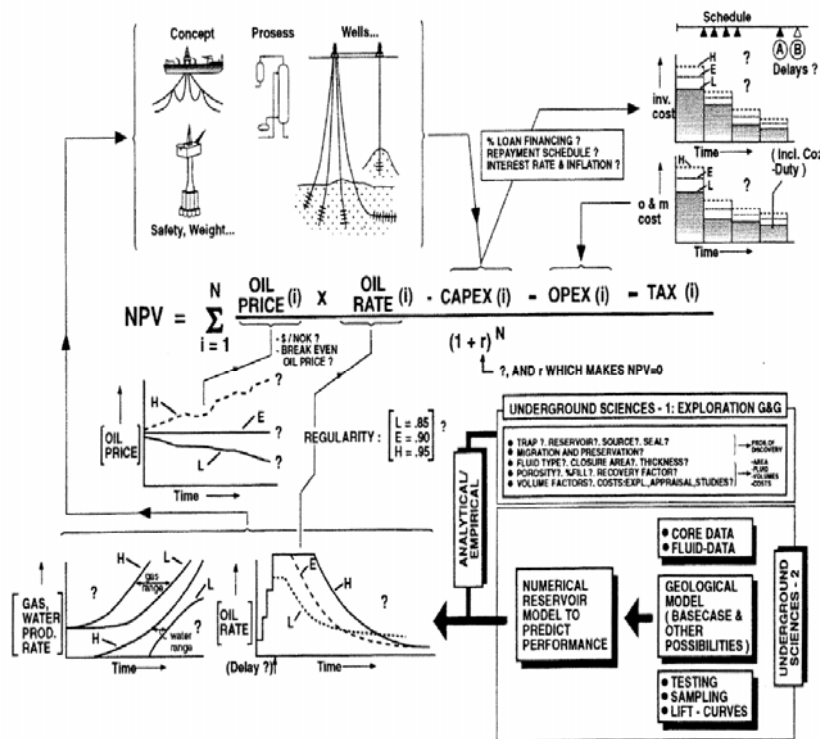


Day 4 05.12.2019

NPV calculations
 Reserve estimation
 probability/decision trees



- Usually royalties and taxes must be considered in NPV calculations.
 fixed amount(%) of revenue (%,) of net profit

- Other costs such as EXPEX (exploration expenditures)
 ABEX (Abandonment costs)

might be included in NPV calculations

will be covered more
 in detail in petroleum
 economics course
 (Trygve Strøm)

$$NPV = \sum_{i=1}^N \frac{Revenue(i) - expenses(i)}{(1+dc)^i} = \frac{P_o(i) \cdot \Delta N_p(i) + P_g(i) \cdot \Delta G_p(i) - CAPEX(i) - OPEX(i)}{(1+dc)^i}$$

year
 counter

dc discount factor $\sim$ (6% $\sim$ 12%)

$$\left(\frac{1}{1+dc}\right)^i$$

for year 1 : $\frac{1}{(1.06)^1} = 0.94$
 6%

for year 10 : $\frac{1}{(1.06)^{10}} = 0.56$
 6%

class exercise

CAPEX + DRILLEX + OPEX

discounted cash flow

time	ΔG_p	Revenue	CAPEX	DRILLEX	OPEX	Expenses	Cash flow	DCF
1	0	0	(-)	(-)	0	(-)	Revenue - Expenses	$\frac{CF}{(1+dc)^t}$
2	0	0	(-)	(-)	0	(-)		
3	0	0	(-)	(-)	0	(-)		
4	0	0	(-)	(-)	0	(-)		
5	0	0	(-)	(-)	0	(-)		
6	ΔG_{p6}	$\Delta G_p \cdot P_g$	0	0	(-)	(-)		
7	ΔG_{p7}	"	0	0	(-)	(-)		
8	"	"	0	0	(-)	(-)		
9	"	"	0	0	(-)	(-)		
10	"	"	0	0	(-)	(-)		
11	"	"	0	0	(-)	(-)		

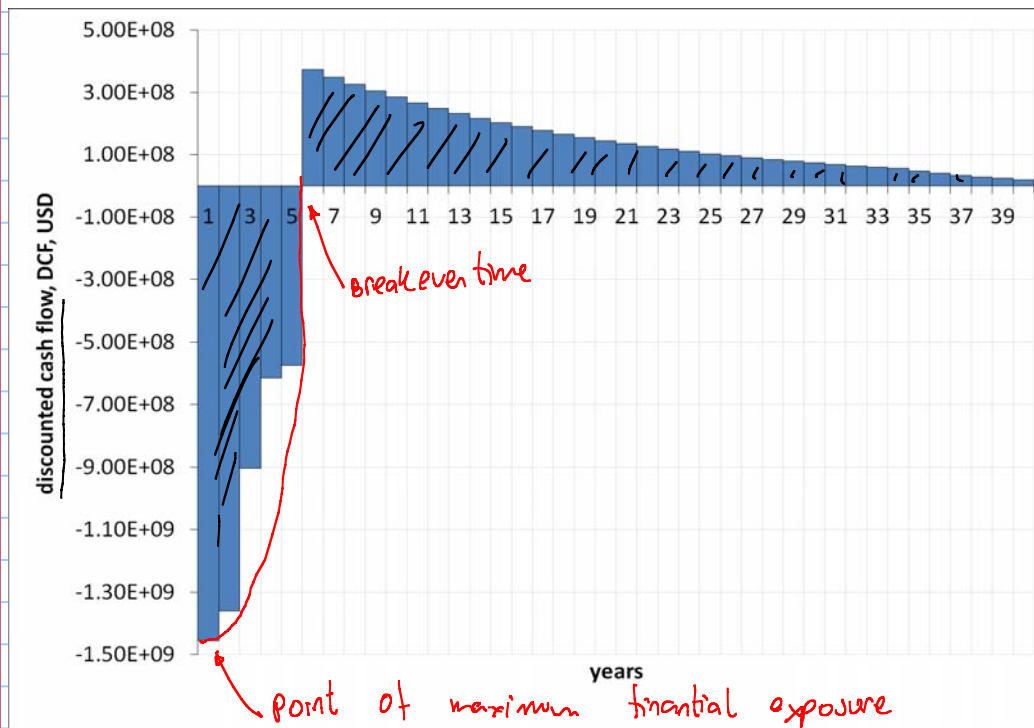
$\sum \frac{CF}{(1+dc)^t} = NPV$

B2 example

Well drilling cost	150	[1E6 USD]	Observations:
water depth	2500	[m]	Maximum 5 wells can be drilled per year
Discount rate	0.07	[-]	all CAPEX is invested evenly during the first 5 years
Uptime	360	days/year	
OPEX	1.20E+08	USD/year	
Gas price	0.11	[USD/Sm ³]	
CAPEX _{LING}	3.48E+09	USD	
CAPEX _{SUBSEA}	5.58E+08	USD	

