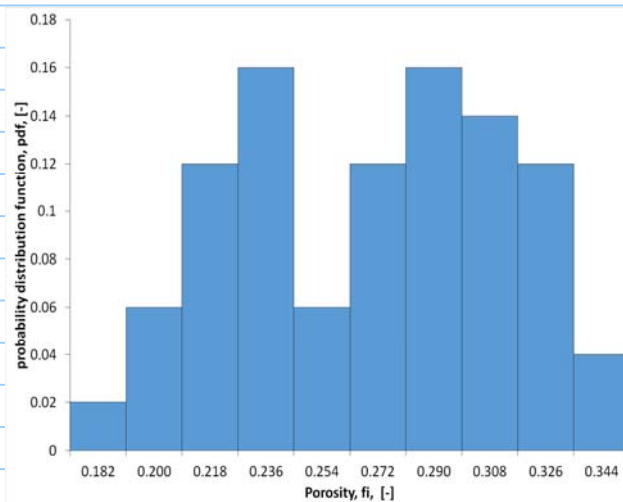


discrete probability distribution

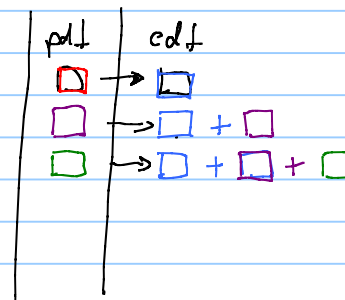


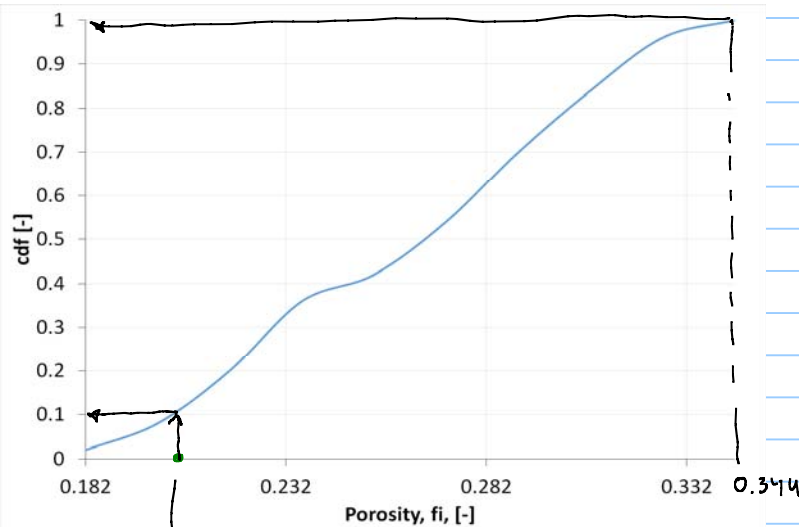
continuous probability distribution

(class) exercise → generate discrete frequency distribution for measured porosity data



cumulative distribution function (cdf)



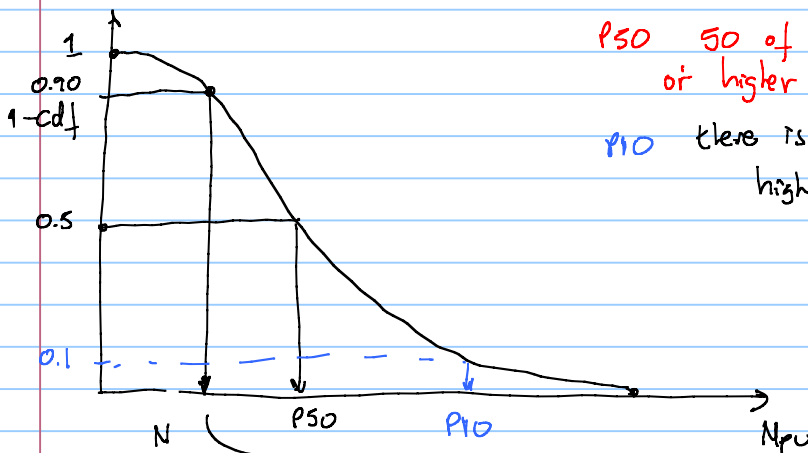


100% of the population has
 $\Phi = 0.344$ or less

$\Phi = 0.2 \rightarrow cdf = 10\%$

there is 10% probability that the porosity of my population is equal to $\Phi = 0.2$ or less

in reserves



P50 50% of the population will have NPV $\geq$ P50 or higher

P10 there is 10% chance that NPV will be P10 or higher

each company uses their own percentiles

90 $\rightarrow$ 80

50 $\rightarrow$ 66

10 $\rightarrow$ 15, 5

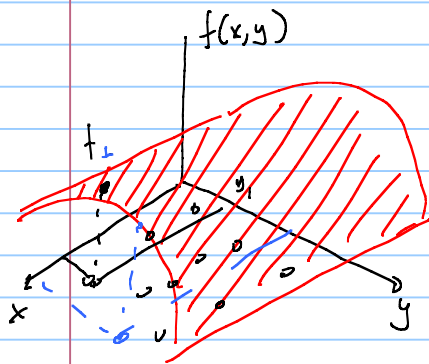
P90 90% of the total population will have NPV of P90 or bigger

P10 P50 P90 P00 Hebron

Hebron Ben Nevis Oil	Upside Volumes		Best Estimate Volumes		Downside Volumes	
	MBO	Mm ³	MBO	Mm ³	MBO	Mm ³
D-94 Fault Block	1601	255	1328	211	1077	171
I-13 Fault Block	252	40	187	30	141	22
Total Hebron Ben Nevis	1870	297	1515	241	1204	191
Total Hebron Ben Nevis Gas	Upside Volumes		Best Estimate Volumes		Downside Volumes	
	GCF	* GSm ³	GCF	GSm ³	GCF	GSm ³
Solution Gas D-94 Block	112	3.2	145	4.1	189	5.4
Solution Gas I-13 Block	10	0.3	14	0.4	22	0.6
Non-associated Gas	n/a	n/a	n/a	n/a	n/a	n/a
Gas Cap D-94 Block only	0	0	0	0	31	0.9

* GSm³ = 10⁹ cubic meters

to compute the pdf and cdf of N_{pu} , we will use sampling method called Monte-Carlo



$$f(x,y) = x^2 + y^2 \quad \text{random sampling}$$

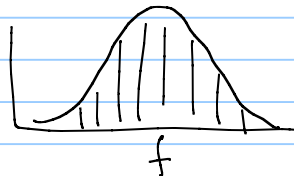
$$x_1, y_1 \rightarrow f_1$$

$$x_2, y_2 \rightarrow f_2$$

repeat for many random samples

$$(f_1, f_2, \dots, f_N)$$

apply a frequency analysis to the results



JOURNAL OF THE AMERICAN STATISTICAL ASSOCIATION

Number 247

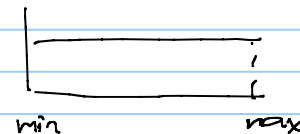
SEPTEMBER 1949

Volume 44

THE MONTE CARLO METHOD

NICHOLAS METROPOLIS AND S. ULAM
Los Alamos Laboratory

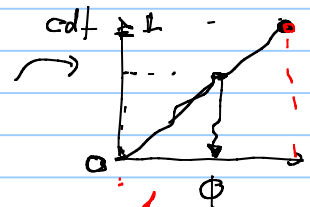
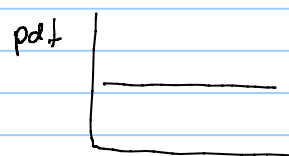
1) • Assign pdf for all input data

$$\left. \begin{array}{l} \Phi \\ V_R \\ B_0 \\ I_0 \\ N_{TG} \\ F_{RW} \end{array} \right\}$$


2) • take a random sample for each variable in each range.

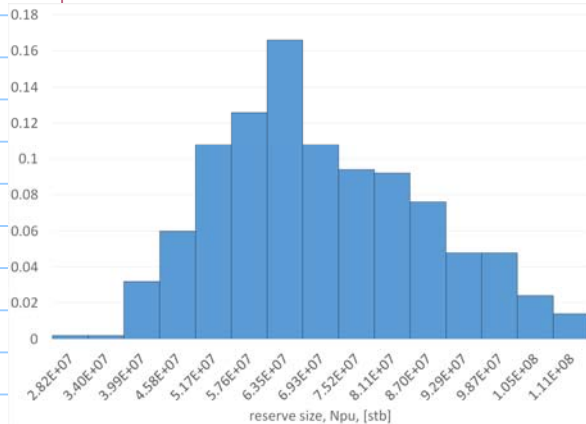
$$\text{cdf} = \frac{(X - X_{\min})}{(X_{\max} - X_{\min})}$$

$$X = \text{RAND}(0-1) [X_{\max} - X_{\min}] + X_{\min}$$

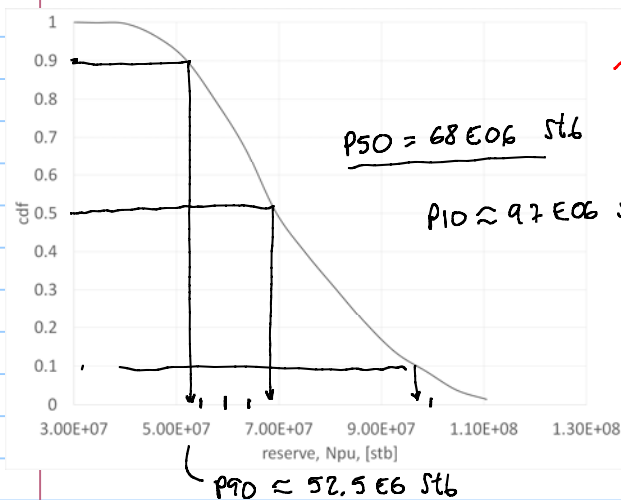


- 3) • compute N_{pu} with all random input.
- 4) • record N_{pu} value
- 5) • repeat from step 2, "Many" times (500)

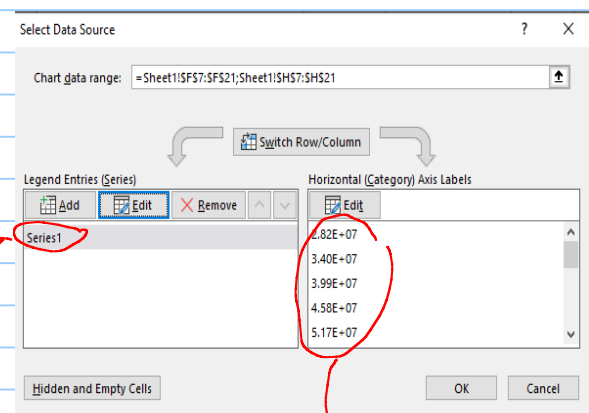
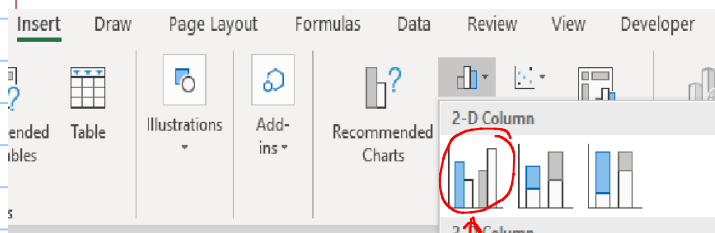
Class exercise



