

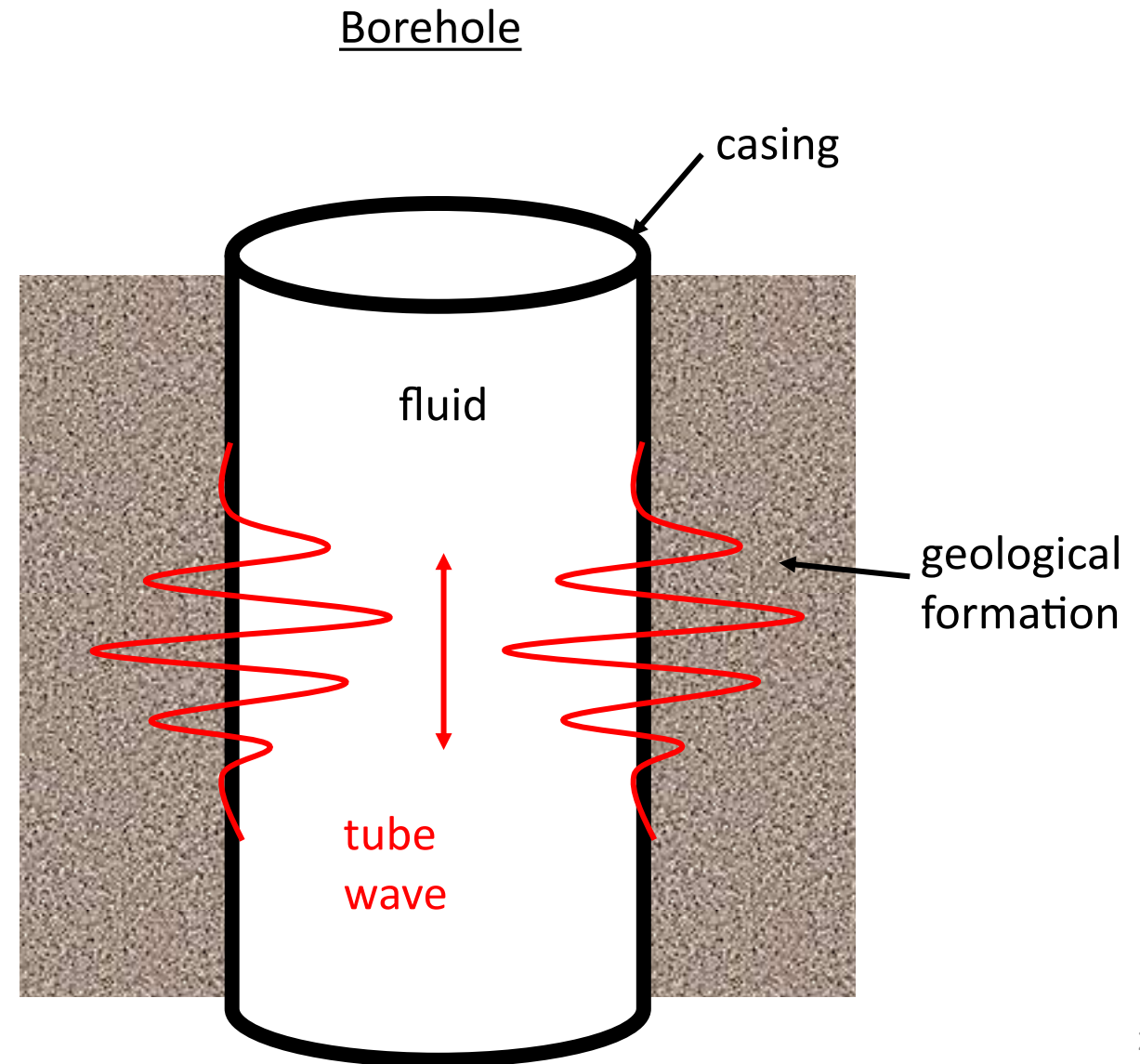
# Estimating S-wave velocities and changes from tube waves

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- Tube wave history
  - Lamb (1898), Biot (1952), Somers (1953), ...
- Generated at interfaces striking the borehole (Hardage, 1981)
- Usage:
  - identification of fractures (Hornby et al. 1989; Li et al., 1994)
  - permeability of formation when coupled to borehole fluid (White, 1965; Chang et al., 1988; Winkler et al. 1989)
  - estimate S-wave of formation from acoustic logging (Stevens and Day, 1986)
  - often considered as noise in VSP



➔ Is it possible to estimate the Shear Modulus and S-Wave velocity changes in the geological formation by measuring Tube waves?

## Advantages

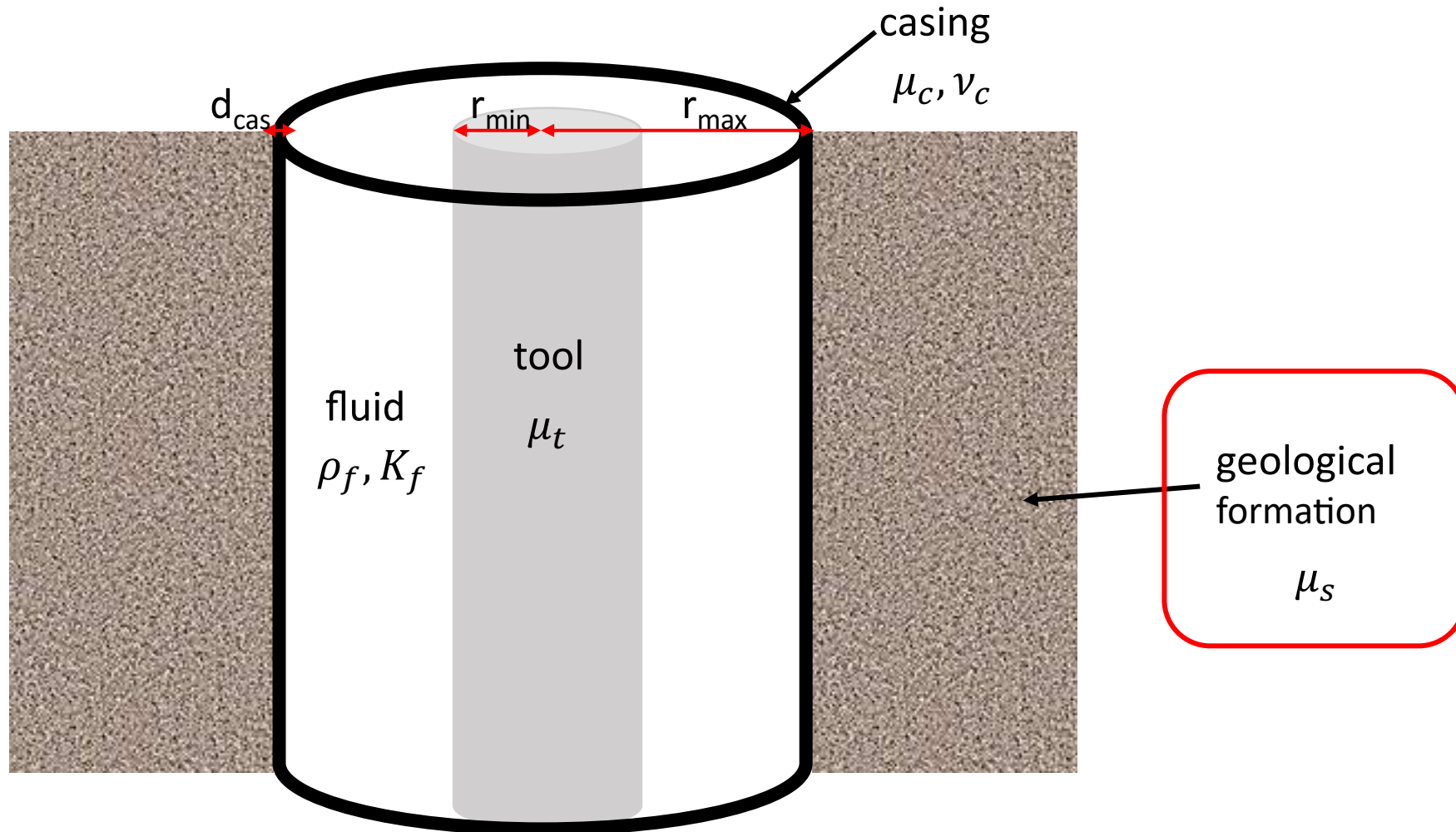
- Fixed source position
  - position and firing time is not required
- Only hydrophones are required
  - free from mechanical noise (Peng, 1996)
  - low-cost
- Permanently installed system
- Might use passive seismic recordings

## Problems

- Precise estimation of tube wave velocity
- Tube wave depends on several borehole parameter (casing, logging tool, borehole fluid)

Theory

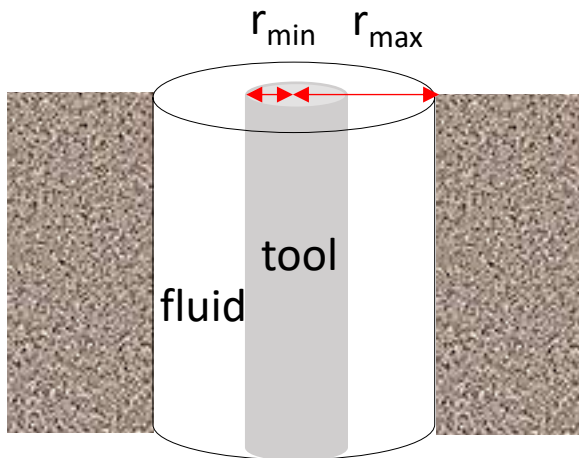
Important parameter for Tube wave vs. Shear Modulus of formation



## (1) Only logging tool:

(Marzetta and Schoenberg, 1985)

$$v_{t1} = \left\{ \rho_f \left[ \frac{1}{K_f} + \frac{1}{1-\eta} \left( \frac{1}{\mu_s} + \frac{\eta}{\mu_t} \right) \right] \right\}^{-\frac{1}{2}}$$

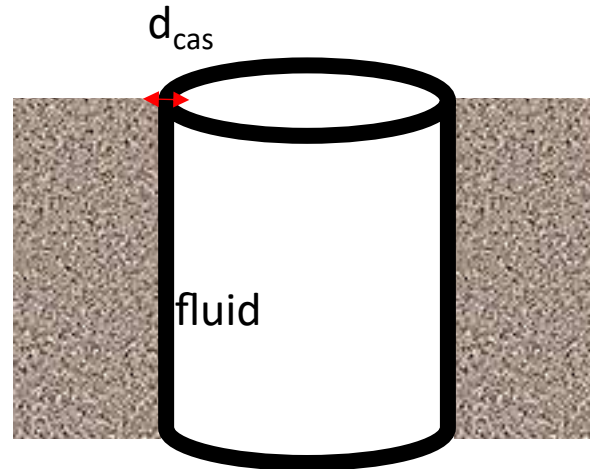


## (2) Only casing:

(Marzetta and Schoenberg, 1985, Norris 1990)

$$v_{t2} = \left\{ \rho_f \left[ \frac{1}{K_f} + \frac{1}{N} \right] \right\}^{-\frac{1}{2}}$$

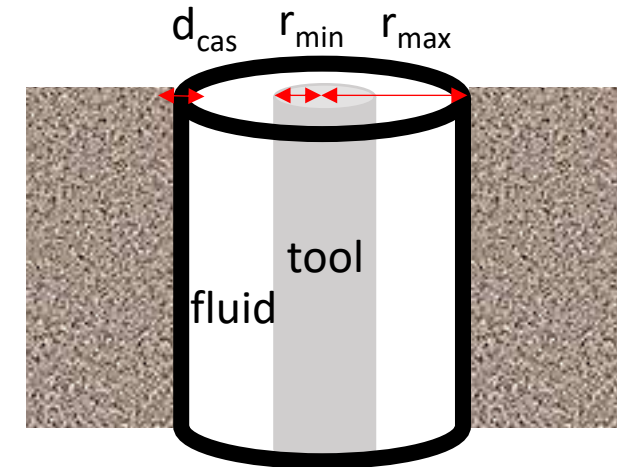
$$N = \frac{2(1-\nu_c)\mu_s + (\mu_c - \mu_s)(1-a^2)(1-\beta v_c^2)}{2(1-\nu_c) - \left(1 - \frac{\mu_s}{\mu_c}\right)(1-2\nu_c + \beta v_c^2)(1-a^2)}$$



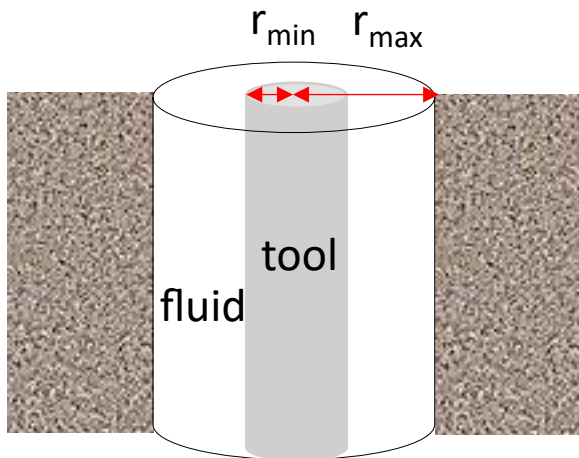
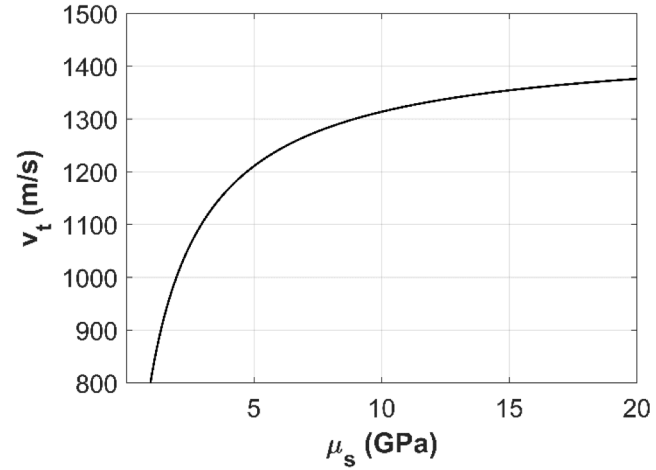
## (3) Logging tool and casing:

(Norris, 1990)

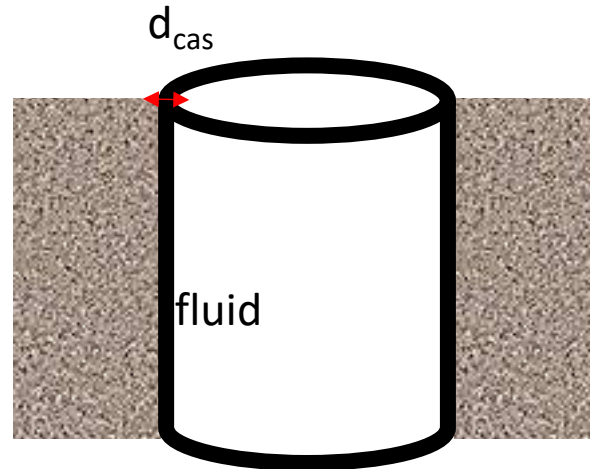
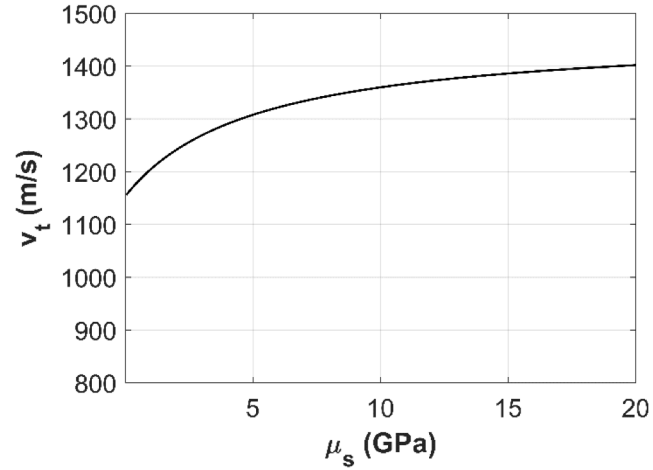
$$v_{t3} = \left\{ \rho_f \left[ \frac{1}{K_f} + \frac{\eta}{(1-\eta)\mu_t} + \frac{1}{(1-\eta)N} \right] \right\}^{-\frac{1}{2}}$$



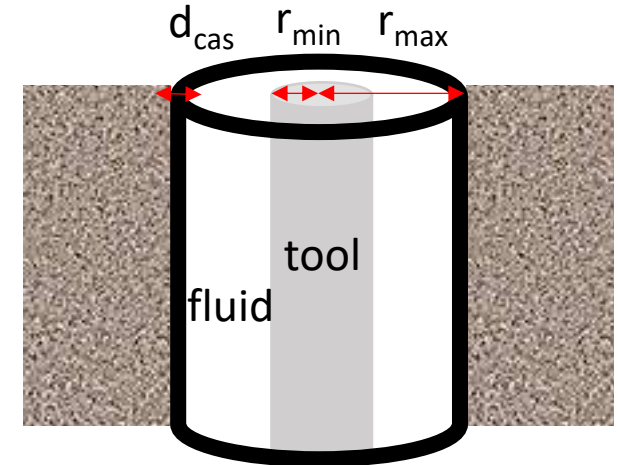
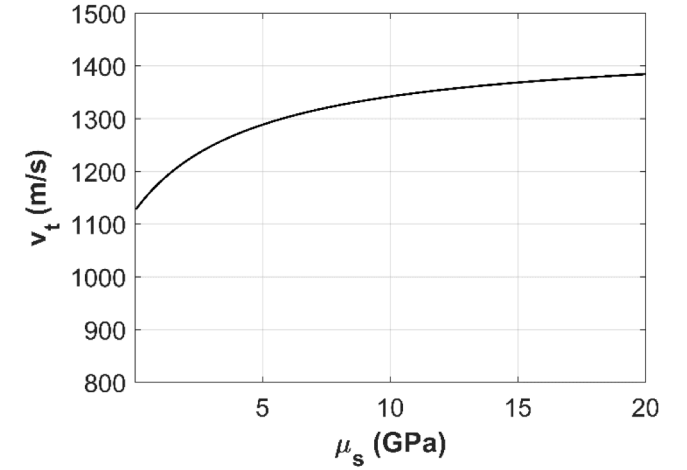
(1) Only logging tool:



(2) Only casing:

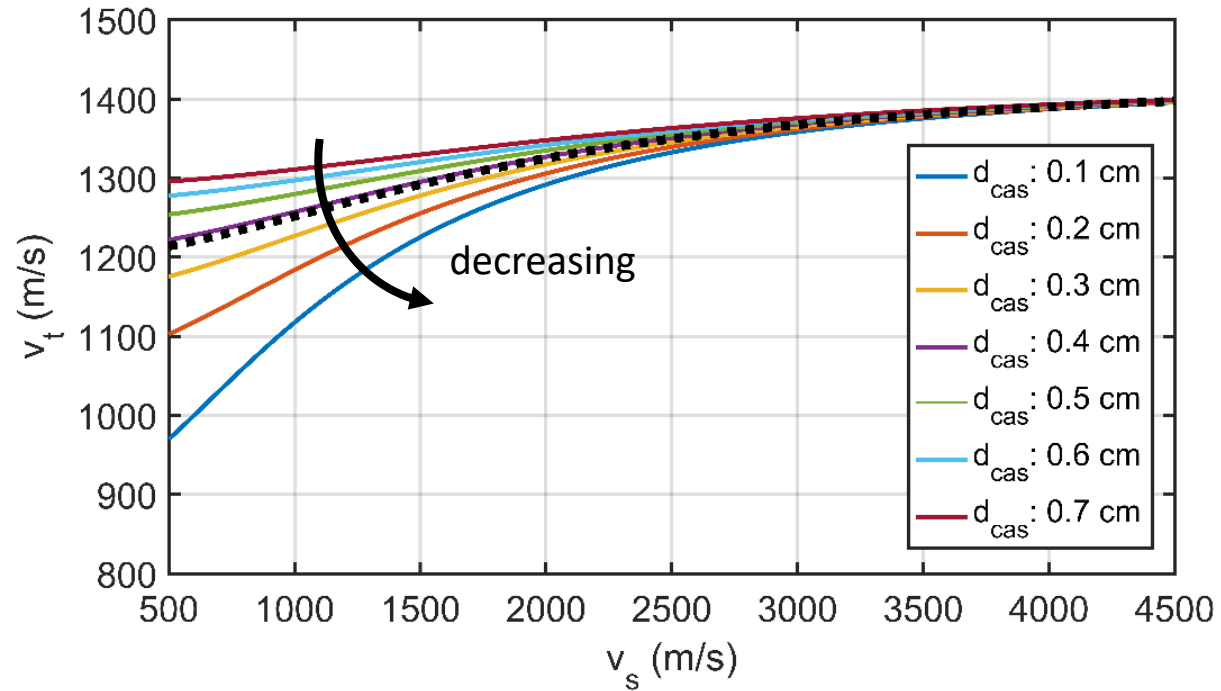


(3) Logging tool and casing:

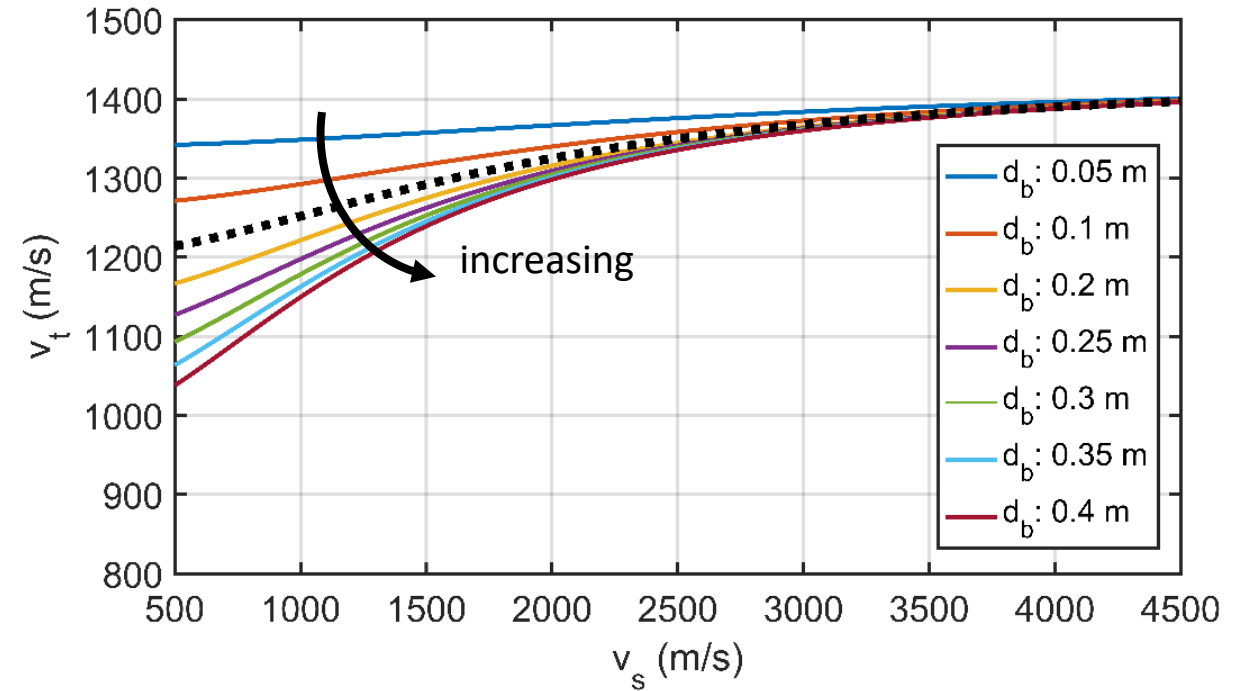


# Sensitivity to different parameter

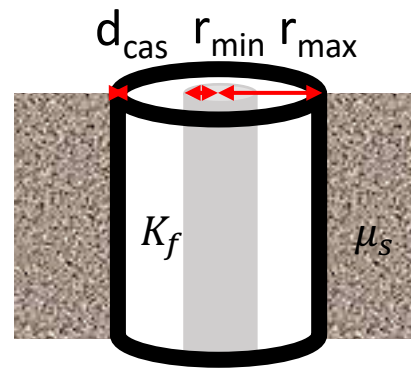
### Casing thickness



### Borehole diameter



..... reference





# Experiments

# Experiments

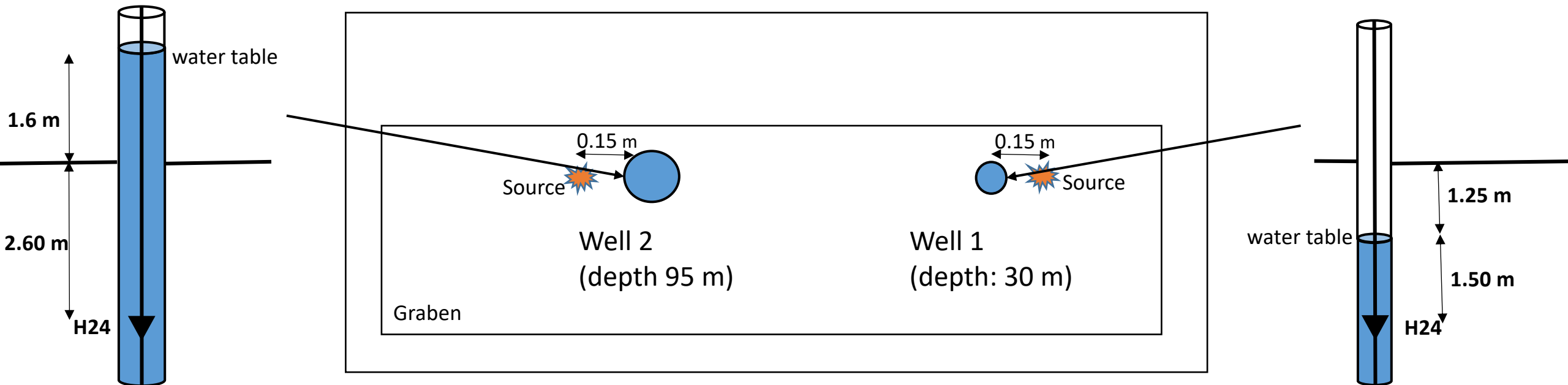
Workhall



Wells



Source



# Experiments

Receiver: 24 channel hydrophone array

- spacing: 1 m
- frequency range 1 Hz – 10000 Hz

Tests:

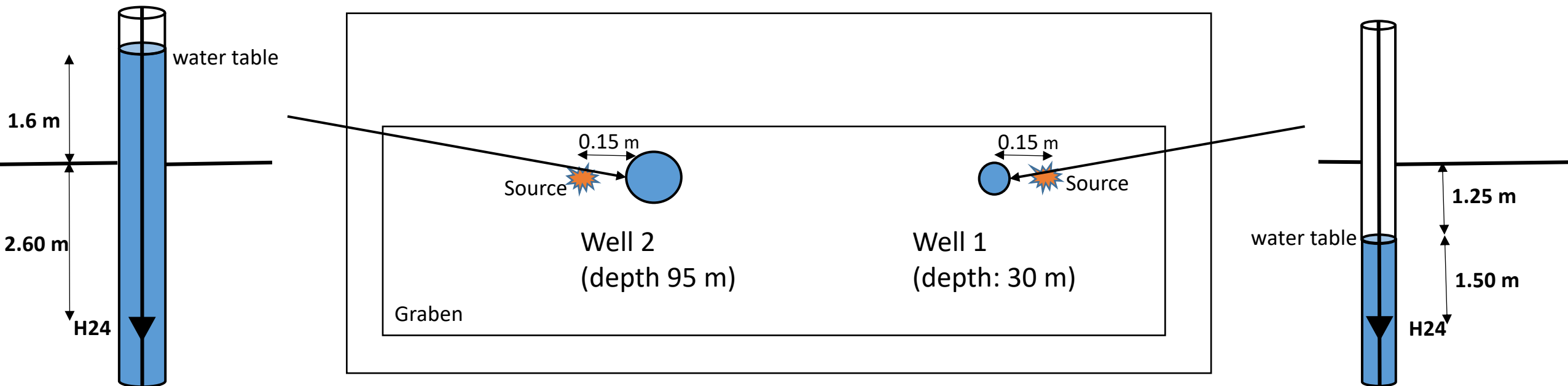
- Well 1: September 17, October 17 and March 18
- Well 2: October 17

Well 1:

- diameter: 15 cm
- casing thickness: 4 mm

Well 2:

- diameter: 30 cm
- casing thickness: 5 mm

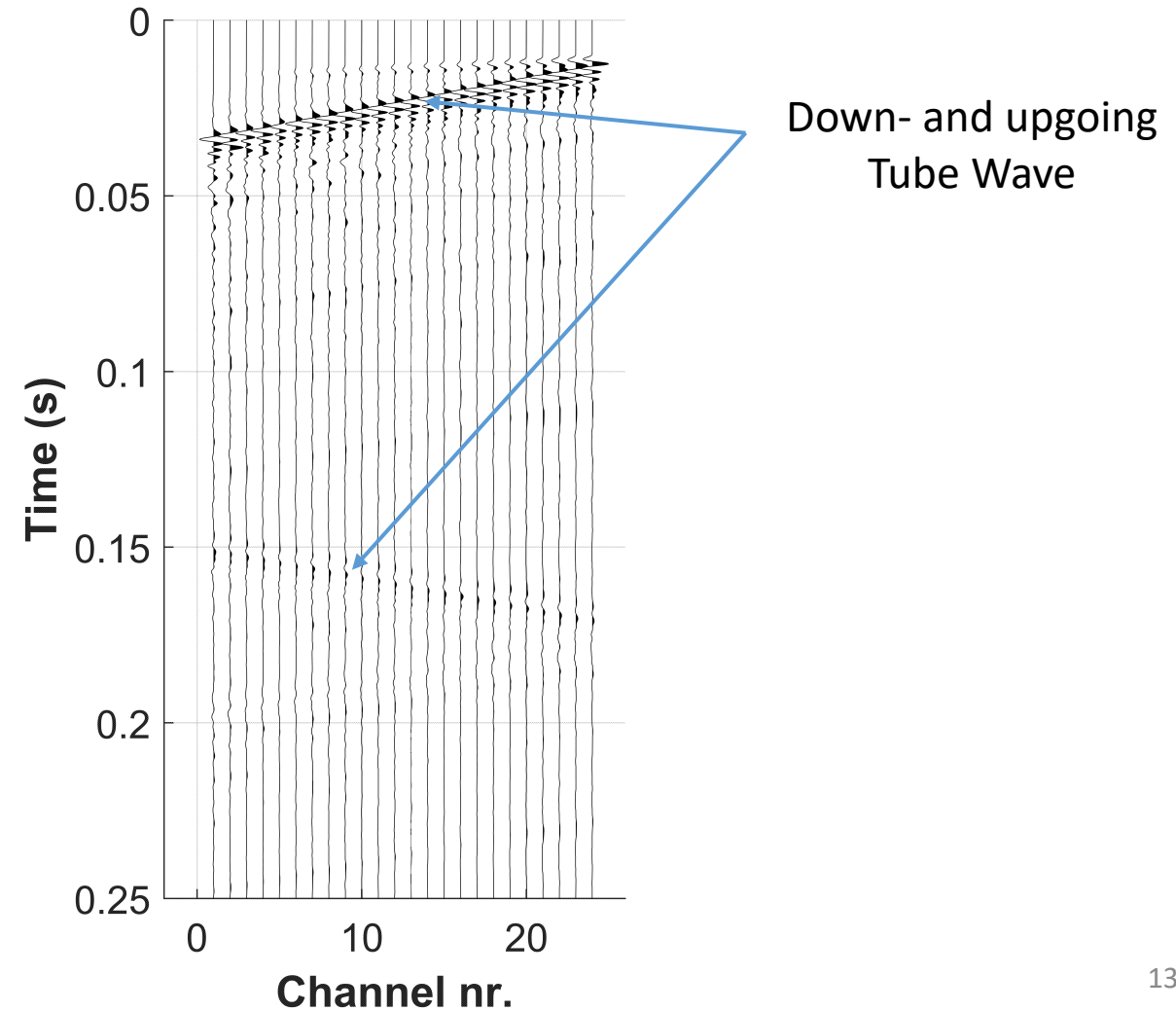
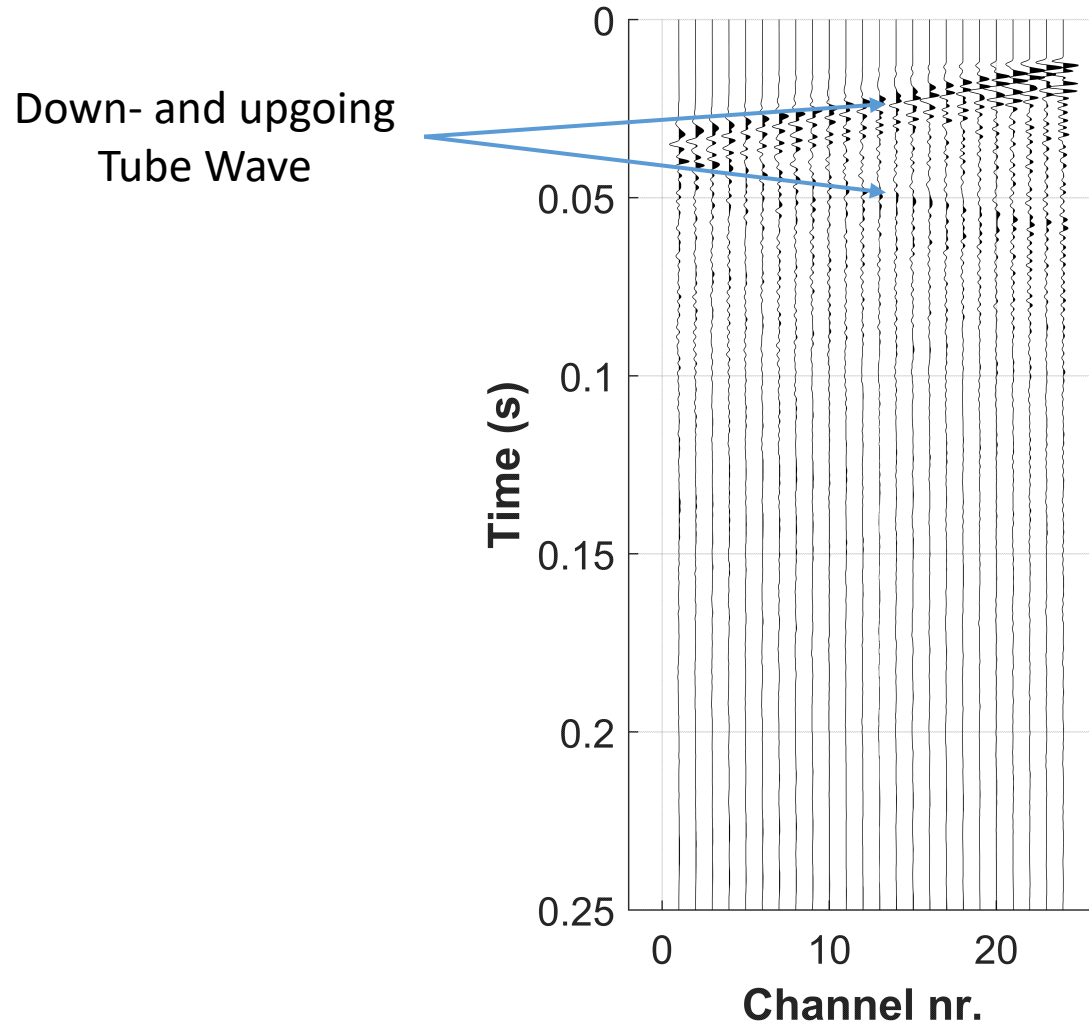