Time	Gas production in year	Revenue	DRILLEX	CAPEX _{SUBSEA}	CAPEX _{LING}	OPEX	Total Cost	Cash Flow	Discounted Cash Flow: PV(i)
end of year	[Sm ³]	USD	USD	USD	USD	USD	USD	USD	USD
1	0	0.00E+00	7.50E+08	1.12E+08	6.95E+08	0	1.56E+09	-1.56E+09	-1.46E+09
2	0	0.00E+00	7.50E+08	1.12E+08	6.95E+08	0	1.56E+09	-1.56E+09	-1.36E+09
3	0	0.00E+00	3.00E+08	1.12E+08	6.95E+08	0	1.11E+09	-1.11E+09	-9.04E+08
4	0	0.00E+00	0.00E+00	1.12E+08	6.95E+08	0.00E+00	8.07E+08	-8.07E+08	-6.16E+08
5	0	0.00E+00	0.00E+00	1.12E+08	6.95E+08	0.00E+00	8.07E+08	-8.07E+08	-5.75E+08
6	6.5E+9	6.80E+08	0.00E+00	0.00E+00	0.00E+00	1.20E+08	1.20E+08	5.60E+08	3.73E+08
7	6.5E+9	6.80E+08	0.00E+00	0.00E+00	0.00E+00	1.20E+08	1.20E+08	5.60E+08	3.49E+08
8	6.5E+9	6.80E+08	0.00E+00	0.00E+00	0.00E+00	1.20E+08	1.20E+08	5.60E+08	3.26E+08
9	6.5E+9	6.80E+08	0.00E+00	0.00E+00	0.00E+00	1.20E+08	1.20E+08	5.60E+08	3.05E+08
10	6.5E+9	6.80E+08	0.00E+00	0.00E+00	0.00E+00	1.20E+08	1.20E+08	5.60E+08	2.85E+08
11	6.5E+9	6.80E+08	0.00E+00	0.00E+00	0.00E+00	1.20E+08	1.20E+08	5.60E+08	2.66E+08
12	6.5E+9	6.80E+08	0.00E+00	0.00E+00	0.00E+00	1.20E+08	1.20E+08	5.60E+08	2.49E+08
13	6.5E+9	6.80E+08	0.00E+00	0.00E+00	0.00E+00	1.20E+08	1.20E+08	5.60E+08	2.33E+08
14	6.5E+9	6.80E+08	0.00E+00	0.00E+00	0.00E+00	1.20E+08	1.20E+08	5.60E+08	2.17E+08
15	6.5E+9	6.80E+08	0.00E+00	0.00E+00	0.00E+00	1.20E+08	1.20E+08	5.60E+08	2.03E+08
16	6.5E+9	6.80E+08	0.00E+00	0.00E+00	0.00E+00	1.20E+08	1.20E+08	5.60E+08	1.90E+08
17	6.5E+9	6.80E+08	0.00E+00	0.00E+00	0.00E+00	1.20E+08	1.20E+08	5.60E+08	1.77E+08
18	6.5E+9	6.80E+08	0.00E+00	0.00E+00	0.00E+00	1.20E+08	1.20E+08	5.60E+08	1.66E+08
19	6.5E+9	6.80E+08	0.00E+00	0.00E+00	0.00E+00	1.20E+08	1.20E+08	5.60E+08	1.55E+08
20	6.5E+9	6.80E+08	0.00E+00	0.00E+00	0.00E+00	1.20E+08	1.20E+08	5.60E+08	1.45E+08
21	6.5E+9	6.80E+08	0.00E+00	0.00E+00	0.00E+00	1.20E+08	1.20E+08	5.60E+08	1.35E+08
22	6.5E+9	6.80E+08	0.00E+00	0.00E+00	0.00E+00	1.20E+08	1.20E+08	5.60E+08	1.26E+08
23	6.5E+9	6.80E+08	0.00E+00	0.00E+00	0.00E+00	1.20E+08	1.20E+08	5.60E+08	1.18E+08
24	6.5E+9	6.80E+08	0.00E+00	0.00E+00	0.00E+00	1.20E+08	1.20E+08	5.60E+08	1.10E+08
25	6.5E+9	6.80E+08	0.00E+00	0.00E+00	0.00E+00	1.20E+08	1.20E+08	5.60E+08	1.03E+08
26	6.5E+9	6.80E+08	0.00E+00	0.00E+00	0.00E+00	1.20E+08	1.20E+08	5.60E+08	9.65E+07
27	6.5E+9	6.80E+08	0.00E+00	0.00E+00	0.00E+00	1.20E+08	1.20E+08	5.60E+08	9.02E+07
28	6.5E+9	6.80E+08	0.00E+00	0.00E+00	0.00E+00	1.20E+08	1.20E+08	5.60E+08	8.43E+07
29	6.5E+9	6.80E+08	0.00E+00	0.00E+00	0.00E+00	1.20E+08	1.20E+08	5.60E+08	7.88E+07
30	6.5E+9	6.80E+08	0.00E+00	0.00E+00	0.00E+00	1.20E+08	1.20E+08	5.60E+08	7.36E+07
31	6.5E+9	6.80E+08	0.00E+00	0.00E+00	0.00E+00	1.20E+08	1.20E+08	5.60E+08	6.88E+07
32	6.5E+9	6.80E+08	0.00E+00	0.00E+00	0.00E+00	1.20E+08	1.20E+08	5.60E+08	6.43E+07
33	6.5E+9	6.80E+08	0.00E+00	0.00E+00	0.00E+00	1.20E+08	1.20E+08	5.60E+08	6.01E+07
34	6.5E+9	6.80E+08	0.00E+00	0.00E+00	0.00E+00	1.20E+08	1.20E+08	5.60E+08	5.62E+07
35	6.0E+9	6.30E+08	0.00E+00	0.00E+00	0.00E+00	1.20E+08	1.20E+08	5.10E+08	4.78E+07
36	5.5E+9	5.81E+08	0.00E+00	0.00E+00	0.00E+00	1.20E+08	1.20E+08	4.61E+08	4.03E+07
37	5.1E+9	5.36E+08	0.00E+00	0.00E+00	0.00E+00	1.20E+08	1.20E+08	4.16E+08	3.40E+07
38	4.7E+9	4.95E+08	0.00E+00	0.00E+00	0.00E+00	1.20E+08	1.20E+08	3.75E+08	2.87E+07
39	4.4E+9	4.58E+08	0.00E+00	0.00E+00	0.00E+00	1.20E+08	1.20E+08	3.38E+08	2.42E+07
40	4.0E+9	4.24E+08	0.00E+00	0.00E+00	0.00E+00	1.20E+08	1.20E+08	3.04E+08	2.03E+07
							NPV		1.92E+08

① Homework: repeat NPV calculation for $q_{plateau} = 25 \text{ EOG Sm}^3/\text{d}$



Revenue and Cost Profiles

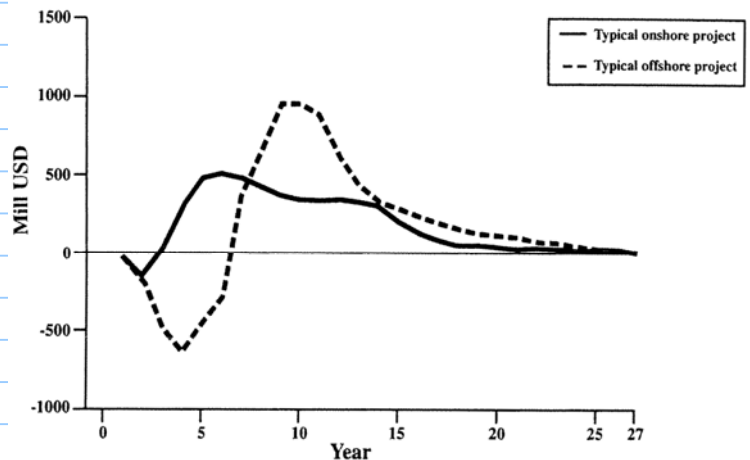
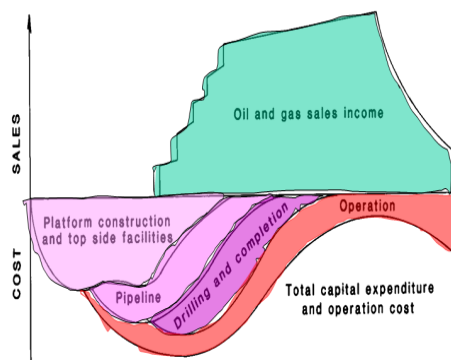