		Net to Gros		Oil Saturation	Formation Volume F		Ultimate Recovery Factor
	Rock volume	Porosity	N/G	So={1-Sw}	Bo	Fr	
	bbl	fraction	fraction	fraction	Res bbl/STB	fraction	
Min	2.00E+09	0.18	0.3	0.8	1.35	0.42	
Max	2.50E+09	0.3	0.5	0.9	1.6	0.65	
MC it	Rock volume	Porosity	N/G	So={1-Sw}	Bo	Fr	Npu
[-]	bbl	fraction	fraction	fraction	Res bbl/STB	fraction	[stb]
1	2.16E+09	1.94E-01	4.97E-01	8.25E-01	1.39E+00	6.10E-01	7.51E+07
2	2.28E+09	2.51E-01	4.17E-01	8.06E-01	1.46E+00	5.76E-01	7.59E+07
3	2.44E+09	2.77E-01	4.31E-01	8.23E-01	1.52E+00	5.77E-01	9.12E+07



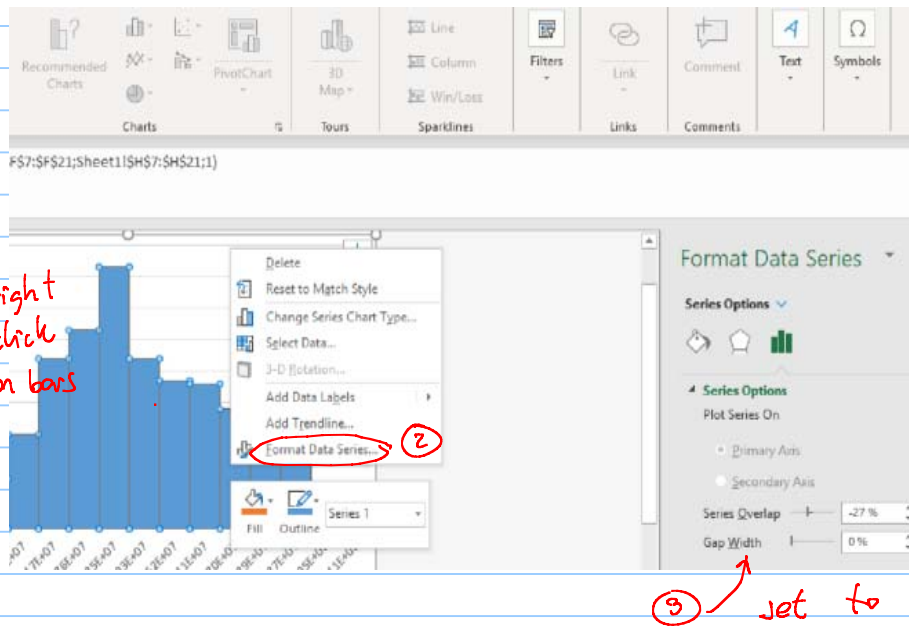
nr	bin	count	pdf	cdf
1	2.82E+07	1	0.002	1
2	3.40E+07	1	0.002	0.998
3	3.99E+07	16	0.032	0.996
4	4.58E+07	30	0.06	0.964
5	5.17E+07	54	0.108	0.904
6	5.76E+07	63	0.126	0.796
7	6.35E+07	83	0.166	0.67
8	6.93E+07	54	0.108	0.504
9	7.52E+07	47	0.094	0.396
10	8.11E+07	46	0.092	0.302
11	8.70E+07	38	0.076	0.21
12	9.29E+07	24	0.048	0.134
13	9.87E+07	24	0.048	0.086
14	1.05E+08	12	0.024	0.038
15	1.11E+08	7	0.014	0.014



② Homework make plots of pdf/cdf
Npu

pdf

set bins



tool useful $\rightarrow$: An easier way to quantify the effect of uncertainty instead of faster way using monte Carlo

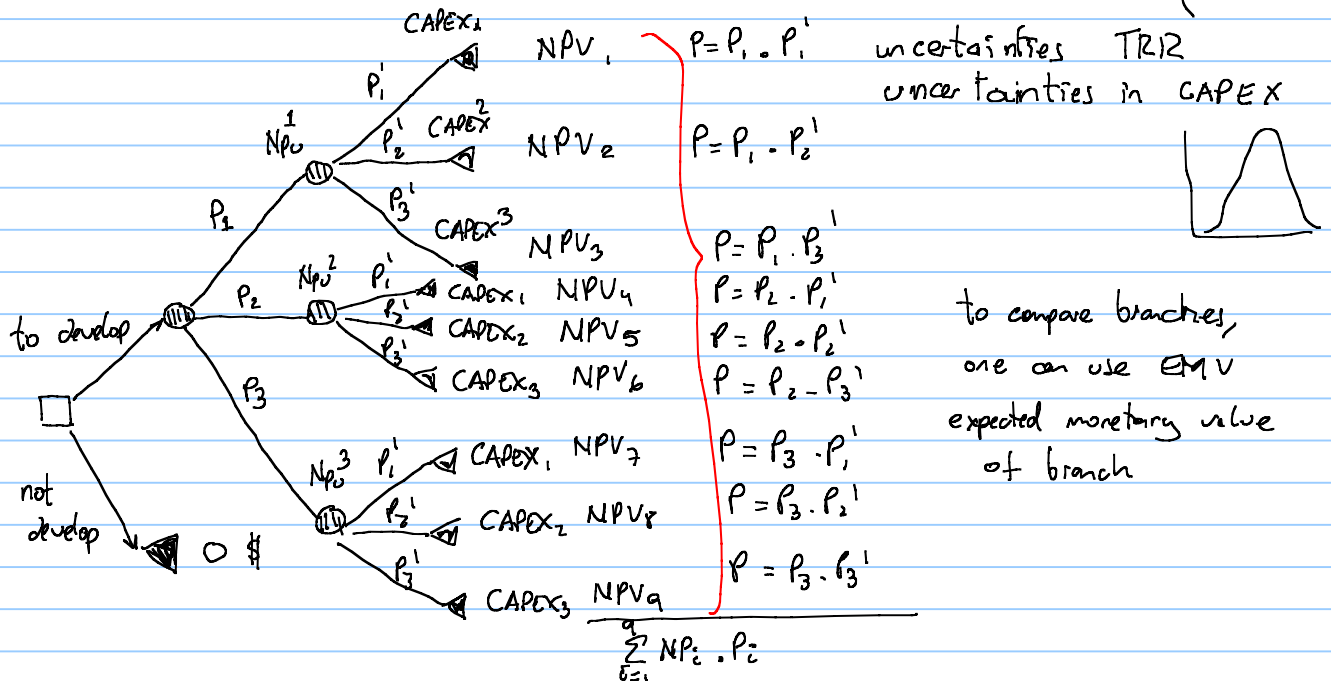
: to provide support when taking decision

Probability trees / decision trees

□ choice node
decision node

⊗ chance

◀ end node



class exercise

08_decision_Tree
08_Decision_tree_exercise

xlsx

docx

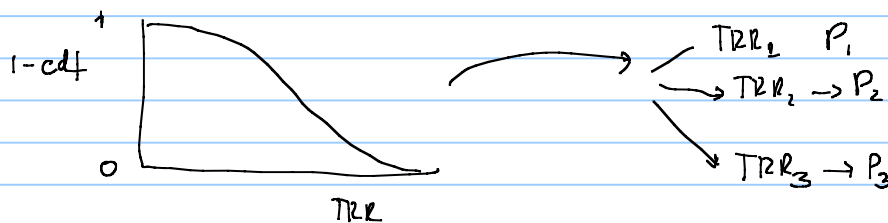
Your company is deciding whether to develop a reservoir or not in the Rovuma region. To help them take the decision, you have proposed to use a probability tree.

The value of the development can be estimated using the simplified equation:

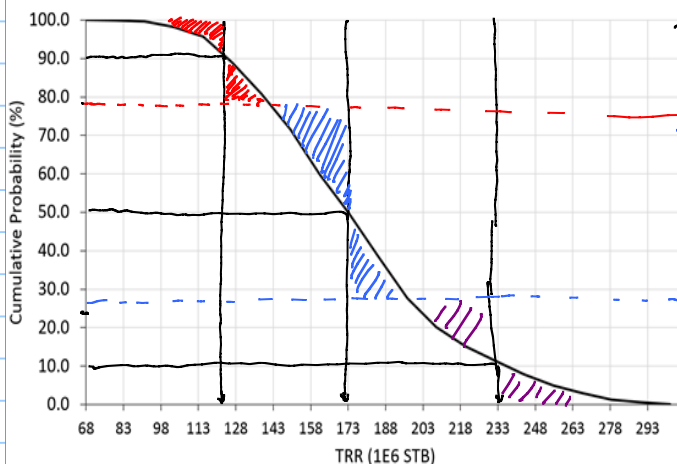
$$NPV = TRR \cdot 60 \cdot 0.4 - CAPEX.$$

- What is the mean expected value of the development? Is it worth to look further into developing this field?
- The capex values exhibit a normal probability distribution. However, it has already been discretized by a colleague:
 - CAPEX1: 0.7 E9 USD, P1: 0.3
 - CAPEX2: 1.1 E9 USD, P2: 0.4
 - CAPEX3: 1.5 E9, P3: 0.3.

