

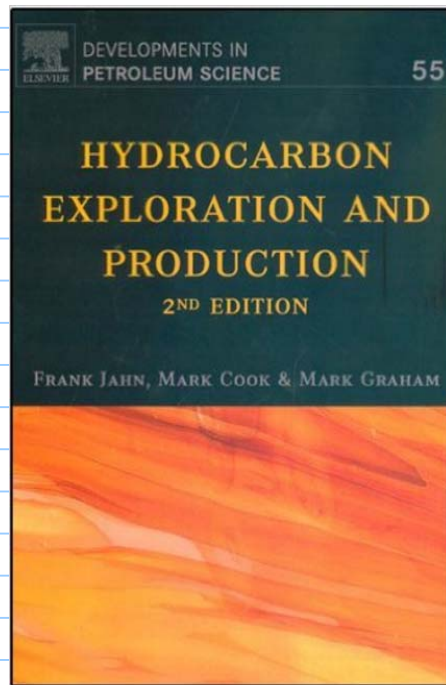
# ME683 - Field development and operations . Prof. Milan Stanko (NTNU)

• 3.12.2018 - 07.12.2018 09:00 → 14:00

• excel exercises

• evaluation { Prof. Liberato Hauke  
10% delivery of exercises  
2x15% mini test (2018, 2019)  
60% final exam (2019)

• Reference material:



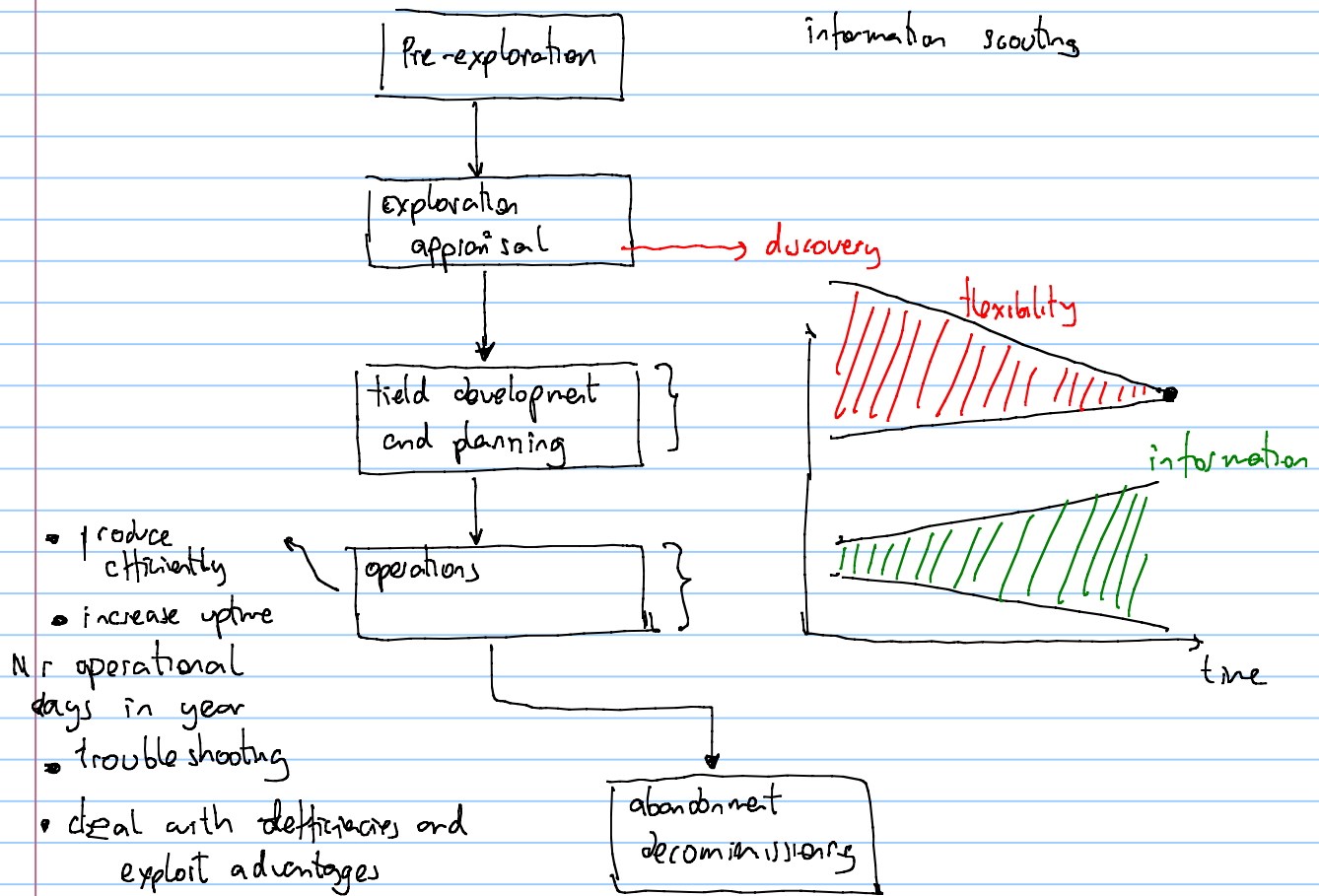
Frank Jahn, Mark Cook  
Mark Graham

• material from previous courses: <http://www.ipt.ntnu.no/~stanko/files/Courses/ME683>

<http://www.ipt.ntnu.no/~stanko/files/Courses/TPG4230>

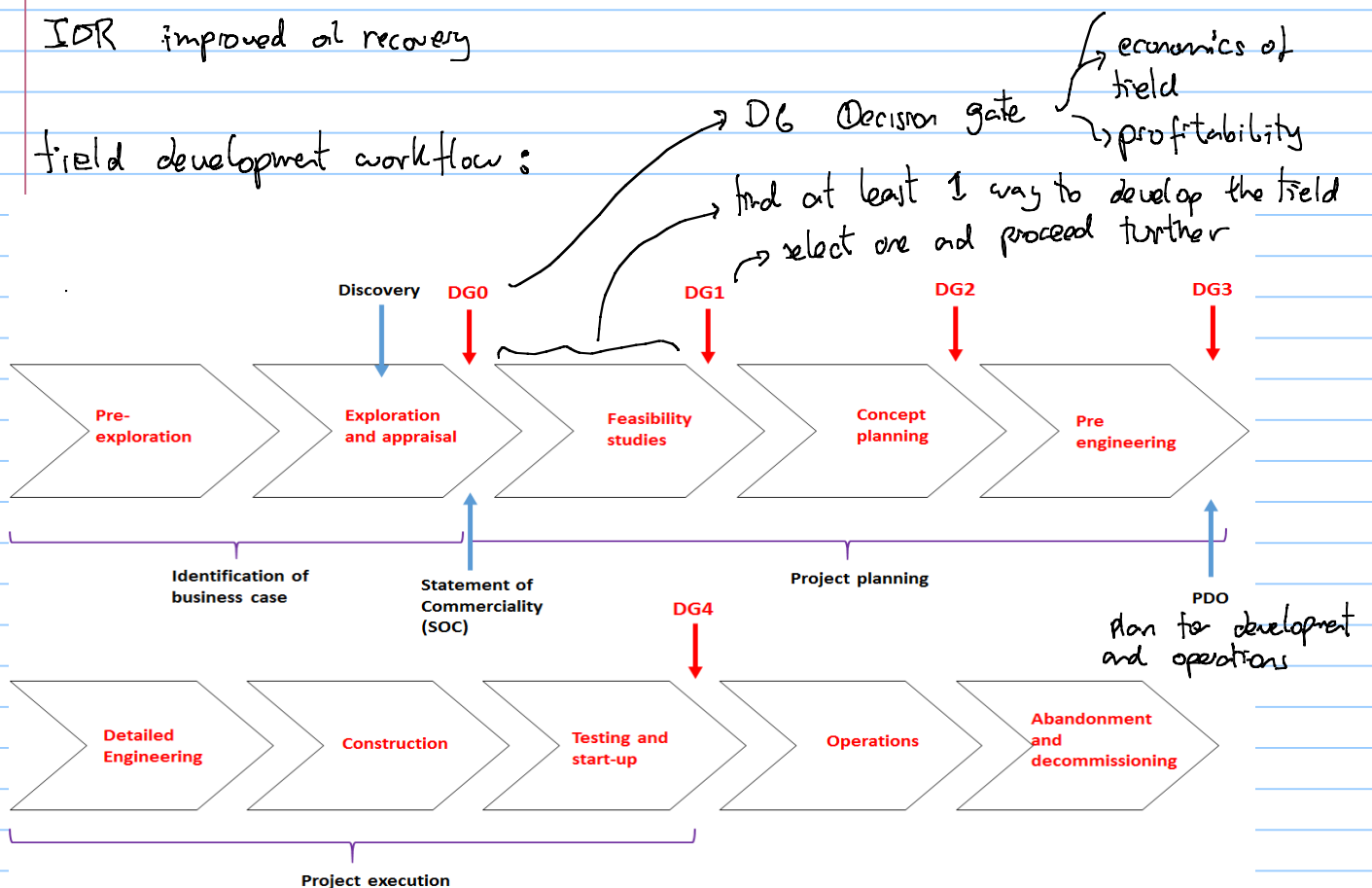
Milan's youtube channel → "playlist" → TPG4230 Field development and operations  
<https://www.youtube.com/channel/UCWMfsCe1NQMgx4UZWrVvFg> (2017)

# Life cycle of an oil/gas offshore field



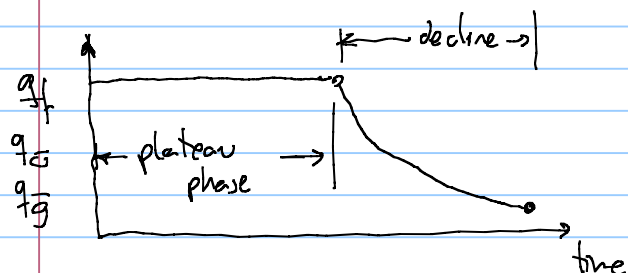
IOR improved oil recovery

field development workflow:

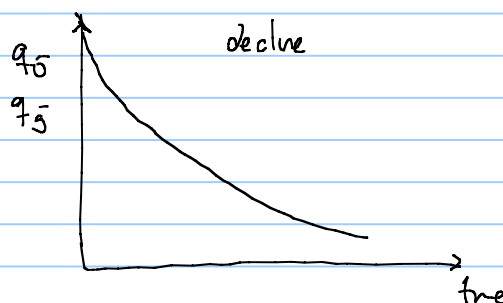


- Production scheduling: defining how much oil/gas will be produced with time from field

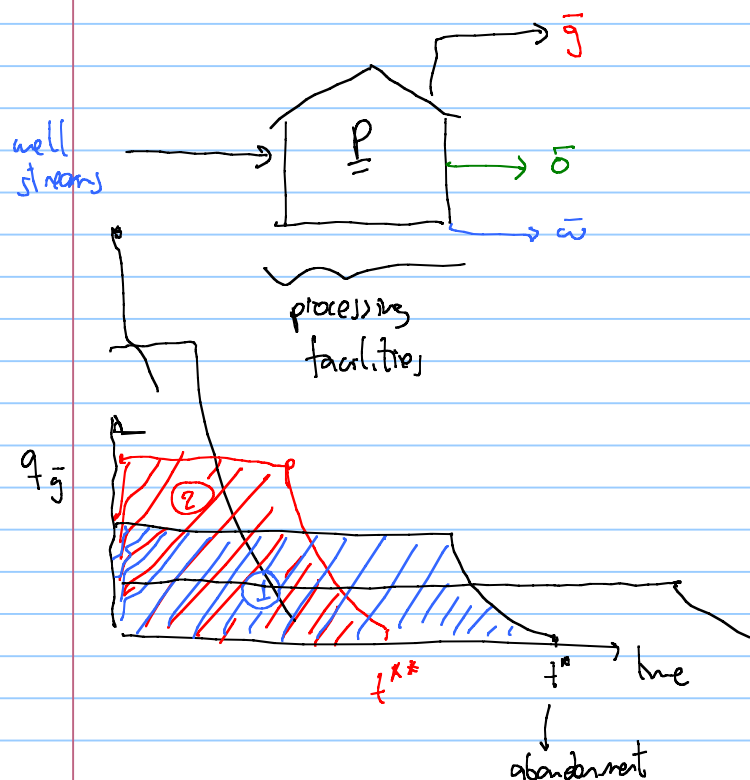
Production mode A (plateau)



Production mode B (potential)



$\bar{o}$  at standard conditions



cumulative production

$$G_p = \int_0^{t^*} q_g dt$$

according to SPE

Society of Petroleum engineers

initial oil in place (OOIP) — N oil surface volume  
G gas  
Q oil/gas

at abandonment  $G_p \rightarrow G_{pu}$   
ultimate

Mode A

- typically used for new standalone developments
- for medium-large recoverable size ( $\frac{N}{G}$ )
- find a balance between revenue ( $q_g \cdot p_g$ ) and cost!

if  $\uparrow q_g \rightarrow$  more revenue (early revenue)

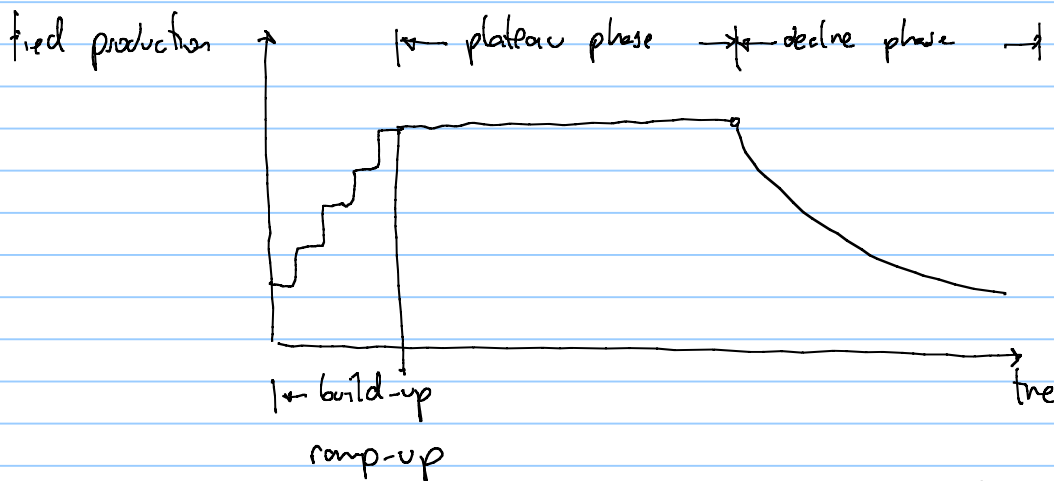
$\uparrow q_g \rightarrow$  more expensive facilities

- contracts for oil it is sold on market  
for gas it is typical to have contract { amount  $\rightarrow$   
period of time

Mode B

marginal

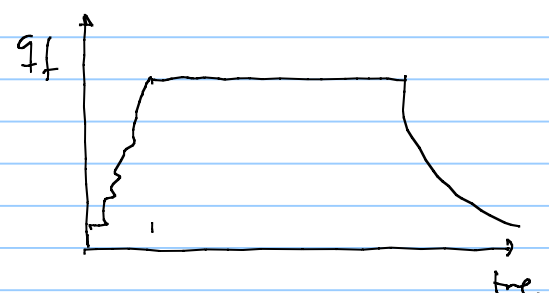
- typically used for small-medium size reservoirs that have an existing facility close by with spare capacity
- to produce as much as possible as quick as possible



land-based field

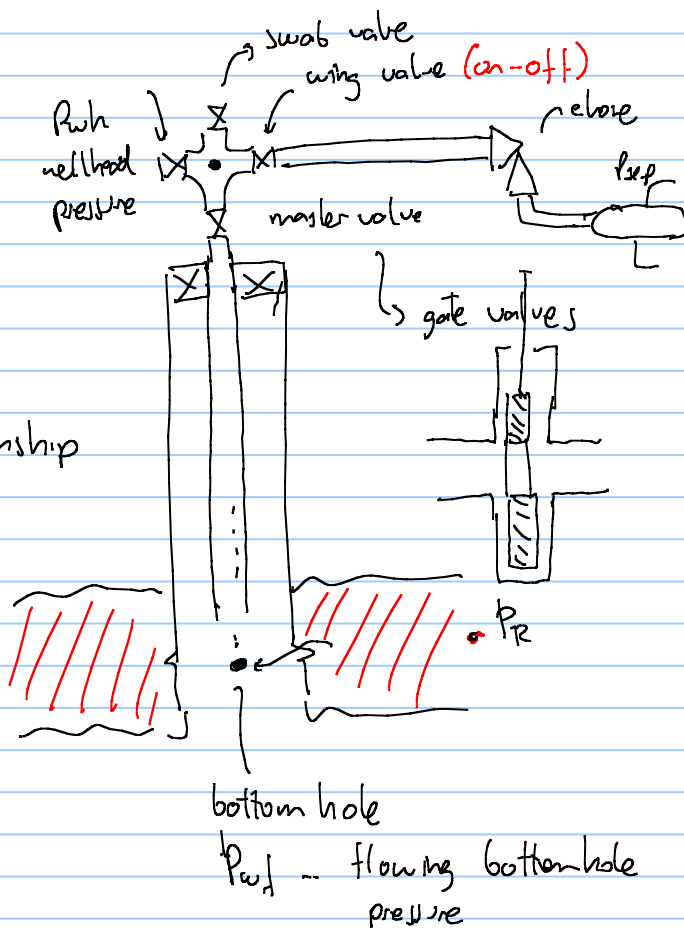
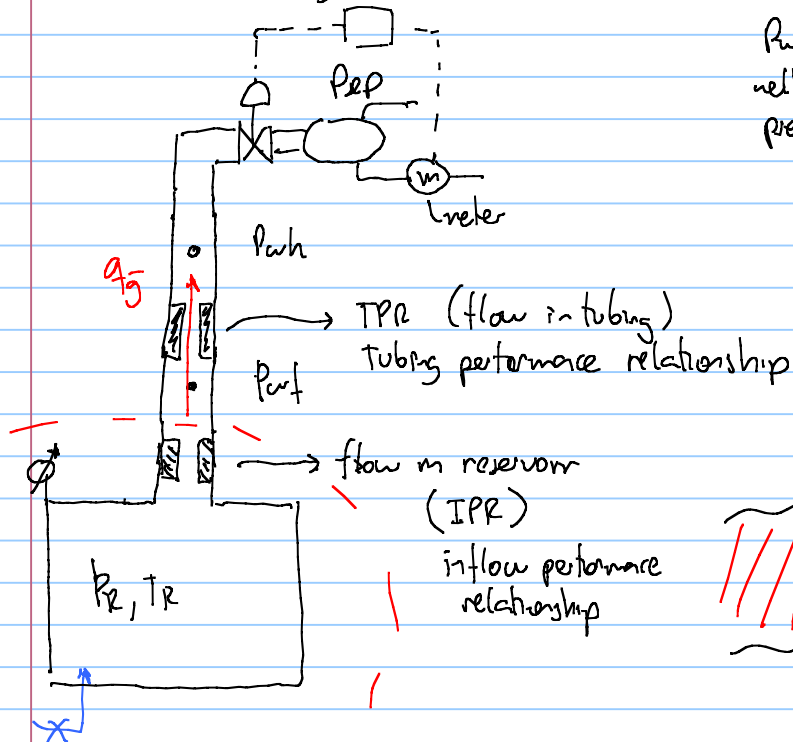


offshore fields





## Mechanical analog of a field

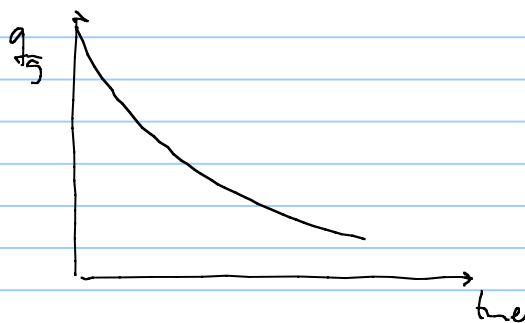
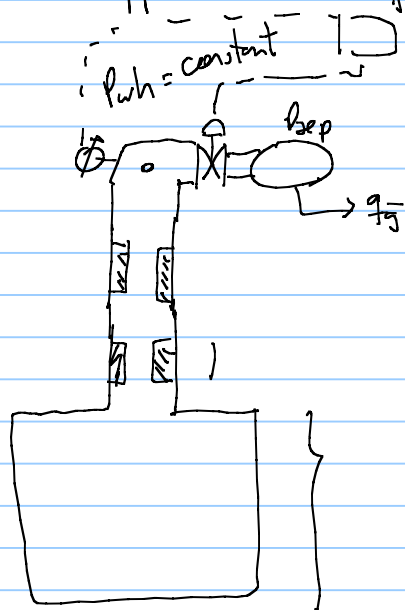


$$q_g = f(P_R, P_{sep}, \text{chose openings})$$

with the  $P_R - P_{sep}$  goes down ↓

if  $P_R - P_{sep}$  is high  $q_g \uparrow$ , therefore, i need to close!

what happens in case of node B (potential)



Rule of thumb to decide on plateau height (first estimate)

for oil fields 10% yearly outtake of TRR (total recoverable reserves)

$$q_{\text{plateau}} = \frac{0.1 \cdot N_{\text{pv}}}{\underbrace{N_{\text{days/year}}}_{\text{uptime}}} = \frac{N_{\text{day}}}{365}$$

Goliat oil field  $N_{\text{pv}} = 180 \text{ E}6 \text{ stb}$

$q_{\text{plateau}}?$

$$q_{\text{plateau}} = \frac{0.1 \cdot 180 \text{ E}6 \text{ stb}}{328.5} \approx 55000 \text{ stb/d}$$

$$90\% \text{ uptime} = N_{\text{day}} = 0.9 \cdot 365 = 328.5$$

for gas field

annual oftake 2-5% of TRR

$$q_{\text{g-plateau}} = \frac{G_{\text{pv}} \cdot (0.02 - 0.05)}{\underbrace{N_{\text{day/year}}}_{\text{operational}}}$$

for Block 2 offshore Tanzania

$$G = 311 \text{ E}9 \text{ Sm}^3$$

$$RF = 0.7$$

$$G_{\text{pv}} = 217.7 \text{ E}9 \text{ Sm}^3$$

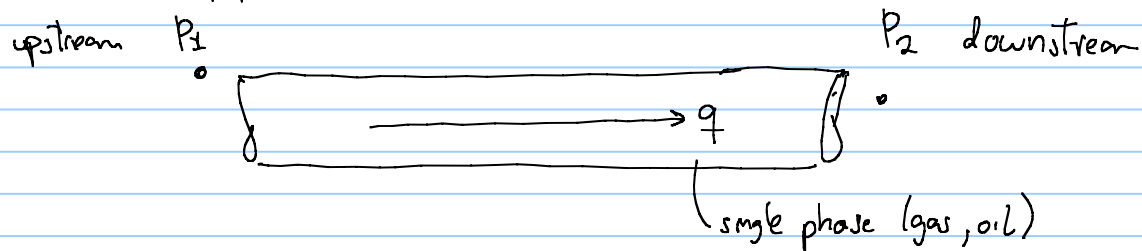
recovery factor  $RF = \frac{G_{\text{pv}}}{G}$

$$q_{\text{g-plateau}} = \frac{217.7 \text{ E}9 \cdot (0.025)}{328.5}$$

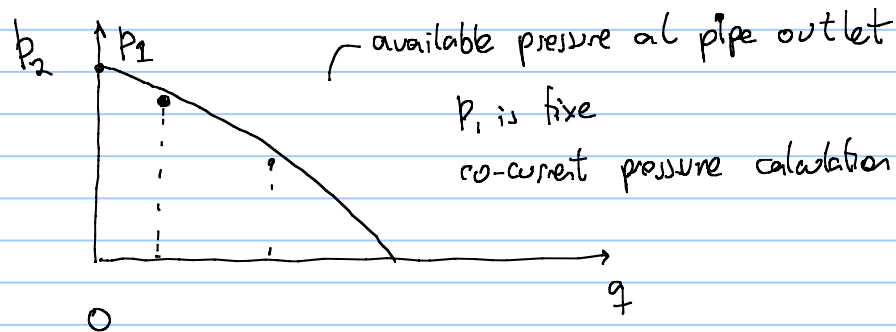
$$q_{\text{g-plateau}} = 16.6 \text{ E}6 \text{ Sm}^3/\text{d}$$

# flow equilibrium (Nodal analysis, inflow-outflow analysis)

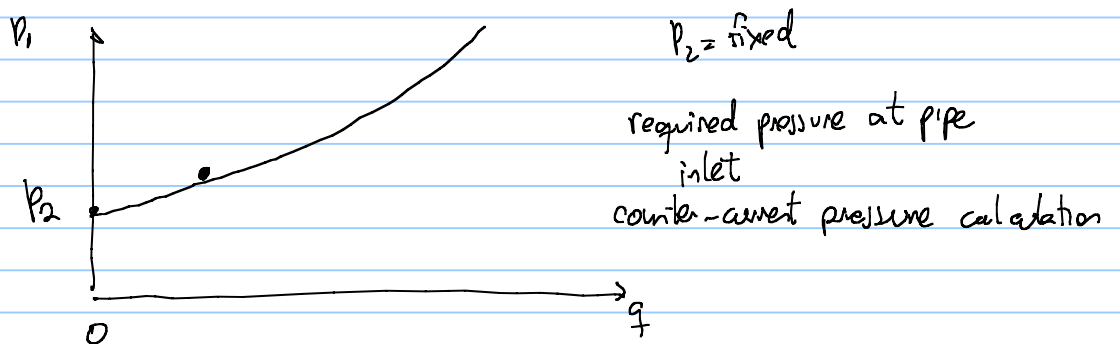
- Horizontal pipe



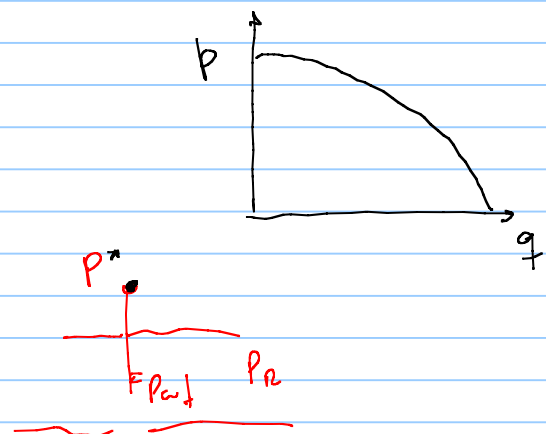
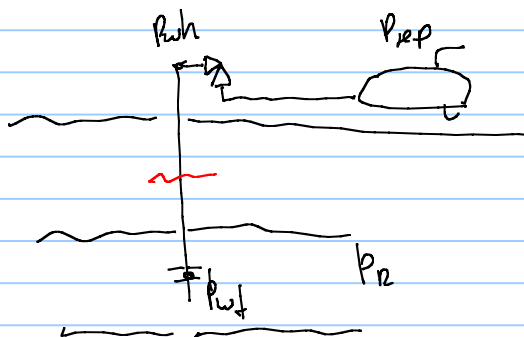
- keep  $P_1$  fixed, change  $q$ , what happens with  $P_2$ ?

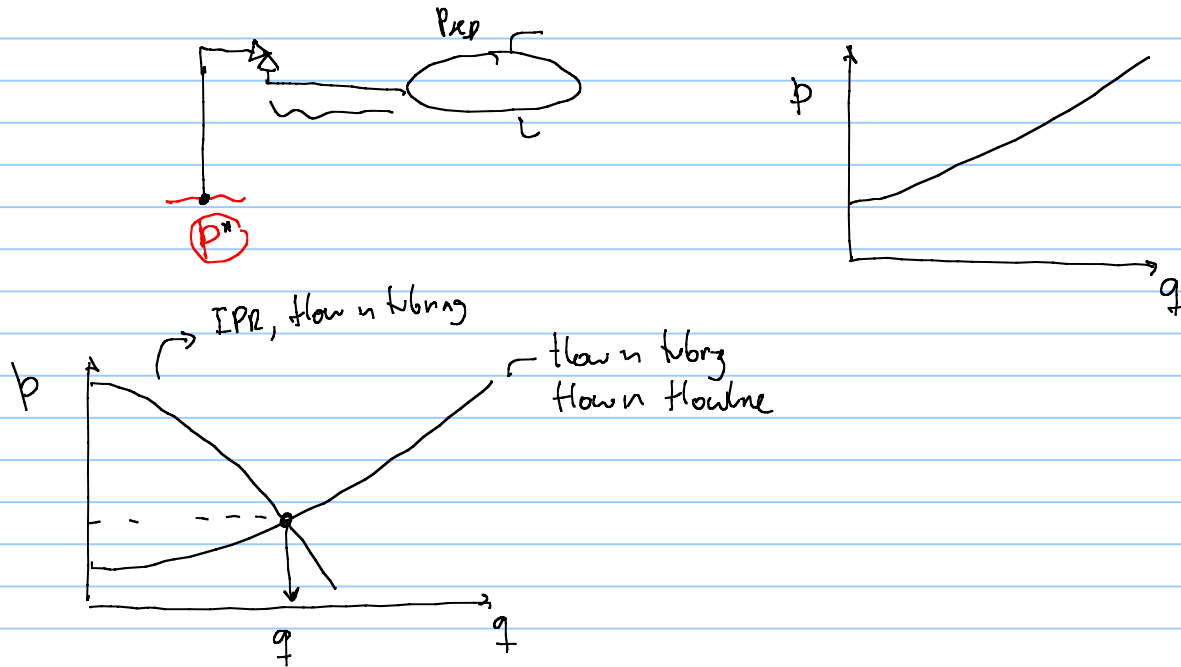


- keep  $P_2$  fixed, change  $q$ , what happens with  $P_1$ ?

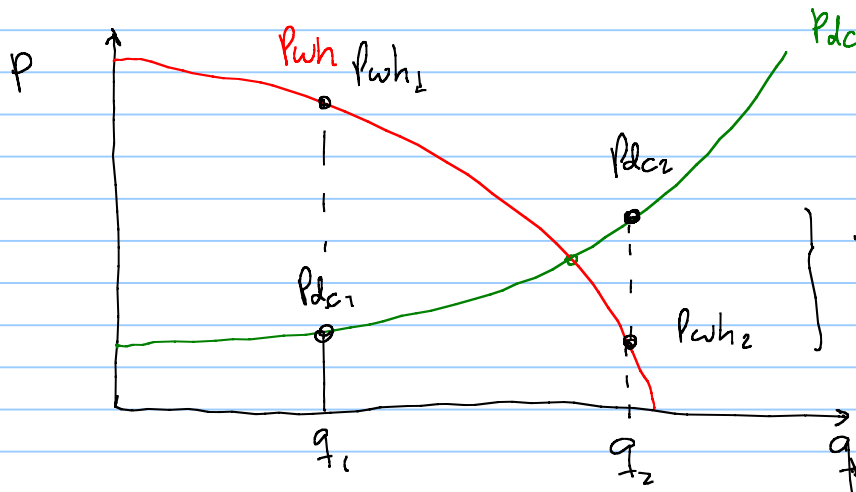
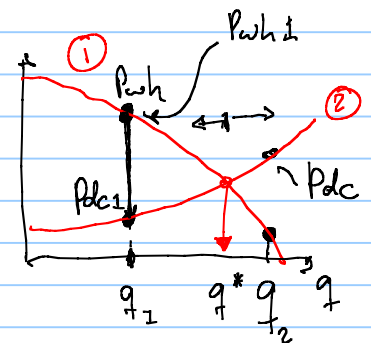
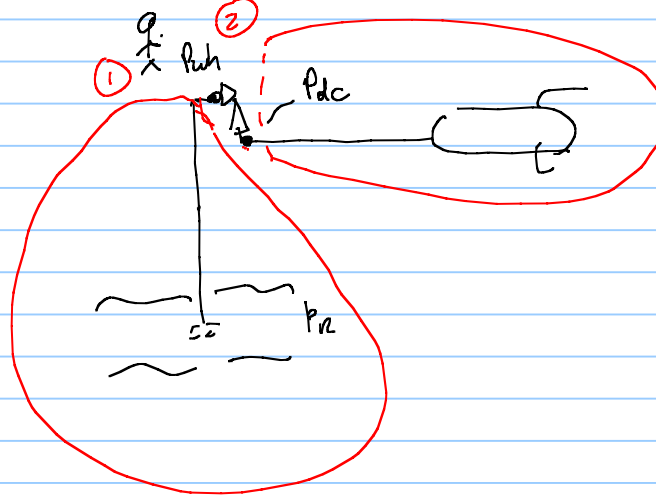


- provide  $P_1, P_2$ , calculate  $q$





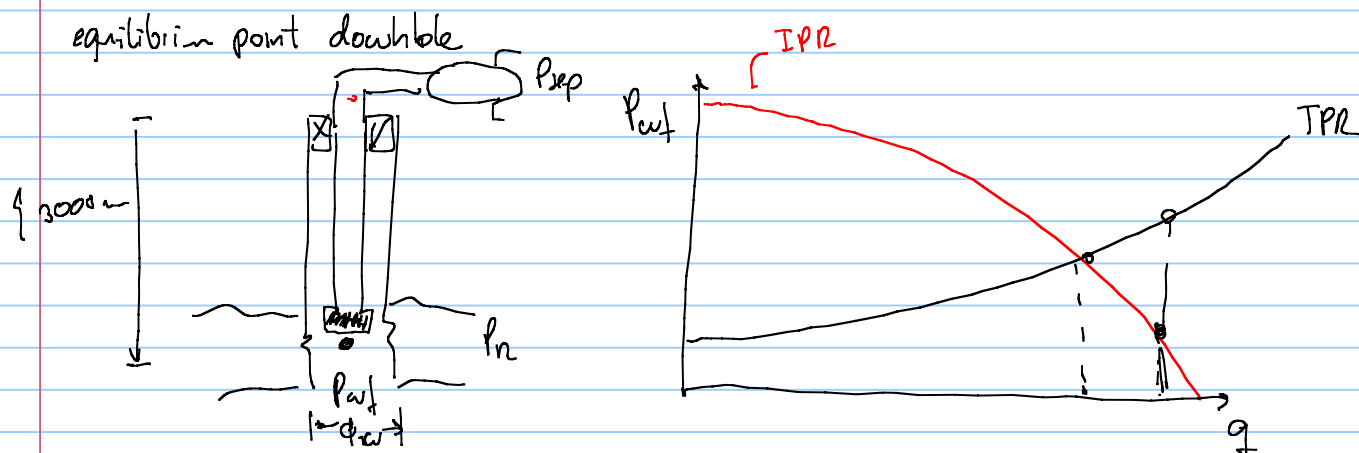
changing equilibrium point @ wellhead



give energy to fluid  
(liquid  $\rightarrow$  pump  
gas  $\rightarrow$  compressor)

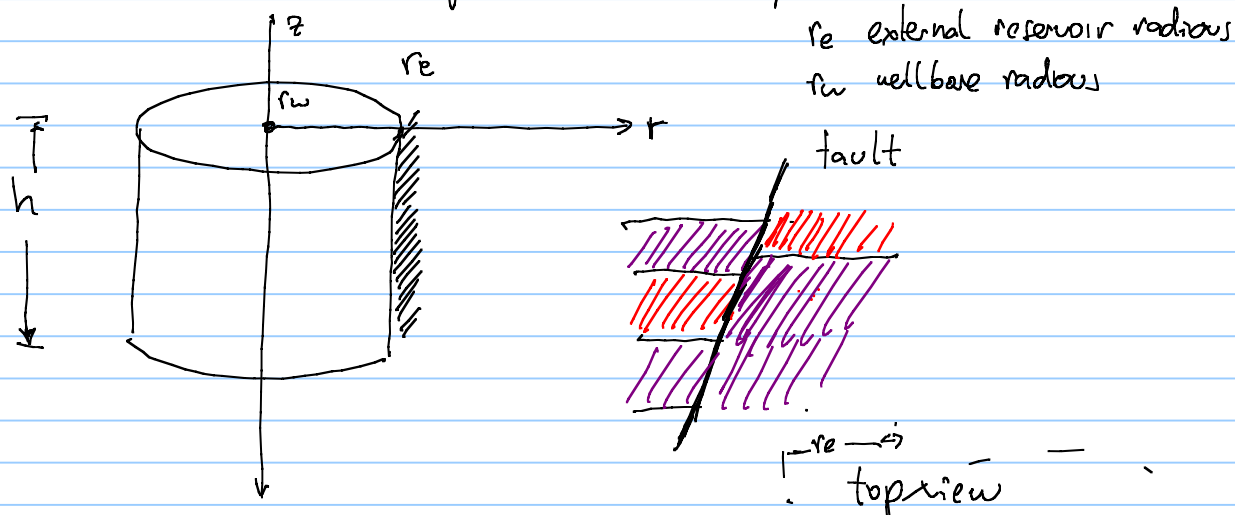
equilibrium point @ wellhead  $\rightarrow$  choke design

$\rightarrow$  topside / surface compression

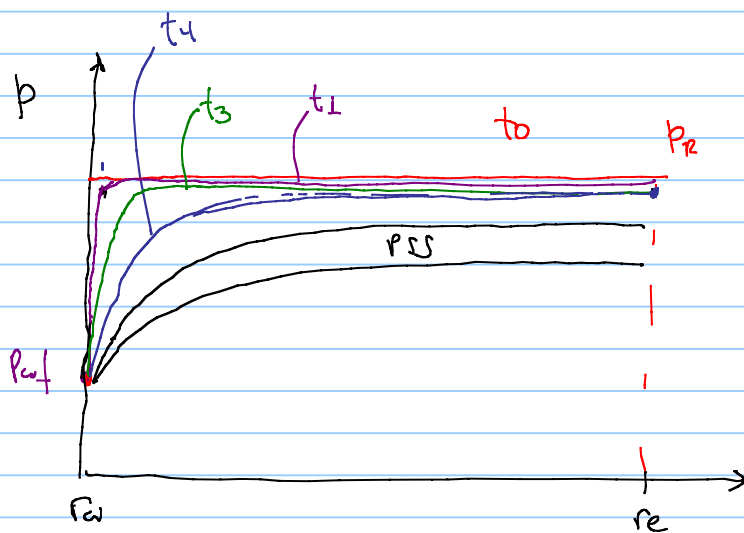


- downhole pump (ESP electric submersible pump)
- downhole choke (not very common)

- flow in formation (Inflow performance relationship)



assume initially no production,  $p_r$ ,  $t_0$



@  $t_4$  pressure change reaches the boundary  $r_e$

flow regimes in wellbore  
 $t_0 \rightarrow t_4$   
 infinite acting (transient)

from  $t_y$  and forward  $\rightarrow$  steady state (if  $P_e$  is kept constant) SS  
 pseudo steady state (PSS) if  $P_e$  changes with time  
 if no flow at boundary

for wells with medium to high permeability and  $\rightarrow$  1 darcy

transient is short  $\rightarrow$  hrs  $\rightarrow$  days

in that case most of production happens at PSS or SS

then we use IPR for PSS, SS

$$IPR = f(P_R, P_{wf}, \text{reservoir properties})$$

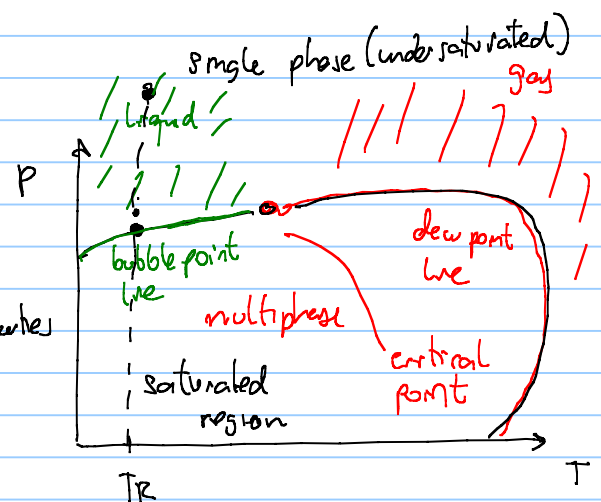
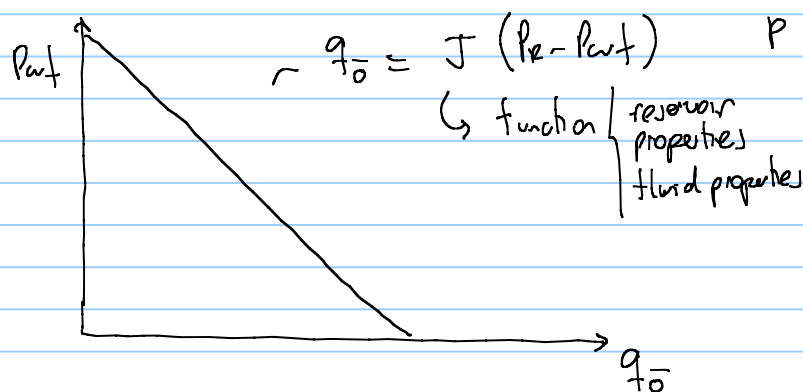
$$IPR \neq f(t)$$

if significant part of production happens when is transient then

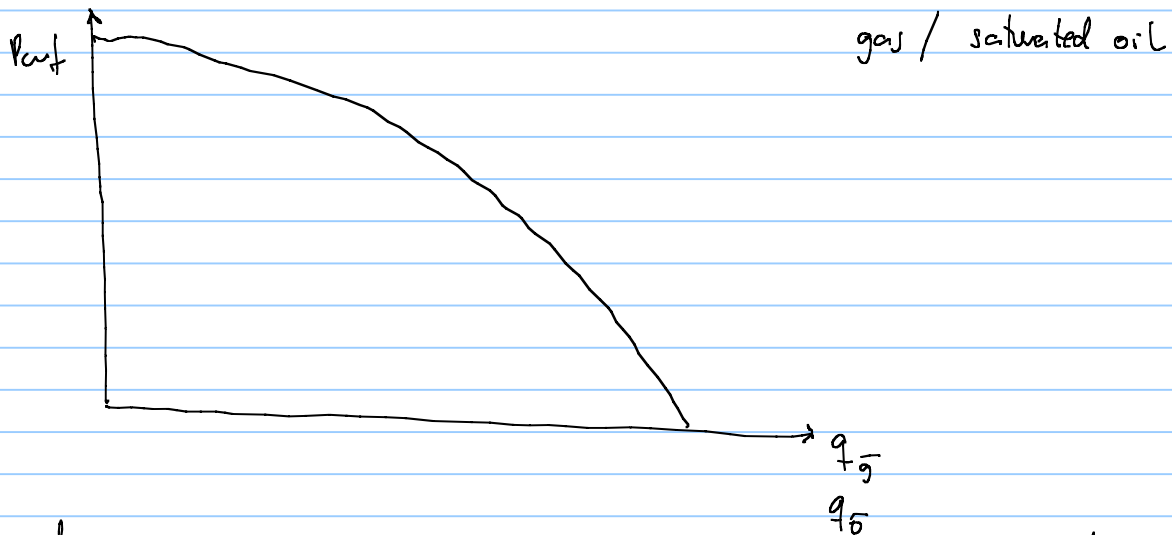
$$IPR = f(t)$$

In this course we will assume PSS

IPR equation



only oil (undersaturated oil)  $P_{wf} \geq P_b(T_R)$



for dry gas } back pressure equation

$$q_g = C_R (P_R^2 - P_{wf}^2)^{\frac{1}{n}}$$

back pressure coefficient      empirical equation

back pressure exponent

$0.5 \leq n \leq 1$

↓      → Darcy flow (laminar flow)

turbulent flow

• for saturated oil  $P_{wf} < P_b(T_R)$

Vogel

$$\frac{q_g}{q_{gmax}} = 1 - 0.2 \frac{P_{wf}}{P_R} - \frac{P_{wf}^2}{P_R^2}$$

flow in tubing (A.K.A. the tubing equation for dry gas)

$$P V = n R T$$

$$n = \frac{P_o}{M_w}$$

# Tubing flow Equation-Dry gas

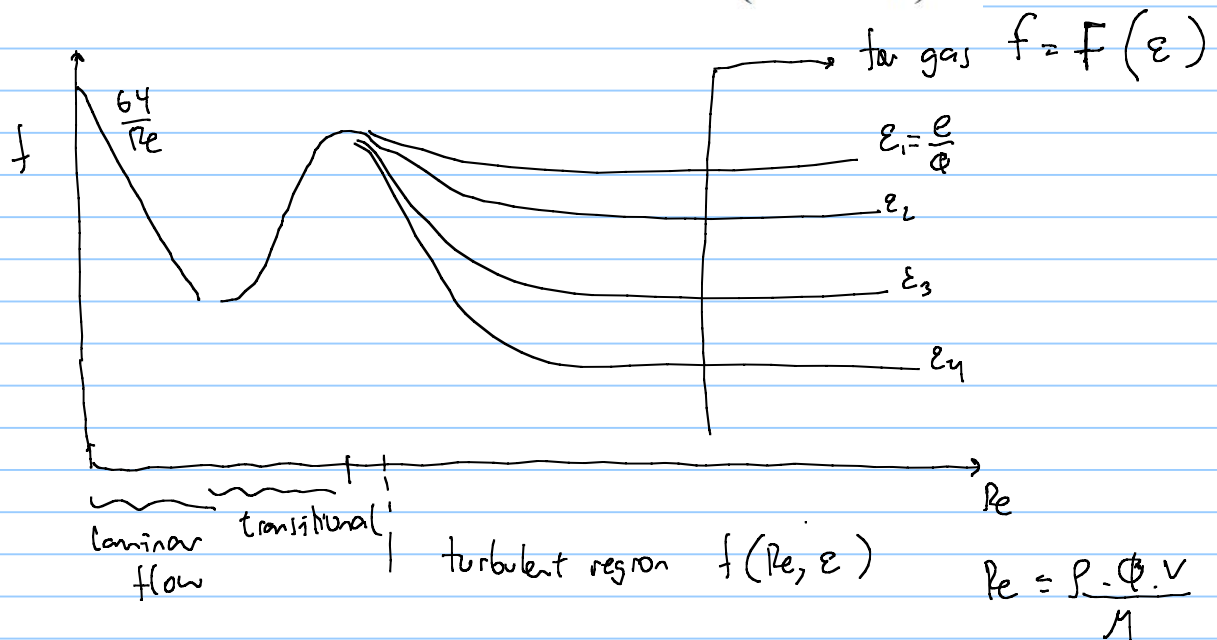
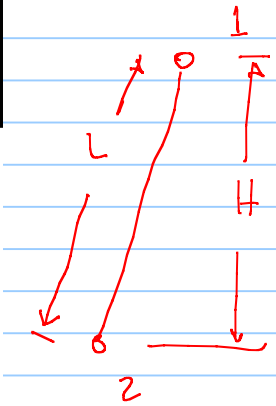
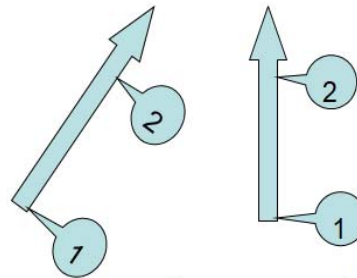
$$q_{sc} = \left( \frac{\pi}{4} \right) \left( \frac{R}{M_{air}} \right)^{0.5} \left( \frac{T_{SC}}{P_{SC}} \right) \left[ \frac{D^5}{\gamma_g f_M Z_{av} T_{av} L} \right]^{0.5} \left( \frac{s e^s}{e^s - 1} \right)^{0.5} \left( \frac{p_1^2}{e^s} - p_2^2 \right)^{0.5}$$

$$\frac{s}{2} = \frac{M_g g}{Z_{av} R T_{av}} H = \frac{(28.97) \gamma_g g}{Z_{av} R T_{av}} H$$

$$q_{gsc} = C_T \left( \frac{p_1^2}{e^s} - p_2^2 \right)^{0.5}$$

$$p_{inlet} = p_1 = e^{s/2} \left( p_2^2 + \frac{q_g^2}{C_T^2} \right)^{0.5}$$

$$p_{wh} = p_2 = \left( \frac{p_1^2}{e^s} - \frac{q_g^2}{C_T^2} \right)^{0.5}$$



$$f_M = \frac{0.01748}{D^{0.224} \left[ \left| \frac{39.37 \text{ inch}}{1 \text{ m}} \right| \right]^{0.224}} = \frac{0.0077}{D^{0.224}}$$

Smith (1950)

$\bar{\epsilon}$  depend mainly on  $\phi$

$$f = F(\phi)$$

$$q_g = C_T \left( \frac{p_1^2}{e^s} - p_2^2 \right)^{0.5}$$

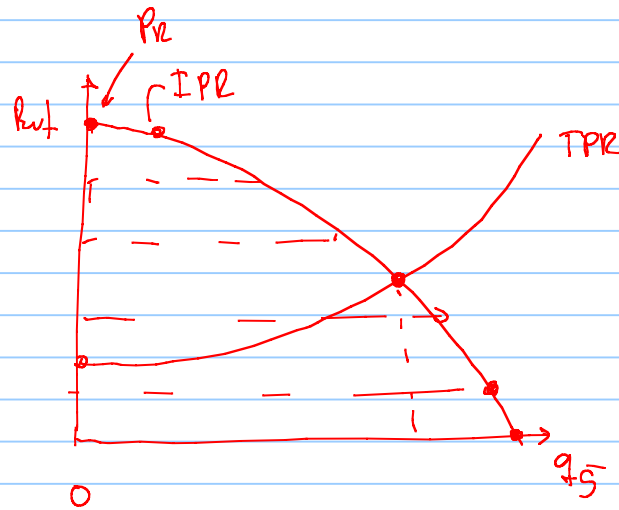
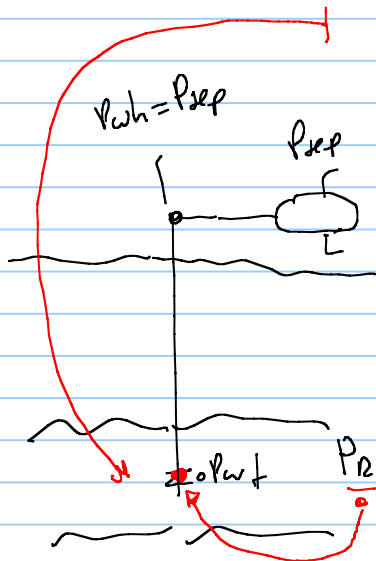
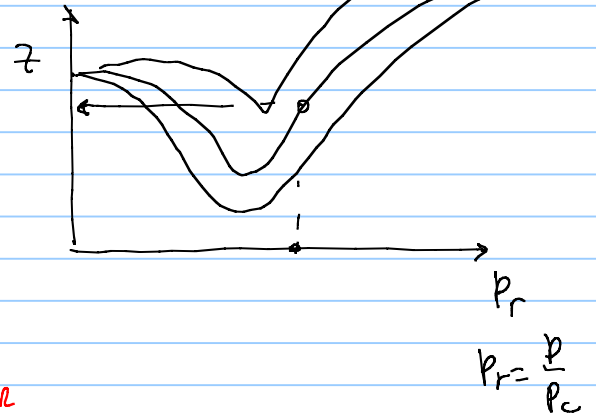
$$p_1 = 200 \text{ bara} \quad p_2 = 80 \text{ bara}$$



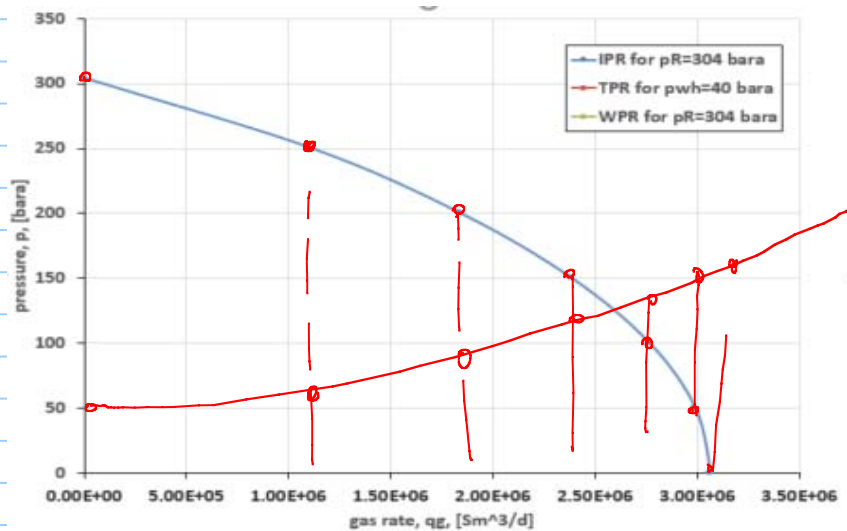
flow equilibrium of single gas well

 $z$ 

$$pV = zRT$$

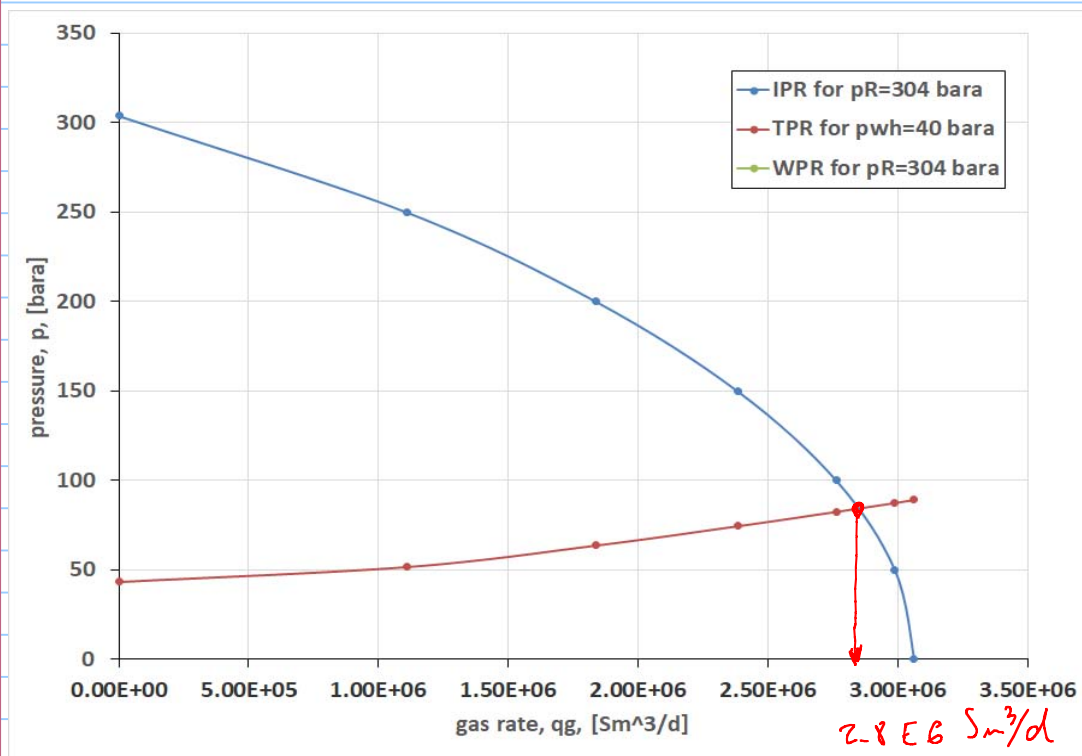


| pwf_avail<br>[bara] | IPR<br>qg<br>[Sm <sup>3</sup> /d] |
|---------------------|-----------------------------------|
| 304                 | 0.00E+00                          |
| 250                 | 1.11E+06                          |
| 200                 | 1.84E+06                          |
| 150                 | 2.38E+06                          |
| 100                 | 2.76E+06                          |
| 50                  | 2.99E+06                          |
| 0                   | 3.06E+06                          |



$$q_g = C_T \left( \frac{p_1^2}{e^s} - p_2^2 \right)^{0.5}$$

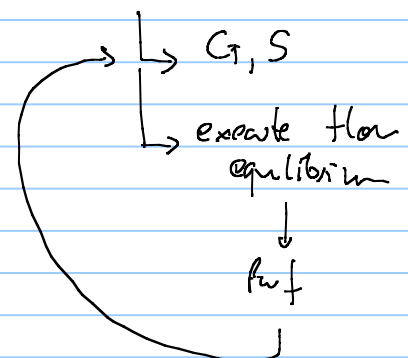
$$q_g = C_T \left( \frac{p_{wf}^2}{e^s} - p_{wh}^2 \right)^{0.5}$$