# Results

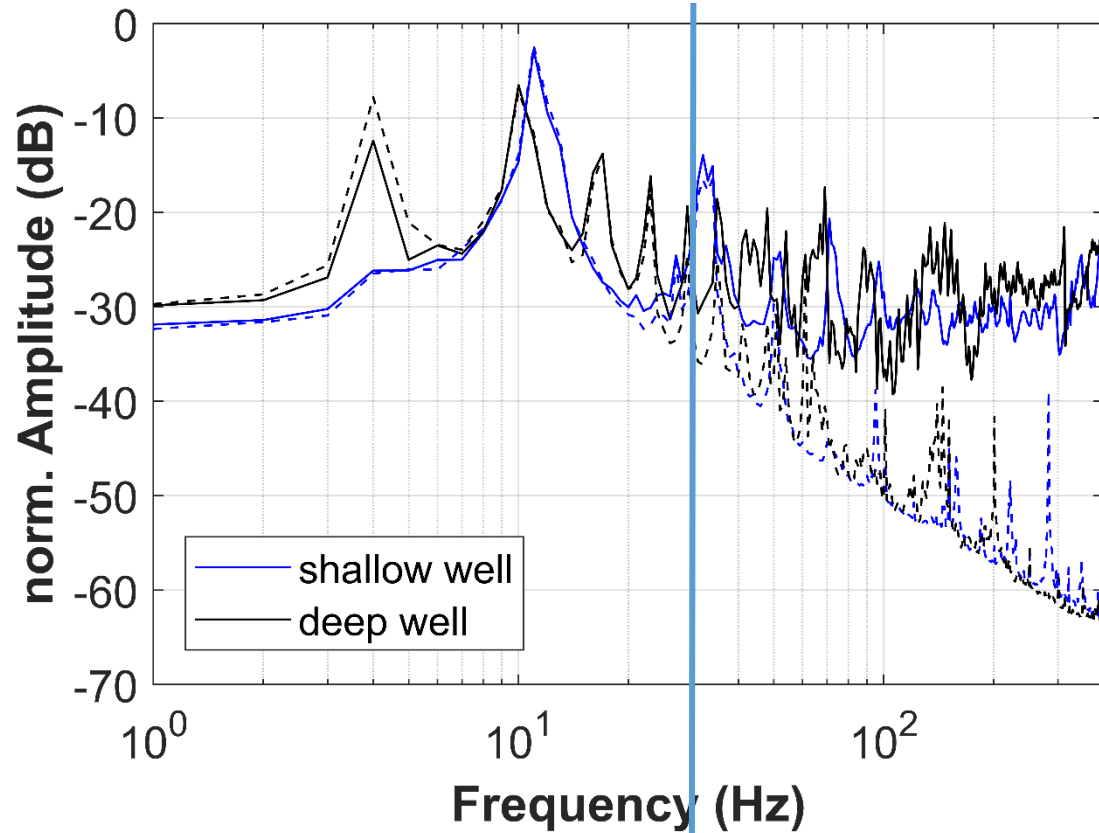
Well 1 (30 m)

Well 2 (95 m)

bandpass filter: 50 Hz – 450 Hz

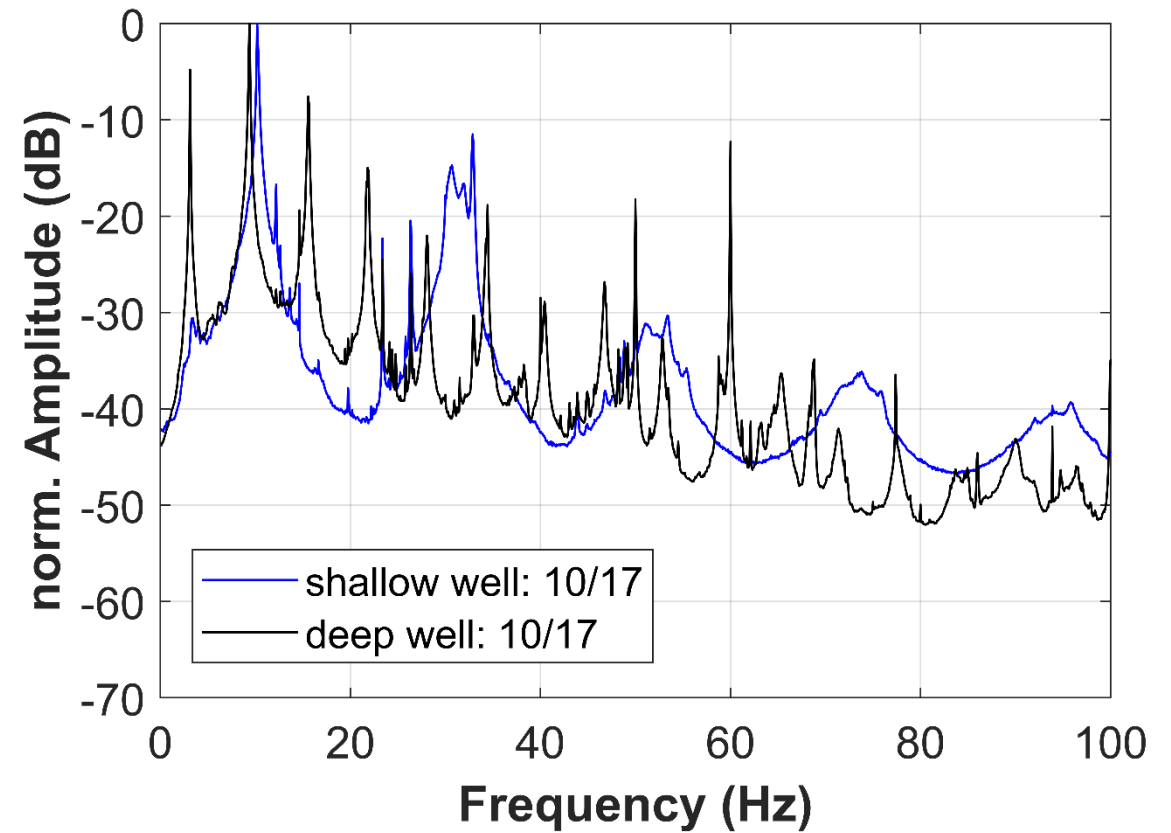


Active recordings and noise



> 30 Hz: signal above noise level

Passive recordings

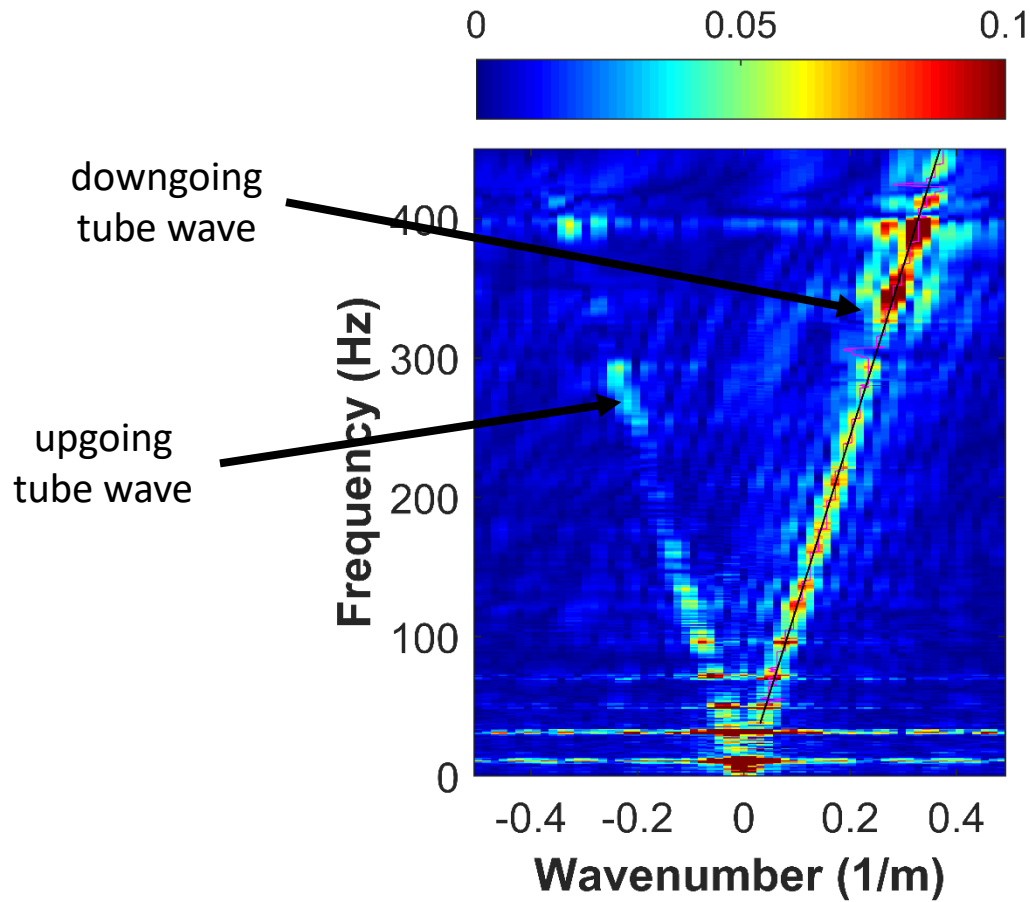


Peaks at  $f = \frac{1200 \frac{m}{s}}{4 * z_w} (2m - 1), m = 1, 2, 3, \dots$

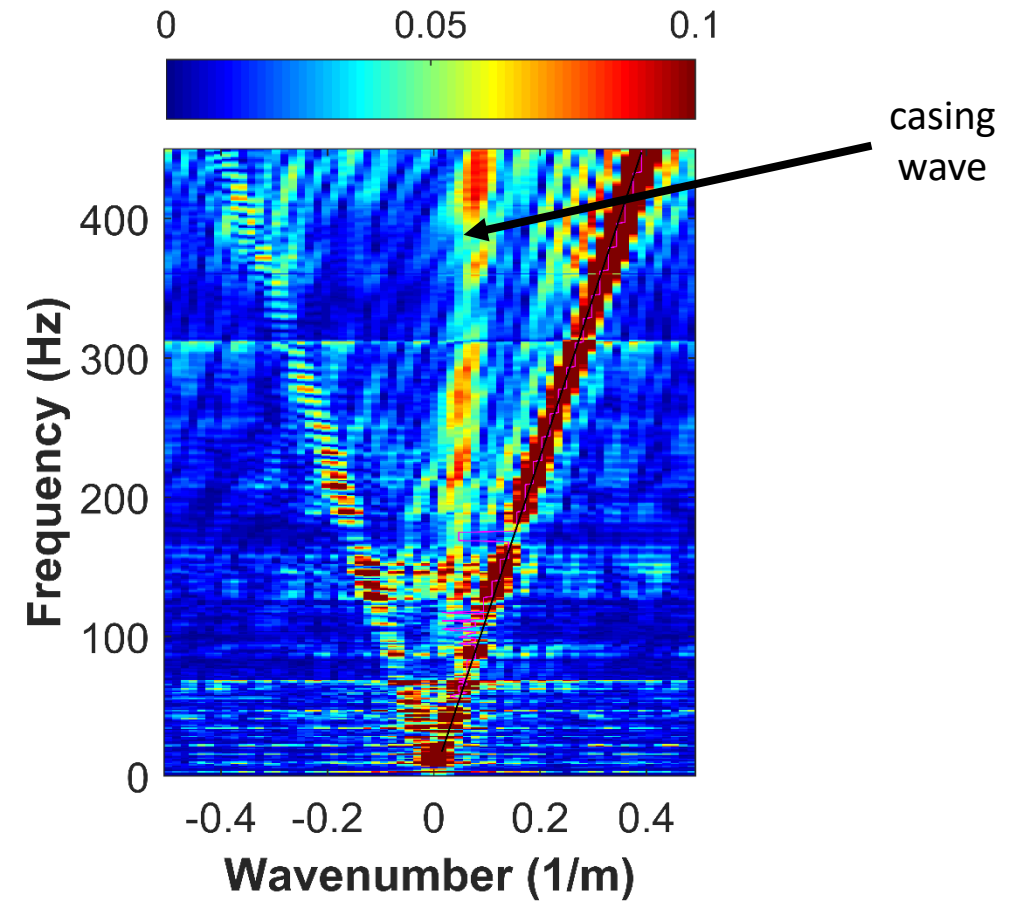
- Shallow well  $\Delta f = 20$  Hz
- Deep well  $\Delta f = 6$  Hz

# Tube Wave Velocity

Well 1 (30 m)



Well 2 (95 m)



Least-squares line fit to estimate velocity

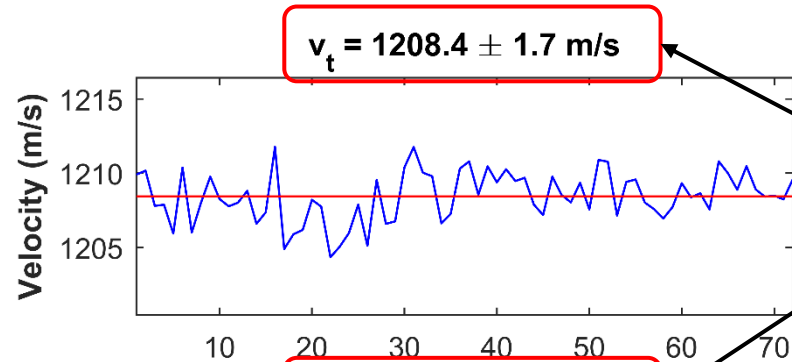
- between 50-450 Hz
- dispersion effect: velocity decrease  $< 0.02\%$  between 0-1000 Hz

# Tube Wave Velocity

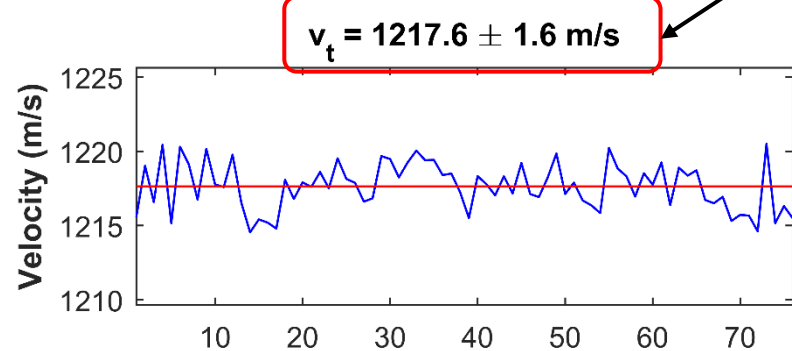
Well 1 (30 m)

Well 2 (95 m)

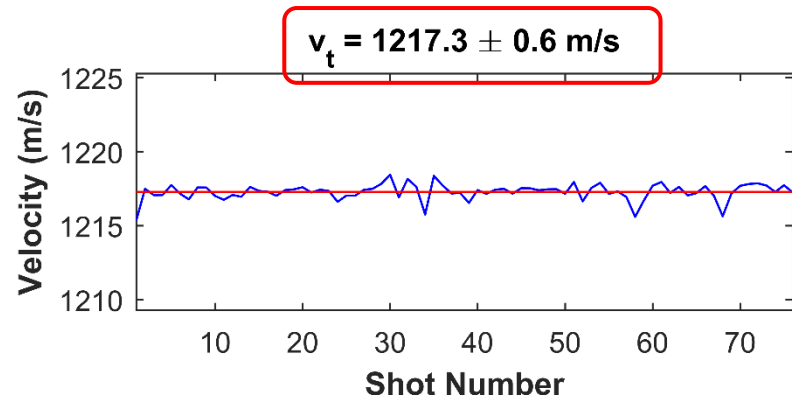
September 17



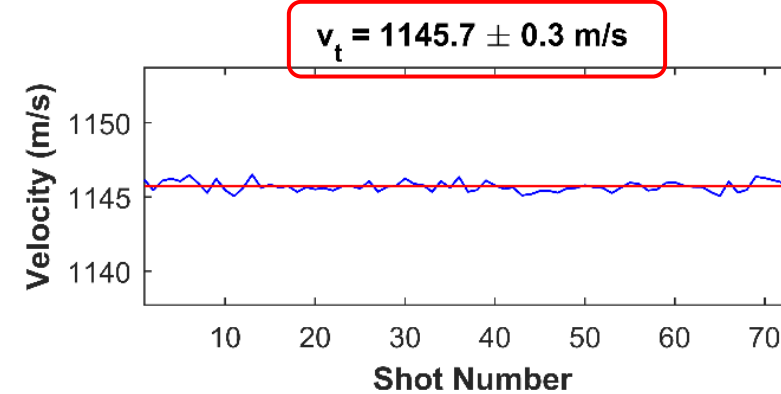
October 17



March 18



could be caused by temperature difference in borehole fluid  
(1°C → 2 m/s)



October 17

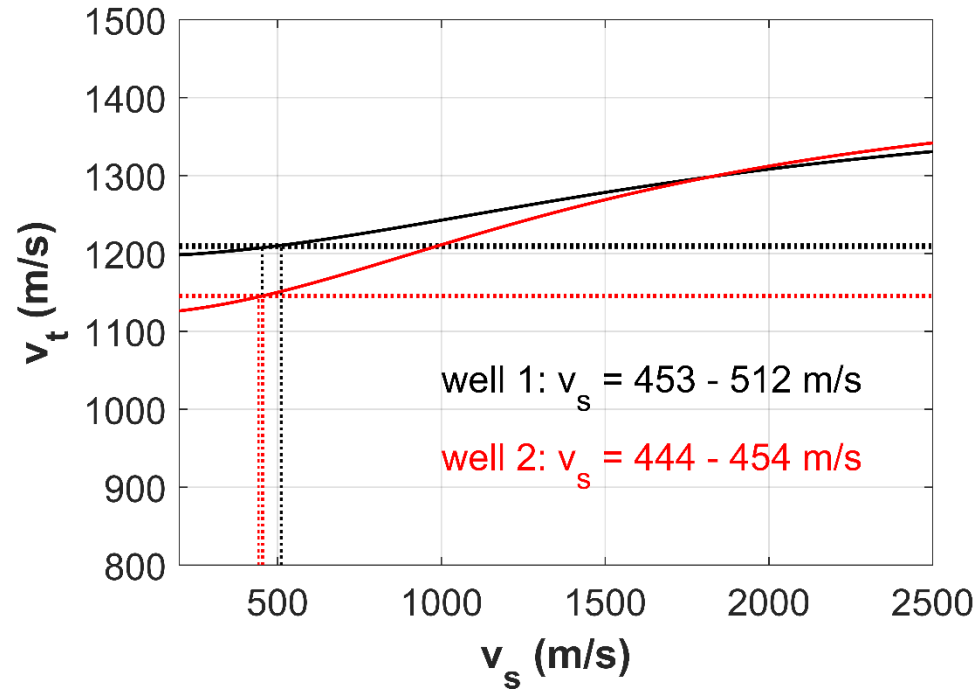
➡ High accuracy in results



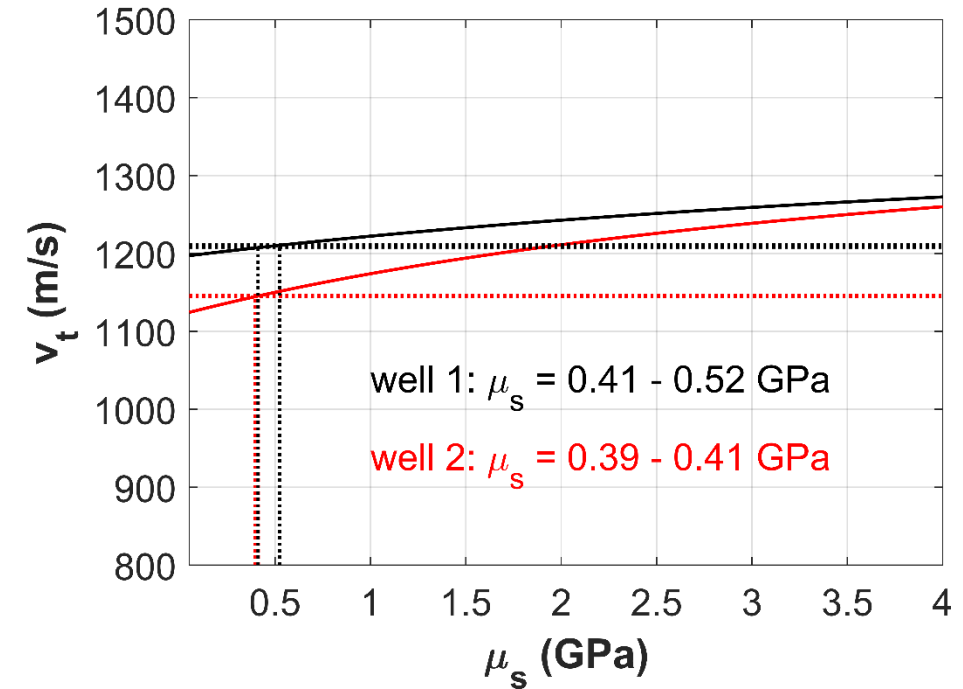
# Estimated Formation Properties

## S-wave velocity

( $\rho = 2000 \text{ kg/m}^3$ )