how to discretize TRR



Expectation Curve for Total Recoverable Oil Reserves



$$P_{90} = 122 \text{ EOB stb}$$

$$P_{50} = 173 \text{ EOB stb}$$

$$P_{10} = 233 \text{ EOB stb}$$

} P1

} P2

move the line until two red areas are same

from chart $P_1 = 0.2$

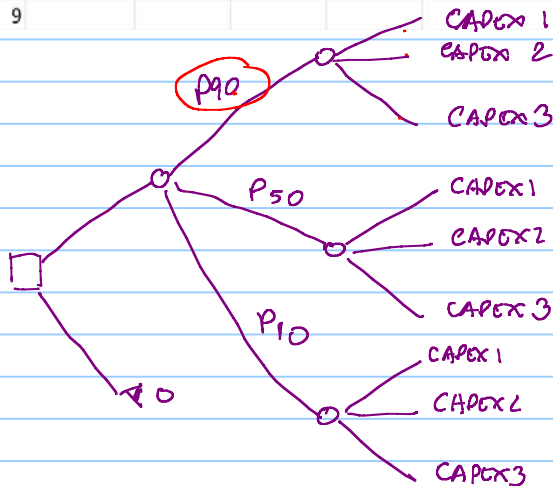
$$P_2 = 0.55$$

$$P_3 = 1 - 0.2 - 0.55 = 0.25$$

$$P_1 + P_2 + P_3 = 1$$

let's make the tree in excel

OPTION	TRR	P_TRR	CAPEX	P_capex	MV = TRR*60*0.4-CAPEX	P=P_capex*P_TRR	MV*P
[-]	[stb]	[-]	[USD]	[-]	[USD]	[-]	[USD]
1	P90	0.2	CAPEX1	0.3	NPV1	0.2 * 0.3	0.06
2	P90	0.2	CAPEX2	0.4	NPV2	0.2 * 0.4	0.08
3	P90	0.2	CAPEX3	0.3	NPV3	0.2 * 0.3	0.06
4							
5							
6							
7							
8							
9							



$$EMV = \sum ()$$

OPTION	TRR	P_TRR	CAPEX	P_capex	NPV = TRR*60*0.4-CAPEX	P=P_capex*P_TRR	MV*P
[-]	[stb]	[-]	[USD]	[-]	[USD]	[-]	[USD]
1	1.22E+08	0.2	7.00E+08	0.3	2.23E+09	0.06	1.34E+08
2	1.22E+08	0.2	1.10E+09	0.4	1.83E+09	0.08	1.46E+08
3	1.22E+08	0.2	1.50E+09	0.3	1.43E+09	0.06	8.57E+07
4	1.73E+08	0.55	7.00E+08	0.3	3.45E+09	0.165	5.70E+08
5	1.73E+08	0.55	1.10E+09	0.4	3.05E+09	0.22	6.71E+08
6	1.73E+08	0.55	1.50E+09	0.3	2.65E+09	0.165	4.38E+08
7	2.33E+08	0.25	7.00E+08	0.3	4.89E+09	0.075	3.67E+08
8	2.33E+08	0.25	1.10E+09	0.4	4.49E+09	0.1	4.49E+08
9	2.33E+08	0.25	1.50E+09	0.3	4.09E+09	0.075	3.07E+08
					EMV		3.17E+09

it is worth to develop the field !

③ Homework : do this exercise by yourselves

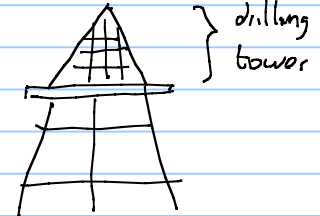
Day 5 06.12.2019

• offshore structures for oil and gas production. what component does the structure must have?

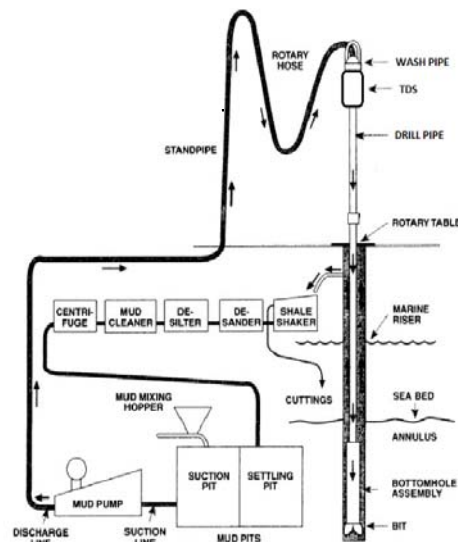
- Facilities for drilling and full intervention. This includes drilling tower, BOP, drilling floor, mud package, cementing pumps, storage deck for drill pipes and tubulars, drilling risers.
- Facilities for light well intervention.
- Processing facilities: separator trains for primary oil, gas and water separation, gas processing train, water processing train.
- Gas injection system
- Gas compression units for pipeline transport
- Water injection system
- Living quarters
- Helideck.
- Power generation.
- Flare system.
- Utilities (hydraulic power fluid, compressed air, drinking water unit, air condition system, ventilation and heating system)
- Bay for wellheads and christmas trees
- Production manifolds
- Oil storage
- Facilities for oil offloading
- Control system
- Monitoring system
- System for storage, injection and recovery of production chemicals (wax, scale, hydrate or corrosion inhibitors)
- Repair workshop

same of components I need

→ drilling package (\$)



→ gas turbine (20-30 MW)

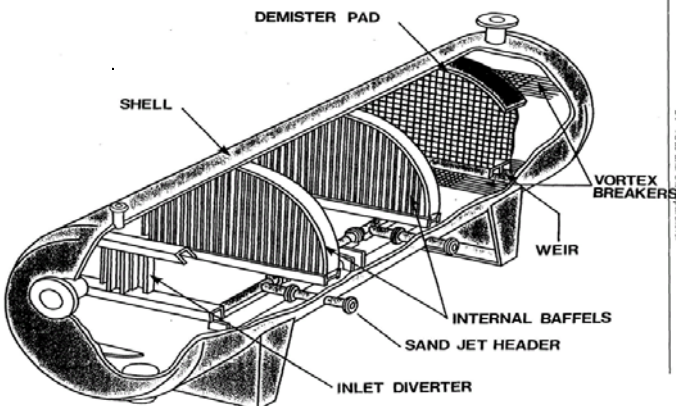
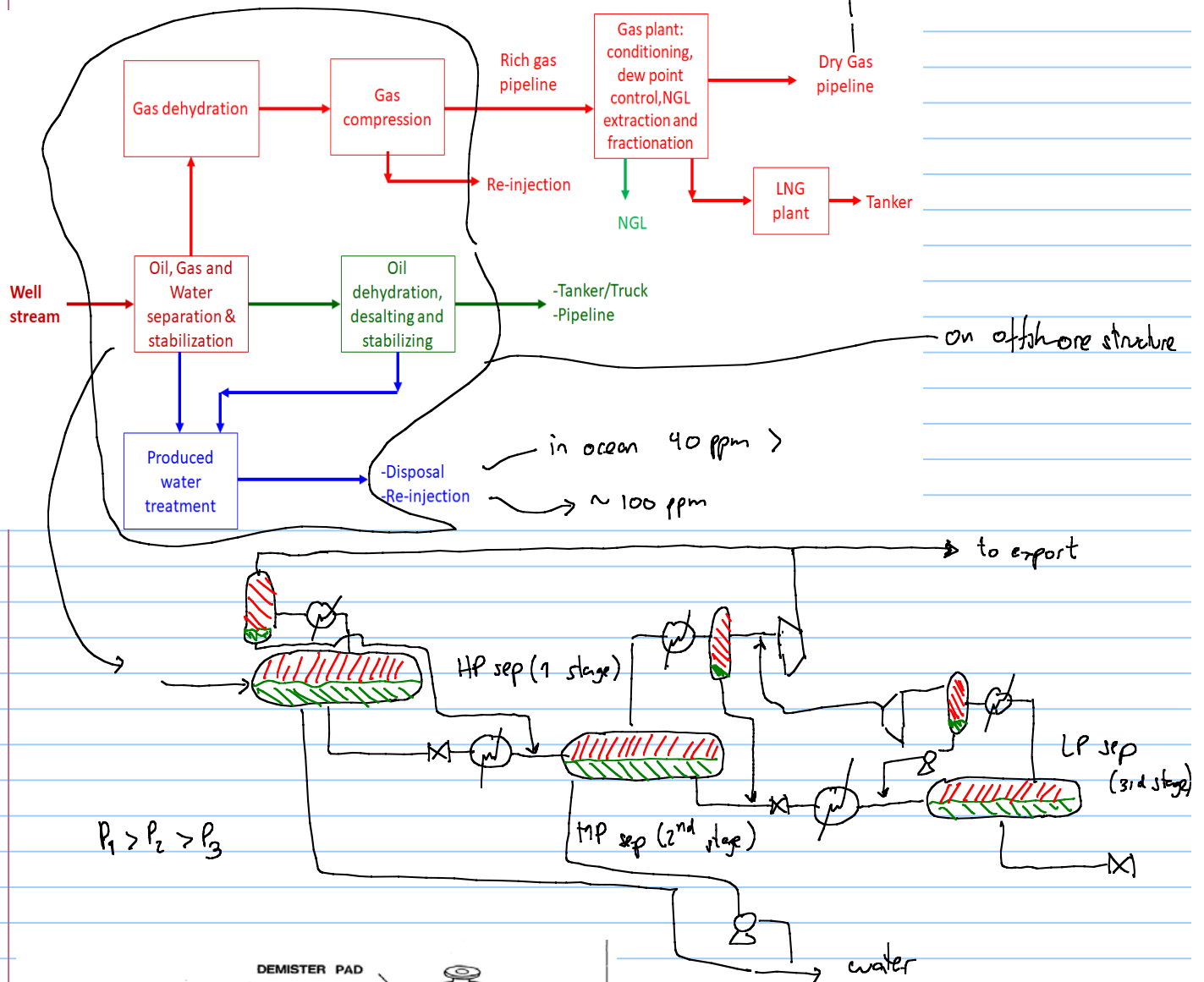
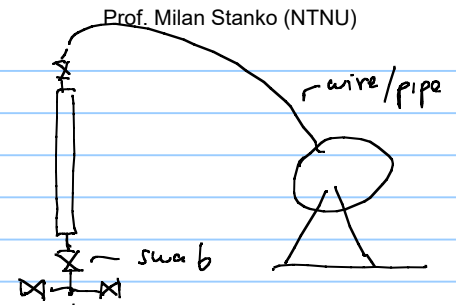


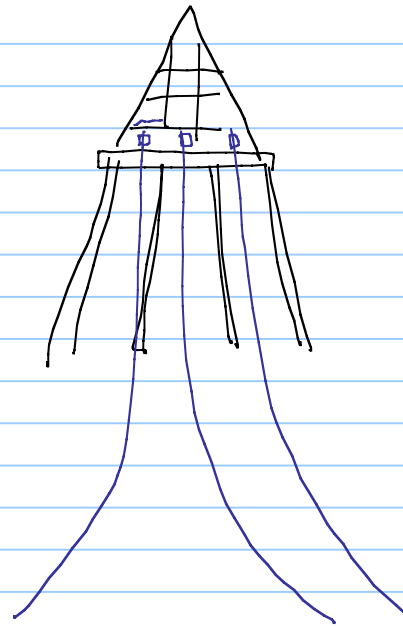
mud package



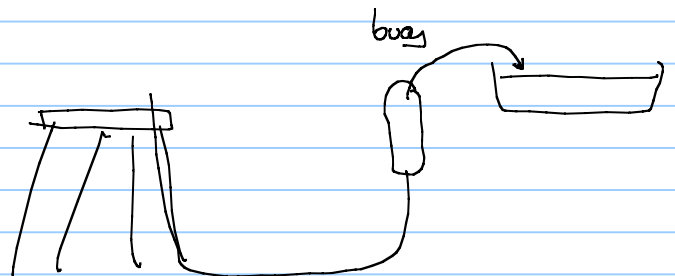
→ drilling pipe } storage
tubing
casing

"light" well intervention: $\rightarrow$ wireline / slickline
 $\rightarrow$ coiled tubing

