



ROSE
Rock Seismic Research Project

S-waves in acoustic transversely isotropic media with a tilted symmetry axis

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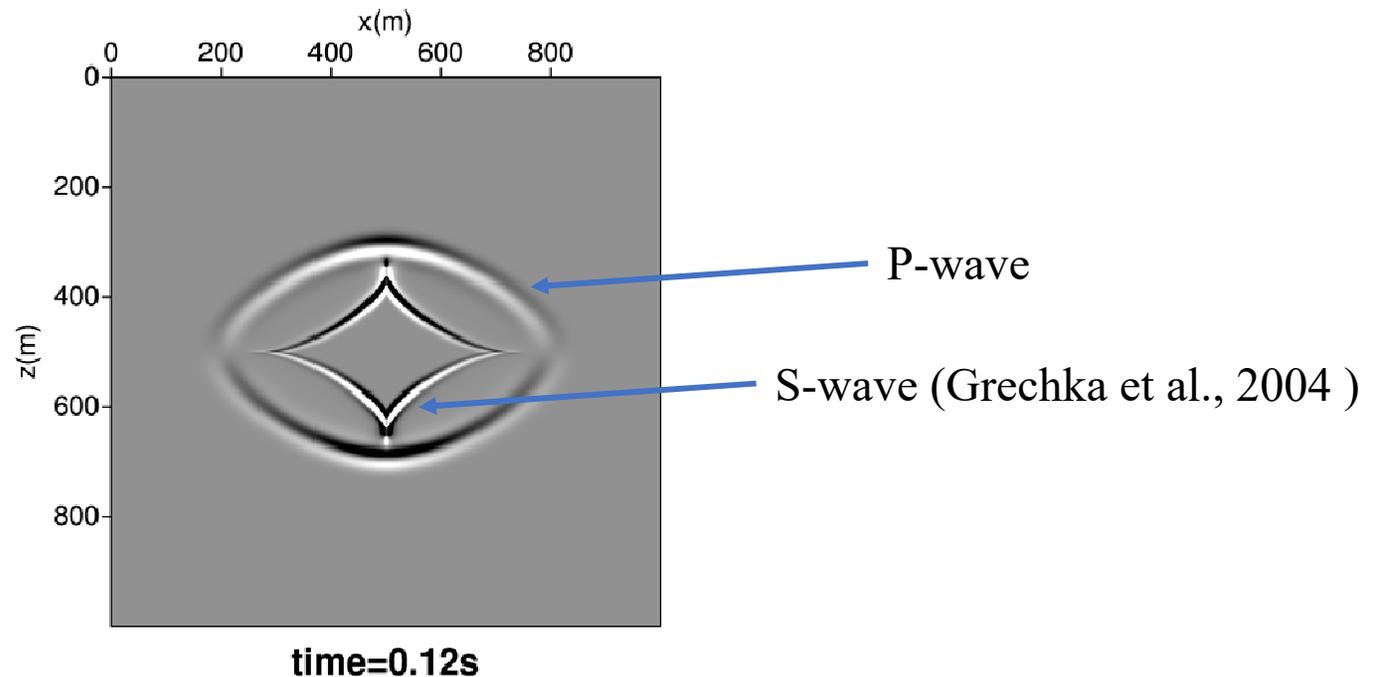
23. 04. 2018 Trondheim

Outline

- An overview of the acoustic anisotropic media
- Slowness surface
- Travelttime functions
- S-wave in multi-layered acoustic TTI media
- Reflected waves and converted waves
- Conclusion

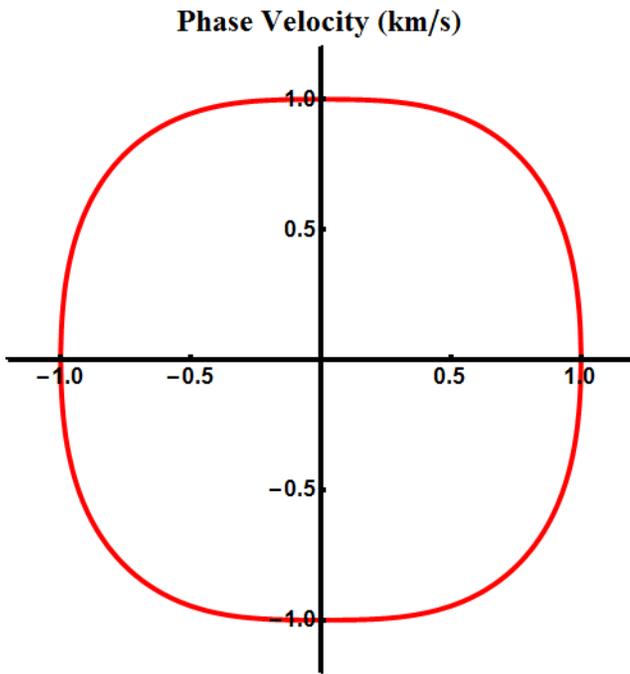
An overview of the acoustic anisotropic media

The acoustic VTI medium was firstly proposed by setting the $v_{s0} = 0$ (Alkhalifah, 1998).

