

Natural Gas Petroleum Engineering ↔ "FLOW"

TASK (DRY)

① GAS RATE EQ Well q_g ↔ Δp Reservoir → Pipeline

@
STC
1 atm 60°F

MMscf/D

Mscf/D
 Sm^3/d

SPE:
scf/D
standard m^3/d



(a) Reservoir Δp_R — q_g

Given Today's p_e

(b) "Tubing" Δp_T — q_g

Calc q_{gw}

q_{gr} gas rate in the reservoir @ p_r, T_r

Mike J. Fetkovich
Mscf/D

MULTIPOINT TESTING OF GAS WELLS

by

M. J. Fetkovich

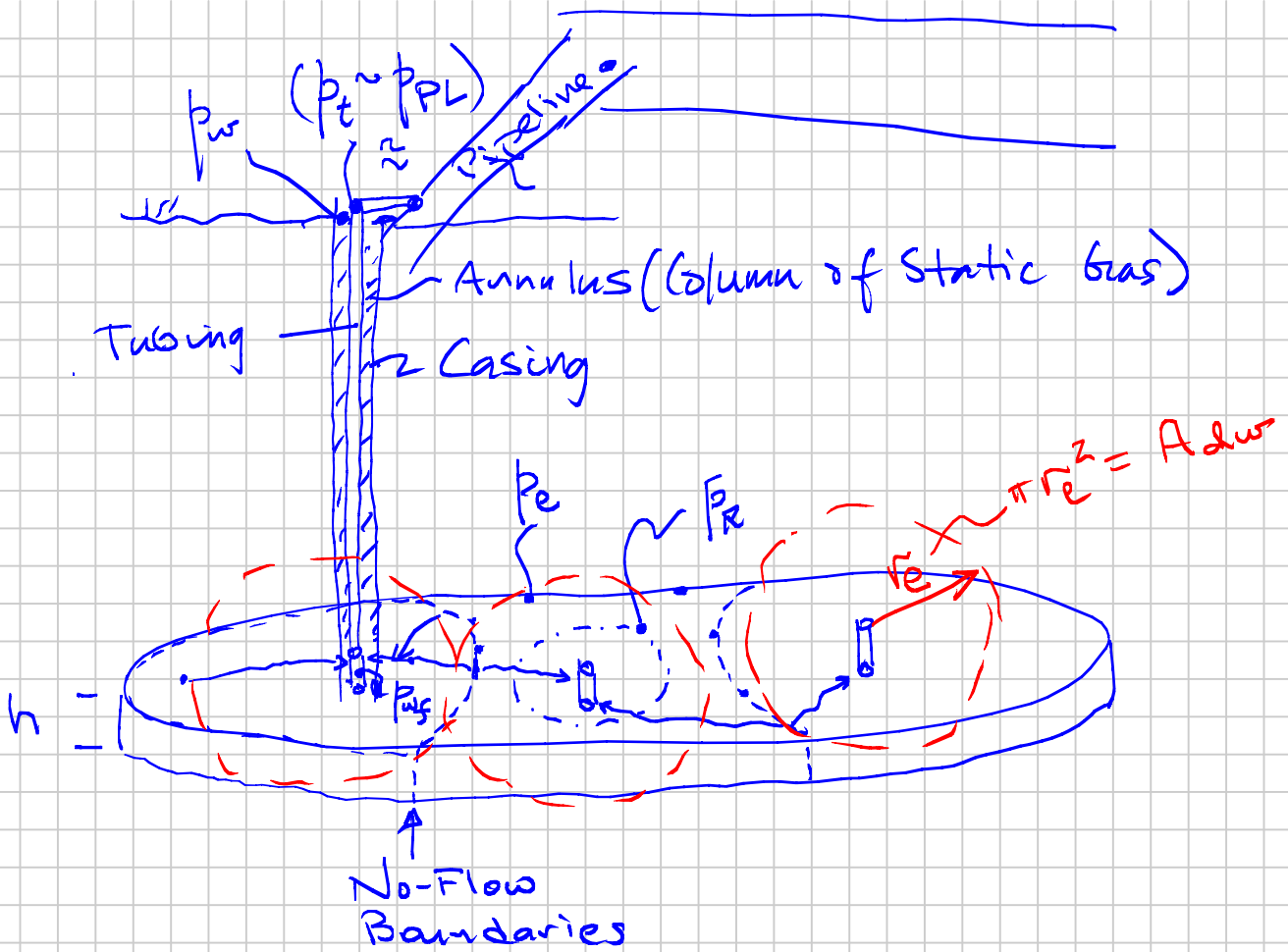
Phillips Petroleum Company

List our pressures

- ③ p_{wf} = wellbore flowing pressure
- ② \bar{p}_R = volumetric average reservoir pressure