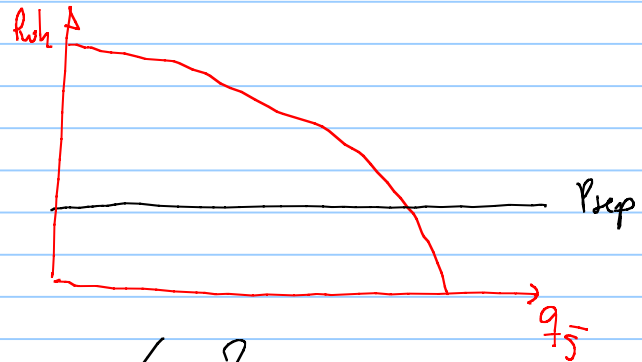
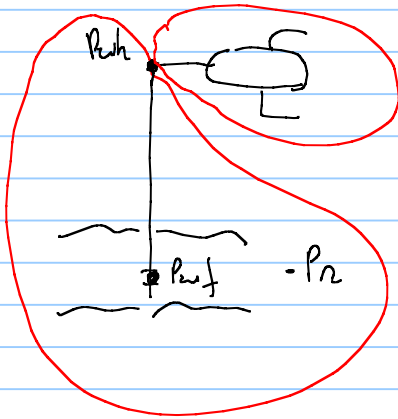
|              |           | IPR                  | TPR     |                   |
|--------------|-----------|----------------------|---------|-------------------|
|              | pwf_avail | qg                   | pwf_req | pwf_avail-pwf_req |
|              | [bara]    | [Sm <sup>3</sup> /d] | [bara]  | [bara]            |
|              | 304       | 0.00E+00             | 43.2    | 260.8             |
|              | 250       | 1.11E+06             | 51.6    | 198.4             |
|              | 200       | 1.84E+06             | 63.7    | 136.3             |
|              | 150       | 2.38E+06             | 74.4    | 75.6              |
|              | 100       | 2.76E+06             | 82.5    | 17.5              |
|              | 50        | 2.99E+06             | 87.4    | -37.4             |
|              | 0         | 3.06E+06             | 89.1    | -89.1             |
| intersection | 84.4      | 2.85E+06             | 84.4    | 0.0               |

to get a better approximation of  $C_{T,S}$

assuming  $p_{wf} = p_R$

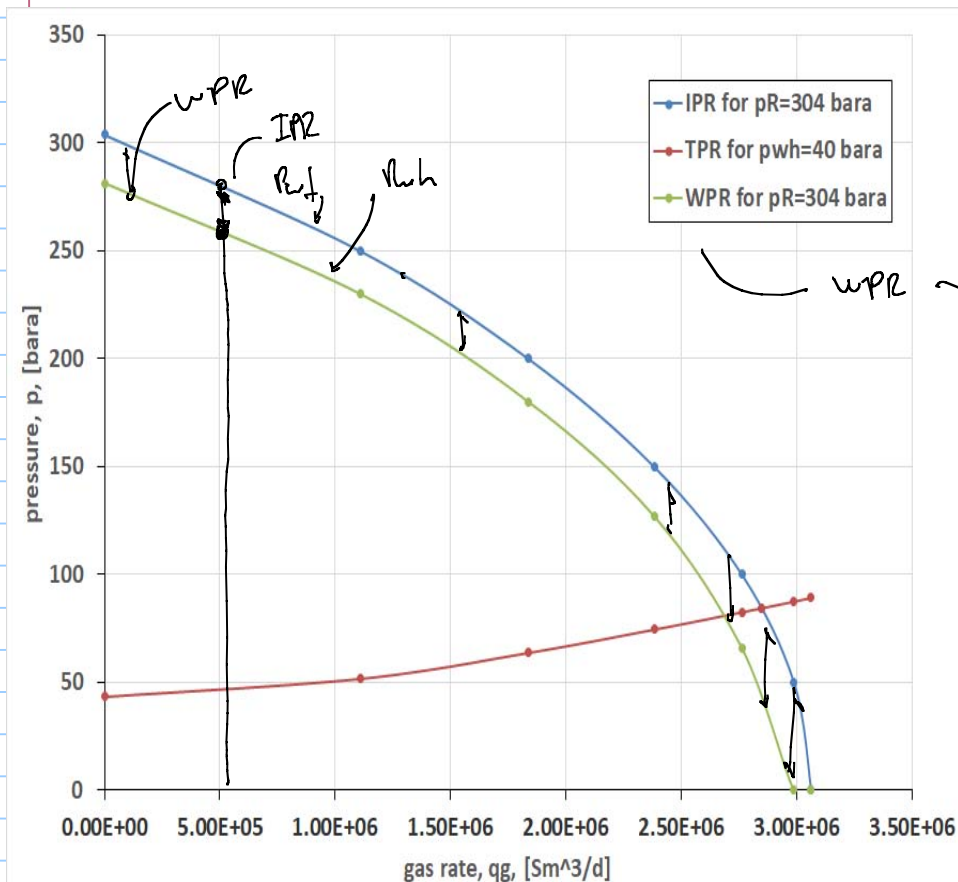


flow equilibrium at well head

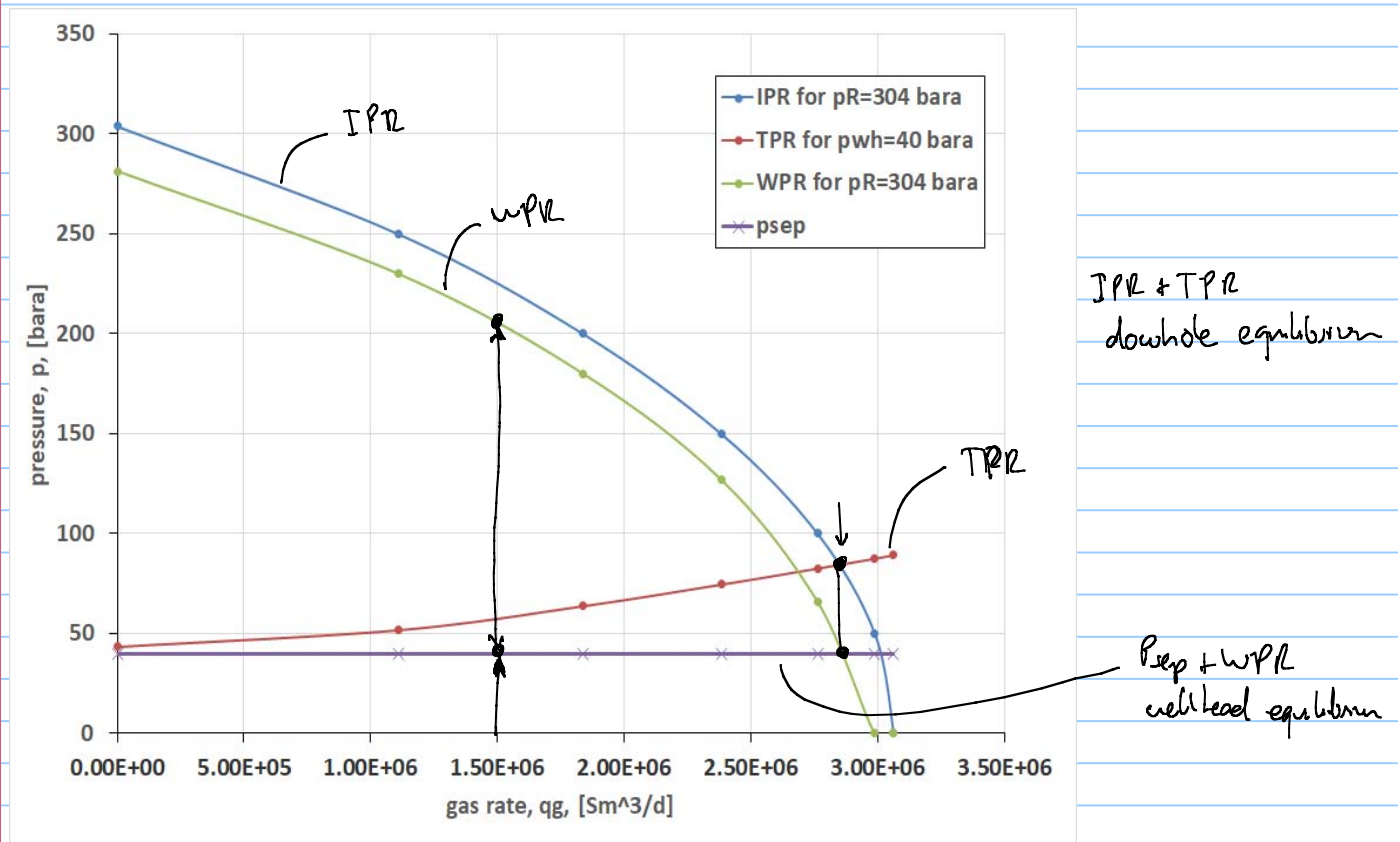


$$q_g \propto C_T \left( \frac{p_{wf}^2}{e^s} - p_{wh}^2 \right)^{0.5}$$

$$p_{wh} = \left( \frac{p_{wf}^2}{e^s} - \left( \frac{q_g}{C_T} \right)^2 \right)^{0.5}$$

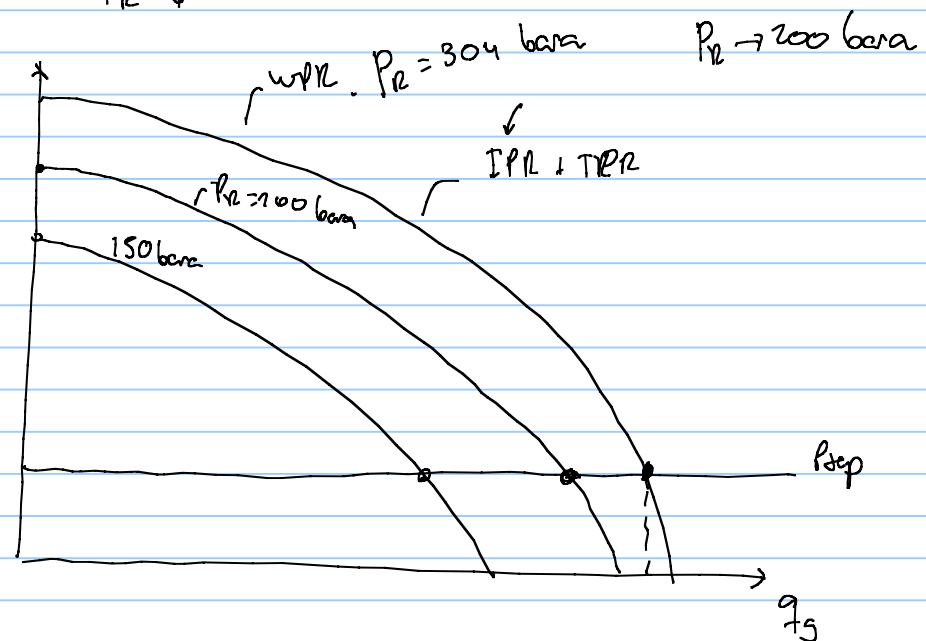


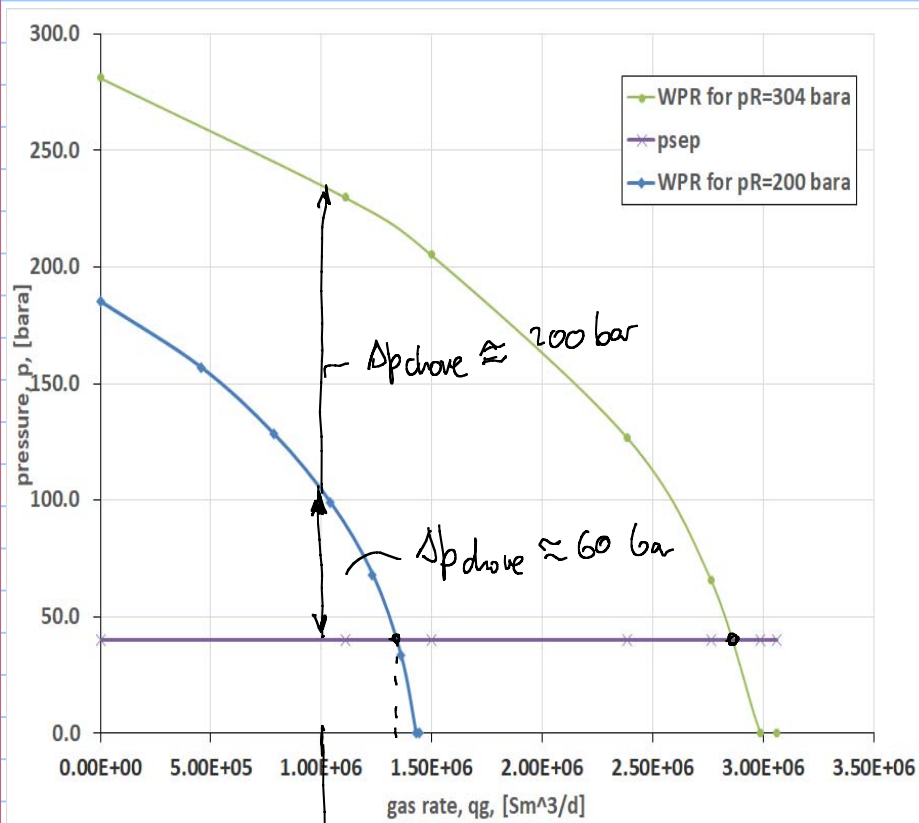
WPR  $\rightarrow$  well head performance relationship



to deliver a rate of  $1.5 \times 10^6$  Sm<sup>3</sup>/d I need to apply chocking at wellhead for 165.2 bar  $\Delta p$

• effect of depletion  $p_R \downarrow$





$1.0 \times 10^6$  Sm<sup>3</sup>/d

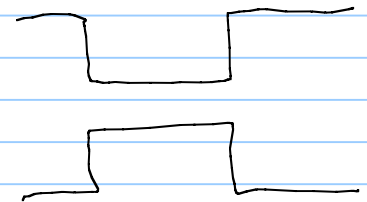
②  $P_R = 304$  bara

$q_g = 2.85 \times 10^6$  Sm<sup>3</sup>/d

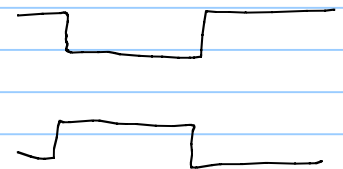
③  $P_R = 200$  bara

$q_g = 1.35 \times 10^6$  Sm<sup>3</sup>/d

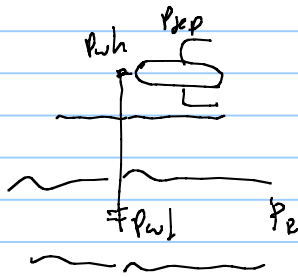
when  $P_R = 304$  bara



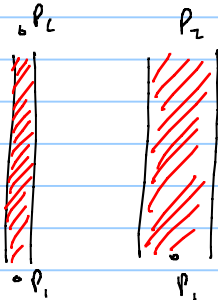
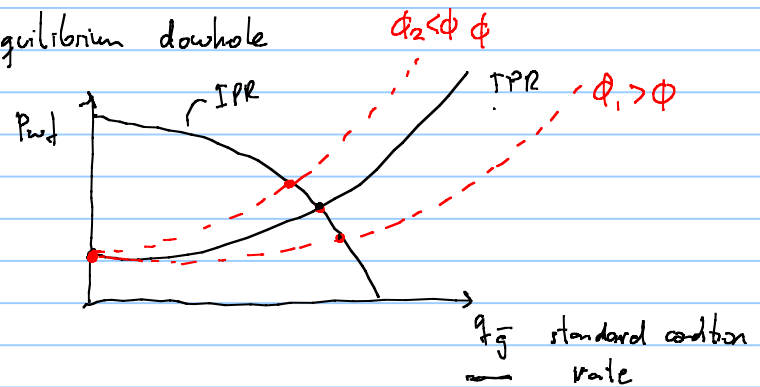
when  $P_R = 200$  bara



Day 2

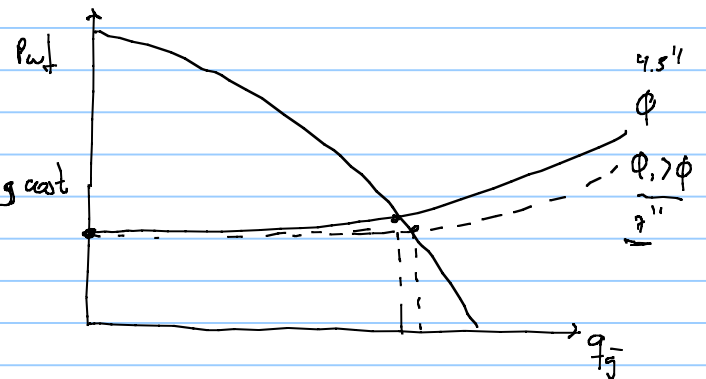


flow equilibrium downhole

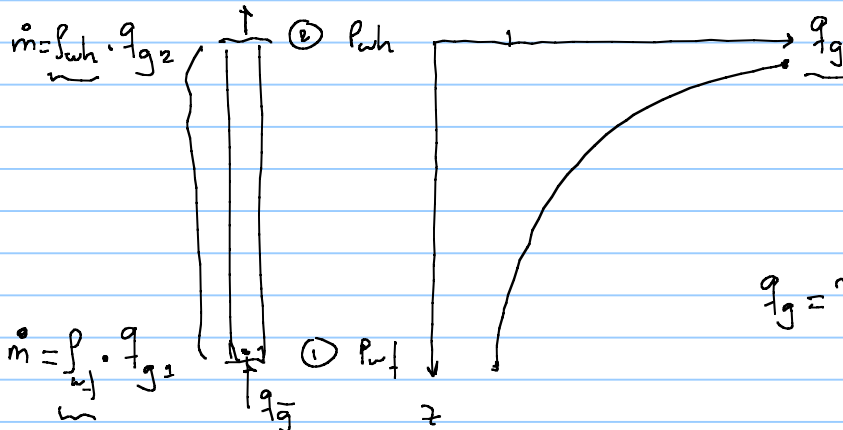
variation of tubing size " $\phi$ "How to choose  $\phi$  tubing

- minimize tubing  $\Delta p \rightarrow$  max rate

- minimize tubing cost



- avoid erosion



$$\rho \bar{V} = zRT$$

$$\rho \frac{1}{\rho} = \frac{zRT}{\rho}$$

$$\frac{\rho'}{zRT} = \rho'$$

$$q_g = v_g \cdot A$$



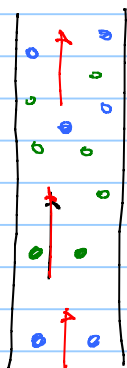
$$p_{wf} > p_{wh} \rightarrow q_{g1} < q_{g2}$$

- Select  $\phi$  such that we don't get erosion in tubing

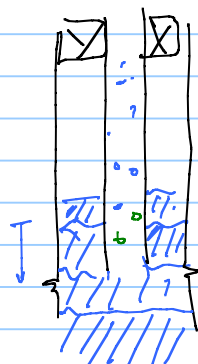
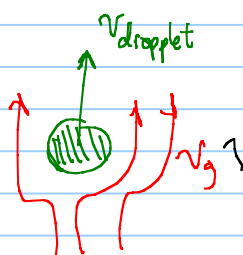
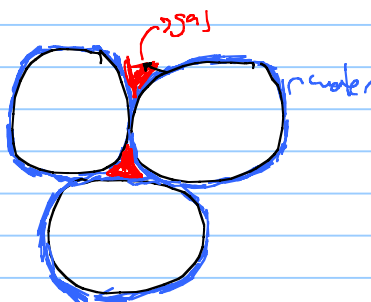
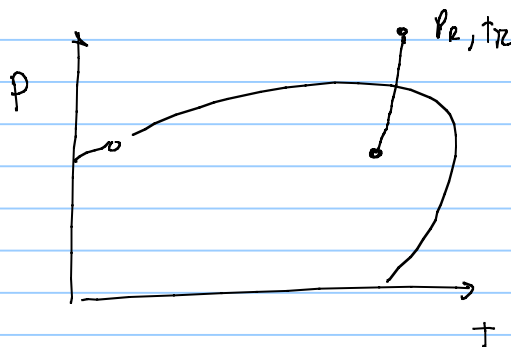
$$v_{g@wh} < v_{erosion} \rightarrow \text{API 14E}$$

American petroleum institute

# • liquid loading

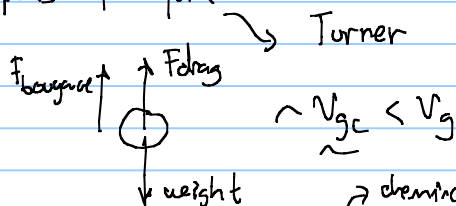


→ condensate  
→ water in solution dissolved in the gas



liquid loading → accumulation of liquid in wellbore  
→ additional backpressure against formation which brings  $q_g \downarrow$

Select  $\phi$  of tubing such that  $v_g$  is high enough to lift droplets of liquid



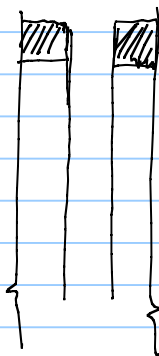
Turner

$$\sim v_{gc} < v_g$$

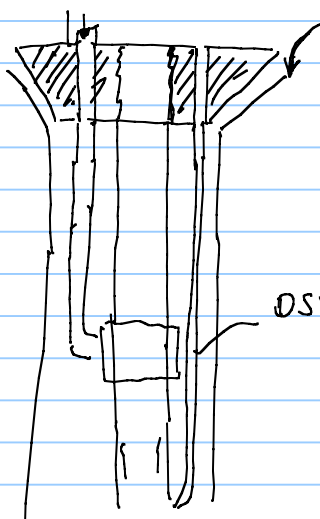
$F_{buoyant}$  ↑  
 $F_{drag}$  ↑  
weight ↓

chemical injection (scale inhibitor)  
downhole pressure gauge  
power cable  
landing shoulder

# • tubing hanger

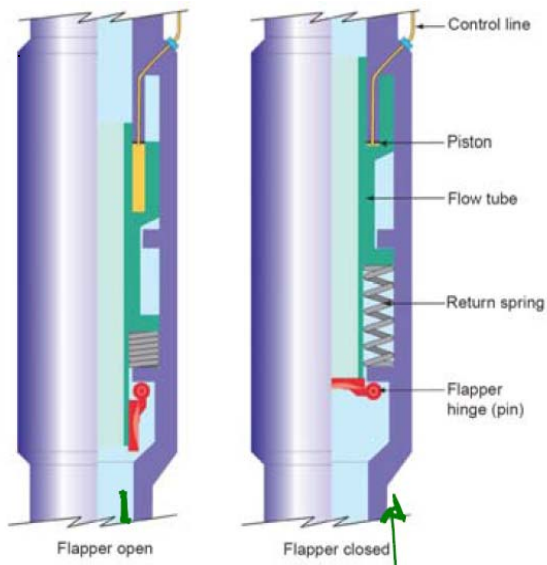


$\phi$  of the tubing has to be small enough to allow tubing hanger integrity

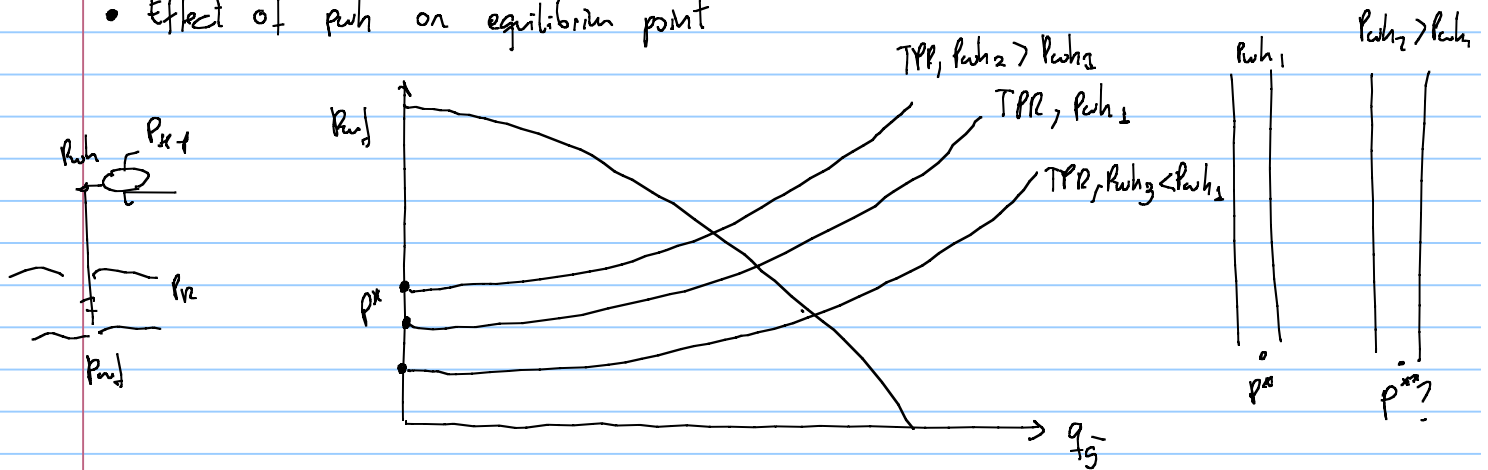


DSV downhole safety valve  
100m - 200m below wellhead

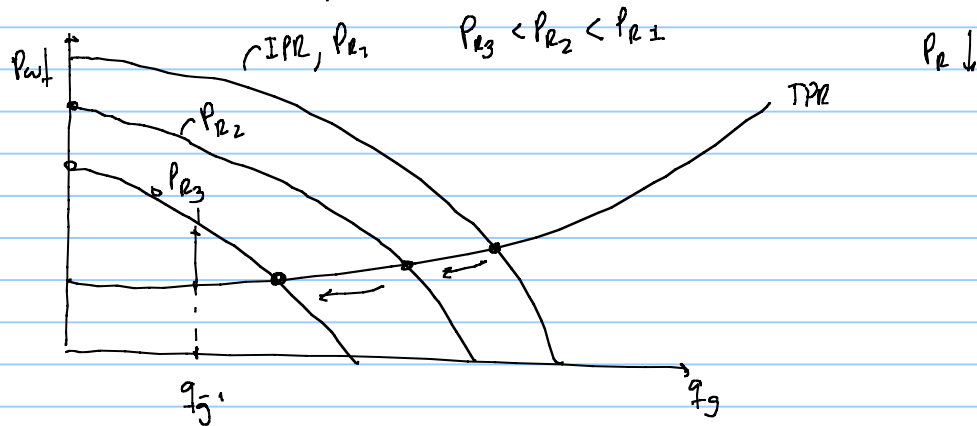




- Effect of  $p_{wh}$  on equilibrium point



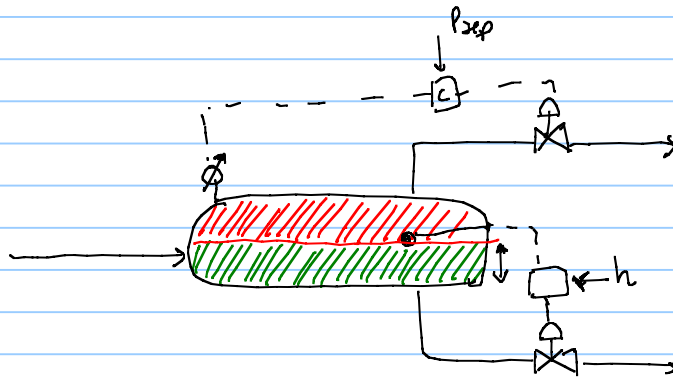
- effect of depletion on flow equilibrium



Short



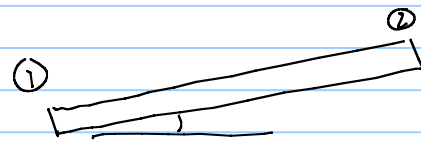
separator



flowline

$$q_g = C_T \left( \frac{P_1^2}{e^s} - P_2^2 \right)^{0.5}$$

$$q_g = C_{FL} \left( \frac{P_{in}^2}{e^s} - P_{out}^2 \right)^{0.5}$$

if pipe is horizontal  $s=0$ 

$$\left( P_{in}^2 - P_{out}^2 \right)^{0.5} \quad C_T ?$$

$$C_{FL} = \text{const.} \cdot \left( \frac{s e^s}{e^s - 1} \right)$$

 $s=0$ 

$$\frac{0-1}{1-1} = \frac{0}{0} \text{ undefined!}$$

l'Hopital

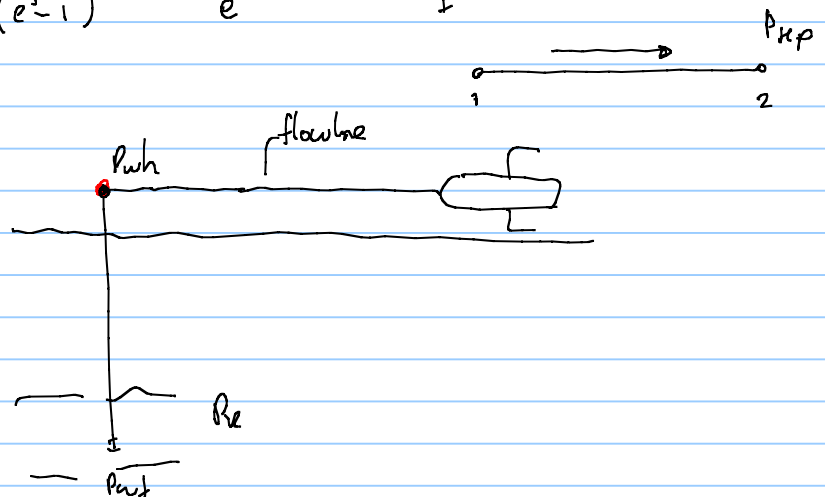
 $\lim_{x \rightarrow 0} f(x) \rightarrow \text{undefined}$ 

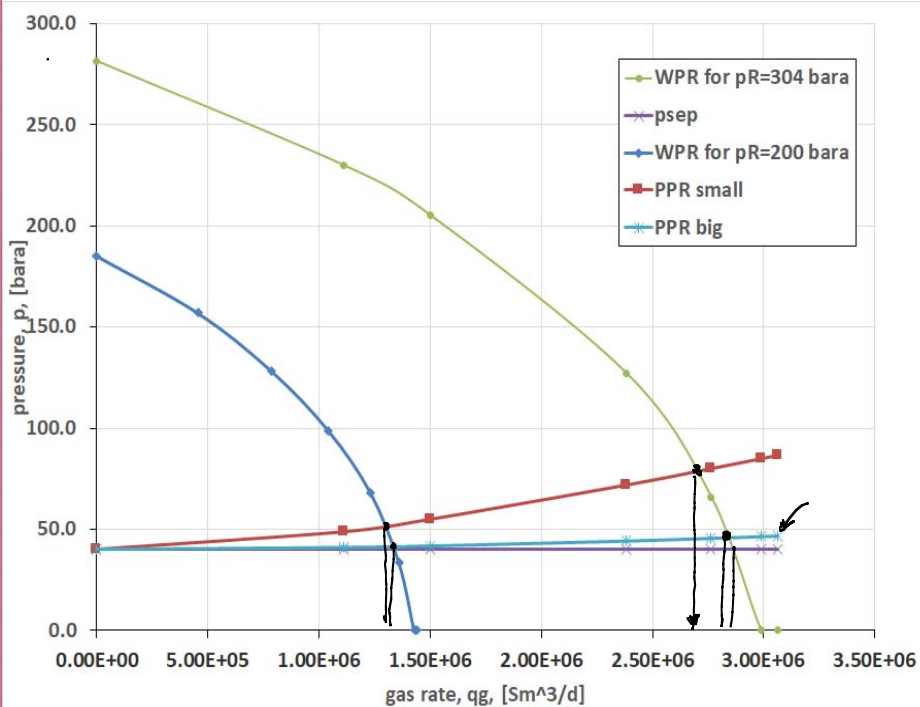
$$\lim_{x \rightarrow 0} \frac{f(x)}{g(x)} \rightarrow \lim_{x \rightarrow 0} \frac{f'(x)}{g'(x)}$$

$$\frac{\frac{d}{ds}(s e^s)}{\frac{d}{ds}(e^s - 1)} = \frac{s \cdot e^s + e^s}{e^s} = \frac{1}{1} = 1$$

$$q_g = C_{FL} (P_{in}^2 - P_{out}^2)^{0.5}$$

Exercise



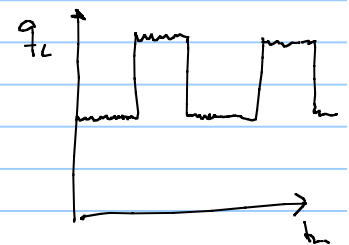
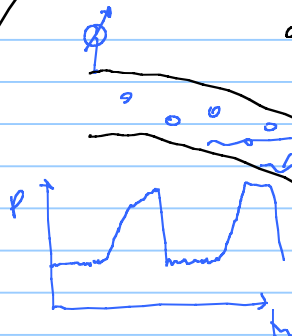


• pipeline sizing  $\rightarrow$  minimize  $\Delta p$ , maximize rate  $q_g$

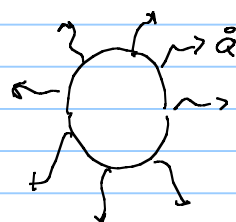
$\rightarrow$  cost !

$\rightarrow$  erosion

$\rightarrow$  liquid accumulation  $\rightarrow$  liquid slugging (intermittent flow of gas and liquid)  
design our flowlines to avoid accumulation



$\rightarrow$  big  $\Phi$  leads to more cooling  $\rightarrow$  more oil/water condensation, more liquid accumulation



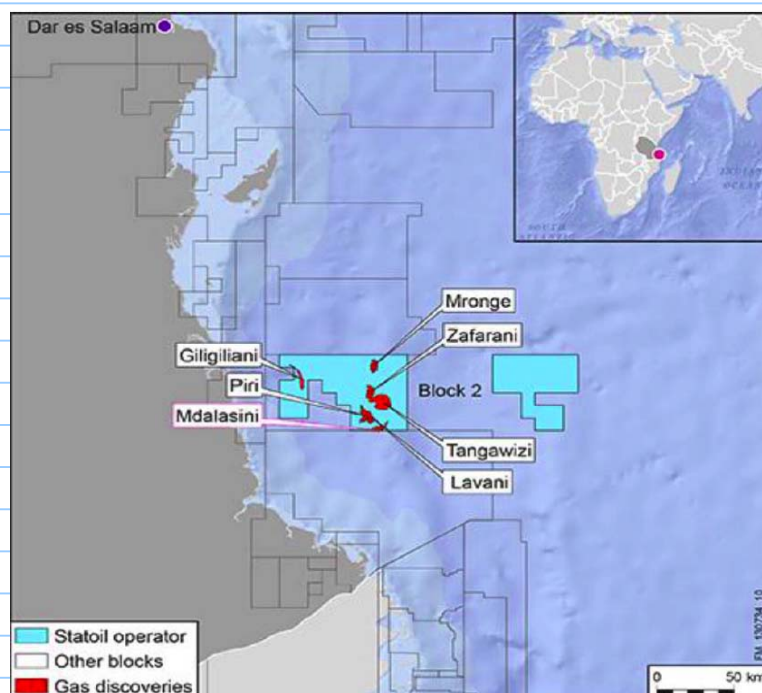
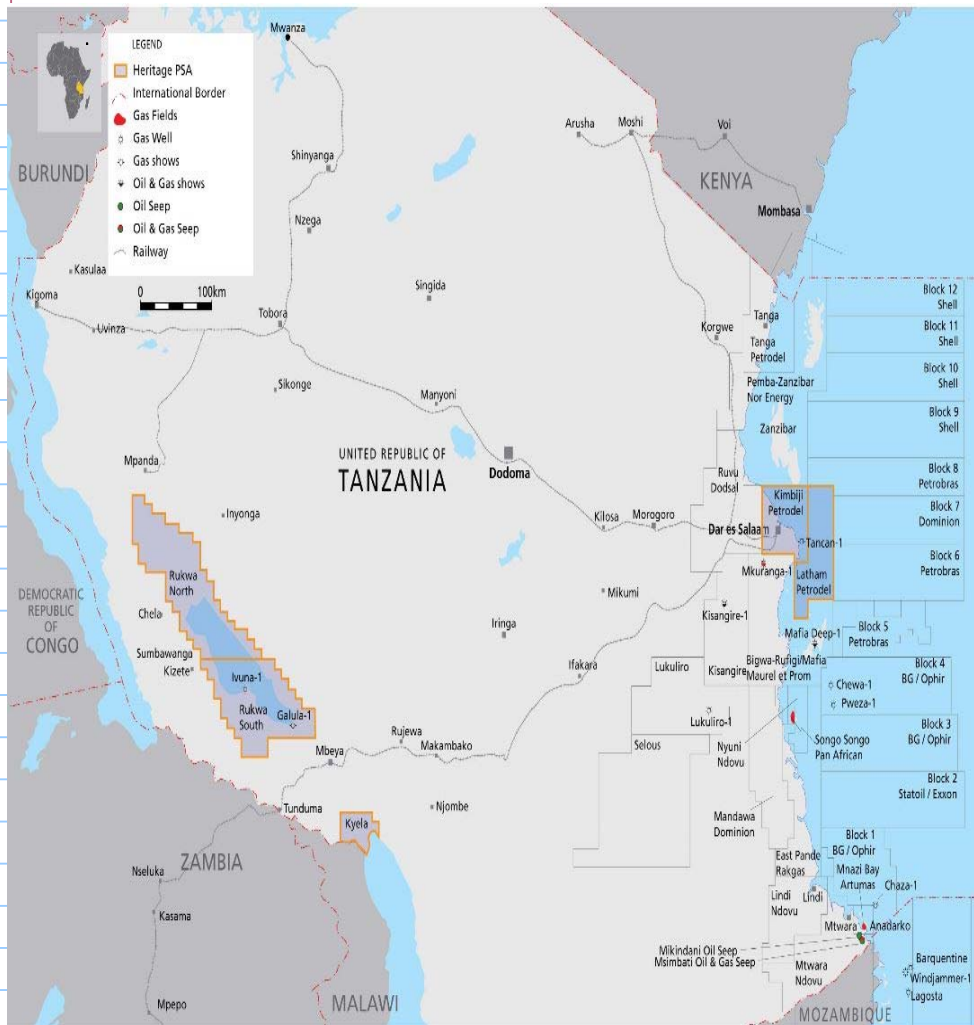
corrosion  $\rightarrow$  corrosion TOL top of line

corrosion

$\rightarrow$  Hydrates if  $T$  is low  
 $\rightarrow$  oil flowlines max,  $\Delta T$   $\Delta p$   $\uparrow$

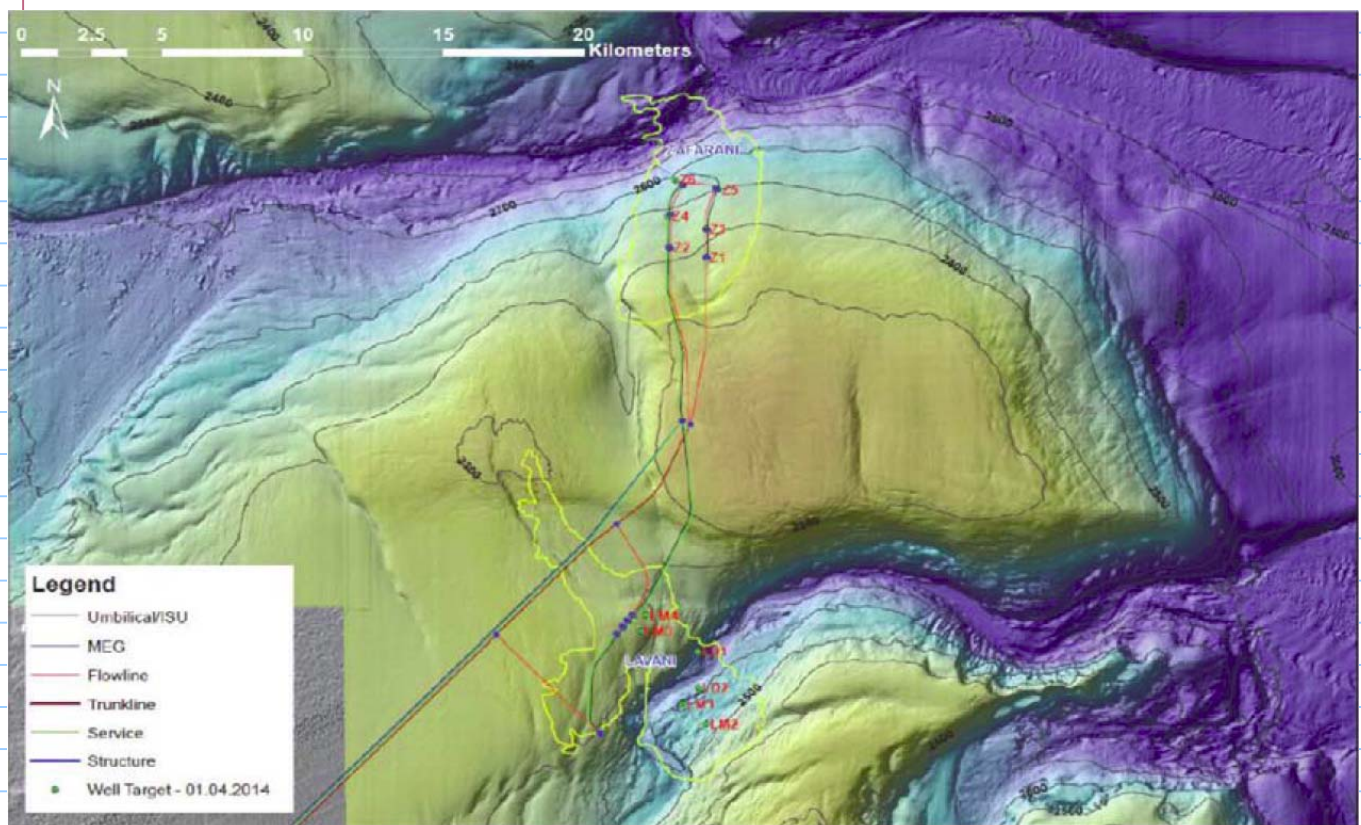
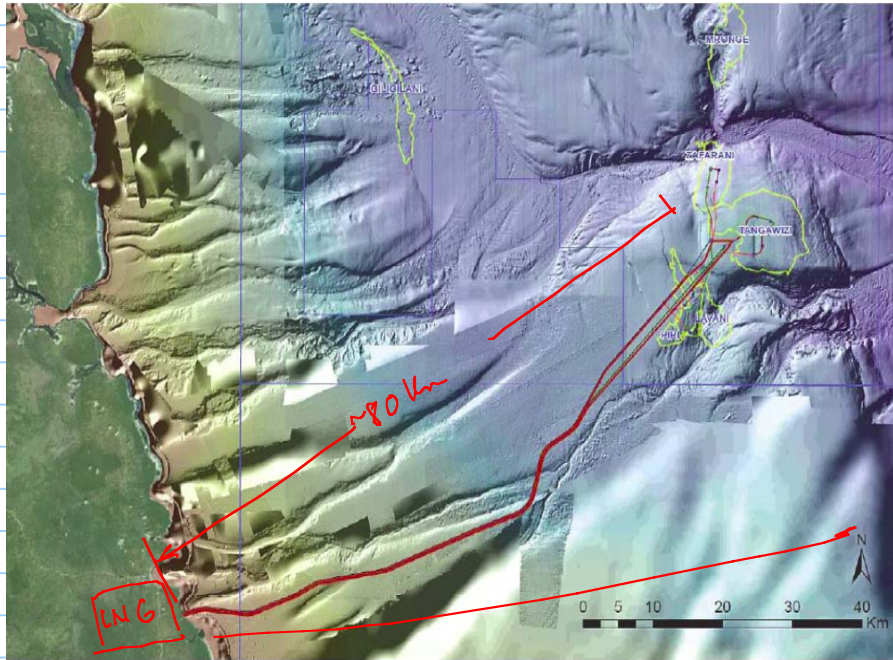
field production scheduling → define, calculate/estimate the field production profile with time

## Block 2 offshore Tanzania



water depth 2200 - 2600 m

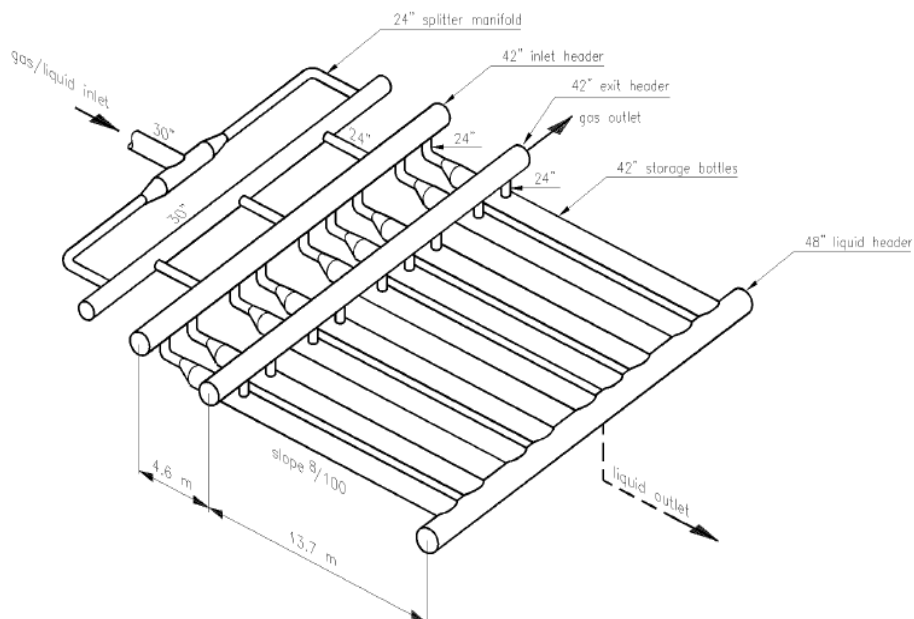
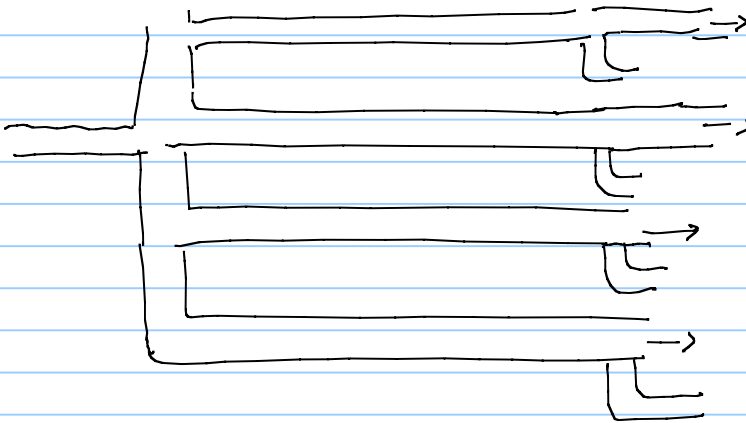




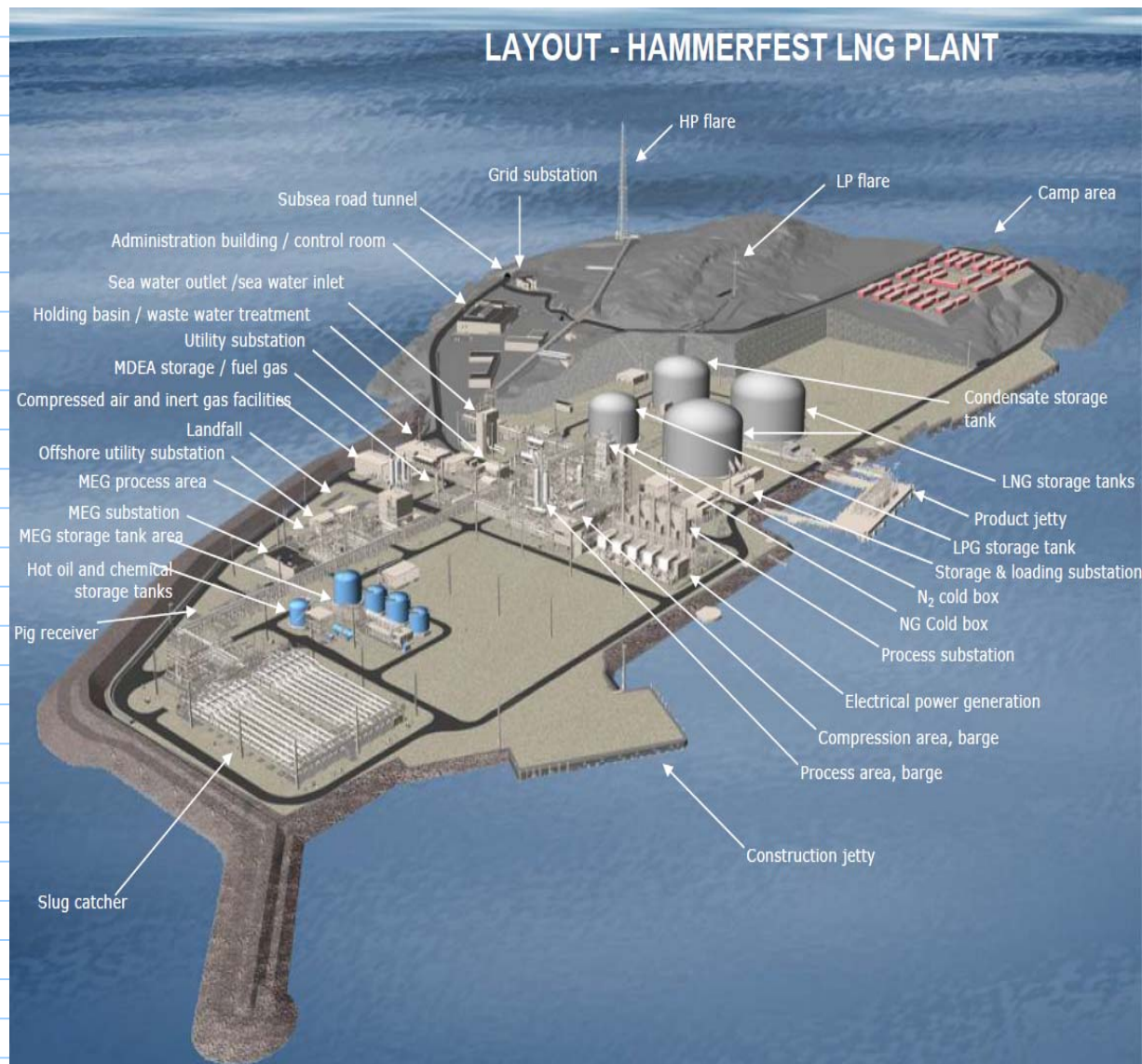
Snowwhite (Snøhvit) Subsea to beach



onshore facilities: slugcatcher



## LNG plant



- contract for a fixed amount of gas  $18 \text{ EG Sm}^3/\text{d}$

↳ plateau length  $\rightarrow$  choosing node A

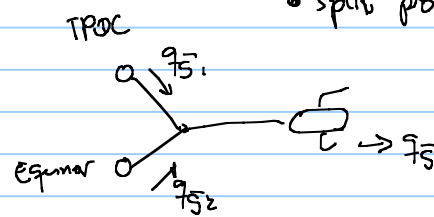
↳ post plateau production profile  $\rightarrow$  open choke (node B)

- Subsea layout/architecture

Pr

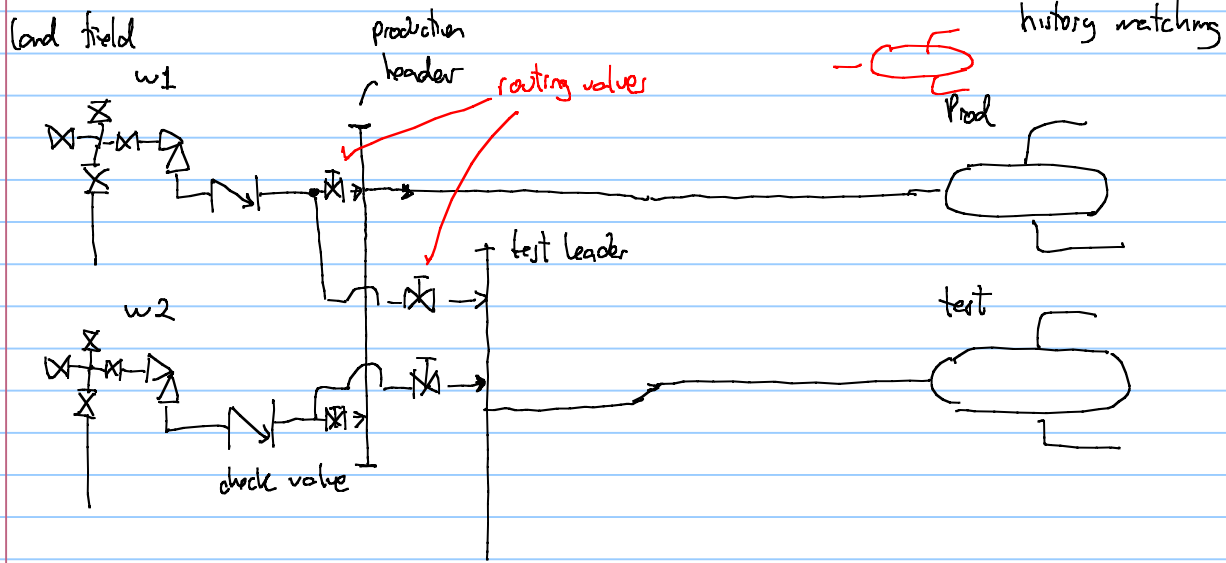
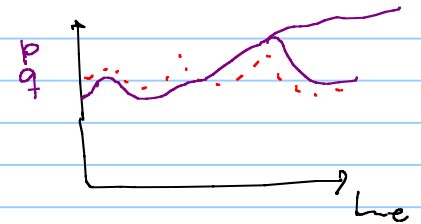
Production manifold

- route the production of wells
  - test wells
- allocation → determine source of gas/oil