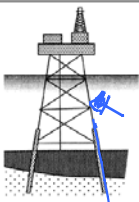
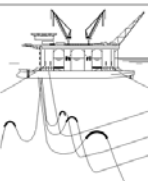


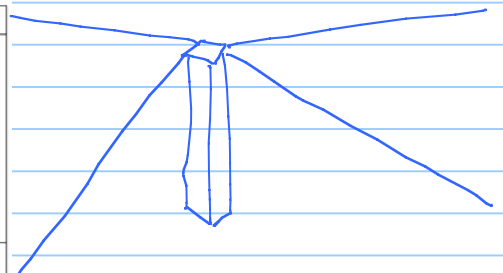


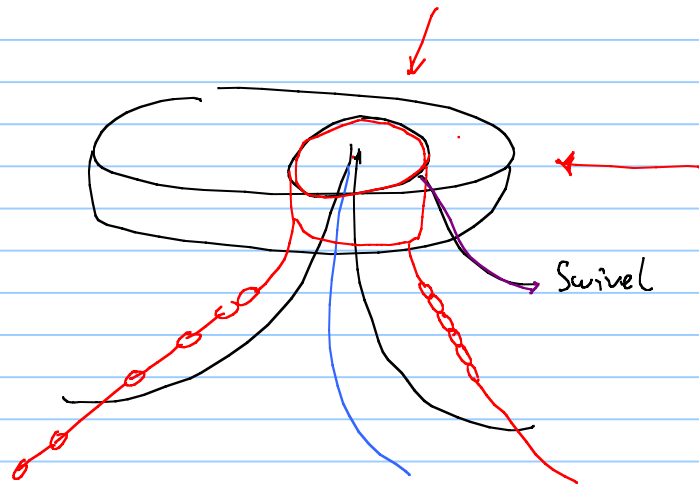
oil offloading



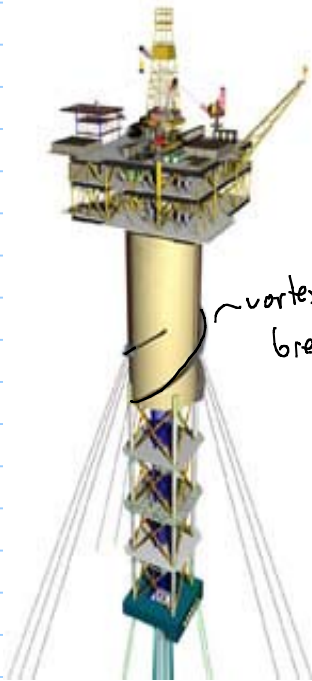
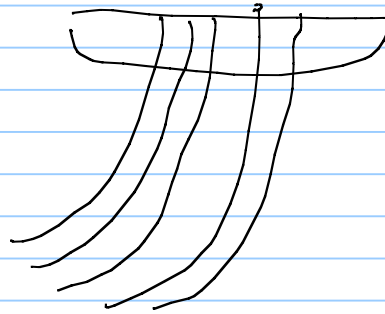
type of offshore structures

Bottom-supported	Fixed		Compliant	
				
	Jacket	Gravity-Based Structure	Compliant tower	
Floating	Neutrally <u>bouyant</u>			Positively <u>bouyant</u>
				
	Ship FPSO	Semi-Sub	Sevan FPSO	Spar
				Tension Leg Platform (TLP)

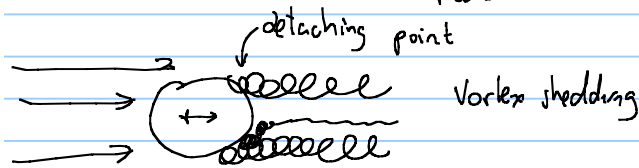
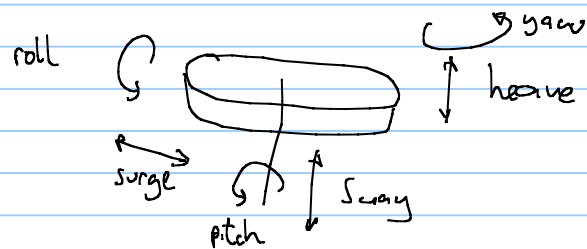




if weather conditions are not harsh and are not changing, we don't need swivel

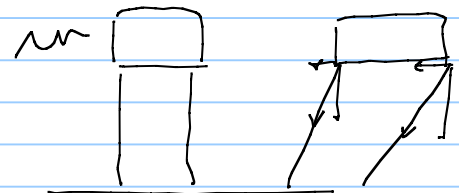
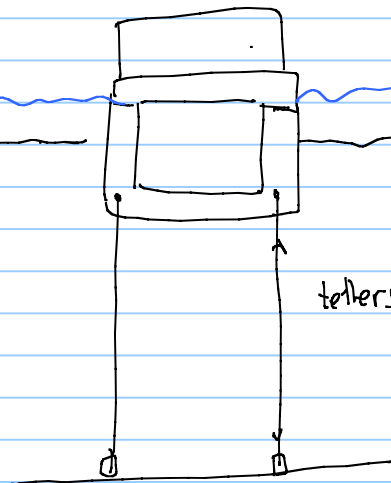


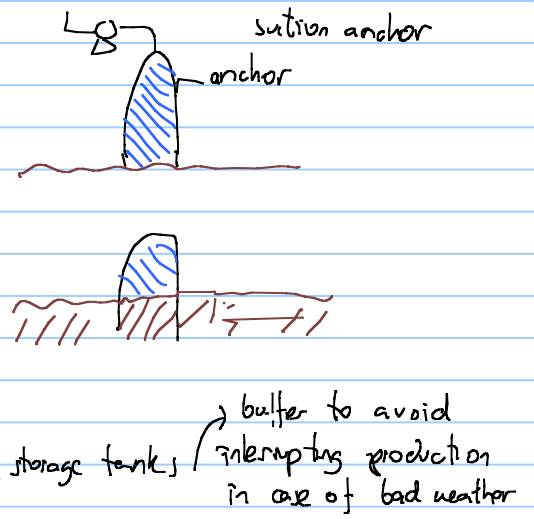
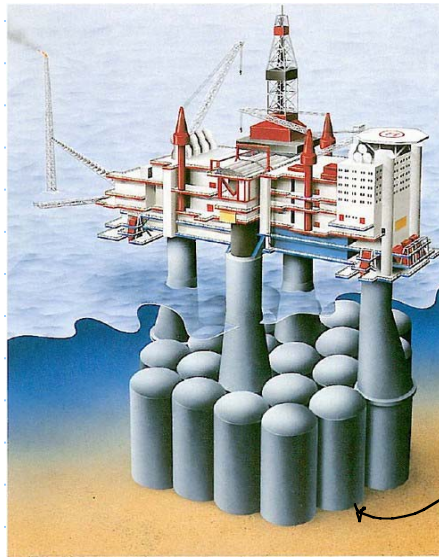
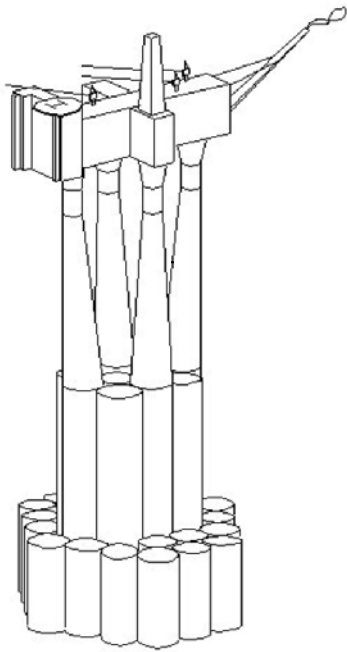
the big draft hinders movement



