

Water-Oil (Gas-Oil) Immiscible Displacement

- Buckley-Leverett Theory (1942)

- Muskat Comments (1950)

- Standing notes (197x) "Fractional Flow"

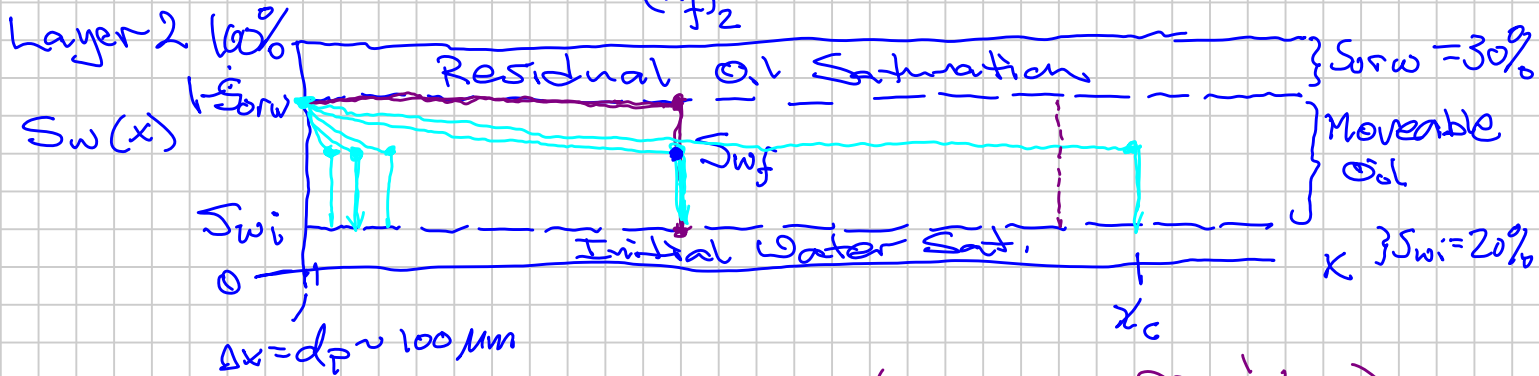
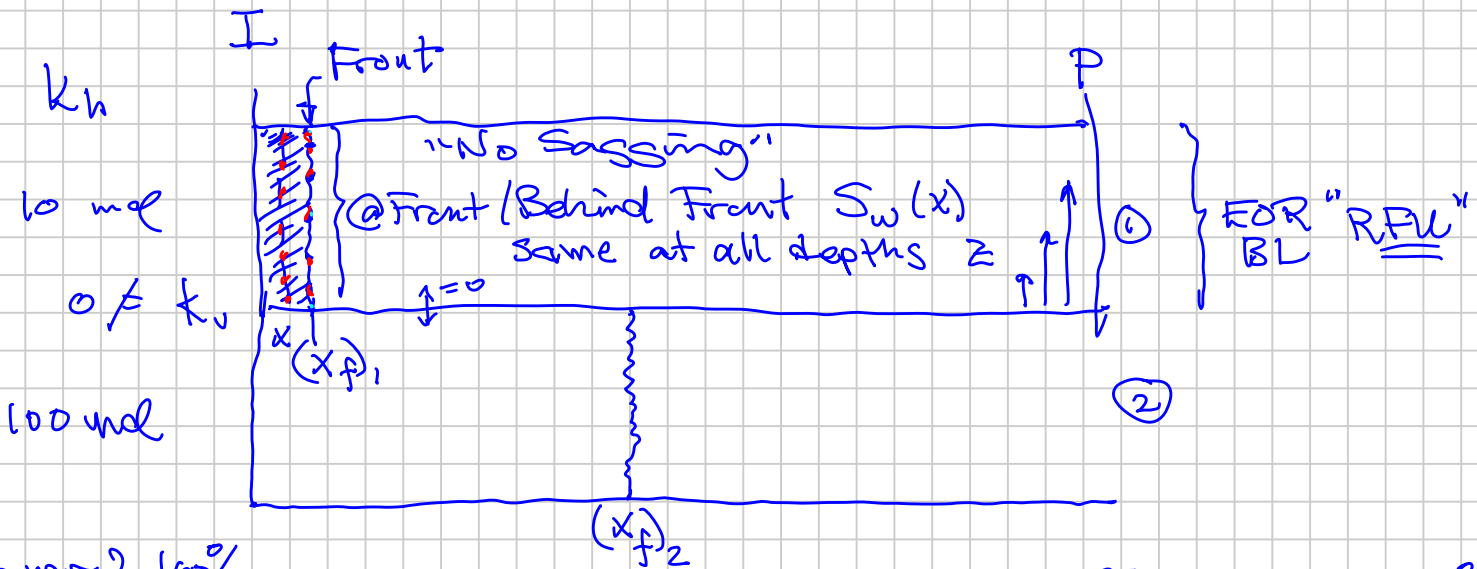
- Mathematical verification (?)

using 'Method of Characteristics'