- split profit

- to improve reservoir models
- compare model v.s. data



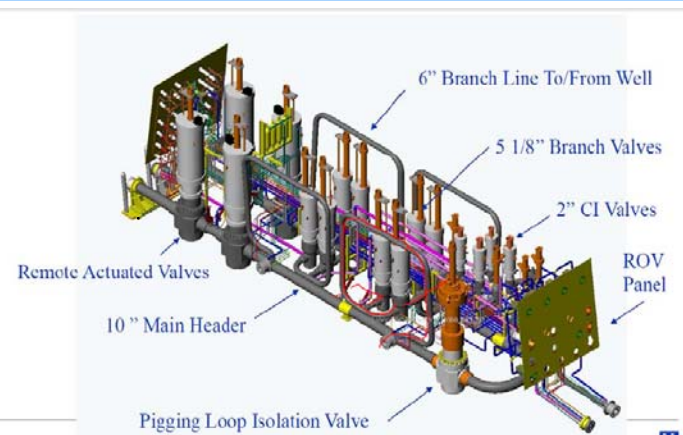
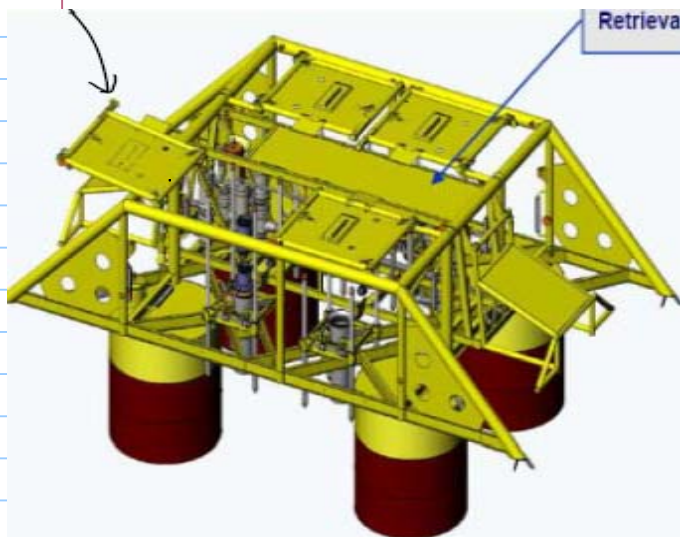
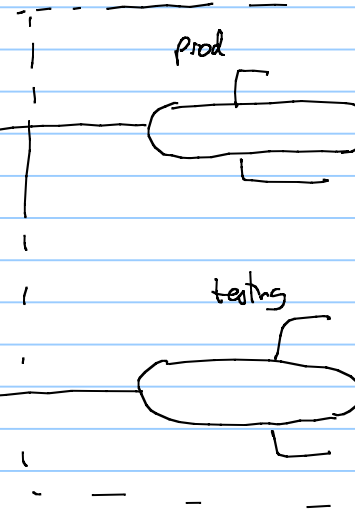
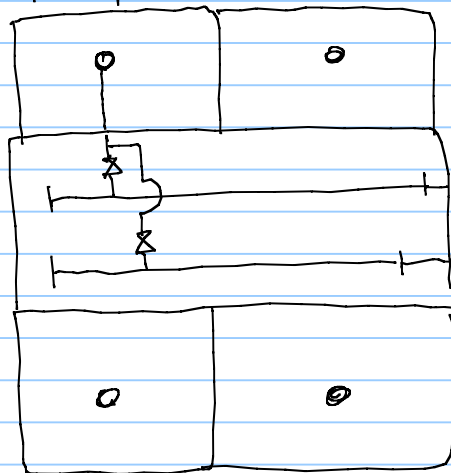




floating, production, storage offloading vessel  
platform / FPSO

Subsea systems  
template wells

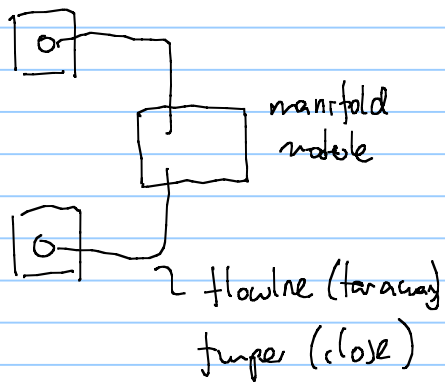
4-well template



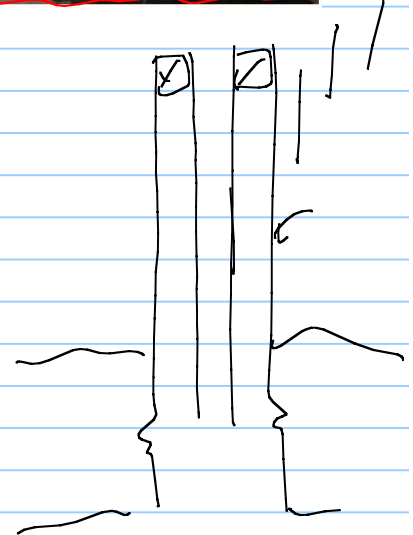
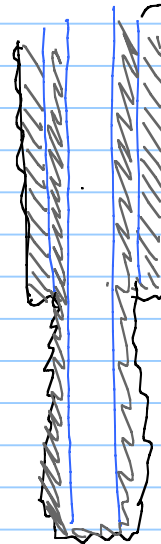


two types of subsea wells

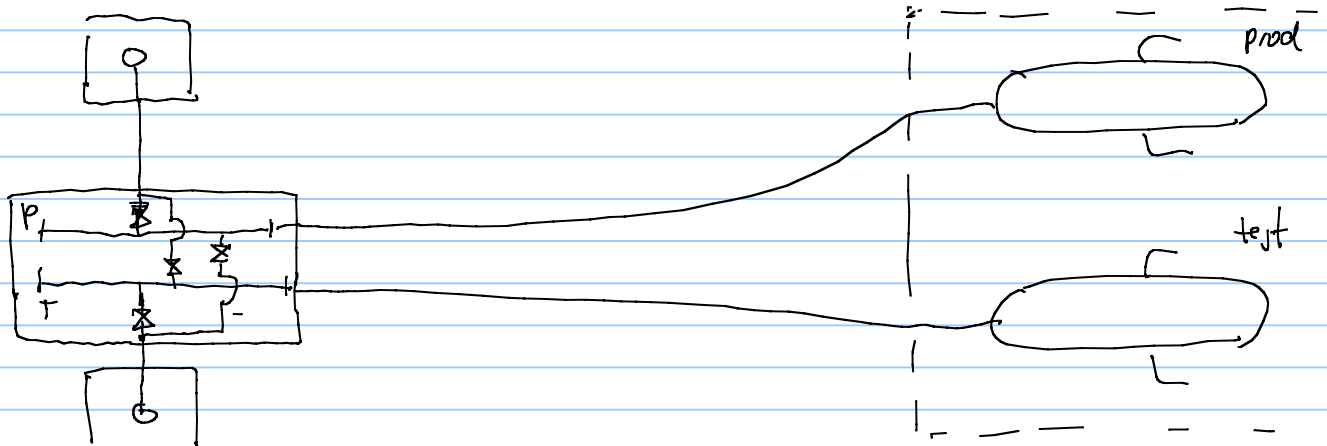
Satellite wells

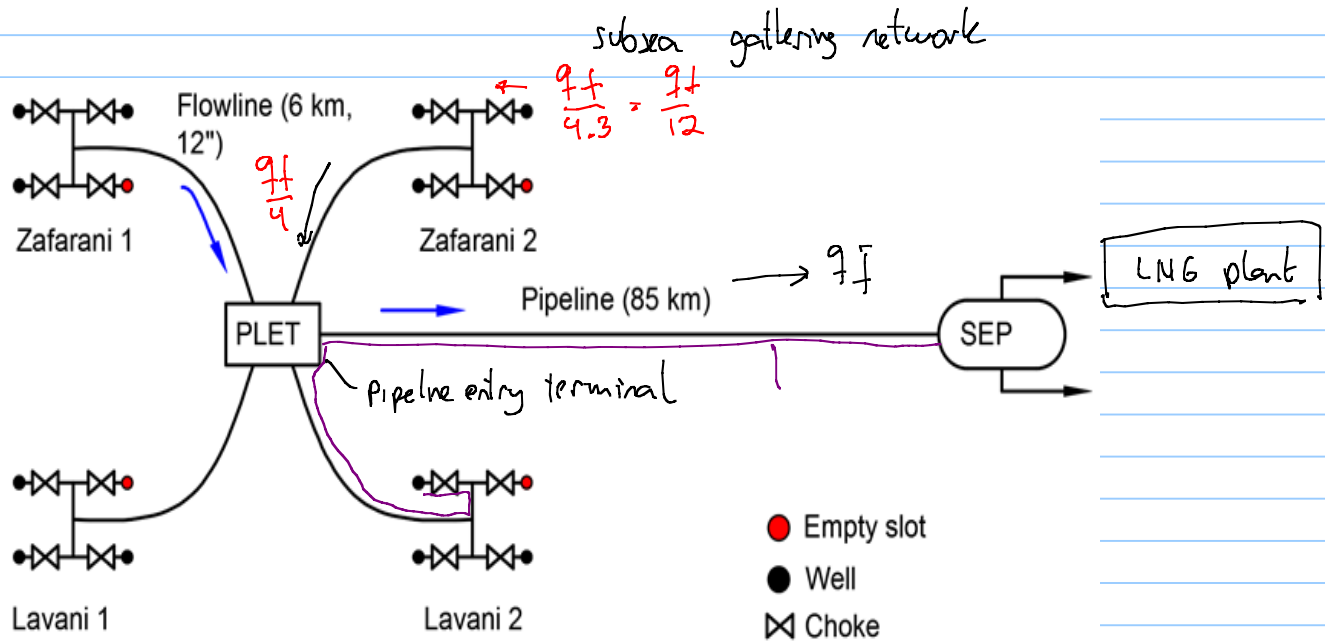
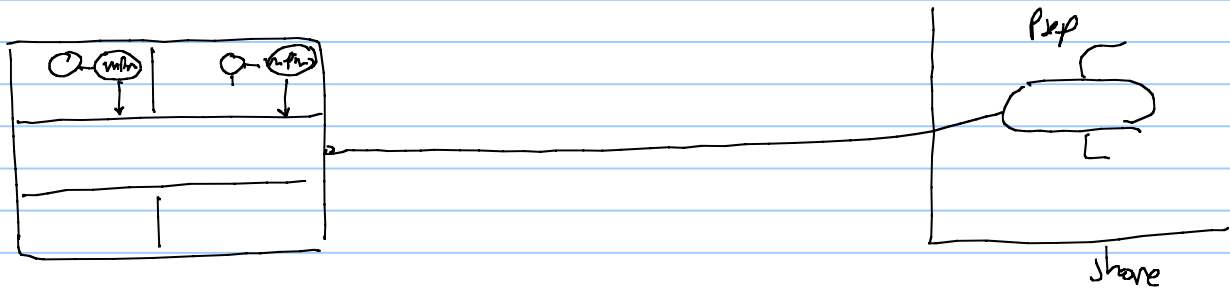


first pipe that is placed in hole  $\rightarrow$  conductor

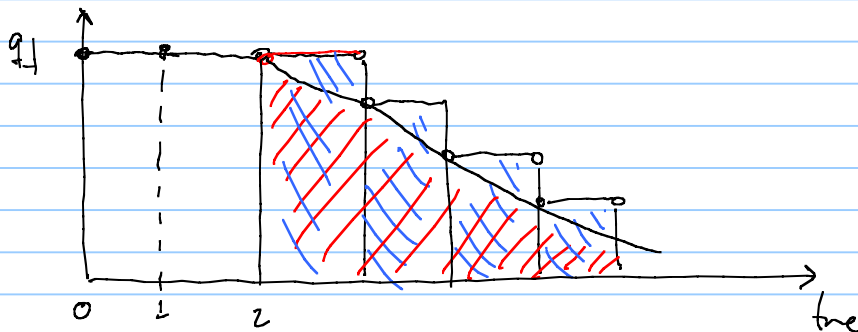


CONDUCTOR / DRILLING PROCESS

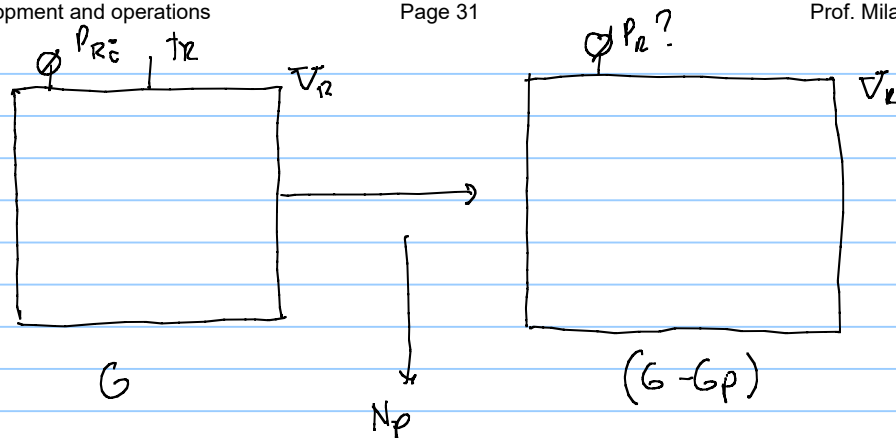




How to calculate  $P_2 = f(t)$ ?



Dry gas material Balance



$$P V = R Z T_R$$

$$P \frac{V}{m} = R Z T_R$$

$$m_i = \frac{P_i V_R}{R Z_i T_R}$$

$$m^* = \frac{P_R V_R}{R Z_R T_R}$$

$$G_p \approx (m_i - m^*)$$

final equation

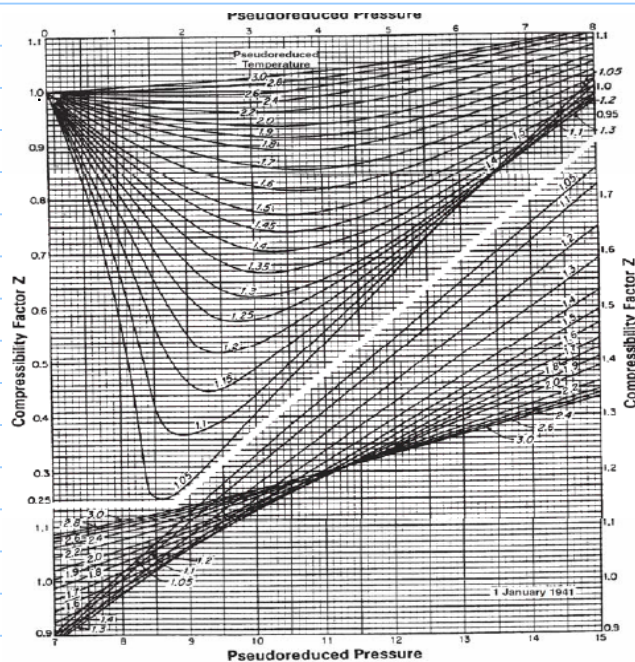
$$P_R = \frac{P_i}{Z_i} \left( 1 - \frac{G_p}{G} \right)$$

neglecting rock compressibility

Recovery factor

$$P_R = P_i \frac{Z_R}{Z_i} \left( 1 - RF \right)$$

0  $q_{field}$   
1  $q_{field}$



$$Z_R = f(T_R, P_R)$$

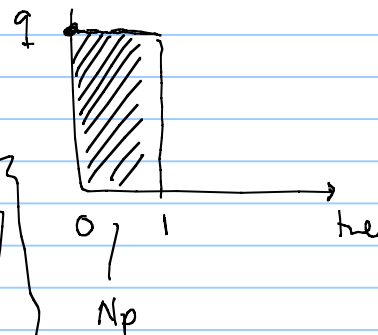
assume  $P_{R,assumed}$

calculate  $Z_R$

equation calculate  $P_R$

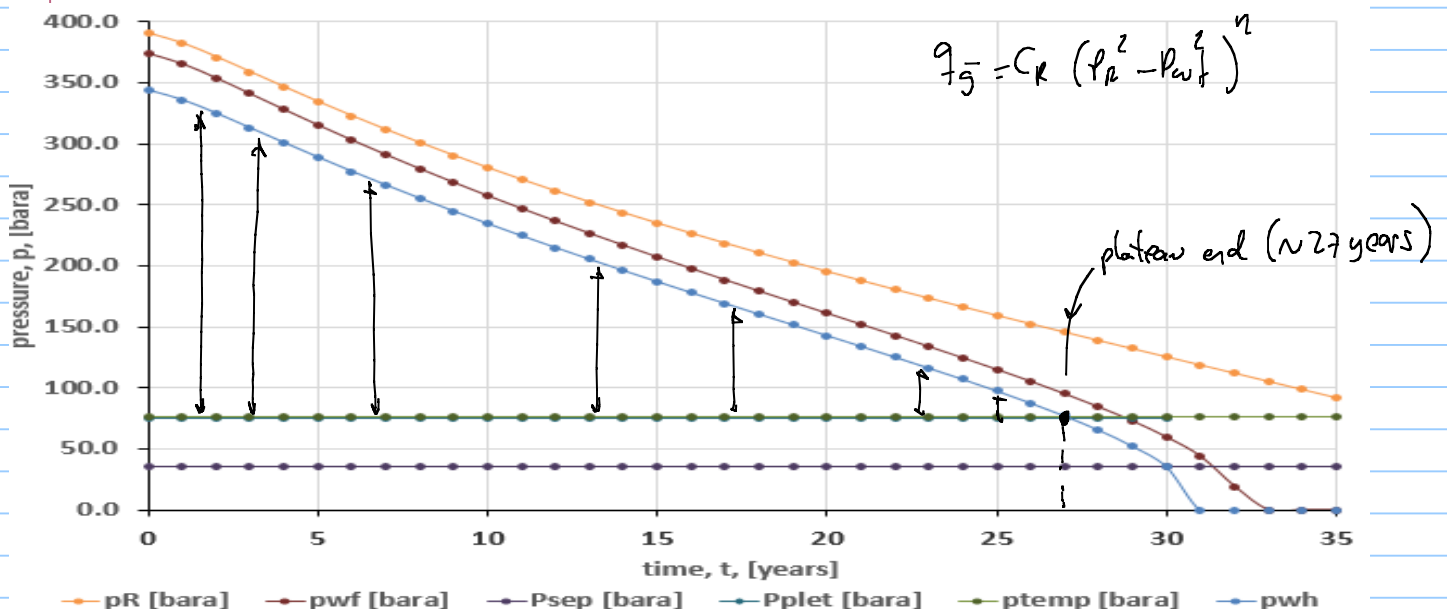
is  $P_{R,assumed} = P_{R,calc}$ ?

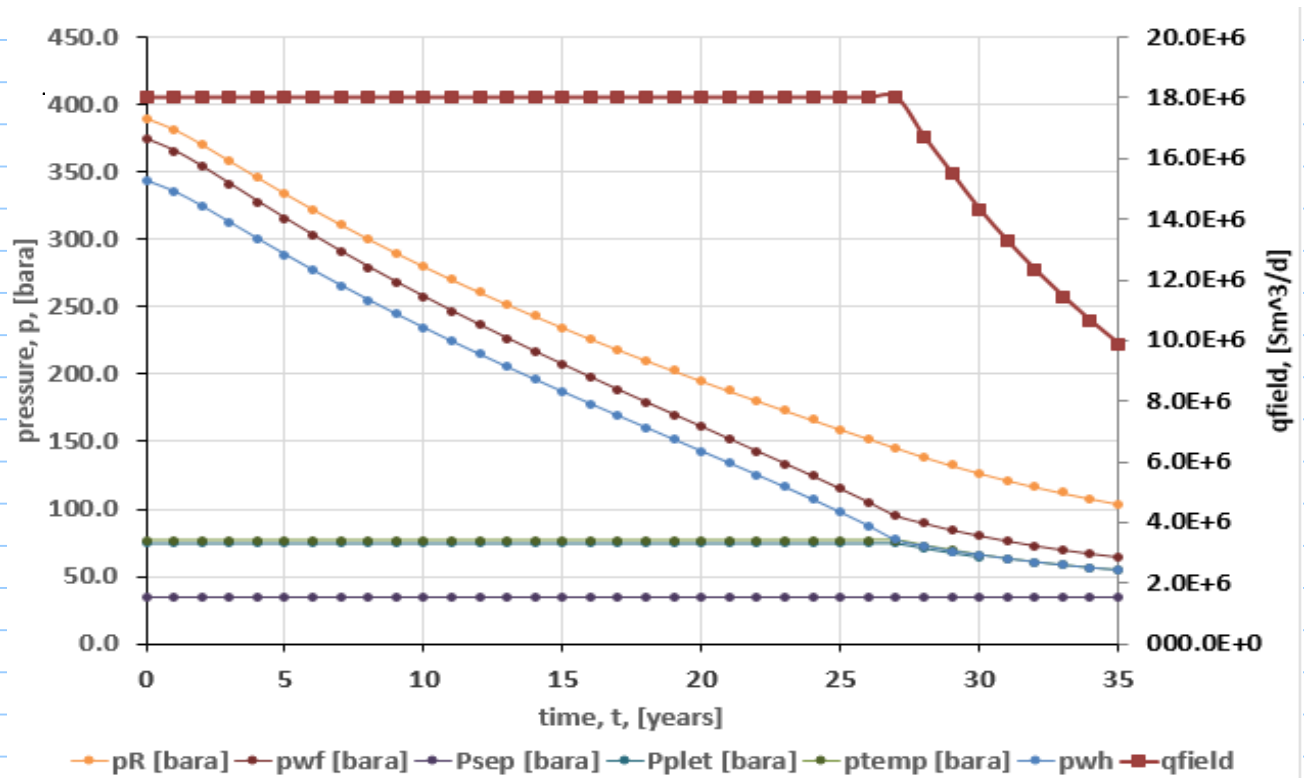
yes



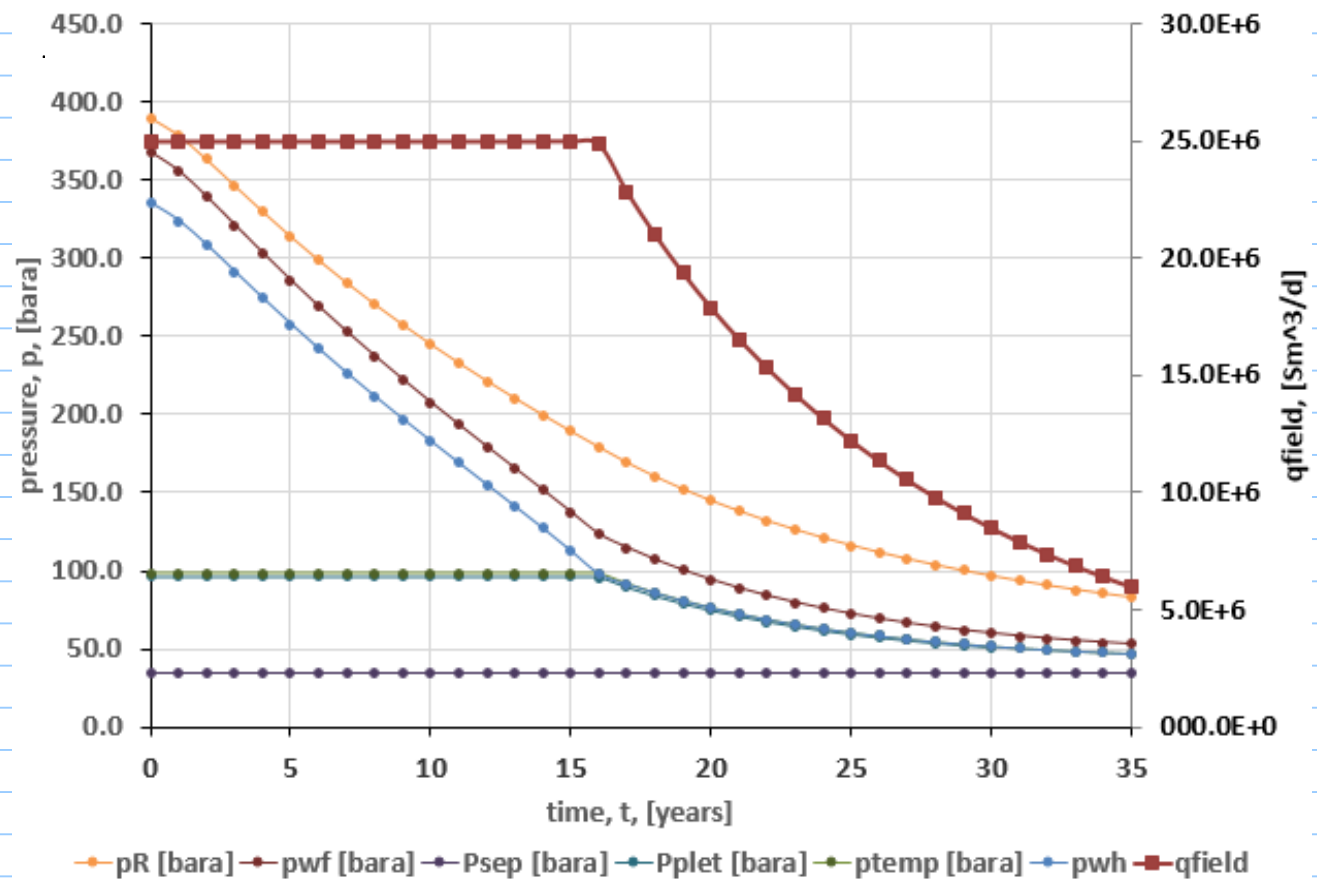
$t_{ne}$   $p_R$   $p_{R_1} \rightarrow p_{R_2}$  slow changing  
 $t_1$   $p_{R_1}$   $Z_{R_2}$  with  $(p_{R_1})$   
 $t_2$   $p_{R_2}$   $Z_{R_i}$  with  $p_{R_{i-1}}$   
 $t_3$   $p_{R_3}$   
 $\vdots$   
 $\vdots$   
 $\vdots$   
 $\frac{Sm^3}{d}$  years  $\frac{N_{days}}{year}$   
 $t_i - t_{i-1}$  uphse  
 $\Delta p = q_{year} (1 - 0) \cdot uphse$

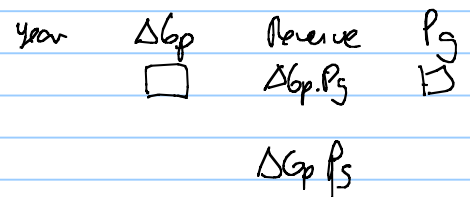
| time    | qwell                | qfield               | $\Delta Gp$        | Gp                 | RF   | pR     | Z     | pwf    | pwh    | Psep   | Pplet  | qtemp                | ptemp  | Deltphchoke | time    |
|---------|----------------------|----------------------|--------------------|--------------------|------|--------|-------|--------|--------|--------|--------|----------------------|--------|-------------|---------|
| [years] | [Sm <sup>3</sup> /d] | [Sm <sup>3</sup> /d] | [Sm <sup>3</sup> ] | [Sm <sup>3</sup> ] | [-]  | [bara] | [-]   | [bara] | [bara] | [bara] | [bara] | [Sm <sup>3</sup> /d] | [bara] | [bara]      | [years] |
| 0       | 1.50E+06             | 18.0E+6              | 6.5E+9             | 000.0E+0           | 0.00 | 390.0  | 1.045 | 374.0  | 343.6  | 35.0   | 75.1   | 4.50E+06             | 76.7   | 267         | 0       |
| 1       | 1.50E+06             | 18.0E+6              | 6.5E+9             | 6.5E+9             | 0.02 | 381.9  | 1.036 | 365.6  | 335.7  | 35.0   | 75.1   | 4.50E+06             | 76.7   | 259         | 1       |
| 2       | 1.50E+06             | 18.0E+6              | 6.5E+9             | 13.0E+9            | 0.04 | 370.6  | 1.024 | 353.8  | 324.7  | 35.0   | 75.1   | 4.50E+06             | 76.7   | 248         | 2       |
| 3       | 1.50E+06             | 18.0E+6              | 6.5E+9             | 19.4E+9            | 0.06 | 358.4  | 1.012 | 340.9  | 312.7  | 35.0   | 75.1   | 4.50E+06             | 76.7   | 236         | 3       |
| 4       | 1.50E+06             | 18.0E+6              | 6.5E+9             | 25.9E+9            | 0.08 | 346.1  | 0.999 | 328.0  | 300.6  | 35.0   | 75.1   | 4.50E+06             | 76.7   | 224         | 4       |
| 5       | 1.50E+06             | 18.0E+6              | 6.5E+9             | 32.4E+9            | 0.10 | 334.0  | 0.987 | 315.3  | 288.7  | 35.0   | 75.1   | 4.50E+06             | 76.7   | 212         | 5       |
| 6       | 1.50E+06             | 18.0E+6              | 6.5E+9             | 38.9E+9            | 0.13 | 322.4  | 0.976 | 302.9  | 277.1  | 35.0   | 75.1   | 4.50E+06             | 76.7   | 200         | 6       |
| 7       | 1.50E+06             | 18.0E+6              | 6.5E+9             | 45.4E+9            | 0.15 | 311.2  | 0.966 | 291.0  | 265.9  | 35.0   | 75.1   | 4.50E+06             | 76.7   | 189         | 7       |
| 8       | 1.50E+06             | 18.0E+6              | 6.5E+9             | 51.8E+9            | 0.17 | 300.4  | 0.957 | 279.4  | 255.1  | 35.0   | 75.1   | 4.50E+06             | 76.7   | 178         | 8       |
| 9       | 1.50E+06             | 18.0E+6              | 6.5E+9             | 58.3E+9            | 0.19 | 290.0  | 0.948 | 268.2  | 244.6  | 35.0   | 75.1   | 4.50E+06             | 76.7   | 168         | 9       |
| 10      | 1.50E+06             | 18.0E+6              | 6.5E+9             | 64.8E+9            | 0.21 | 280.0  | 0.940 | 257.3  | 234.4  | 35.0   | 75.1   | 4.50E+06             | 76.7   | 158         | 10      |
| 11      | 1.50E+06             | 18.0E+6              | 6.5E+9             | 71.3E+9            | 0.23 | 270.4  | 0.933 | 246.8  | 224.5  | 35.0   | 75.1   | 4.50E+06             | 76.7   | 148         | 11      |
| 12      | 1.50E+06             | 18.0E+6              | 6.5E+9             | 77.8E+9            | 0.25 | 261.0  | 0.926 | 236.5  | 214.8  | 35.0   | 75.1   | 4.50E+06             | 76.7   | 138         | 12      |
| 13      | 1.50E+06             | 18.0E+6              | 6.5E+9             | 84.2E+9            | 0.27 | 252.0  | 0.920 | 226.5  | 205.3  | 35.0   | 75.1   | 4.50E+06             | 76.7   | 129         | 13      |
| 14      | 1.50E+06             | 18.0E+6              | 6.5E+9             | 90.7E+9            | 0.29 | 243.2  | 0.915 | 216.7  | 196.0  | 35.0   | 75.1   | 4.50E+06             | 76.7   | 119         | 14      |
| 15      | 1.50E+06             | 18.0E+6              | 6.5E+9             | 97.2E+9            | 0.31 | 234.7  | 0.910 | 207.1  | 186.9  | 35.0   | 75.1   | 4.50E+06             | 76.7   | 110         | 15      |
| 16      | 1.50E+06             | 18.0E+6              | 6.5E+9             | 103.7E+9           | 0.33 | 226.4  | 0.906 | 197.6  | 178.0  | 35.0   | 75.1   | 4.50E+06             | 76.7   | 101         | 16      |
| 17      | 1.50E+06             | 18.0E+6              | 6.5E+9             | 110.2E+9           | 0.35 | 218.3  | 0.902 | 188.3  | 169.1  | 35.0   | 75.1   | 4.50E+06             | 76.7   | 92          | 17      |
| 18      | 1.50E+06             | 18.0E+6              | 6.5E+9             | 116.6E+9           | 0.38 | 210.4  | 0.899 | 179.1  | 160.3  | 35.0   | 75.1   | 4.50E+06             | 76.7   | 84          | 18      |
| 19      | 1.50E+06             | 18.0E+6              | 6.5E+9             | 123.1E+9           | 0.40 | 202.7  | 0.897 | 170.0  | 151.6  | 35.0   | 75.1   | 4.50E+06             | 76.7   | 75          | 19      |





for higher plateau  $25 \times 10^6 \text{ Sm}^3/\text{d}$

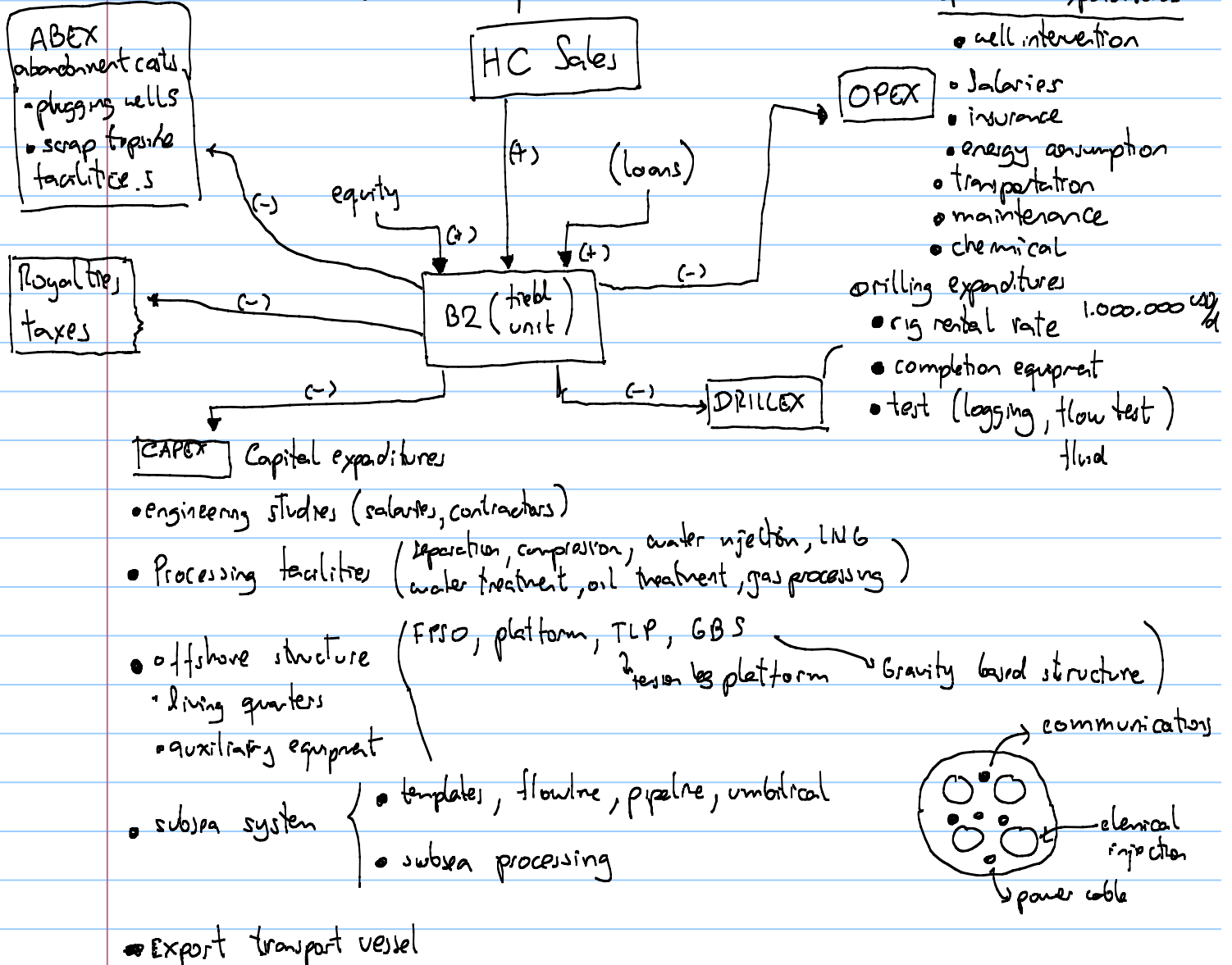




Note Title

05.12.2018

# Cash flow in field development





How do we deal with expenses and income?



### Cash flow calculations

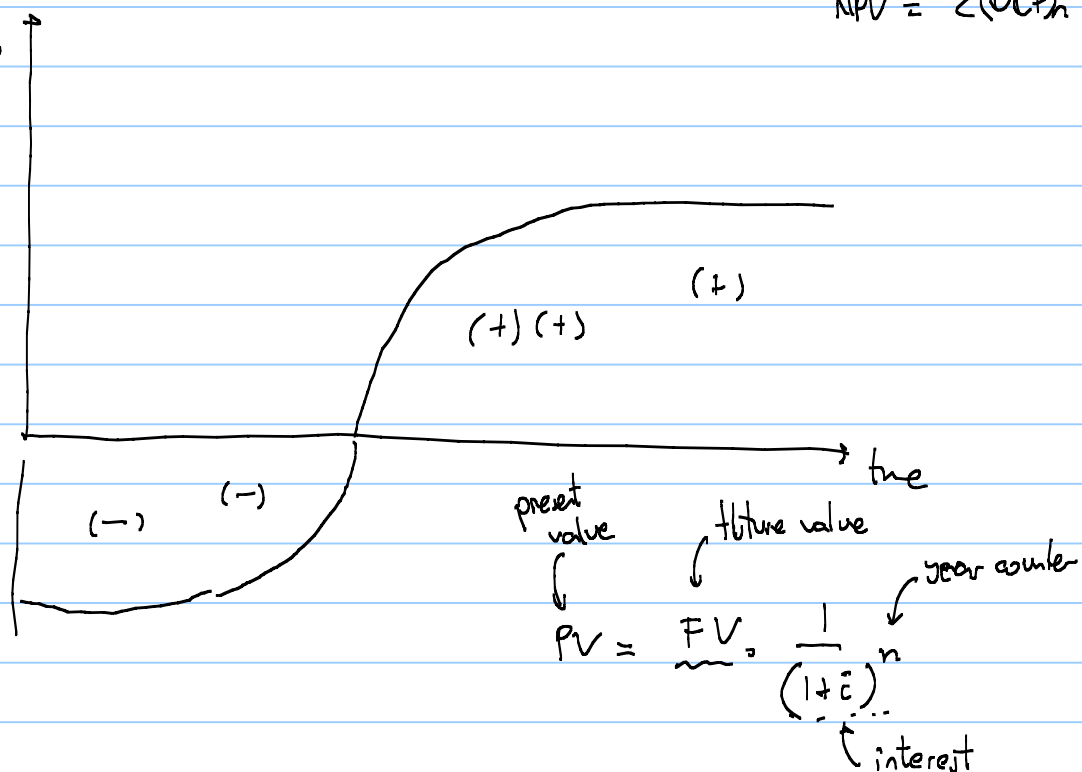
Revenue - tax - royalty

discounted cash flow

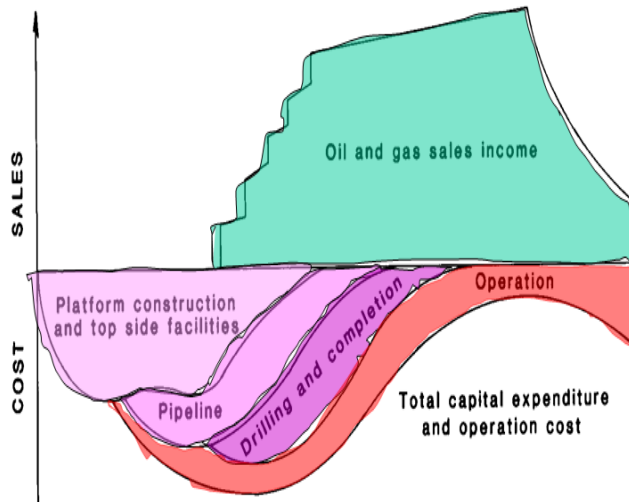
| t                   | Revenue | CAPEX | DRILLER | OPEx | Net income | Cash flow              | DCF                  |
|---------------------|---------|-------|---------|------|------------|------------------------|----------------------|
| year 1              | 0       | (-)   | (-)     | 0    | 0          | (income - expenditure) | $\frac{CF}{(1+i)^n}$ |
| year 2              | 0       | (-)   | (-)     | 0    | 0          | (-)                    | -                    |
| year 3              | 0       | (-)   | (-)     | 0    | 0          | (-)                    | -                    |
| start of production | 0       | (-)   | (-)     | 0    | 0          | (-)                    | -                    |
|                     | (+)     | 0     | 0       | (-)  | (+)        | (+)                    | -                    |
|                     | (+)     | 0     | 0       | (-)  | (+)        | (+)                    | -                    |
|                     | (+)     | 0     | 0       | (-)  | (+)        | (+)                    | -                    |
|                     | (+)     | 0     | 0       | (-)  | (+)        | (+)                    | -                    |
|                     | (+)     | 0     | 0       | (-)  | (+)        | (+)                    | -                    |
|                     | (-)     | 0     | 0       | (-)  | (+)        | (+)                    | -                    |

$$NPV = \sum (DCF)_n$$

Cash flow



## Revenue and Cost Profiles



## The Ultimate driver in E&P operations

**NPV=**

+ gas price  $\cdot$  Gas production(i)

$$\sum_{i=0}^n \frac{\text{OIL PRICE}(i) \times \text{OIL PROD}(i) - \text{CAPEX}(i) - \text{OPEX}(i) - \text{TAX}(i)}{(1+r)^i}$$

(1+r)<sup>i</sup>

discount factor

~6-10%

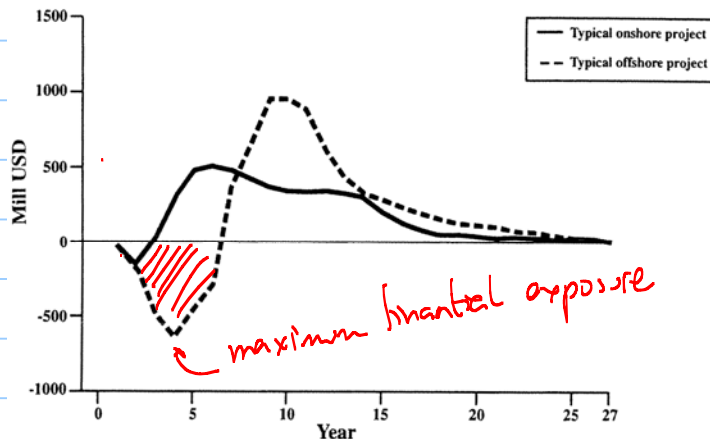
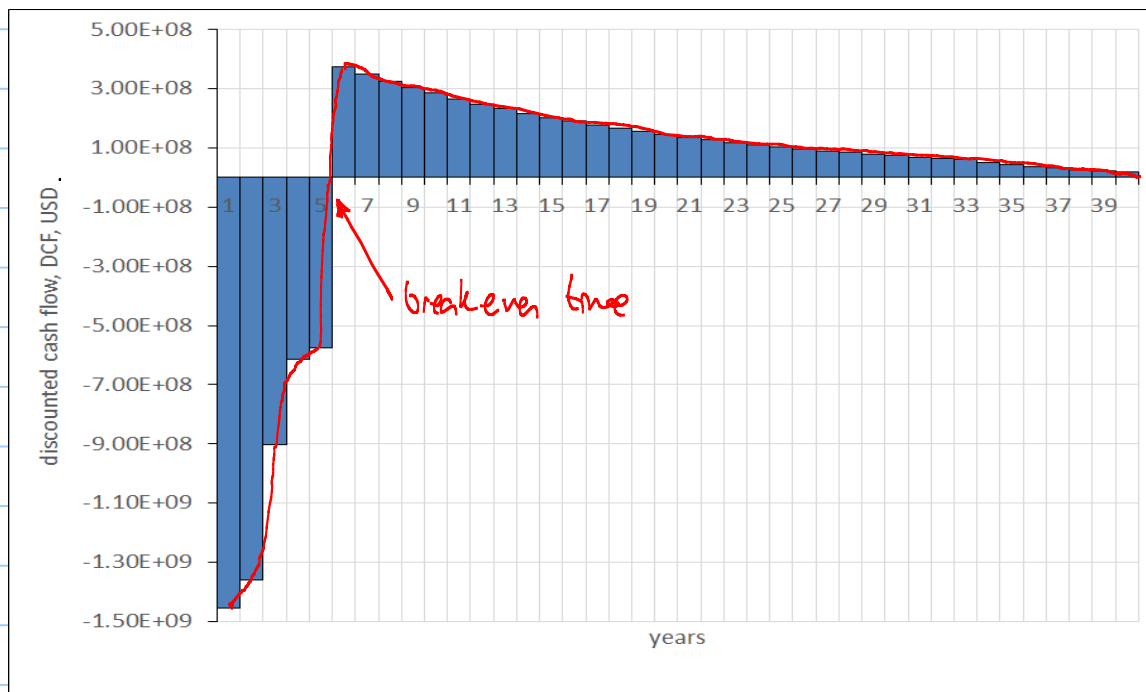


Fig. 9. Typical before tax cash flow profiles for offshore and onshore projects.

## Class exercise



| Time        | Gas production in year | Revenue  | DRILLEX  | CAPEX <sub>SUBSEA</sub> | CAPEX <sub>LNG</sub> | OPEX     | Total Cost | Cash Flow | Discounted Cash Flow: PV(i) |
|-------------|------------------------|----------|----------|-------------------------|----------------------|----------|------------|-----------|-----------------------------|
| end of year | [Sm <sup>3</sup> ]     | USD      | USD      | USD                     | USD                  | USD      | USD        | USD       | USD                         |
| 1           | 0                      | 0.00E+00 | 7.50E+08 | 1.12E+08                | 6.95E+08             | 0        | 1.56E+09   | -1.56E+09 | (-) -1.46E+09               |
| 2           | 0                      | 0.00E+00 | 7.50E+08 | 1.12E+08                | 6.95E+08             | 0        | 1.56E+09   | -1.56E+09 | (-) -1.36E+09               |
| 3           | 0                      | 0.00E+00 | 3.00E+08 | 1.12E+08                | 6.95E+08             | 0        | 1.11E+09   | -1.11E+09 | (-) -9.04E+08               |
| 4           | 0                      | 0.00E+00 | 0.00E+00 | 1.12E+08                | 6.95E+08             | 0        | 8.07E+08   | -8.07E+08 | (-) -6.16E+08               |
| 5           | 0                      | 0.00E+00 | 0.00E+00 | 1.12E+08                | 6.95E+08             | 0        | 8.07E+08   | -8.07E+08 | (-) -5.75E+08               |
| 6           | 6.5E+9                 | 6.80E+08 | 0.00E+00 | 0.00E+00                | 0.00E+00             | 1.20E+08 | 1.20E+08   | 5.60E+08  | (+) 3.73E+08                |
| 7           | 6.5E+9                 | 6.80E+08 | 0.00E+00 | 0.00E+00                | 0.00E+00             | 1.20E+08 | 1.20E+08   | 5.60E+08  | (+) 3.49E+08                |
| 8           | 6.5E+9                 | 6.80E+08 | 0.00E+00 | 0.00E+00                | 0.00E+00             | 1.20E+08 | 1.20E+08   | 5.60E+08  | (+) 3.26E+08                |
| 9           | 6.5E+9                 | 6.80E+08 | 0.00E+00 | 0.00E+00                | 0.00E+00             | 1.20E+08 | 1.20E+08   | 5.60E+08  | (+) 3.05E+08                |
| 10          | 6.5E+9                 | 6.80E+08 | 0.00E+00 | 0.00E+00                | 0.00E+00             | 1.20E+08 | 1.20E+08   | 5.60E+08  | (+) 2.85E+08                |
| 11          | 6.5E+9                 | 6.80E+08 | 0.00E+00 | 0.00E+00                | 0.00E+00             | 1.20E+08 | 1.20E+08   | 5.60E+08  | (+) 2.66E+08                |
| 12          | 6.5E+9                 | 6.80E+08 | 0.00E+00 | 0.00E+00                | 0.00E+00             | 1.20E+08 | 1.20E+08   | 5.60E+08  | (+) 2.49E+08                |
| 13          | 6.5E+9                 | 6.80E+08 | 0.00E+00 | 0.00E+00                | 0.00E+00             | 1.20E+08 | 1.20E+08   | 5.60E+08  | 2.33E+08                    |
| 14          | 6.5E+9                 | 6.80E+08 | 0.00E+00 | 0.00E+00                | 0.00E+00             | 1.20E+08 | 1.20E+08   | 5.60E+08  | 2.17E+08                    |
| 15          | 6.5E+9                 | 6.80E+08 | 0.00E+00 | 0.00E+00                | 0.00E+00             | 1.20E+08 | 1.20E+08   | 5.60E+08  | 2.03E+08                    |
| 16          | 6.5E+9                 | 6.80E+08 | 0.00E+00 | 0.00E+00                | 0.00E+00             | 1.20E+08 | 1.20E+08   | 5.60E+08  | 1.90E+08                    |

I always have to perform sensitivity analyses on input

Ceteris Paribus "one change at a time"

• gas prices / oil prices (HC)

• cost figures  $\pm 40\%$

$\pm 20\%$  (PDO)

change  $\rightarrow$  calculate NPV

go back to original.