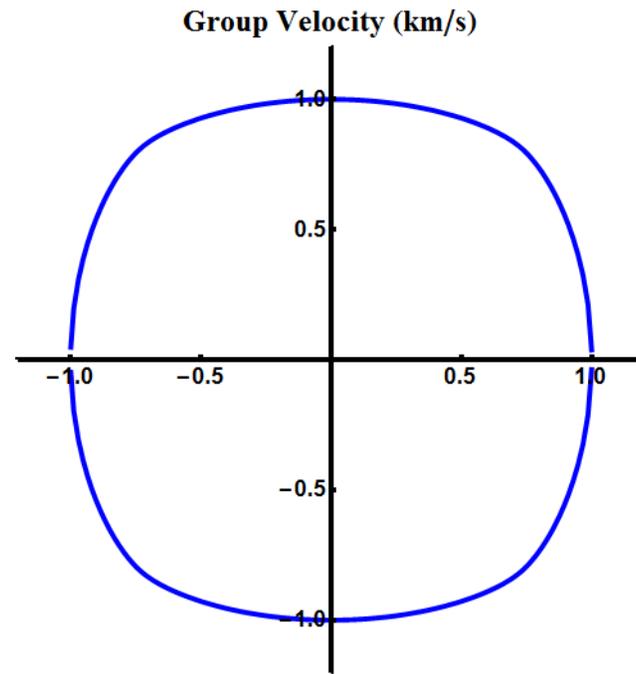


An overview of the acoustic anisotropic media

SV-wave in elastic VTI media

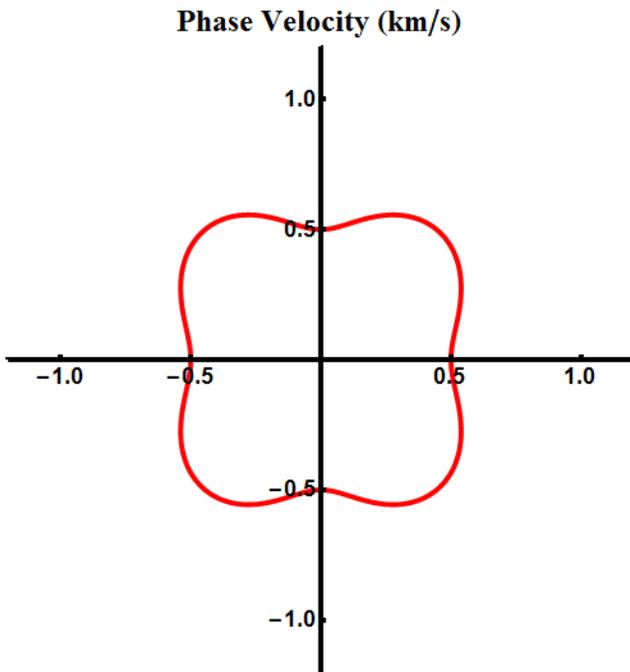


$$v_{S0} = 1.0 \text{ km/s}$$

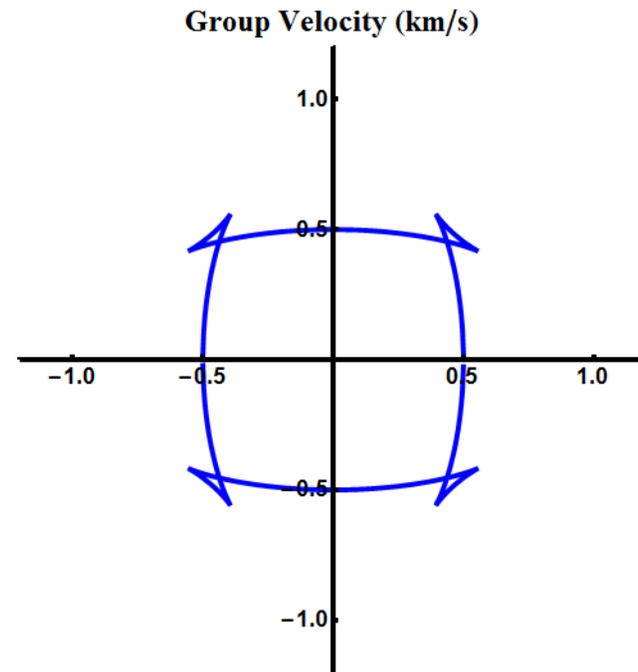


An overview of the acoustic anisotropic media

SV-wave in elastic VTI media



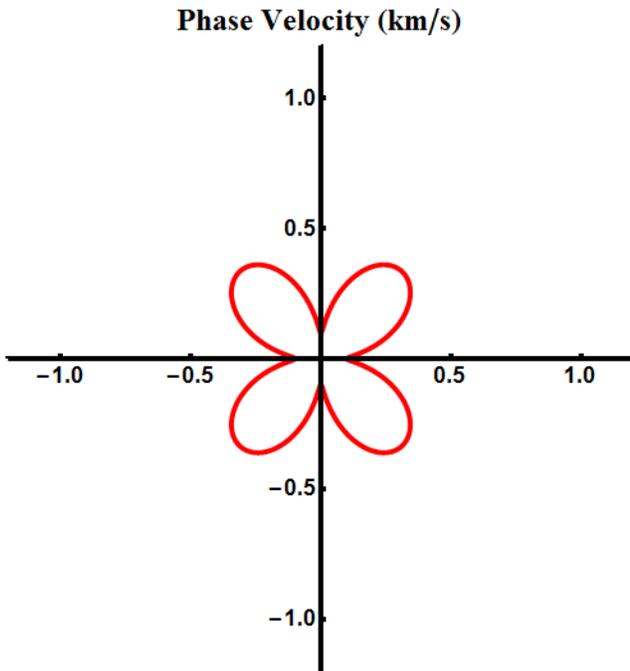
$$v_{S0} = 0.5 \text{ km/s}$$



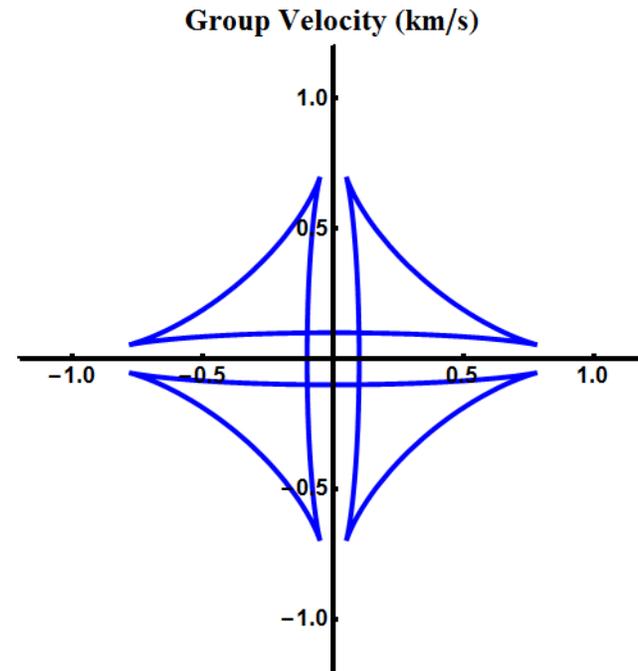
off-axis triplication

An overview of the acoustic anisotropic media

SV-wave in elastic VTI media



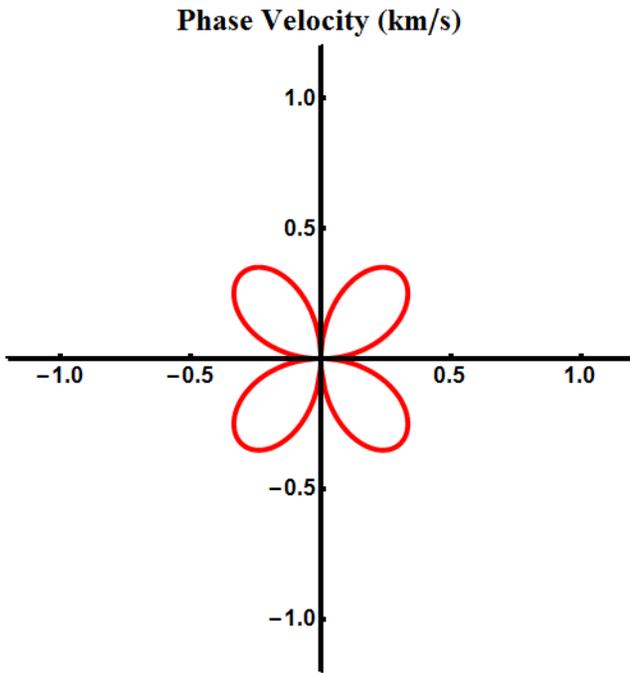
$$v_{S0} = 0.1 \text{ km/s}$$



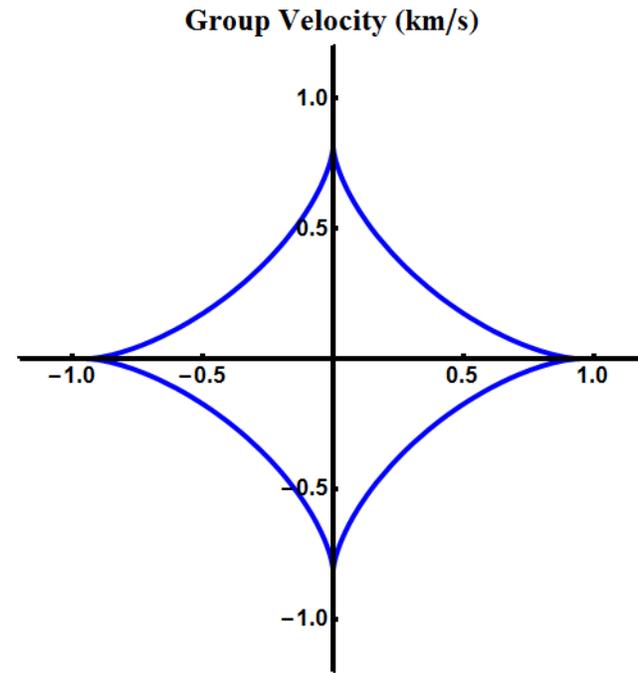
off-axis triplexation

An overview of the acoustic anisotropic media

S-wave in acoustic VTI media



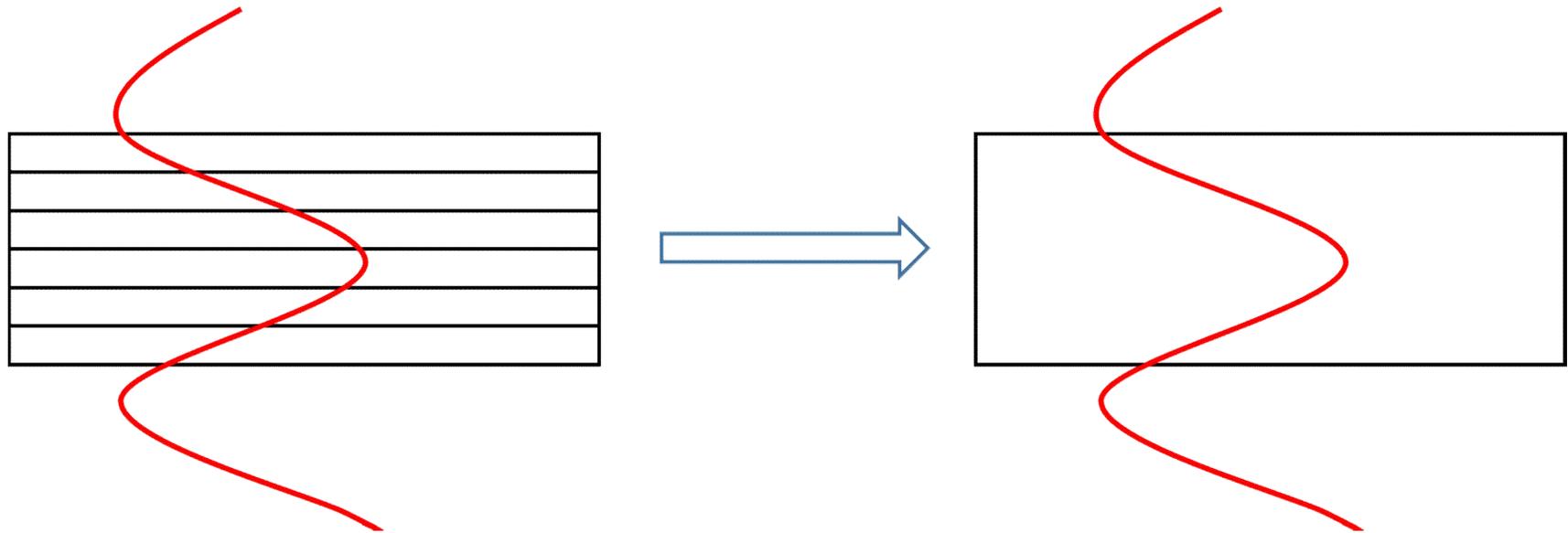
