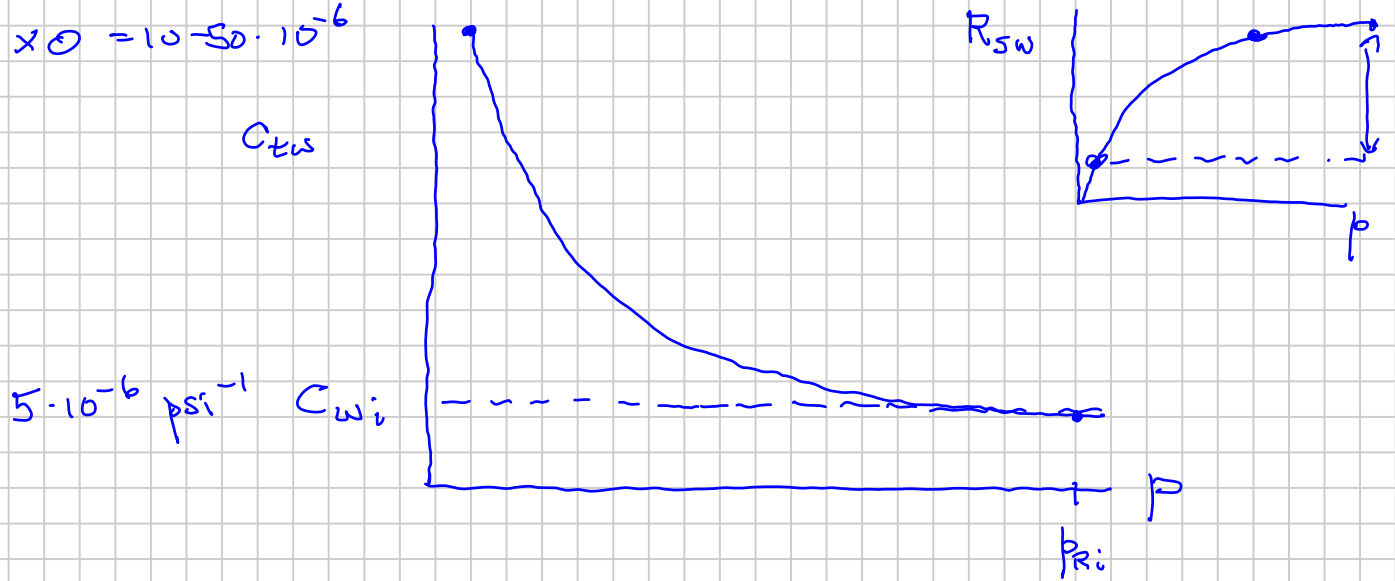


$c_{tw}(p)$: Biggest impact at lower pressures

$\times 10^{-50} \cdot 10^{-6}$



$$c = -\frac{1}{V_t} \left(\frac{dV_t}{dp} \right)_{T, m}$$

$p < p_{ri}$ split into g+w