## Shear modulus



Smaller estimated range in well 2

- higher accuracy of tube wave velocity
- different borehole geometry

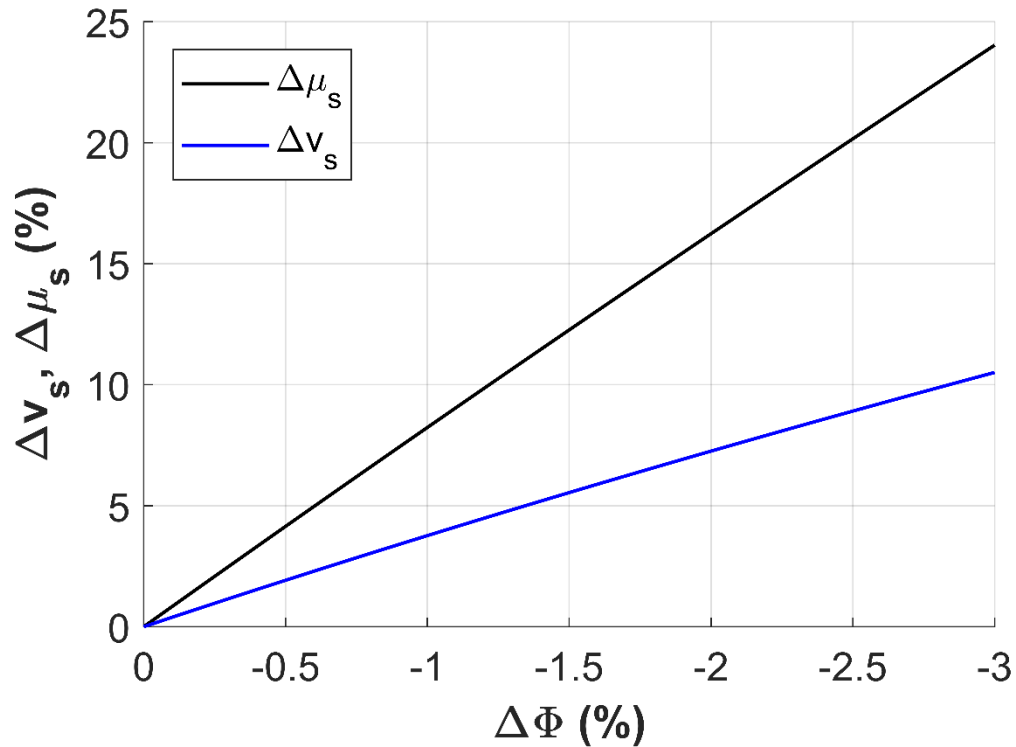
Field example

# Field example: CO<sub>2</sub> injection

## Changes due to CO<sub>2</sub> injection

### Precipitation of salt

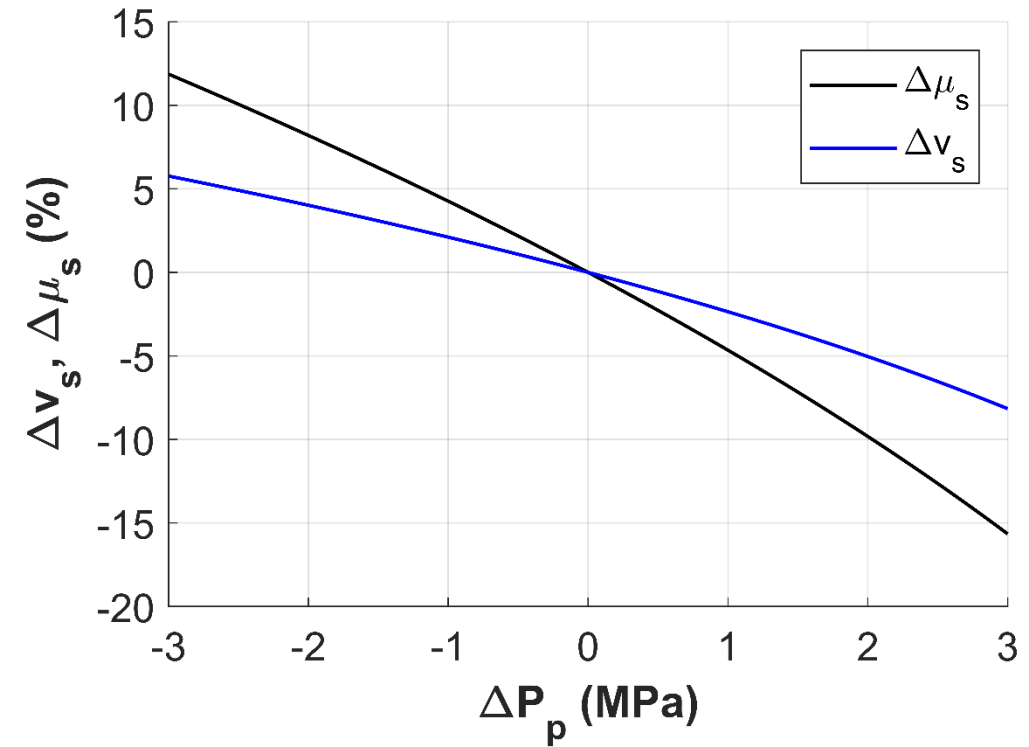
(Lab examples: Vanorio et al., 2011; Grude et al. 2014)



- sandstone, initial porosity  $\Phi = 0.3$
- salinity: 50000 ppm

### Pore pressure $P_p$ increase

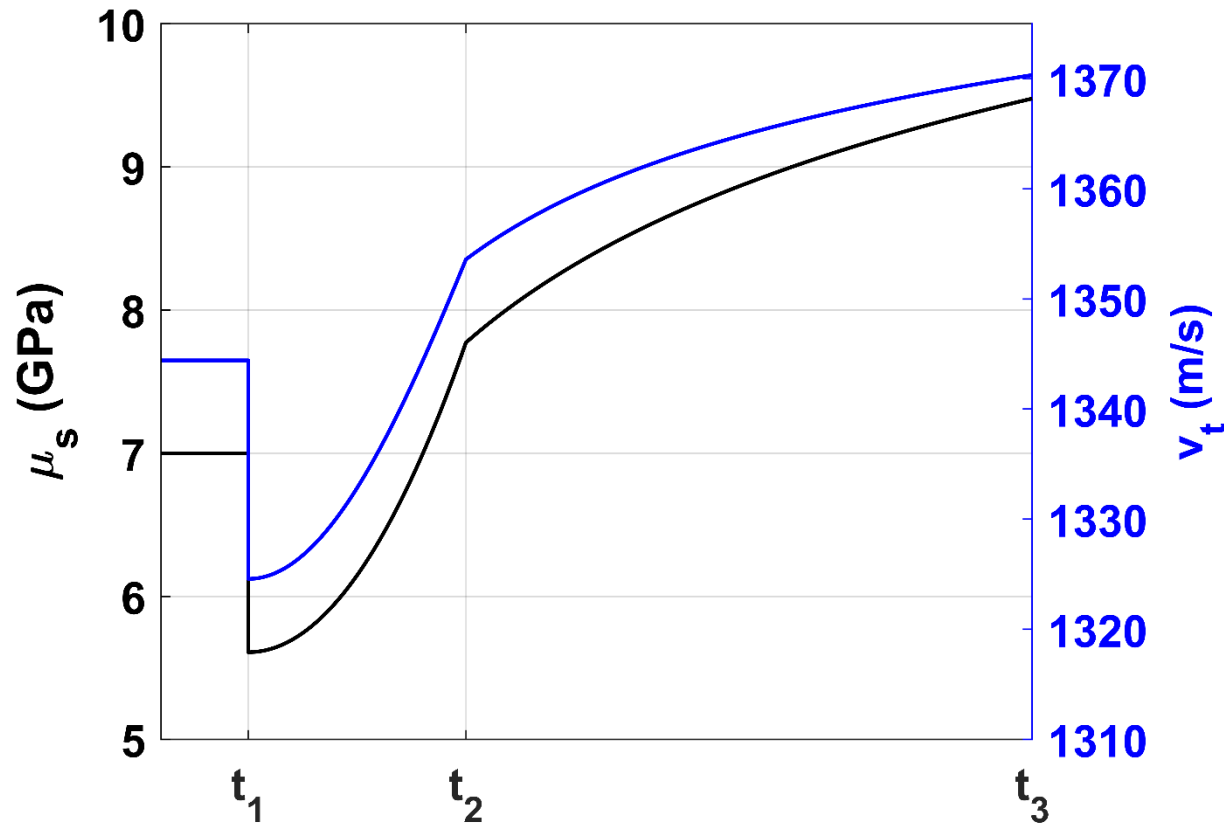
(Field examples: Duffaut and Landrø, 2007; Grude et al. 2014)



- initial  $P_p = 7.5$  MPa (ca. 750 m depth)
- Hertz-Mindlin model

# Field example: CO<sub>2</sub> injection

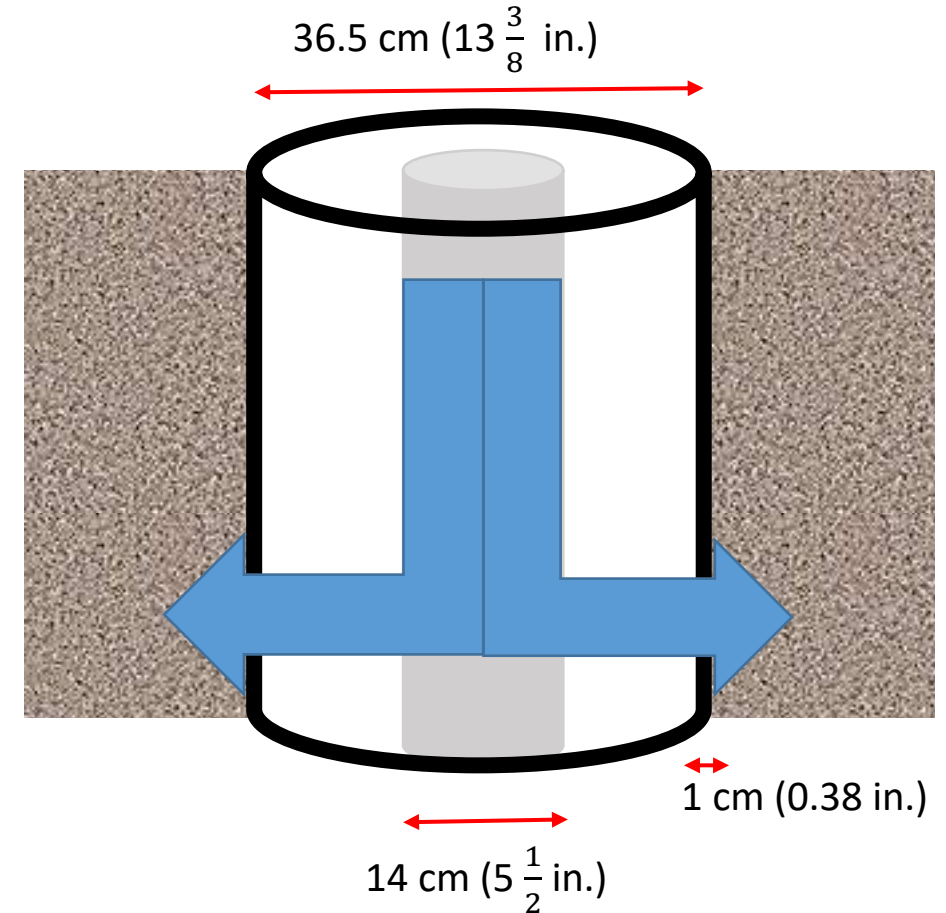
Time steps during CO<sub>2</sub> injection



$t_1$ : injection starts

$t_2$ : injection stops

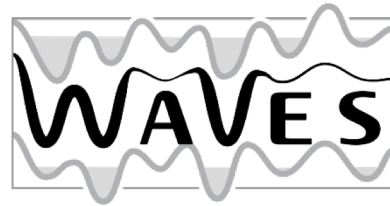
$t_3$ : initial pore pressure is reached



- initial  $P_p = 7.5$  MPa (ca. 750 m depth)
- decrease of 2.5 MPa due to injection

- Absolute estimation of shear modulus/S-wave is difficult
  - additional measurements required
- Monitoring could be feasible
  - temperature in borefluid should be measured
  - high accuracy of measured tube wave velocity required
- Feasibility depends on geological setting and borehole set-up
  - borehole should have: thin casing, large diameter, small casing shear modulus
  - geological formation with low initial shear modulus
- Advantages
  - no firing time and source location required (Passive Seismics?)
  - hydrophones: cheap, permanent monitoring system (Fibre Optics?)
- Disadvantages
  - tube wave depends on several parameter

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Norwegian University of Science and Technology Trondheim



- Biot, M. A. [1952] Propagation of elastic waves in a cylindrical bore containing a fluid. *Journal of Applied Physics*, **13**, 997-1005.
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- Lamb, H. [1898] On the velocity of sand in a tube as affected by the elasticity of the wall. *Manchester Memoires*, **42**, 1-16.
- Marzetta, T. L. and Schoenberg, M. [1985] Tube waves in cased boreholes. *SEG Technical Program Expanded Abstract*, 34-36.
- Norris, A. N. [1990] The speed of a tube wave. *Journal of Acoustical Society of America*, **87**, 414-417.
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- Somers, E. [1953] Propagation of acoustic waves in a liquid-filled cylindrical hole surrounded by an elastic solid. *Journal of Applied Physics*, **24**, 513-521.
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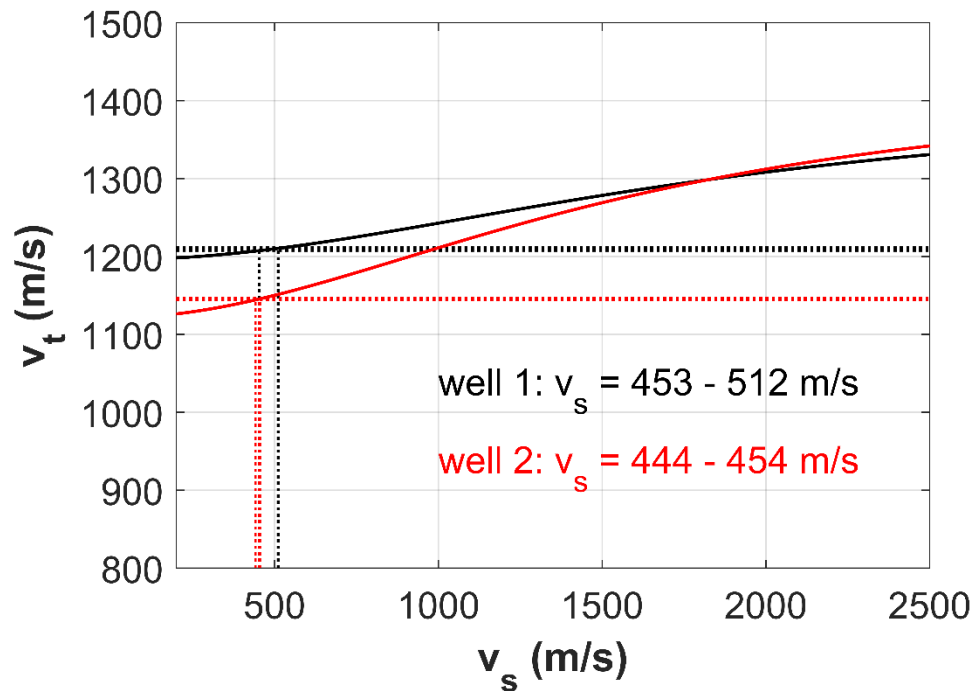
# Appendix



# Estimated Formation Properties

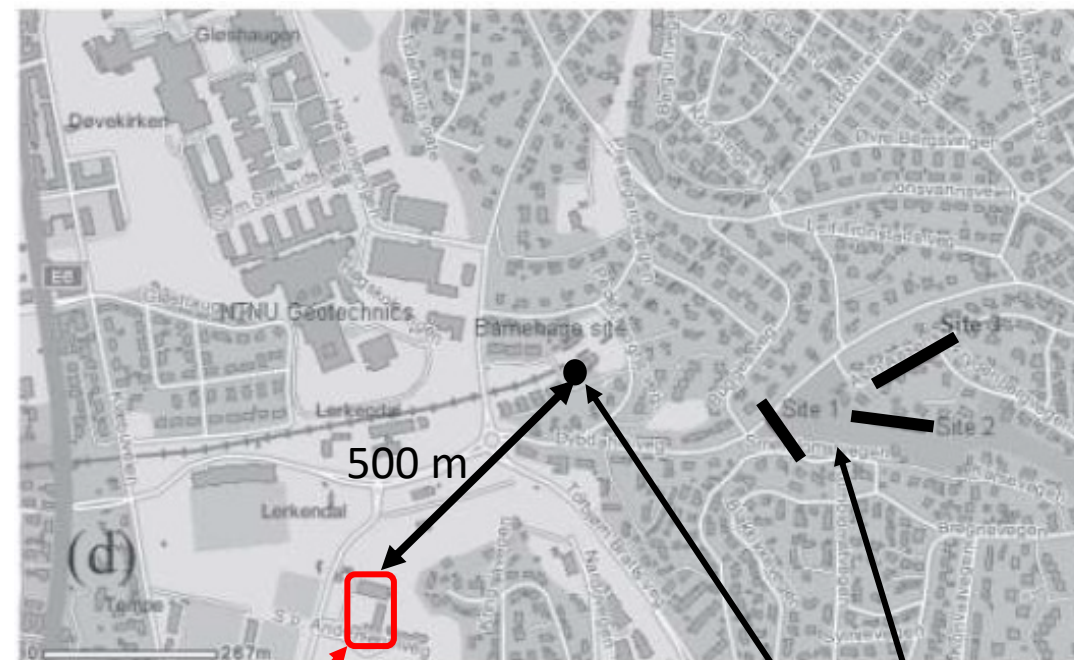
## S-wave velocity

( $\rho = 2000 \text{ kg/m}^3$ )