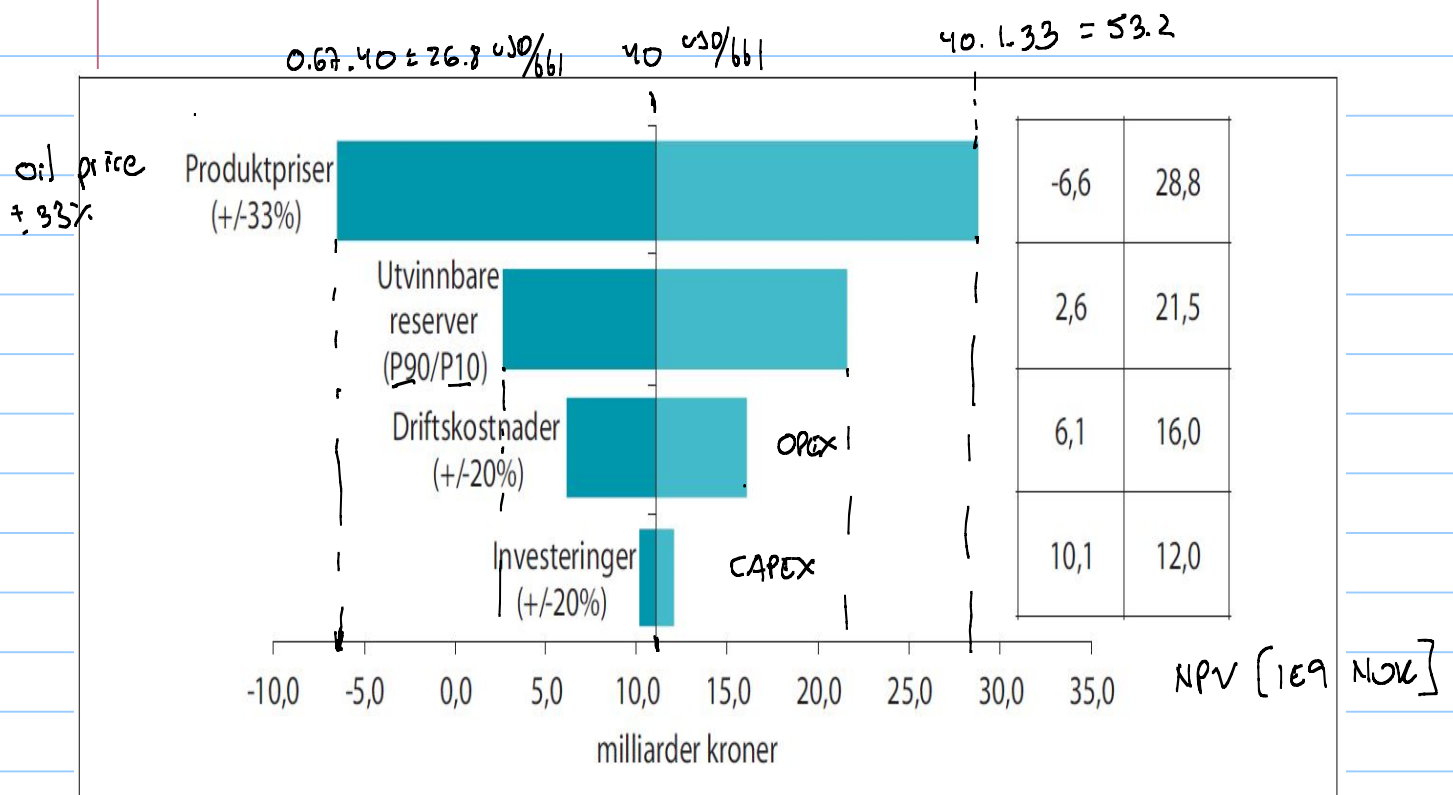
change  
NPV  
↓

• reserve size

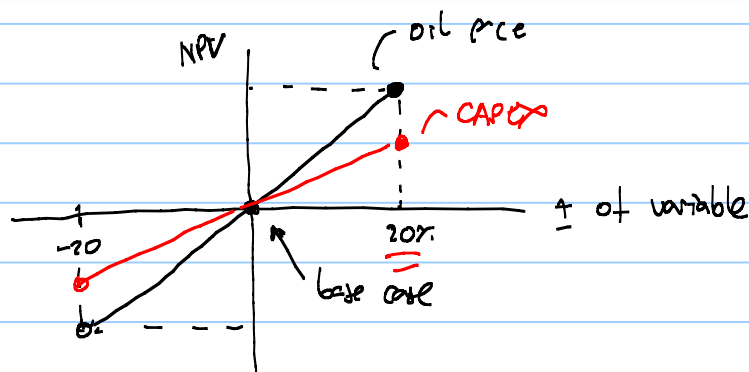
• opex

•  
•

• Tornado chart



• Spider plot



NPV base case 170 E6 USD

gas price  $\pm 20\%$  NPV NPV  
 CAPEX  $\pm 20\%$  NPV NPV  
 OPEX  $\pm 20\%$

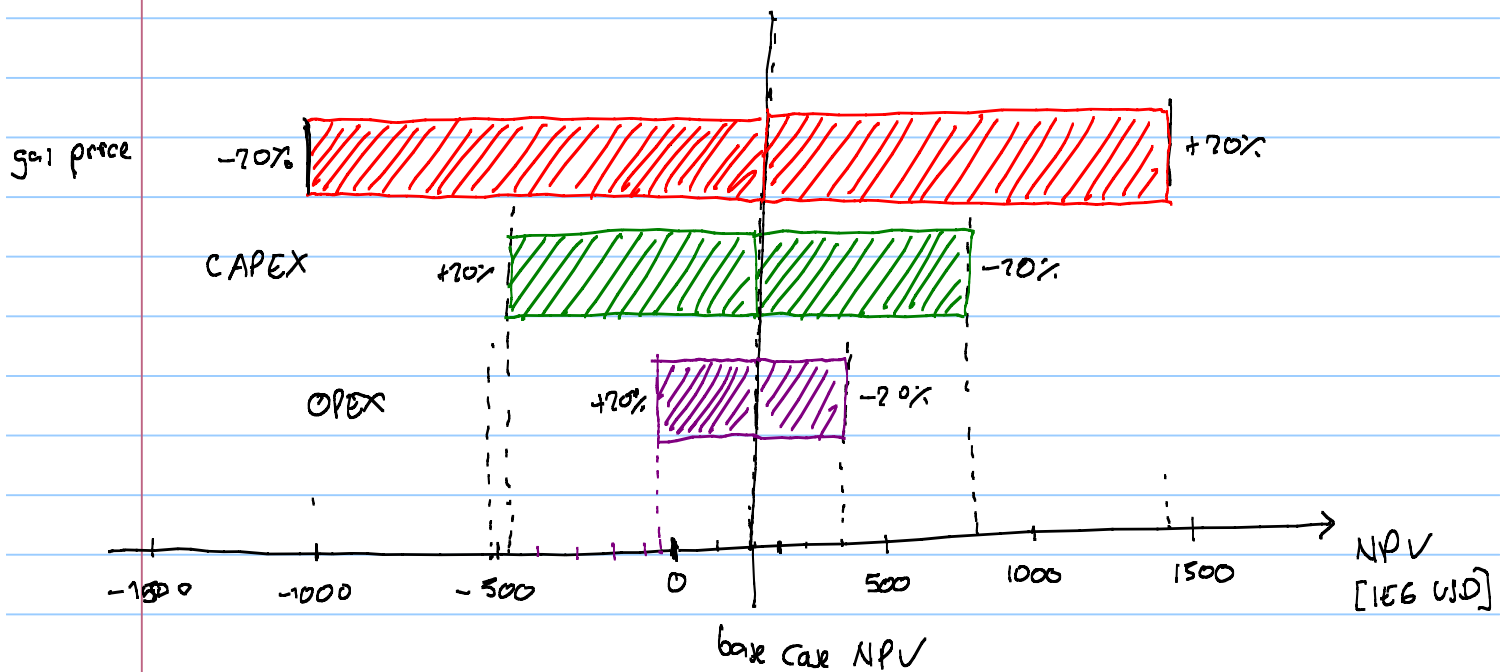
change variable ✓

↓  
 calculate NPV ✓

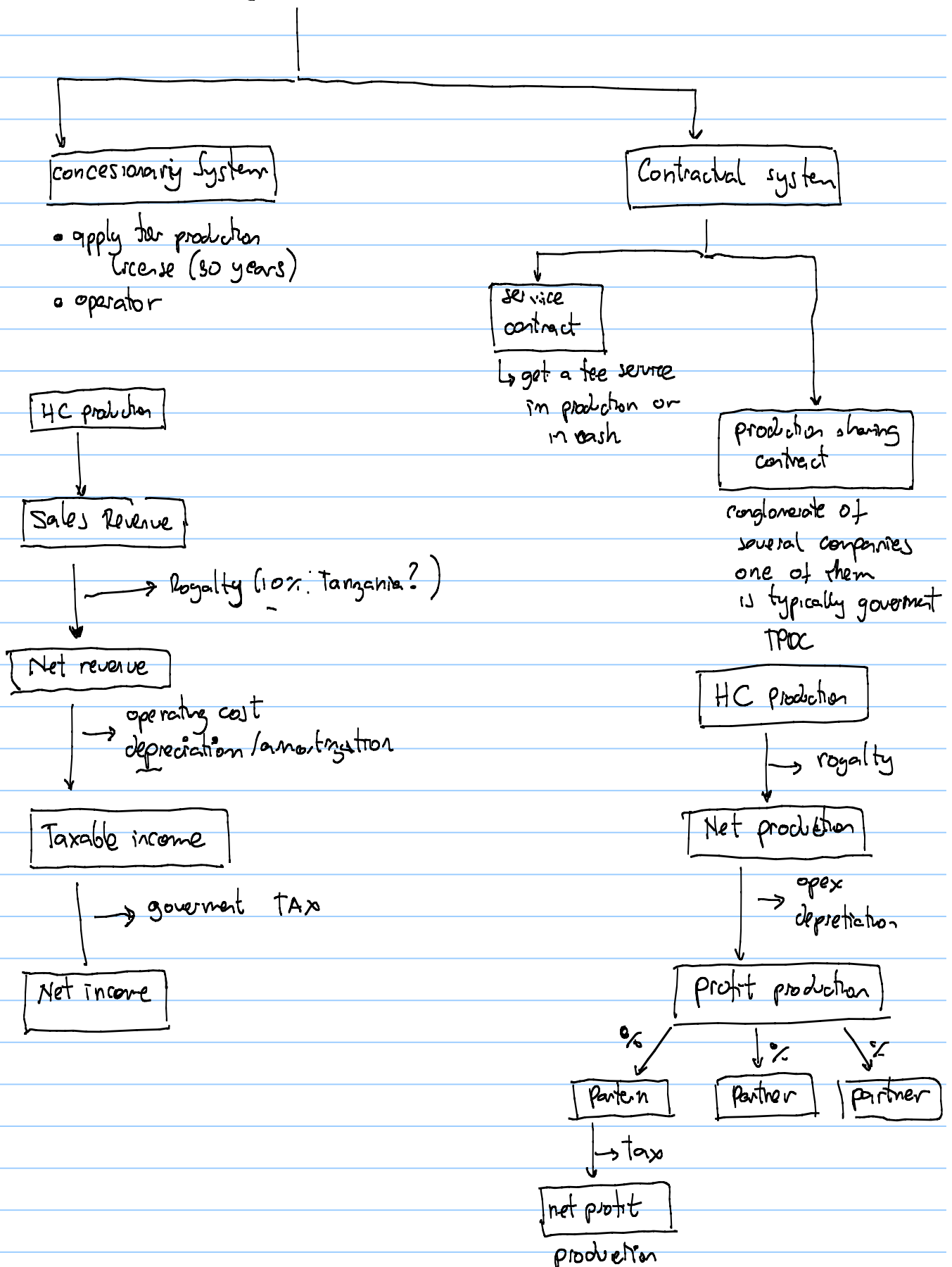
↓  
 save NPV on table

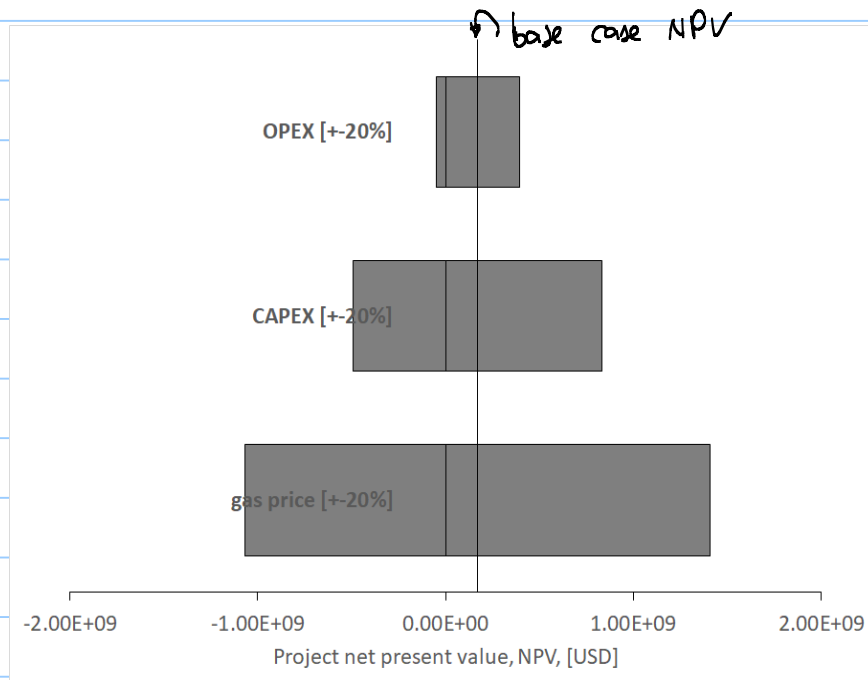
↓  
revert back to original

|                      |           |          |
|----------------------|-----------|----------|
| Base case NPV [USD]  | 1.70E+08  |          |
| Sensitivity analysis |           |          |
|                      | Low NPV   | High NPV |
| gas price [+20%]     | -1.07E+09 | 1.41E+09 |
| CAPEX [+20%]         | -4.91E+08 | 8.32E+08 |
| OPEX [+20%]          | -5.12E+07 | 3.92E+08 |

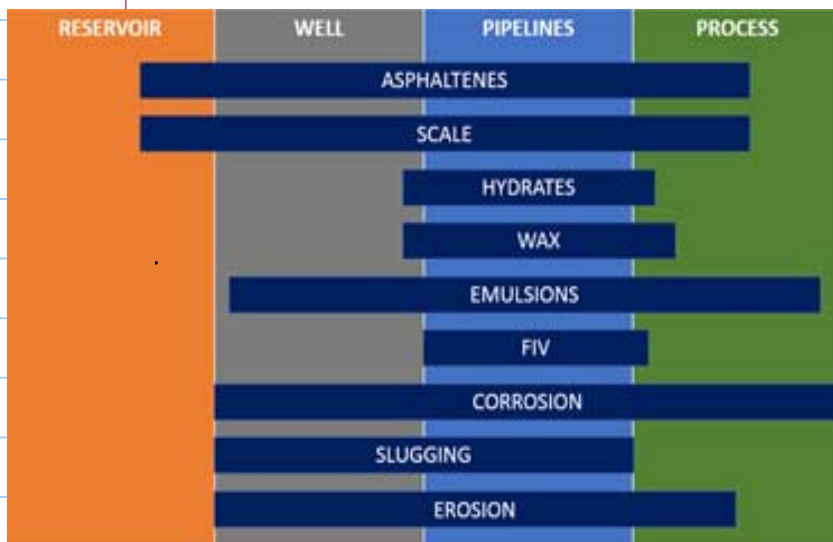


# Petroleum fiscal systems





B2 pipeline to shore

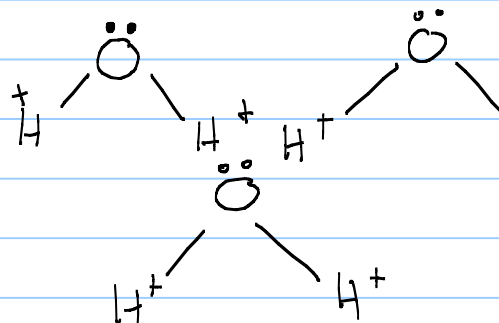


flow assurance: ensuring the uninterrupted flow of hydrocarbons from reservoir to processing facilities

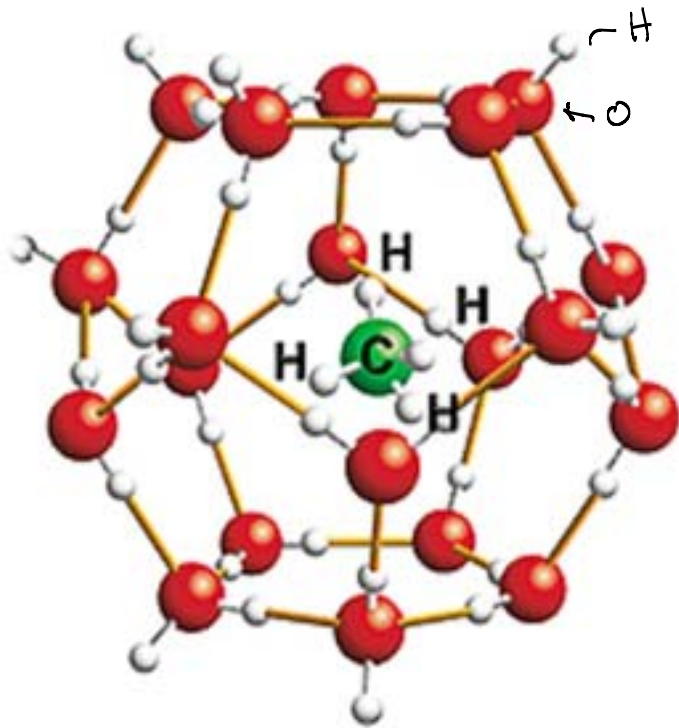
- HYDRATES (gas)
- WAX (oil)
- scaling (gas + oil)
- slugging
- corrosion
- emulsion
- foaming
- asphaltene precipitation
- erosion

Natural gas

Hydrates



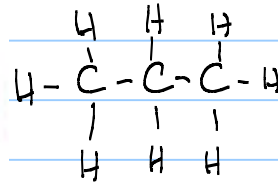




when T

$\sim 9 \text{ \AA}$   $1 \text{E}-10 \text{ m}$

small molecules go inside  
the cage  $\rightarrow$  CH<sub>4</sub>



C<sub>2</sub>H<sub>6</sub>

C<sub>3</sub>H<sub>8</sub>

CO<sub>2</sub>

N<sub>2</sub>

:

"Ice" like structure

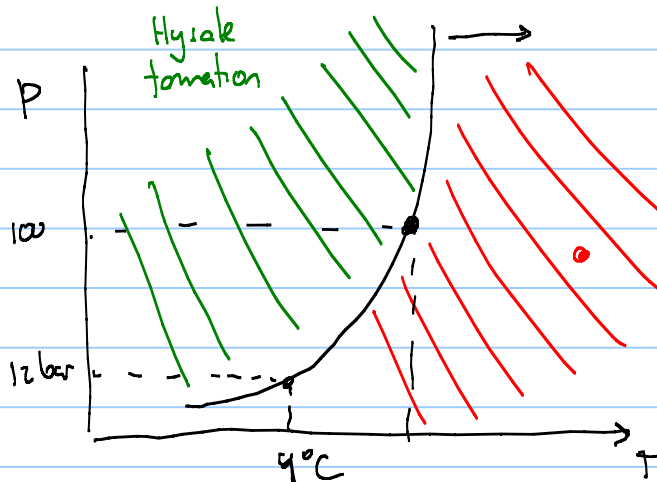


operational problem  $\rightarrow$  pipeline  
plugging

• Hydrate formation conditions

• Small HC molecules CH<sub>4</sub>  
C<sub>2</sub>H<sub>6</sub>

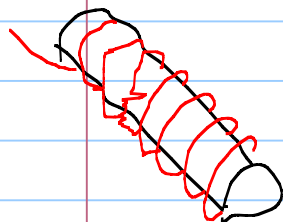
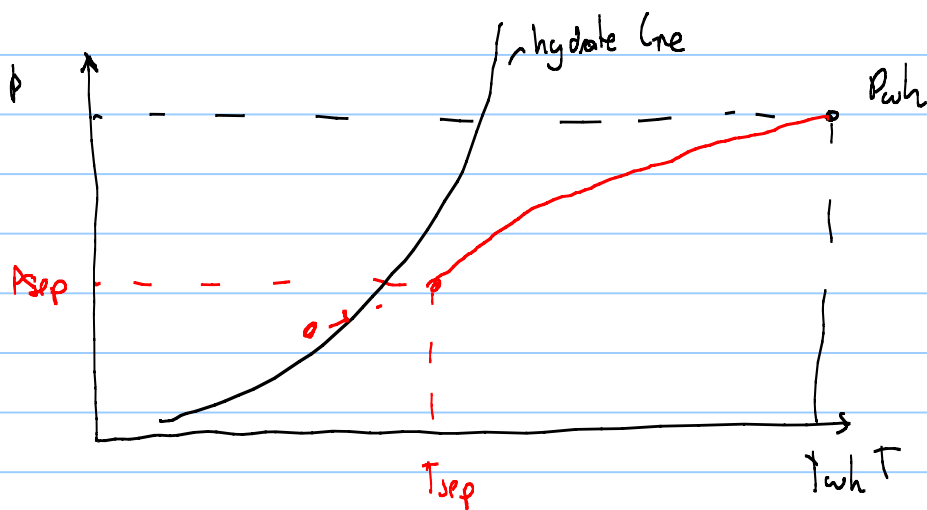
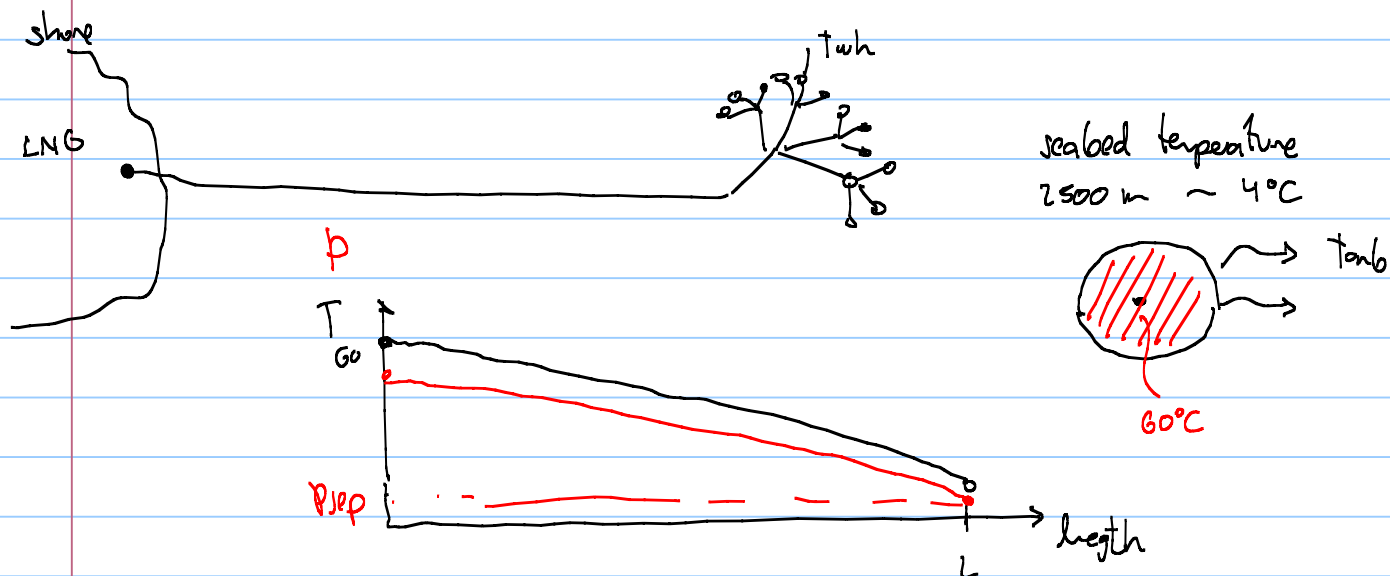
• free water  $\left\{ \begin{array}{l} \text{from reservoir} \\ \text{water condensed} \\ \text{from gas} \end{array} \right.$



• special conditions of P, T

Hydrate "free" zone

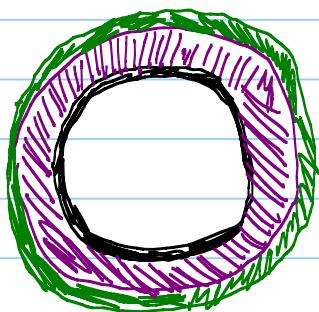
How to operate in "safe" zone  $\rightarrow$  conservative hydrate management  
 traditional hydrate management



counteracting measures:

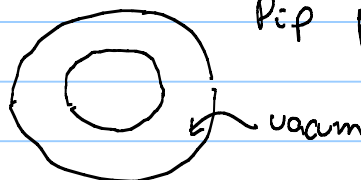
- heating pipe (heat tracing)
  - $\rightarrow$  effective for short distances (<20km)

convection (fluid)  
 conduction (solid)  
 radiation (wave)

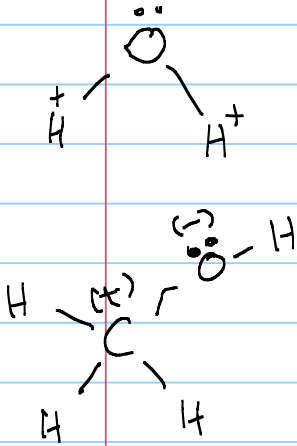
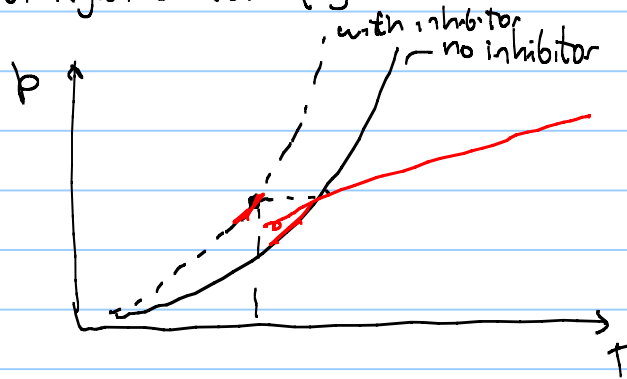


• pipe insulation

Pip pipe in pipe \$



Make hydrate formation region smaller (hydrate inhibitor)

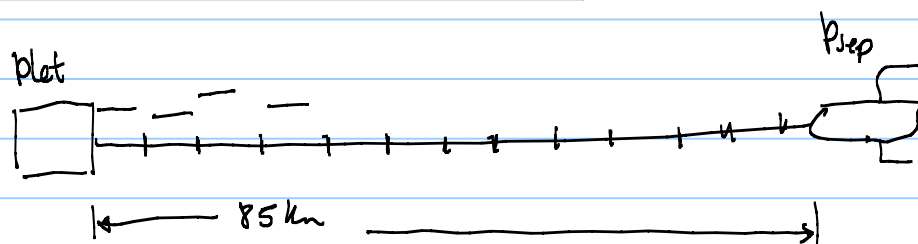
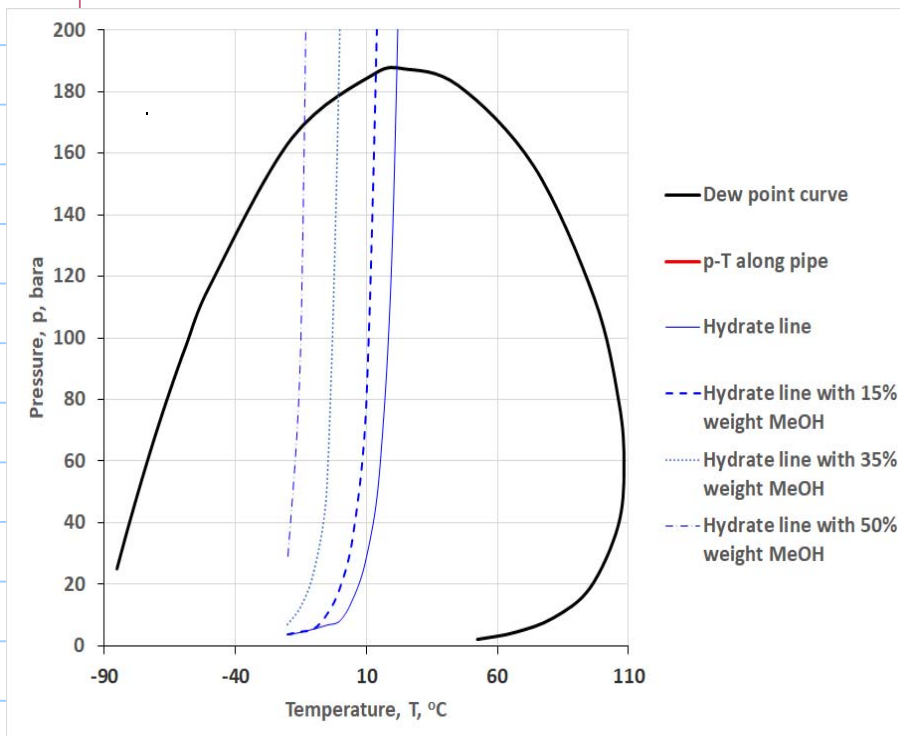


Some hydrate inhibitor: MeOH methanol

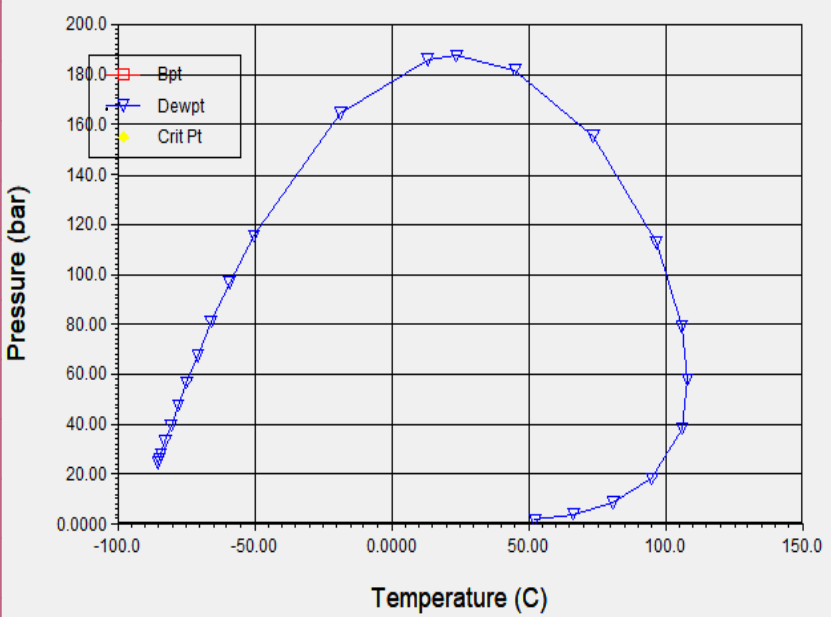
: TEG tri-ethylene glycol

: MEG mono-ethylene glycol

$$10\% < \frac{\text{inhibitor}}{\text{water} + \text{inhibitor}} < 60\%$$



$$\text{vapour mass fraction} = \text{vapour mole fraction} = \frac{\text{moles vapor}}{\text{total moles}}$$

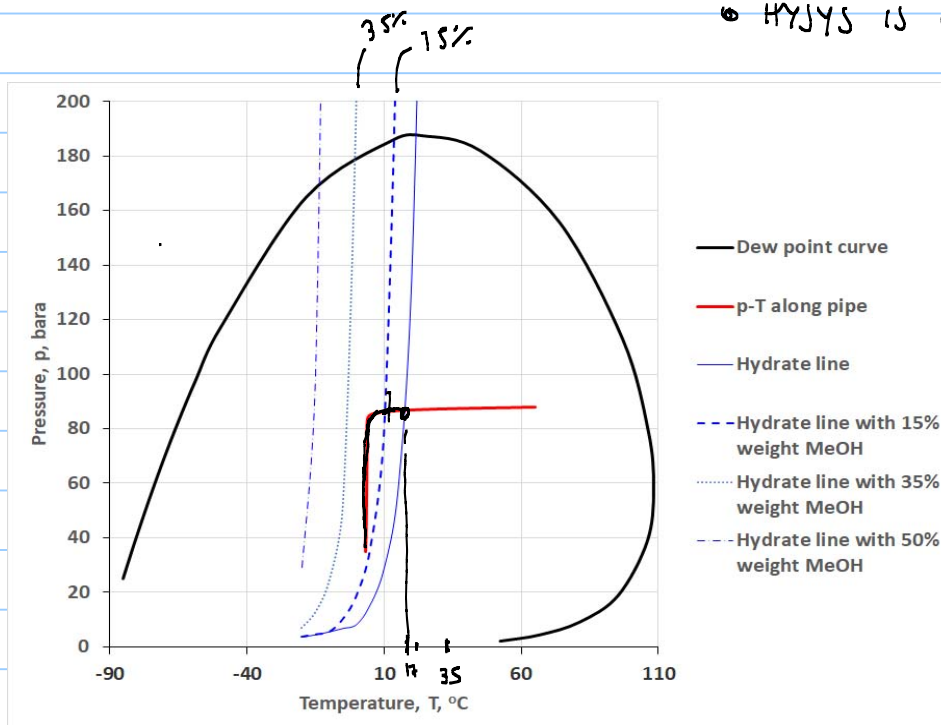


pipeline  $\Delta p$  with excel  $\approx 40$  bara  
 pipeline  $\Delta p$  with HYSYS = 53 bara

} 10% difference !

• HYSYS is considering variation of  $\rho, \eta$  along pipe

• HYSYS is considering liquid !



I need to inject 35% (weight) of inhibitor into the pipeline  
MeOH

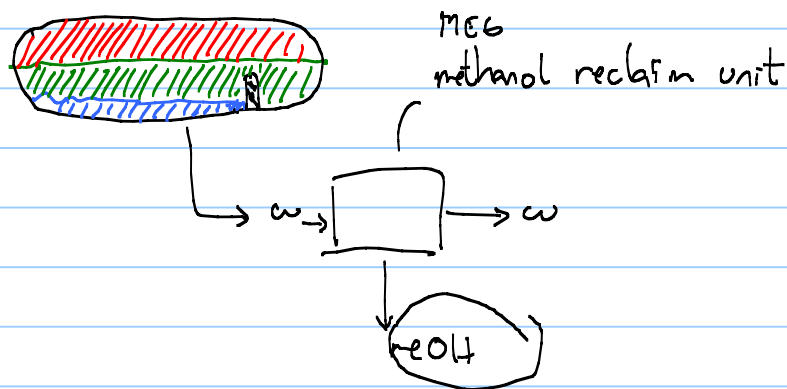
$$\left\{ \begin{aligned} 0.35 &= \frac{\dot{m}_{\text{inhibitor}}}{\dot{m}_{\text{inhibitor}} + \dot{m}_{\text{water}}} \end{aligned} \right.$$

$$\dot{m}_{\text{water}} = q_w \cdot \rho_w = 69 \frac{\text{m}^3}{\text{d}} \cdot 854 \frac{\text{kg}}{\text{m}^3} = \left( \frac{\text{kg}}{\text{d}} \right)$$

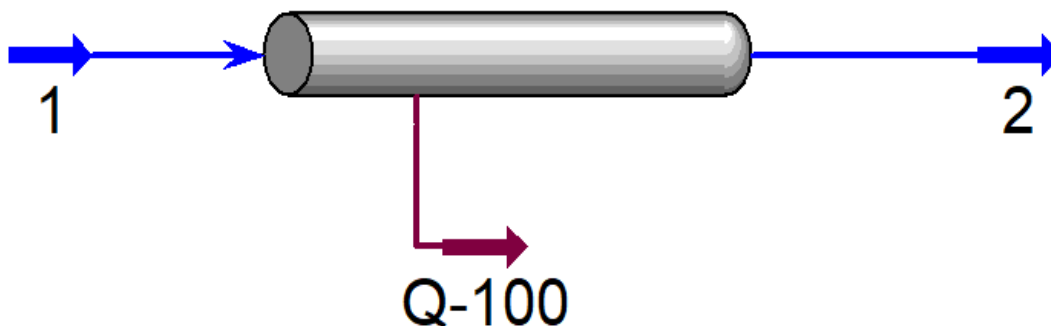
$$\dot{m}_{\text{inhibitor}} (1 - 0.35) = 0.35 \dot{m}_{\text{water}}$$

$$\dot{m}_{\text{inhibitor}} = \frac{(0.35)}{(1 - 0.35)} \cdot \dot{m}_{\text{water}}$$

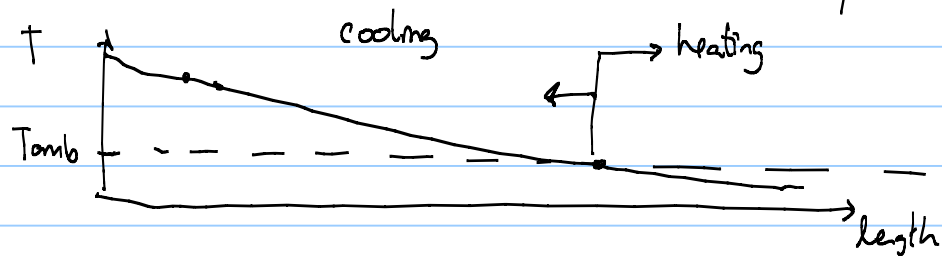
$$\dot{m}_{\text{inhibitor}} = 0.54 \cdot 59000 \frac{\text{kg}}{\text{d}} = \underline{\underline{35000 \frac{\text{kg}}{\text{d}}}}$$



PIPE-100



in gas pipelines  $T$  can go below ambient temperature



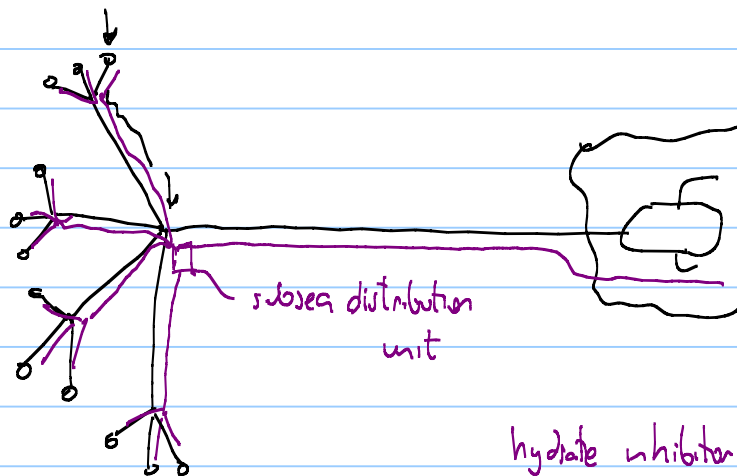
Joule Thompson effect

$$\frac{dh}{dx} = \frac{dT}{dx} \frac{dh}{dT} + \frac{dp}{dx} \frac{dh}{dp}$$

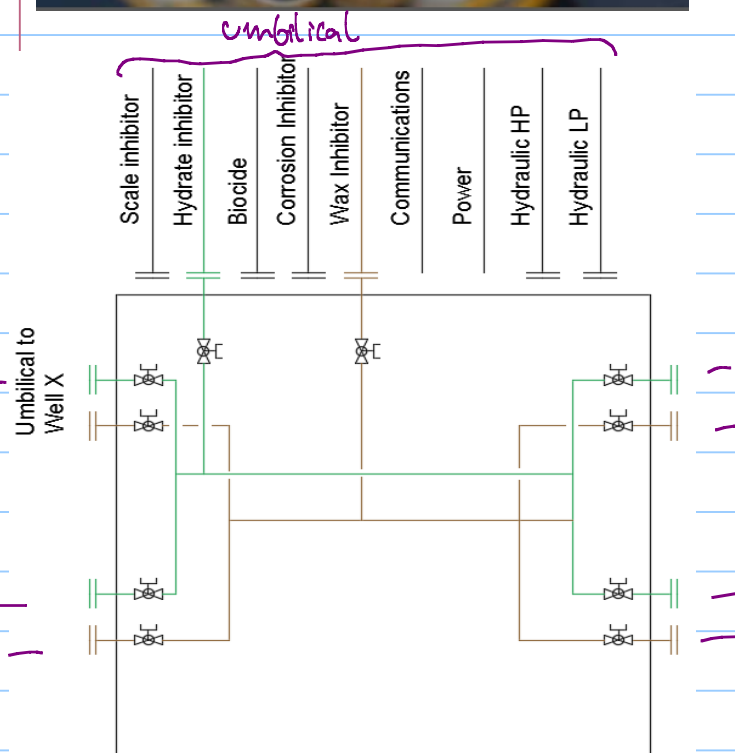
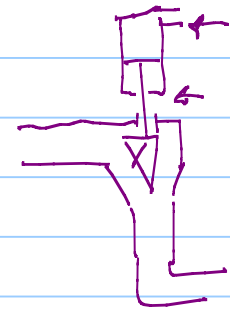
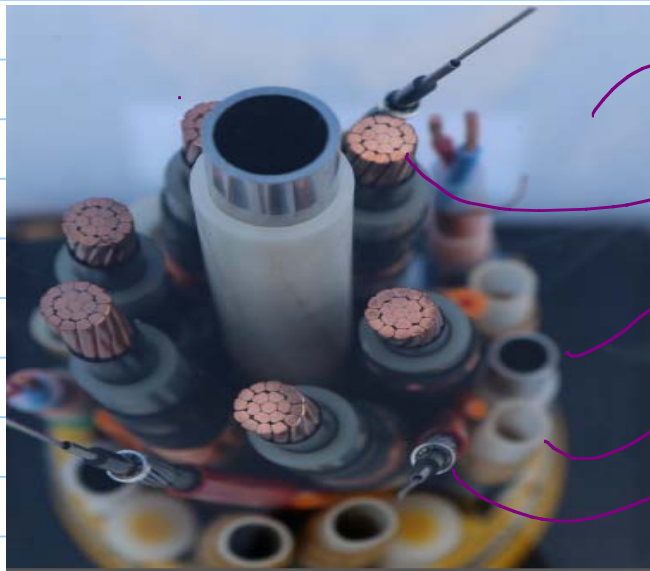
↑  
more relevant in liquid and in gas + lots of liquid

① → [ ] → ②

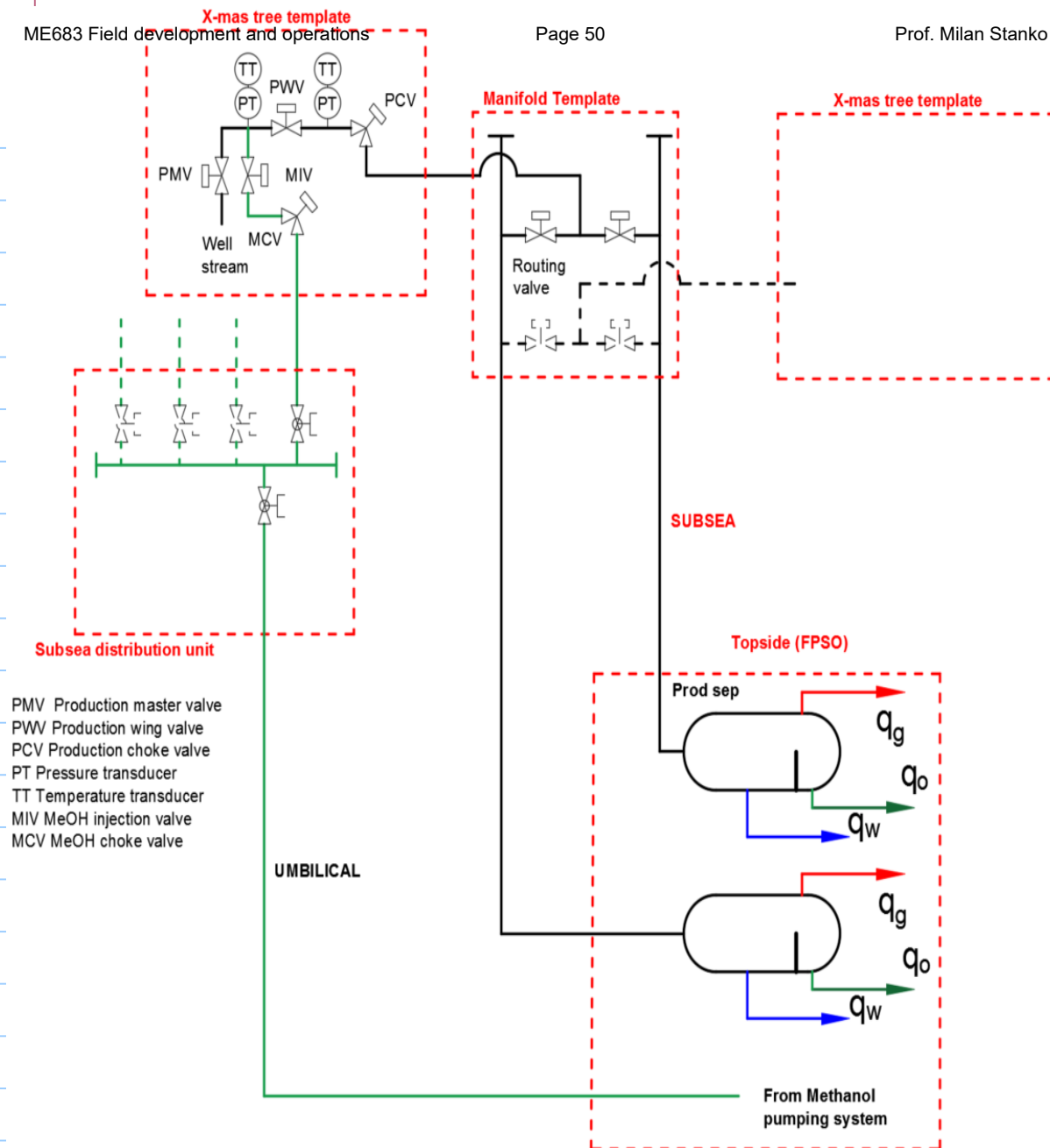
$mh(h_2 - h_1) = \dot{Q}$



hydrate inhibitor are injected with umbilical







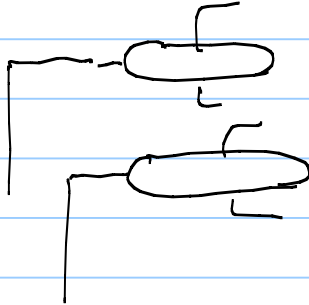
Note Title

06.12.2018

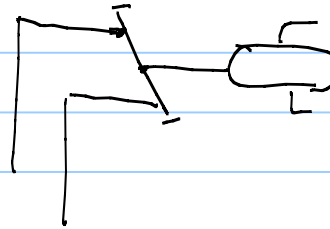
Day 4

Gathering system / comingling system

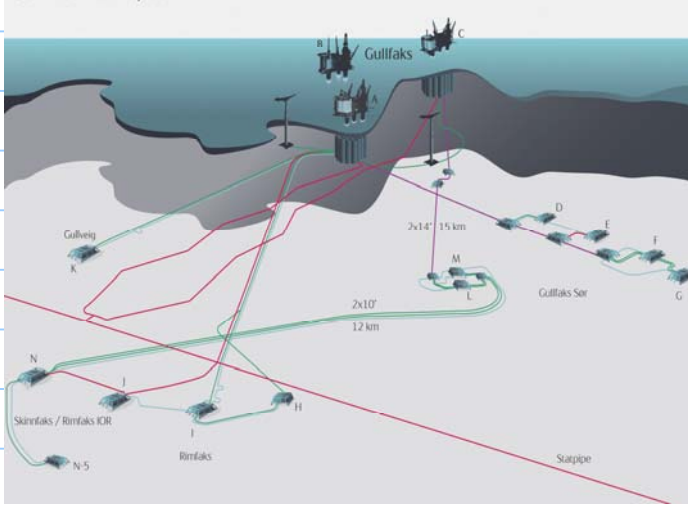
Networks  $\rightarrow$  collection/system of pipes, flowlines and pipelines that take production from wells to processing facilities.



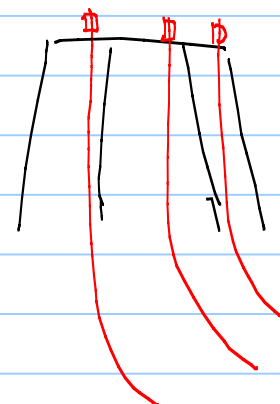
standalone wells

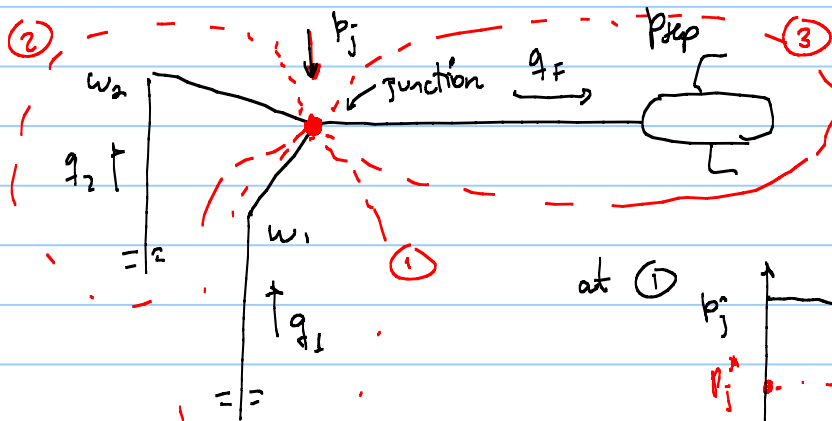
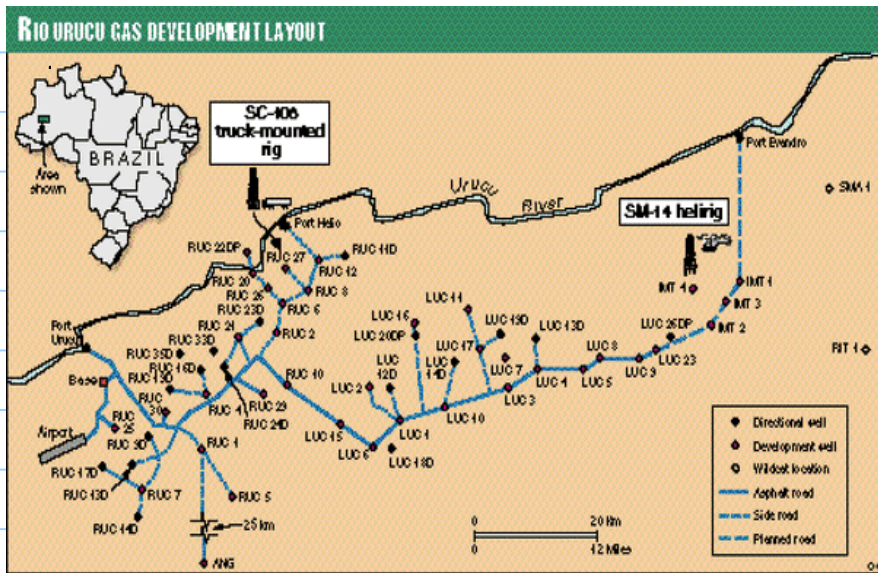


Gullfaks field lay out



subsea systems





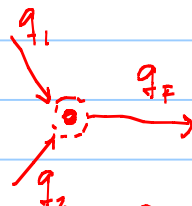
Solving process

1. Assume  $p_j^*$

in curve ① read  $q_1^*$

In curve ② read  $q_2^*$

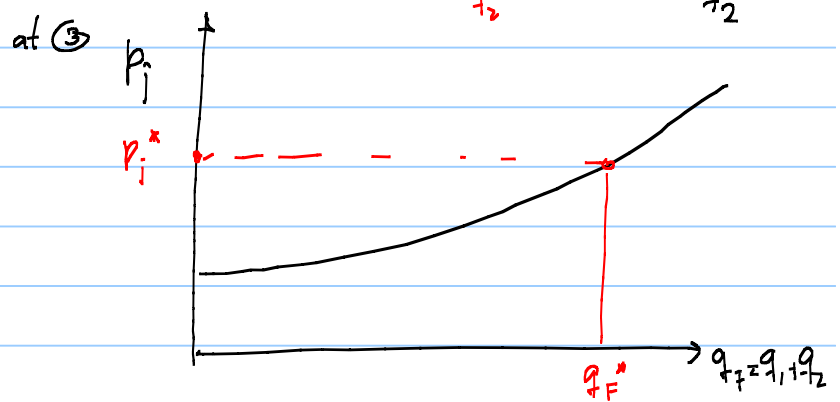
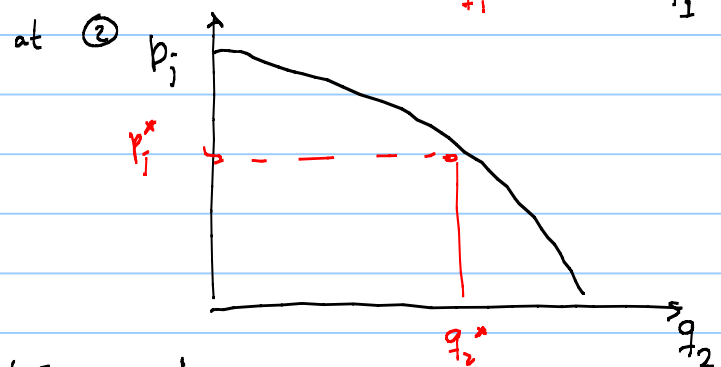
in curve ③ read  $q_F^*$



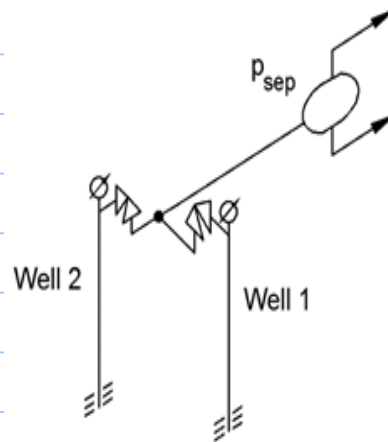
$$q_F = q_1 + q_2$$

verify  $q_F^* = q_1^* + q_2^*$

yes → solution

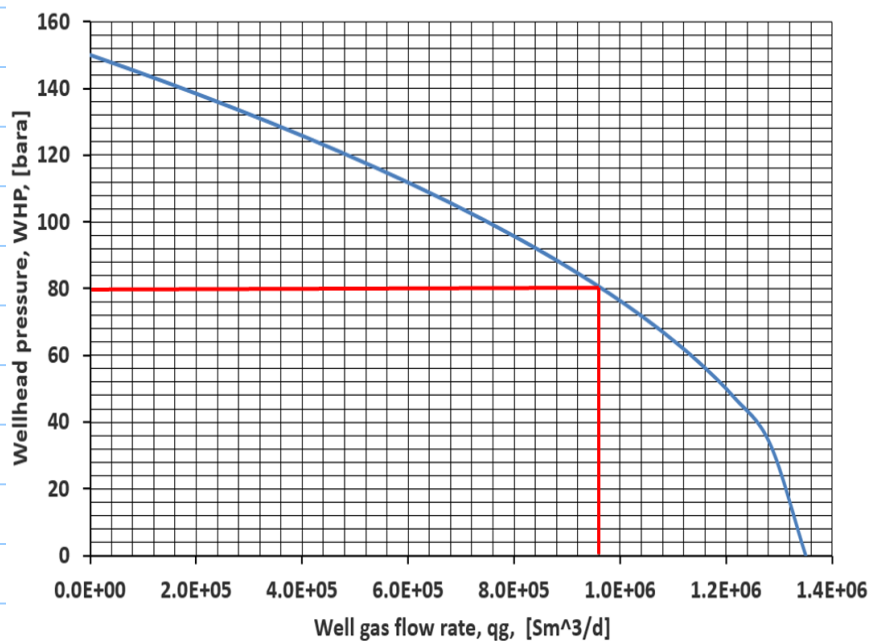


ch3 exercise:



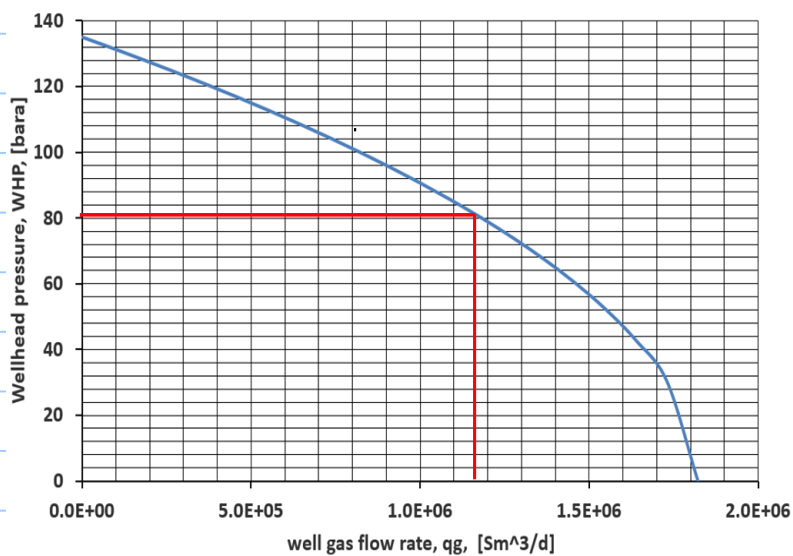
iteration 1

wellhead performance relationship - Well 1



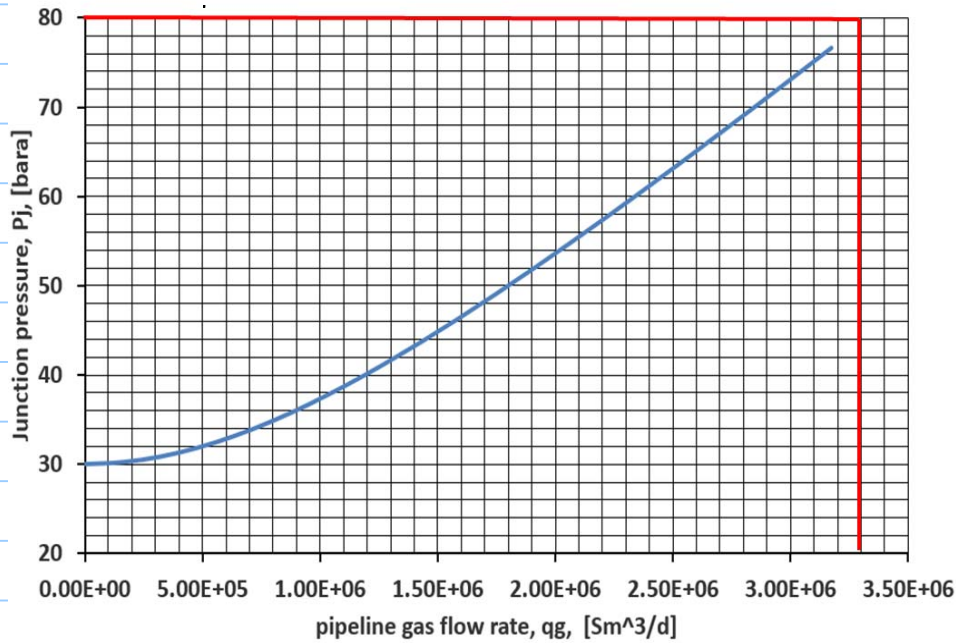
assume  $p_i^* = 80 \text{ bara}$   
 $q_1^* = 9.6 \times 10^5 \text{ Sm}^3/\text{d}$

wellhead performance relationship - Well 2



$p_i^* = 80 \text{ bara}$   
 $q_2^* = 1.1 \times 10^6 \text{ Sm}^3/\text{d}$

Pipeline performance relationship



$$P_j^* = 80 \text{ bara}$$

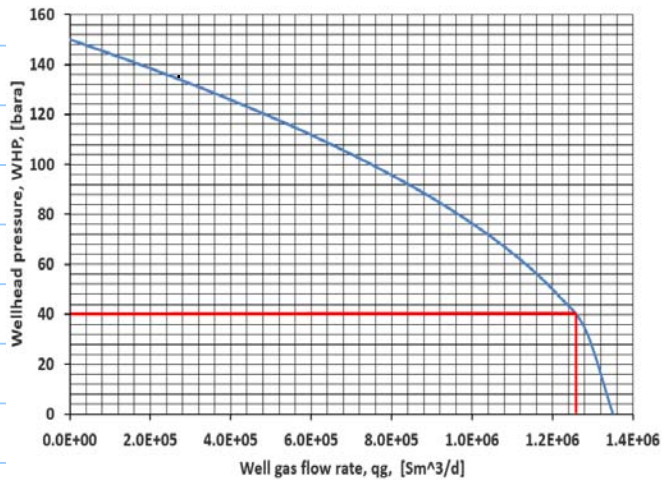
$$q_F^* = 3.3 \times 10^6 \text{ Sm}^3/\text{d}$$

$$\underbrace{9.6 \times 10^5 \text{ Sm}^3/\text{d} + 1.17 \times 10^6 \text{ Sm}^3/\text{d}}_{\text{Second iteration}} \stackrel{?}{=} 3.3 \times 10^6 \text{ Sm}^3/\text{d} \quad \begin{aligned} E &= (q_F - q_1 - q_2) \\ E^{(1)} &= 1.17 \times 10^6 \text{ Sm}^3/\text{d} \end{aligned}$$

