

# Applicability of AVO inversion to long-offset data from curved interfaces

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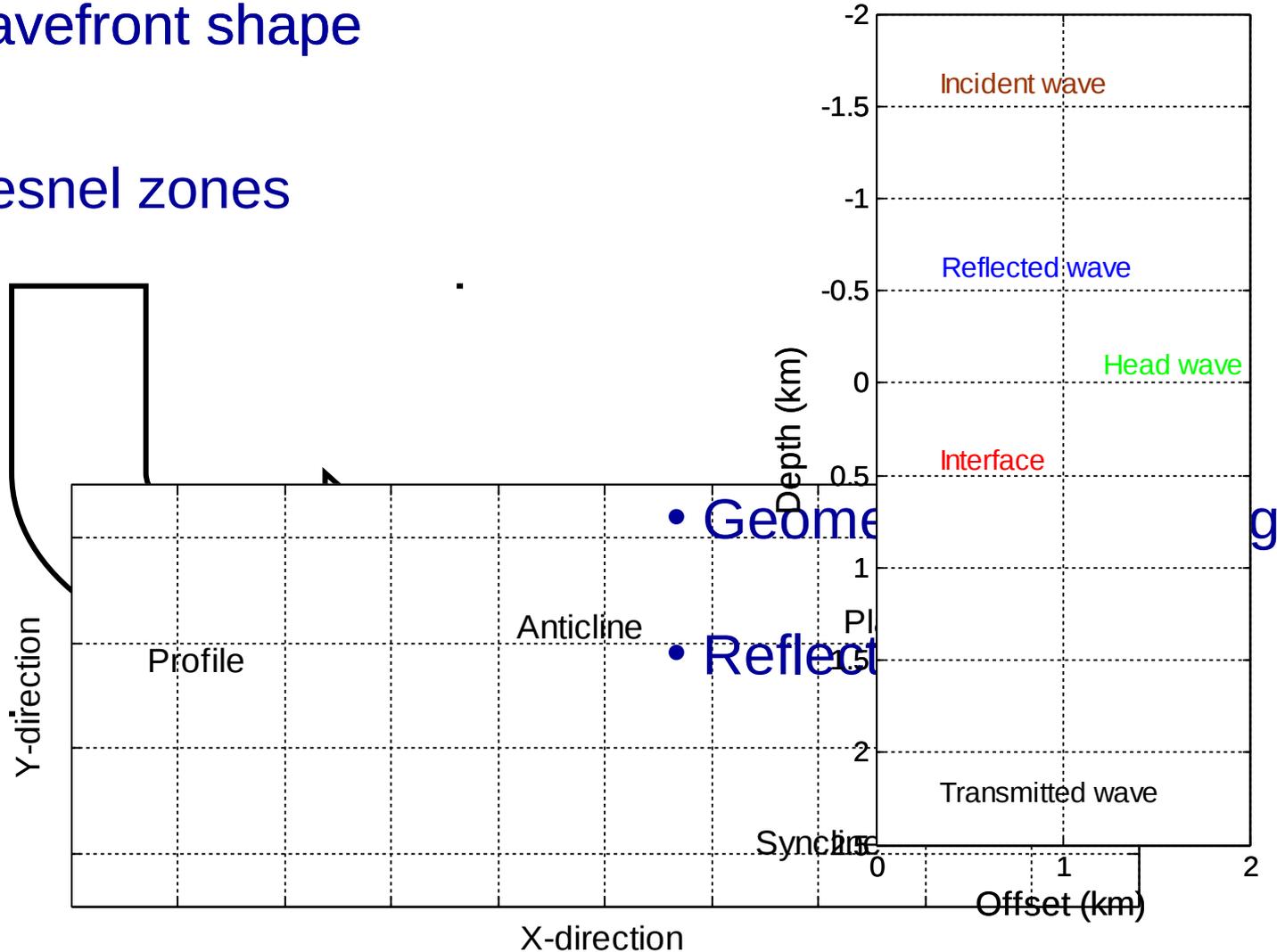
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# Plane vs. curved interface