$$v_{S0} = 0.0 \text{ km/s}$$



off-axis triplication

An overview of the acoustic anisotropic media

Acoustic VTI media can also be practical from the upscaling point of view (Grechka et al., 2004).

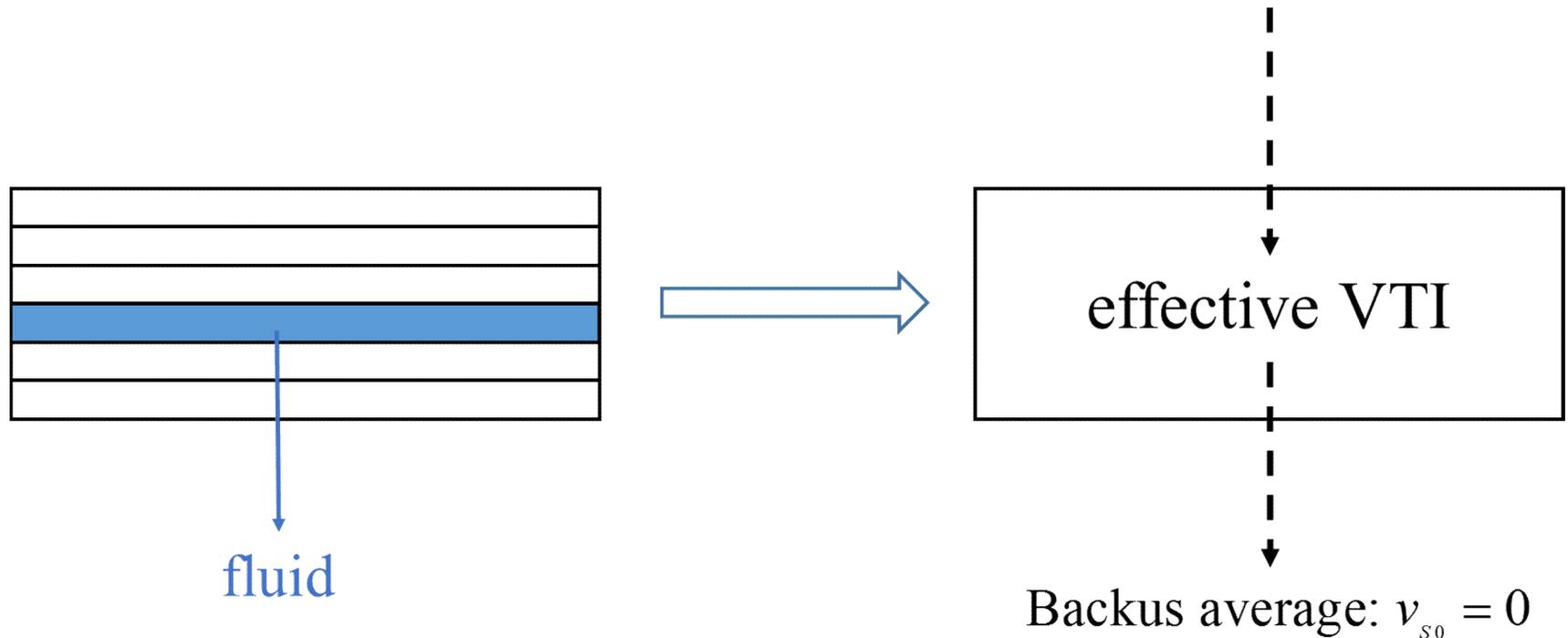


thin isotropic/VTI layers

effective VTI

long wave equivalent medium theory (Backus, 1962)

An overview of the acoustic anisotropic media



The acoustic TI media can be obtained by:

- manually setting the $v_{s0} = 0$
- equivalent media from the upscaling point of view

Anomalously low S-wave velocity (10-50m/s) was observed in unconsolidated ocean-bottom sediments (Ayres and Theilen, 1999).

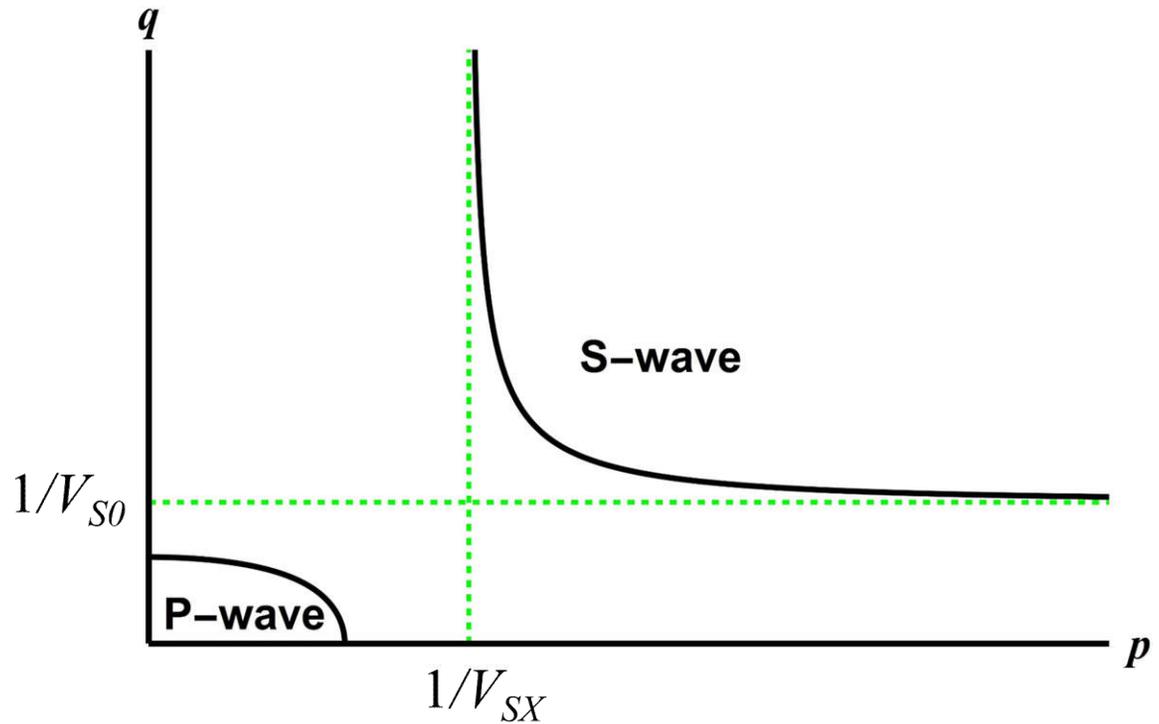
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Slowness surface