Fig. 9. Typical before tax cash flow profiles for offshore and onshore projects.

we should always evaluate the effect of uncertainty

Sensitivity analysis

P_g, P_o
 Cost figures
 production rates

→ change one variable at the time while keeping all others fixed

for gas price $P_g \rightarrow 1.2 P_g (+20)\%$

$\rightarrow 0.8 P_g (-20)\%$

for our problem, evaluate the effect of uncertainty :

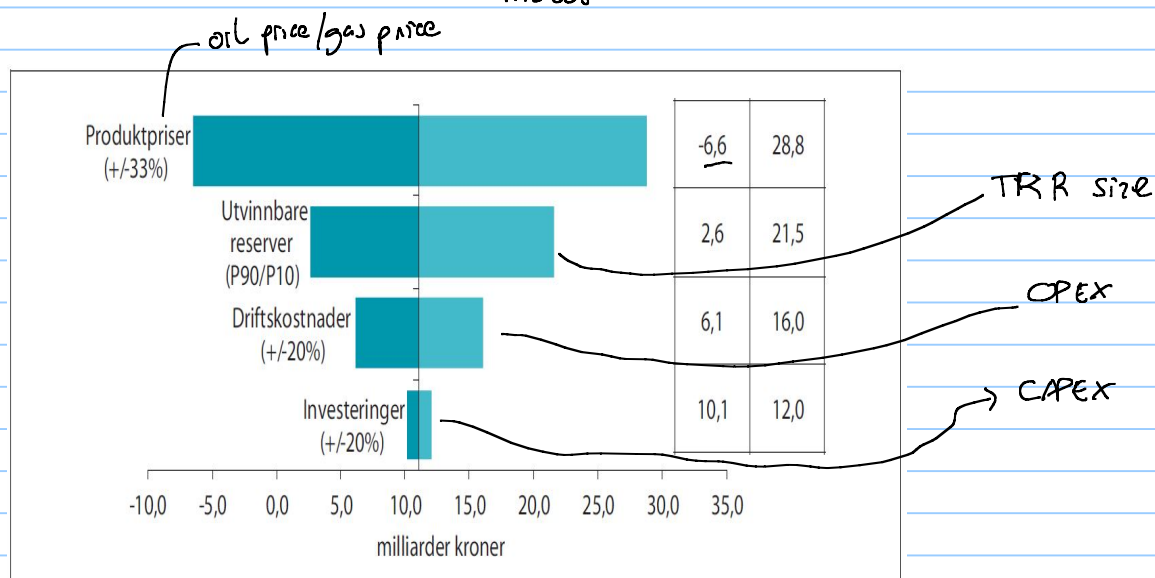
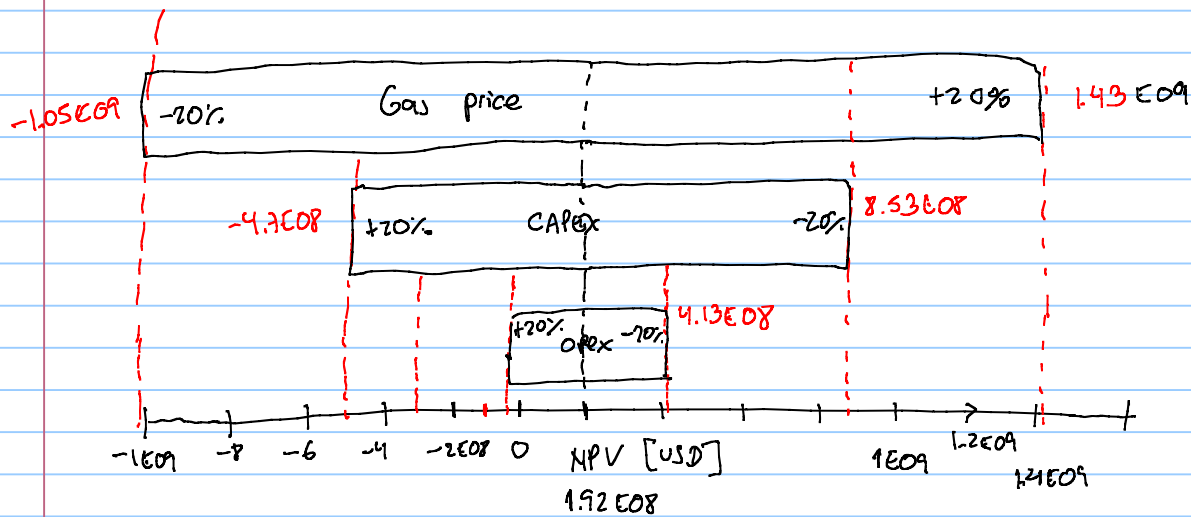
$\pm 20\%$ gas price
 $\pm 20\%$ Capex values
 $\pm 20\%$ OPEX

1) • change $P_g \rightarrow P_g \cdot 1.2 \rightarrow$ Compute NPV $\rightarrow$ return to P_g

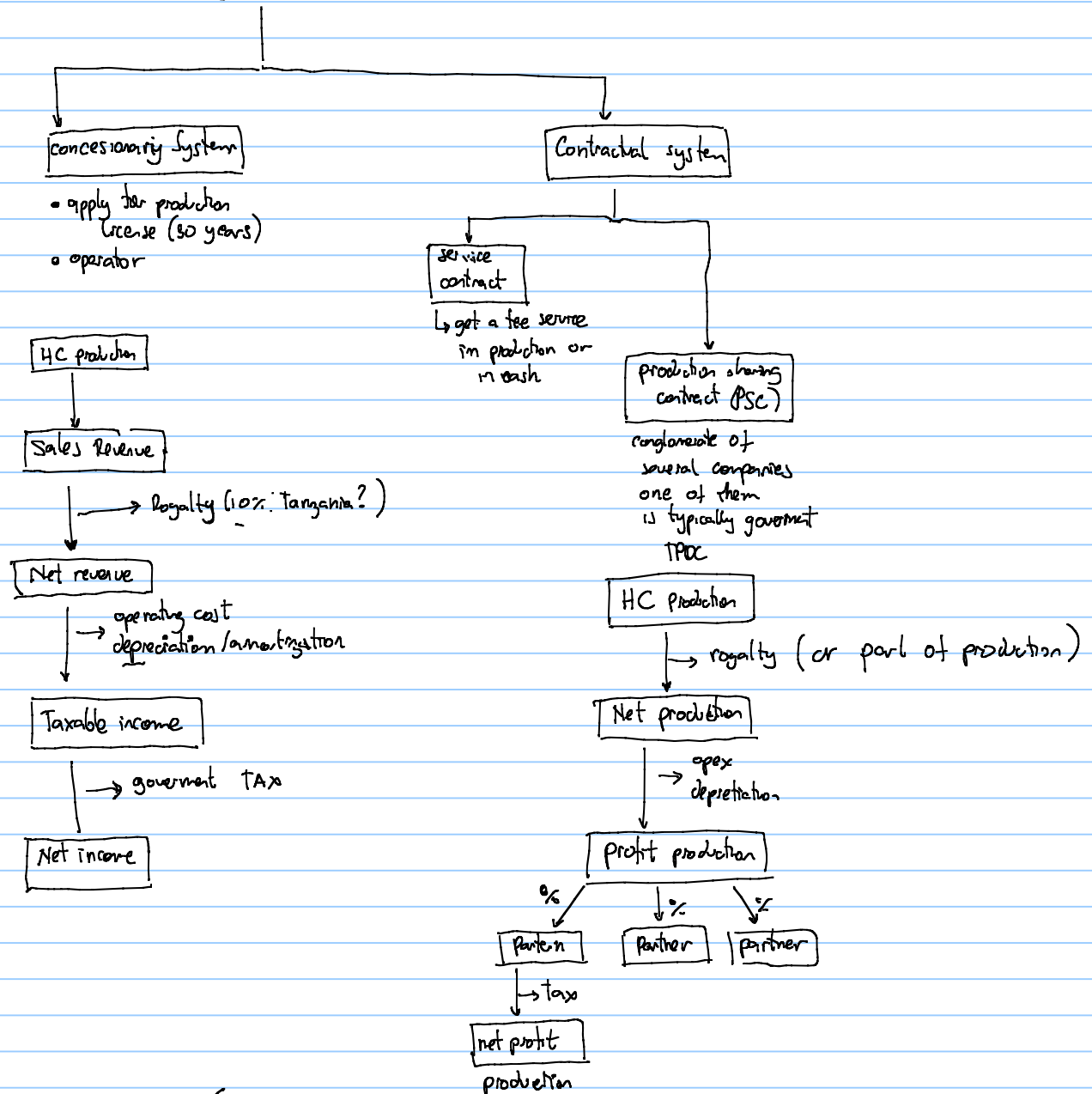
2) • change $P_g \rightarrow P_g \cdot 0.8 \rightarrow$ Compute NPV $\rightarrow$ return to P_g