$$V_t = V_w + V_g(p)$$

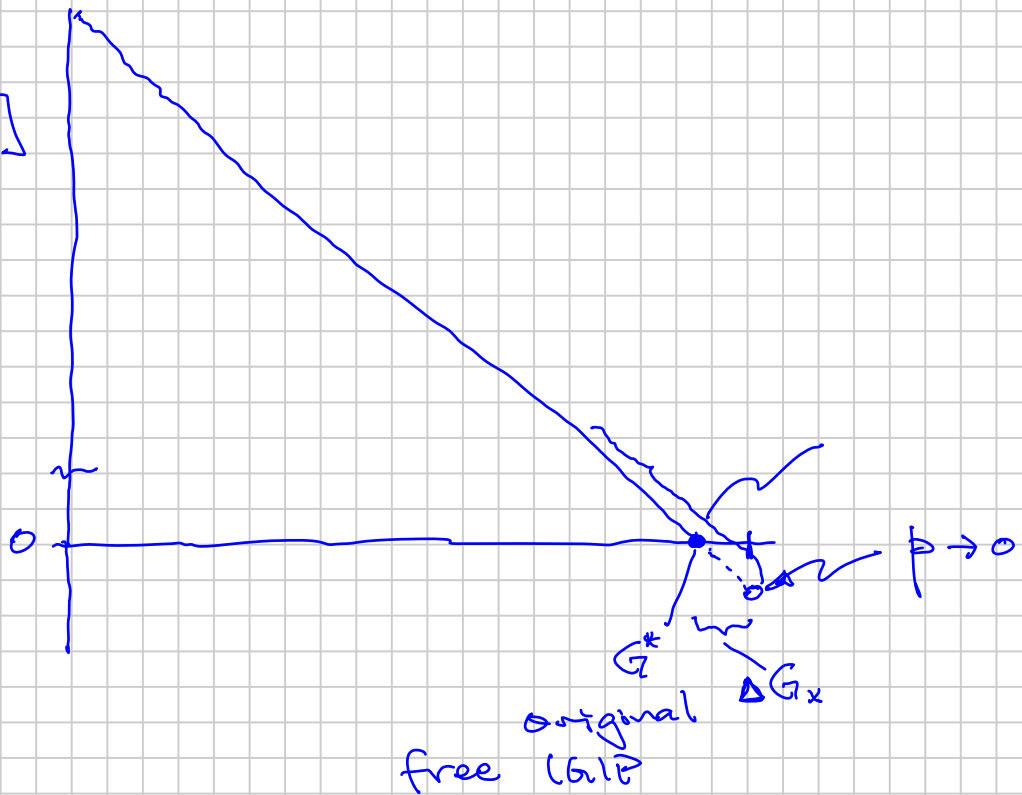
$\sim \text{const}$

$$V_{g(p)} = (R_{si} - R_s(p)) B_g(p)$$

$$\boxed{(R_{si} - R_s(p)) B_g(p)}$$

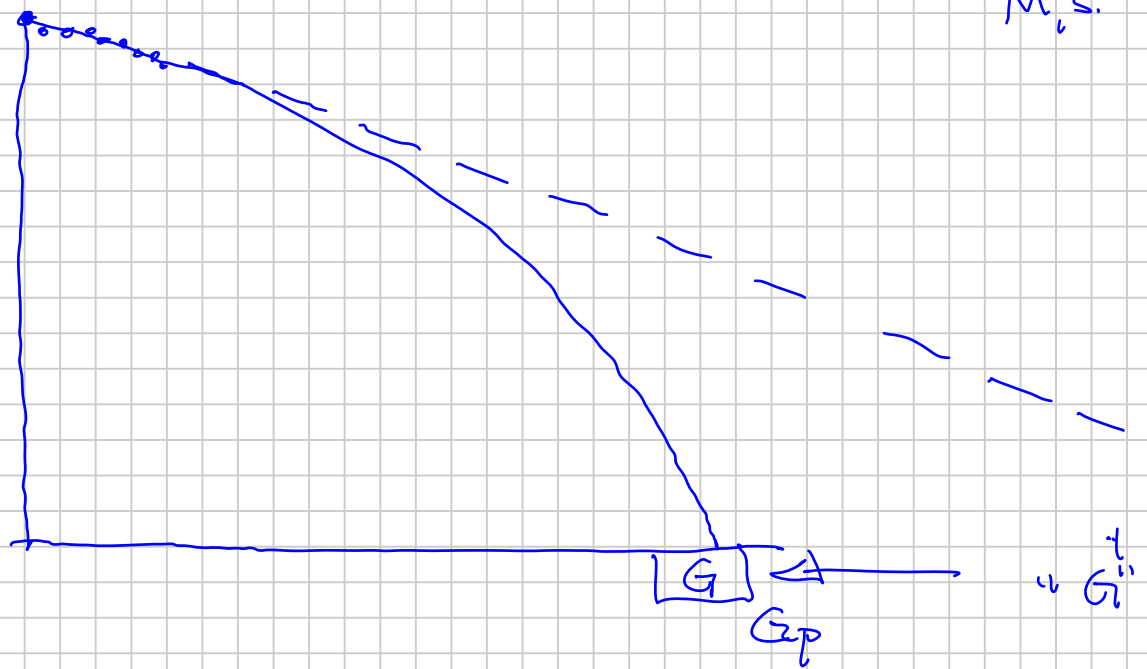
Oil M.B.