## “Reference” test site Edberg

Long and Donohue, 2007



➔  $v_s$  at wells ca. 450 m/s  
(down to 26 m depth)

➔  $v_s$  at Edberg site ca. 300 m/s  
(down to 10 m depth)

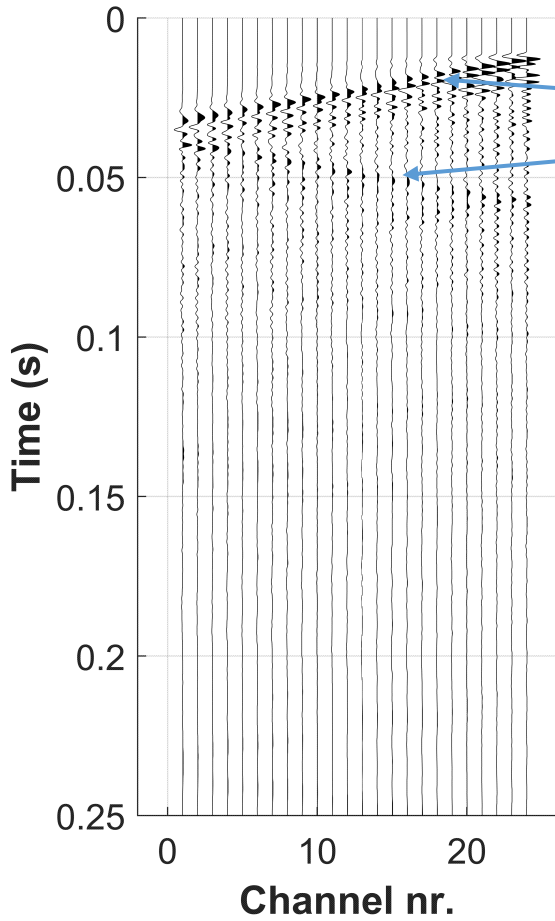
- Theory
  - Relation between Tube wave and S-wave in the surrounding formation
- Experiments
  - Set up and parameter
- Results
  - Measured Tube wave
  - Estimation of S-wave in the surrounding formation
- Discussion
  - Sensitivity analysis
  - Theoretical field example
- Conclusion

# Recordings

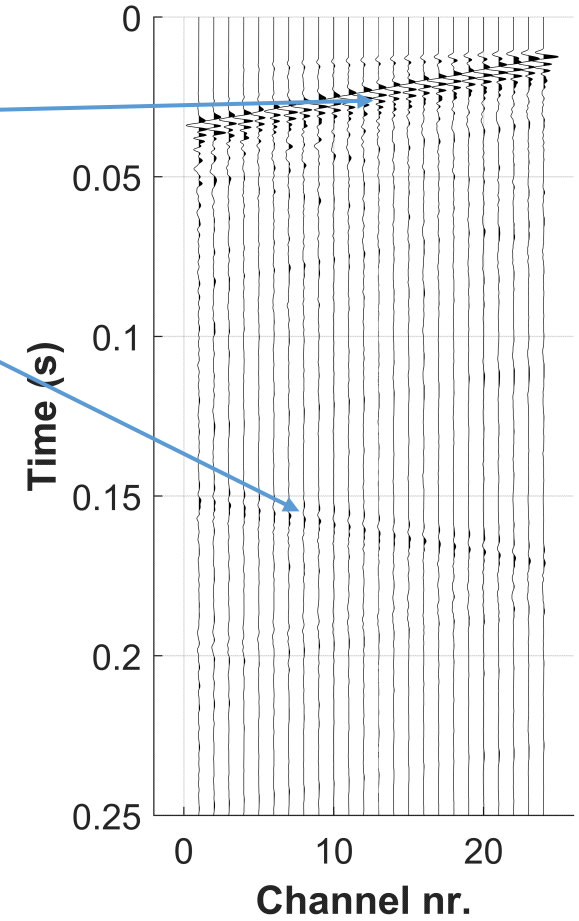
Well 1 (30 m)

bandpass filter: 50 Hz – 450 Hz

Well 2 (95 m)

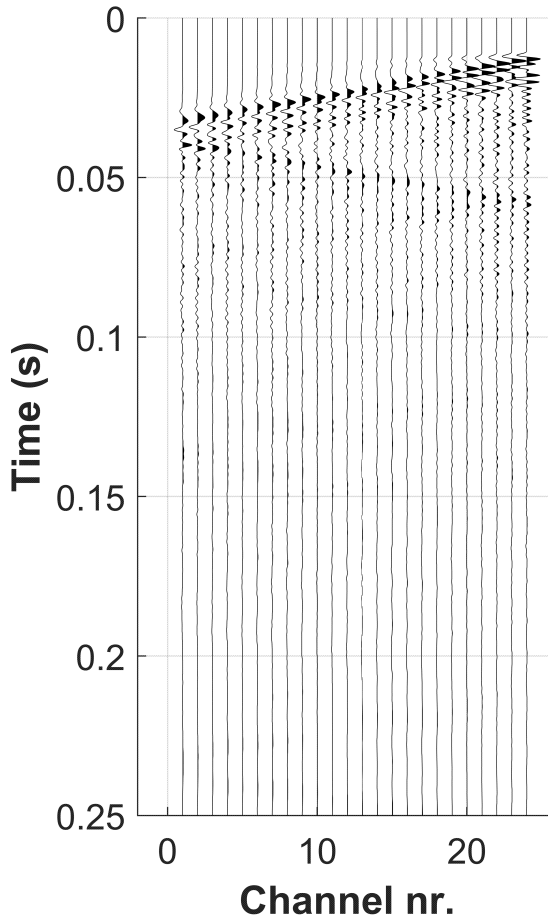


Down- and upgoing  
Tube Wave

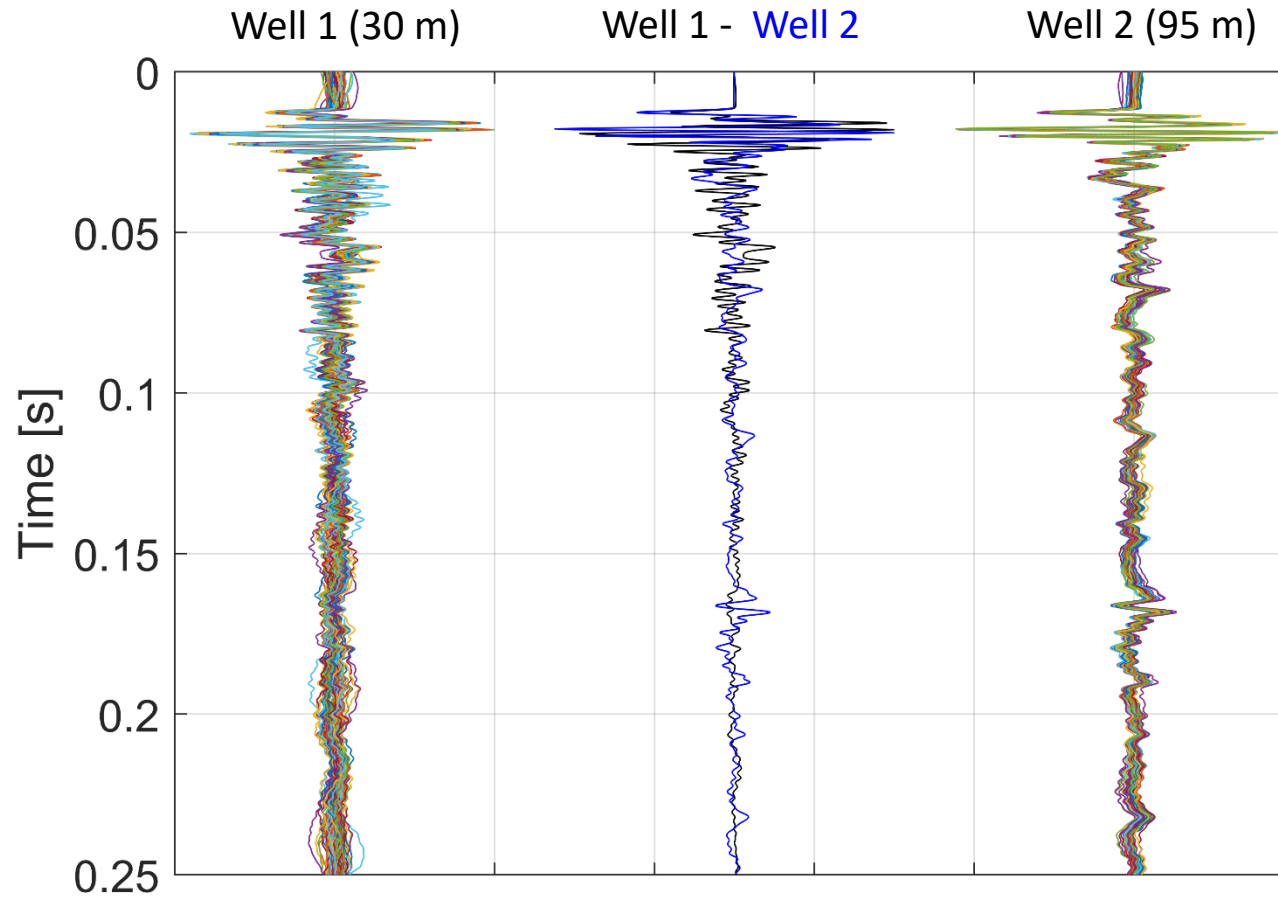
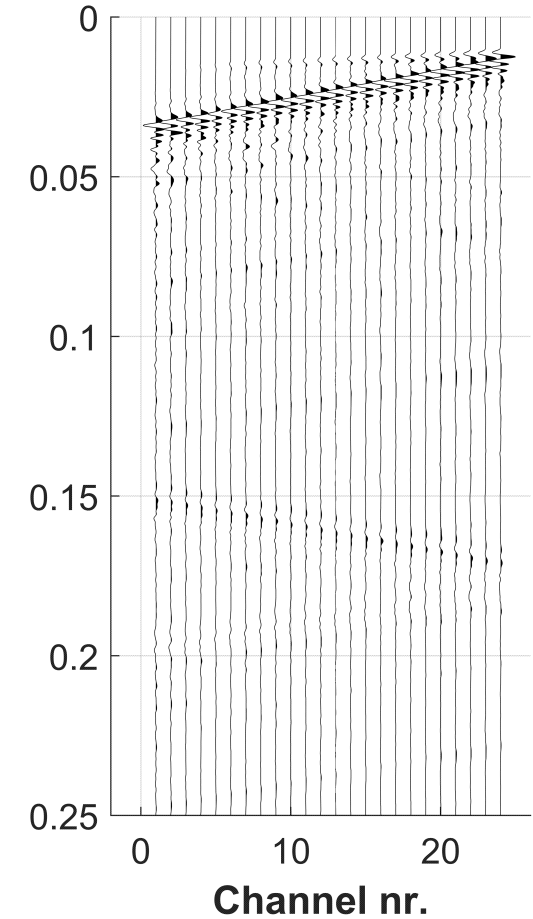


## Single receiver (Nr.: 20)

Well 1 (30 m)

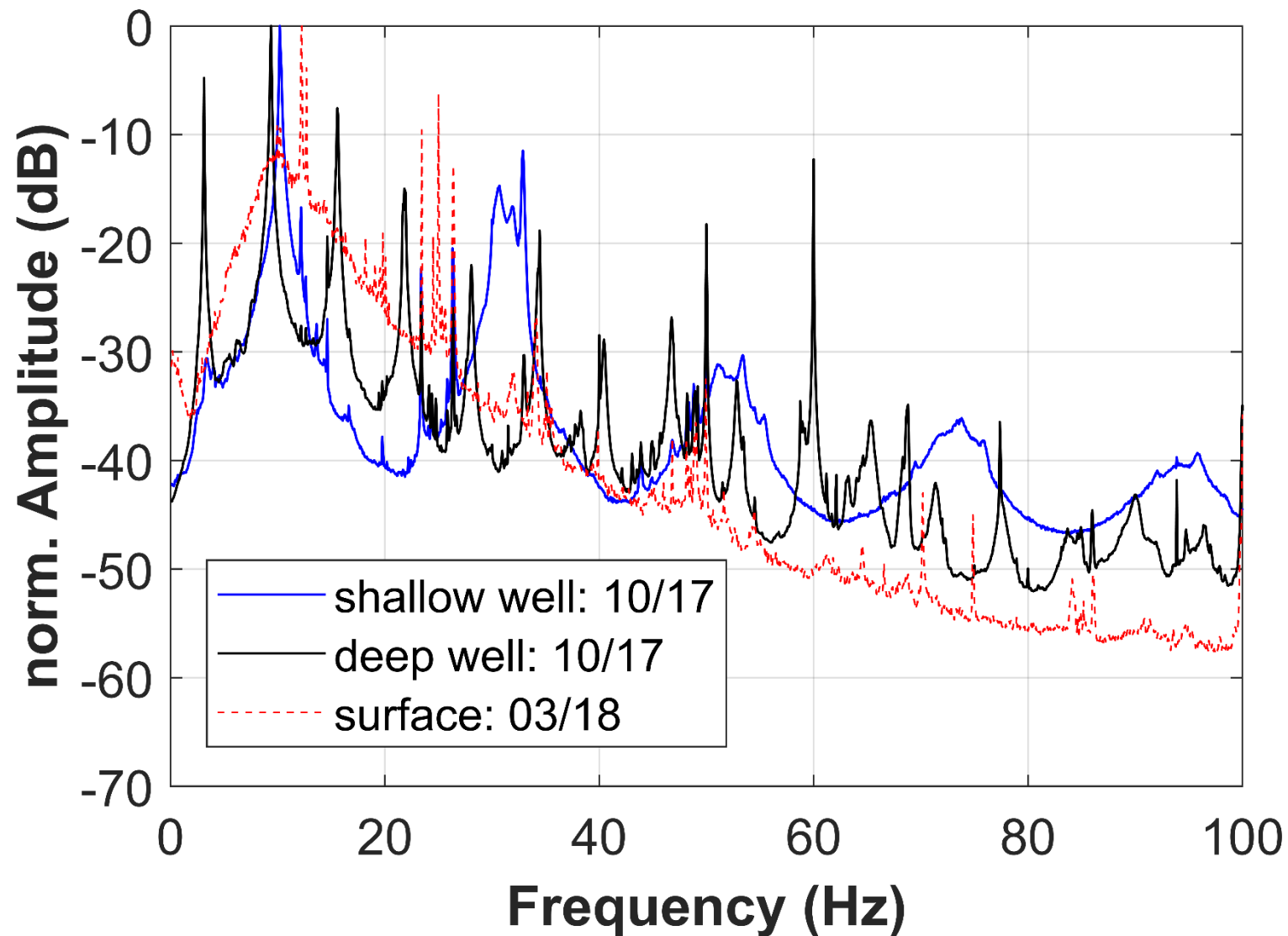


Well 2 (95 m)



- repeatability of 80 hammer shots
- longer repeatable signal in deep well

## Passive recordings

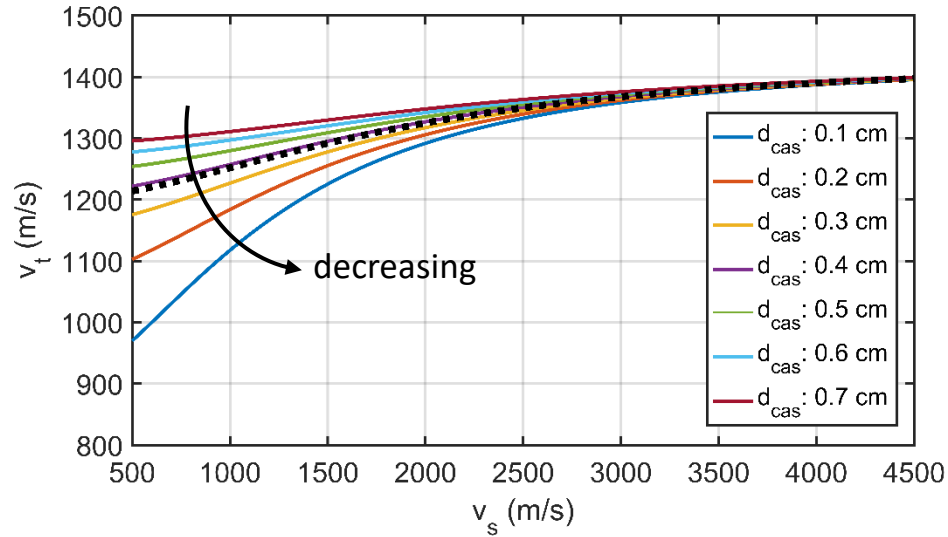


Peaks at  $f = \frac{1200 \frac{m}{s}}{4 \cdot 30 m} (2m - 1)$ ,  $m = 1, 2, 3, \dots$

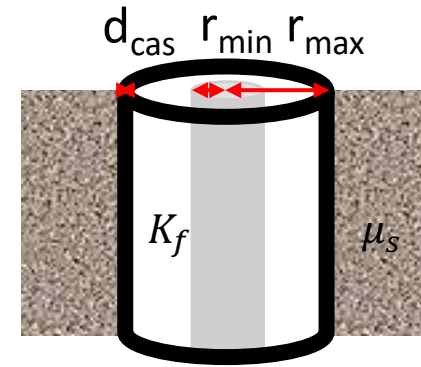
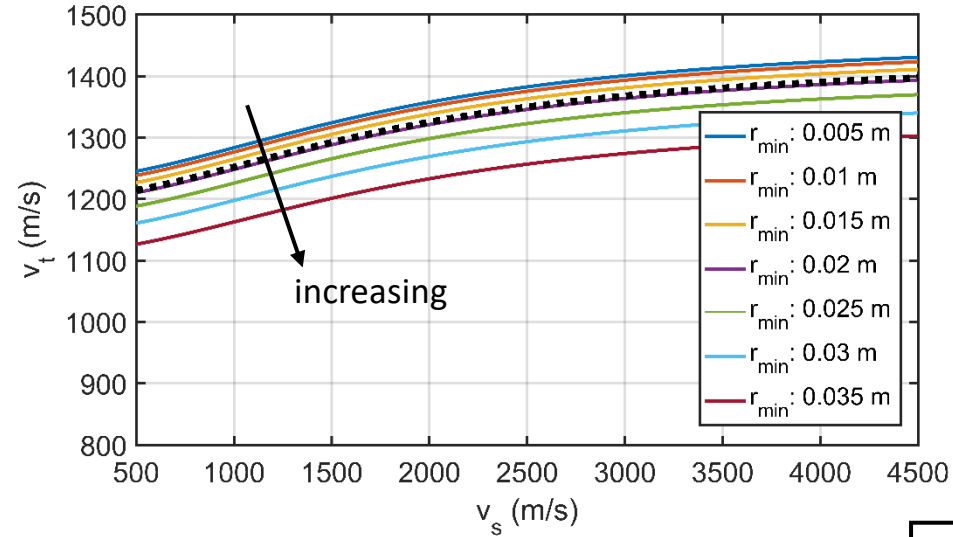
- Shallow well  $\Delta f = 20$  Hz
- Deep well  $\Delta f = 6$  Hz