Variable	NPV		
	-20%	BASE CASE	+20%
gas price	-1.05E9	1.92E8	1.43E09
CAPEX	8.53E08	1.92E8	-4.7E8
OPEX	4.13E08	1.92E8	-3E07

tornado chart



Petroleum fiscal systems

Reserve estimation (060, 061, 062)

→ estimating $N, G \rightarrow N_{pu}, G_{pu}$

$$N_{pu} = N \cdot F_{ru}$$

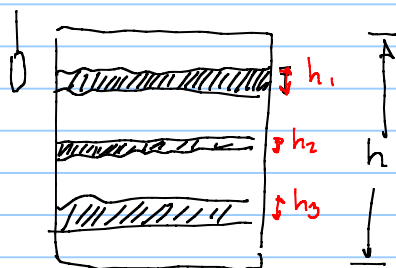
$$G_{pu} = G \cdot F_{ru}$$

ultimate recovery factor

$$N = \frac{\overbrace{V_R} \cdot \overbrace{\phi} \cdot \overbrace{S_o} \cdot \overbrace{N_{Tc}}}{\underbrace{B_o}}$$



N_{TG} --- Net to gross



reservoir rock layers which are not "clean" not "hydrocarbon-bearing" rock

$$N_{TG} = \frac{\sum h_i}{h} = \frac{h_1 + h_2 + h_3}{h}$$

is a multiplier to the total rock volume, to account for the presence of non productive layers.

$$N_{pu} = N_{FGU} = \frac{V_R \cdot \Phi \cdot S_o \cdot N_{TG} \cdot F_{RU}}{B_o}$$

The input to this equation is not a single number!

$\Phi \rightarrow$

$V_R \rightarrow$

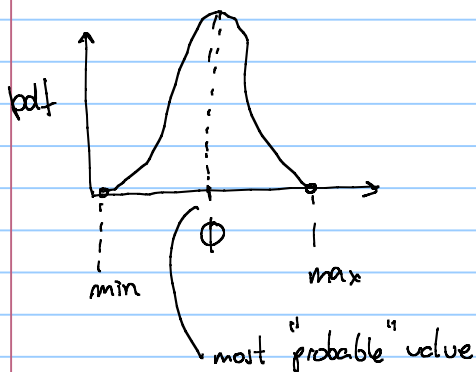
$S_o \rightarrow$

$B_o \rightarrow$

$N_{TG} \rightarrow$

$F_{RU} \rightarrow$

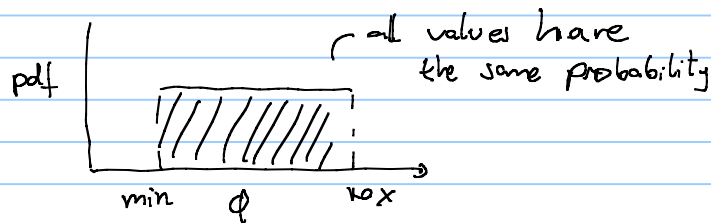
we are also interested in computing N_{pu} as a range, with associated probabilities



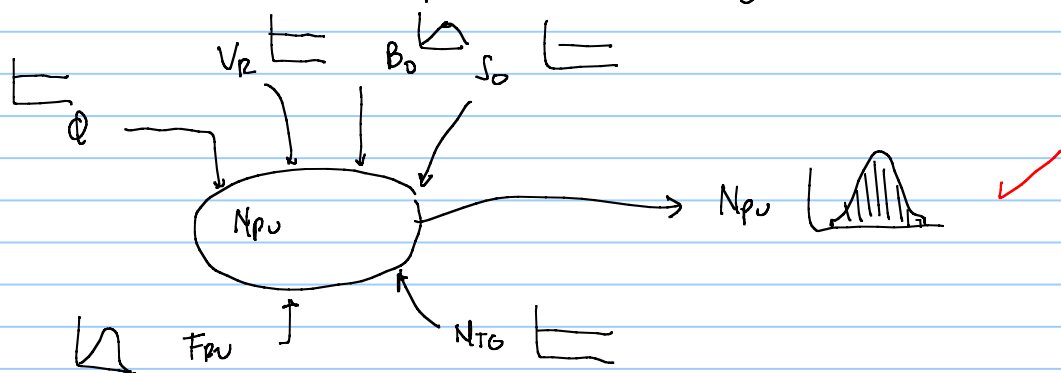
pdf probability density function

pdf probability distribution function

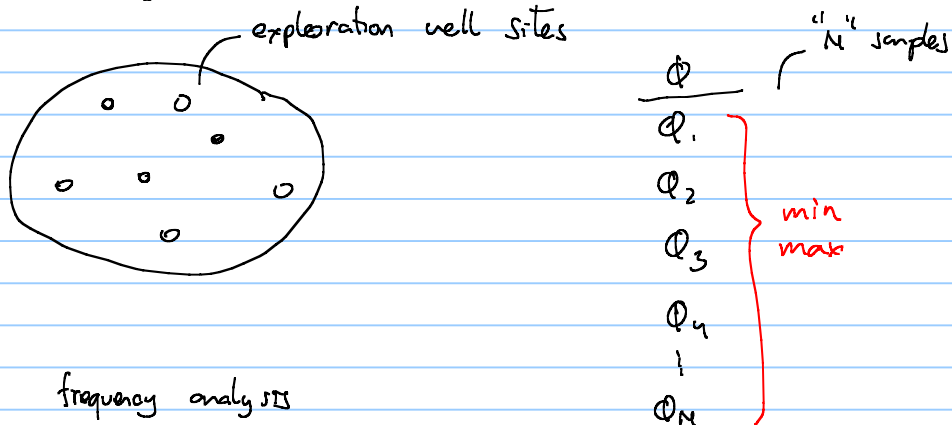
if i have no prior information



what i am interested in computing is the resulting distribution for N_{pu}



estimating probability distribution using measured data



frequency analysis

Φ $\leftarrow$ "N" samples

Φ_1

Φ_2

Φ_3

Φ_4

$\vdots$

Φ_N

min
max

min
max

make

- define certain number of bins n
 n should be much less than N (number of samples)
- determine minimum and maximum values of sample

n should be much less than N (number of samples)