Second iteration

$$P_j^* = 40 \text{ bara}$$

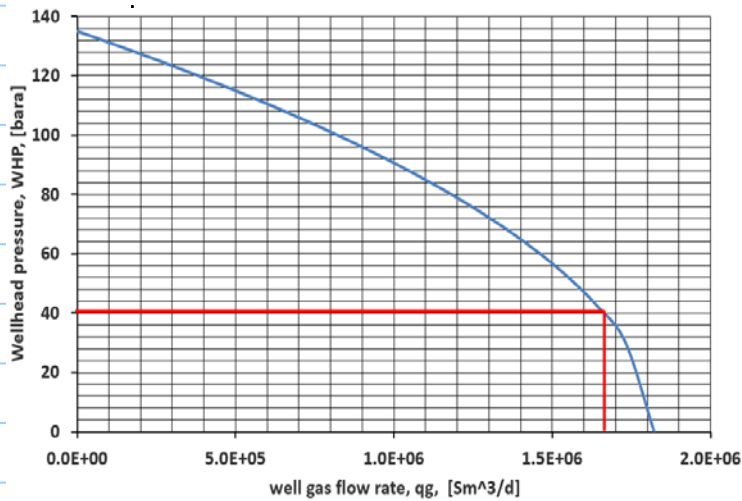
wellhead performance relationship - Well 1



$$P_j^* = 40 \text{ bara}$$

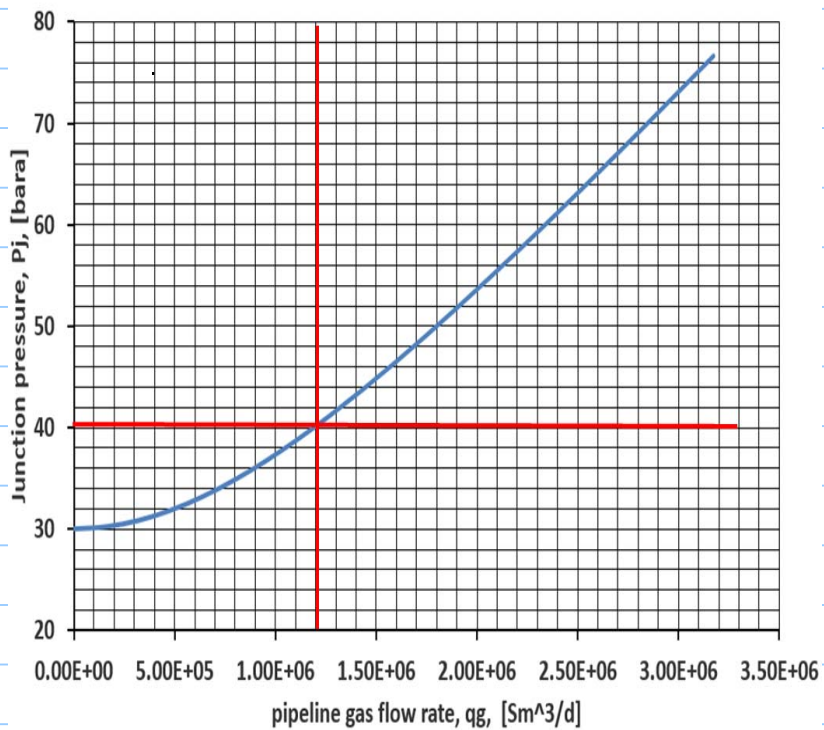
$$q_{g1}^* = 1.25 \times 10^6 \text{ Sm}^3/\text{d}$$

wellhead performance relationship - Well 2



$$q_2^* = 1.67 \text{ E}6 \text{ Sm}^3/\text{d}$$

Pipeline performance relationship

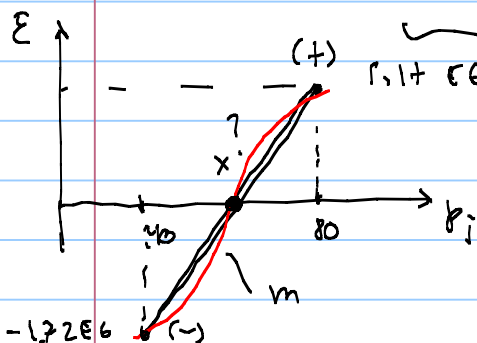


$$q_F = 1.2 \text{ E}6 \text{ Sm}^3/\text{d}$$

$$q_1^* + q_2^* \stackrel{?}{=} q_F$$

$$1.25 \text{ E}6 \text{ Sm}^3/\text{d} + 1.67 \text{ E}6 \text{ Sm}^3/\text{d} = 1.2 \text{ E}6 \text{ Sm}^3/\text{d}$$

$$\varepsilon^L = -1.72 \text{ E}6 \text{ Sm}^3/\text{d}$$





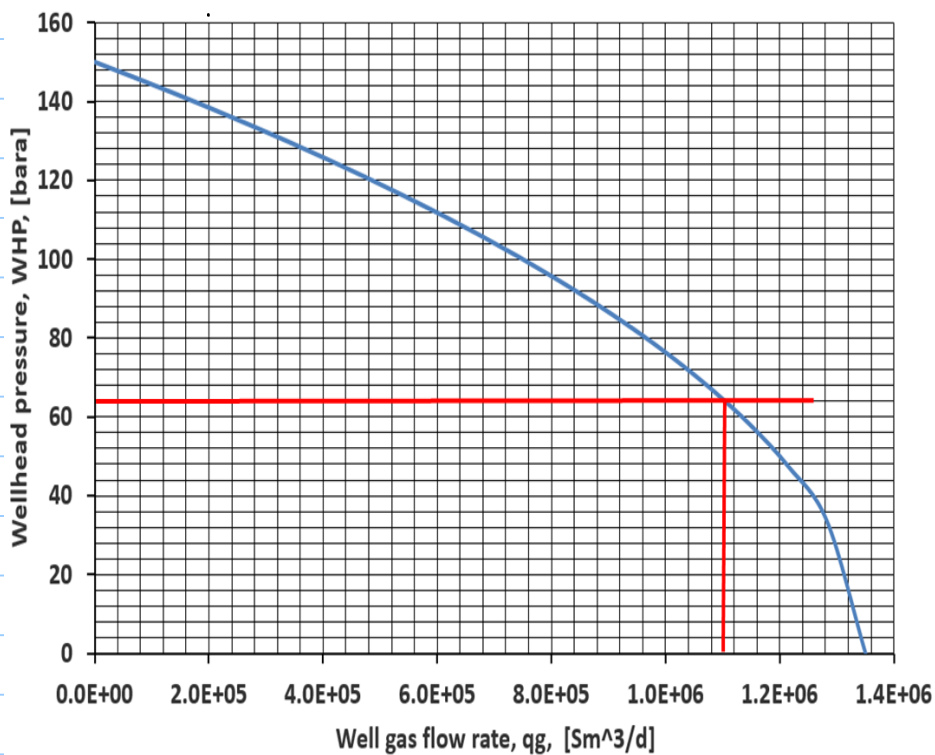
$$m = \frac{y_2 - y_1}{x_2 - x_1} = \frac{1.17 \text{ Eg} - (-1.72 \text{ Eg})}{80 - 40} = 0.07225 \text{ Eg}$$

$$m = \frac{y_2 - y}{x_2 - x} = \frac{1.17 \text{ Eg} - 0}{80 - x} = 0.07225 \text{ Eg}$$

$$x = 80 - \frac{1.17 \text{ Eg}}{0.07225 \text{ Eg}} = 63.8 \text{ bara}$$

Iteration 3  $p_j^* = 64 \text{ bara}$

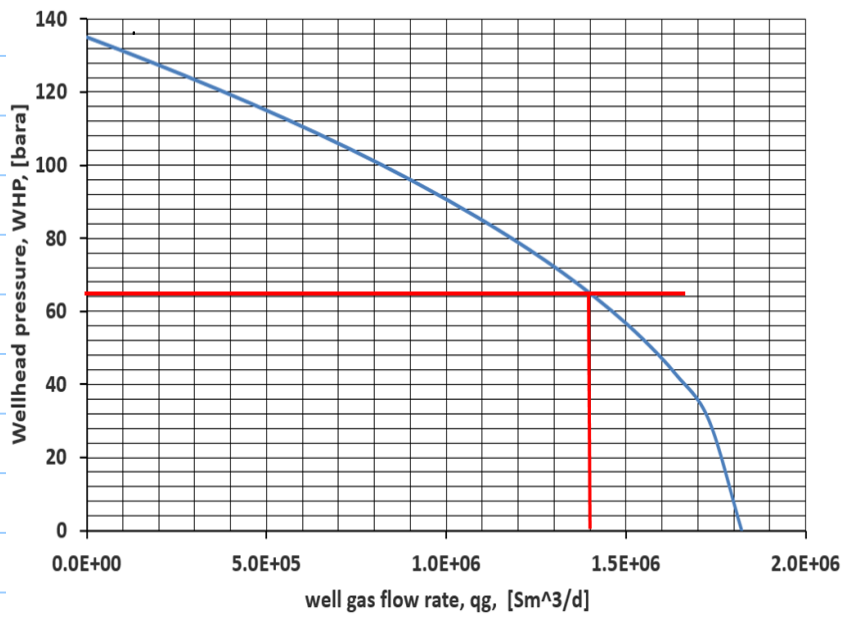
wellhead performance relationship - Well 1



$$q_1 = 1.1 \text{ Eg Sm}^3/\text{d}$$

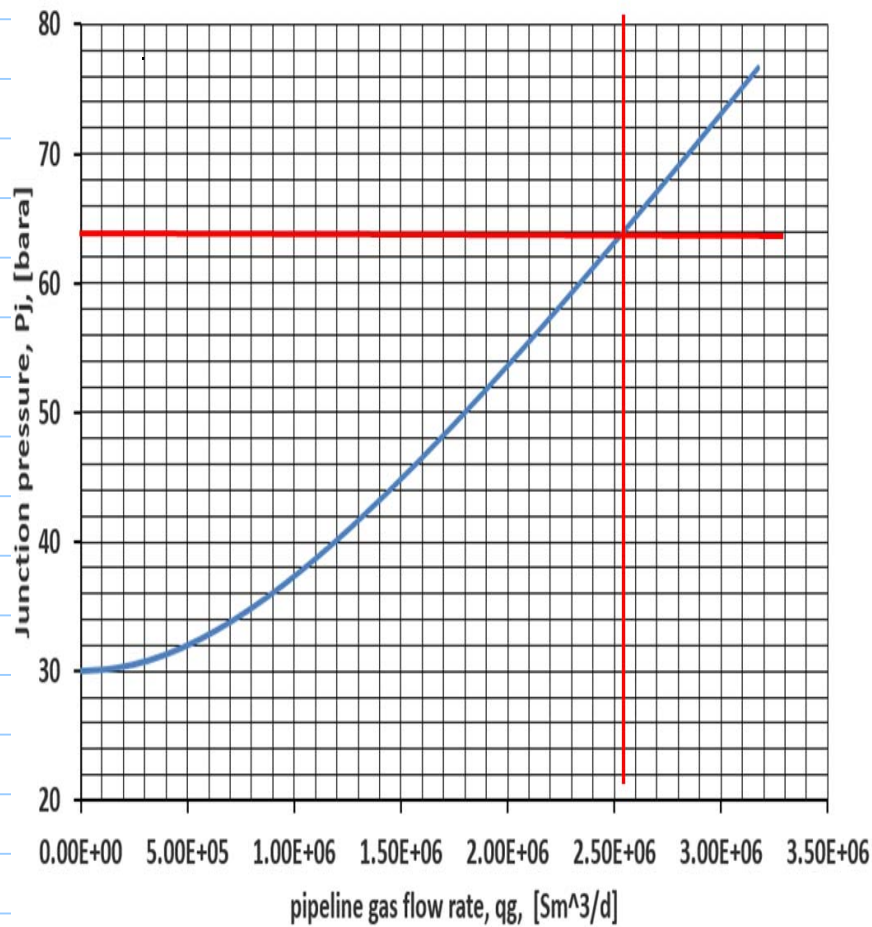


wellhead performance relationship - Well 2



$$q_2 = 1.4 \text{ E}6 \text{ Sm}^3/\text{d}$$

Pipeline performance relationship

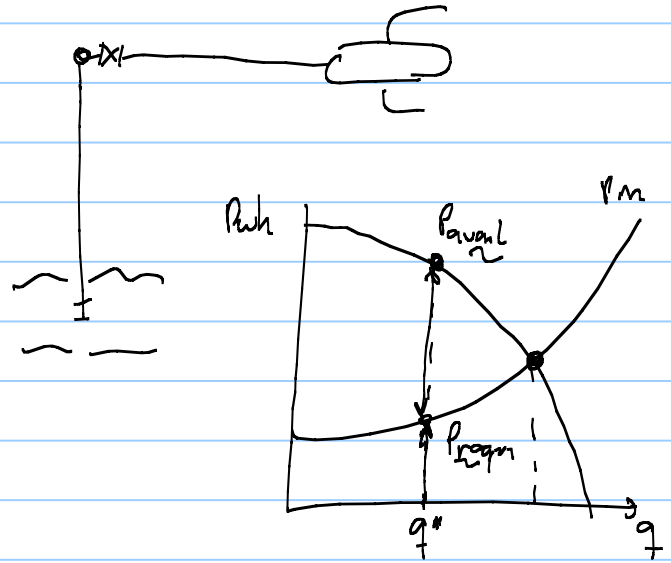


$$q_F = 2.55 \text{ E}6 \text{ Sm}^3/\text{d}$$

$$P_j = q_F = 2.55 \text{ Sm}^3/\text{d}$$

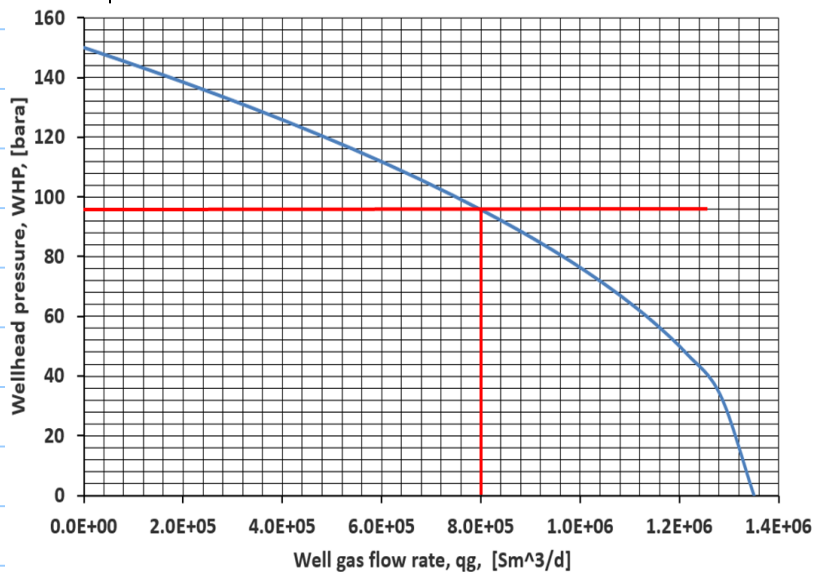
$$\begin{aligned} 1.1 \text{ E}6 + 1.4 \text{ E}6 &= 2.55 \text{ E}6 \\ 2.5 &= 2.55 \end{aligned} \quad \checkmark$$

According to reservoir engineer  
 $8.5 \text{ Sm}^3/\text{d} > q_1$   
 $1.6 \text{ Sm}^3/\text{d} > q_2$

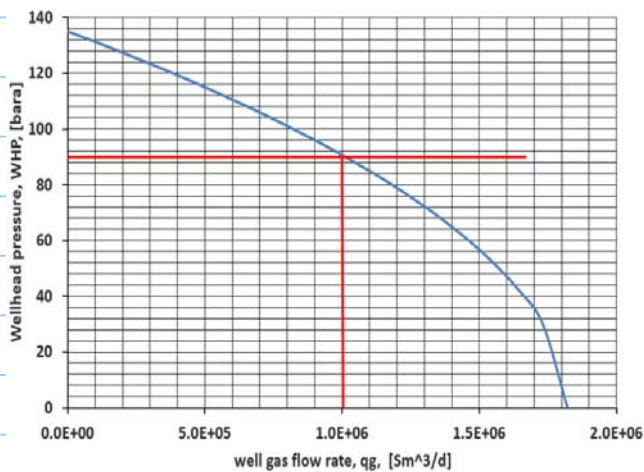


$P_{wh \text{ available } (w_1)} = 96 \text{ bara}$

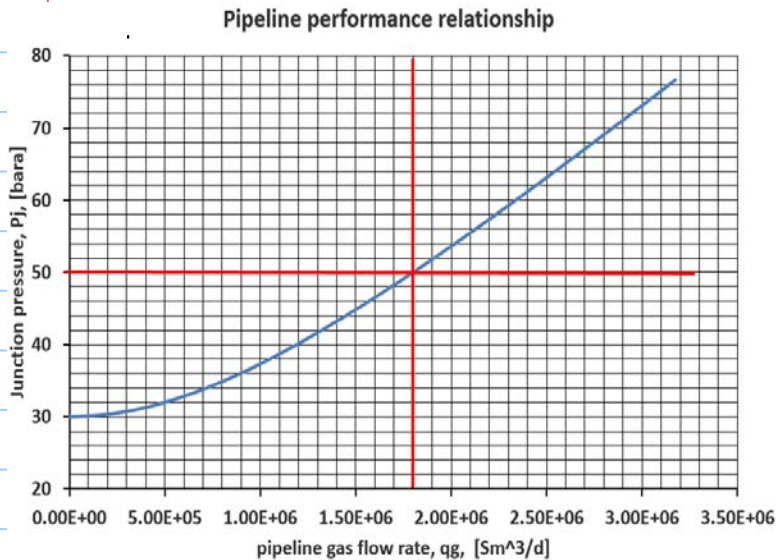
wellhead performance relationship - Well 1



wellhead performance relationship - Well 2



$P_{wh \text{ available } 2} = 90 \text{ bara}$



$$P_{in, \text{flowline}} = 50 \text{ bara}$$

$$P_{wh1} = 96 \text{ bara}$$

$$P_{wh2} = 90 \text{ bara}$$

$$P_{in} = 50 \text{ bara}$$

$$\left. \begin{array}{l} P_{wh1} > P_{in} \\ P_{wh2} > P_{in} \end{array} \right\} \text{the nodes are feasible}$$

$$\Delta p_{chone1} = 96 - 50 = 46 \text{ bar}$$

$$\Delta p_{chone2} = 90 - 50 = 40 \text{ bar}$$

|              |                                                                                   | unknowns | equations |
|--------------|-----------------------------------------------------------------------------------|----------|-----------|
| $w1$         | $\dot{q}_{g1} = C_{r1} (P_{R1}^2 - P_{wh1}^2)^{n1}$                               | 2        | 1         |
|              | $\dot{q}_{g1} = C_{T1} \left( \frac{P_{wh1}^2}{e^{f1}} - P_{wh1}^2 \right)^{0.5}$ | 1        | 1         |
| $w2$         | $\dot{q}_{g2} = C_{r2} (P_{R2}^2 - P_{wh2}^2)^{n2}$                               | 2        | 1         |
|              | $\dot{q}_{g2} = C_{T2} \left( \frac{P_{wh2}^2}{e^{f2}} - P_{wh2}^2 \right)^{0.5}$ | 1        | 1         |
| flowline     | $\dot{q}_F = C_{F2} (P_{in}^2 - P_{sep}^2)^{0.5}$                                 | 2        | 1         |
| mass balance | $\dot{q}_F = \dot{q}_1 + \dot{q}_2$                                               | 0        | 1         |
|              | $P_{in} = P_{wh1}$                                                                | 0        | 1         |
|              | $P_{in} = P_{wh2}$                                                                | 0        | 1         |

8 equations and 8 unknowns !

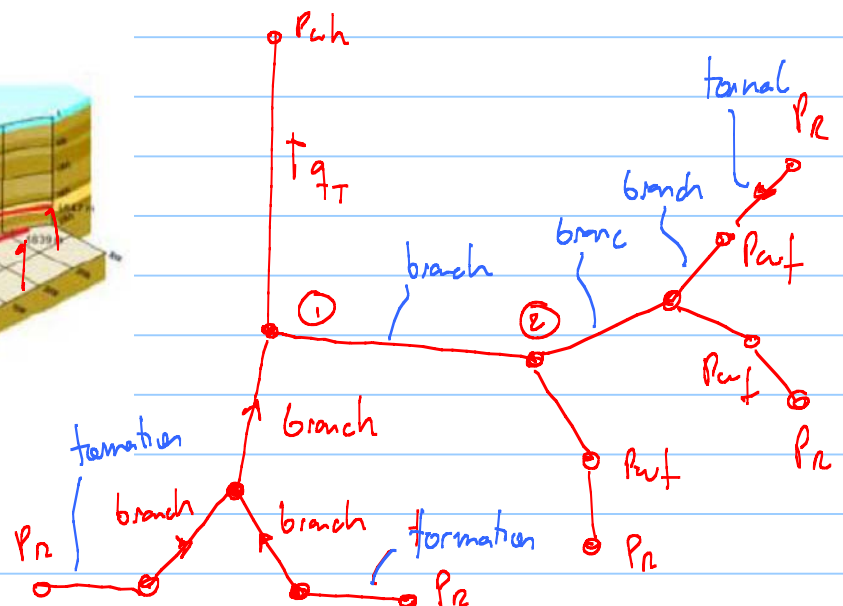
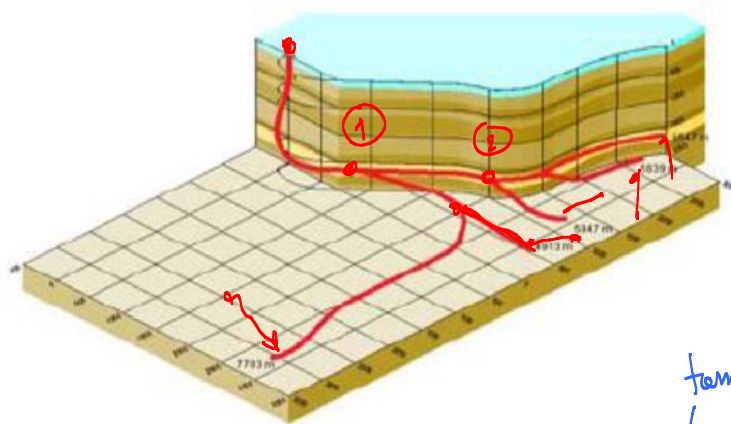
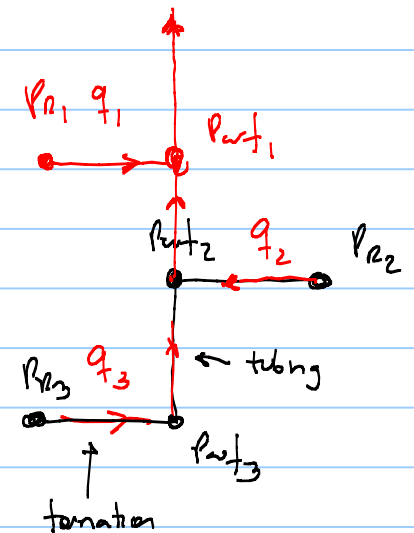
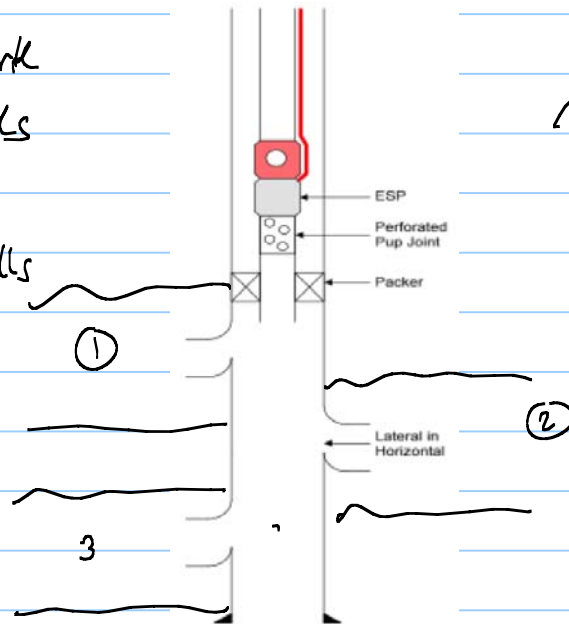
there are other types of network in petroleum production systems

injection networks



distributing network  
Downhole Networks

multi-zone wells



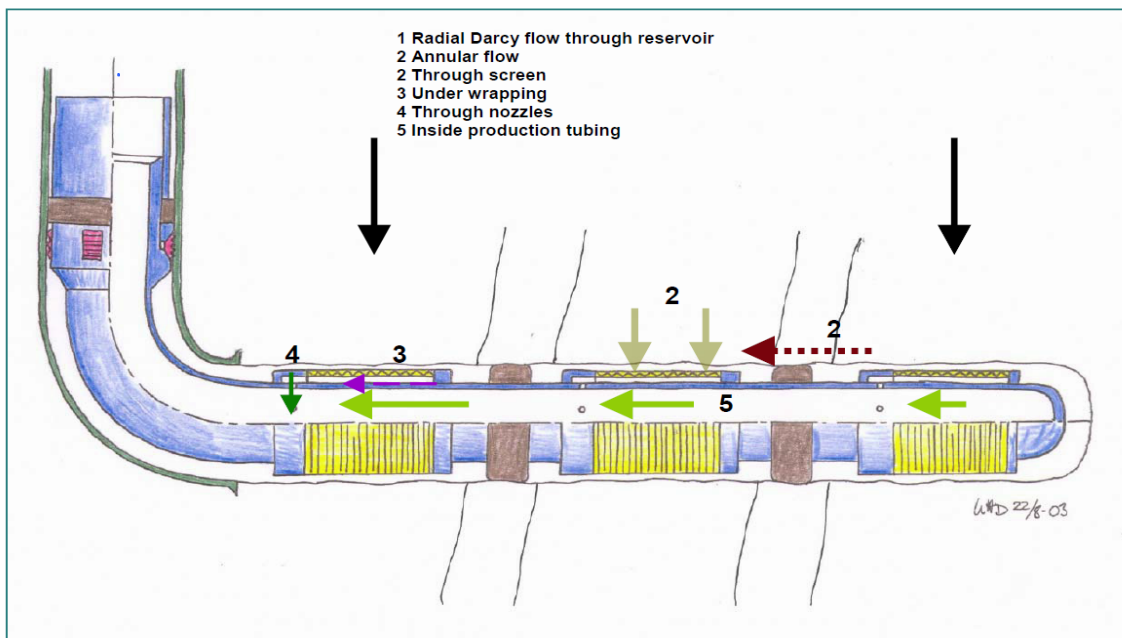
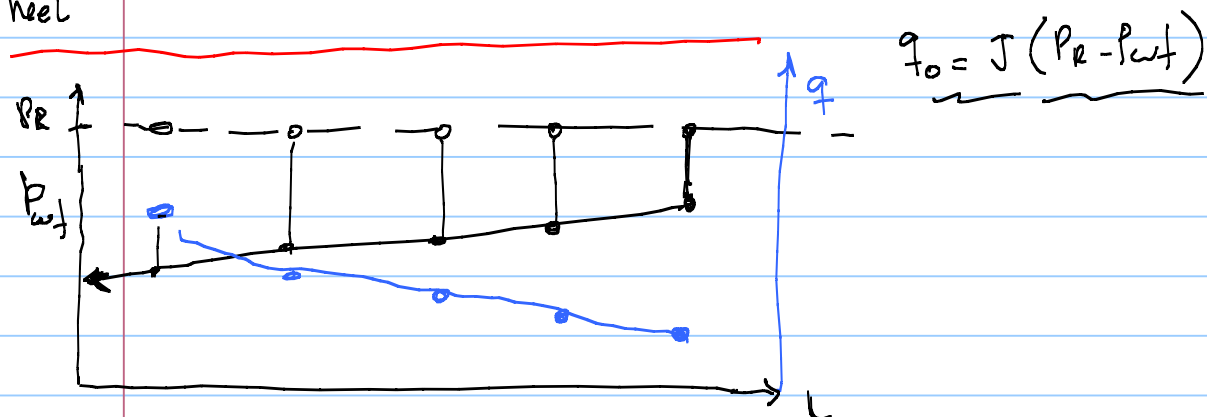
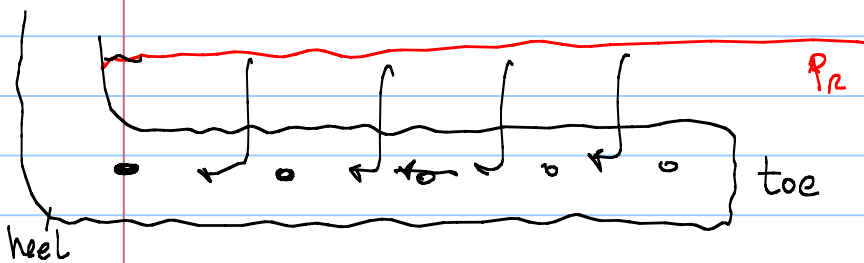
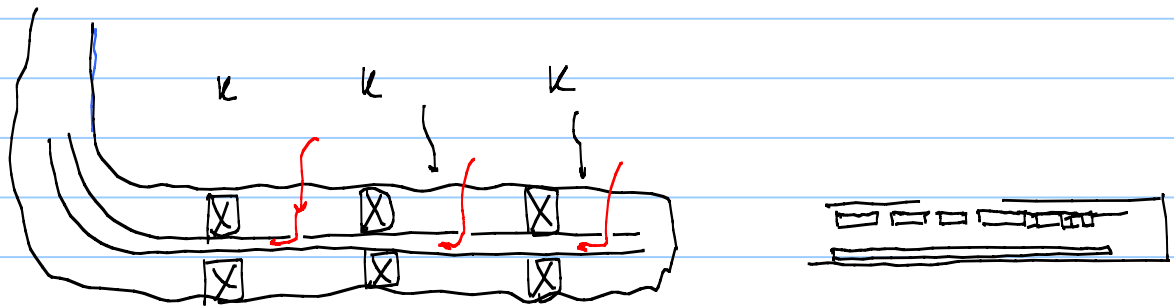
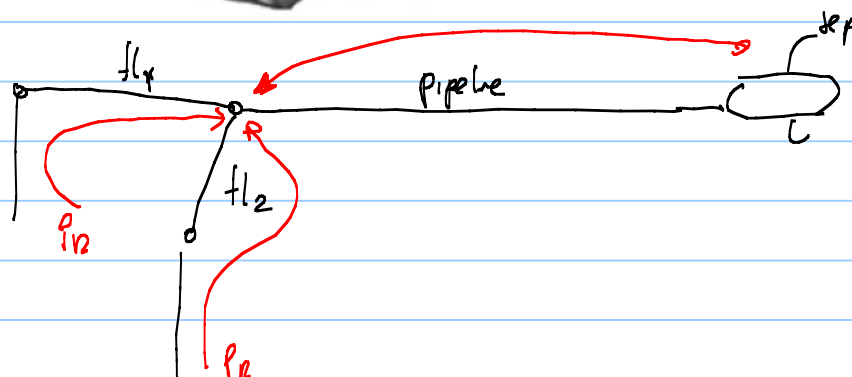
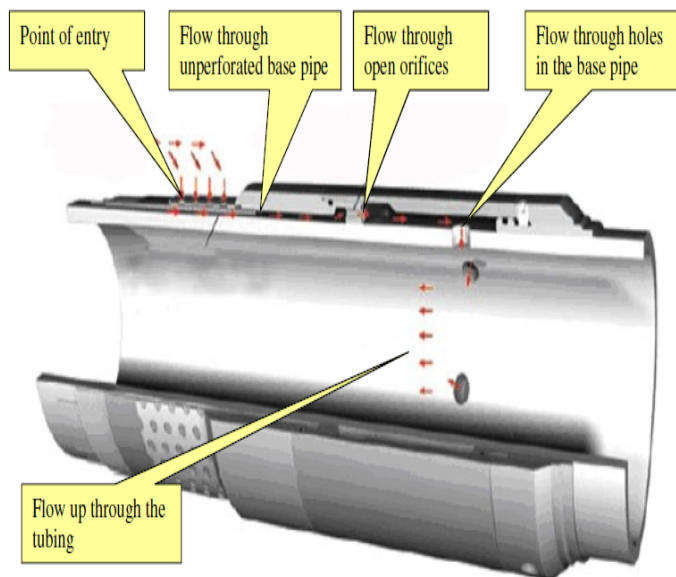
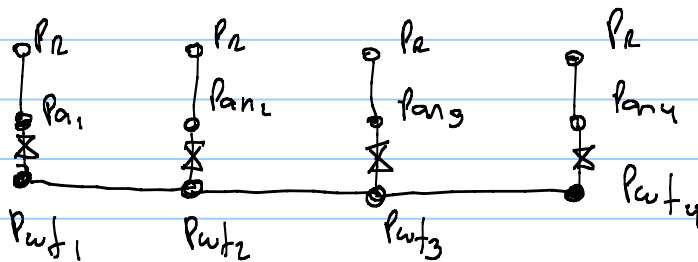
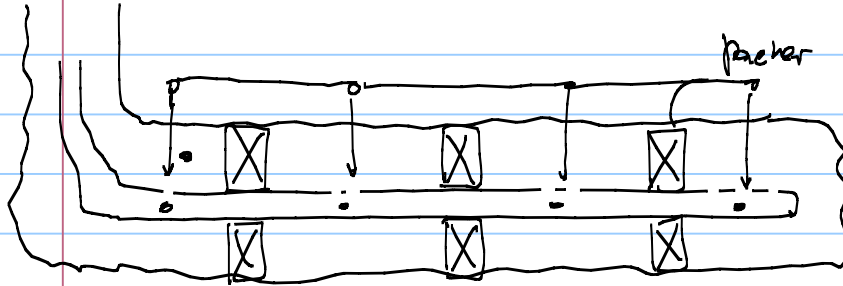
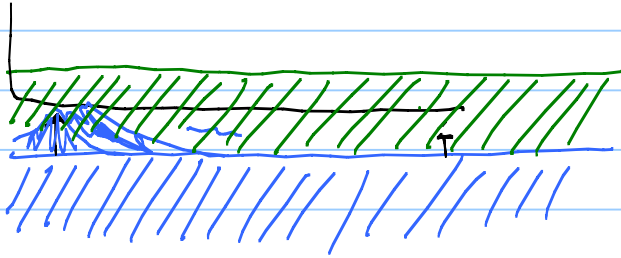


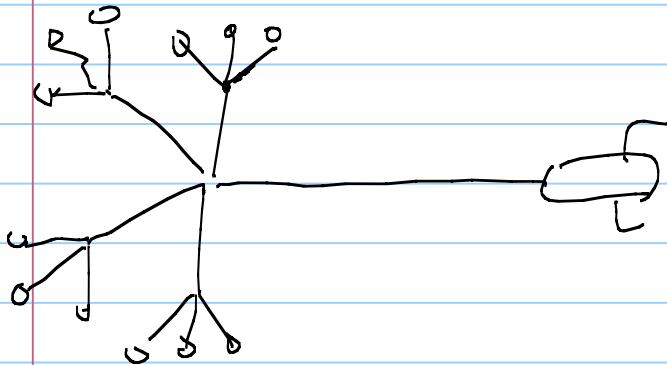
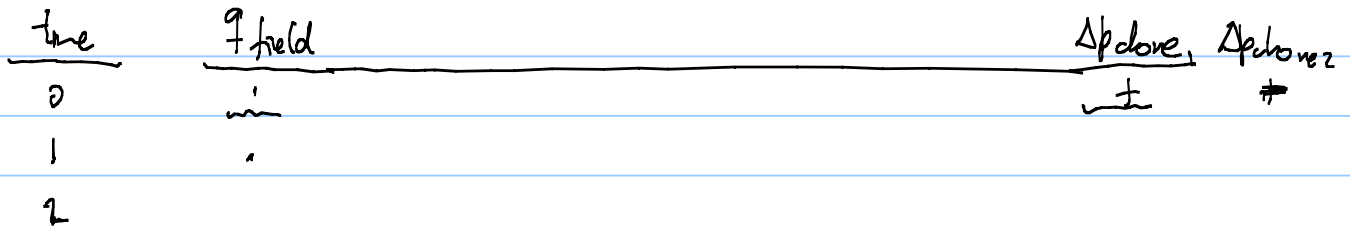
Figure-8 Functioning and interplay of an ICD completion architecture. Fluids enter the screen and flow between the axial wires and the un-perforated base pipe into the ICD housing, before passing through the nozzles and entering into the base pipe. All these flow issues are properly analyzed and put in the right perspective to achieve an optimal well completion design and solution.



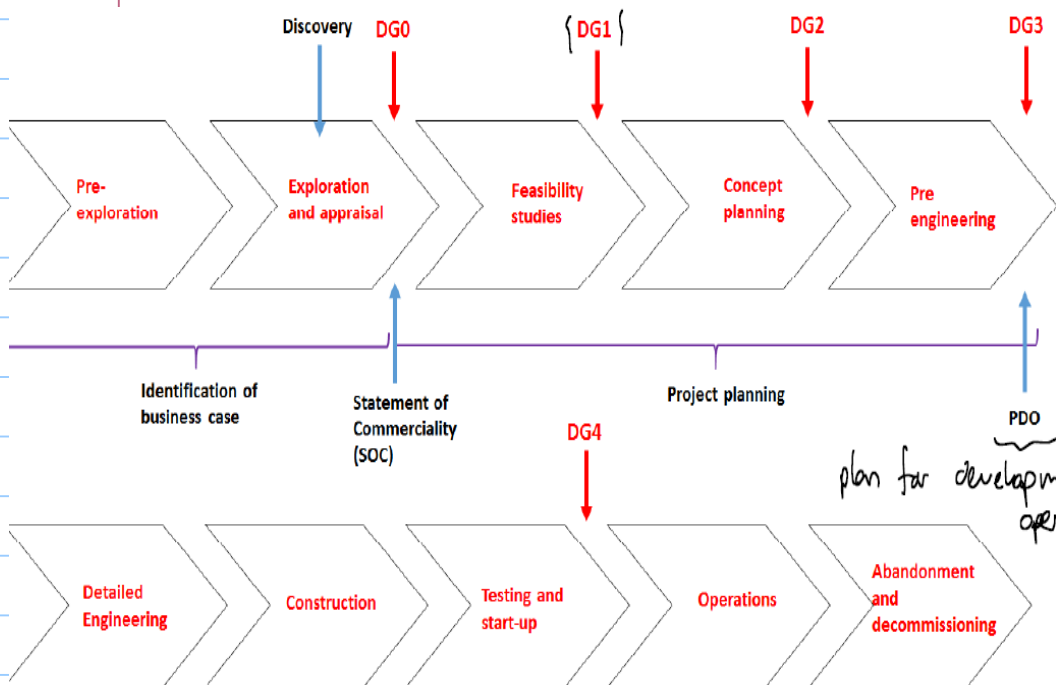




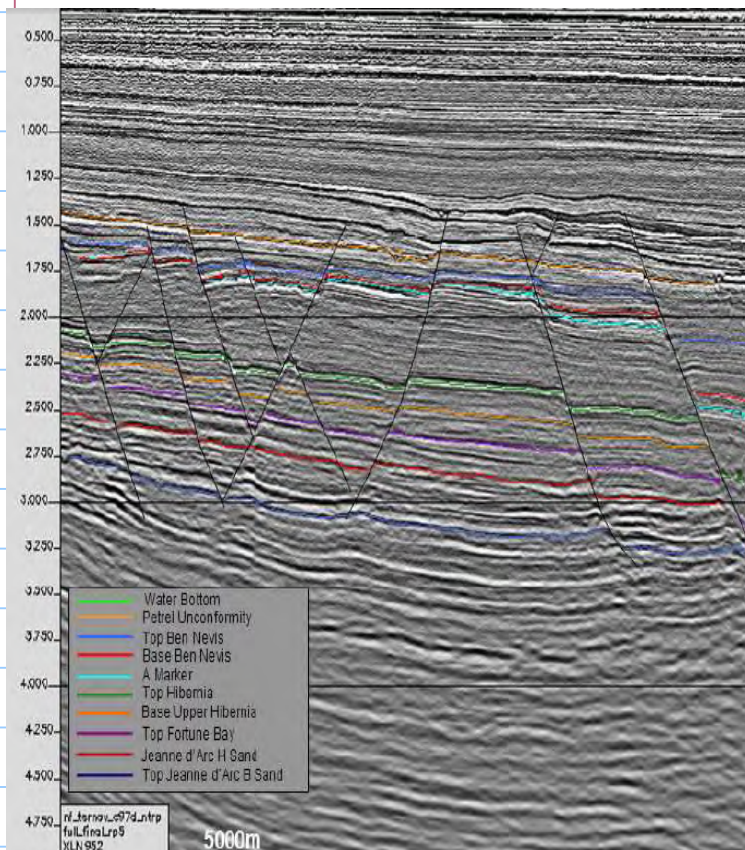
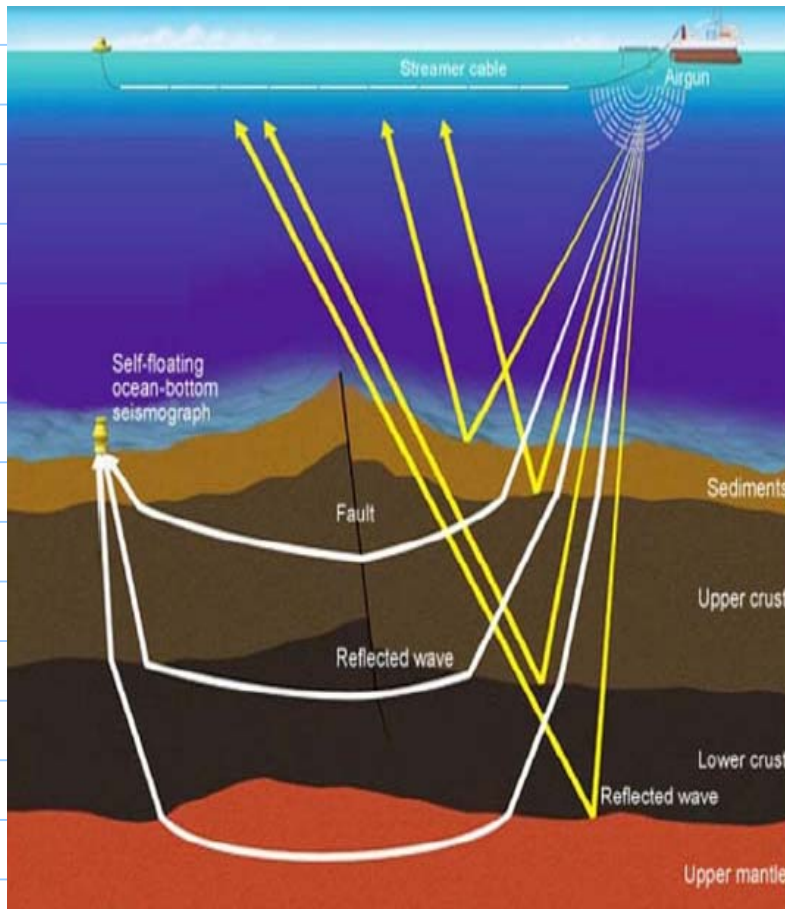




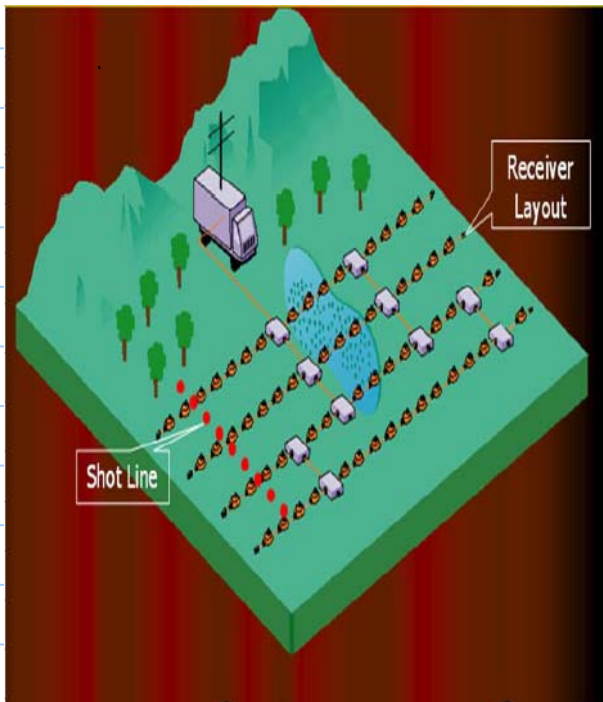
Reserve estimation  $\begin{cases} N, G & OOIP, OGIP \\ N_{pu}, G_{pu} & TRR \text{ Total reasonable reserves} \end{cases}$



## exploration seismic (offshore)

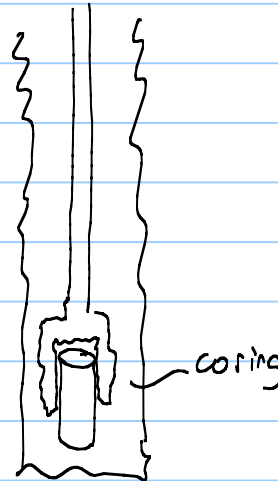


Geophysicist



land-based seismic

exploration drilling



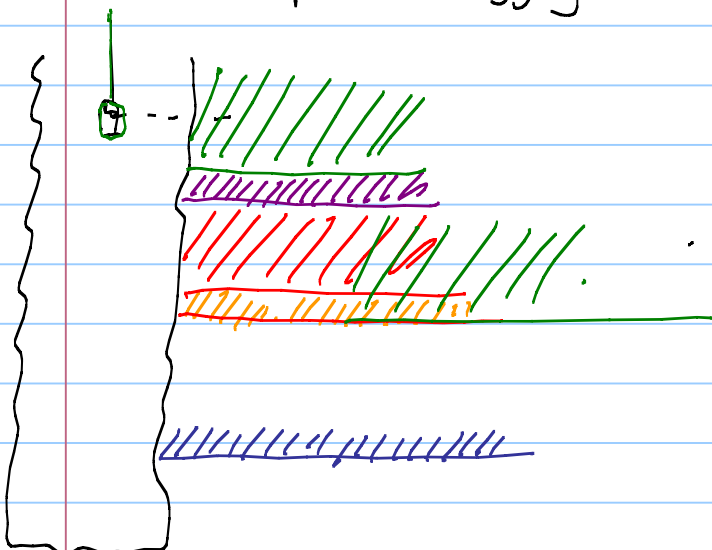
porosity permeability  
 $\phi$   $S_w$ ,  $K$



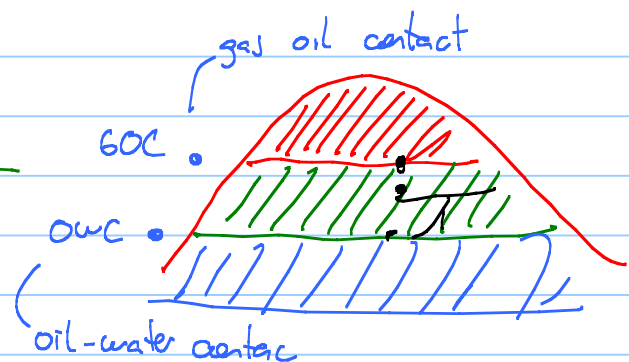
core sample

coring

exploration logging



$S_w$ , detecting Hydrocarbon  
 bearing rock

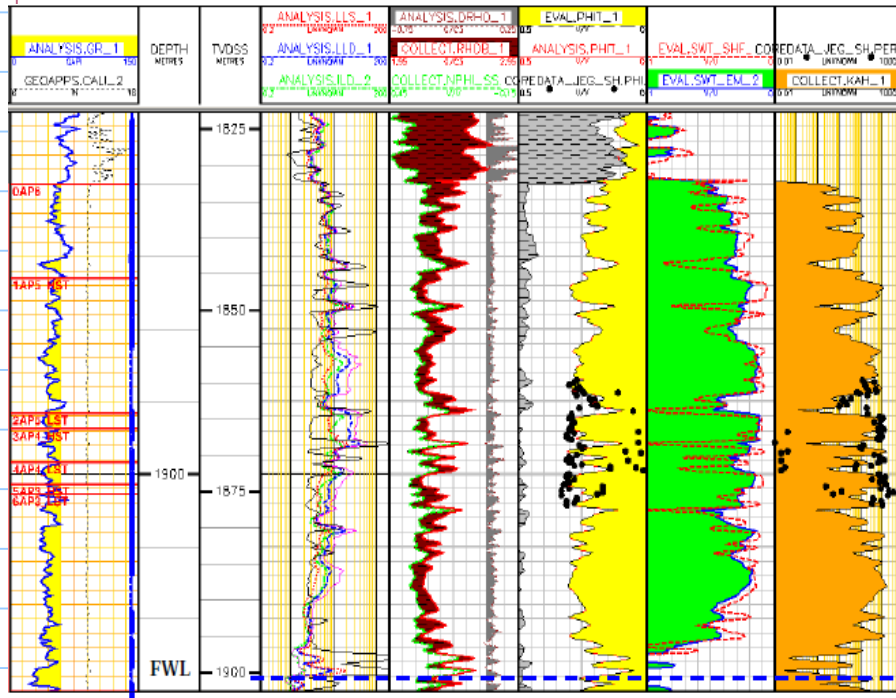


gas oil contact

GOC

OWC

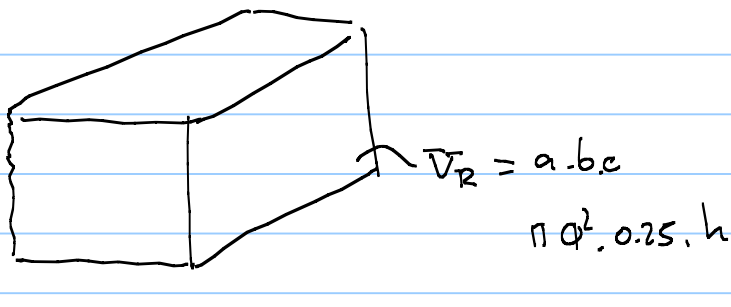
oil-water contact



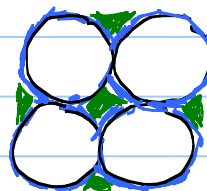
oil reservoir

$$TRR = NpU = \frac{V_{fluid} (1 - S_w)}{B_o} \cdot \phi \cdot S_o (M_{TG})$$

connate water saturation  
Net to gross



$$\phi = \frac{V_{\text{available}}}{V_R}$$

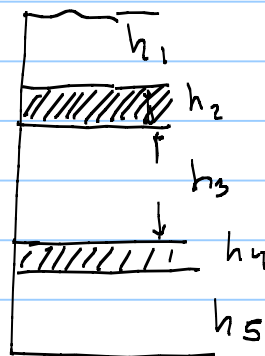
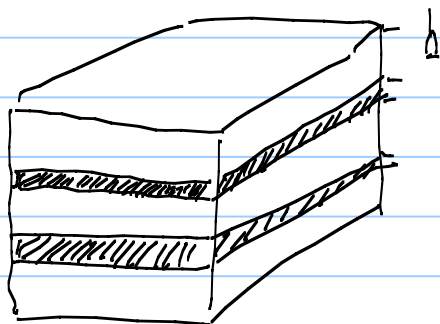


$$S_w = \frac{V_{\text{water}}}{V_{\text{pore}}}$$

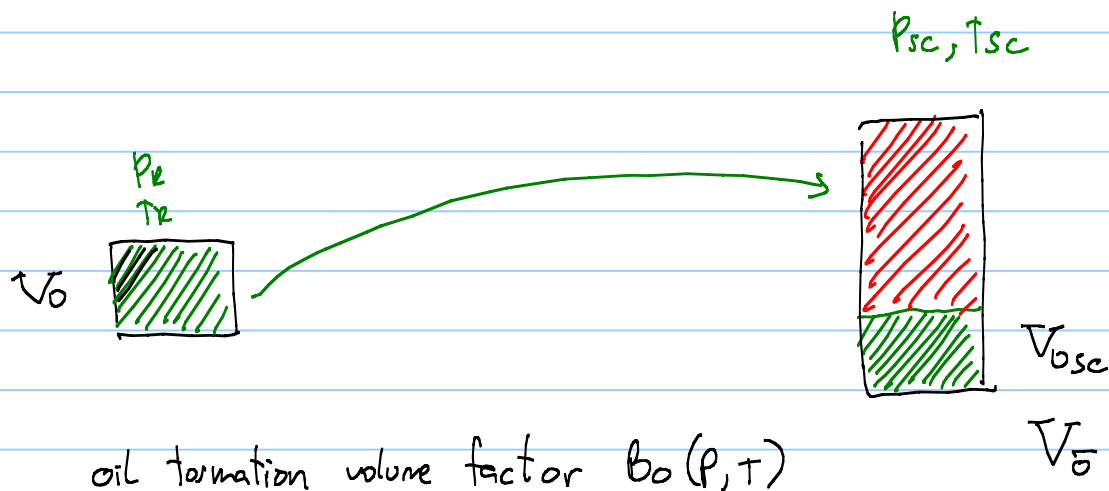
$$S_o$$

$$S_g$$

$$S_w + S_o + S_g = 1$$



$$\text{(Net to Gross)} = \frac{(h_1 + h_3 + h_5)}{(h_1 + h_2 + h_3 + h_4 + h_5)}$$



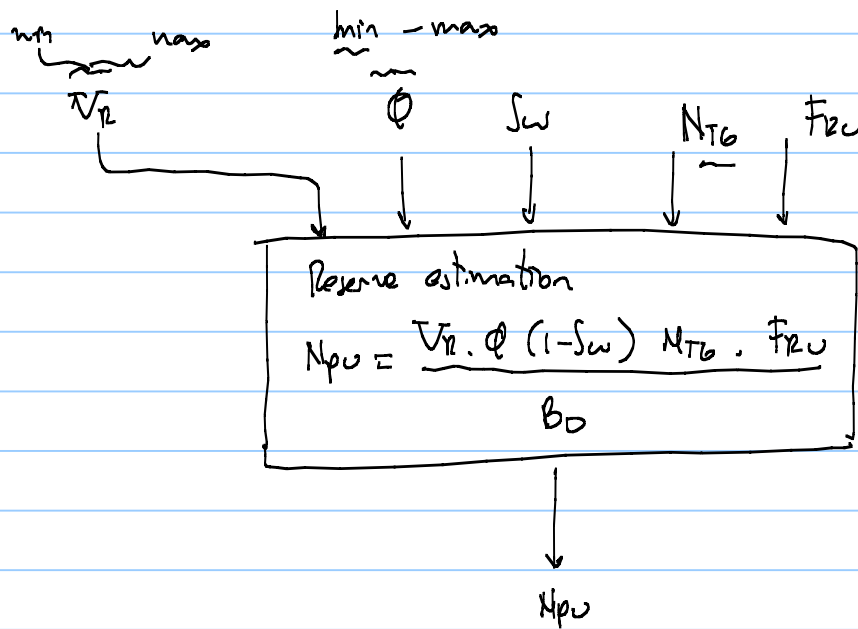
$$B_o = \frac{V_o(p, T)}{V_o} \approx 1 \rightsquigarrow 2$$