Tension leg platform

limit movement





storage tanks → buffer to avoid interrupting production in case of bad weather

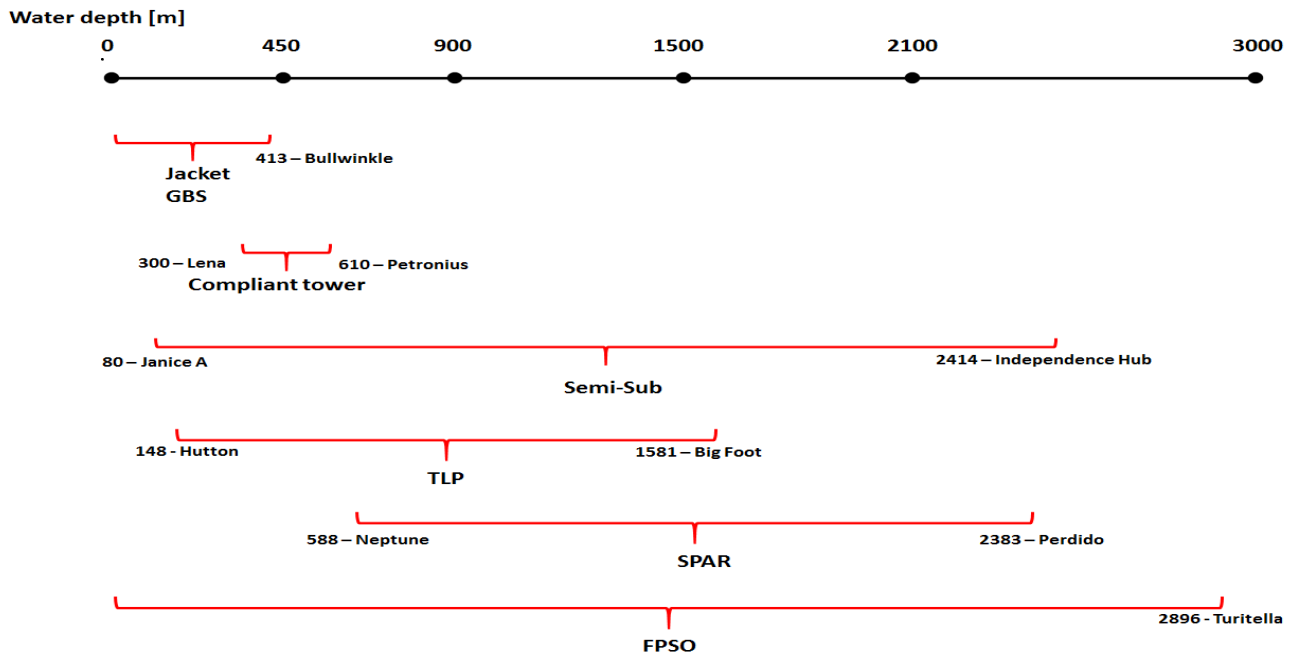


Semi submersible

How do we select offshore structures? 1) water depth

bottom supported structures are used for water depths below 600 m

floating structures are used for any water depth but typically for > 600 m

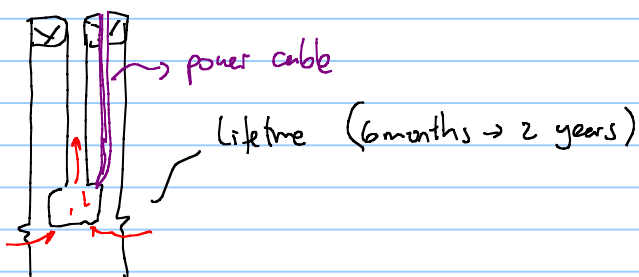
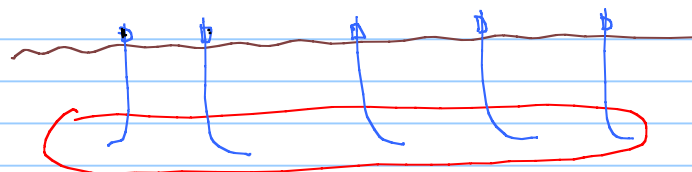
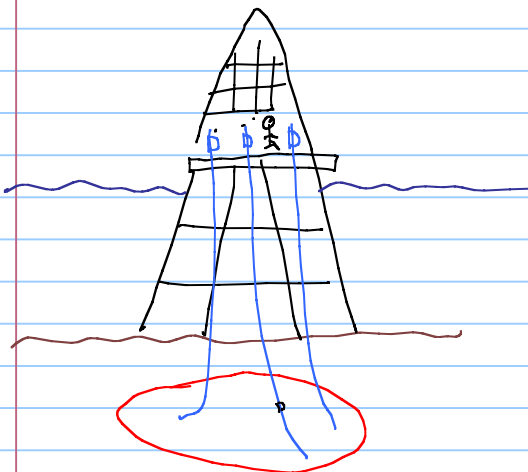


2) location of X-mas tree → dry (platform)
→ wet (subsea)

↳ spread of reservoir

Can I reach all reservoir targets from same location?

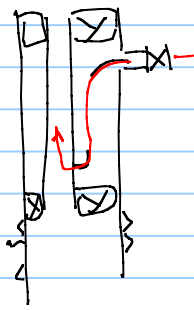
reservoir structure and spread



↳ water depth. Dry wells have a limit up to 1500 m

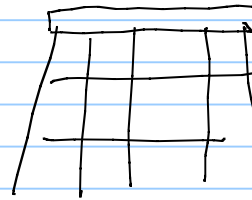
↳ well intervention needs:

if Artificial Lift (electric submersible pumps or gas lift, then I prefer to have dry wells



gas lift. by injecting gas, p_{max} is reduced, Δp is also reduced.

↳ infill drilling (to prolong plateau, high uncertainty in subsurface)



to have spare slots on platform will be very expensive. therefore it is preferred to use subsea wells.

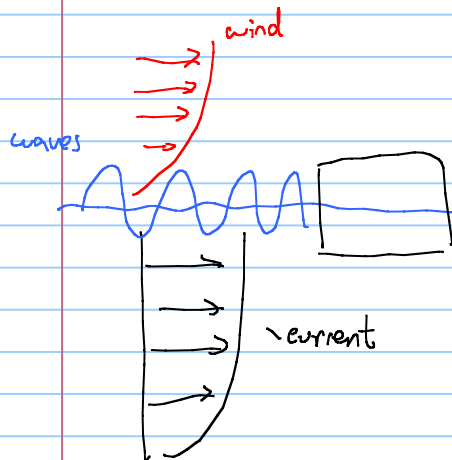
there are only a few structures that allow dry X-mas → Jacket, GBS, compliant tower, TLP, (semi-sub), SPAR

- oil storage {
 - harsh weather conditions
 - social / political uncertainty
 that might interrupt regular tanker schedule

GBS → 300.000 ~ 500.000 stb

SPAR → 150.000 stb

FPSO → 1.000.000 - 3.000.000 stb

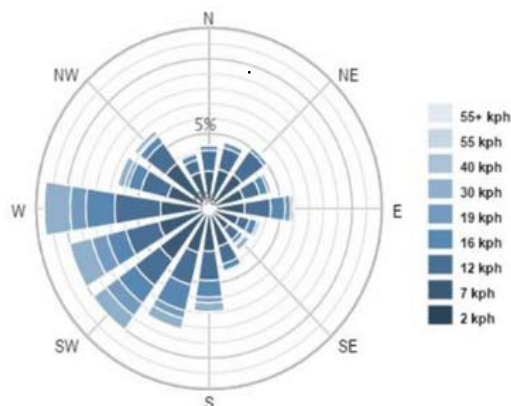


- loads caused by
 - wind
 - waves
 - currents

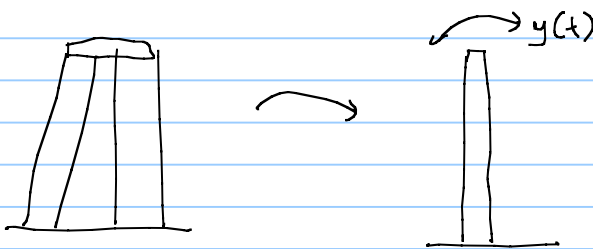
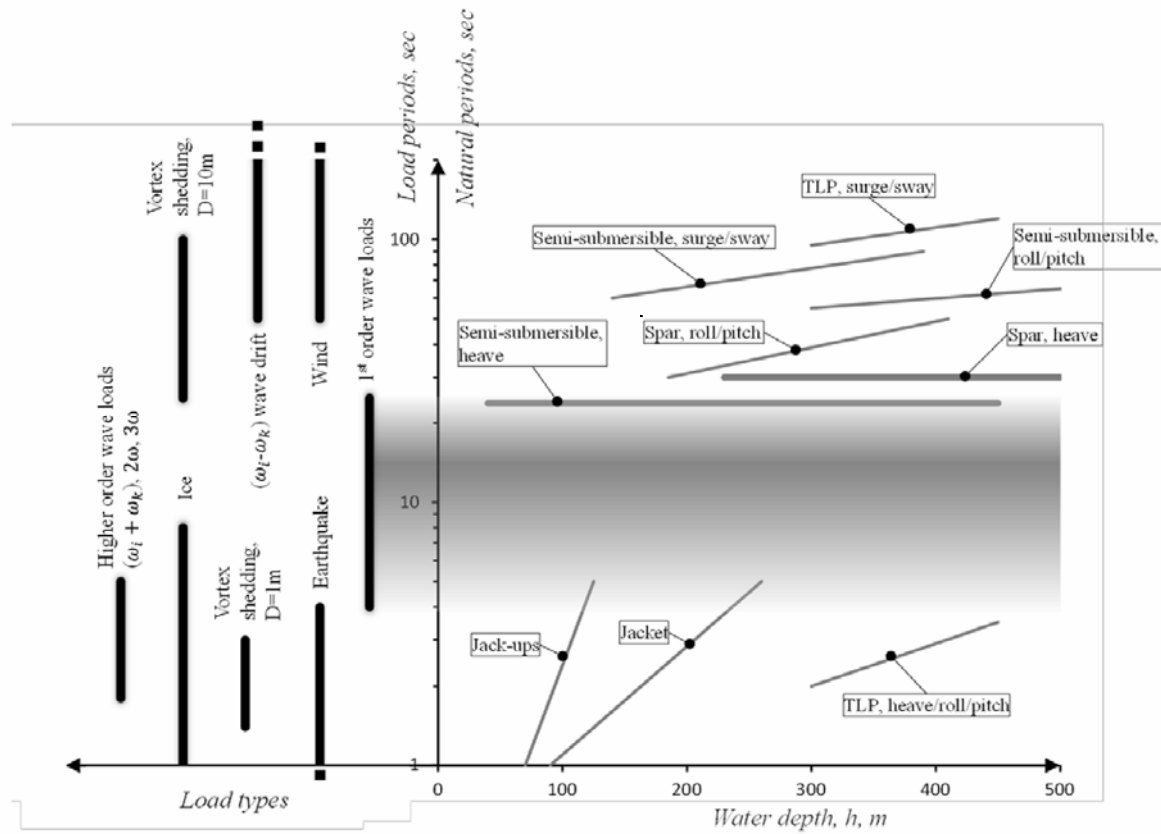
each offshore location has some characteristic

wave	magnitude
wind	direction
current	frequency/period

heave (t)
 surge (t)
 sway (t)
 roll (t)
 pitch (t)
 yaw (t)



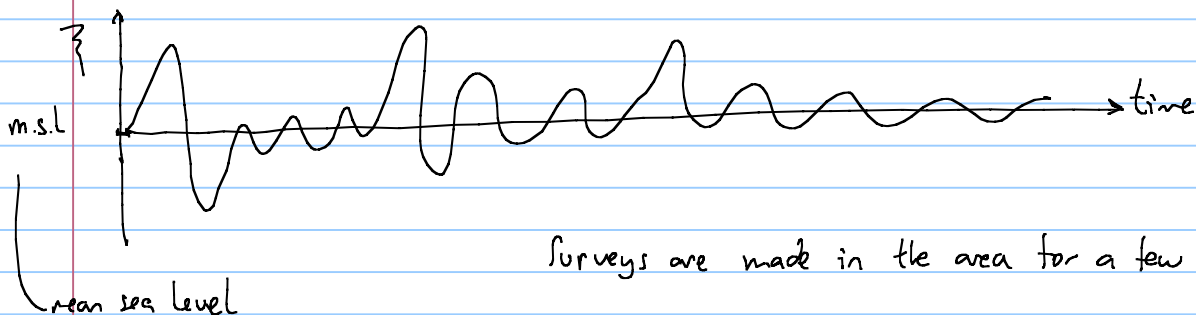
each structure has a natural frequency which give maximum movement, therefore I have to avoid using structures which their natural frequency coincides with excitation frequency



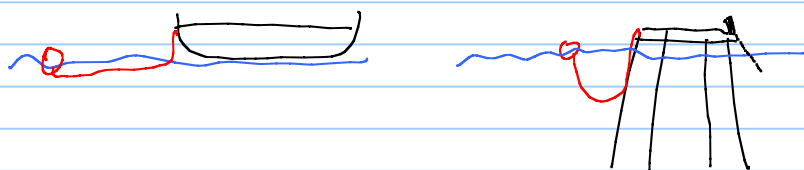
How do we characterize the conditions of wave, wind, current of an offshore location?