- Wavefront shape
- Fresnel zones



# Outline

- How to deal with curvature
  - Geometrical spreading
  - Reflected wavefield
- Synthetic modelling
- Results
  - Extracted and theoretical AVO
  - Inversion
- Conclusions



# How to account for curvature?

- Geometrical spreading (V. Červený et al., 1974)

$$L = V \left[ \left( R_s + R_{s|x} + 2R_s R_{s|x} D_{11} / \cos \theta \right) \left( R_s + R_{s|x} + 2R_s R_{s|x} D_{22} \cos \theta \right) \right]^{\frac{1}{2}}$$

$R_s$	- source - reflection point distance
$R_{s x}$	- reflection point - receiver distance
$\theta$	- incidence angle
$D_{11}, D_{22}$	- main curvatures
$V$	- velocity

- Effective reflection coefficient (M. Ayzenberg et al., 2007)

# Effective reflection coefficient (ERC)

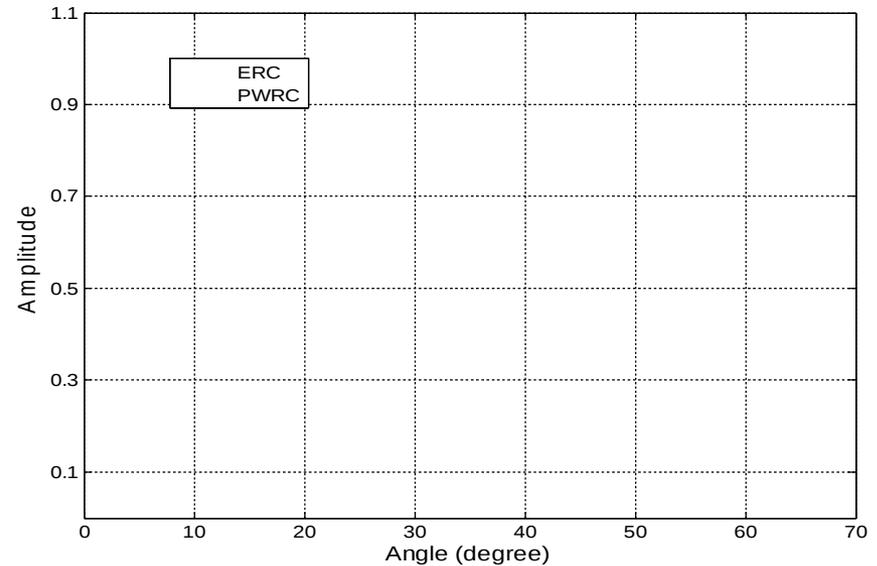
Incident wave

Plane-wave decomposition

Multiplication with  
plane-wave reflection  
coefficient (PWRC)

Summation

Division by incident wave



$$\chi(x) = \chi \left[ \theta; \frac{\omega R^*}{V} \right]$$

$\theta$  - incidence angle

$\omega = 2\pi f$  - frequency

$R^*$  - apparent wavefront radius

$V$  - velocity

# $R^*$ for curved interface

Apparent wavefront radius at interface  
(Ayzenberg et al., 2007):

$$R^*(s) = \frac{R_s}{1 - \frac{2 \cos \theta}{1 + \cos^2 \theta} [D_{11} + D_{22}] R_s}$$

$R_s$	- source - reflection point distance
$\theta$	- incidence angle
$D_{11}, D_{22}$	- main curvatures of interface