# Sensitivity to different parameter

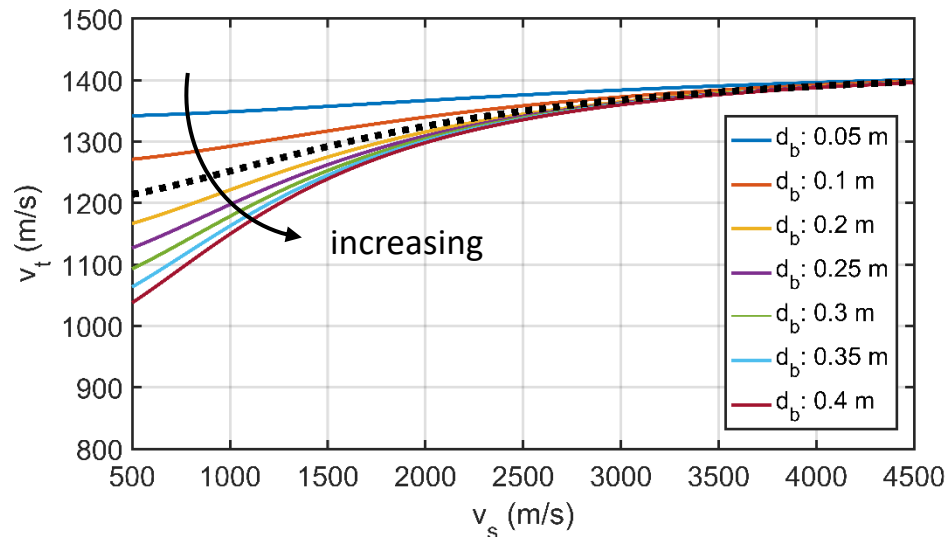
## Casing thickness



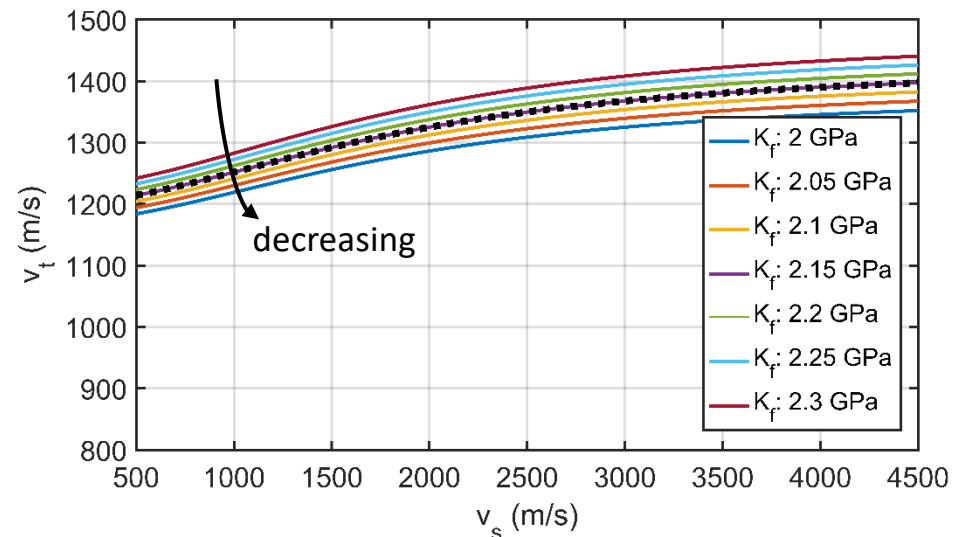
## Tool thickness



## Borehole thickness



## Bulk Modulus: borehole fluid



..... experimental result

- Geometry

- $r_{\min} = 0.035 \text{ m}$

- $r_{\max} = 0.07 \text{ m}$

- $d_{\text{cas}} = 0.0038 \text{ m}$

- $\eta = r_{\min}^2 / r_{\max}^2$

- $a = (r_{\max} - d_{\text{cas}}) / r_{\max}$

- Fluid  $\rightarrow$  Water

- $\rho_f = 1000 \frac{\text{kg}}{\text{m}^3}$

- $K_f = 2.15 * 10^9 \text{ Pa}$

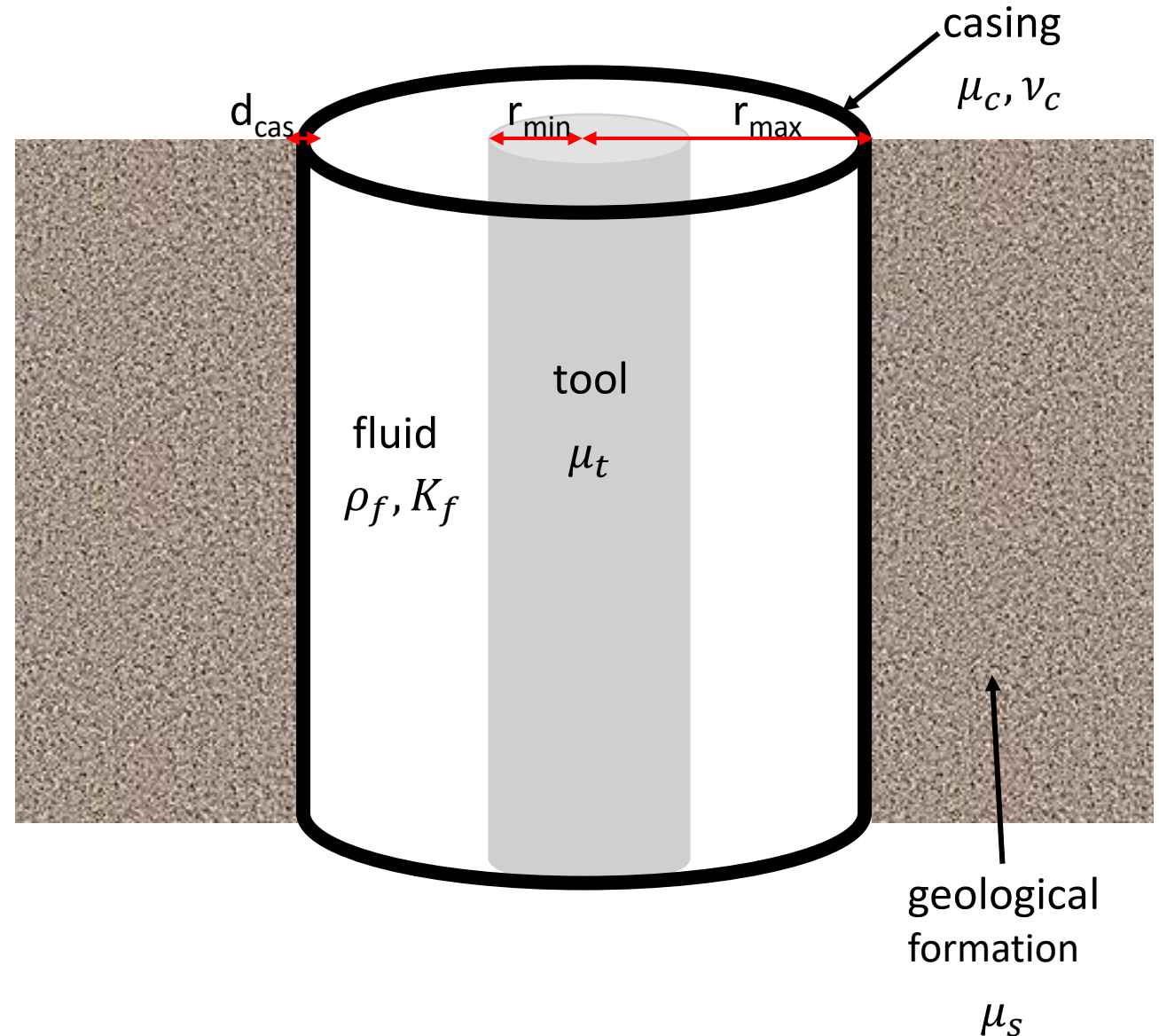
- Casing  $\rightarrow$  Steel

- $\mu_c = 77 * 10^9 \text{ Pa}$

- $\nu_c = 0.3$

- Logging tool  $\rightarrow$  Keflar

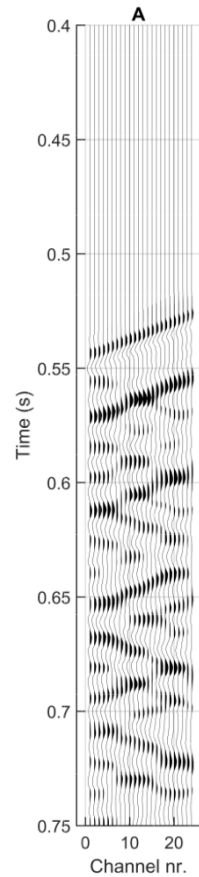
- $\mu_t = 2.9 * 10^9 \text{ Pa}$



# Measured and Modelled Data

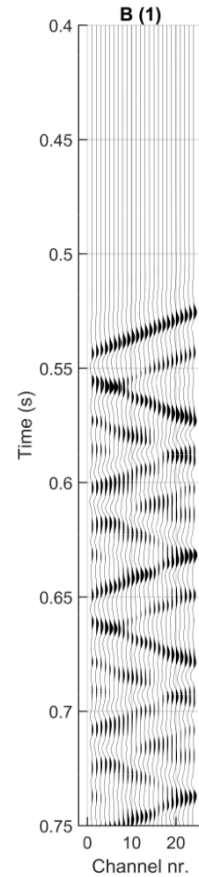
Recorded data:

- stacked
- f-k filtered

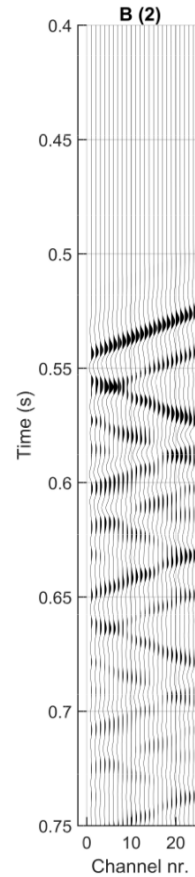


Model:

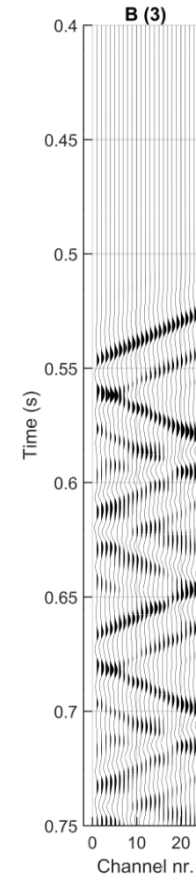
- tube wave starts at borehole head
- different velocities, reflection coefficients at bottom, no attenuation



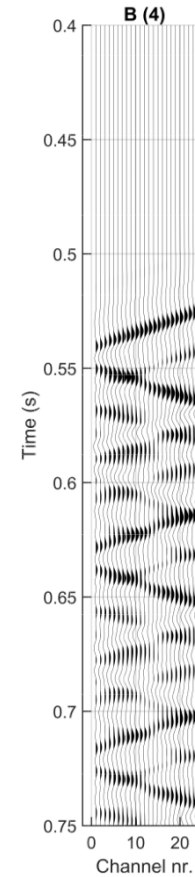
$$v_t = 1250 \frac{m}{s}, R_b = 0.9$$



$$v_t = 1250 \frac{m}{s}, R_b = 0.7$$



$$v_t = 1100 \frac{m}{s}, R_b = 0.9$$



$$v_t = 1500 \frac{m}{s}, R_b = 0.9$$



- Velocity of the tube wave is influenced by (Galperin, 1985)
  - **the borehole casing**
  - **elastic constants of surrounding formation**
  - elastic constants of drilling fluid
  - the logging tool
  
- Intensity of the tube wave is influenced by (Galperin, 1985)
  - contact between casing and formation, e.g. cementation - better coupling → higher intensity
  - density of the fluid - lower density → lower intensity
  - depth below water level - increasing depth → lower intensity
  - for Geophones: applied force for clamping the tool - higher force → lower intensity

# Vs change due to loading

## In soil

- Boussinesq's formula

$$\sigma_z = \frac{Q}{z^2} I_B$$

Boussinesq stress coefficient:

$$I_B = \frac{3}{2\pi} \frac{1}{\left(1 + \left(\frac{r}{z}\right)^2\right)^{\frac{5}{2}}}$$

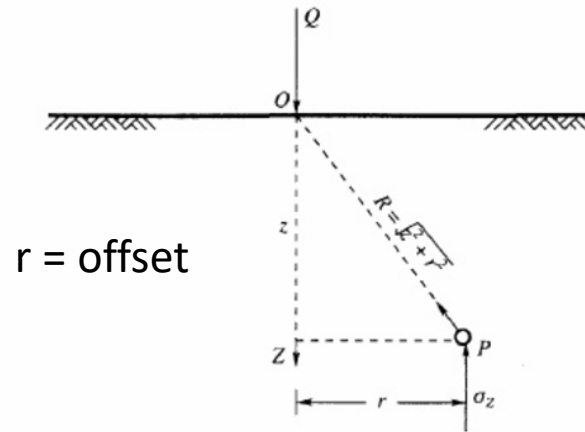
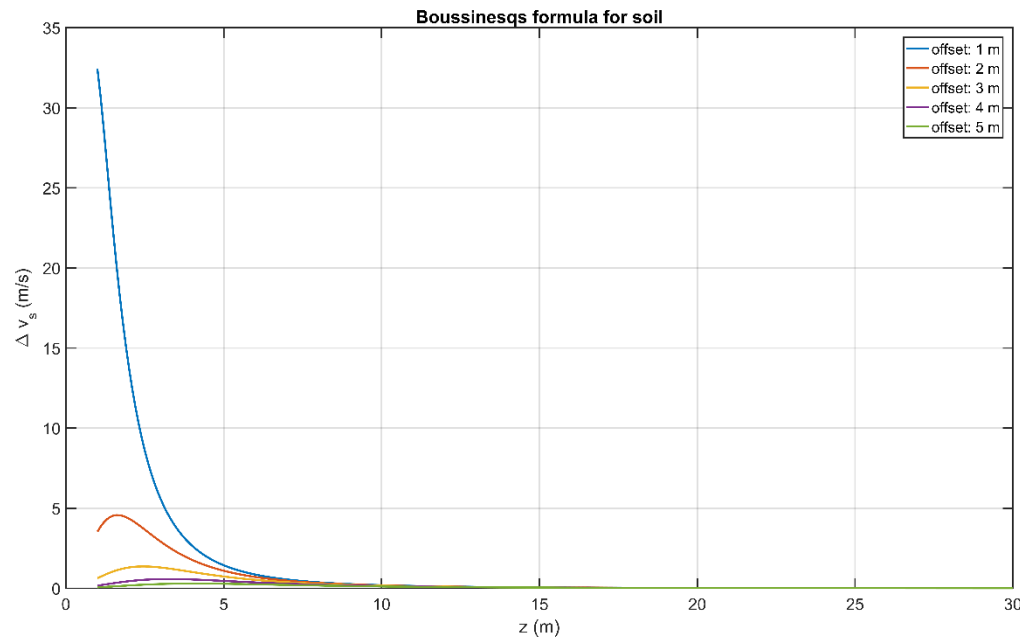


Figure 6.1 Vertical pressure within an earth mass



Force at surface:

- $m = 200000 \text{ kg}$
- $A = 100 \text{ m}^2$
- $g = 10 \text{ m/s}^2$

# Vs change due to loading

## In rocks

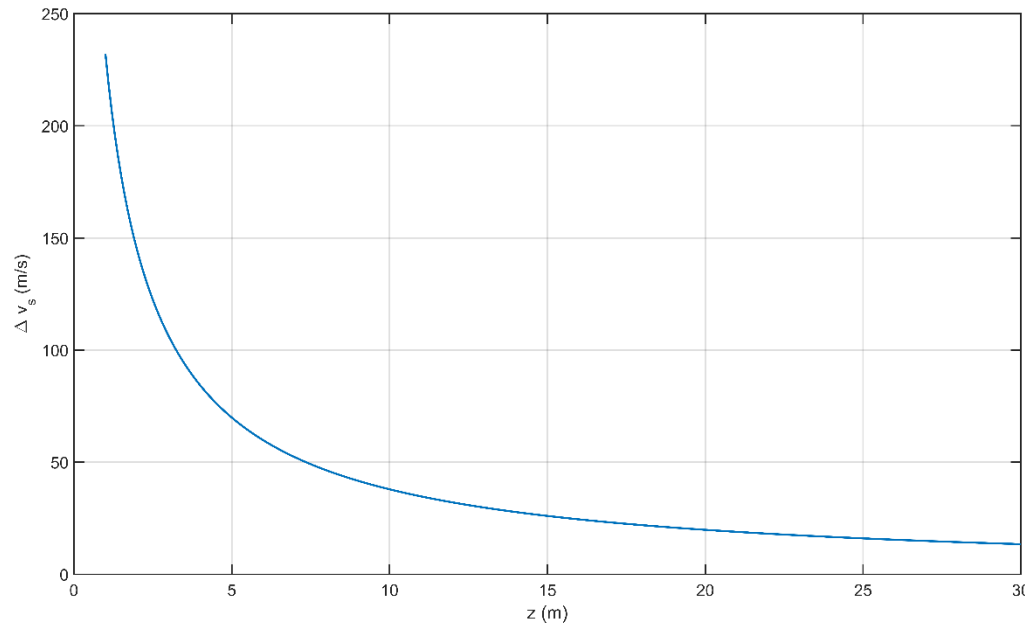
assuming  $v_s = v_{s0} * \left(\frac{P}{P_0}\right)^{\frac{1}{6}}$

$$P_0 = P_{lit} - P_{pore}$$

$$P = P_{lit} + P_{load} - P_{pore}$$

$$P_{lit} = \rho_r g z, \quad P_{pore} = \rho_f g z,$$

$$P_{load} = \frac{m g}{A}$$



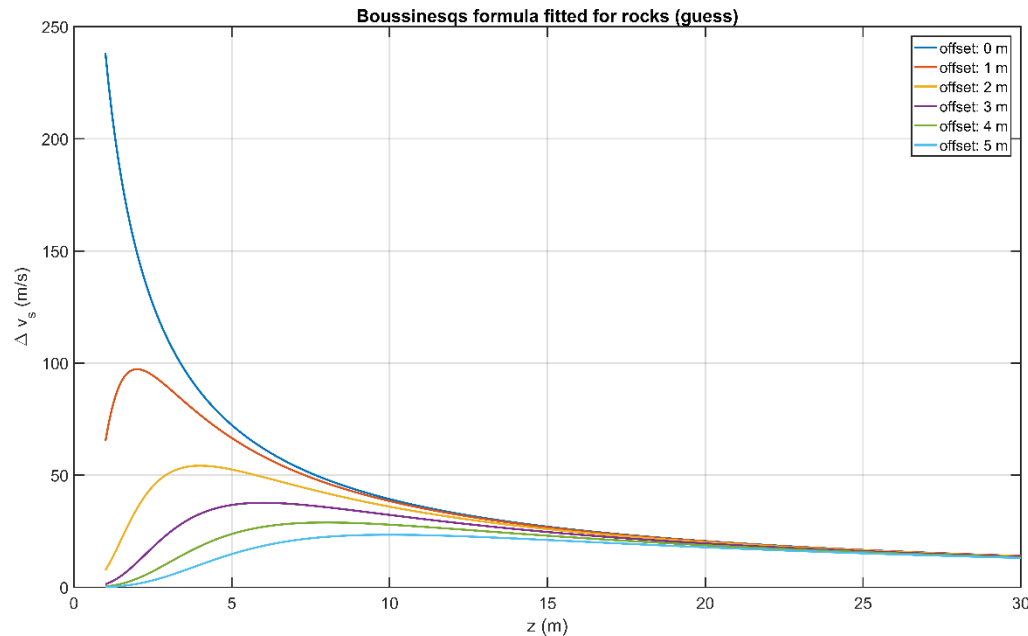
Force at surface:

- $m = 200000 \text{ kg}$
- $A = 100 \text{ m}^2$
- $g = 10 \text{ m/s}^2$

## In rocks

- Modified guess of Boussinesq's formula

$$P_{load} = P_{surface} I_2$$
$$I_2 = \frac{1}{\left(1 + \left(\frac{r}{z}\right)^2\right)^{\frac{5}{2}}}$$



Force at surface:

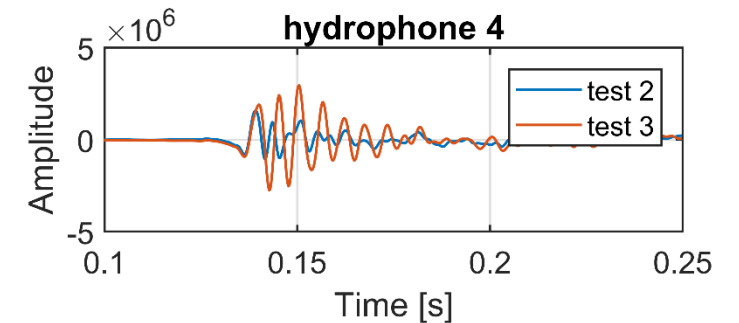
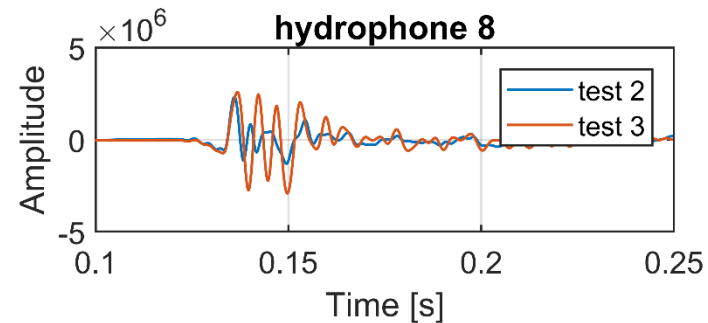
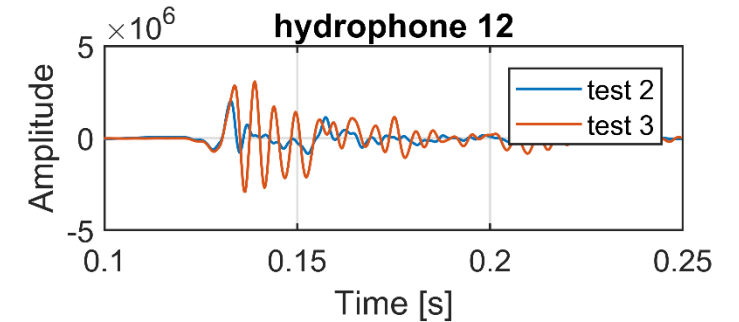
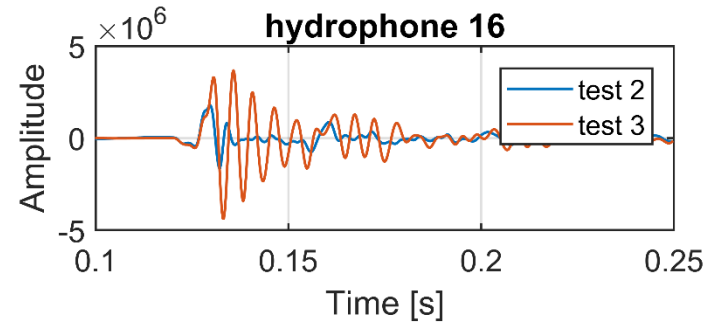
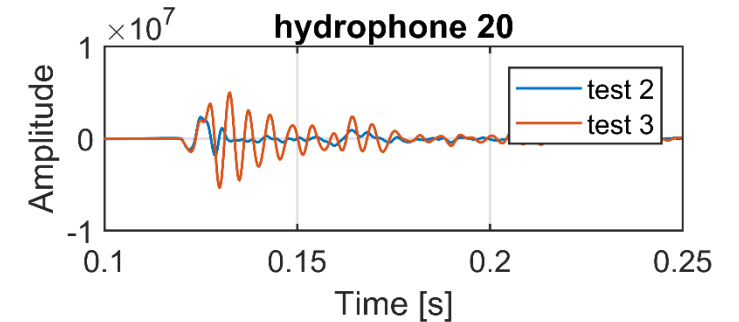
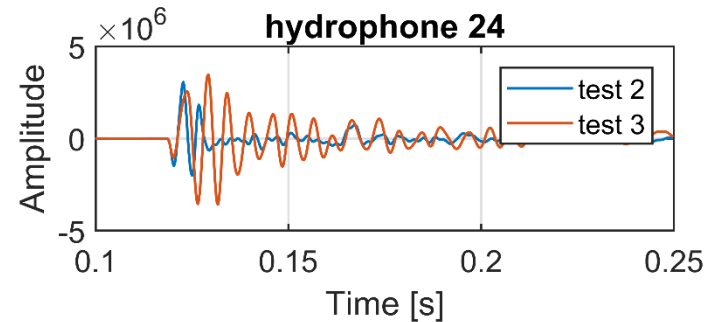
- $m = 200000 \text{ kg}$
- $A = 100 \text{ m}^2$
- $g = 10 \text{ m/s}^2$



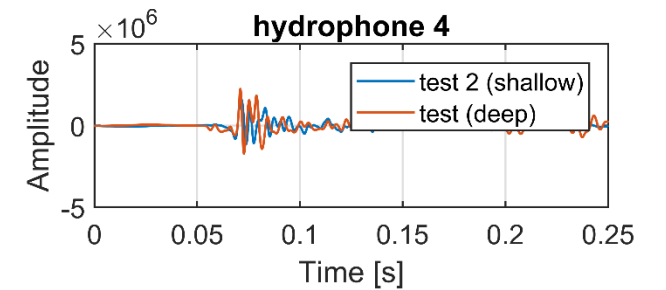
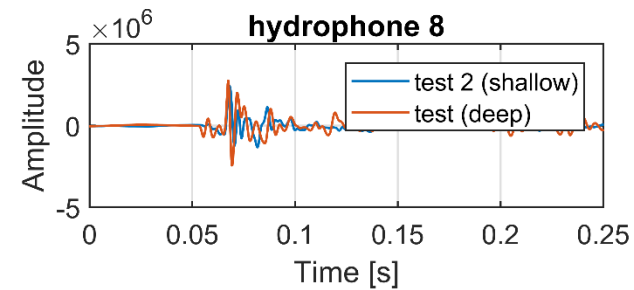
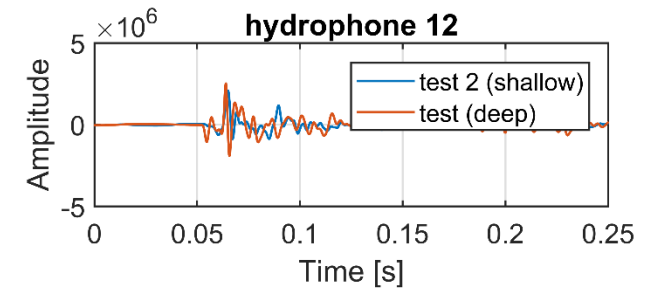
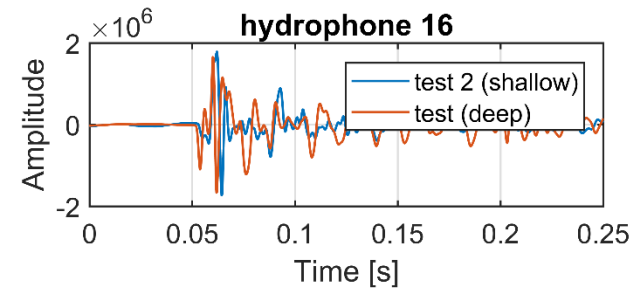
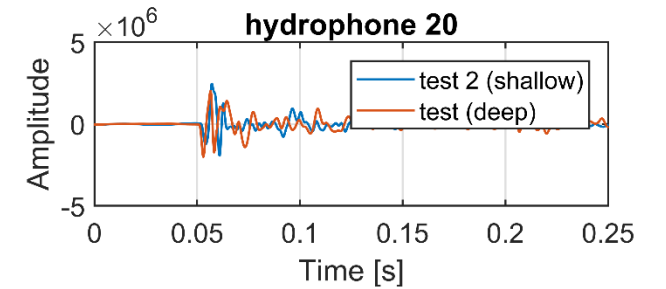
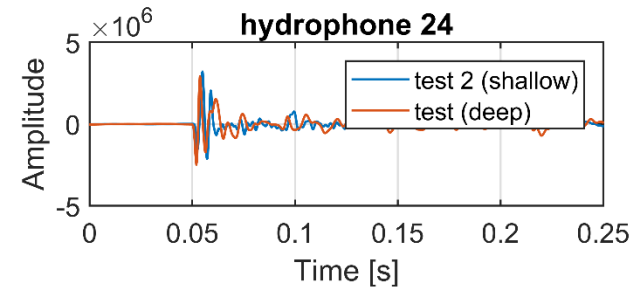
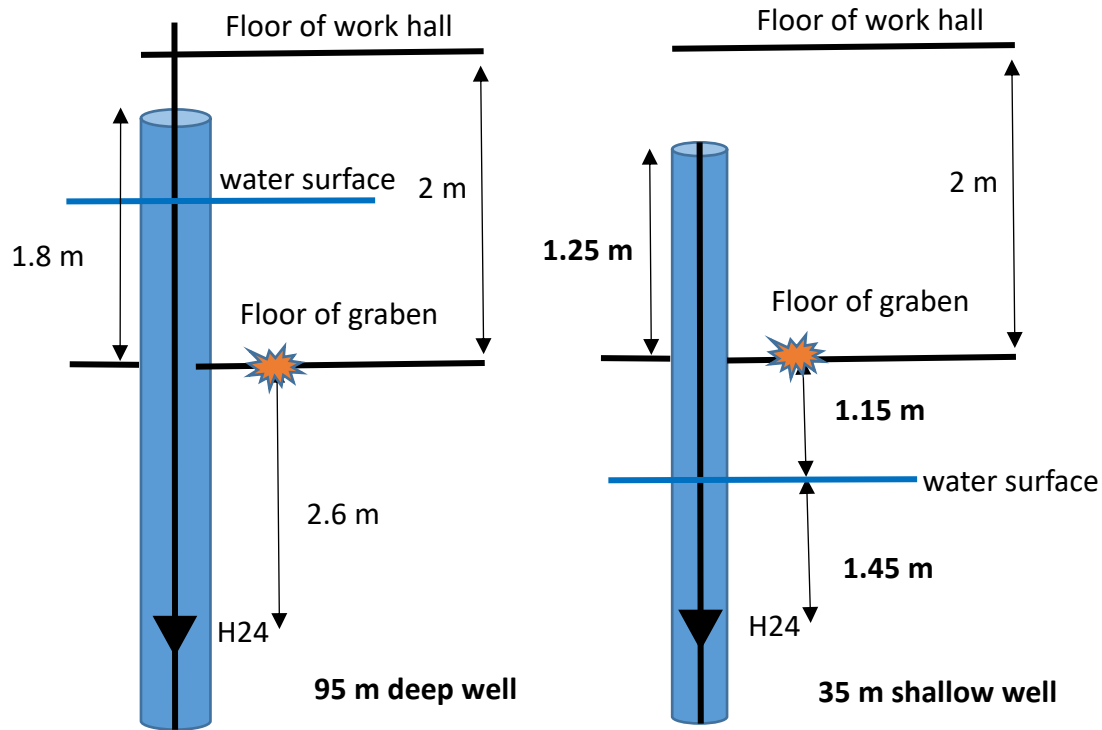
$$\Delta v_s = \pm 20 - 30 \frac{\text{m}}{\text{s}}$$

# 1. Holding construction of hydrophone array

- holding board: “seals” the well and more energy is kept inside the borehole (test 3)
- holding metal frame: nearly open to the top of the borehole (test 2)

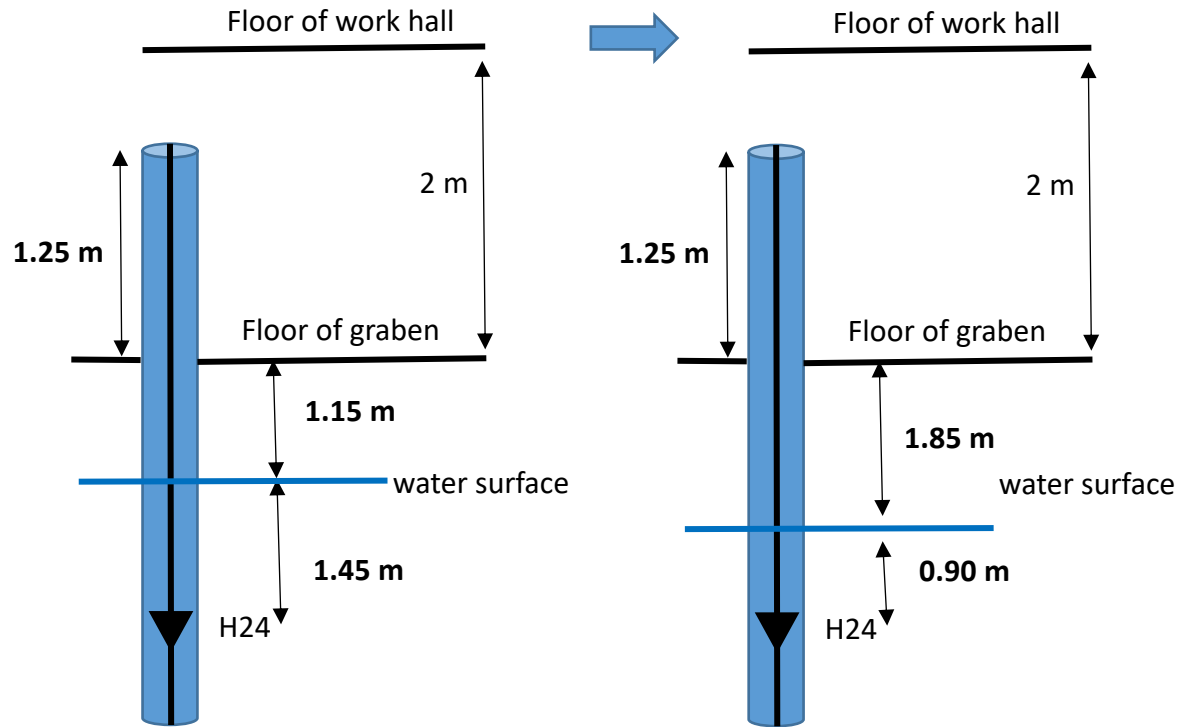


# 2. Position of water table in well



- different interaction of first downgoing tube wave and ghost reflection in shallow and deep well

# 3. Variation of water table position



Effective pressure change of 0.01 Mpa

$$\Delta p_e = (\rho_r - \rho_f) * g * \Delta z$$

$\Delta z$  = difference in water table

→ max. 0.1 % velocity change (1.2 m/s in  $v_S$ )  
(Hertz-Mindlin)

Effective pressure change of 0.01 Mpa

$$\Delta p_e = (\rho_r - \rho_f) * g * \Delta z$$

$\Delta z$  = difference in water table

different for near surface soils/unconsolidated rocks???