$$= \int_{V_{dw}} p(V) dV$$
- ① p_e = pressure at the external outer boundary
- p_t = tubing flowing pressure
- p_w = annulus pressure flowing @ surface

$p_{wf} \rightarrow p_t$: Tubing (Friction + Gravity) | $p_{wf} \rightarrow p_w$ (Annulus Gravity)



Homogeneous (ϕ, S_w, k) Reservoir

$$V_{dw} \propto \frac{q_{fw}}{\sum_{u=1}^3 q_{fu}} = \frac{q_{fw}}{q_F} = \frac{V_{dw}}{V_{dF}}$$

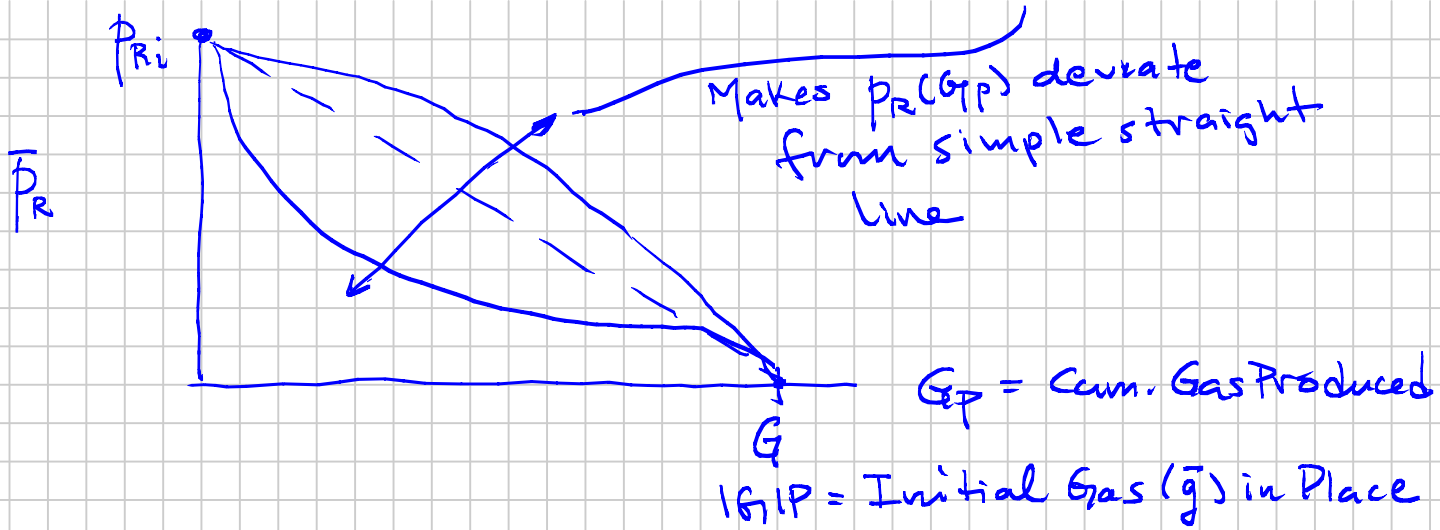
#1 Job of a Petroleum Engineer is
Forecast $q(t)$ $q \neq 0 \Rightarrow$ Revenues, NPV, Company Value

TASK

②
$$\underline{p_R(t)} = f \left(\int_0^t q_{GF} dt \right) =$$

$$\underline{G_p} = \text{cumulative gas production}$$

Gas Material Balance: $p_R(G_p, \dots)$



Society of Petroleum Engineers

SPE 22921

APPLICATION OF A GENERAL MATERIAL BALANCE FOR HIGH-PRESSURE GAS RESERVOIRS

by M. J. Fetkovich, D. E. Reese, and C. H. Whitson, Phillips Petroleum Co.