$$\frac{p}{2} [1 - c_e(p)(p_i - p)]$$



$$\begin{aligned} \text{True } G &= G^* + \Delta G_x \\ &= R_{swi} \cdot \text{IWIP} \\ &\quad \uparrow \\ &\quad M_i S. \end{aligned}$$

ΔG



"EOR"

$$v_D \quad v_P$$

$$v_D = l \cdot m/d$$

Prove:

$$t_f \neq \frac{L_f}{v_D}$$

$$t_f = \frac{L_f}{v_P}$$

$$v_P = \frac{v_D}{\phi \Delta S}$$

of the injected phase

$$S_{oc} = S_{wi} = 0.2$$

$$S_w \text{ (Behind Front) } = 1 - S_{orw} = 0.75$$

In Swept Volume 0.25

$$\Delta S_w = 0.55$$

Modeling Methods

① Mat. Bal.

② Approx. Flow Eqs

- Pseudosteady state "Rate" Eqs

Oil: IPR (Inflow Performance Relationship)

Gas: BPE ("Reservoir" Backpressure Eq.)

$$\left. \begin{matrix} q_{fg} \\ q_{fo} \\ q_{fw} \end{matrix} \right\} \left(\begin{matrix} \downarrow \\ P_R \\ \downarrow \\ P_{wf} \end{matrix} \right)$$

Steady State : doesn't change with time

Pseudo SS : (a) Something does change with time
- But very slowly

$p_R(t)$
slowly

(b) Now (at some time)
the system behaves SS

③ Numerical Reservoir Simulation (>1980-90s)

<1980
→60s

BOAST (?) COMAI (2) (4) "INTERCOMP" (Coats et al)

THERM } : NOLEN } -

>1980

ECL100

ECL300

SENSOR

VIP

NEXUS

INTERSECT

...

Review: See paper (optional) SPE Chapter 17
by Coats et al. (2009): optional reading

- Finite Difference

- Conventional IMPES (implicit / implicit) Adaptive
- Streamline (key: EOR Volumetric Sweep) "Conformance"

- Grid Refinement

- Each RFU!
- Numerical dispersion (fake mixing)
⇒ Very problem / process dependent
⇒ Requires attention, always
- Wells: PSS Rate $E_{qs} = N_w \cdot N_c$
⇒ Needs fully implicit treatment
- Connects wells to Grid Cells
- May include Reservoir-to-Surface connections
 - VL Tables (Vertical Lift)
 - VL Eqs (VIP)

$P_{wf} \rightarrow P_t$

$\Delta p(q_g, q_o, q_w, P_{wf})$

DEPLETION RECOVERY

① Volumetric Material Balance

$$(\bar{p}_R)_{RFU} = f(Q_p; \bar{p}_{Ri}, Q_{pu})$$

$$\bar{p}_R(Q_p)$$

~ Est.

Ultimate Recovery
("EUR")

@ $\bar{p}_R \rightarrow \text{Abandonment}$

Theoretical

$\bar{p}_R \rightarrow 0$

② PSS Rate Eq.

$$q = f(\bar{p}_R, \bar{p}_{wf}; \underbrace{\frac{PI}{J}, C \& n; A, B}_{\text{constants}})$$

$$q(\bar{p}_{wf}, \bar{p}_R) = \frac{dq}{dt}$$

③ Couple MB & Rate Eq.