- determine minimum and maximum values of sample

 Φ_{mir}

$$\Delta\phi_z = \frac{\phi_{max} - \phi_{min}}{n-1}$$

$$Q_{max}$$

- generate bins

bins

Omiz

$$\Phi_1 = \Phi_{m\hat{r}} + \Delta\Phi$$

$$\Phi_1 = \Phi_0 + \Delta\Phi$$

1

$$\Phi_{max} = \Phi_{i-1} + \Delta\Phi$$

Qmiz

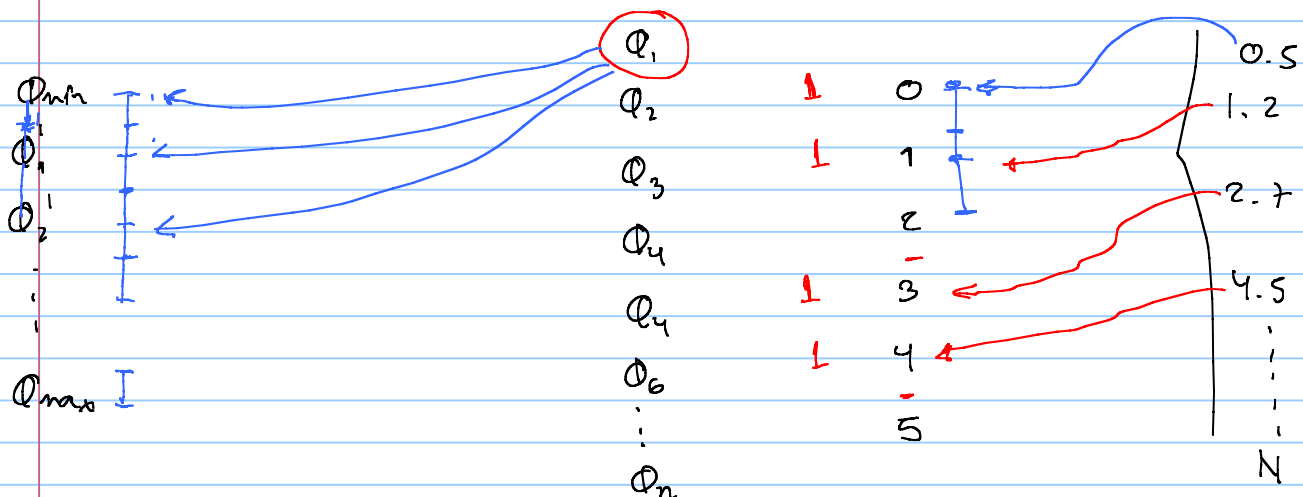
$$\Delta\phi = \frac{\phi_{max} - \phi_{min}}{2}$$

$Q_1 -$

$$Q_{max}$$

$$\phi_i = \phi_{min} + \frac{(\phi_{max} - \phi_{min})}{2} =$$

- look at each value in sample and assign it to a bin

 Q_2 Q₂ Φ_y

Q_2

 O_6

1

 Φ_n 

1

2

3

4

5

Q. 5

1. 2

2.7

1. 2

1

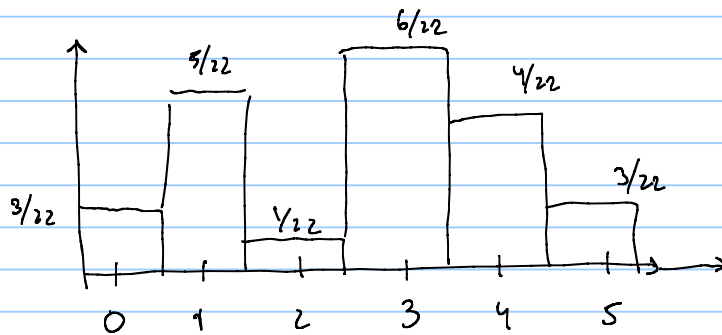
1

- count the number of samples assigned to each bin and probability

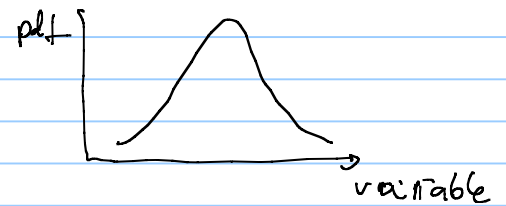
$n = 6$

bin	Count	frequency
0	3	$3/22$
1	5	$5/22$
2	1	$1/22$
3	6	$6/22$
4	4	$4/22$
5	3	$3/22$

$N = 22$

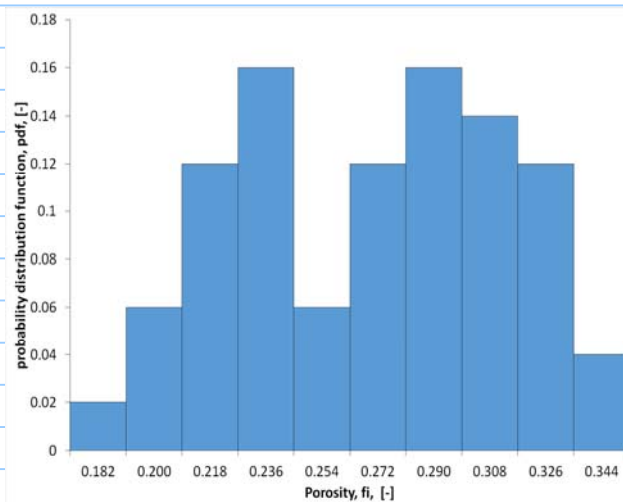


discrete probability distribution

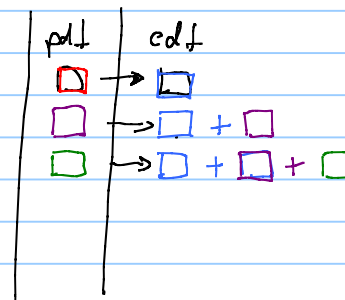


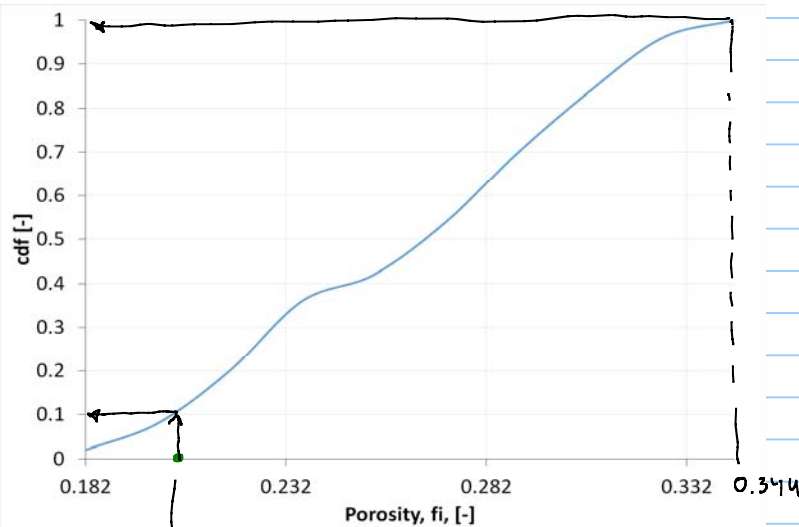
continuous probability distribution

(class) exercise → generate discrete frequency distribution for measured porosity data



cumulative distribution function (cdf)