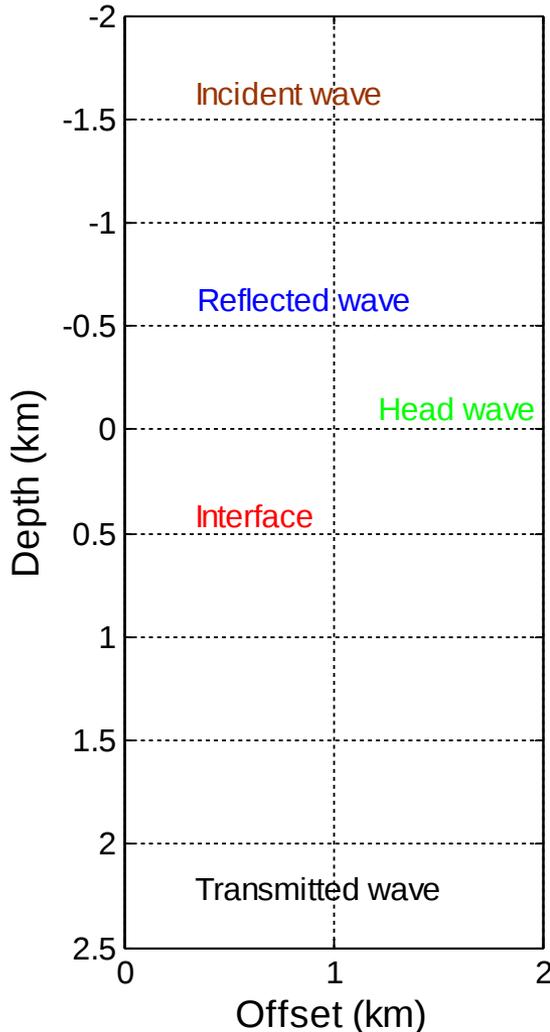
Apparent wavefront radius at receiver:

$$R^*(x) = \frac{1 + \cos^2 \theta}{\cos^2 \theta [K_{11}^*(x) - \delta K_{11}(x)] + K_{22}^*(x)}$$

$K_{11}^*, K_{22}^*$	- apparent main curvatures of reflected wavefront
$\delta K_{11}$	- head wavefront curvature