For the acoustic VTI medium,
the slowness surface is
(Alkhalifah, 1998)

$$q = \frac{1}{v_{p0}} \sqrt{\frac{(1 + 2\eta)v_{pn}^2 p^2 - 1}{2\eta v_{pn}^2 p^2 - 1}}$$



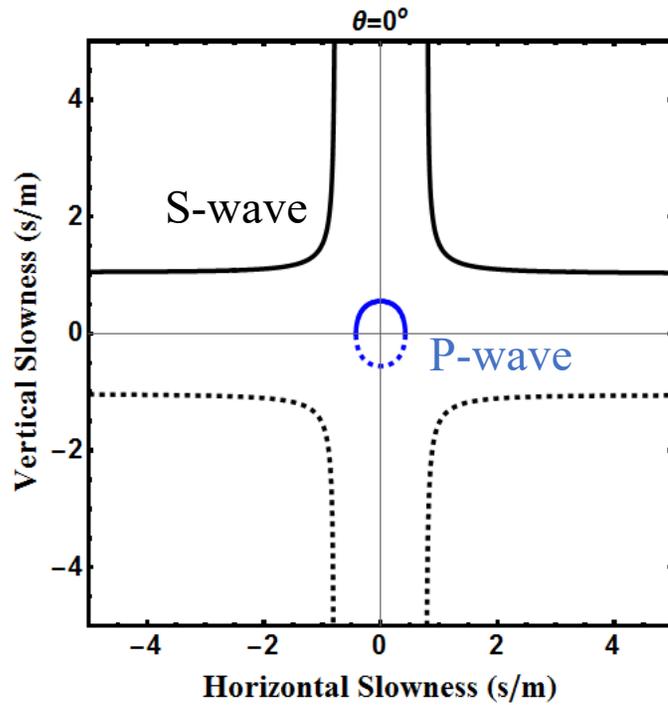
Slowness mapping from VTI to TTI

$$\begin{bmatrix} p_n \\ q_n \end{bmatrix} = \begin{bmatrix} \cos \theta & \sin \theta \\ -\sin \theta & \cos \theta \end{bmatrix} \begin{bmatrix} p \\ q \end{bmatrix}$$

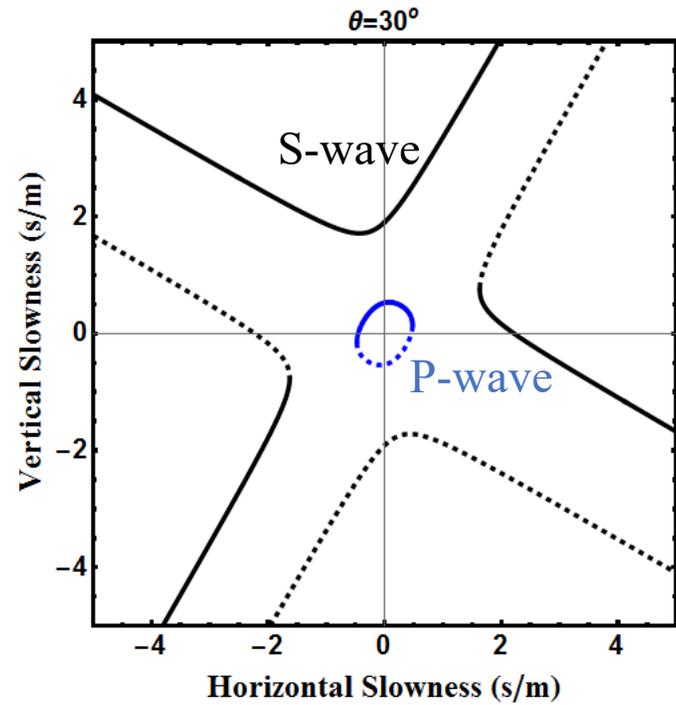
↓
TTI

↓
VTI

Slowness surface



Acoustic VTI



Acoustic TTI

Solid: Downwards wave

Dashed: Upwards wave

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Traveltime functions

Slowness surface in acoustic VTI



Traveltime in acoustic VTI

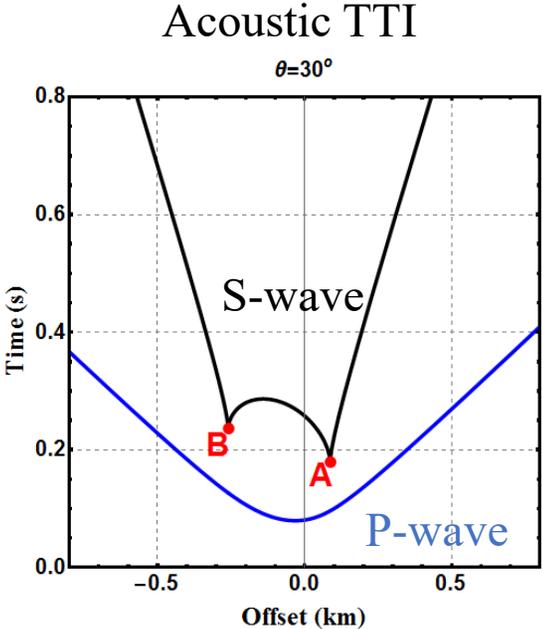
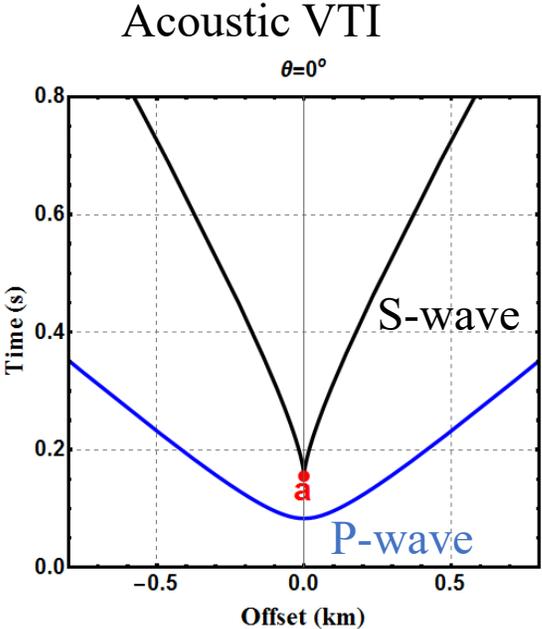