TASK ③ PRODUCTION DECLINE PERFORMANCE
 - OF individual wells and/or
 - Entire Field

"DECLINE CURVE ANALYSIS" (DCA)

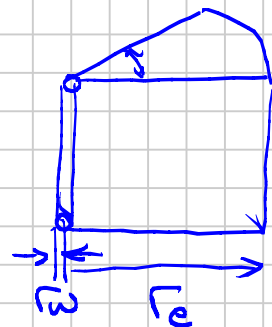
Father of DCA : M J Fetkovich

Reservoir Gas Rate Equation

$$q_g \leftrightarrow p_{wf} \cdot p_R (p_e)$$

$$q_g = \frac{(kh)(p_R - p_{wf})}{T_R \cdot \left[\ln \frac{r_e}{r_w} - \frac{3}{4} \right]}$$

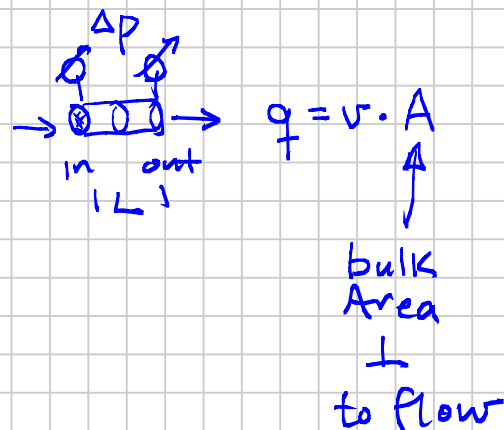
~8-10



Darcy Velocity

Darcy's Law: $v = \frac{k}{\mu} \cdot \frac{\Delta p}{L}$

↑
≠ pore velocity



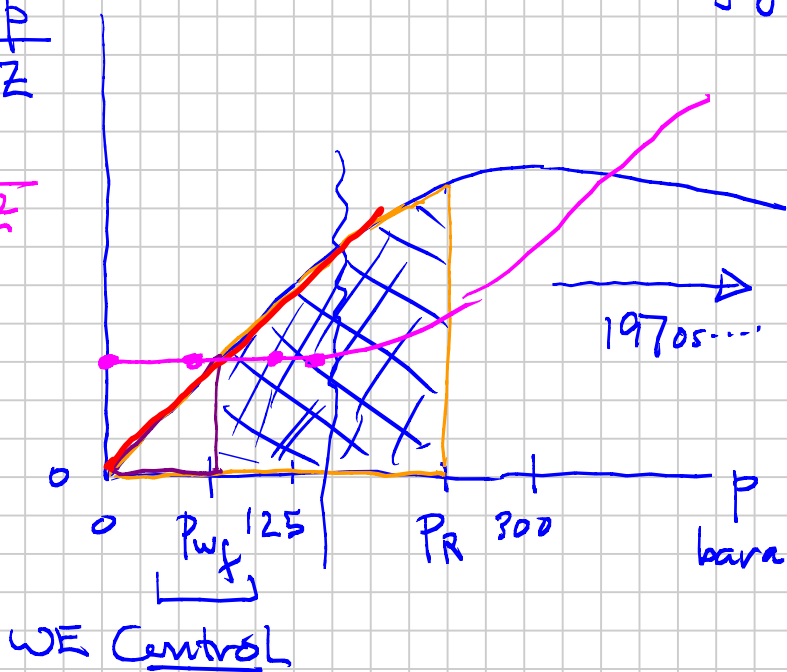
$$p_{PR} = 2 \int_0^{p_R} \frac{p'}{\mu Z} dp'$$

$\left(\frac{p}{\mu Z} \right)$

$$p_{pwf} = 2 \int_0^{p_{wf}} \frac{p}{\mu Z} dp$$

$\frac{2p}{\mu Z}$
 $\frac{1}{\mu Z}$

$p_{PR} - p_{pwf} =$ Driving Potential for Darcy



History Lesson: 1966 Al-Hussainy Ramey & Crawford

< 1960s+ $p_{Ri} \leq 150$ bara

$\frac{p}{\mu Z} = m \cdot p$ straight line

$$p_{PR} = 2 \int_0^p \frac{p}{\mu Z} dp$$

$m(p)$: OLD SPE

Low-Pressure Gas Rate Equation

$$q_g = \frac{(kh) \cdot 2 \cdot (P_R^2 - P_{wf}^2)}{\underbrace{T_R (\mu Z)^*}_{const} \left[\ln \frac{r_e}{r_w} - \frac{3}{4} \right]}$$