- One-dimensional flow theory ($H \perp I \parallel V$)
 $0 < \alpha \leq 90^\circ$

$$q, k, \phi, h, k_r, \Delta p, \dots \rightarrow 1D \text{ or } 2D$$

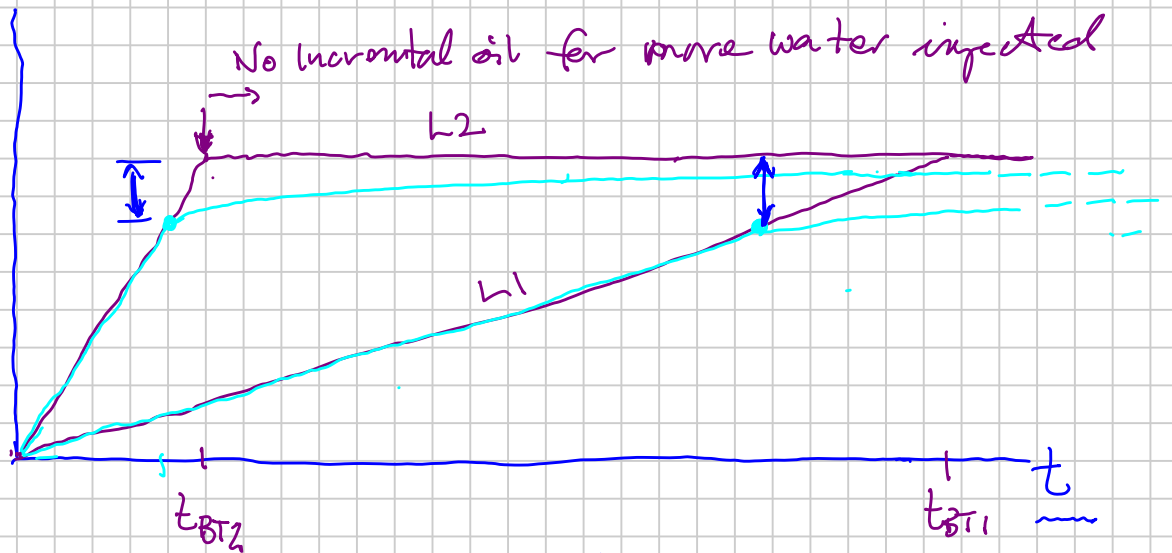
- Alternative: "Leaky Piston" (Muskat)



- Leaky Piston (optimistic, $R_{F0} \neq t_{BT}$)

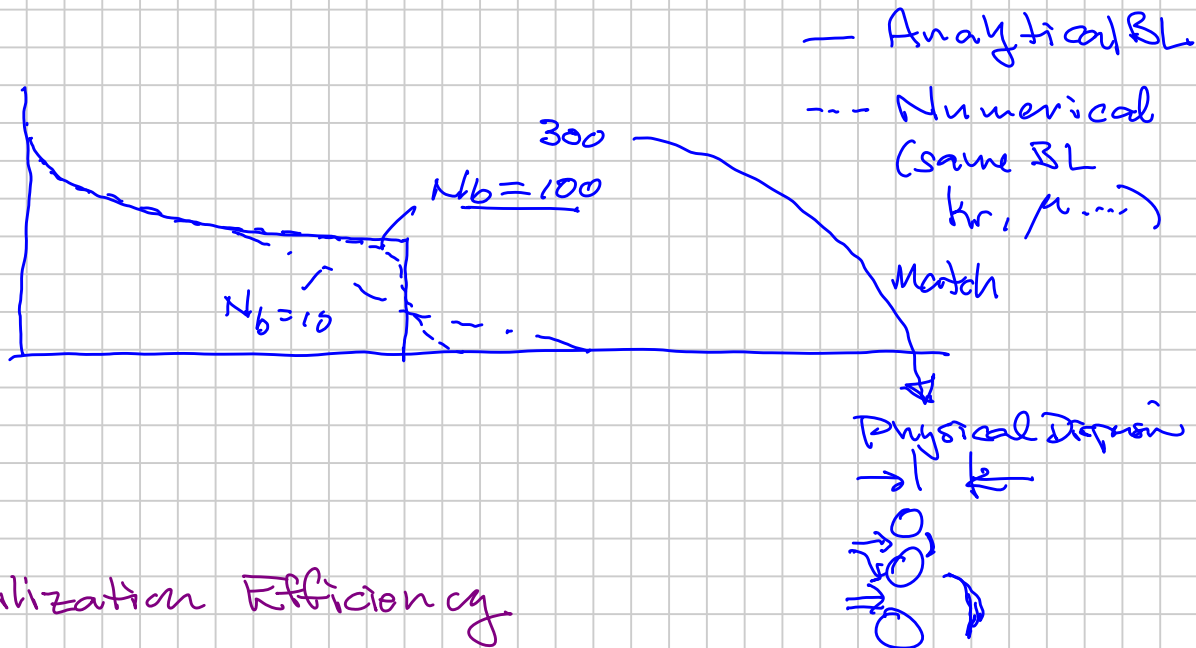
- BL: $S_w \rightarrow 1 - S_{orw}$ requires "infinite" amount of water passing the pore

N_p



$[q_i(t)]_e$ for BL vs LP

Assuming the same water rate injected into $L1 \neq L2$ prior to BT



Injectant Utilization Efficiency

$$\frac{\$80/\text{bbl} \Delta q_{fo}}{\$10/\text{bbl} \Delta q_{fio}} = \underbrace{\text{constant} \sim 1}_{\text{before BT}} \rightarrow 0.x \rightarrow 0$$

(max) BL Leaky Piston
 is $\frac{\Delta FW}{\Delta FW}$ Oil Stripping After BT

Standing Fraction Flow Notes

① Fractional Flow Eqs.

② Frontal Advance Eq. (BL) $S_w(x, z)$
↓
PVI
/ "dimensionless time"

③ Average Saturation ($\bar{S}_w \Rightarrow \bar{S}_o$)
Behind Front

④ Injection Volume ($\frac{PVI}{V_{iD}}$) - Recovery $\frac{N_p}{N}$
Relationship