*Mapping (Stovas and
Alkhalifah, 2013)*

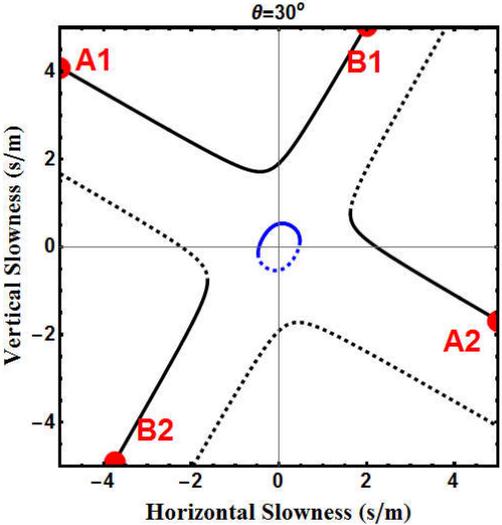
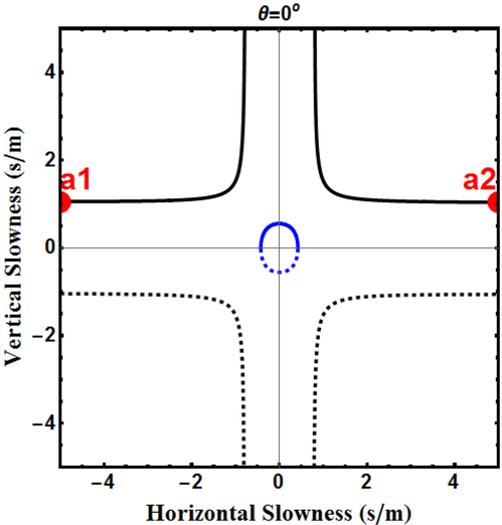
Traveltime in acoustic TTI

Traveltime functions

traveltime



slowness surface



Outline

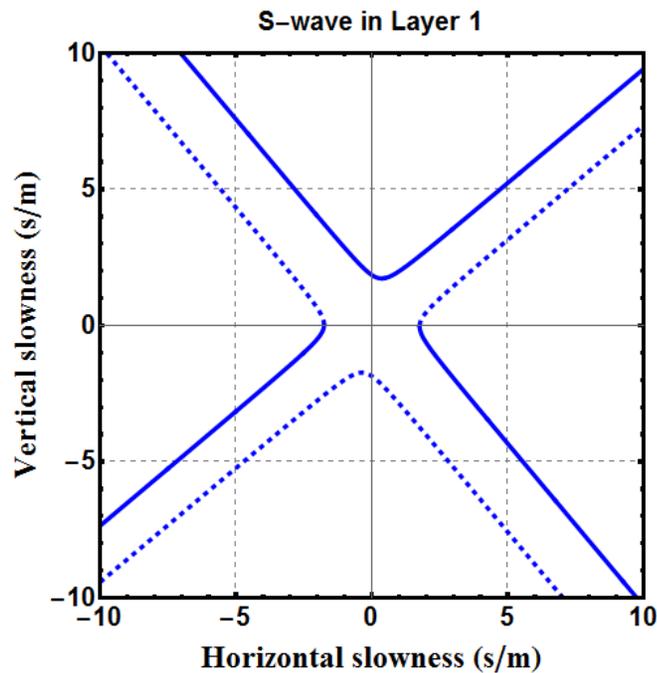
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S-wave in multi-layered acoustic TTI media

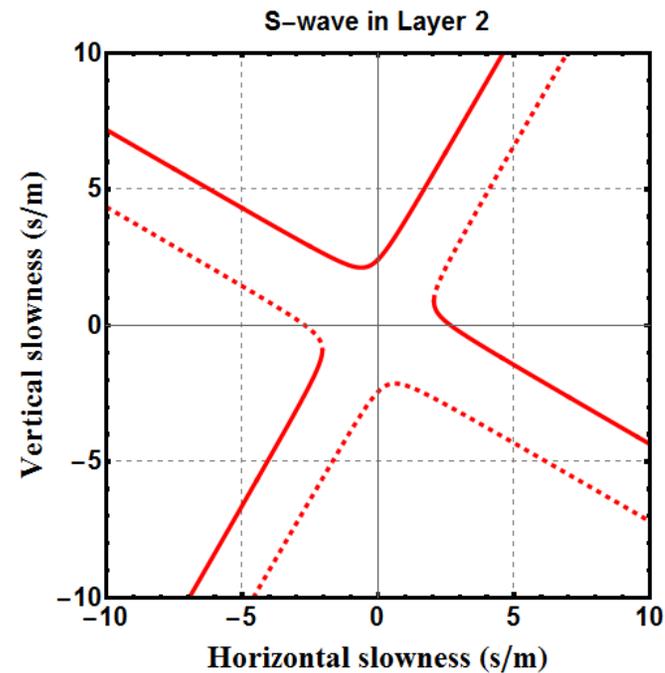
The effective slowness surface in multi-layered media is defined as:

$$q_n(p_n)_{eff} = \frac{\sum_i q_{n,i}(p_n)z_i}{\sum_i z_i}$$

Two-layered acoustic TTI model:

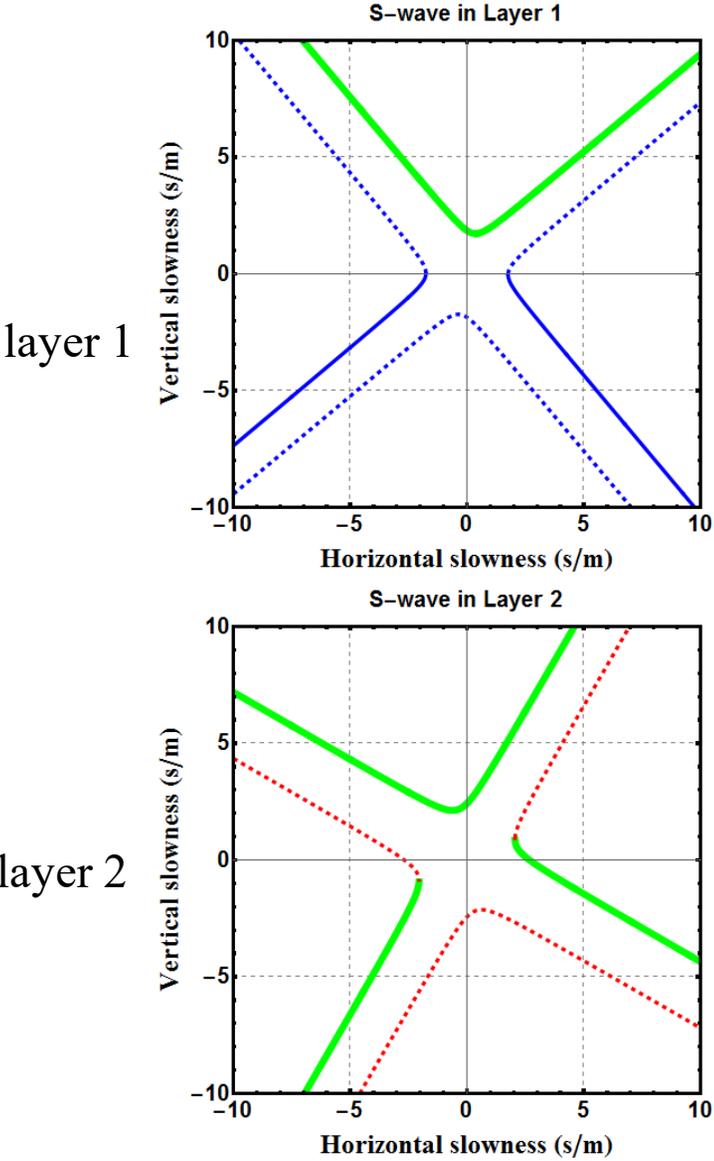


Blue: layer 1

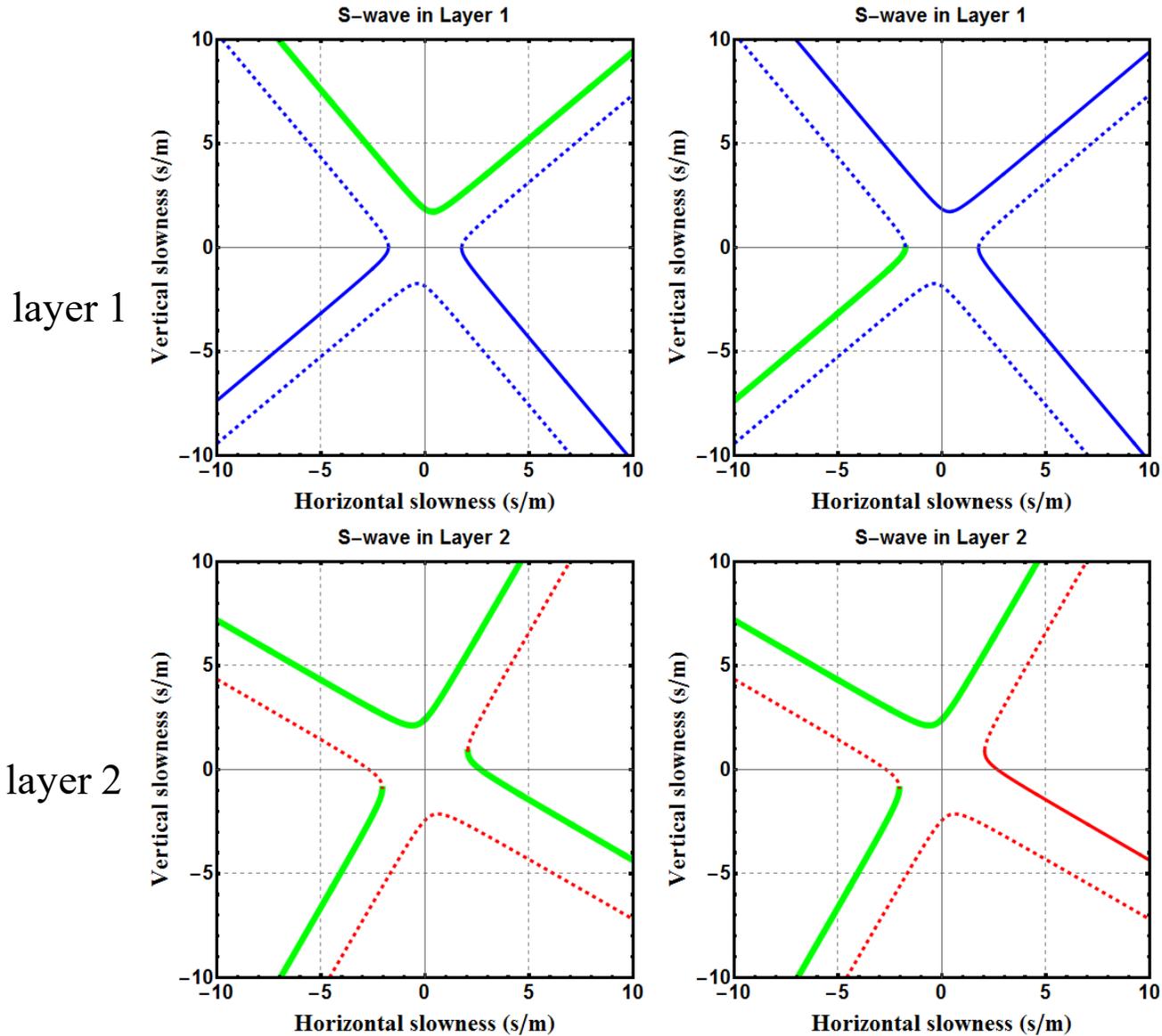


Red: layer 2

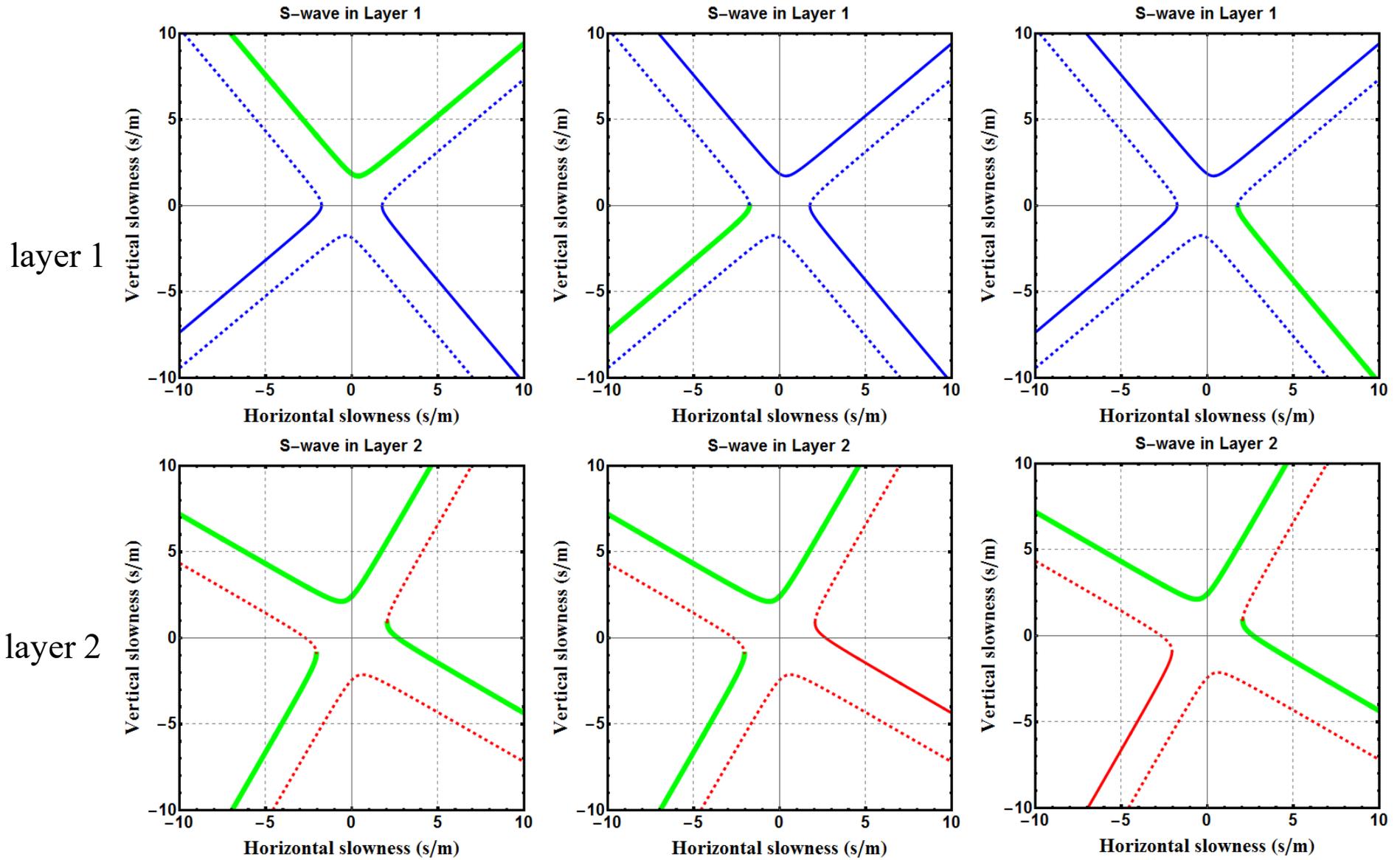
S-wave in multi-layered acoustic TTI media