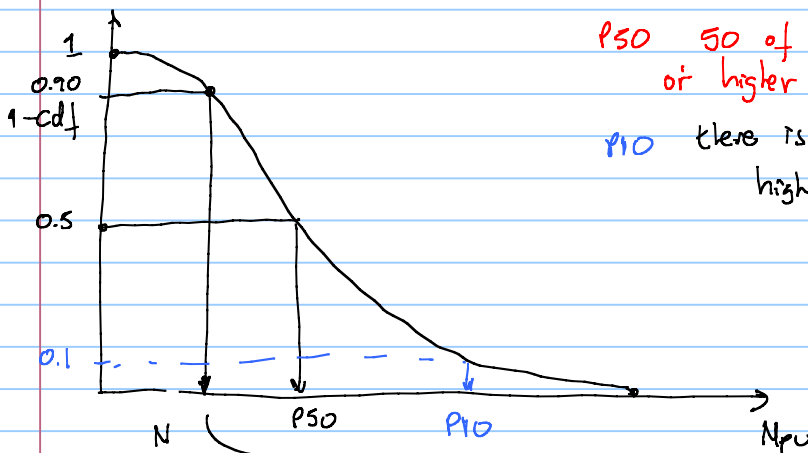




100% of the population has
 $\Phi = 0.344$ or less

$\Phi = 0.2 \rightarrow cdf = 10\%$ there is 10% probability that the porosity of my population is equal to $\Phi = 0.2$ or less

in reserves



P50 50% of the population will have N_{pv} or higher

P10 there is 10% chance that N_{pv} will be P10 or higher

each company uses their own percentiles

90 $\rightarrow$ 80

50 $\rightarrow$ 66

10 $\rightarrow$ 15, 5

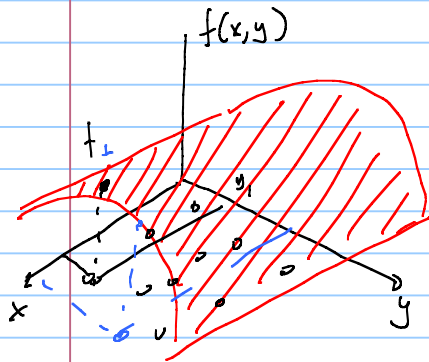
P90 90% of the total population will have N_{pv} of P90 or bigger

P10 P50 P90 P00 Hebron

Hebron Ben Nevis Oil	Upside Volumes		Best Estimate Volumes		Downside Volumes	
	MBO	Mm ³	MBO	Mm ³	MBO	Mm ³
D-94 Fault Block	1601	255	1328	211	1077	171
I-13 Fault Block	252	40	187	30	141	22
Total Hebron Ben Nevis	1870	297	1515	241	1204	191
Total Hebron Ben Nevis Gas	Upside Volumes		Best Estimate Volumes		Downside Volumes	
	GCF	* GSm ³	GCF	GSm ³	GCF	GSm ³
Solution Gas D-94 Block	112	3.2	145	4.1	189	5.4
Solution Gas I-13 Block	10	0.3	14	0.4	22	0.6
Non-associated Gas	n/a	n/a	n/a	n/a	n/a	n/a
Gas Cap D-94 Block only	0	0	0	0	31	0.9

* GSm³ = 10⁹ cubic meters

to compute the pdf and cdf of N_{pu} , we will use sampling method called Monte-Carlo



$$f(x,y) = x^2 + y^2 \quad \text{random sampling}$$

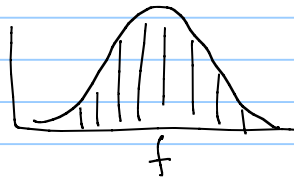
$$x_1, y_1 \rightarrow f_1$$

$$x_2, y_2 \rightarrow f_2$$

repeat for many random samples

$$(f_1, f_2, \dots, f_N)$$

apply a frequency analysis to the results



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Number 247

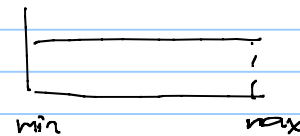
SEPTEMBER 1949

Volume 44

THE MONTE CARLO METHOD

NICHOLAS METROPOLIS AND S. ULAM
Los Alamos Laboratory

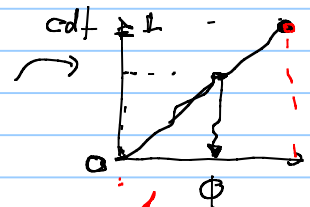
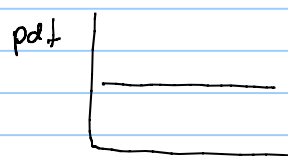
1) • Assign pdf for all input data

$$\left. \begin{array}{l} \Phi \\ V_R \\ B_0 \\ S_0 \\ N_{TG} \\ F_{RW} \end{array} \right\}$$


2) • take a random sample for each variable in each range.

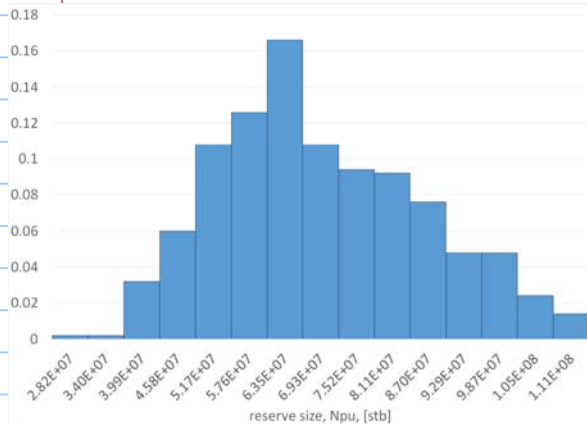
$$\text{cdf} = \frac{(X - X_{\min})}{(X_{\max} - X_{\min})}$$

$$X = \text{RAND}(0-1) [X_{\max} - X_{\min}] + X_{\min}$$

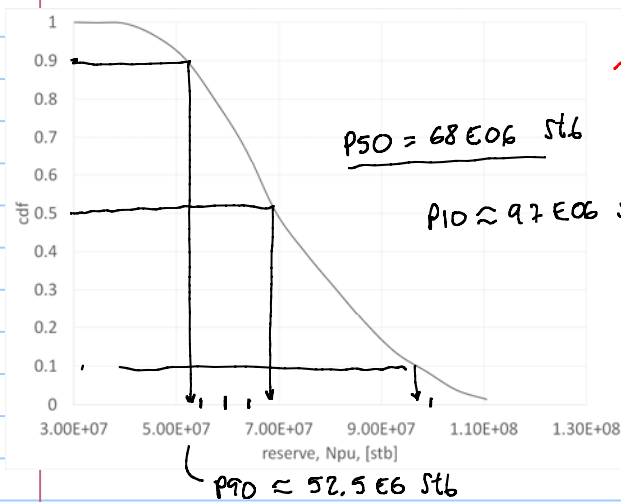


- 3) • compute N_{pu} with all random input.
- 4) • record N_{pu} value
- 5) • repeat from step 2, "Many" times (500)