Waves

usually considered fixed in magnitude and direction

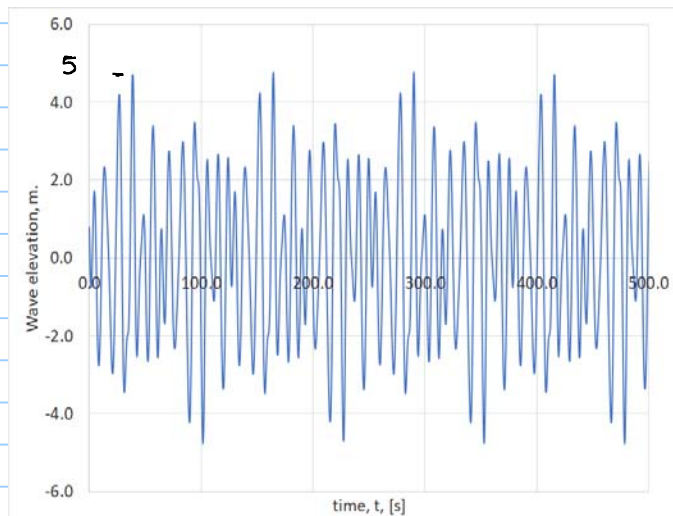


Surveys are made in the area for a few years (2 years)

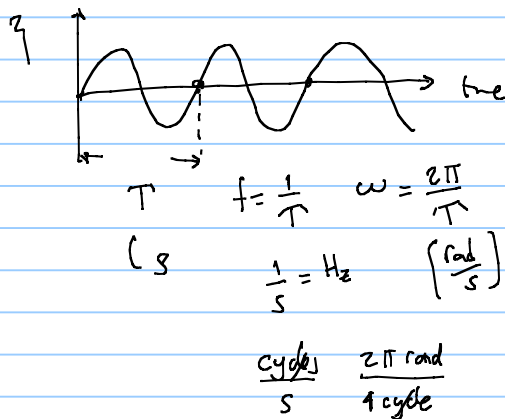


Exercise 9

Time [s]	Elevation [m]
0.0	0.8
0.5	0.0
1.0	-0.5
1.5	-0.8
2.0	-0.6
2.5	-0.1
3.0	0.5
3.5	1.1
4.0	1.6



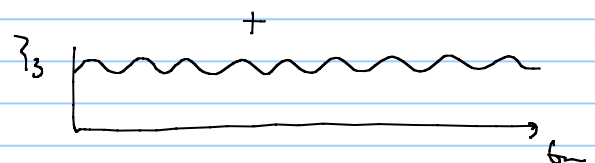
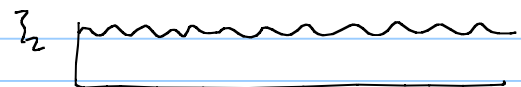
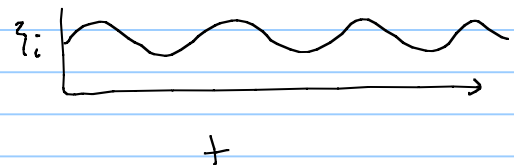
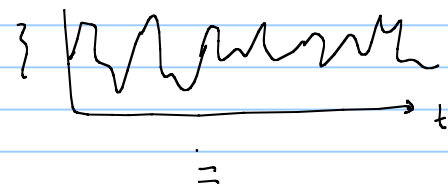
our intention is to determine a characteristic period / frequency



Fourier (french mathematician)

all signals can be expressed as a sum of sinusoidal functions

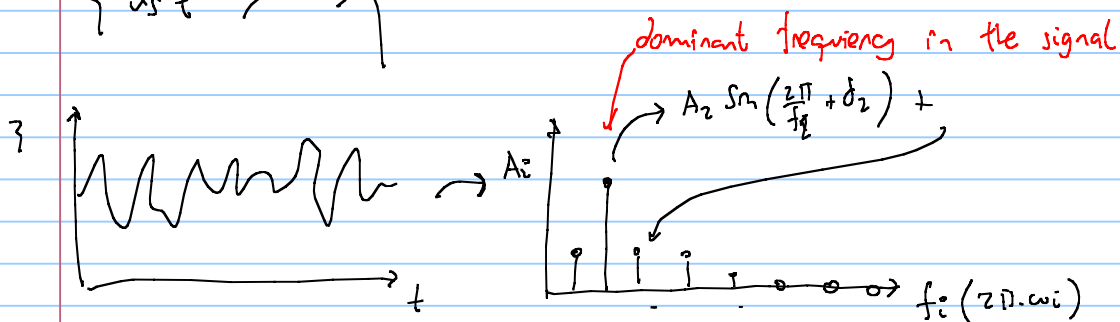
$$z(t) = \sum_{i=1}^N A_i \sin(\omega_i t + \delta_i)$$

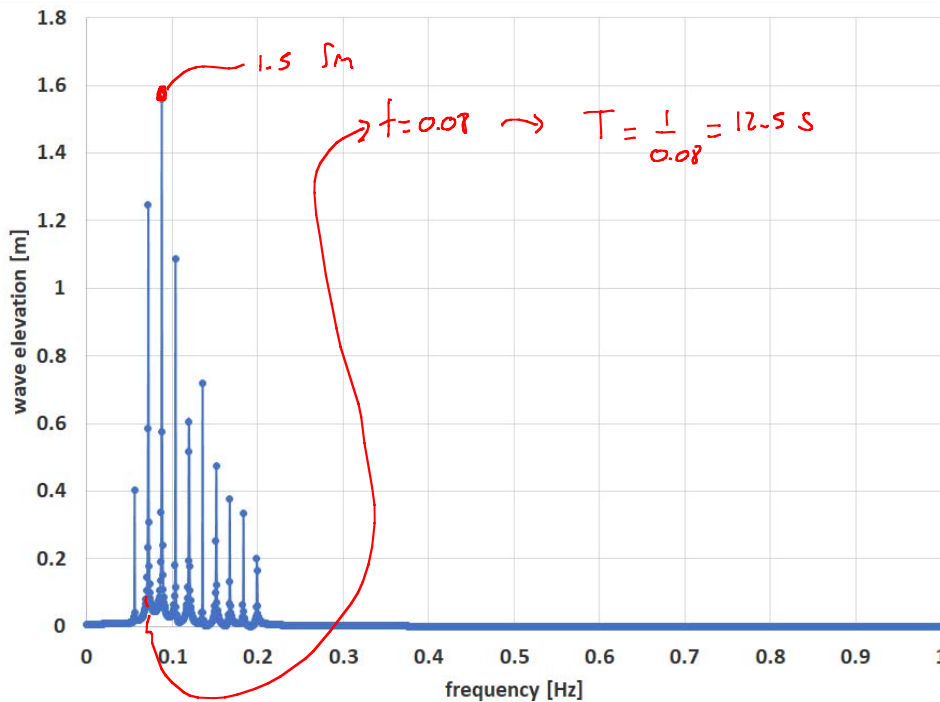


to process wave signals, we typically use

Fourier transform (FFT) fast Fourier transform

$$z \text{ vs } t \rightarrow \begin{cases} A_i & \omega_i & \delta_i \end{cases}$$





this frequency analysis is typically made for "sea states" (periods of time of about 3hrs) during which it is assumed they exhibit a dominant magnitude and period

$3h \rightarrow A, T$
 $3h \rightarrow A, T$
 $3h \rightarrow A, T$

repeat this analysis for 2 years

Apply a frequency analysis on the results

	Spectral Peak period (T _p) [s]																					
Hs [m]	0-3	3-4	4-5	5-6	6-7	7-8	8-9	9-10	10-11	11-12	12-13	13-14	14-15	15-16	16-17	17-18	18-19	19-20	20-21	21-22	22-23	
0-1	15	290	1367	2876	3716	3527	2734	1849	1138	656	362	192	101	52	26	13	7	3	2	1	0	
1-2	1	81	1153	5308	12083	17323	18143	15262	10980	7053	4169	2316	1229	631	315	155	75	36	17	8	4	
2-3	0	2	94	1050	4532	10304	15020	15953	13457	9752	5991	3403	1795	894	426	197	88	39	17	7	3	
3-4	0	0	2	72	686	2782	6171	8847	9189	7493	5082	2991	1577	762	345	148	61	24	9	4	1	
4-5	0	0	0	2	51	433	1645	3495	4807	4750	3638	2286	1229	584	251	100	37	13	5	1	0	
5-6	0	0	0	0	2	39	294	1037	2069	2664	2440	1709	968	463	193	72	25	8	2	1	0	
6-7	0	0	0	0	0	2	32	215	692	1264	1485	1228	767	382	159	57	18	5	1	0	0	
7-8	0	0	0	0	0	0	2	27	157	447	730	762	555	302	130	46	14	4	1	0	0	
8-9	0	0	0	0	0	0	0	2	23	112	276	392	355	223	104	38	11	3	1	0	0	
9-10	0	0	0	0	0	0	0	0	2	19	77	160	192	148	79	31	9	2	0	0	0	
10-11	0	0	0	0	0	0	0	0	0	2	16	50	85	85	55	24	8	2	0	0	0	
11-12	0	0	0	0	0	0	0	0	0	0	2	12	29	40	33	18	7	2	0	0	0	
12-13	0	0	0	0	0	0	0	0	0	0	0	2	8	15	17	12	5	2	0	0	0	
13-14	0	0	0	0	0	0	0	0	0	0	0	0	2	5	7	6	4	1	0	0	0	
14-15	0	0	0	0	0	0	0	0	0	0	0	0	0	1	2	3	2	1	0	0	0	
15-16	0	0	0	0	0	0	0	0	0	0	0	0	0	0	1	1	1	1	0	0	0	
16-17	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	
17-18	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	
Sum	16	373	2616	9308	21070	34410	44041	46687	42514	34212	24268	15503	8892	4587	2143	921	372	146	55	22	8	

flow assurance considerations in field development

ensure the uninterrupted flow of hydrocarbons from reservoir to processing facilities

- Wax $C_{12} \rightarrow$ long chain alkanes that precipitate from oil at low temperature

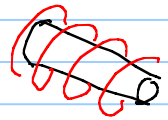


cause plugging of pipelines, cause malfunctioning of equipment.