* At $P_R \approx P_{sc}$

$$q_g = C (P_R^2 - P_{wf}^2)$$

$$M\&F : \int \frac{1}{\mu_g B_g} dp = \underbrace{\frac{T_{sc}}{P_{sc} T_R}}_{\frac{p}{\mu Z}}$$

$$ARC : 2 \int \frac{p}{\mu Z} dp$$

$$B_g = \frac{P_{sc}}{T_{sc}} \cdot \frac{Z T_R}{p} \quad \frac{1}{B_g} = \frac{T_{sc}}{T_R P_{sc}} \frac{p}{Z}$$

Field Units:

q_g	scf/D
k	md
h	ft
p	psia
T	°R
μ	cp

$$q_g = \frac{0.703 kh (P_R^2 - P_{wf}^2)}{T_R (\mu Z)^* \left[\ln \frac{r_e}{r_w} - \frac{3}{4} \right]}$$

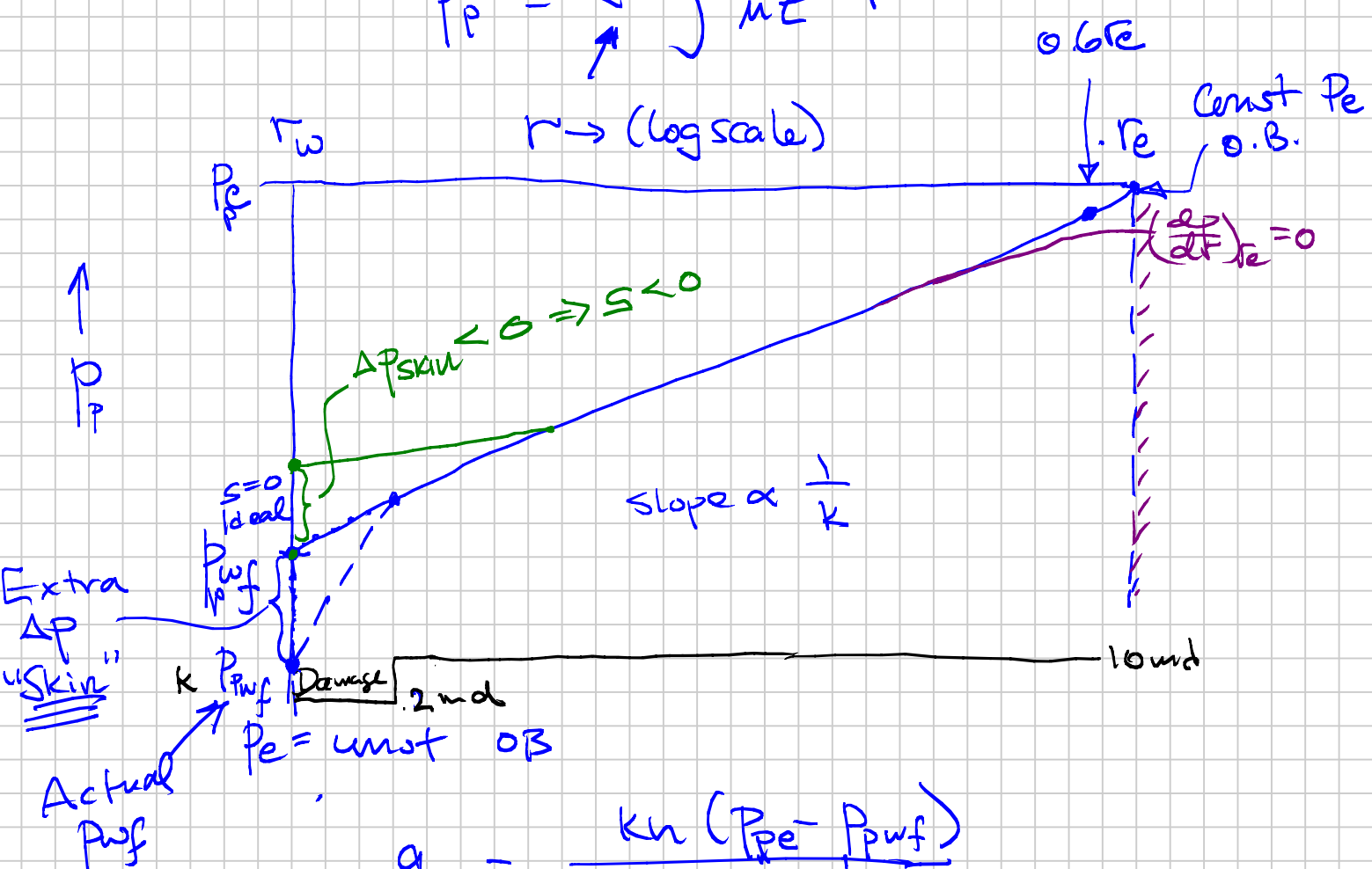
Assuming Steady State Flow : $q_{mass} = const @ \text{ all } r$