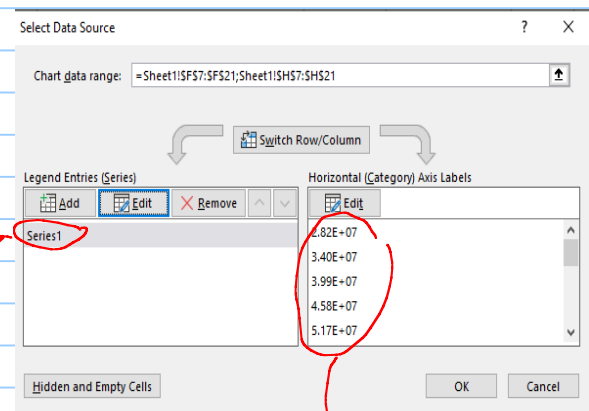
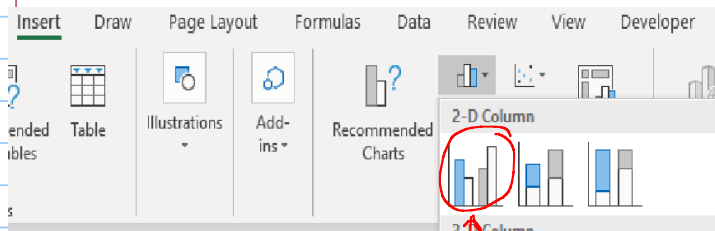
Class exercise



		Net to Gros		Oil Saturation	Formation Volume F		Ultimate Recovery Factor
	Rock volume	Porosity	N/G	So=(1-Sw)	Bo	Fr	
	bbl	fraction	fraction	fraction	Res bbl/STB	fraction	
Min	2.00E+09	0.18	0.3	0.8	1.35	0.42	
Max	2.50E+09	0.3	0.5	0.9	1.6	0.65	
MC it	Rock volume	Porosity	N/G	So=(1-Sw)	Bo	Fr	Npu
[-]	bbl	fraction	fraction	fraction	Res bbl/STB	fraction	[stb]
1	2.16E+09	1.94E-01	4.97E-01	8.25E-01	1.39E+00	6.10E-01	7.51E+07
2	2.28E+09	2.51E-01	4.17E-01	8.06E-01	1.46E+00	5.76E-01	7.59E+07
3	2.44E+09	2.77E-01	4.31E-01	8.23E-01	1.52E+00	5.77E-01	9.12E+07



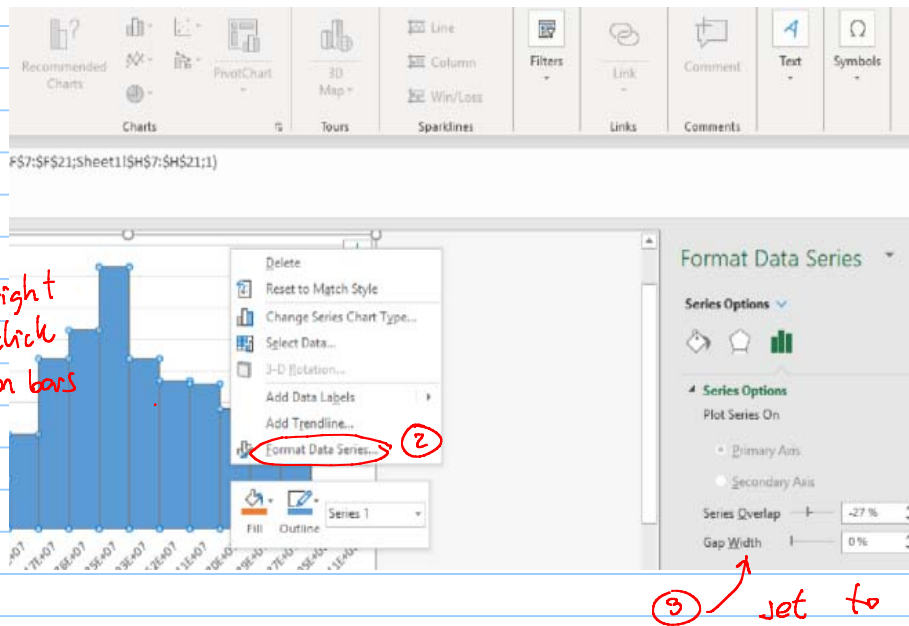
nr	bin	count	pdf	cdf
1	2.82E+07	1	0.002	1
2	3.40E+07	1	0.002	0.998
3	3.99E+07	16	0.032	0.996
4	4.58E+07	30	0.06	0.964
5	5.17E+07	54	0.108	0.904
6	5.76E+07	63	0.126	0.796
7	6.35E+07	83	0.166	0.67
8	6.93E+07	54	0.108	0.504
9	7.52E+07	47	0.094	0.396
10	8.11E+07	46	0.092	0.302
11	8.70E+07	38	0.076	0.21
12	9.29E+07	24	0.048	0.134
13	9.87E+07	24	0.048	0.086
14	1.05E+08	12	0.024	0.038
15	1.11E+08	7	0.014	0.014



② Homework make plots of pdf/cdf
 N_{pu}

pdf

set bins



tool useful $\rightarrow$: An easier way to quantify the effect of uncertainty instead of faster way using monte Carlo

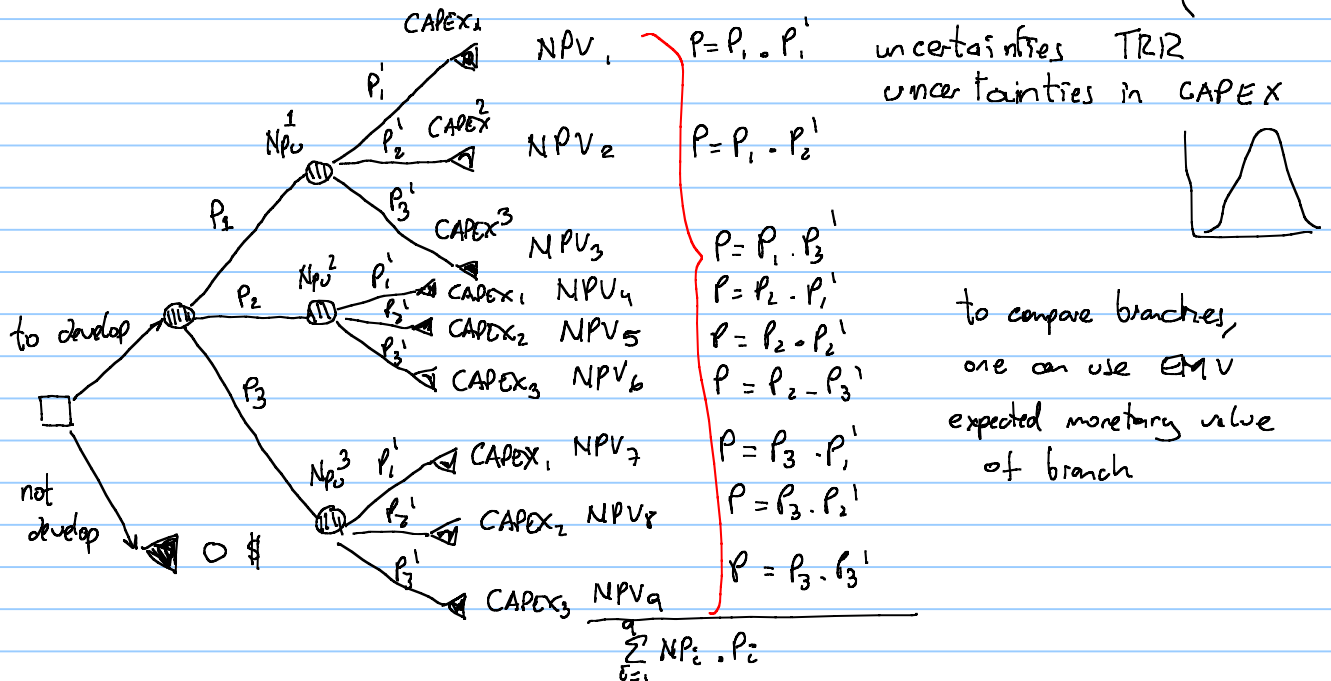
: to provide support when taking decision