$$K_{11}^*, K_{22}^* = f(R_s, R_{s|x}, \theta, D_{11}, D_{22})$$

$$\delta K_{11} = f(R_{s|x}, \theta, D_{11})$$



# Modelling

$$Z = 0.7 - 0.2 \exp(-C x^2 - D y^2)$$

## Concentric structure

$$C = D = 1 \text{ km}^{-2}$$

## Linear structure

$$C = 1; \quad D = 0 \text{ km}^{-2}$$

Crossline

$$V_{p_1} = 2 \text{ km/s}$$

Inline

$$V_{s_1} = 1.1 \text{ km/s}$$

$$\rho_1 = 1.8 \text{ kg/m}^3$$

$$V_{p_2} = 2.8 \text{ km/s}$$

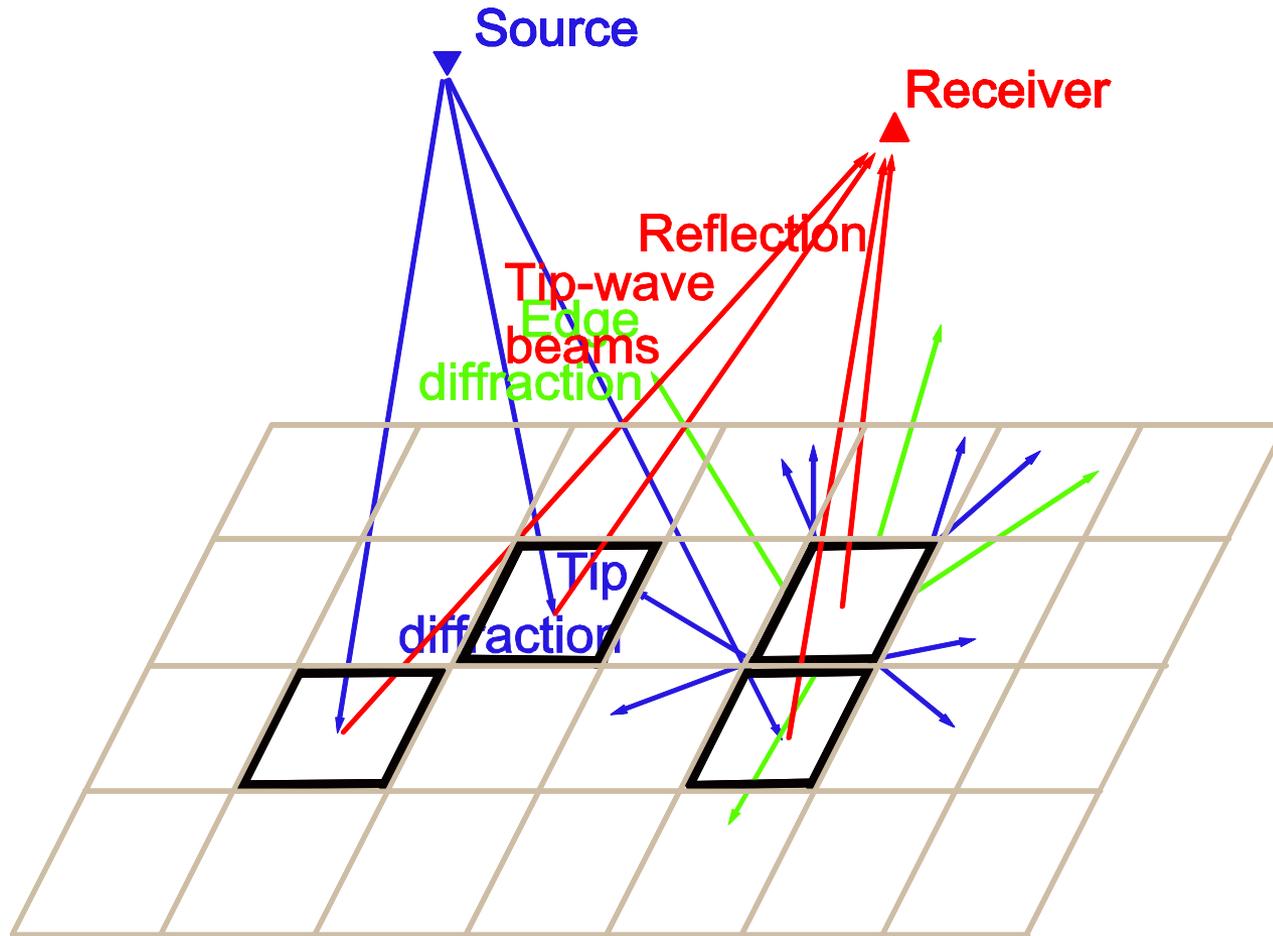
$$V_{s_2} = 1.6 \text{ km/s}$$

$$\rho_2 = 2.1 \text{ kg/m}^3$$

$$D_{11} = D_{22} = 0.4 \text{ km}^{-1}$$

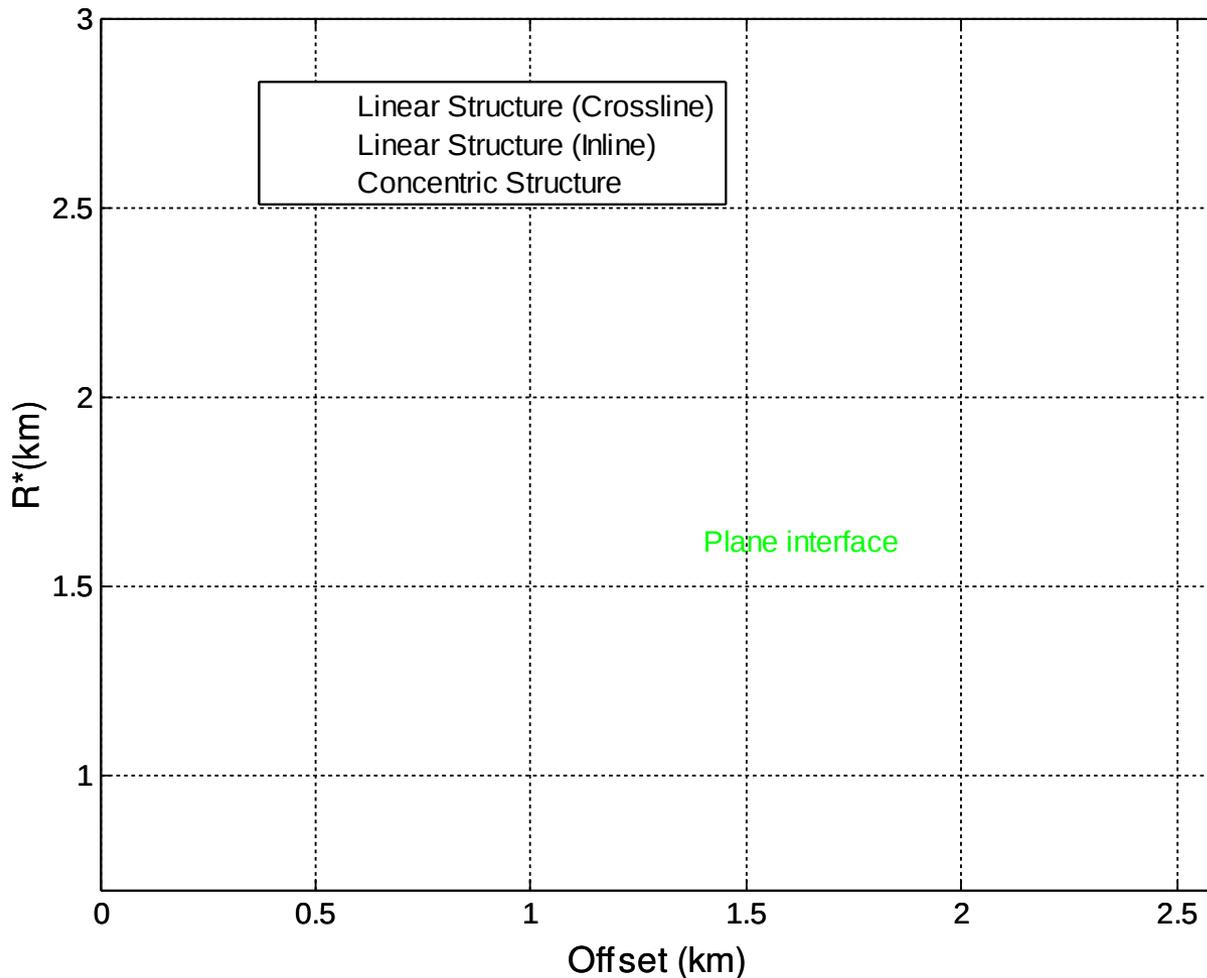
$$D_{11} = 0.4; \quad D_{22} = 0 \text{ km}^{-1}$$