S-wave in multi-layered acoustic TTI media

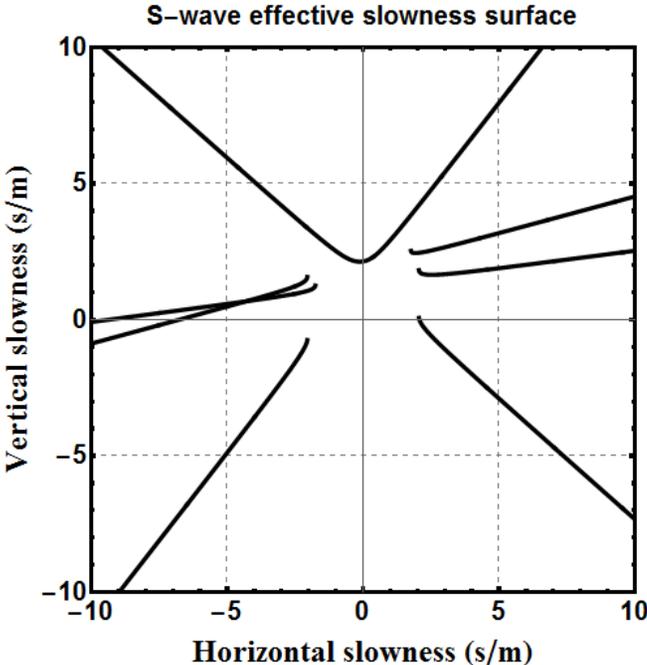


S-wave in multi-layered acoustic TTI media

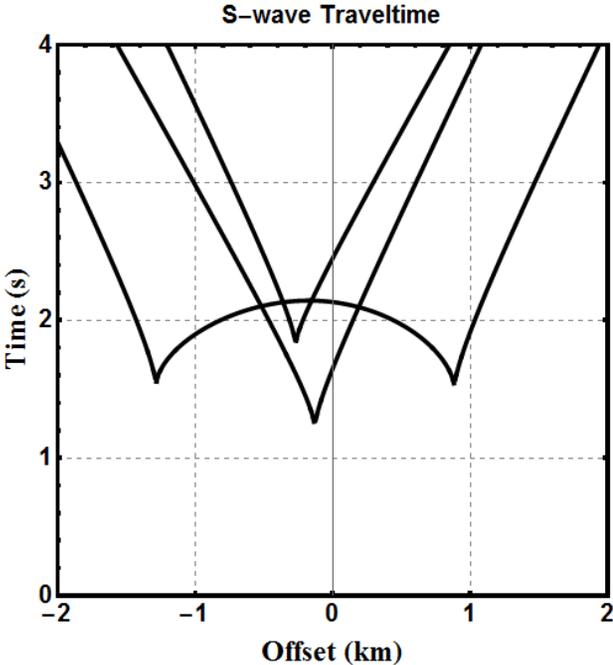


S-wave in multi-layered acoustic TTI media

Effective slowness surface



Traveltime



S-wave in multi-layered acoustic TTI media

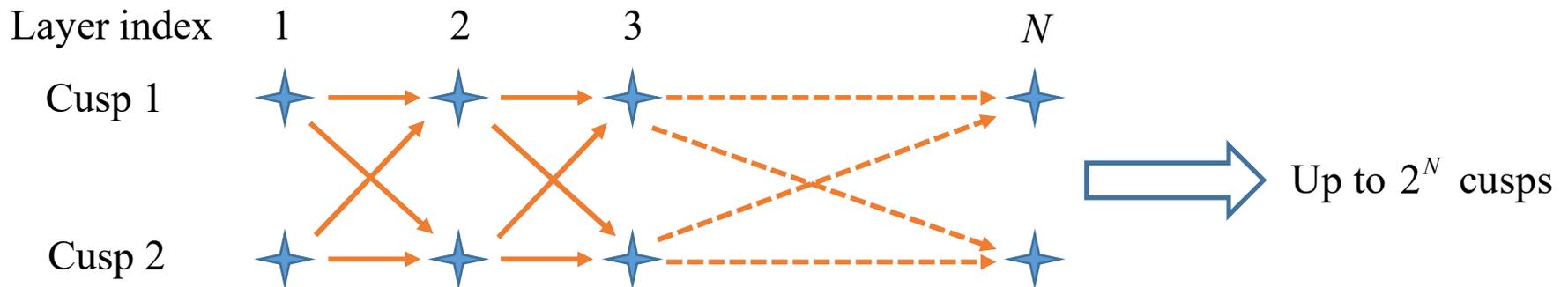
For a model composed of N acoustic TTI layers and M acoustic VTI layers ($M > 0$), the downward (or upward) S-wave has:

Maximum number of effective slowness surface branches : 2^{N+1}

Maximum values of the travelttime-offset functions: 2^N

Maximum number of cusps: 2^N

The cusp points offset and travelttime can be obtained by accumulating the counterparts for either cusp in every layer



Outline

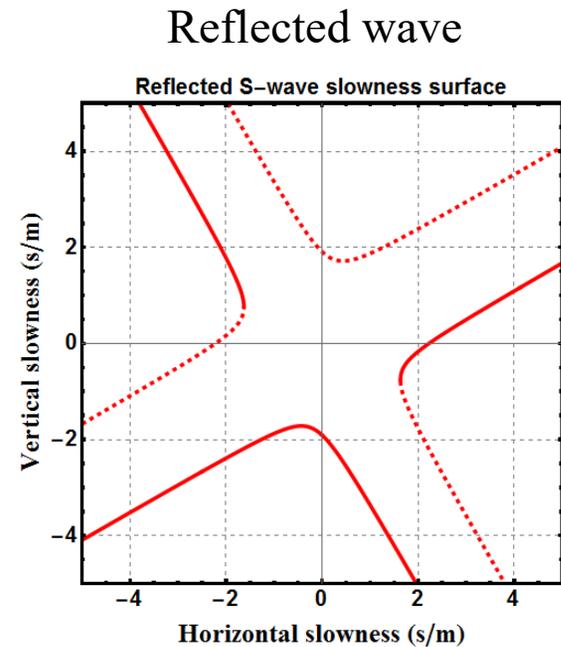
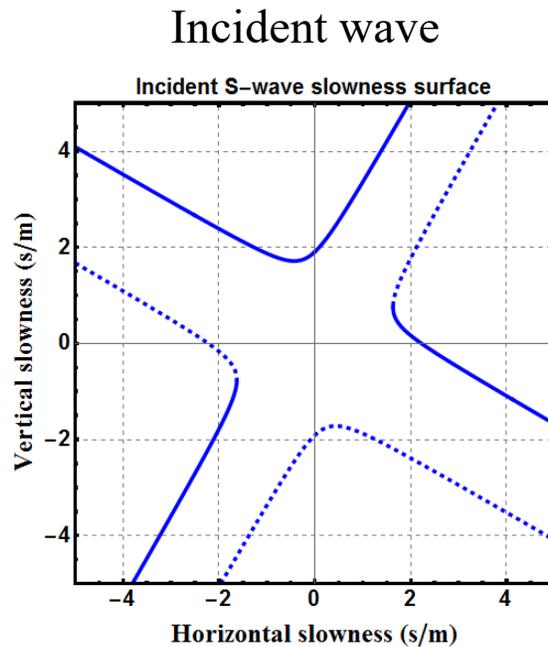
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Reflected waves