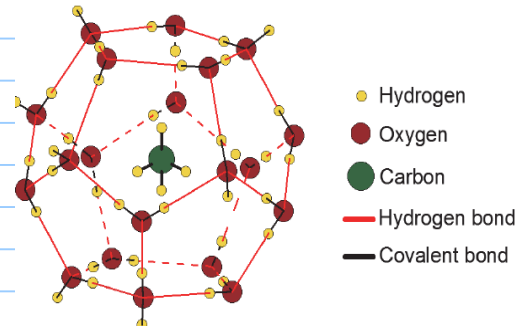
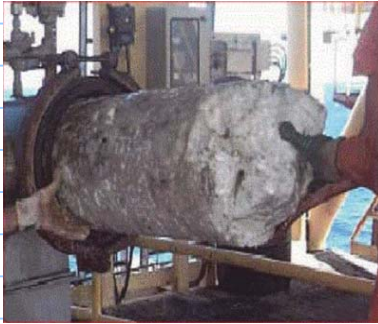
to avoid wax:

- wax inhibitor

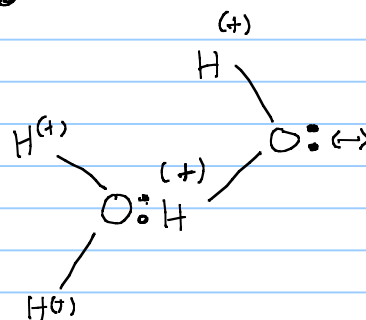
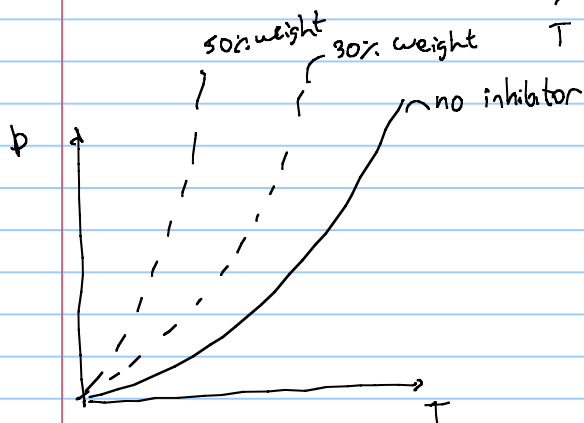
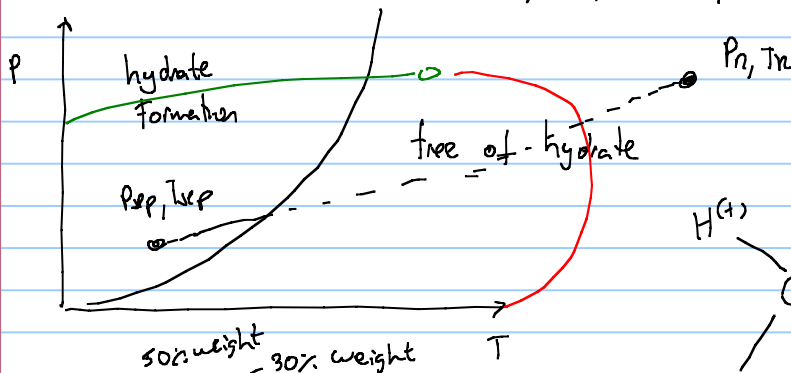
- use better pipe insulation
- use pipe heating



- hydrates



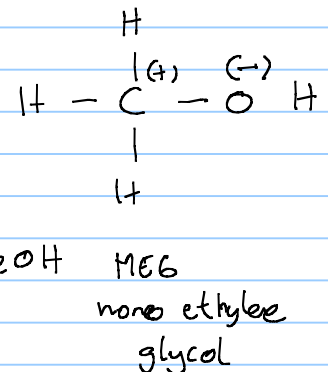
- free water
- small molecules of HC, C_1 , C_2 , CO_2 9 Å
- P, T, low temperature, high pressure



How to avoid hydrates?

- avoid cooling fluid
- heat the fluid
- chemical inhibitor $\rightarrow$

MeOH
methanol

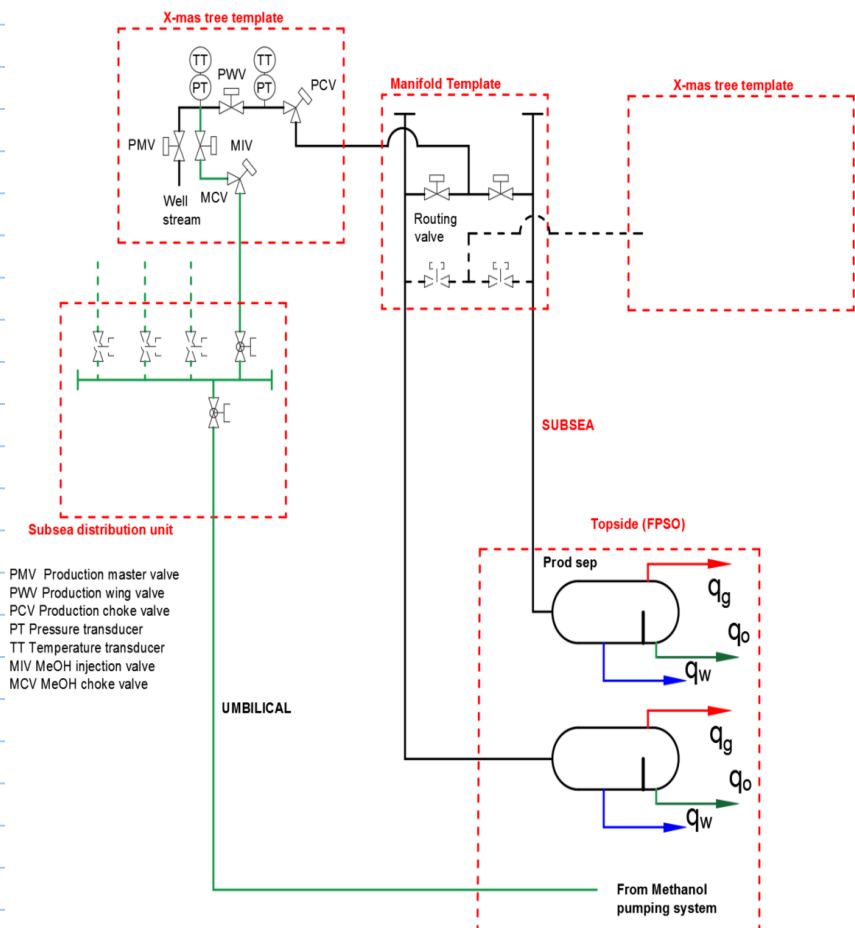
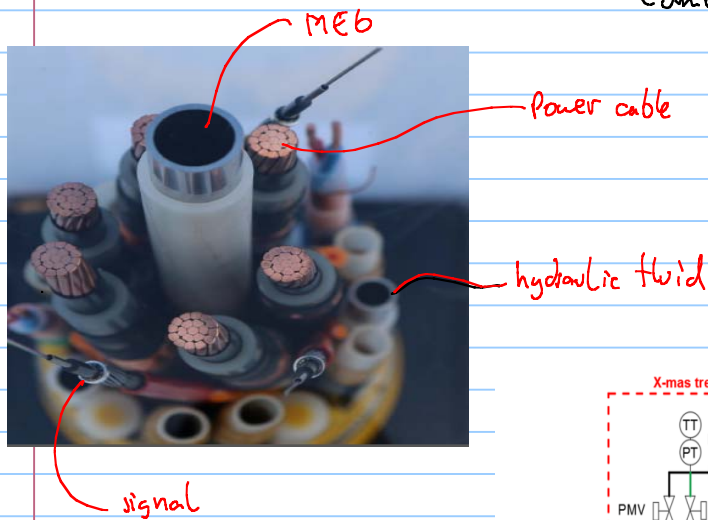
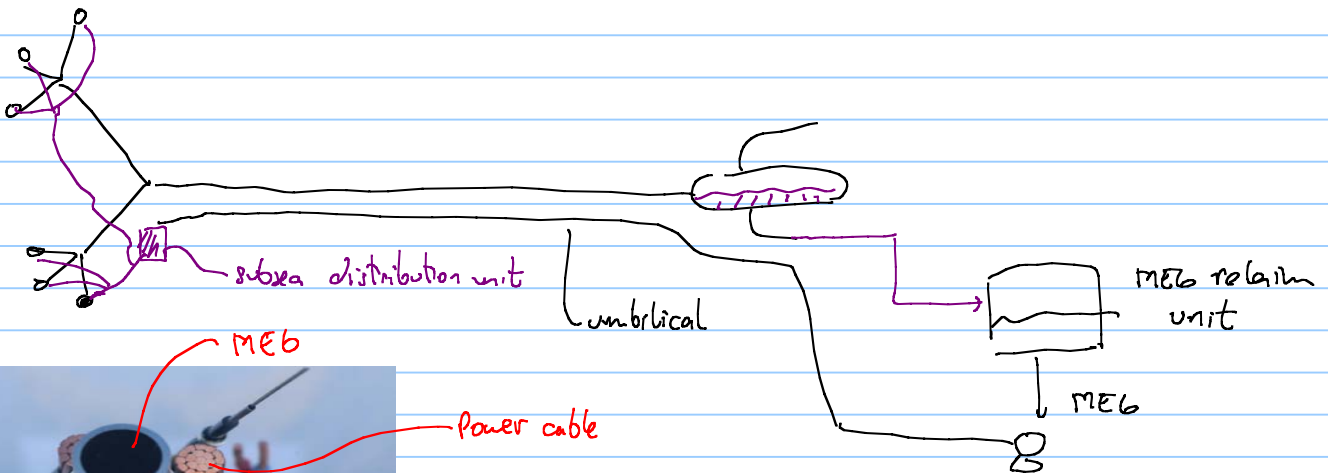


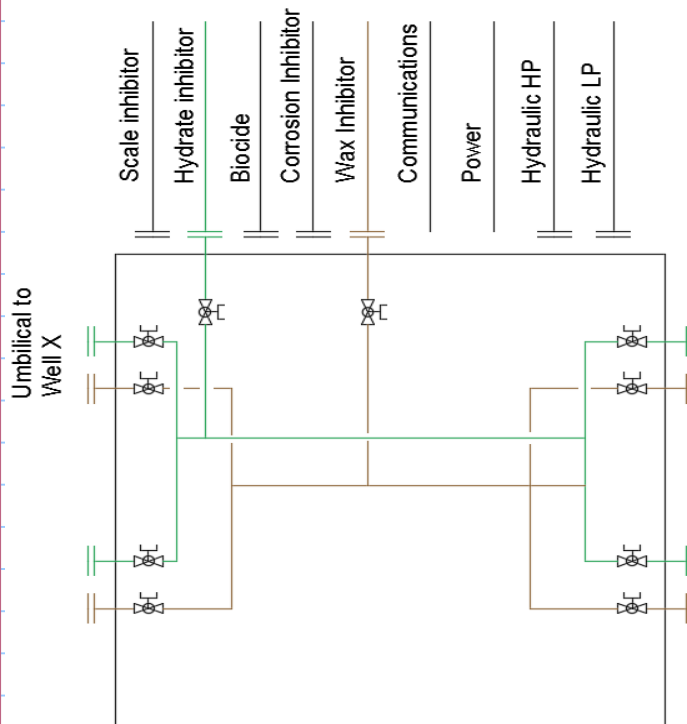
$$\text{weight \%} = \frac{\text{mass of inhibitor}}{\text{mass of inhibitor} + \text{mass water}}$$

50 bbls of water $\sim$ 50 bbls of MEG

if MEG or MeOH are not recovered (reclaim) this can lead to huge expenses!