# Tip-wave superposition method (TWSM)



Valid for seismic frequencies

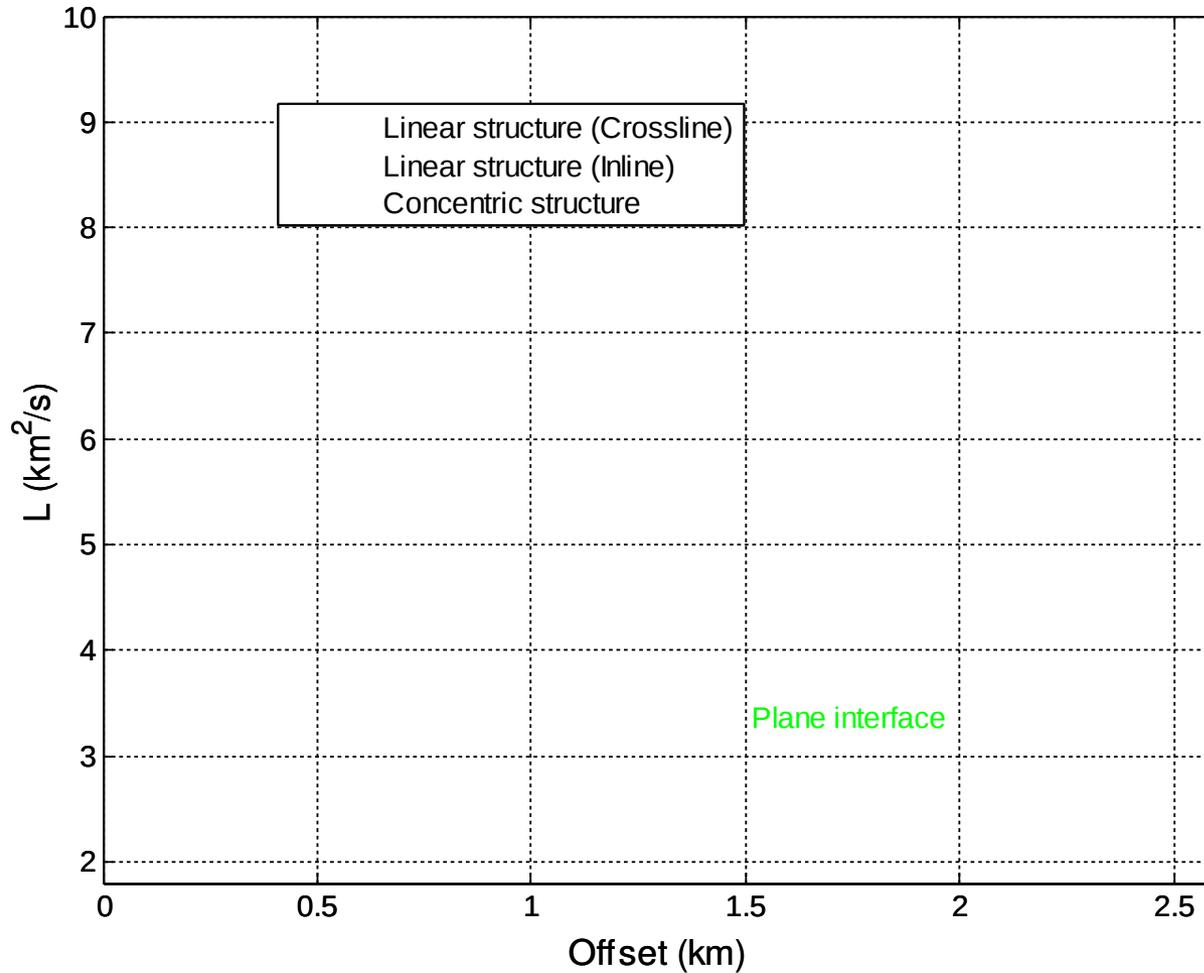
# Apparent wavefront radii



Largest apparent radius is in Crossline direction

Smallest apparent radius is in Inline direction

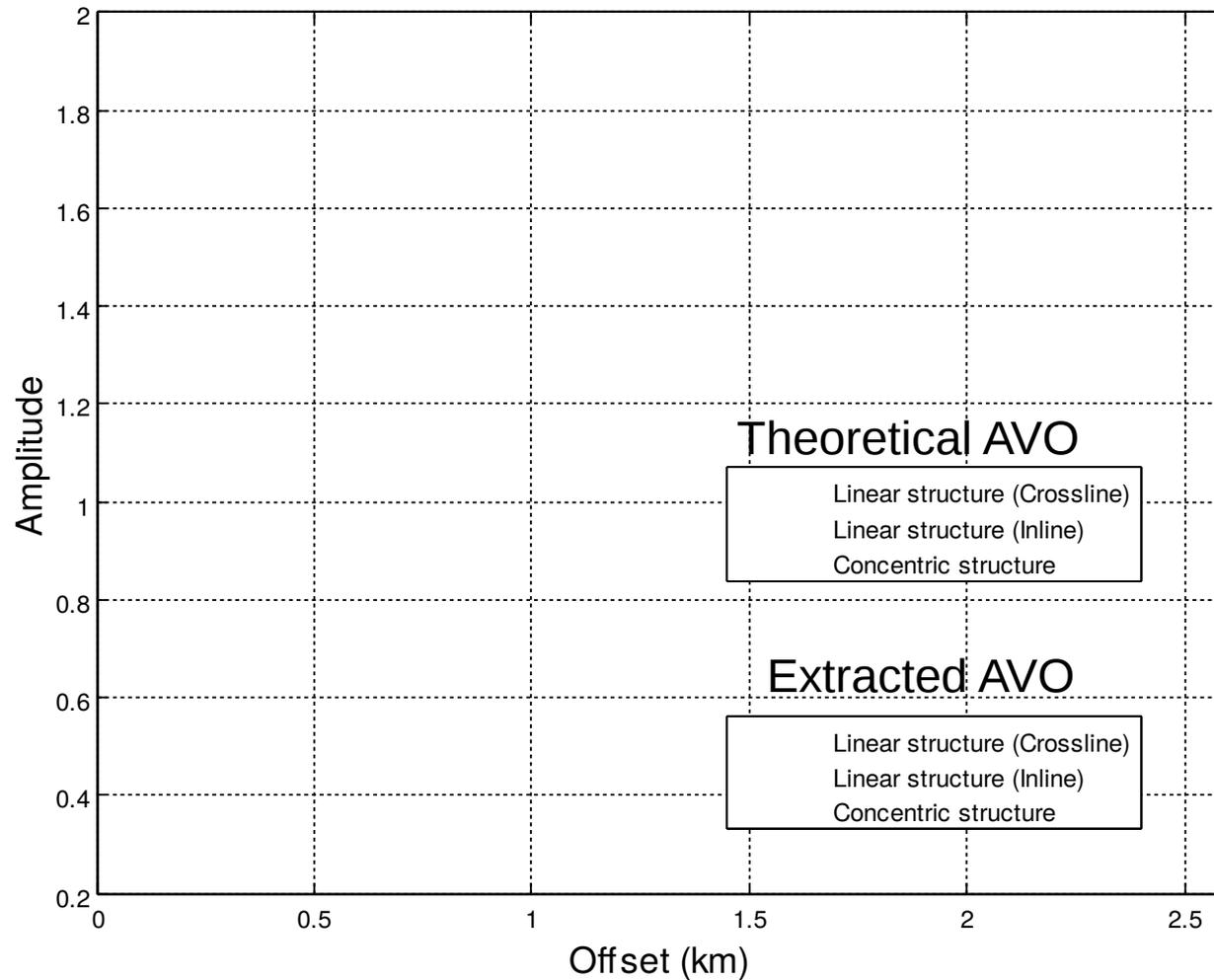
# Geometrical spreading



Largest geometrical spreading is for Concentric Structure

Smallest geometrical spreading is in Inline direction