1.2, 1.3

$$N = \frac{V_R \cdot \phi \cdot (1 - S_w) \cdot N_{T6}}{B_o}$$

recovery factor  $F_R = \frac{N_{pu}}{N}$

$$N_{pu} = TRR = \frac{V_R \cdot \phi \cdot (1 - S_w) \cdot N_{T6}}{B_o} \cdot F_R$$



this calculation is NOT deterministic (one input  $\rightarrow$  one output)

probability distribution function pdf



class exercise to find pdf of porosity based on core measurement

100



06\_Porosity\_distribution

xls

30 720 03.12.2018 06:21 -a--

|                 |                | por_min | [-] | 0.182 |
|-----------------|----------------|---------|-----|-------|
|                 |                | por_max | [-] | 0.344 |
| Measurement nr. | Porosity value |         |     |       |
| 1               | 0.344          |         |     |       |
| 2               | 0.250          |         |     |       |
| 3               | 0.321          |         |     |       |
| 4               | 0.232          |         |     |       |
| 5               | 0.235          |         |     |       |
| 6               | 0.239          |         |     |       |
| 7               | 0.205          |         |     |       |
| 8               | 0.324          |         |     |       |
| 9               | 0.260          |         |     |       |
| 10              | 0.205          |         |     |       |
| 11              | 0.221          |         |     |       |
| 12              | 0.290          |         |     |       |
| 13              | 0.260          |         |     |       |
| 14              | 0.303          |         |     |       |
| 15              | 0.208          |         |     |       |
| 16              | 0.288          |         |     |       |
| 17              | 0.260          |         |     |       |
| 18              | 0.233          |         |     |       |
| 19              | 0.220          |         |     |       |

$$\phi_{\min}$$

$$\phi_{\max}$$

$$\frac{(\phi_{\max} - \phi_{\min})}{N_{\text{points}} - 1}$$

$$\phi_1$$

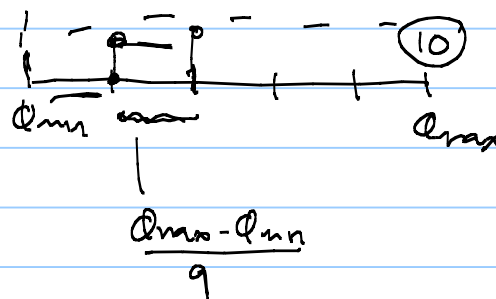
$$\phi_2$$

$$\phi_3$$

$$\phi_4$$

$$\phi_5$$

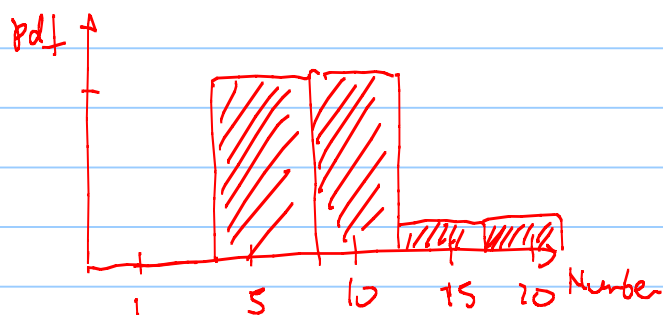
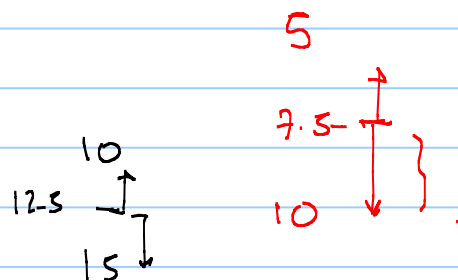
$$\phi_{\max}$$



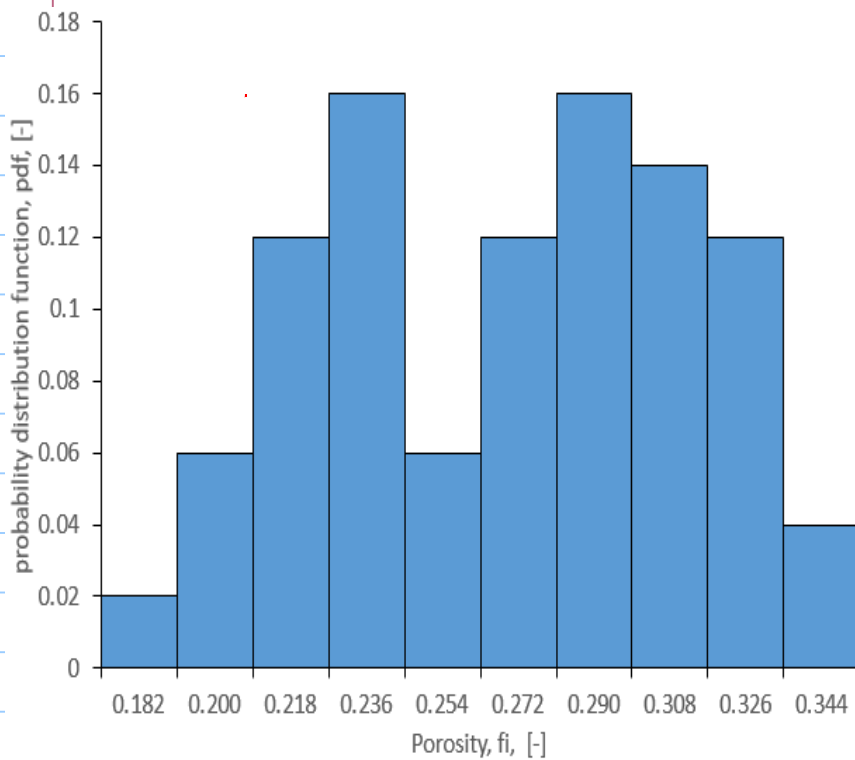
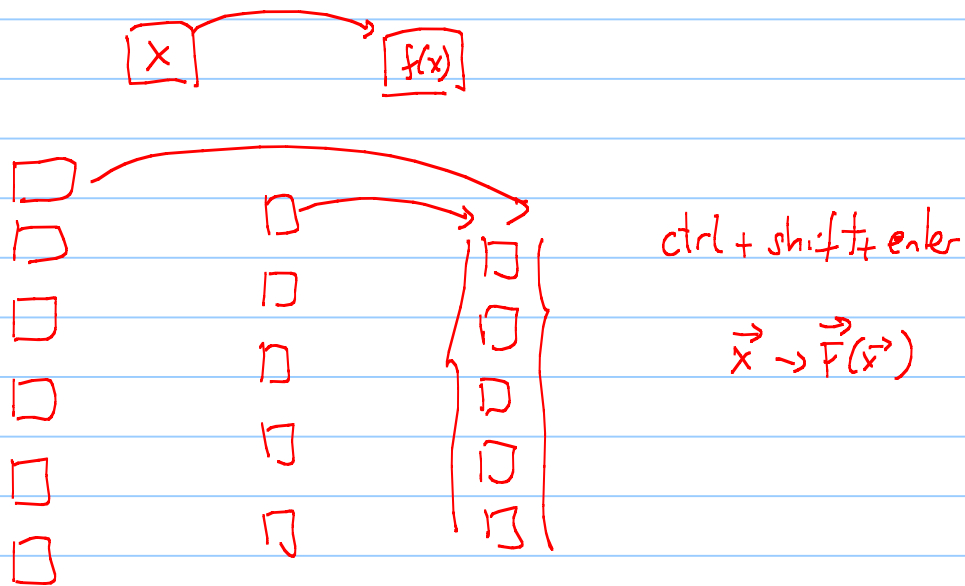
11 7 9  
3 8  
5 4 12  
15 20

bin

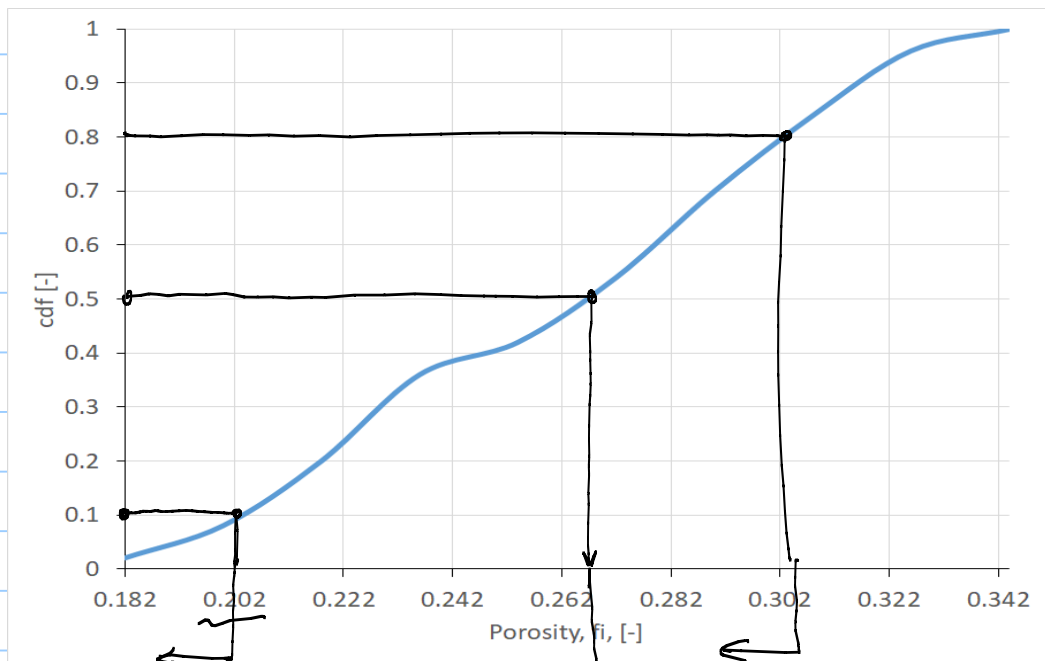
|    |   |
|----|---|
| 1  | 0 |
| 5  | 4 |
| 10 | 4 |
| 15 | 1 |
| 20 | 1 |







cdf cumulative distribution function

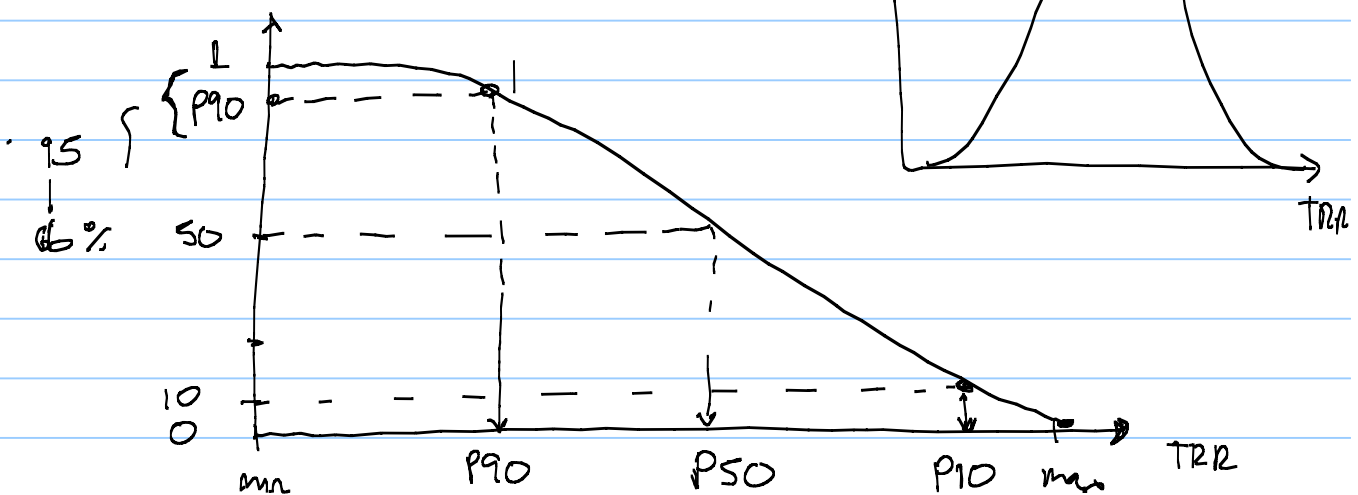


10% of samples have a porosity of 0.202 or lower

50% of sample have a porosity of 0.27 or lower

80% of the samples have a porosity of 0.302 or lower

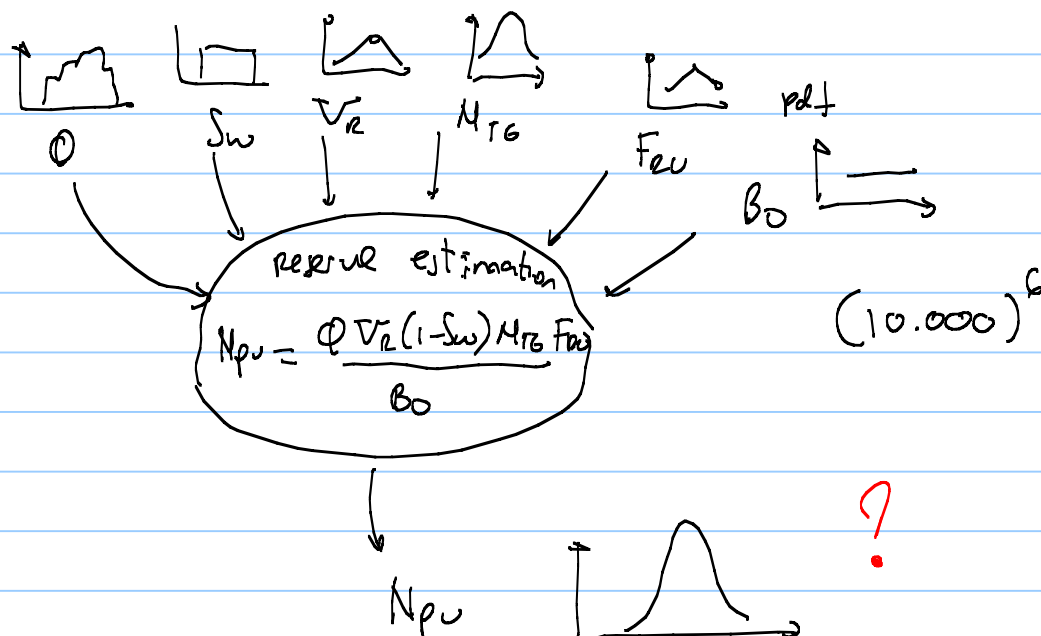
TRR are plotted using cdf



there is a 90% probability that reserves are equal or higher than P90

there is a 50% probability that reserves will be equal or higher than P50

there is a 10% probability that reserves will be equal or higher than P10



Los Alamos laboratory

## JOURNAL OF THE AMERICAN STATISTICAL ASSOCIATION

Number 247

SEPTEMBER 1949

Volume 44

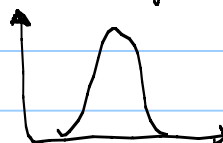
### THE MONTE CARLO METHOD

NICHOLAS METROPOLIS AND S. ULAM  
Los Alamos Laboratory

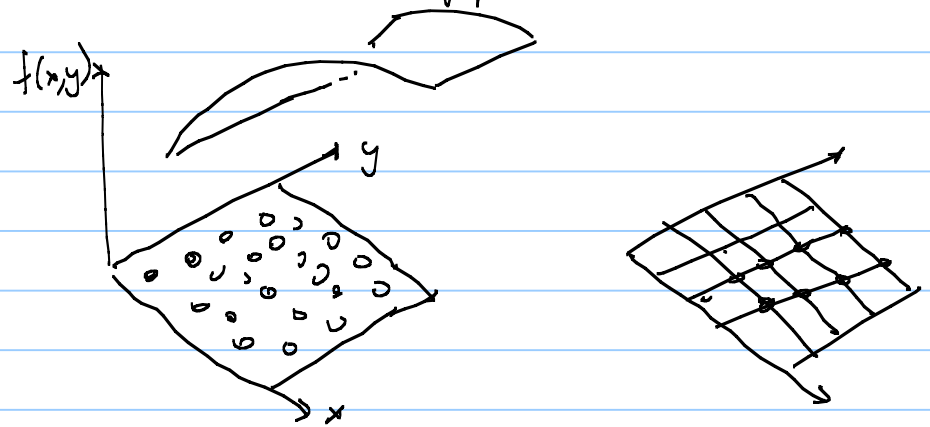
- 1) assume a random number for each parameter (be inside distribution)
- 2) Compute  $N_{pu}$
- 3) Repeat for many, many, many times

| MC iteration | $N_{pu}$  |
|--------------|-----------|
| 1            | $N_{pu1}$ |
| 2            | $N_{pu2}$ |
| 3            | $N_{pu3}$ |
| 4            |           |

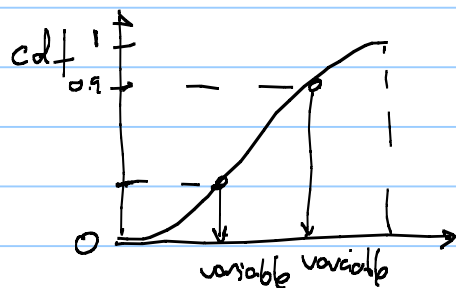
(4) apply a frequency analysis on the output values



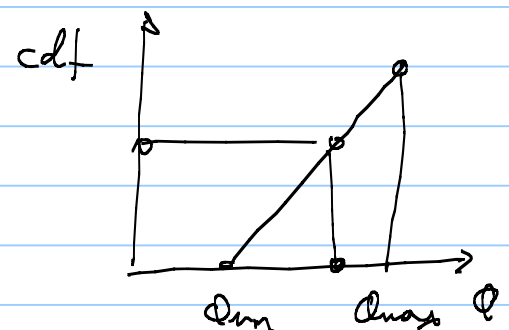
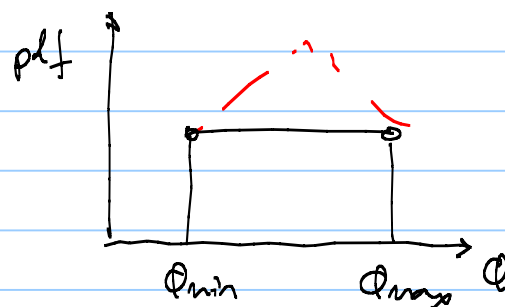
Monte carlo is a sampling method  
to find a representative sample of  
the whole population



How to generate the random values of input?



we for our input only uniform distribution

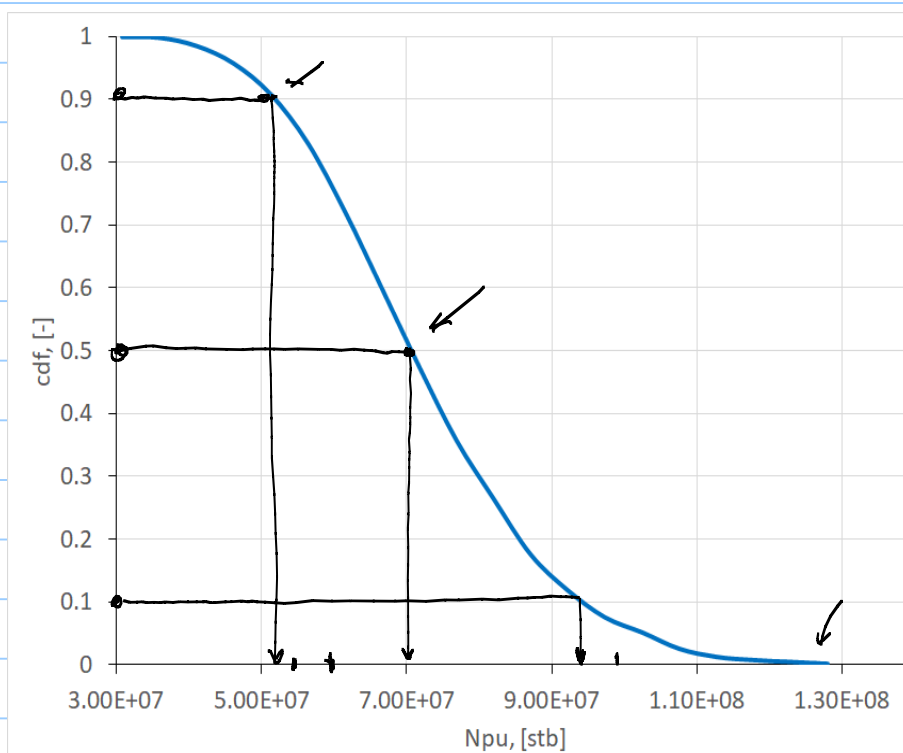


$$\Phi = \Phi_{min} + \overset{0-1}{\text{RAND}()} (\Phi_{max} - \Phi_{min})$$

## Class example TPG4230, Michael Golan and Milan Stanko

|     |             |          | Net to Gros | Oil Saturation | Formation Volume | Ultimate Recovery Factor |
|-----|-------------|----------|-------------|----------------|------------------|--------------------------|
|     | Rock volume | Porosity | N/G         | So=(1-Sw)      | Bo               | Fr                       |
|     | bbl         | fraction | fraction    | fraction       | Res bbl/STB      | fraction                 |
| Min | 2.00E+09    | 0.18     | 0.3         | 0.8            | 1.35             | 0.42                     |
| Max | 2.50E+09    | 0.3      | 0.5         | 0.9            | 1.6              | 0.65                     |

| MC it | Rock volume | Porosity | N/G      | So=(1-Sw) | Bo          | Fr       | Npu      |
|-------|-------------|----------|----------|-----------|-------------|----------|----------|
| [-]   | bbl         | fraction | fraction | fraction  | Res bbl/STB | fraction | [stb]    |
| 1     | 2.07E+09    | 2.00E-01 | 3.84E-01 | 8.37E-01  | 1.38E+00    | 5.79E-01 | 5.60E+07 |
| 2     | 2.41E+09    | 2.47E-01 | 3.34E-01 | 8.66E-01  | 1.47E+00    | 4.83E-01 | 5.66E+07 |
| 3     | 2.19E+09    | 2.20E-01 | 4.33E-01 | 8.80E-01  | 1.45E+00    | 5.36E-01 | 6.81E+07 |
| 4     | 2.04E+09    | 2.53E-01 | 4.98E-01 | 8.85E-01  | 1.42E+00    | 5.74E-01 | 9.20E+07 |
| 5     | 2.30E+09    | 1.98E-01 | 3.31E-01 | 8.65E-01  | 1.46E+00    | 6.15E-01 | 5.49E+07 |
| 6     | 2.01E+09    | 2.27E-01 | 4.51E-01 | 8.46E-01  | 1.45E+00    | 5.46E-01 | 6.57E+07 |

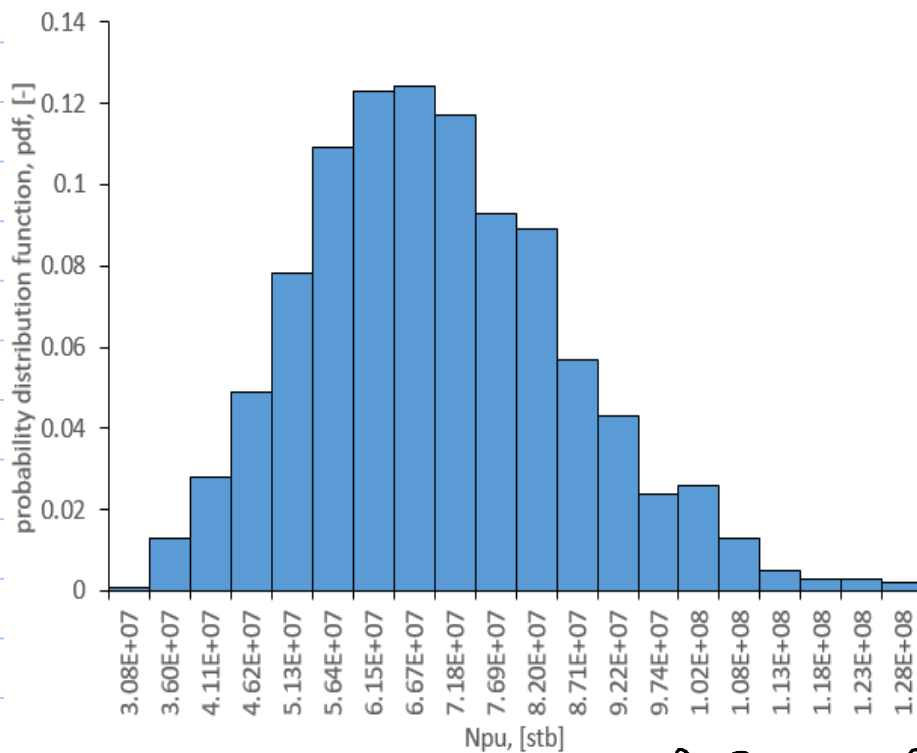


PSO is usually used  
for production  
profile forecasting

$$P_{10} = 95 \text{ EG stb}$$

$$\{P_{50} = 70 \text{ EG stb}$$

$$P_{90} = 52 \text{ EG stb}$$



| Hebron Ben Nevis Oil       | Upside Volumes <span style="margin-left: 20px;">~ P10</span> |                    | Best Estimate Volumes <span style="margin-left: 20px;">P50</span> |                  | Downside Volumes <span style="margin-left: 20px;">P90</span> |                  |
|----------------------------|--------------------------------------------------------------|--------------------|-------------------------------------------------------------------|------------------|--------------------------------------------------------------|------------------|
|                            | MBO                                                          | Mm <sup>3</sup>    | MBO                                                               | Mm <sup>3</sup>  | MBO                                                          | Mm <sup>3</sup>  |
| D-94 Fault Block           | 1601                                                         | 255                | 1328                                                              | 211              | 1077                                                         | 171              |
| I-13 Fault Block           | 252                                                          | 40                 | 187                                                               | 30               | 141                                                          | 22               |
| Total Hebron Ben Nevis     | 1870                                                         | 297                | 1515                                                              | 241              | 1204                                                         | 191              |
| Total Hebron Ben Nevis Gas | Upside Volumes                                               |                    | Best Estimate Volumes                                             |                  | Downside Volumes                                             |                  |
|                            | GCF                                                          | * GSm <sup>3</sup> | GCF                                                               | GSm <sup>3</sup> | GCF                                                          | GSm <sup>3</sup> |
| Solution Gas D-94 Block    | 112                                                          | 3.2                | 145                                                               | 4.1              | 189                                                          | 5.4              |
| Solution Gas I-13 Block    | 10                                                           | 0.3                | 14                                                                | 0.4              | 22                                                           | 0.6              |
| Non-associated Gas         | n/a                                                          | n/a                | n/a                                                               | n/a              | n/a                                                          | n/a              |
| Gas Cap D-94 Block only    | 0                                                            | 0                  | 0                                                                 | 0                | 31                                                           | 0.9              |

\* GSm<sup>3</sup> = 10<sup>9</sup> cubic meters

• when the simulation takes long time

production profiles  
Cost estimation  
NPV calculation

Monte Carlo is impractical (too long running times) → use probability trees.

Class 5

- Probability trees
- Field development
- Offshore structures for HC production

Probability trees  
is used often in appraisal

- traditional approach requires less computing power
- discrete variables vessel type  
decision variable  
sequence
- when simulations take a long time

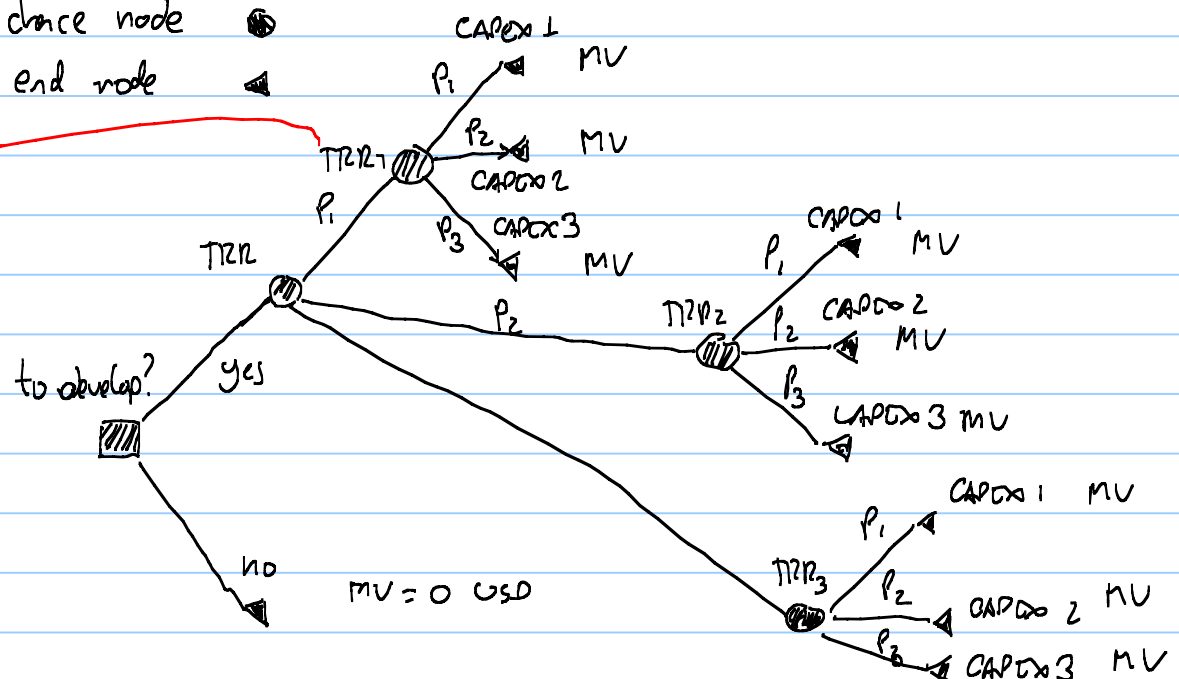
- Identify how many variables the probability tree has
  - (1) • develop or not (2)
  - TIR (3)
  - CAPEX (3)

decision node

chance node

end node 

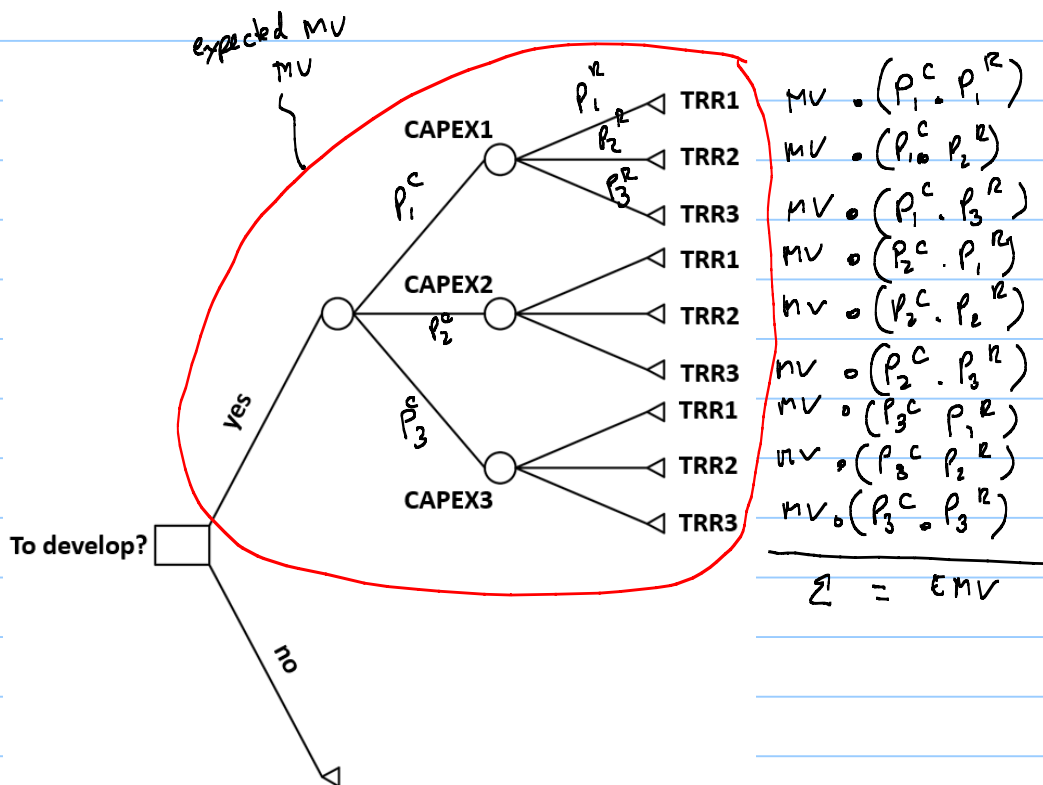
requires  
discretizing  
continuous  
distribution



Cost values (OPEX, CAPEX, OMLT) usually display a Gaussian/Normal distribution

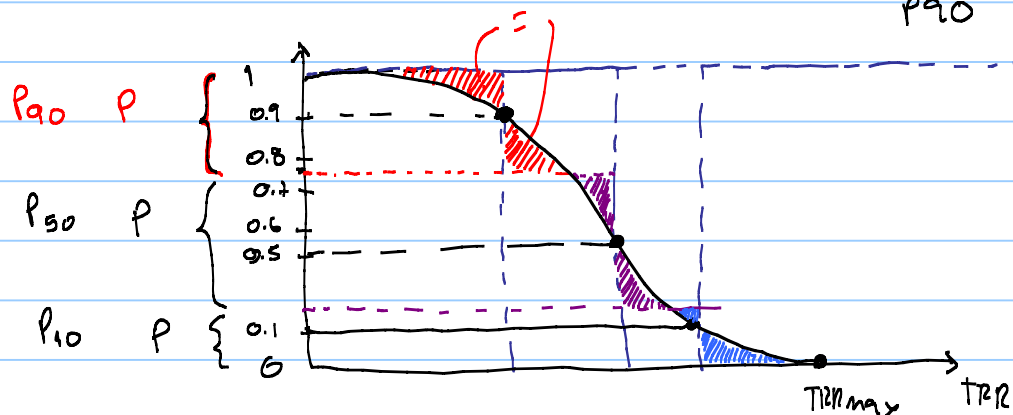




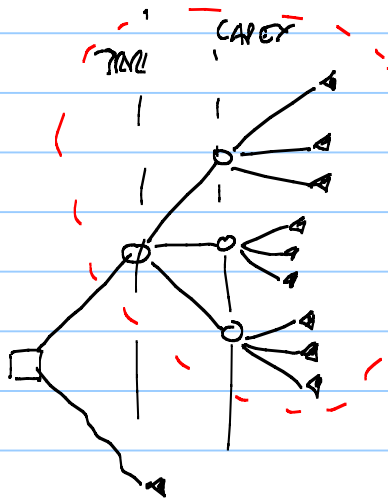
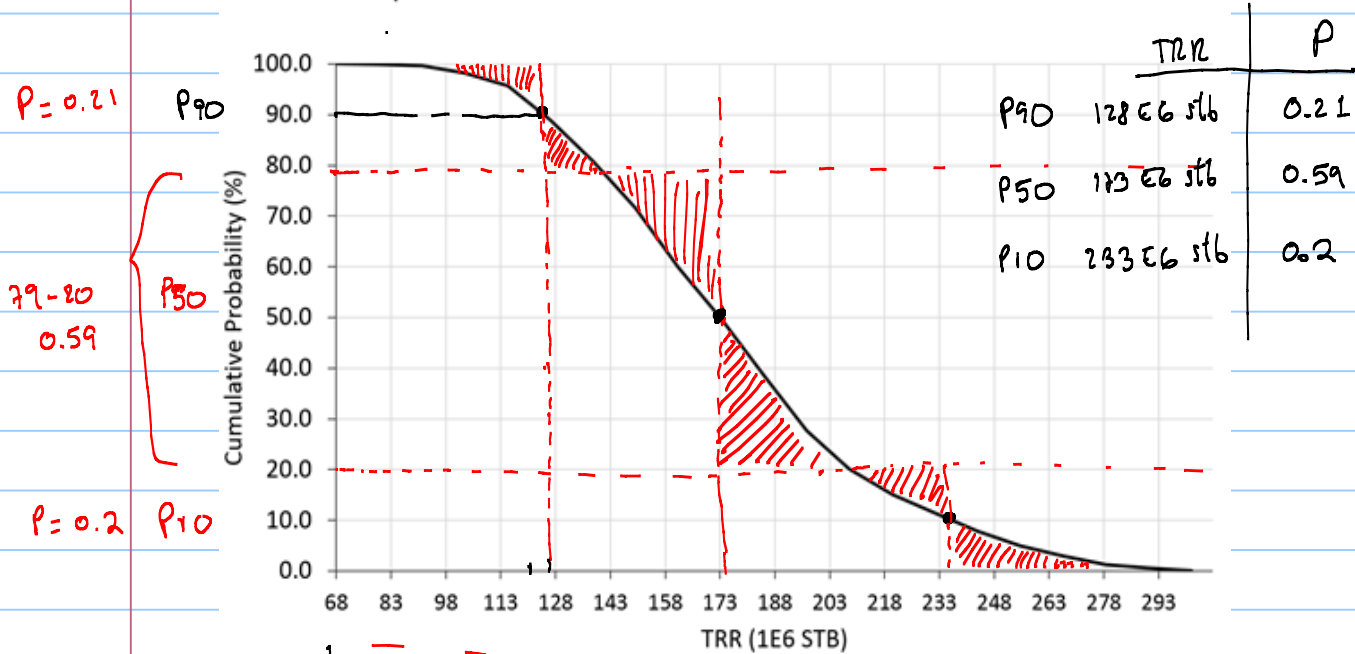


How do we get discretized values of TRR, CAPEX from a continuous function

for TRR, people like to use  $p_{10}$   
 $p_{50}$   
 $p_{90}$



Expectation Curve for Total Recoverable Oil Reserves

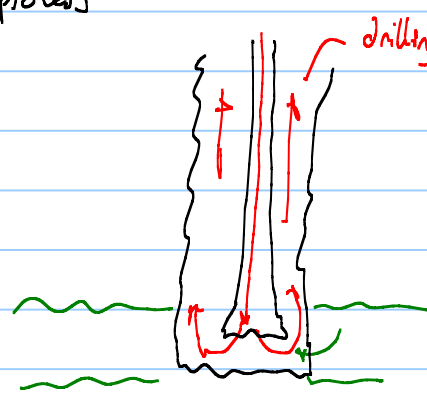


EMV = 3.11 E 9 USD !

| OPTION | TRR      | P_TRR | CAPEX    | P_capex | MV = TRR*60*0.4-CAPEX | P=P_capex*P_TRR | MV*P     |
|--------|----------|-------|----------|---------|-----------------------|-----------------|----------|
| [·]    | [stb]    | [·]   | [USD]    | [·]     | [USD]                 | [·]             | [USD]    |
| 1      | 1.28E+08 | 0.21  | 7.00E+08 | 0.3     | 2.37E+09              | 0.063           | 1.49E+08 |
| 2      | 1.28E+08 | 0.21  | 1.10E+09 | 0.4     | 1.97E+09              | 0.084           | 1.66E+08 |
| 3      | 1.28E+08 | 0.21  | 1.50E+09 | 0.3     | 1.57E+09              | 0.063           | 9.90E+07 |
| 4      | 1.73E+08 | 0.59  | 7.00E+08 | 0.3     | 3.45E+09              | 0.177           | 6.11E+08 |
| 5      | 1.73E+08 | 0.59  | 1.10E+09 | 0.4     | 3.05E+09              | 0.236           | 7.20E+08 |
| 6      | 1.73E+08 | 0.59  | 1.50E+09 | 0.3     | 2.65E+09              | 0.177           | 4.69E+08 |
| 7      | 2.33E+08 | 0.2   | 7.00E+08 | 0.3     | 4.89E+09              | 0.06            | 2.94E+08 |
| 8      | 2.33E+08 | 0.2   | 1.10E+09 | 0.4     | 4.49E+09              | 0.08            | 3.59E+08 |
| 9      | 2.33E+08 | 0.2   | 1.50E+09 | 0.3     | 4.09E+09              | 0.06            | 2.46E+08 |
|        |          |       |          |         |                       | EMV             | 3.11E+09 |

Answer : yes to development!

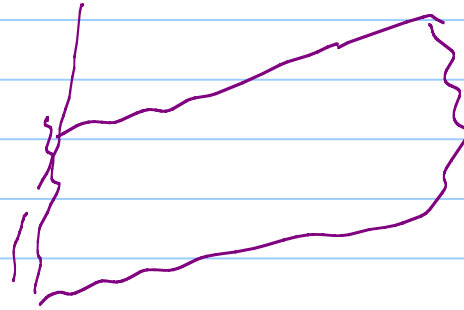
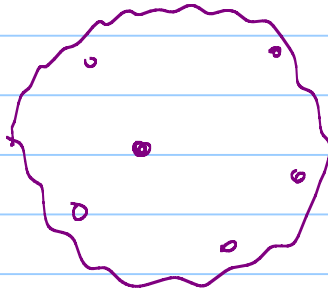
## field development process



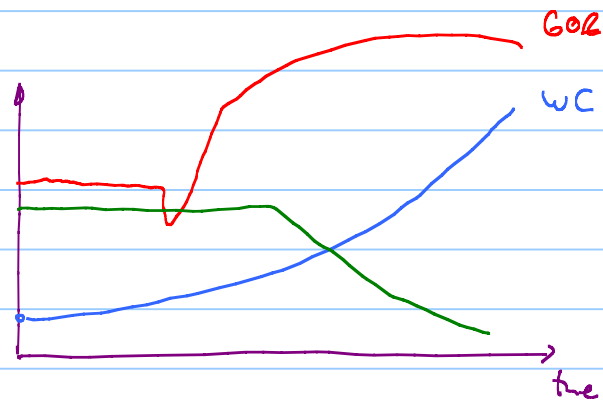
drilling mud : functions :

- carry cuttings to surface
- cool the bit
- lubricate
- pressure control of reservoir fluid

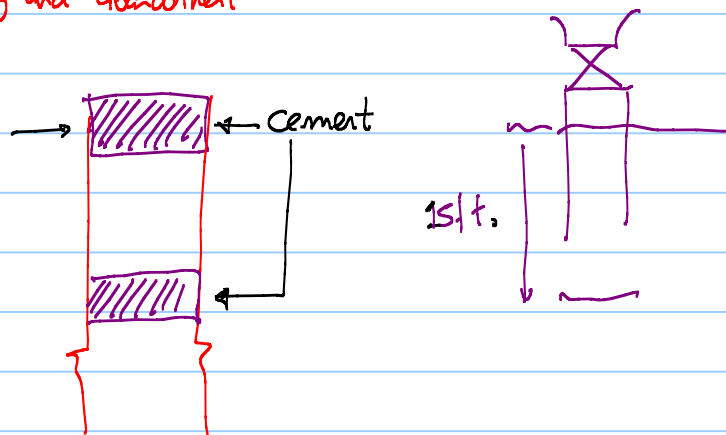
## top view of reservoir



## Debottlenecking

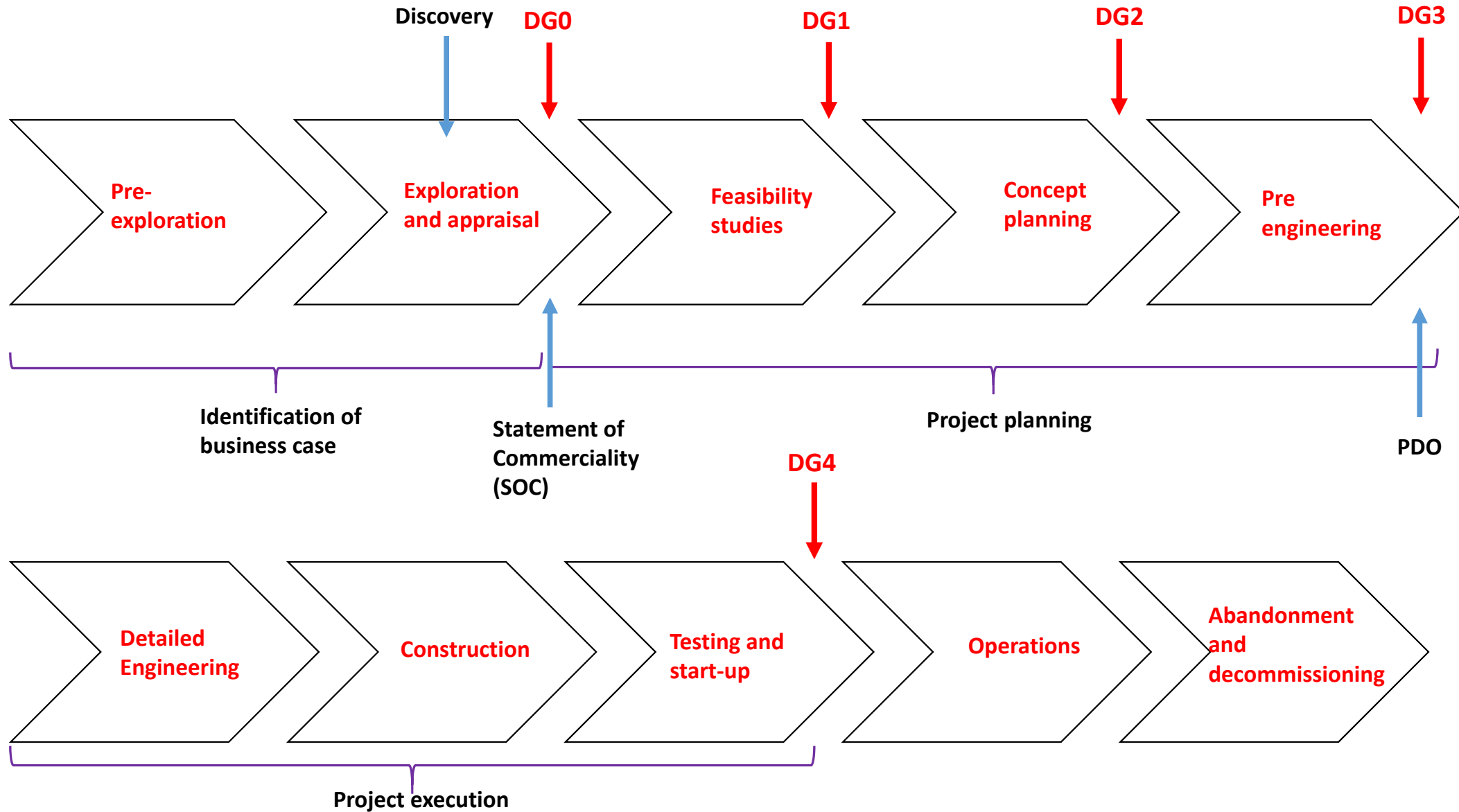


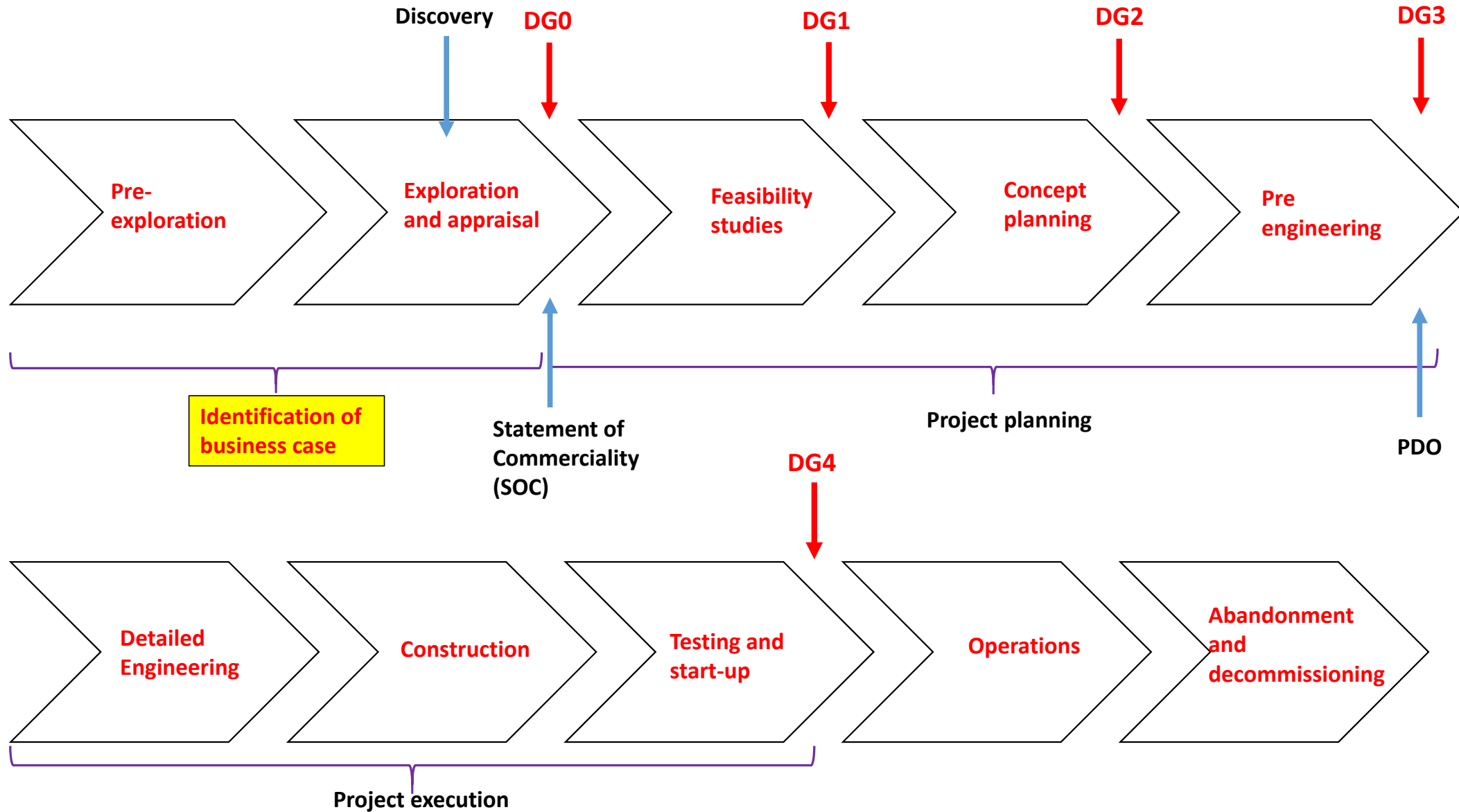
## Plug and abandonment



# THE FIELD DEVELOPMENT PROCESS

Prof. Milan Stanko (NTNU)





# IDENTIFICATION OF BUSINESS CASE

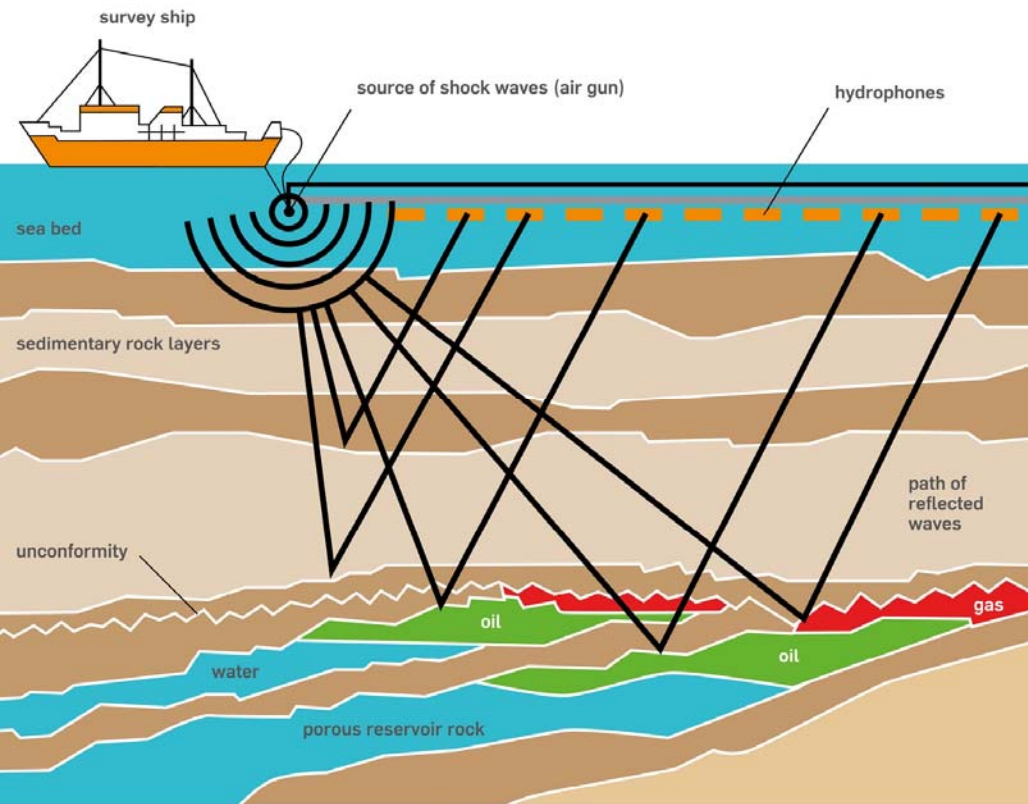
The main goal of this stage is to prove economic potential of the discovery and quantify and reduce the uncertainty in the estimation of reserves.



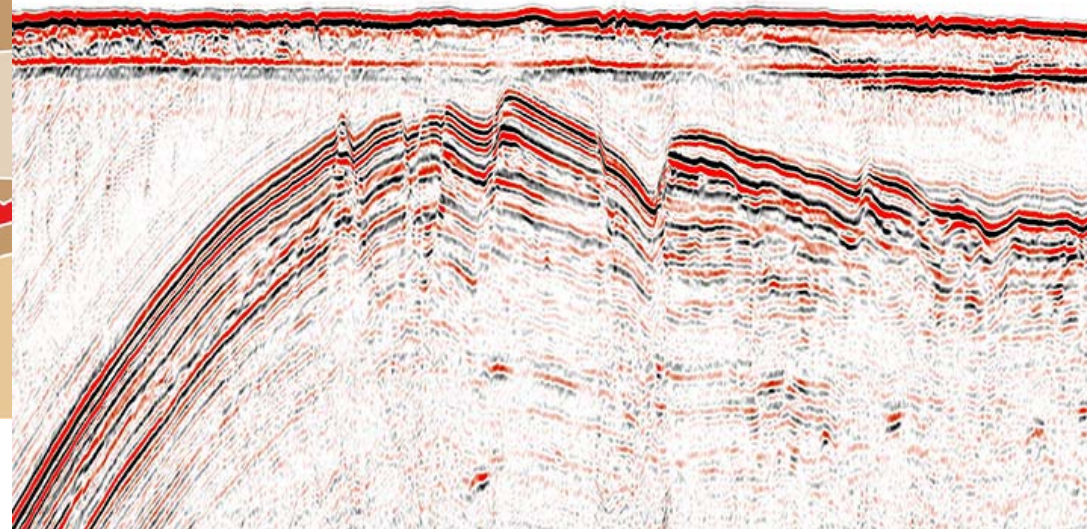
# IDENTIFICATION OF BUSINESS CASE - TASKS

- Pre-exploration – scouting: collecting information on areas of interests. Technical, political, geological, geographical, social, environmental considerations are taken into account. E.g. expected size of reserves, political regime, government stability, technical challenges of the area, taxation regime, personnel security, environmental sensitivity, previous experience in the region, etc.
- Getting pre-exploration access – The exploration license (usually non-exclusive). In the NCS only seismic and shallow wells are allowed. This is usually done by specialized companies selling data to oil companies.
- Identify prospects.