Time dependence of $q(t)$ and $Q_p(t)$
for a given, specified $\bar{p}_{wf}(t)$

- Analytically for special MB/IPR Eqs
 - Iterative (Explicit) ~ Solution Excel
- $$\left\{ \begin{array}{l} q_0 = J(\bar{p}_R - \bar{p}_{wf}) \\ \bar{p}_R = \bar{p}_{Ri} \left(1 - \frac{N_p}{N_{pu}}\right) \end{array} \right\}$$

④ Compare with Empirical (Amp's) DCA Eq.

for $\bar{p}_{wf} = \text{const.}$

Decline Curve Analysis

$$q \approx \frac{q_i}{[1 + bDt]^{1/b}} = q_i e^{-Dt}$$

$$\boxed{b = 0}$$

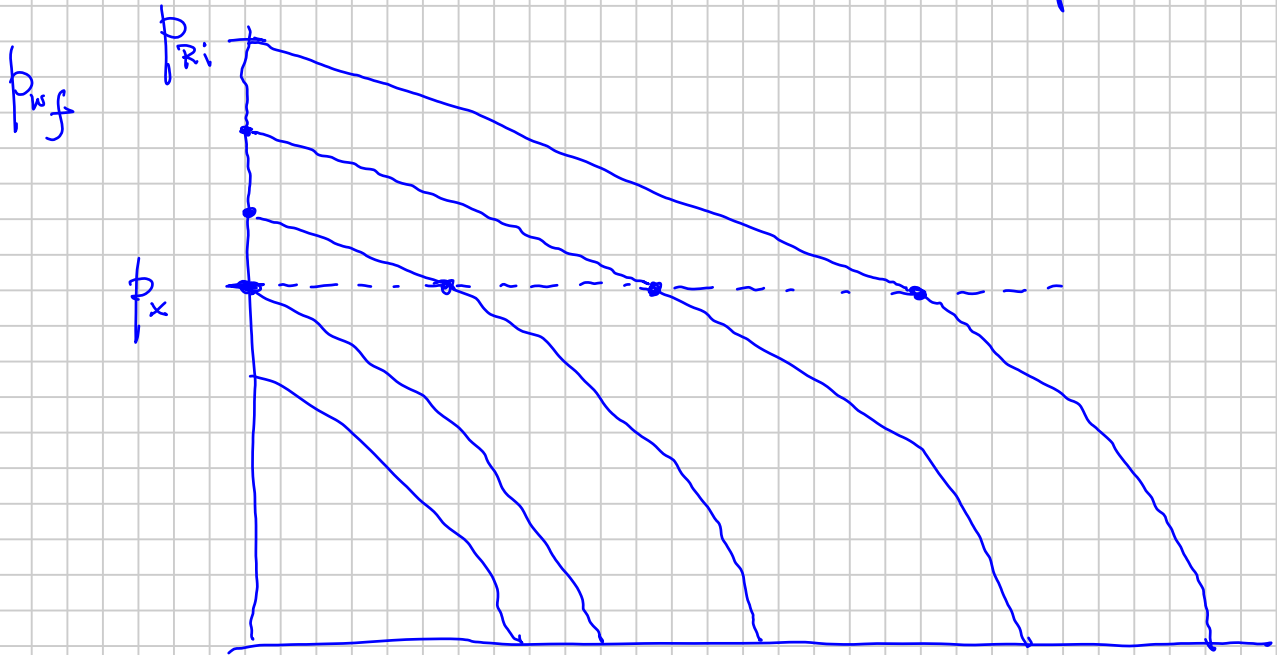
$$\frac{dN_p}{dt} = q_o$$

Generalized Rate Eq. Gas & Oil

Low $P_R < 200 \text{ bar}$ High $P_R > 200 \text{ bar}$

Undersat. Sat. (SGD)

$P_R > P_b$ $P_R < P_b$



$$p_{wf} > p_x : q = \sqrt{J} (P_R - p_{wf})$$

$$p_{wf} < p_x : q = \sqrt{J'} (P_R^2 - p_{wf}^2)$$

$$\text{OILS} : q_o \quad p_x = P_b$$

$$\text{GASES} : q_g \quad p_x \approx 200 \pm \text{bar}$$