Probability trees / decision trees

□ choice node
decision node

⊗ chance

◁ end node



class exercise

08_decision_Tree

xlsx

08_Decision_tree_exercise

docx

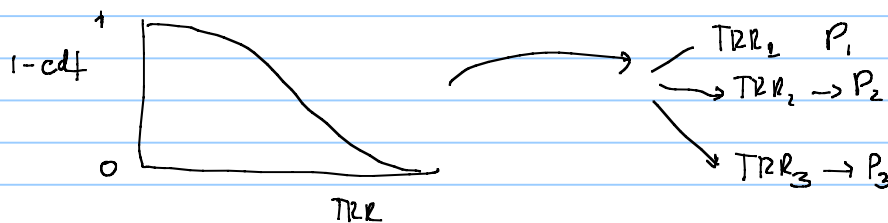
Your company is deciding whether to develop a reservoir or not in the Rovuma region. To help them take the decision, you have proposed to use a probability tree.

The value of the development can be estimated using the simplified equation:

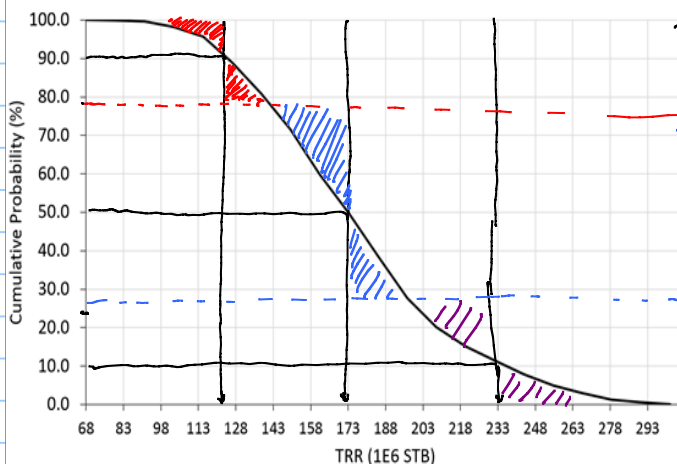
$$NPV = TRR \cdot 60 \cdot 0.4 - CAPEX.$$

- What is the mean expected value of the development? Is it worth to look further into developing this field?
- The capex values exhibit a normal probability distribution. However, it has already been discretized by a colleague:
 - CAPEX1: 0.7 E9 USD, P1: 0.3
 - CAPEX2: 1.1 E9 USD, P2: 0.4
 - CAPEX3: 1.5 E9, P3: 0.3.

how to discretize TRR



Expectation Curve for Total Recoverable Oil Reserves



$$P_{90} = 122 \text{ EOB stb}$$

$$P_{50} = 173 \text{ EOB stb}$$

$$P_{10} = 233 \text{ EOB stb}$$

$\left. \begin{array}{l} P_1 \\ P_2 \end{array} \right\}$

move the line until two red areas are same

from chart $P_1 = 0.2$

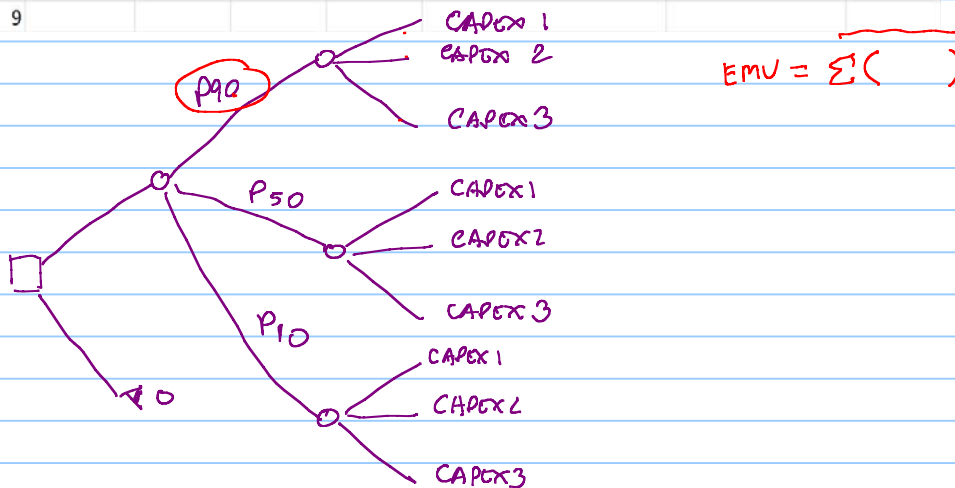
$$P_2 = 0.55$$

$$P_3 = 1 - 0.2 - 0.55 = 0.25$$

$$P_1 + P_2 + P_3 = 1$$

let's make the tree in excel

OPTION	TRR	P_TRR	CAPEX	P_capex	MV = TRR*60*0.4-CAPEX	P=P_capex*P_TRR	MV*P
[-]	[stb]	[-]	[USD]	[-]	[USD]	[-]	[USD]
1	P90	0.2	CAPEX1	0.3	NPV1	0.2 * 0.3	0.06
2	P90	0.2	CAPEX2	0.4	NPV2	0.2 * 0.4	0.08
3	P90	0.2	CAPEX3	0.3	NPV3	0.2 * 0.3	0.06
4							
5							
6							
7							
8							
9							



OPTION	TRR	P_TRR	CAPEX	P_capex	NPV = TRR*60*0.4-CAPEX	P=P_capex*P_TRR	MV*P
[-]	[stb]	[-]	[USD]	[-]	[USD]	[-]	[USD]
1	1.22E+08	0.2	7.00E+08	0.3	2.23E+09	0.06	1.34E+08
2	1.22E+08	0.2	1.10E+09	0.4	1.83E+09	0.08	1.46E+08
3	1.22E+08	0.2	1.50E+09	0.3	1.43E+09	0.06	8.57E+07
4	1.73E+08	0.55	7.00E+08	0.3	3.45E+09	0.165	5.70E+08
5	1.73E+08	0.55	1.10E+09	0.4	3.05E+09	0.22	6.71E+08
6	1.73E+08	0.55	1.50E+09	0.3	2.65E+09	0.165	4.38E+08
7	2.33E+08	0.25	7.00E+08	0.3	4.89E+09	0.075	3.67E+08
8	2.33E+08	0.25	1.10E+09	0.4	4.49E+09	0.1	4.49E+08
9	2.33E+08	0.25	1.50E+09	0.3	4.09E+09	0.075	3.07E+08
					EMV		3.17E+09

it is worth to develop the field !

③ Homework : do this exercise by yourselves