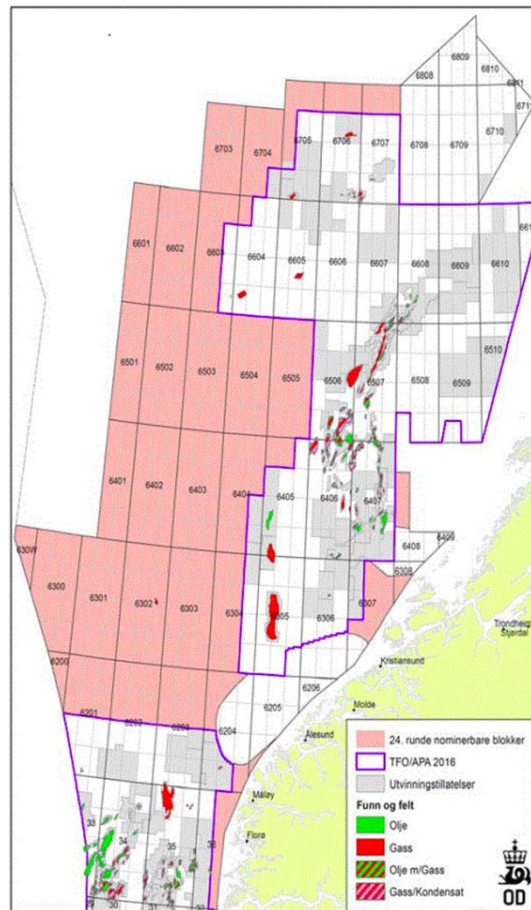
# IDENTIFICATION OF BUSINESS CASE - TASKS



Seismic exploration



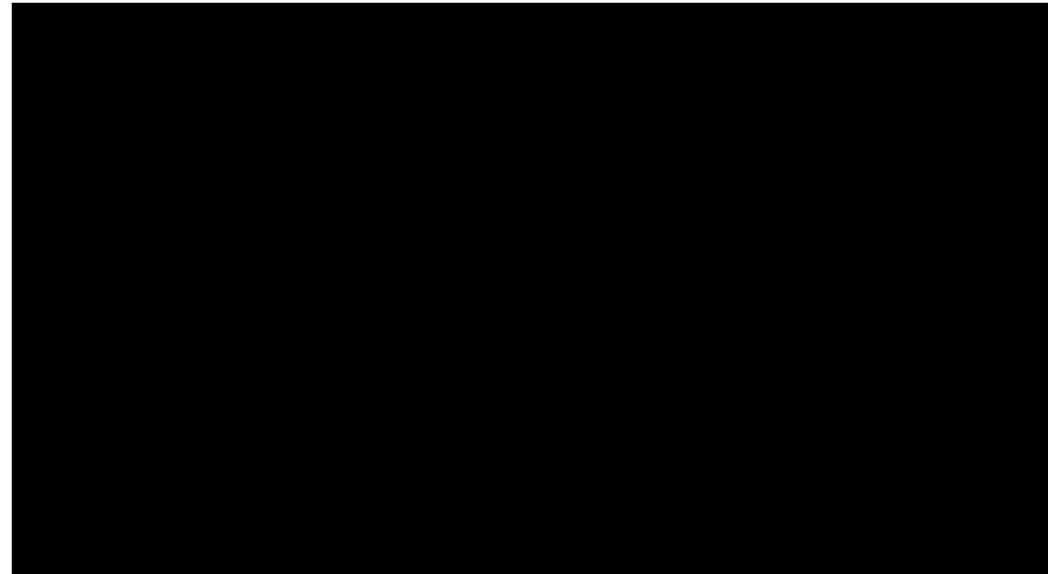
# IDENTIFICATION OF BUSINESS CASE - TASKS



- Apply and obtain exclusive production license. In the NCS: Licensing rounds (frontier areas) or Awards in predefined areas (APA). The current fees are 34 000 NOK/km<sup>2</sup> for the first year, 68 000 NOK/km<sup>2</sup> for the second year and 137 000 NOK/km<sup>2</sup> per year thereafter.

# IDENTIFICATION OF BUSINESS CASE - TASKS

- Exploration. Perform geological studies, geophysical surveys, seismic, exploration drilling (Well cores, wall cores, cuttings samples, fluid samples, wireline logs, productivity test).
- Discovery!



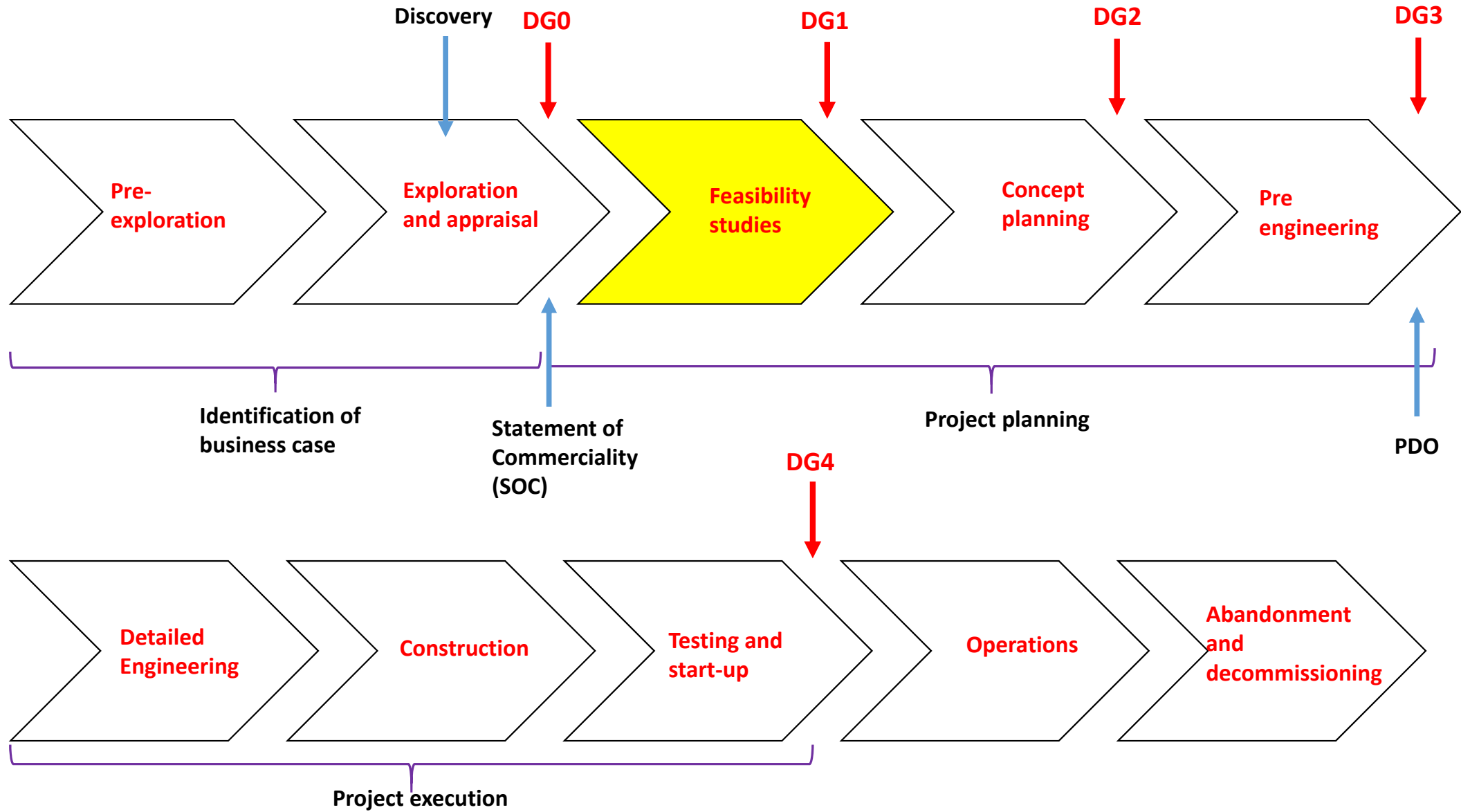
# IDENTIFICATION OF BUSINESS CASE - TASKS

- Assessment of the discovery and the associated uncertainty. Risk management:
  - Probabilistic reserve estimation. Identify and assess additional segments.
  - Perform simplified economic valuation of the resources.
  - Field appraisal to reduce uncertainty: more exploration wells and seismic to determine for example: fault communication, reservoir extent, aquifer behavior, location of water oil contact or gas oil contact.

# IDENTIFICATION OF BUSINESS CASE - TASKS

DG0:

- Issue a SOC (Statement of Commerciality) and proceed with development.
- Continue with more appraisal
- Sell the discovery.
- Do nothing (wait)
- Relinquish to the government



# FEASIBILITY STUDIES - TASKS

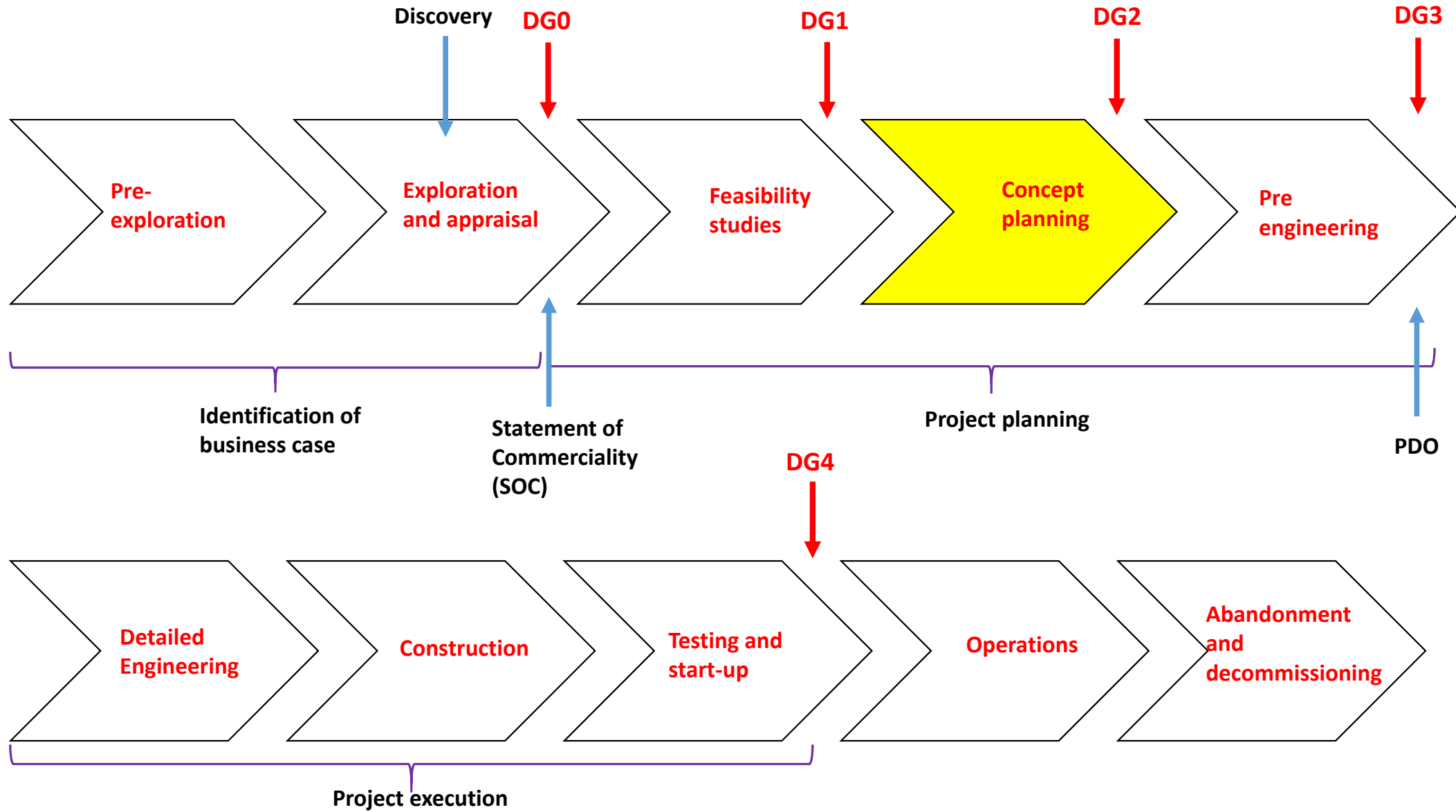
**OBJECTIVE:** Justify further development of the project, finding one or more concepts that are technically, commercially and organizationally feasible

- Define objectives of the development in line with the corporate strategy.
- Establish feasible development scenarios.
- Create a project timeline and a workplan.



# FEASIBILITY STUDIES - TASKS

- Identify possible technology gaps and blockers.
- Identify the needs for new technology.
- Identify added value opportunities.
- Cost evaluation for all options (at this stage, cost figures are  $\pm 40\%$  uncertain)



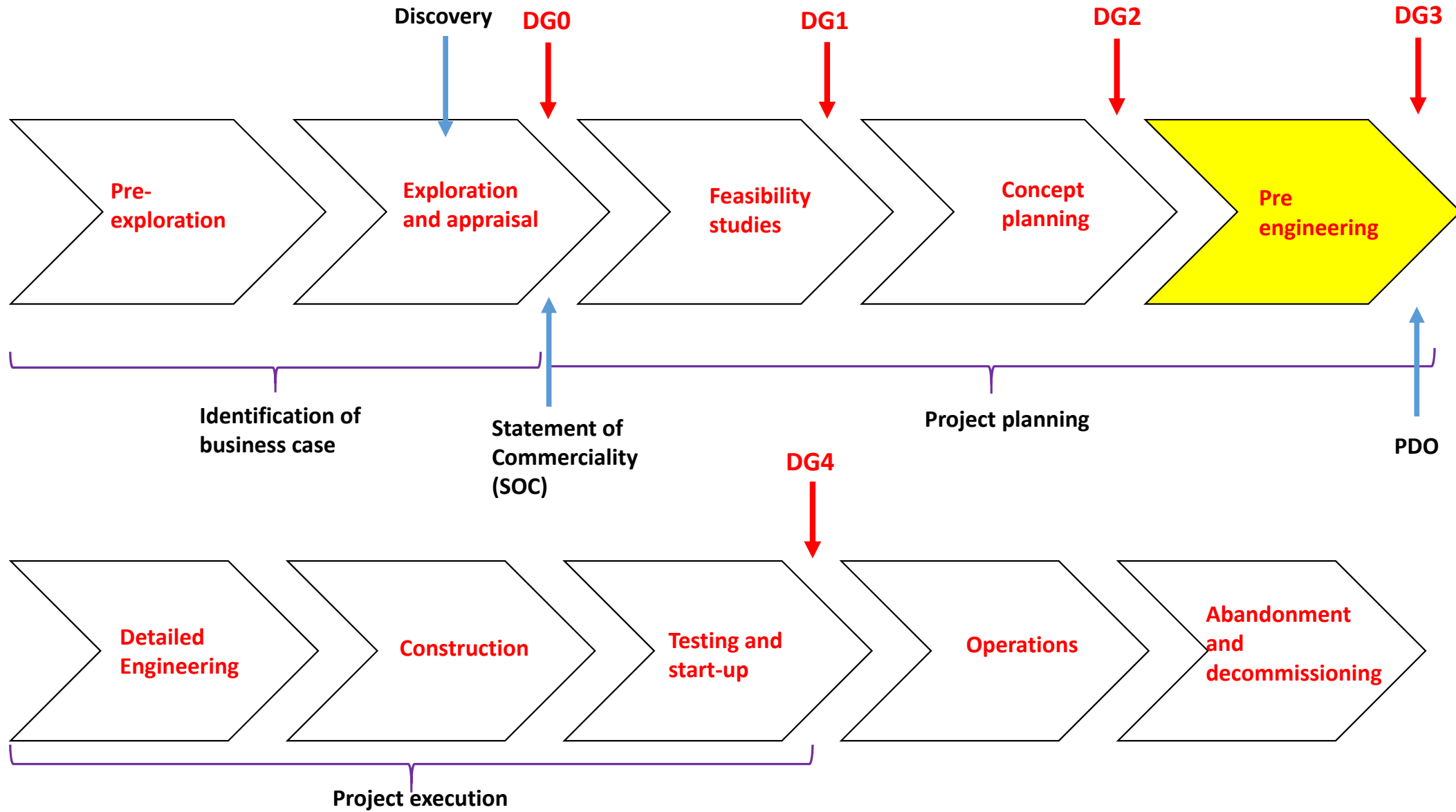
# CONCEPT PLANNING - TASKS

**OBJECTIVE:** Identify development concepts, rank them and select and document a viable concept (Base Case Scenario).

- Evaluate and compare alternatives for development and screen out non-viable options.
- Elaborate a Project Execution Plan (PEP) which describes the project and management system.
- Define the commercial aspects, legislation, agreements, licensing, financing, marketing and supply, taxes.

# CONCEPT PLANNING - TASKS

- Create and refine a static and a dynamic model of reservoir.  
**Define the depletion and production strategy.**
- Define an HSE program
- **Flow assurance evaluation.** Identification of challenges related with fluid properties, multiphase handling and driving pressure.
- Drilling and well planning
- Pre-design of facilities
- Planning of operations, start-up and maintenance
- Cost and manpower estimates of the best viable concept.



# PRE-ENGINEERING - TASKS

OBJECTIVE: Further mature, define and document the development solution based on the selected concept.

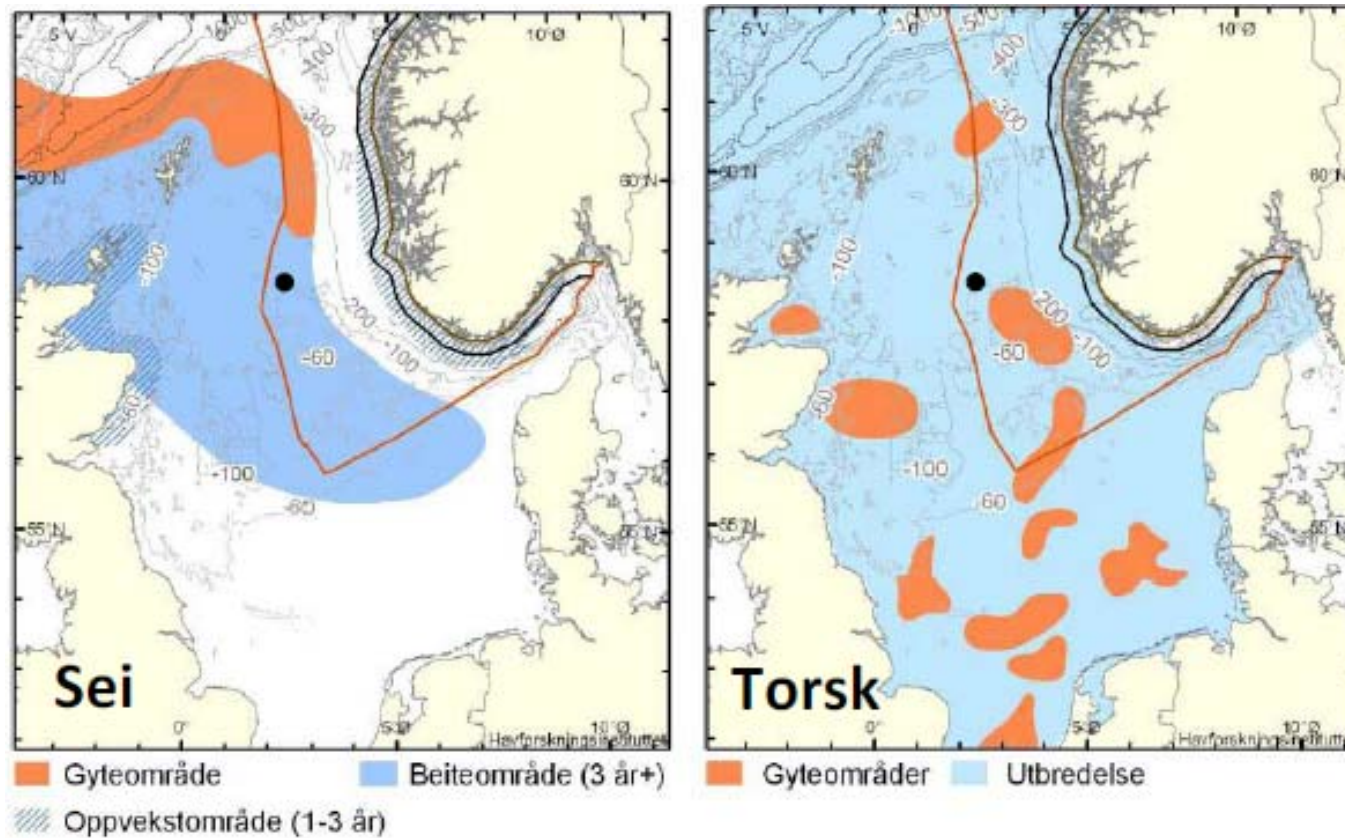
- Selection of the final technical solution. Decide and define all remaining critical technical alternatives.
- Execute Front End Engineering Design (FEED) Studies: determine technical requirements (arranged in packages) for the project based on the final solution chosen. Estimate cost of each package.
- Plan and prepare the execution phase.

# PRE-ENGINEERING - TASKS

- Prepare for submission of the application to the authorities.
- Perform the Environmental impact assessment.
- Establish the basis for awarding contracts.
- Issue:
  - Plan for development and operations
  - Plan for installation and operations of facilities for transport and utilization of petroleum (PIO)
  - Impact assessment report



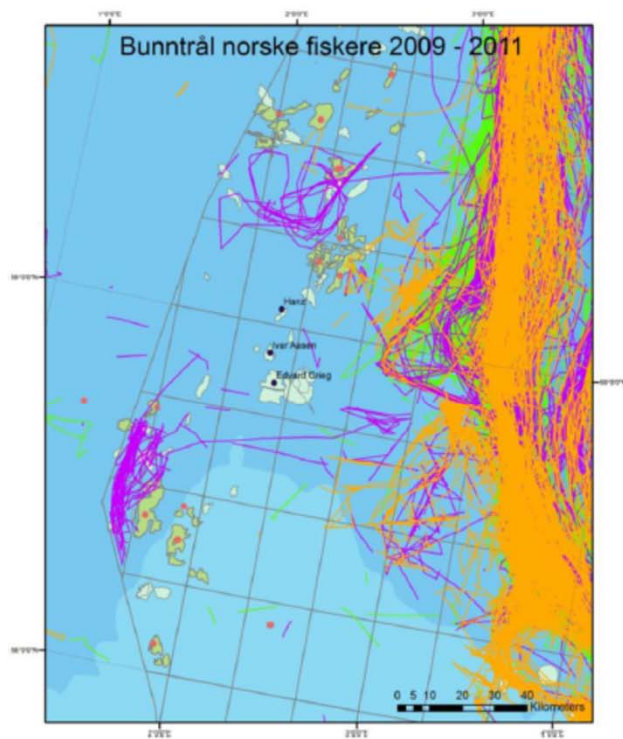
# PRE-ENGINEERING - TASKS





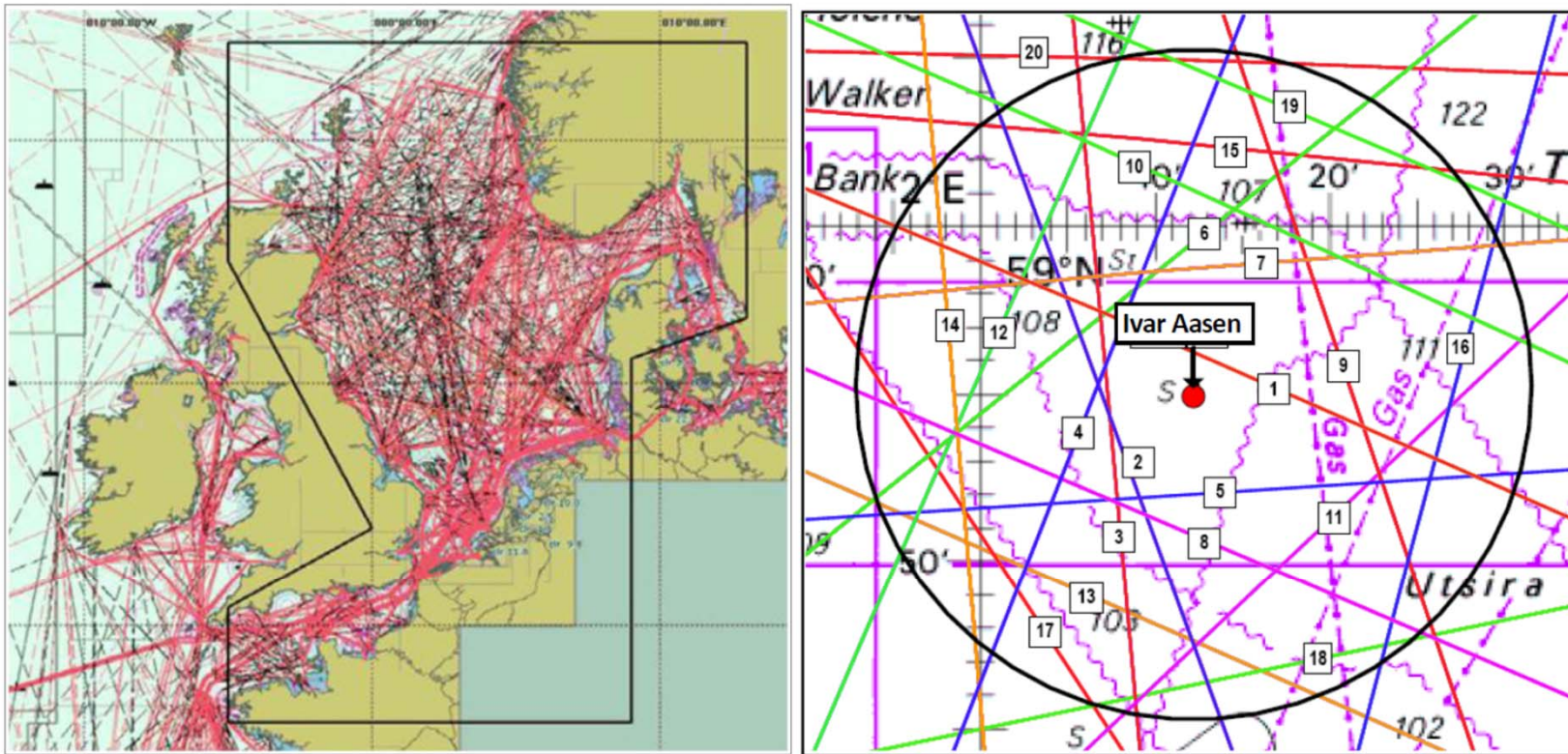
Figur 18. Svært viktige (rød), viktige (oransje) og nokså viktige (gule) leveområder for sjøfugl langs kysten av Nordsjøen i hekketiden. Kartet markerer buffersoner rundt de viktige hekkelokalitetene (NINA)

# PRE-ENGINEERING - TASKS



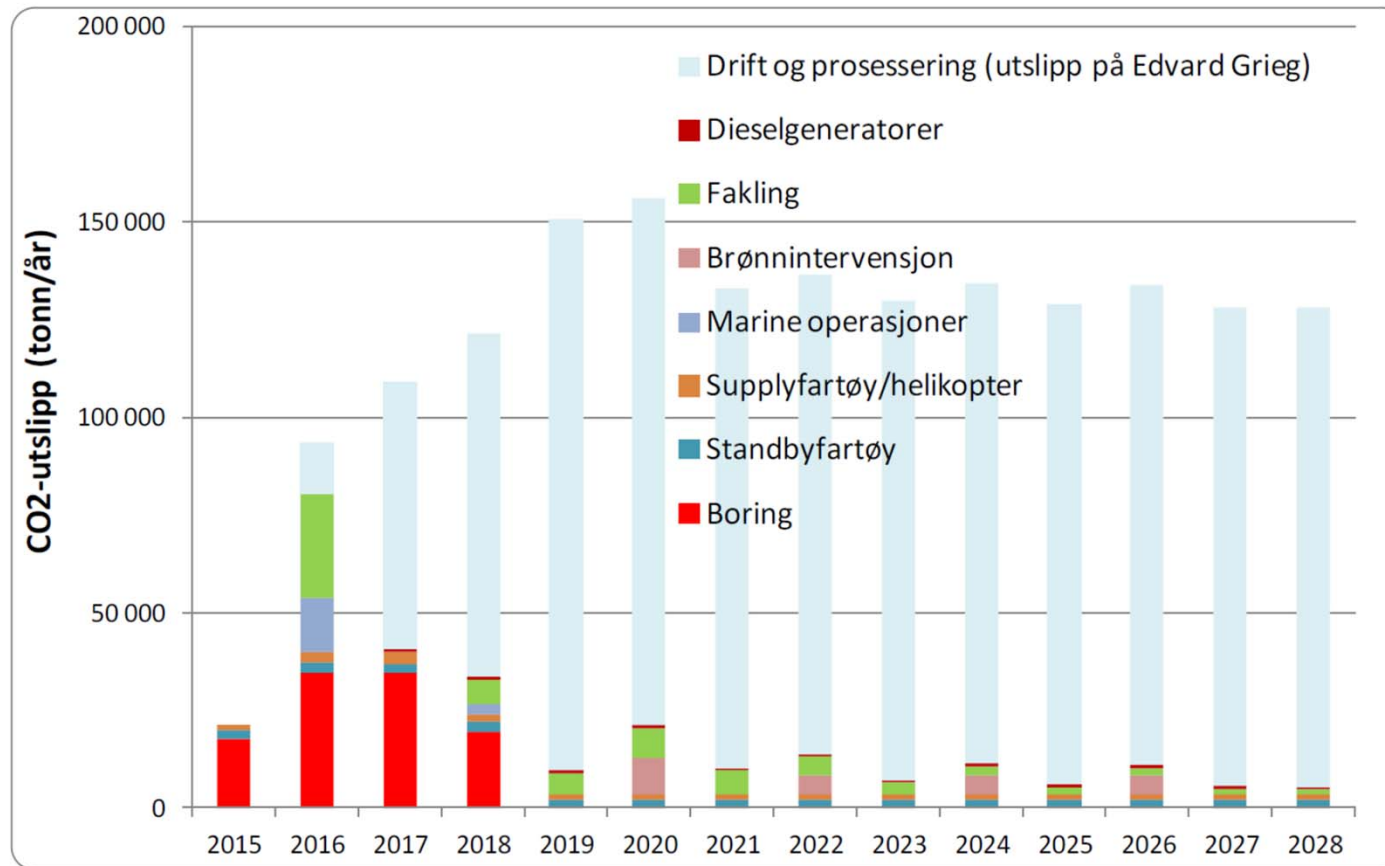
Figur 23. Registrert norsk fiskeriaktivitet med bunntål i området omkring Aasen i 2009 (grønn), 2010 (fiolett) og 2011 (oransje). Figur utarbeidet på grunnlag av data fra Fiskeridirektoratets satellittsporing av større fiskefartøyer

# PRE-ENGINEERING - TASKS



**Figur 24. Trafikkompleksitet i Nordsjøen (venstre) og skipsleder for handels- og offshorefartøy innenfor en radius på 10 nautiske mil fra Aasen (høyre)**

# PRE-ENGINEERING - TASKS



**Figur 25. Samlede utslipp av CO<sub>2</sub> fra Aasenfeltet i perioden 2015 – 2028**

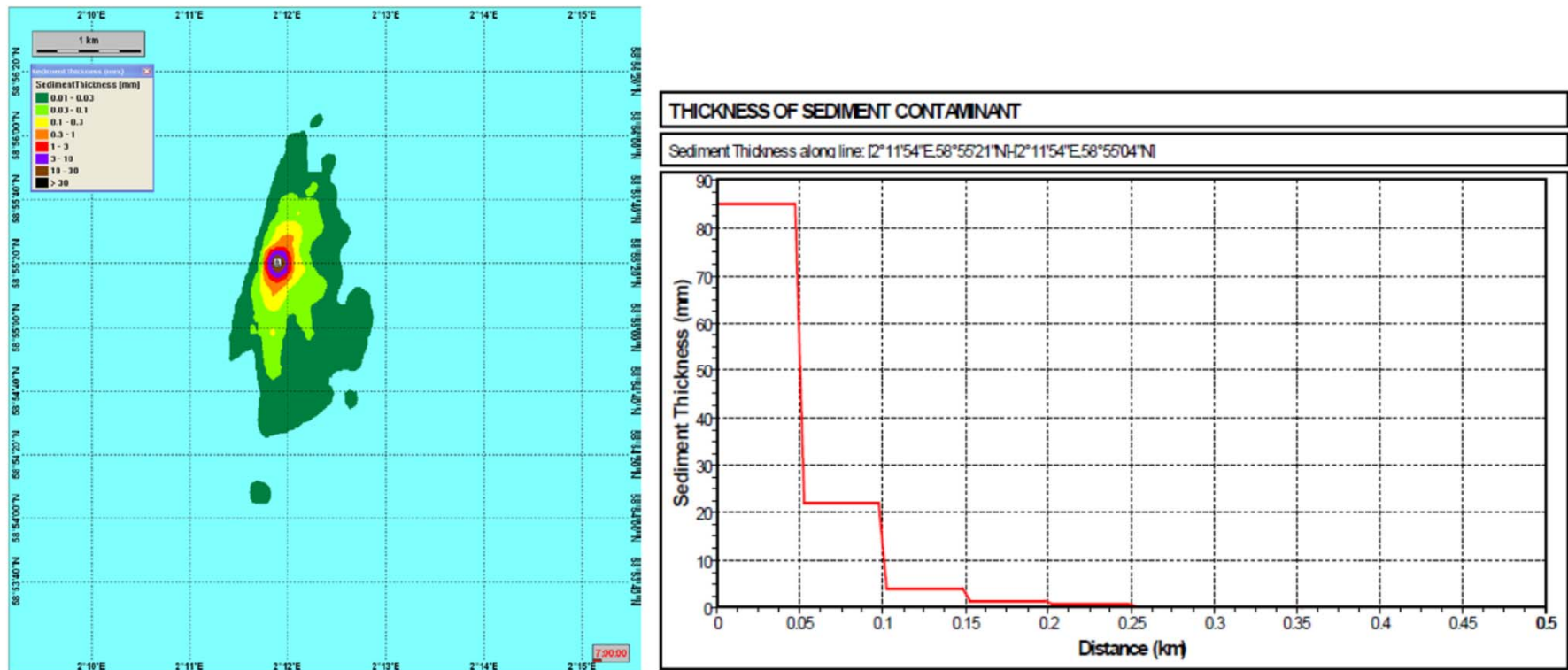


# PRE-ENGINEERING - TASKS

**Tabell 5-1. Foreløpig oversikt over estimerte mengder kaks for typiske produksjonsbrønner på Aasen, West Cable og Hanz**

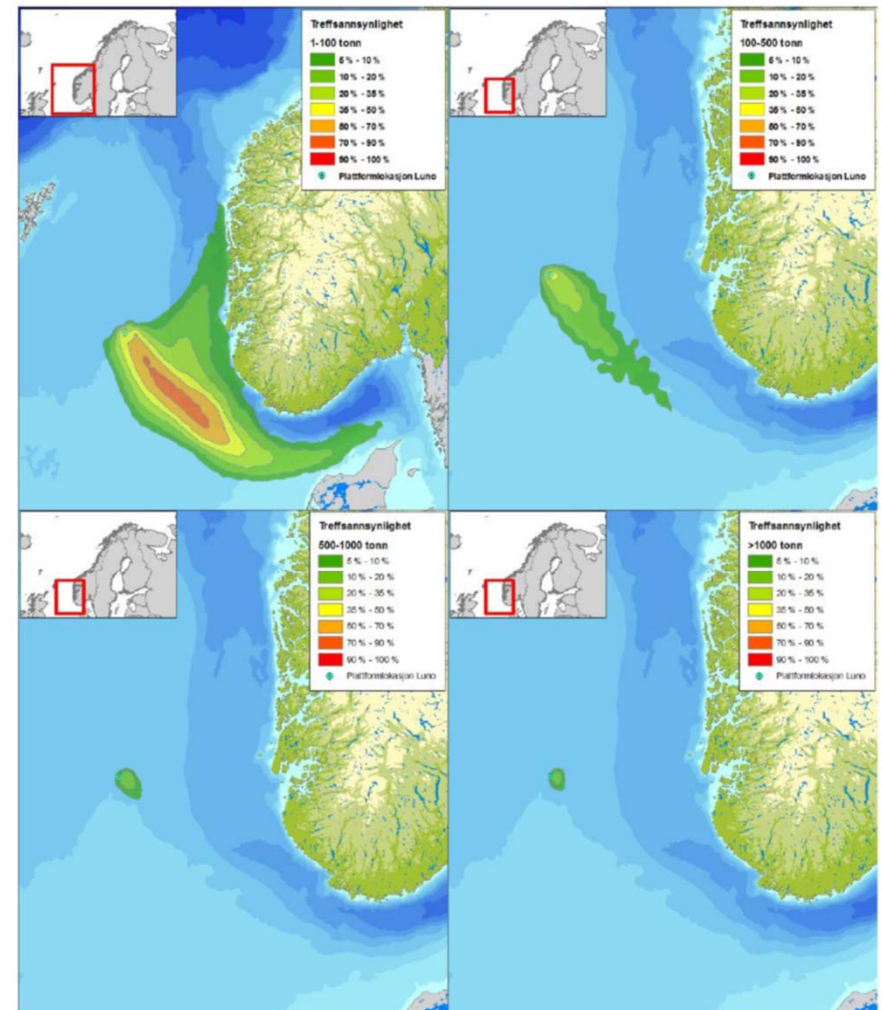
| Seksjon               | Borevæske | Boret lengde (m) |              |              | Mengde borekaks (tonn) |            |            |
|-----------------------|-----------|------------------|--------------|--------------|------------------------|------------|------------|
|                       |           | Aasen            | West Cable   | Hanz         | Aasen                  | West Cable | Hanz       |
| 36"                   | WBM       | 88               | 88           | 86           | 70                     | 70         | 70         |
| 26"                   | WBM       | 370              | 370          | 400          | 150                    | 150        | 160        |
| 17 ½"                 | OBM       | 1 550            | 1 020        | 990          | 310                    | 205        | 200        |
| 12 ¼"                 | OBM       | 860              | 3 890        | 1 700        | 90                     | 390        | 170        |
| 8 ½"                  | OBM       | 1 390            | 1 530        | 90           | 70                     | 80         | 5          |
| <b>SUM (avrundet)</b> |           | <b>4 300</b>     | <b>6 900</b> | <b>3 300</b> | <b>690</b>             | <b>895</b> | <b>605</b> |
| <b>SUM WBM kaks</b>   |           |                  |              |              | <b>220</b>             | <b>220</b> | <b>230</b> |
| <b>SUM OBM kaks</b>   |           |                  |              |              | <b>470</b>             | <b>675</b> | <b>375</b> |

# PRE-ENGINEERING - TASKS



Figur 29. Sedimentering ved utslipp av vannbasert kaks ved havbunnen (sommersituasjon)

# PRE-ENGINEERING - TASKS



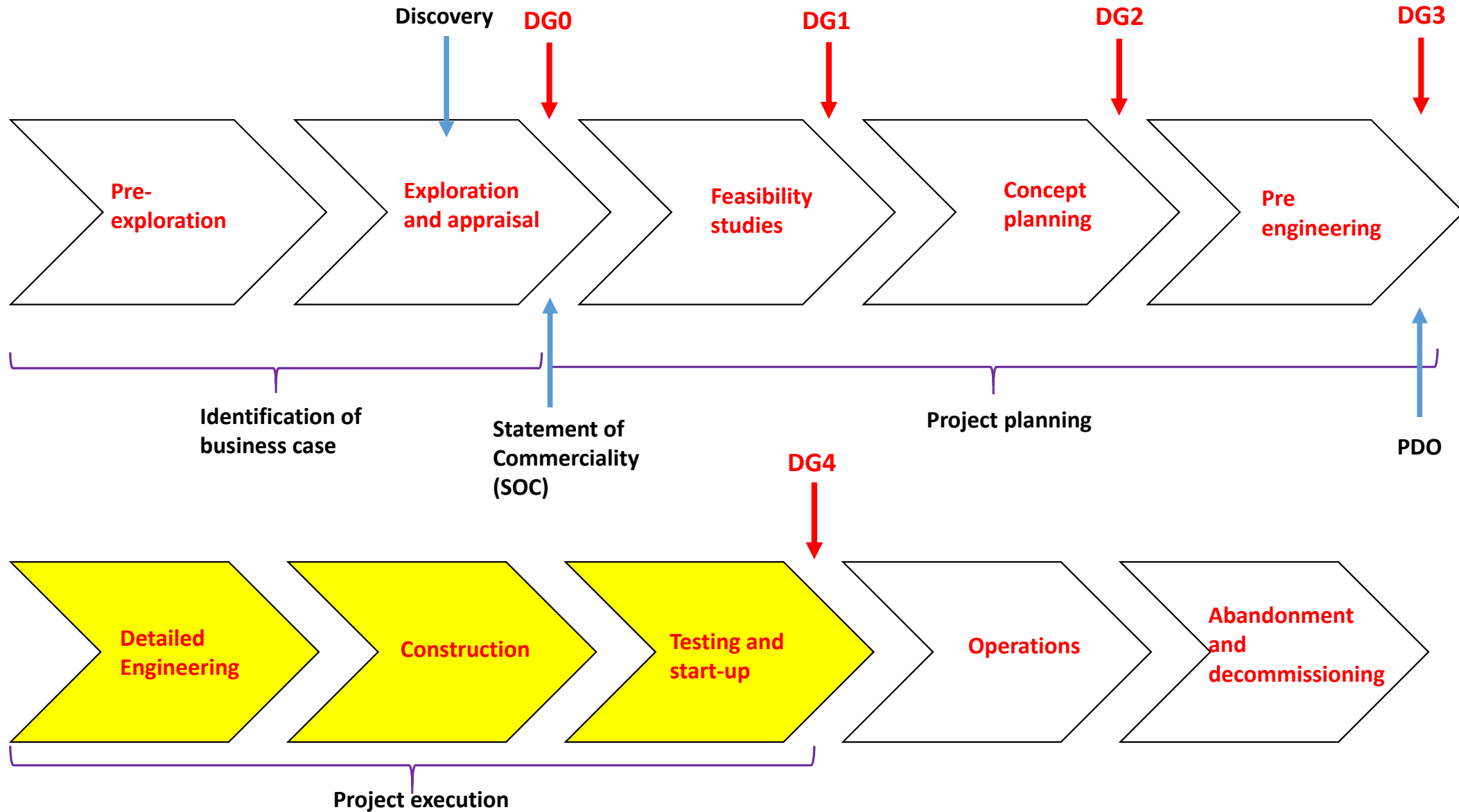
Figur 37. Sannsynligheten for treff av ulike mengdekategorier av olje i 10 × 10 km ruter gitt en sjøbunnsutblåsning fra Aasen/Grieg (helårsstatistikk). Influensområdet er basert på alle utslippsrater og varigheter og deres individuelle sannsynligheter. Merk at det markerte området ikke viser omfanget av et enkelt oljeutslipp, men er det området som berøres i mer enn 5 % av enkeltsimuleringene av oljens drift og spredning (Lundin 2011).

# PRE-ENGINEERING - TASKS

- Wait for the government to study the proposal







# DETAILED ENGINEERING, CONSTRUCTION, TESTING AND STARTUP

**OBJECTIVE:** Detailed design, procurement of the construction materials, construction, installation and commissioning of the agreed facilities.

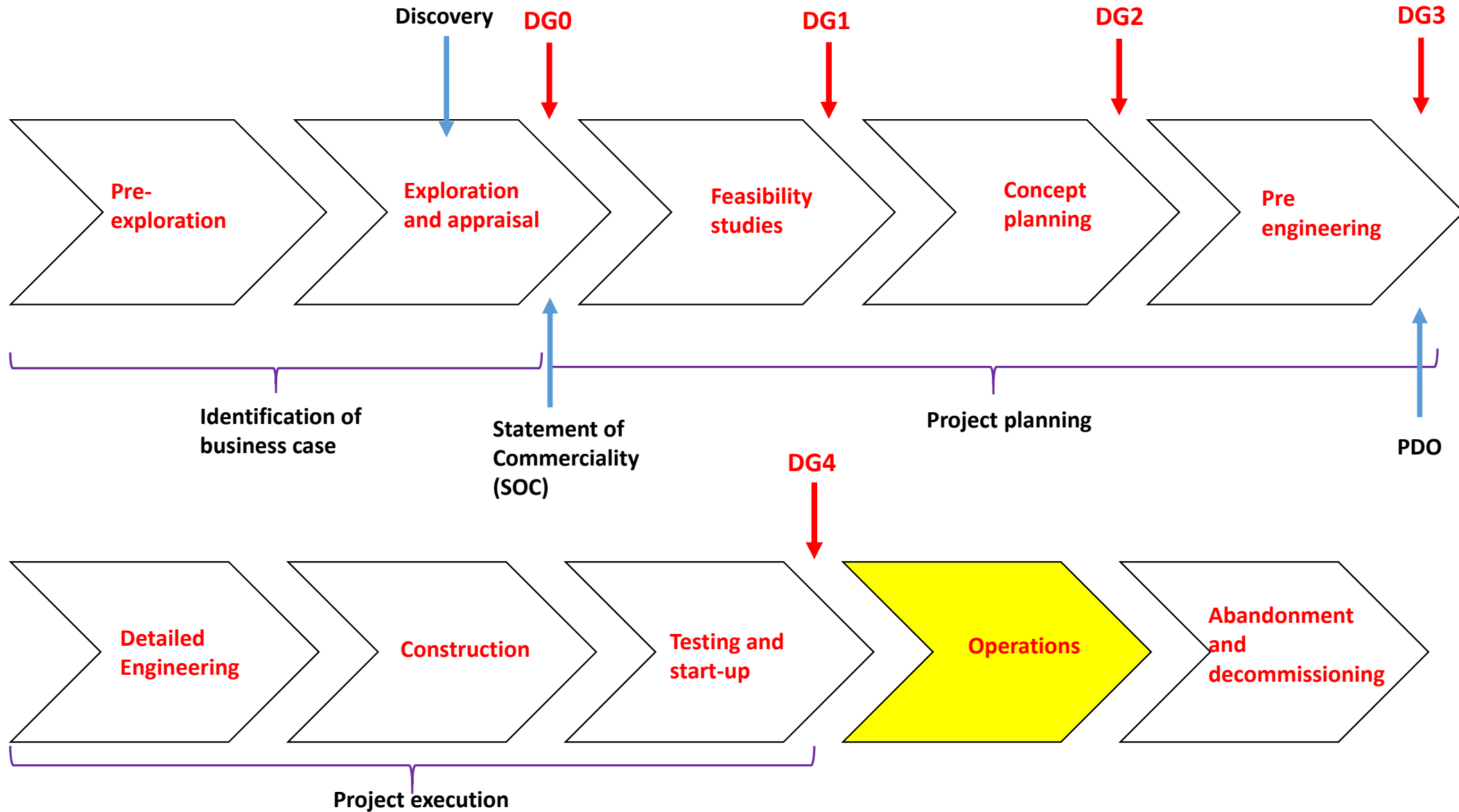
## **Individual contracts**

- Detailed engineering
- Bids, contracts
- Construction, fabrication
- Installation
- Commissioning (Cold or Hot)

**EPCM** (Engineering, procurement, construction, and management contract) with one main contractor.

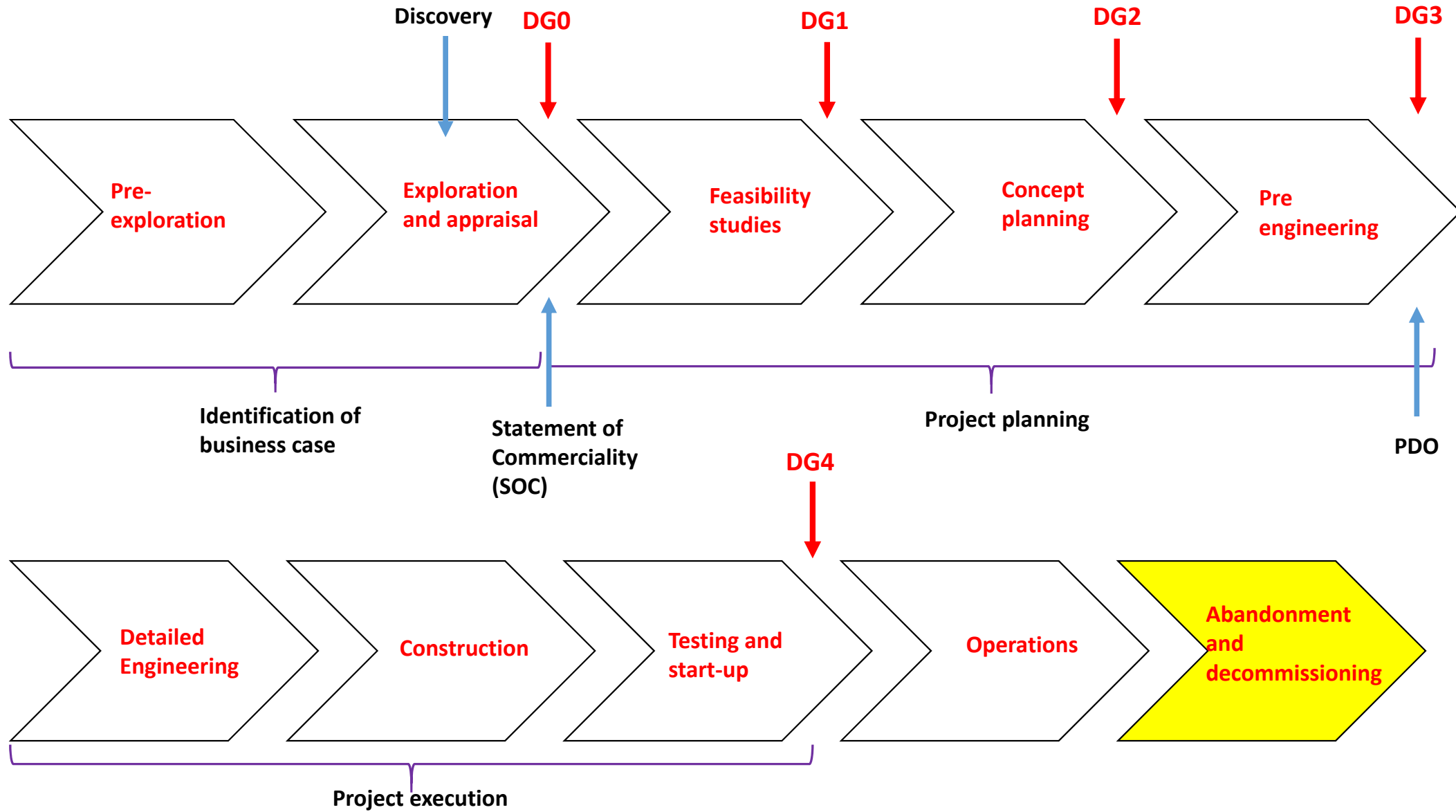
# DETAILED ENGINEERING, CONSTRUCTION, TESTING AND STARTUP

- Constructing wells.
- Perform hand over to asset, operations
- Prepare for start-up, operation and maintenance



# OPERATIONS

- Production startup, Build-up phase, Plateau phase, Decline phase, Tail production, Field shut-down.
- Maintenance.
- Planning Improved Oil recovery methods.
- Allocation and metering.
- De-bottlenecking.
- Troubleshooting.



## DECOMMISSIONING AND ABANDONMENT

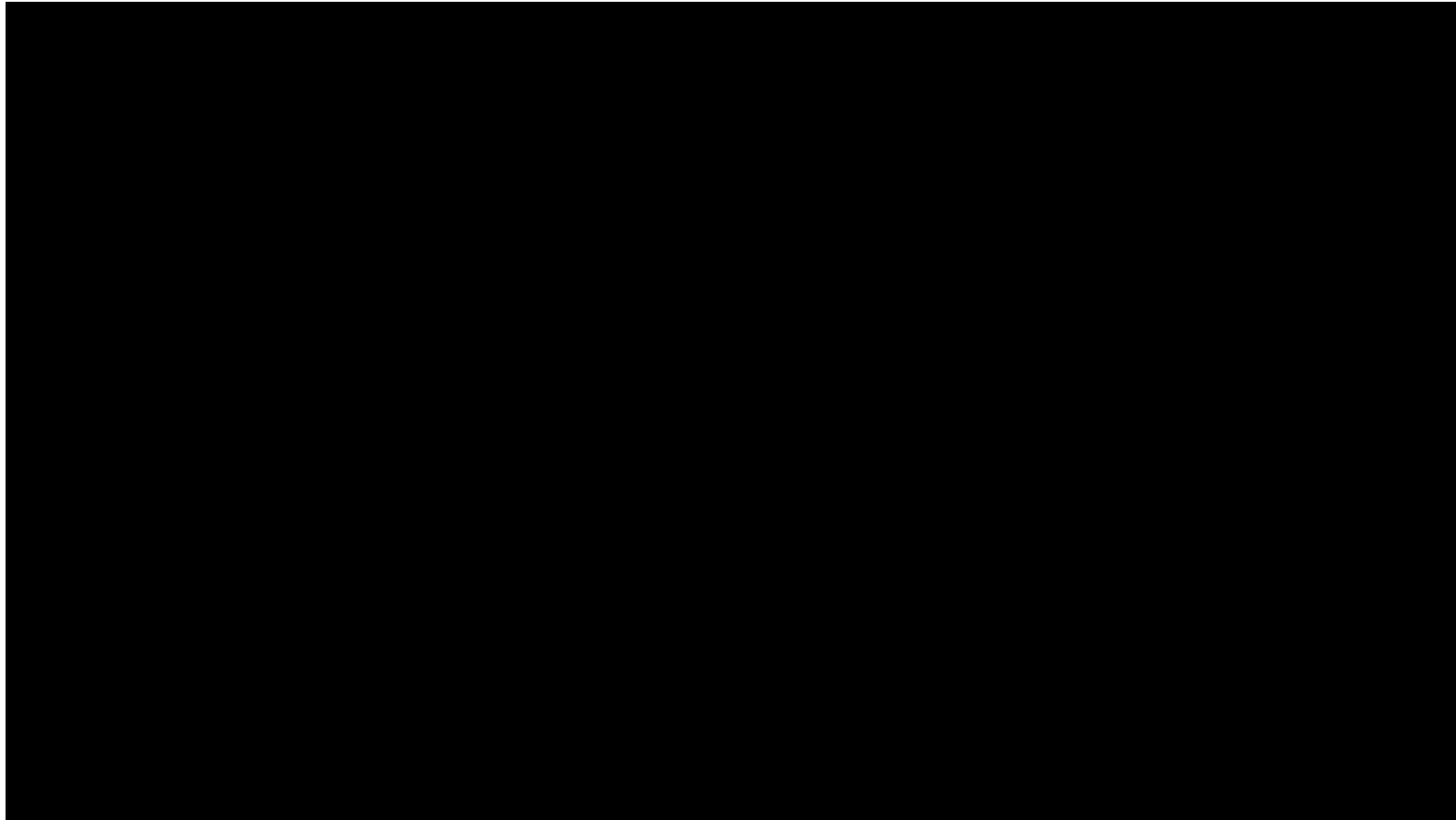
- Engineering “down and clean”: flushing and cleaning tanks, processing equipment, piping.
- Coordinate with relevant environmental and governmental authorities.
- Well plugging and abandonment (P&A)
- Cut and remove well conductor and casing.
- Remove topside equipment.