So usually this fluid is recovered from the production stream





- scale → precipitation of minerals from water

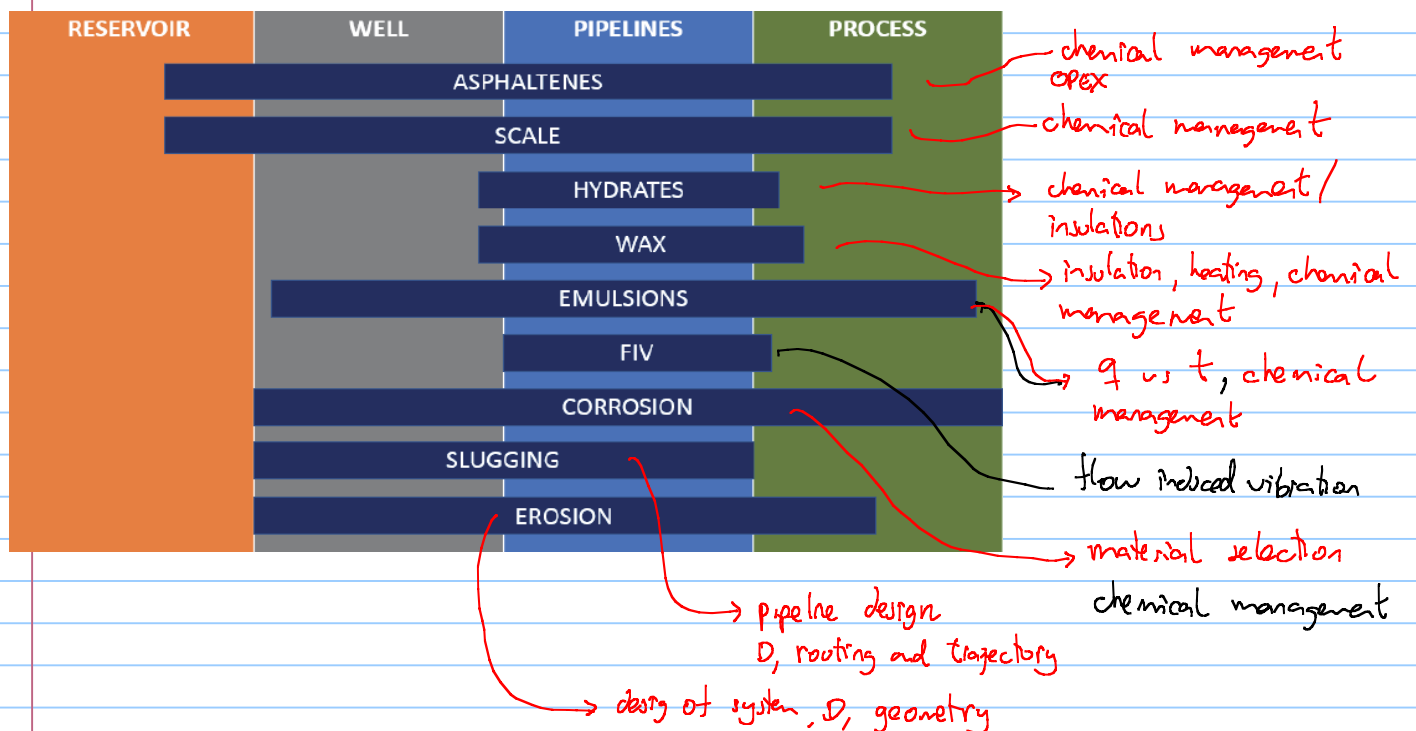


Choke on FCM 100013142 S/N1 01

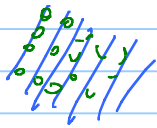
- changes in solubility of these minerals
- changes in T, p, mixing water from different sources (formation water + sea water)

preventive action:

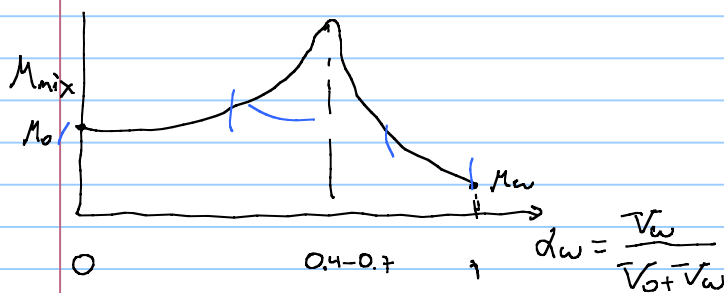
- scale inhibitor
- proper design of injection strategy
- mechanical removal



Emulsions: stable small size dispersion of oil in water
water in oil

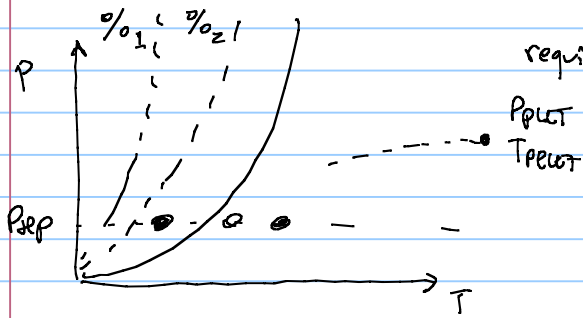


longer separation time required
bottlenecking the system



to deal with emulsions we use
demulsifiers $\rightarrow$ breaks stability of emulsions

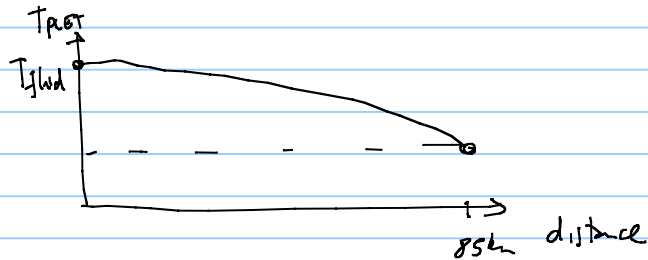
Class exercise: Analyzing hydrate risk in transportation pipeline of B2. Estimate amounts of inhibitor required. (nr. 3)



required information: hydrate line without inhibitor
with inhibitor

• inlet conditions to pipeline

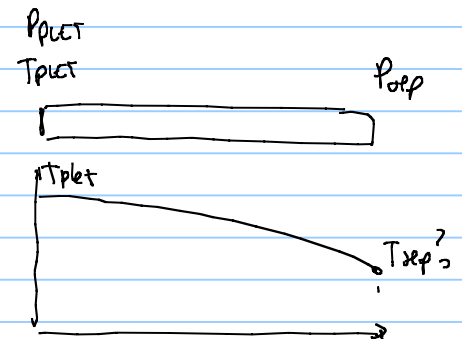
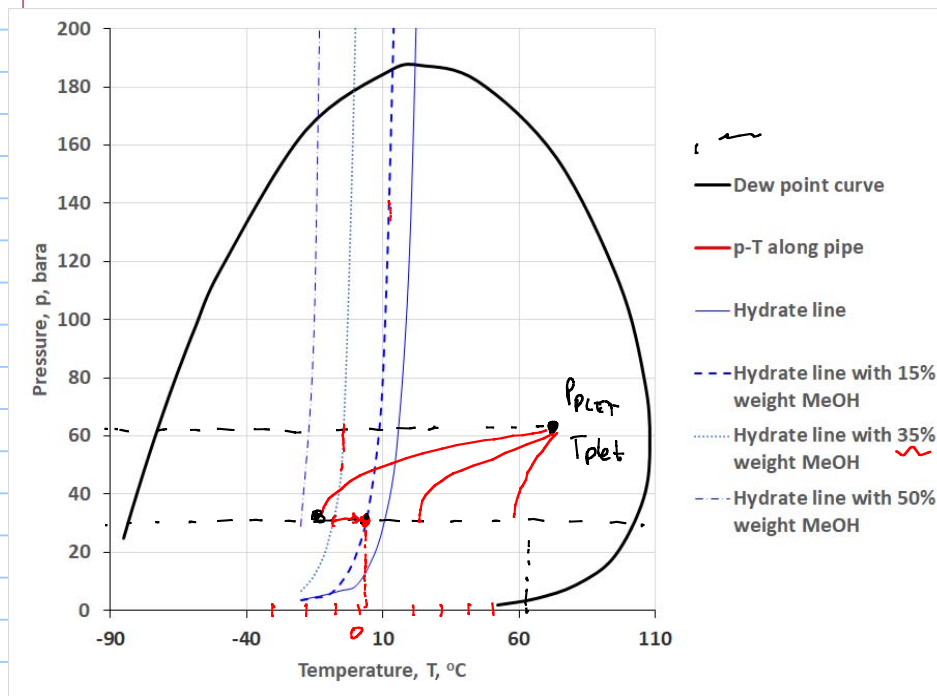
P_{PLET}
 T_{PLET}



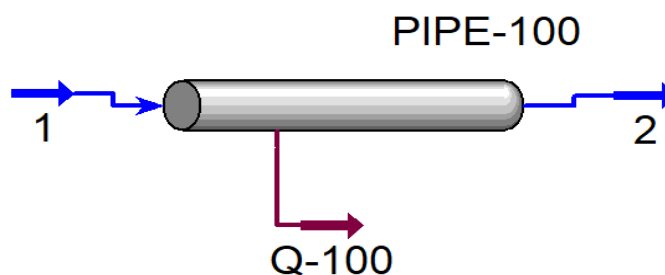
• P_{sep}

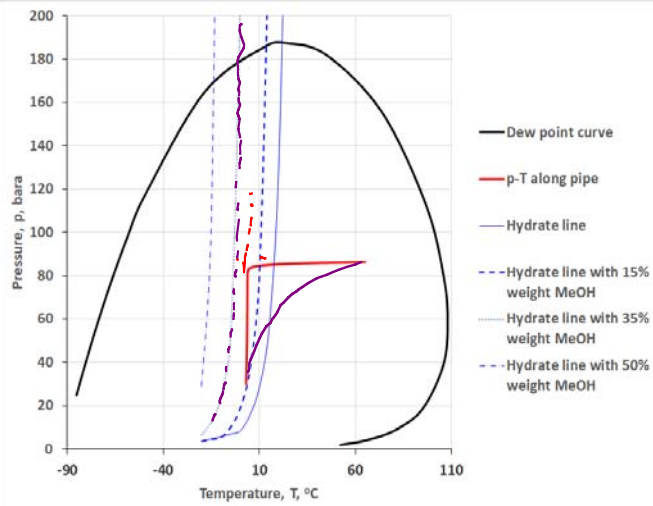
• gas rate

• pipe diameter, length, heat transfer coefficient, T_{amb} (subsea)



$T_{sep} = 3^{\circ}\text{C}$, therefore, there is hydrate formation risk!





Solution: inject 35% w of MeOH



THE END