$$q_{fg} = \frac{0.703 kh (P_{PR} - P_{pwf})}{T_R \left[\ln \frac{r_e}{r_w} - \frac{3}{4} \right]}$$

No-Flow O.B.

because "P_{PR}"

$$P_p \equiv 2 \cdot \int \frac{p}{\mu z} dp$$



$$q_{fg} = \frac{kh (P_e - P_{pwf})}{T_R \left[\ln \frac{r_e}{r_w} \right]}$$

$$q_{fg} = \frac{kh (P_{PR} - P_{pwf})}{T_R \left[\ln \frac{r_e}{r_w} - 0.60 \right]}$$

Physically Δp_{skin} damage $r_d \rightarrow r_w$

Rate Equation, Δp_{skin} occurs. AT r_w

$$q_{Tg} = \frac{0.703 kh (p_{PR} - p_{wf})}{T_R \left[\underbrace{\left(\ln \frac{r_e}{r_w} - \frac{3}{4} \right)}_{\sim 8} + s \right]}$$

Dimensionless Quantity
"Skin"

(Assume Pseudopressure p_p)

$$s = \Delta p_{skin} \cdot \left(\frac{0.703 kh}{q_g T_R} \right)$$

Ideal ($s=0$)

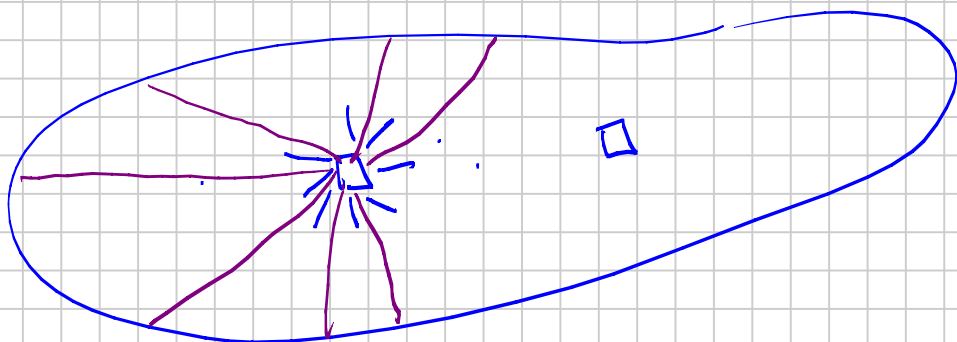
$$\Delta p_{skin} = p_{wf} - p_{wf, actual}$$

Magnitude of (Driller's) Damage Skin

$$s \sim 0 \rightarrow 5 \rightarrow 10 \rightarrow 50^+$$

Skin Effects:

- (Driller's) Damage $s > 0$
 - (Completion) Damage $s > 0$
 - Flow Geometry Damage 1-10
- \vdots
 $\sim 1-2-3$
- $\rightarrow 10-100$



- Stimulation Skin $\sim -1 \rightarrow -5$
- Stimulation Flow Geometry Skin

$$10^6 \text{ Sm}^3/\text{d} = \frac{1}{8+s} \cdot c \cdot \frac{1}{8}$$

$$2 \cdot 10^6 \text{ Sm}^3/\text{d} = c \cdot \frac{1}{8-4} = \frac{c}{4}$$