# DECOMMISSIONING AND ABANDONMENT

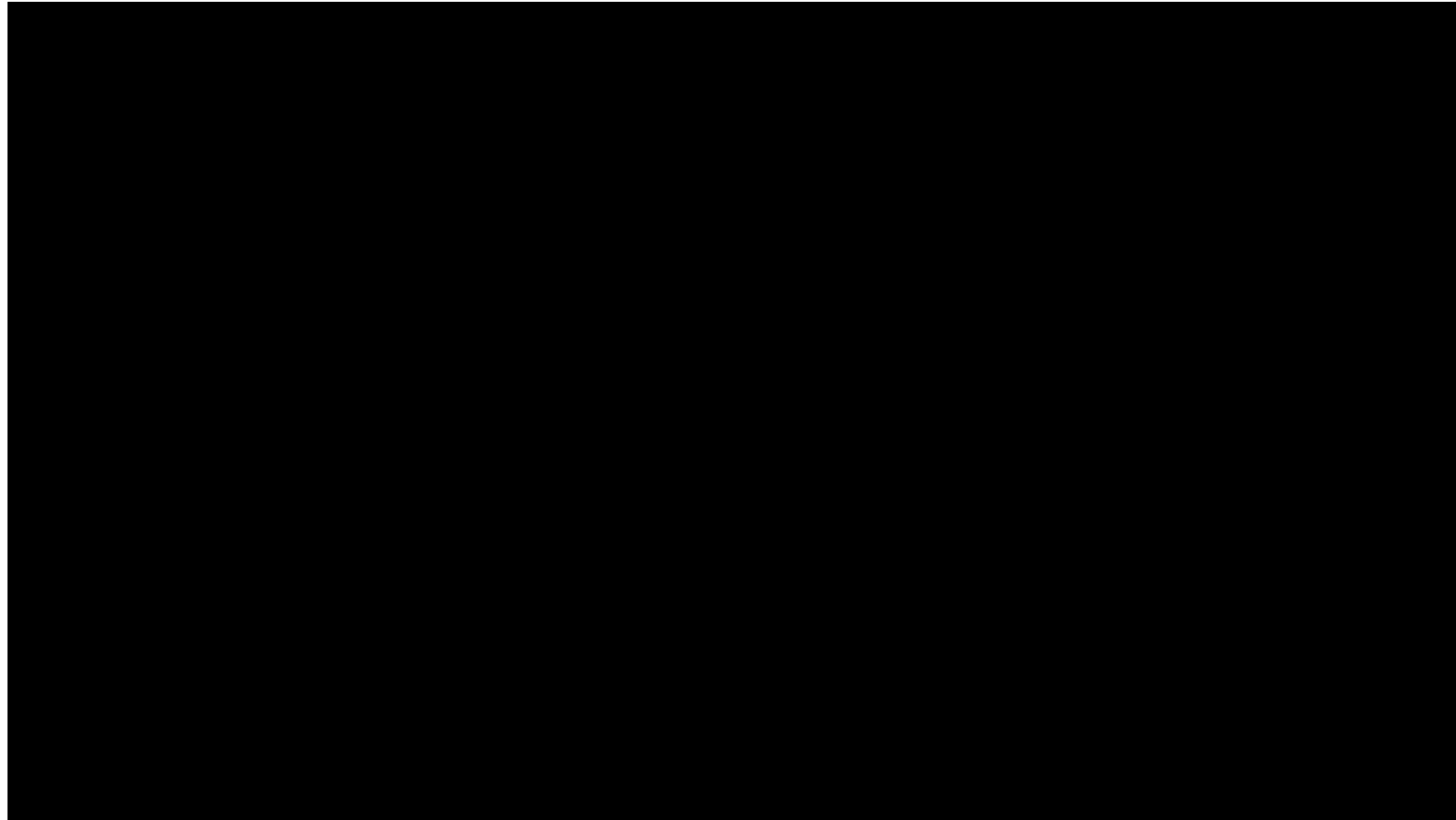
- Removal of the offshore structure: Lifting operations and transport
- Remove or bury subsea pipelines
- Mark and register leftover installations on marine maps
- Monitoring
- Recovery of material: Scrap (steel) and recycling equipment (Gas turbines, separators, heat exchangers, pumps, processing equipment)
- Disposal of residues



# DECOMMISSIONING AND ABANDONMENT



# DECOMMISSIONING AND ABANDONMENT

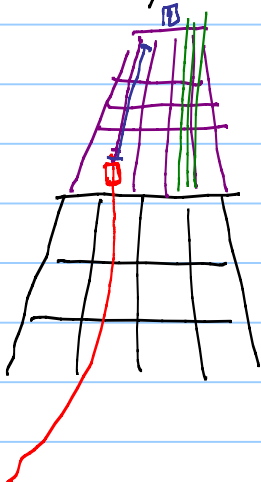


## Offshore structures for oil and gas production

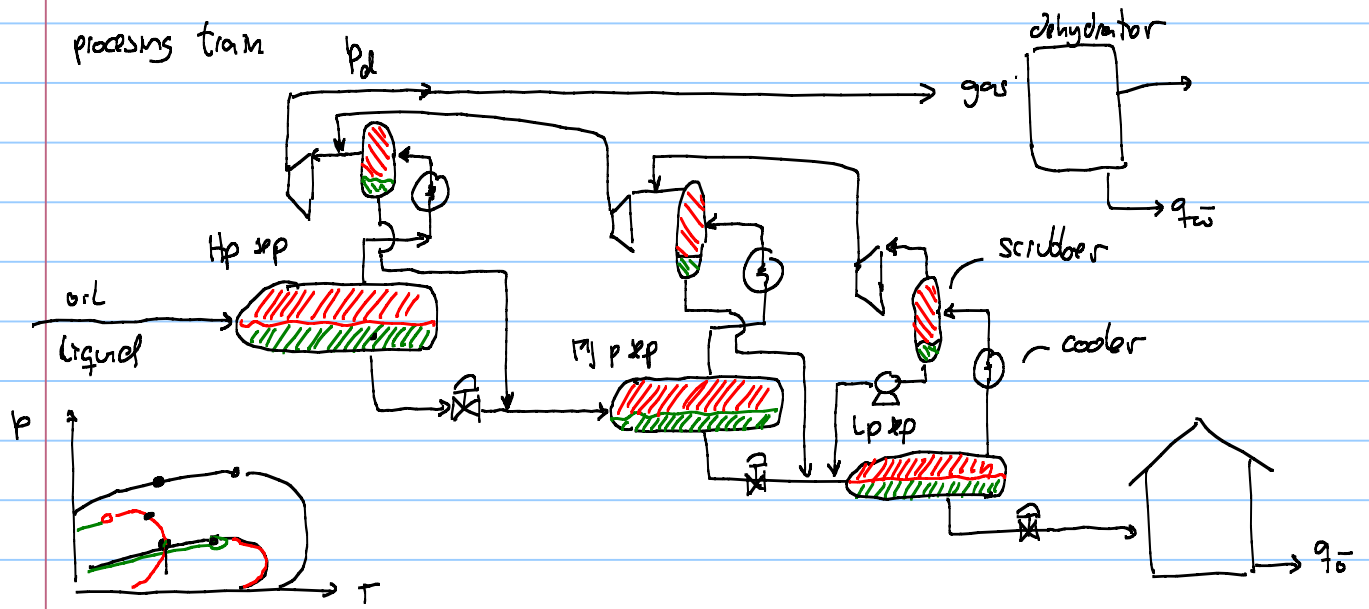
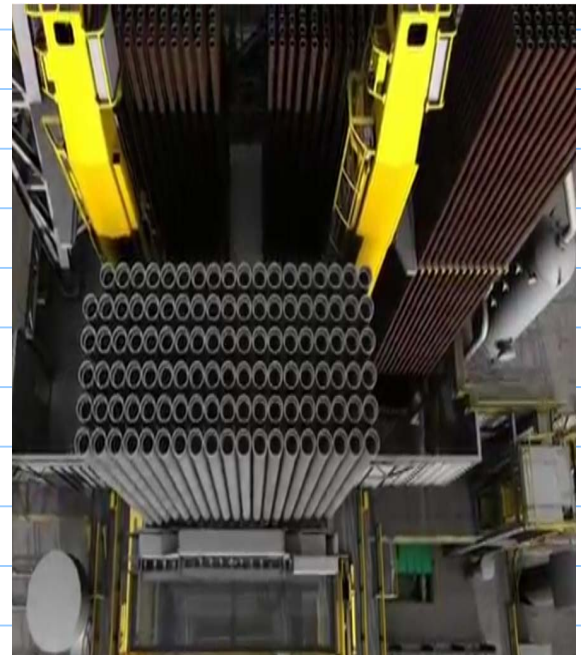
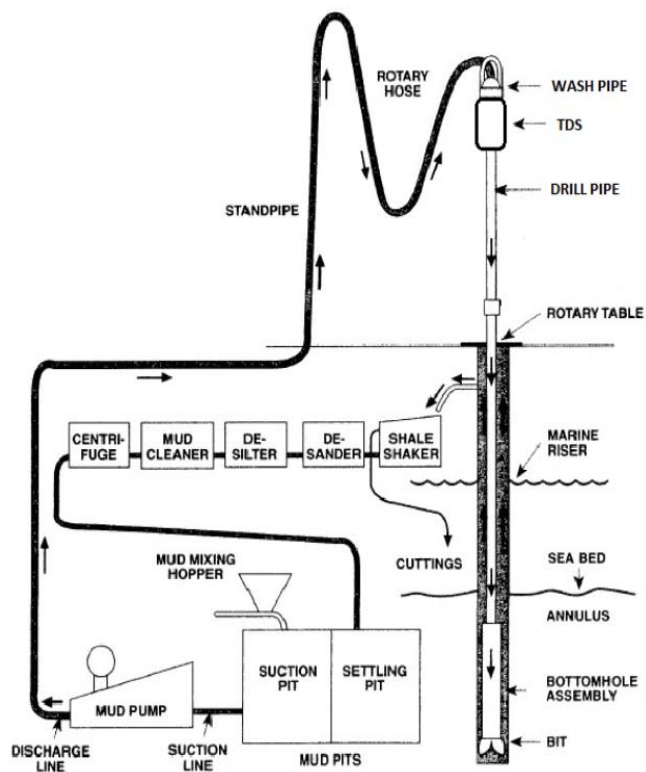
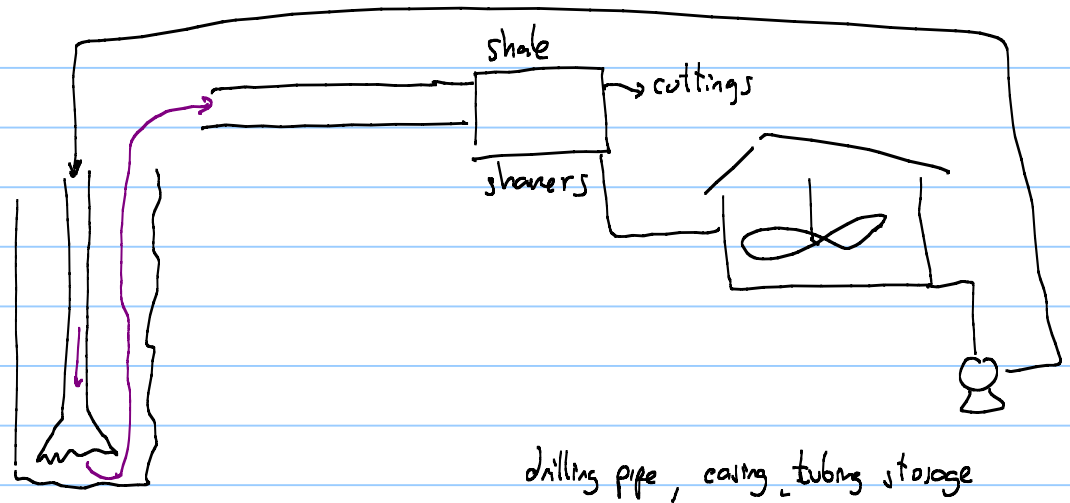
### Components of offshore structure:

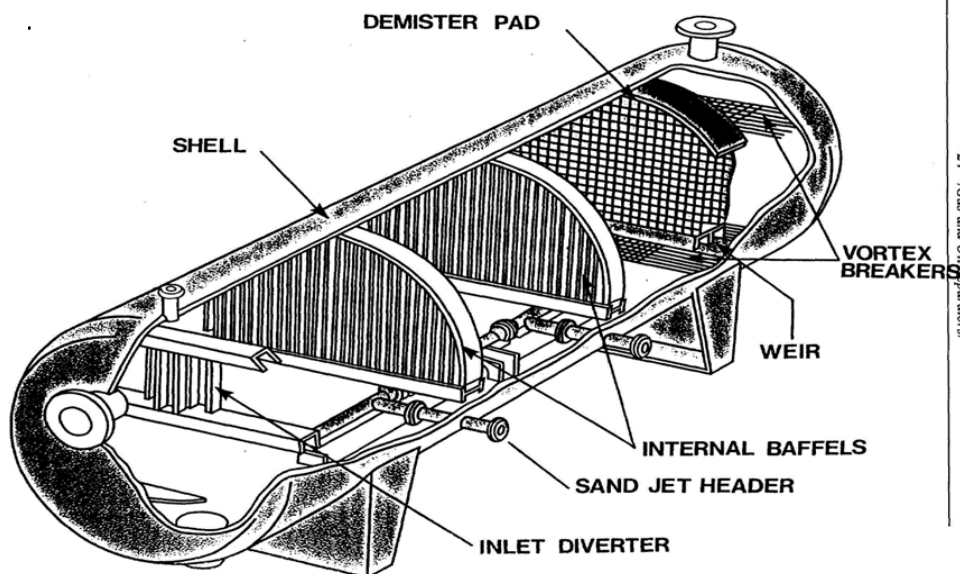
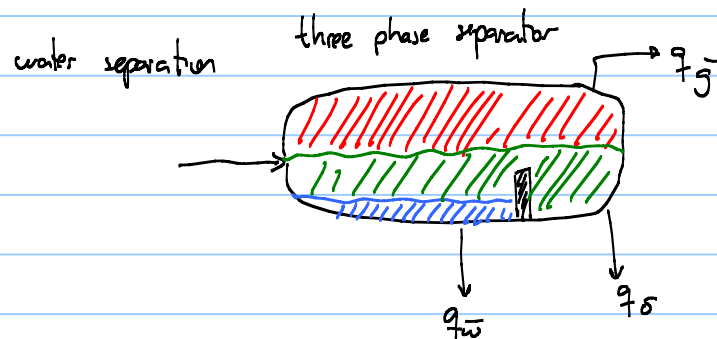
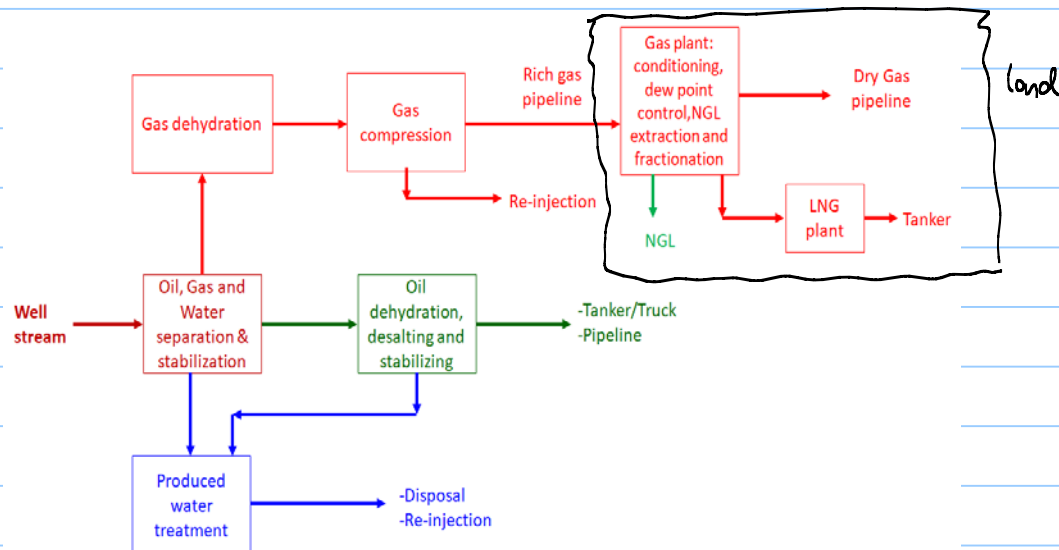
blowout preventor

- Facilities for drilling and full intervention. This includes drilling tower, BOP, (optional) drilling floor, mud package, cementing pumps, storage deck for drill pipes and tubulars, drilling risers.
- - Facilities for light well intervention.   
 ↗ stickline wireline  
 ↘ coiled tubing
- Processing facilities: separator trains for primary oil, gas and water separation, gas processing train, water processing train.
- Gas injection system
- Gas compression units for pipeline transport
- Water injection system
- Living quarters
- Helideck.
- Power generation.   
 ↗ gas turbines
- Flare system.   
 ↗
- Utilities (hydraulic power fluid, compressed air, drinking water unit, air condition system, ventilation and heating system)
- Bay for wellheads and christmas trees (optional)
- Production manifolds
- Oil storage
- Facilities for oil offloading
- Control system
- Monitoring system
- System for storage, injection and recovery of production chemicals (wax, scale, hydrate or corrosion inhibitors), emulsion inhibitor, biocide
- Repair workshop,

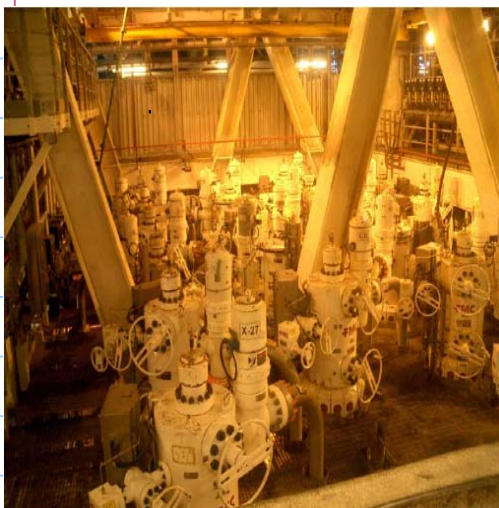


drilling tower



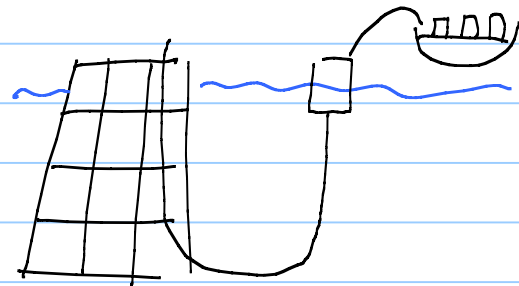


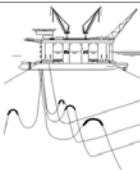
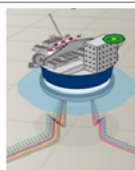
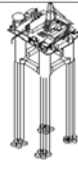
flare



well - bag

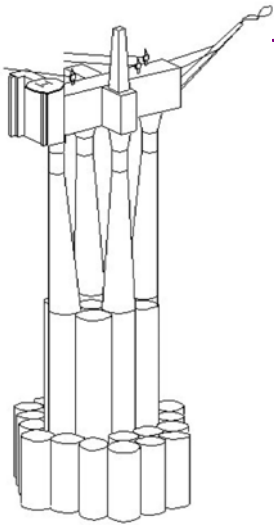
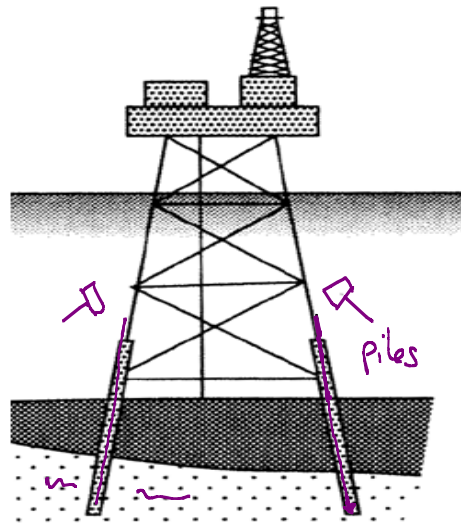
offloading facilities



| Bottom-supported | Fixed                                                                               |                                                                                     | Compliant                                                                           |                                                                                     |                                                                                     |
|------------------|-------------------------------------------------------------------------------------|-------------------------------------------------------------------------------------|-------------------------------------------------------------------------------------|-------------------------------------------------------------------------------------|-------------------------------------------------------------------------------------|
|                  |  |  |  |                                                                                     |                                                                                     |
|                  | Jacket                                                                              | Gravity-Based Structure                                                             | Compliant tower                                                                     |                                                                                     |                                                                                     |
| Floating         | Neutrally buoyant                                                                   |                                                                                     |                                                                                     |                                                                                     | Positively buoyant                                                                  |
|                  |  |  |  |  |  |
|                  | Ship FPSO                                                                           | Semi-Sub                                                                            | Sevan FPSO                                                                          | Spar                                                                                | Tension Leg Platform (TLP)                                                          |



fixed structure

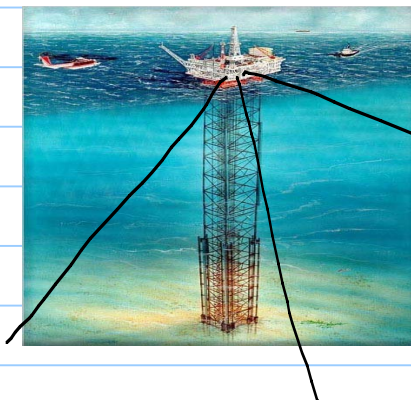
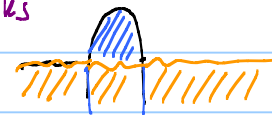


suction anchor

sea bed

mud line

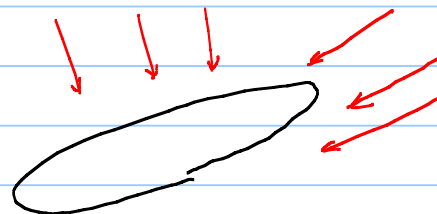
storage tanks

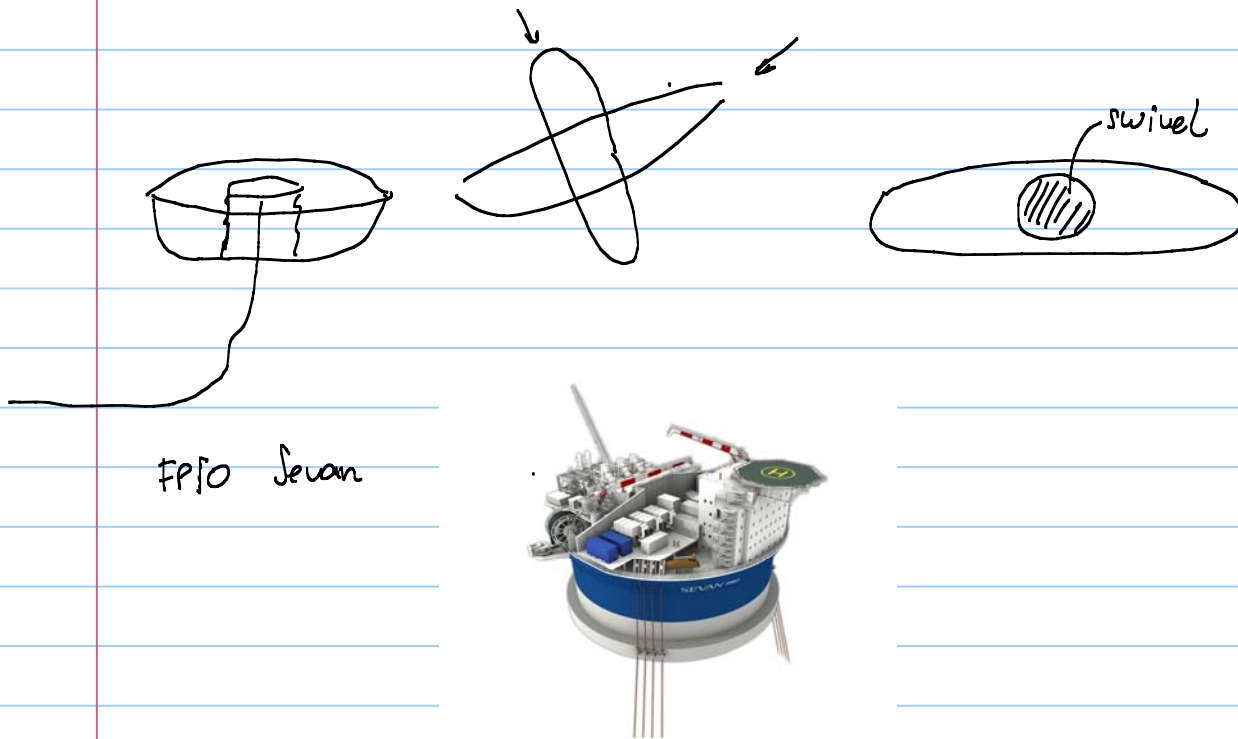


FPSO



high storage (3 EOC stb)



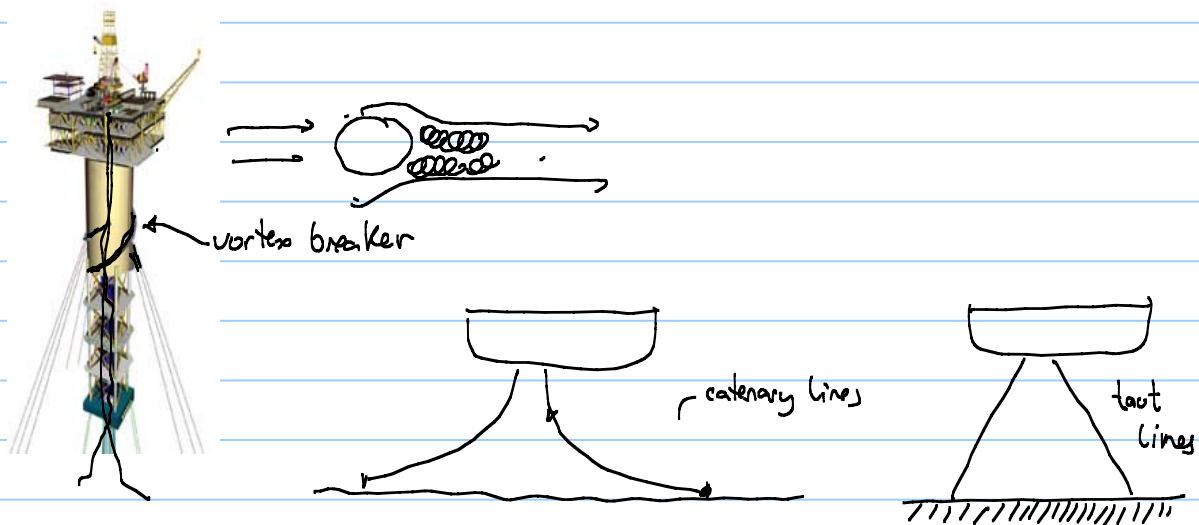


FPSO Sevan



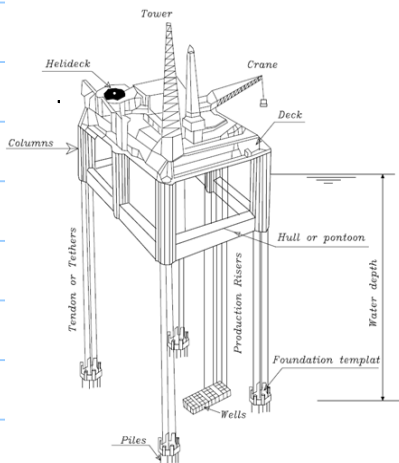
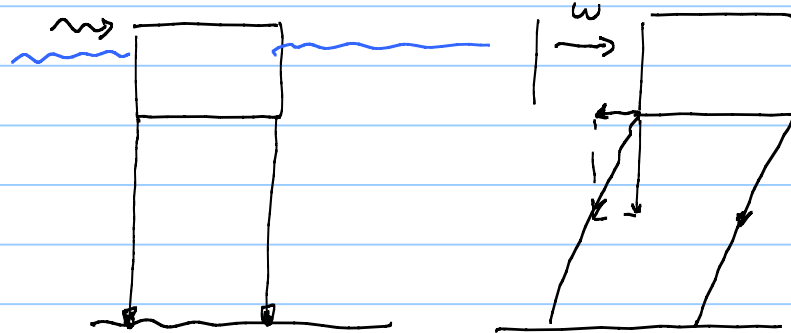
Semi-submersible  
(they are used for drilling subsea)

SPAR





## Positively bougant structure (Tension leg platform)

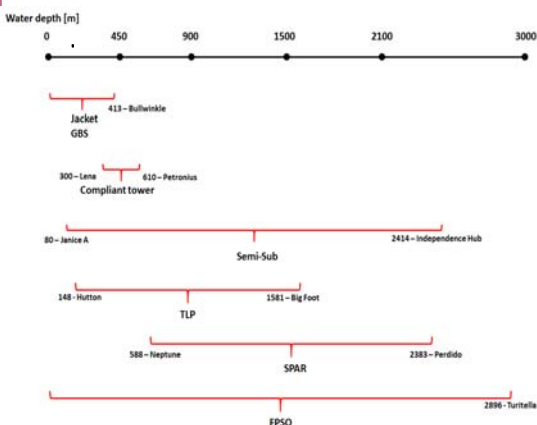


How to we select offshore structures?

technical reasons

1. water depth
2. location of X-mas tree
3. oil storage
4. marine loads

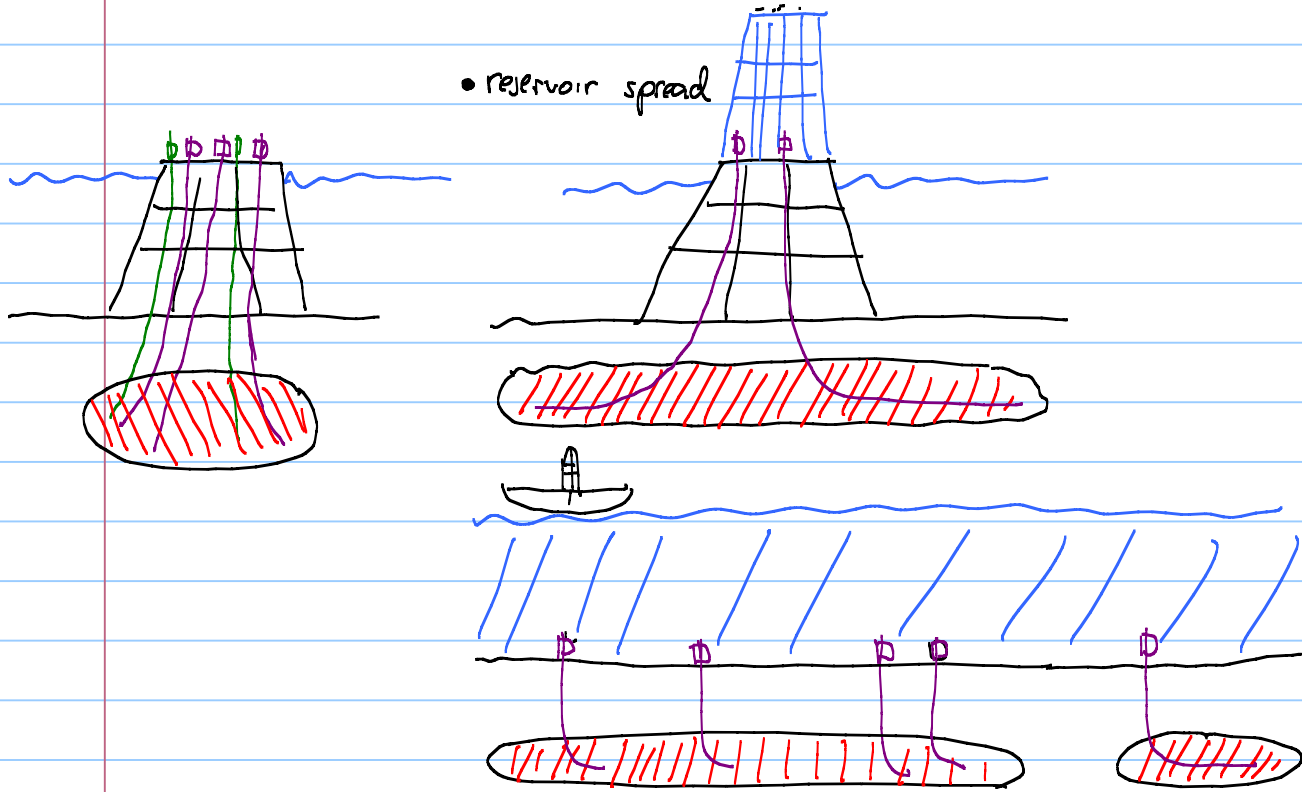
< 600 m bottom supported structures  
> 600 m floating structure



Location of X-mas tree → under the sea  
 → above the sea level

- water depth: only bottom-supported structures, TLP, SPARs allow for dry X-mas trees  
 the current limit is 1500 m

- reservoir spread



- well intervention needs
    - tubing replacement
    - completion modification
    - artificial lift
- ESP lifetime 6 months - 2 years  
 no pump 5 years +

If frequent intervention is needed → dry X-mas trees

If " " is not needed → wet X-mas trees

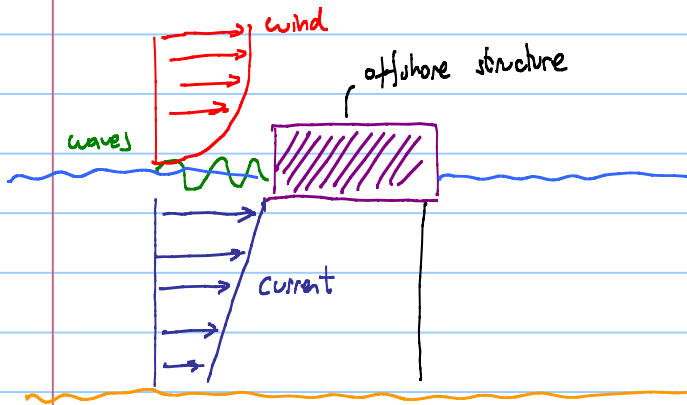
- infill drilling? yes → subsea well might be more suitable. (limited space in platform)

③ oil storage? remoteness → weather conditions → yes!

Structures with storage are GBS, FPSO

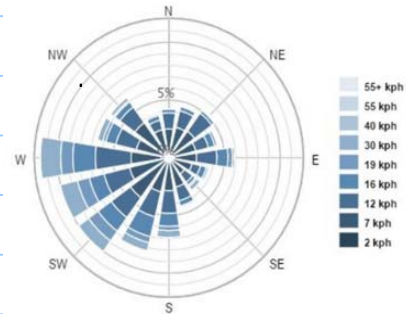
SPAR ~ 150000 stb

• marine loads

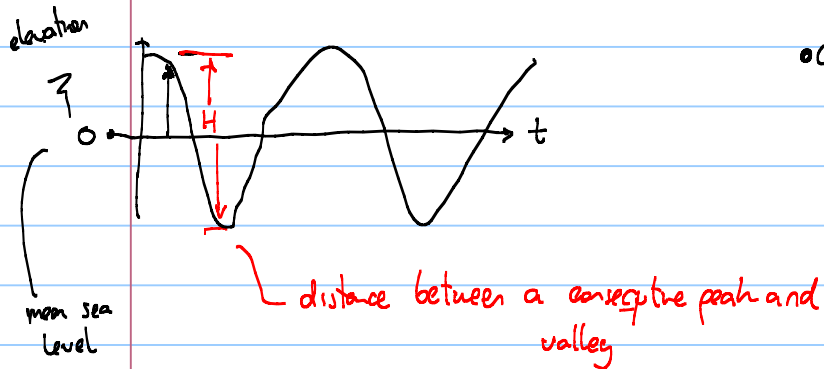


• wind a fixed value is used for design

it's important to look at orientation



• waves

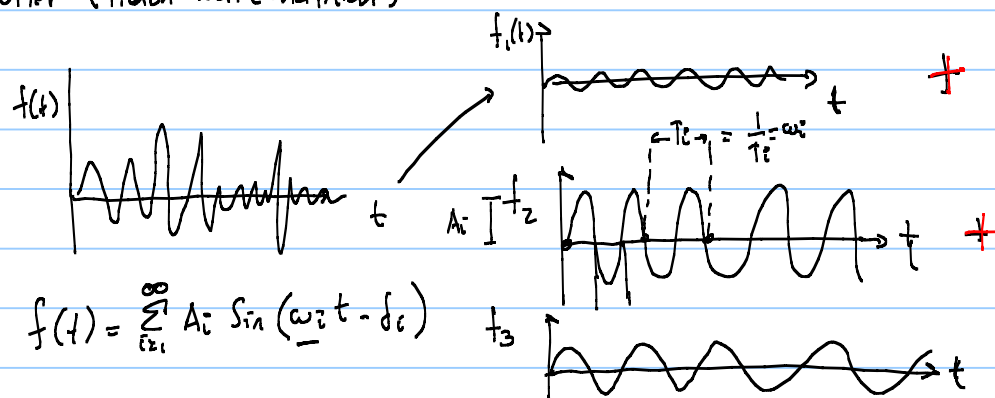


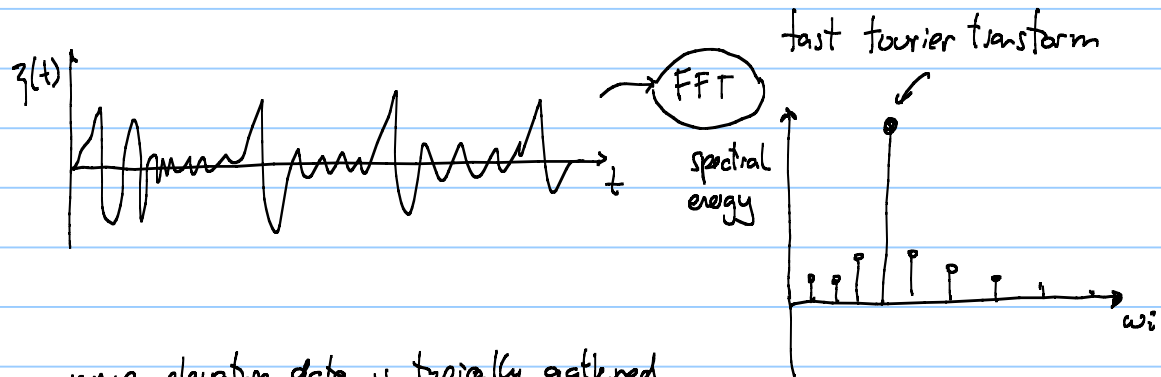
• currents: typically a constant value is used

it is important to look at variation with depth

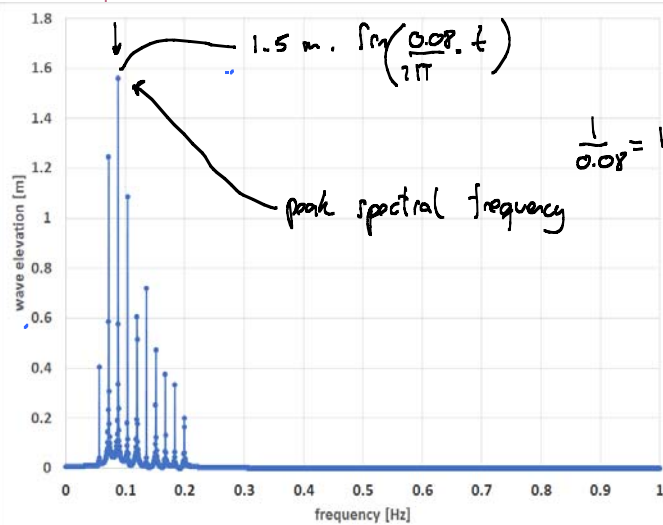
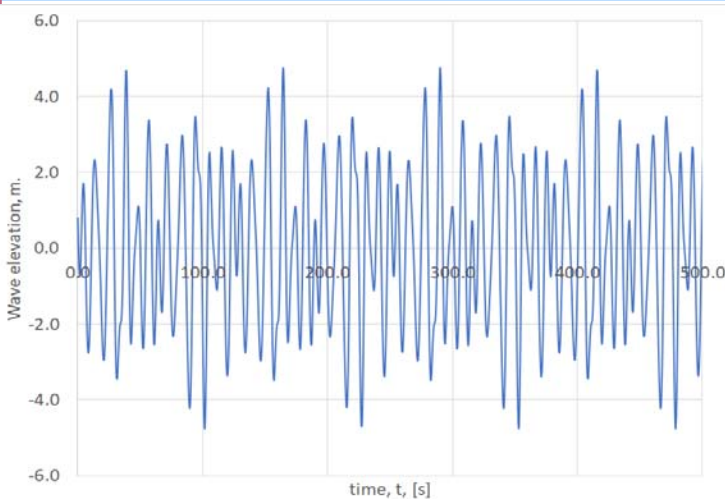
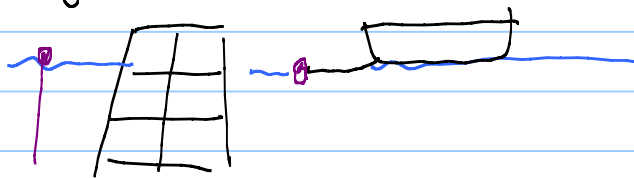


Fourier (trough mathematics)



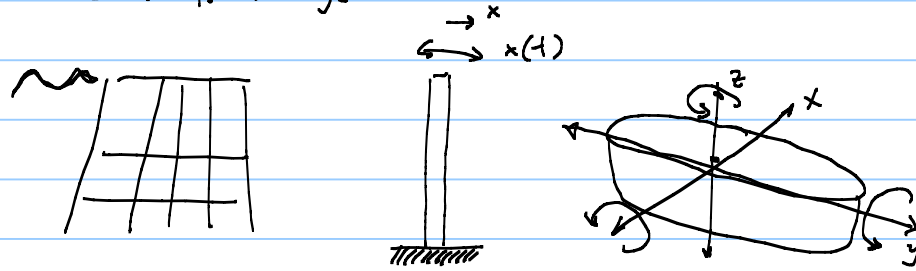


- wave elevation data is typically gathered with buoys



| Time interval [s]              | 2047.5        |          |          |                                          |
|--------------------------------|---------------|----------|----------|------------------------------------------|
| Number of points               | 4096          |          |          |                                          |
| sampling frequency [samples/s] | 2.00          |          |          |                                          |
| Time [s]                       | Elevation [m] | FFT freq | FFT mag  | FFT complex                              |
| 0.0                            | 0.8           | 0        | 0.007144 | -14.6310630637753                        |
| 0.5                            | 0.0           | 0.000    | 0.007144 | -14.6314355376179-2.17584020171838E-002i |
| 1.0                            | -0.5          | 0.001    | 0.007145 | -14.6325531382138-4.35187835418294E-002i |
| 1.5                            | -0.8          | 0.001    | 0.007146 | -14.634416403011-6.52831256995594E-002i  |
| 2.0                            | -0.6          | 0.002    | 0.007147 | -14.6370262285584-8.70534128729824E-002i |
| 2.5                            | -0.1          | 0.002    | 0.007149 | -14.6403838717195-0.108831634337723i     |
| 3.0                            | 0.5           | 0.003    | 0.007151 | -14.6444909513754-0.13061978594503i      |
| 3.5                            | 1.1           | 0.003    | 0.007153 | -14.6493494506153-0.152419871829957i     |
| 4.0                            | 1.6           | 0.004    | 0.007156 | -14.6549617194251-0.174233906173646i     |
| 4.5                            | 1.7           | 0.004    | 0.007159 | -14.6613304778867-0.196063915009091i     |
| 5.0                            | 1.5           | 0.005    | 0.007163 | -14.6684588198886-0.217911938100365i     |
| 5.5                            | 0.9           | 0.005    | 0.007167 | -14.6763502173536-0.239780030911572i     |
| 6.0                            | 0.2           | 0.006    | 0.007172 | -14.6850085250036-0.261670266637959i     |
| 6.5                            | -0.7          | 0.006    | 0.007176 | -14.6944379856753-0.283584738366725i     |
| 7.0                            | -1.6          | 0.007    | 0.007182 | -14.7046432361733-0.305525561331911i     |
| 7.5                            | -2.3          | 0.007    | 0.007187 | -14.7156293137251-0.327494875310597i     |
| 8.0                            | -2.7          | 0.008    | 0.007193 | -14.727401663005-0.349494847163372i      |

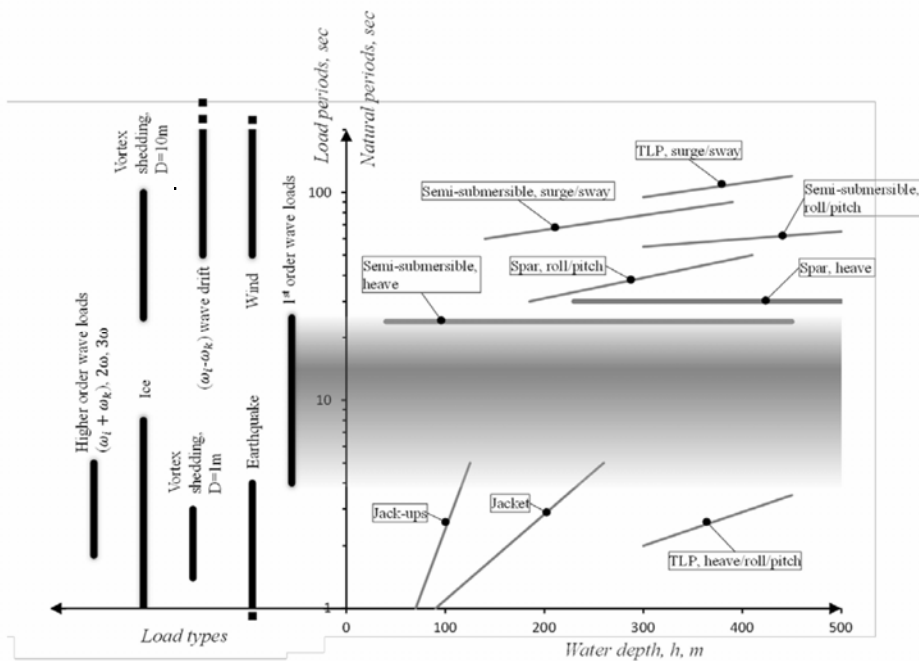
offshore structures move in different ways



natural frequency

if wave frequency is close to the natural frequency of structure then movement will be maximum, stress will also be maximum  $\rightarrow$  high risk of failure

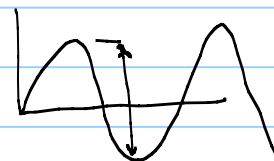
$$T = \frac{1}{\omega}$$



1 assumption to gather wave data: sea state is a period of (3hrs)  
peak spectral period time when the spectral period

| period of time | $t_p$ | $H_s$ | doesn't change much     |
|----------------|-------|-------|-------------------------|
| 1              | 12,5  | ( )   | significant wave height |
| 2              | 9     | ( )   |                         |
| 3              | 2     | ( )   |                         |
| 4              |       |       |                         |
| 5              |       |       |                         |

100.000



- visualize sea-state data

|        | Spectral Peak period ( $T_p$ ) [s] |     |      |      |       |       |       |       |       |       |       |       |       |       |       |       |       |       |       |       |       |       |       |        |  |  |  |
|--------|------------------------------------|-----|------|------|-------|-------|-------|-------|-------|-------|-------|-------|-------|-------|-------|-------|-------|-------|-------|-------|-------|-------|-------|--------|--|--|--|
| Hs [m] | 0-3                                | 3-4 | 4-5  | 5-6  | 6-7   | 7-8   | 8-9   | 9-10  | 10-11 | 11-12 | 12-13 | 13-14 | 14-15 | 15-16 | 16-17 | 17-18 | 18-19 | 19-20 | 20-21 | 21-22 | 22-23 | 23-24 | 24-25 | Sum    |  |  |  |
| 0-1    | 15                                 | 290 | 1367 | 2876 | 3716  | 3527  | 2734  | 1849  | 1138  | 656   | 362   | 192   | 101   | 52    | 26    | 13    | 7     | 3     | 2     | 1     | 0     | 0     | 0     | 18927  |  |  |  |
| 1-2    | 1                                  | 81  | 1153 | 5308 | 12083 | 17323 | 18143 | 15262 | 10980 | 7053  | 4169  | 2316  | 1229  | 631   | 315   | 155   | 75    | 36    | 17    | 8     | 4     | 5     | 1     | 96348  |  |  |  |
| 2-3    | 0                                  | 2   | 94   | 1050 | 4532  | 10304 | 15020 | 15953 | 13457 | 9752  | 5991  | 3403  | 1795  | 894   | 426   | 197   | 88    | 39    | 17    | 7     | 3     | 1     | 1     | 83026  |  |  |  |
| 3-4    | 0                                  | 0   | 2    | 72   | 686   | 2782  | 6171  | 8847  | 9189  | 7493  | 5082  | 2991  | 1577  | 762   | 345   | 148   | 61    | 24    | 9     | 4     | 1     | 0     | 0     | 46246  |  |  |  |
| 4-5    | 0                                  | 0   | 0    | 2    | 51    | 433   | 1645  | 3495  | 4807  | 4750  | 3638  | 2286  | 1229  | 584   | 251   | 100   | 37    | 13    | 5     | 1     | 0     | 0     | 0     | 23327  |  |  |  |
| 5-6    | 0                                  | 0   | 0    | 0    | 2     | 39    | 294   | 1037  | 2069  | 2664  | 2440  | 1709  | 968   | 463   | 193   | 72    | 25    | 8     | 2     | 1     | 0     | 0     | 0     | 11986  |  |  |  |
| 6-7    | 0                                  | 0   | 0    | 0    | 0     | 2     | 32    | 215   | 692   | 1264  | 1485  | 1228  | 767   | 382   | 159   | 57    | 18    | 5     | 1     | 0     | 0     | 0     | 0     | 6307   |  |  |  |
| 7-8    | 0                                  | 0   | 0    | 0    | 0     | 0     | 2     | 27    | 157   | 447   | 730   | 762   | 555   | 302   | 130   | 46    | 14    | 4     | 1     | 0     | 0     | 0     | 0     | 3177   |  |  |  |
| 8-9    | 0                                  | 0   | 0    | 0    | 0     | 0     | 0     | 2     | 23    | 112   | 276   | 392   | 355   | 223   | 104   | 38    | 11    | 3     | 1     | 0     | 0     | 0     | 0     | 1540   |  |  |  |
| 9-10   | 0                                  | 0   | 0    | 0    | 0     | 0     | 0     | 0     | 2     | 19    | 77    | 160   | 192   | 148   | 79    | 31    | 9     | 2     | 0     | 0     | 0     | 0     | 0     | 719    |  |  |  |
| 10-11  | 0                                  | 0   | 0    | 0    | 0     | 0     | 0     | 0     | 0     | 2     | 16    | 50    | 85    | 85    | 55    | 24    | 8     | 2     | 0     | 0     | 0     | 0     | 0     | 327    |  |  |  |
| 11-12  | 0                                  | 0   | 0    | 0    | 0     | 0     | 0     | 0     | 0     | 0     | 2     | 12    | 29    | 40    | 33    | 18    | 7     | 2     | 0     | 0     | 0     | 0     | 0     | 143    |  |  |  |
| 12-13  | 0                                  | 0   | 0    | 0    | 0     | 0     | 0     | 0     | 0     | 0     | 0     | 2     | 8     | 15    | 17    | 12    | 5     | 2     | 0     | 0     | 0     | 0     | 0     | 61     |  |  |  |
| 13-14  | 0                                  | 0   | 0    | 0    | 0     | 0     | 0     | 0     | 0     | 0     | 0     | 0     | 2     | 5     | 7     | 6     | 4     | 1     | 0     | 0     | 0     | 0     | 0     | 25     |  |  |  |
| 14-15  | 0                                  | 0   | 0    | 0    | 0     | 0     | 0     | 0     | 0     | 0     | 0     | 0     | 0     | 1     | 2     | 3     | 2     | 1     | 0     | 0     | 0     | 0     | 0     | 9      |  |  |  |
| 15-16  | 0                                  | 0   | 0    | 0    | 0     | 0     | 0     | 0     | 0     | 0     | 0     | 0     | 0     | 0     | 1     | 1     | 1     | 1     | 0     | 0     | 0     | 0     | 0     | 4      |  |  |  |
| 16-17  | 0                                  | 0   | 0    | 0    | 0     | 0     | 0     | 0     | 0     | 0     | 0     | 0     | 0     | 0     | 0     | 0     | 0     | 0     | 0     | 0     | 0     | 0     | 0     | 0      |  |  |  |
| 17-18  | 0                                  | 0   | 0    | 0    | 0     | 0     | 0     | 0     | 0     | 0     | 0     | 0     | 0     | 0     | 0     | 0     | 0     | 0     | 0     | 0     | 0     | 0     | 0     | 0      |  |  |  |
| Sum    | 16                                 | 373 | 2616 | 9308 | 21070 | 34410 | 44041 | 46687 | 42514 | 34212 | 24268 | 15503 | 8892  | 4587  | 2143  | 921   | 372   | 146   | 55    | 22    | 8     | 6     | 2     | 292172 |  |  |  |

I have to select an offshore structure which natural period is NOT the most frequent spectral peak period in this chart !

Michael Golan refreshment of concepts

(1) Molecular weight of pure component, (2) mole fraction, (3) apparent molecular weight of a mixture, (4) conversions between: component moles-mole fraction-component mass-mass fraction.

$$\overset{2+16}{\text{H}_2\text{O}} \quad \text{mw} = 18 \frac{\text{kg}}{\text{kmol}} \quad \frac{\text{g}}{\text{mol}}$$

exercise: air: 18 mol  $\text{O}_2$        $\chi_{\text{O}_2} = \frac{18}{18+78+4}$

78 mol  $\text{N}_2$        $\chi_{\text{O}_2} = 0.18$

4 mol  $\text{CO}_2$        $\chi_{\text{N}_2} = 0.78$

$\text{O}_2 \rightarrow \text{mw} = 32$

$\text{N}_2 \rightarrow \text{mw} = 28$

$\text{CO}_2 \rightarrow \text{mw} = 44$

$\chi_{\text{CO}_2} = 0.04$

$$M_{\text{air}}? \quad M_{\text{air}} = M_{\text{O}_2} \cdot X_{\text{O}_2} + M_{\text{N}_2} \cdot X_{\text{N}_2} + M_{\text{CO}_2} \cdot X_{\text{CO}_2}$$

$$M_{\text{air}} = 32 \cdot 0.18 + 28 \cdot 0.78 + 48 \cdot 0.04$$

$$M_{\text{air}} = 29.52$$

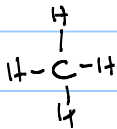
$$M_{\text{air}} = 28.97 \quad \text{in petroleum}$$

$$\text{for gases} \quad Y_g = \frac{M_{\text{gas}}}{M_{\text{air}}} \quad Y_g = 0.8 \quad M_{\text{gas}} = ?$$

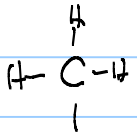
specific gas gravity

$$M_{\text{gas}} = 0.8 \cdot 28.97$$

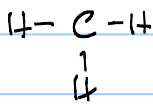
$$M_{\text{gas}} = 23.176$$



$$M_{\text{methane}} = 16$$



$$M_{\text{ethane}} = 30$$



mass fraction?  $[Y]$

$$\text{not} \quad \frac{\text{kg}}{\text{kmol}} \quad \frac{\text{g}}{\text{mol}}$$

$$Y_{\text{O}_2} = \frac{m_{\text{O}_2}}{m_T} = \frac{(n_{\text{O}_2}) \cdot M_{\text{O}_2}}{(n_T) \cdot M_{\text{air}}} =$$

$$\text{mass fraction } Y_{\text{O}_2} = \underset{\substack{\uparrow \\ \text{mole fraction}}}{X_{\text{O}_2}} \cdot \left( \frac{M_{\text{O}_2}}{M_{\text{air}}} \right)$$

$$Y_{\text{O}_2} = \frac{18}{100 \text{ moles}} \cdot \frac{32}{29.52} = 0.195$$



the end