# Extracted vs. theoretical AVO

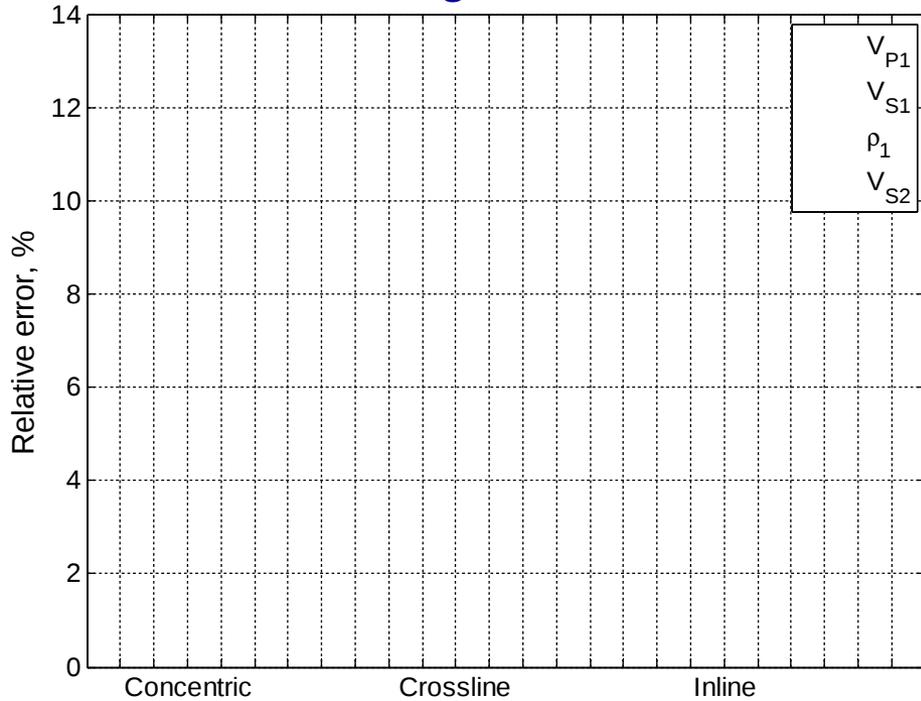


Captures main behavior of extracted AVO

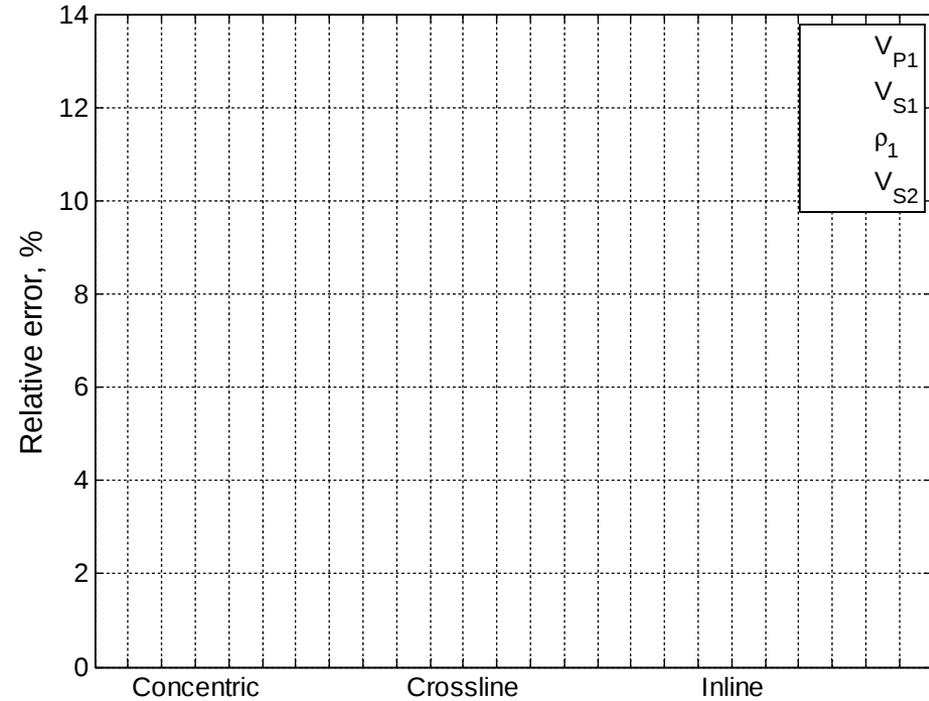
Does not include all effects we observe

# Inversion results

Interface curvature  
neglected



Interface curvature  
included



Inversion is better when curvature is included

# Conclusions

- Interface curvature strongly affects both the geometrical spreading and the reflection coefficient
- Theoretical AVO obtained with our method captures the main behaviour of the extracted AVO but are not that complete
- Inversion results are better when curvature is accounted for



# Acknowledgments

- We would like to acknowledge Statoil for financial support
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