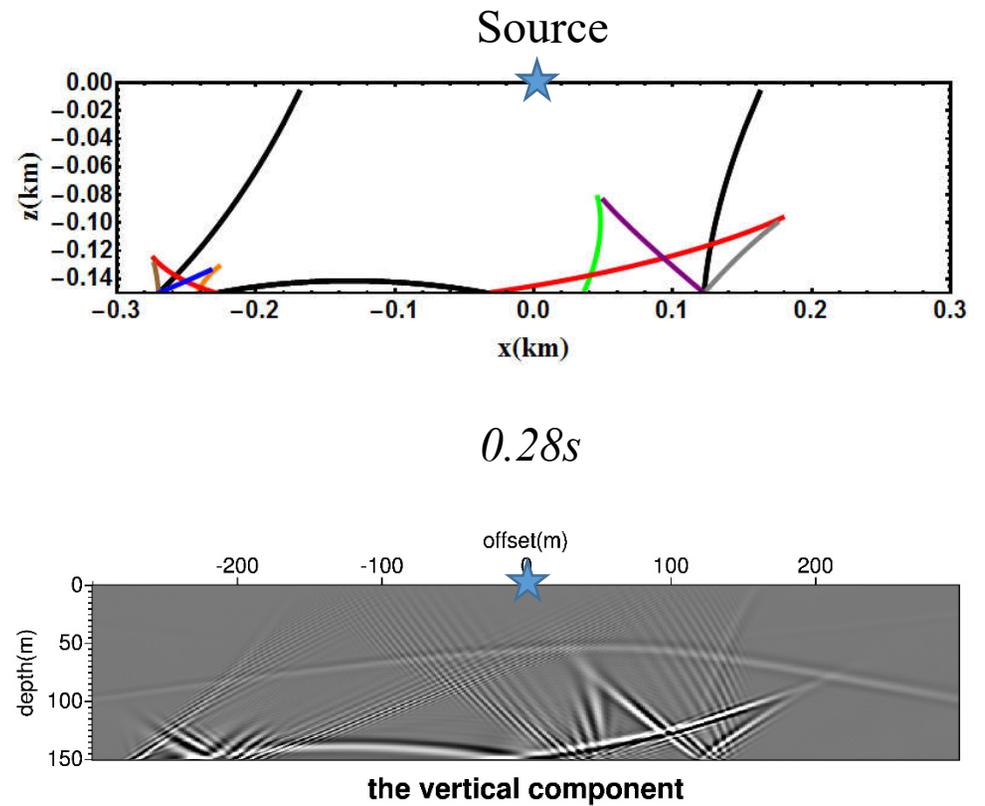
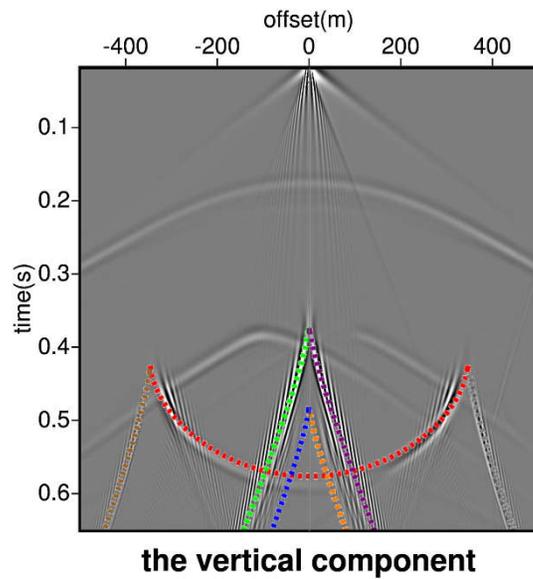
$$\left\{ \begin{array}{ll} \text{In VTI media} & q_{\text{Inc}}(p) = q_{\text{Ref}}(p) \\ \text{In TTI media} & q_{\text{Inc}}(p_n, \theta) \neq q_{\text{Ref}}(p_n, \theta) \end{array} \right.$$

The two-way S-wave in acoustic TTI media is given by: $q_n^{SS}(p_n)_{\text{eff}} = \frac{q_{\text{Inc}}(p_n, \theta) + q_{\text{Ref}}(p_n, \theta)}{2}$

A homogeneous acoustic TTI model



Reflected waves



Converted waves

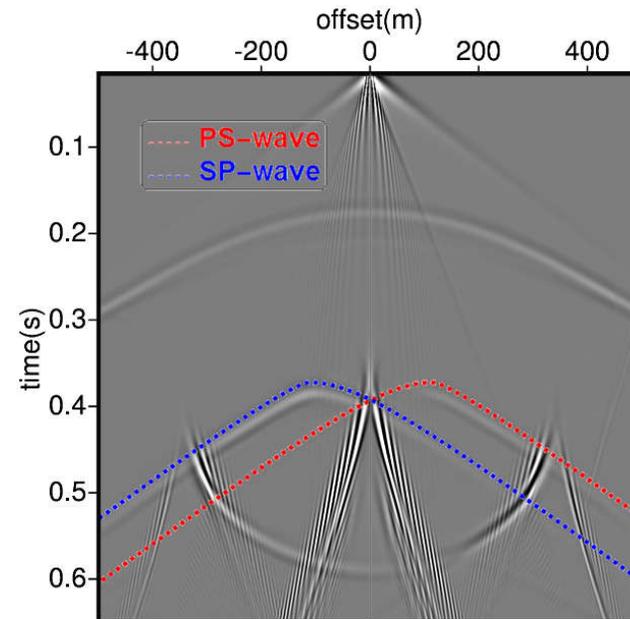
In acoustic VTI media: No converted waves

In acoustic TTI media: $\begin{cases} q_{n,Down}^P(\theta) \neq q_{n,Up}^P(\theta) \\ q_{n,Down}^S(\theta) \neq q_{n,Up}^S(\theta) \end{cases} \Rightarrow \bar{q}_n^{PS}(\theta) \neq \bar{q}_n^{SP}(\theta)$

The converted waves slowness surface in acoustic TTI:

$$\bar{q}_n^{PS}(\theta) = \frac{q_{n,Down}^P(\theta) + q_{n,Up}^S(\theta)}{2}$$

$$\bar{q}_n^{SP}(\theta) = \frac{q_{n,Down}^S(\theta) + q_{n,Up}^P(\theta)}{2}$$



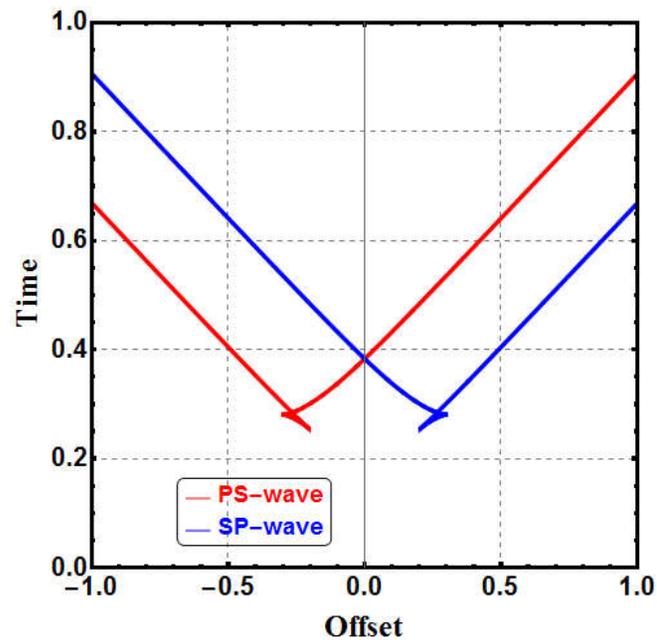
the vertical component

Converted waves

S-wave: Triplications

P-wave: No Triplications

Converted waves: May have triplications



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Conclusion

- Mapping S-wave slowness surface and travelttime from acoustic VTI to acoustic TTI media.
- S-wave (downwards or upwards) slowness surface in homogeneous acoustic TTI media has three branches.
- S-wave moveout function has two cusp points in homogeneous acoustic TTI media. The cusps number can be up to 2^N in N acoustic TTI layers.
- The two-way S-wave travelttime function is multi-valued.
- The converted waves moveout function may have triplications.

Thanks for the financial support by Rose project



Thanks for your attention