# 4. Radial position of hydrophone array

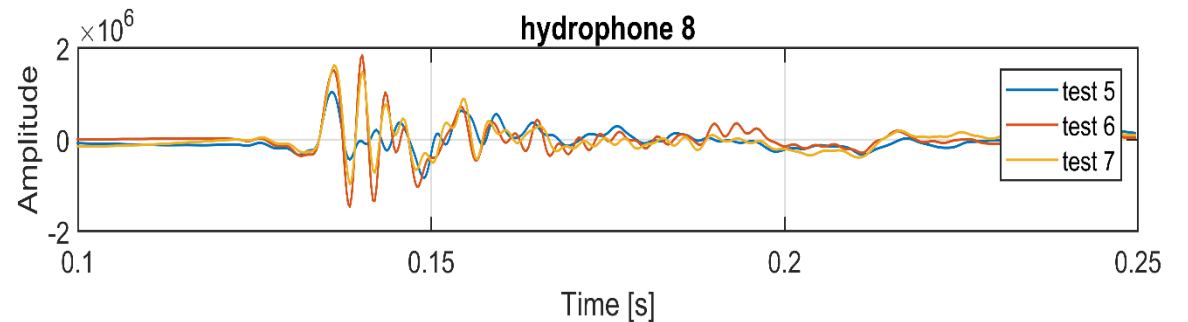
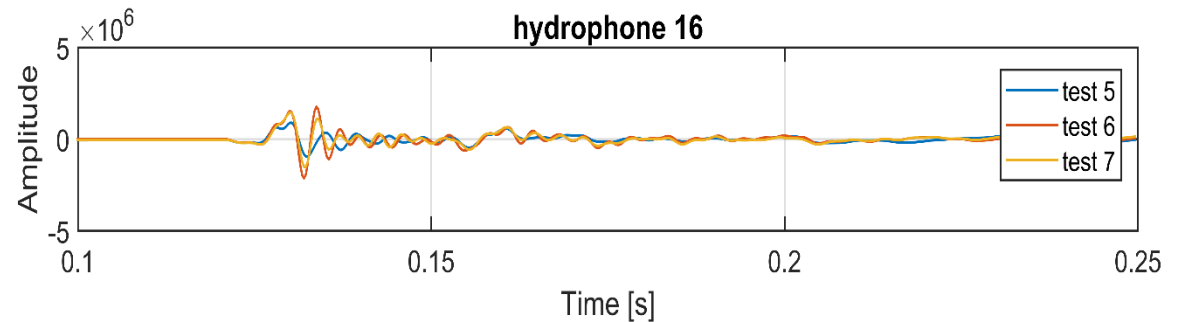
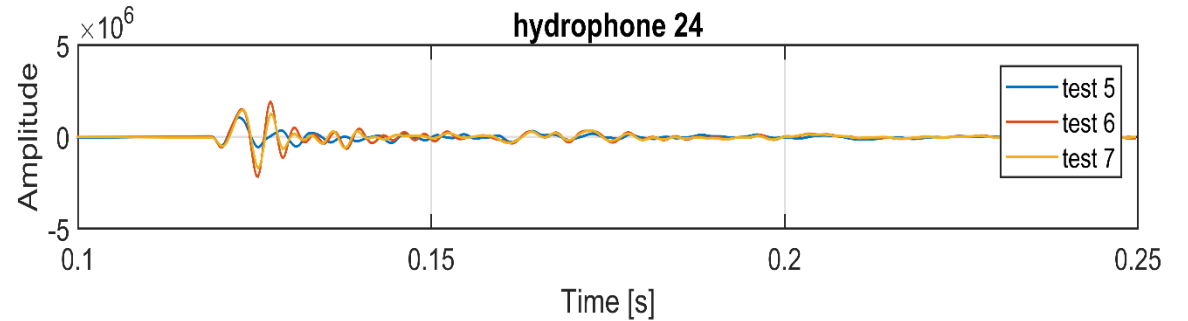


not centered



centered

- change of wave form, interference with other waves for different hydrophone positions → impact on velocity estimation in  $fk$ -domain
- should not cause a change of the tube wave velocity (Norris, 1990)



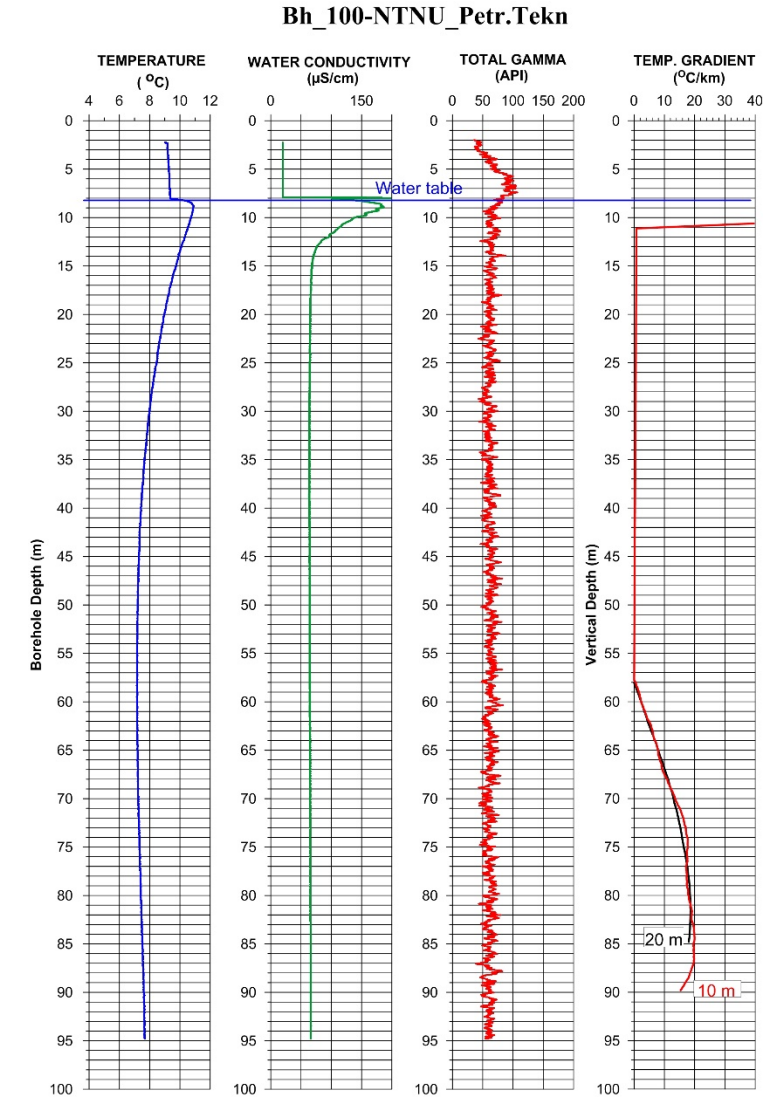
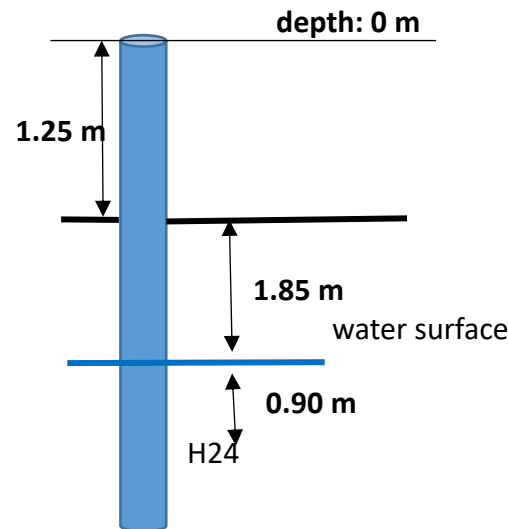
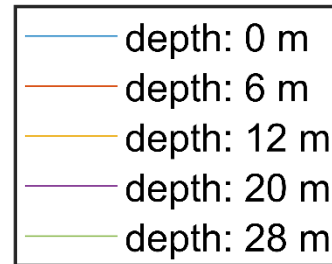
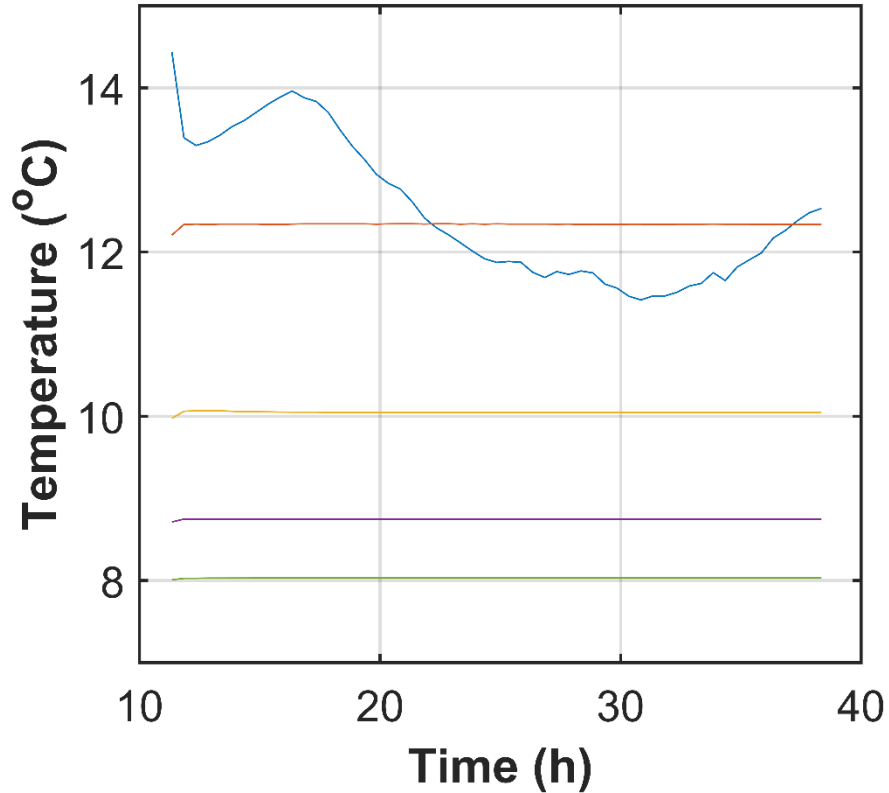
- Test 5: not centered
- Test 6,7 : centered



# 5. Temperature effect

Deep well: 22.11.2016

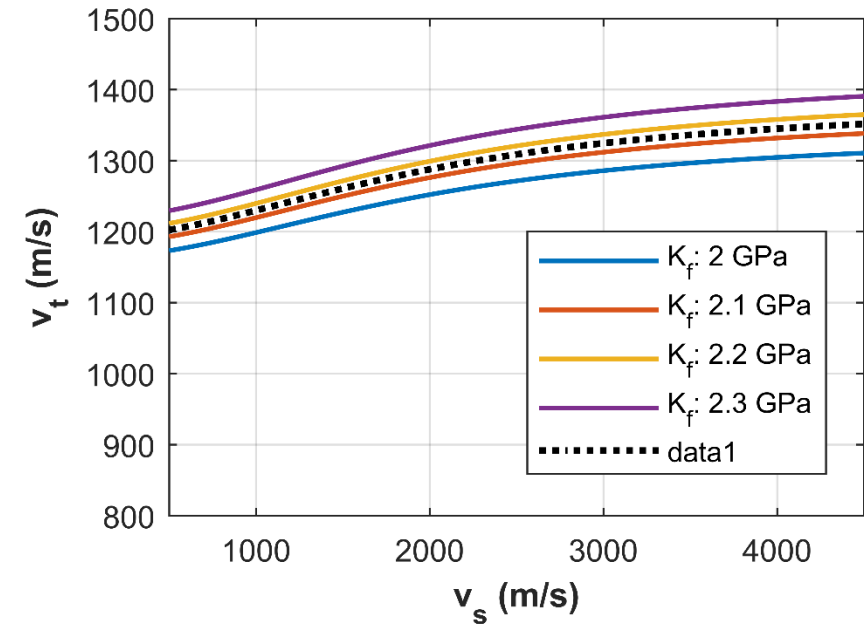
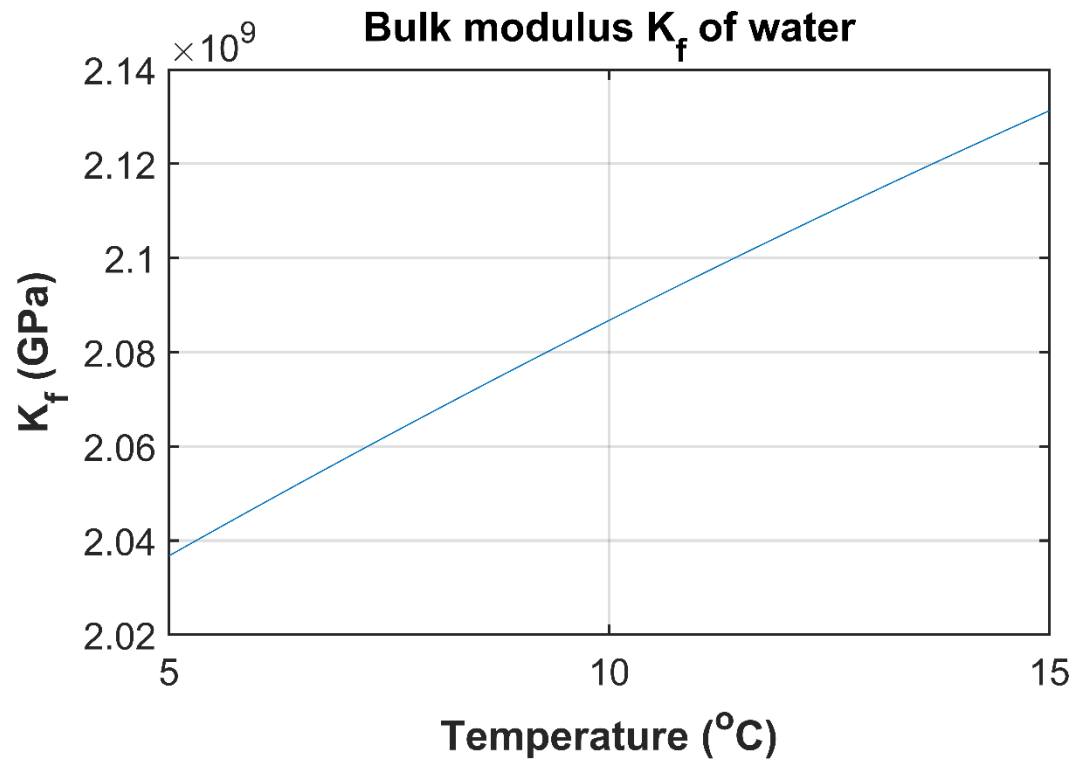
16<sup>th</sup> - 17<sup>th</sup> March 2018,  $t_0 = 11:20$



# 5. Temperature effect

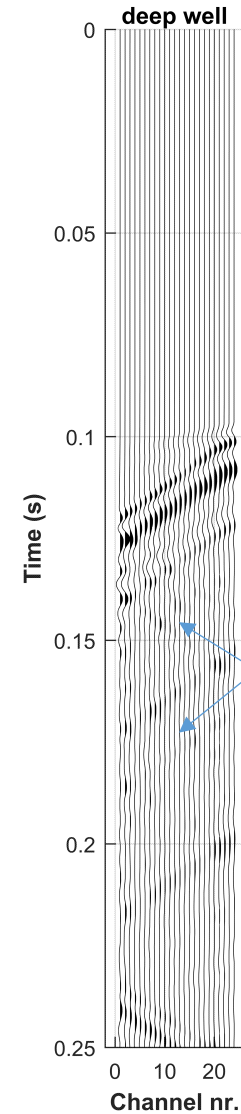
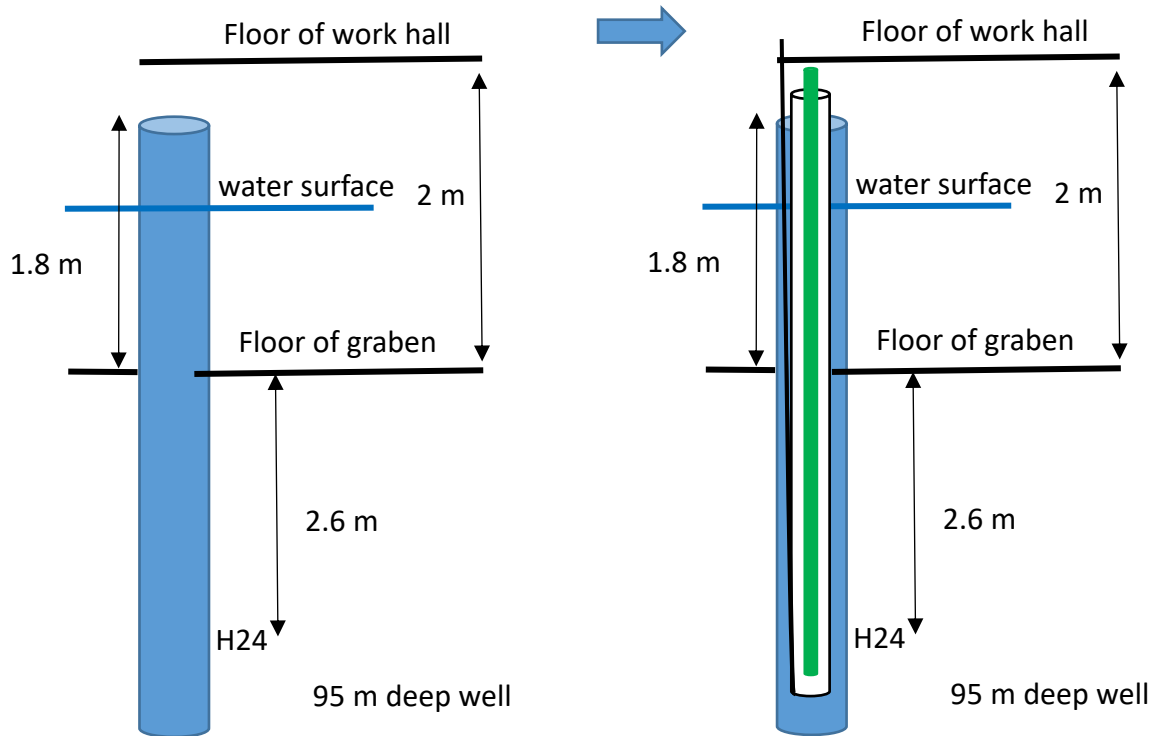
Dixon, 2007:

$$K_f = 2.29 * 10^9(1 - 48 * 10^{-6}(T - 53)^2)$$



# 6. Interaction with second well/near field effect

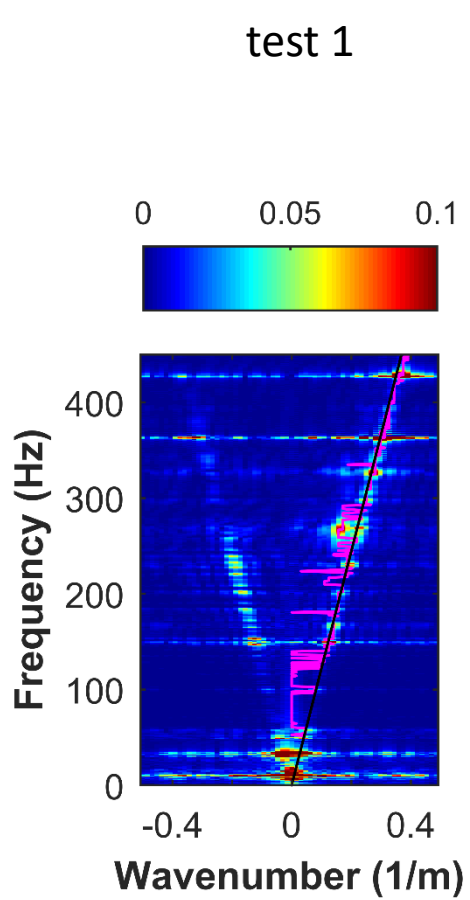
Tool installed in deep well



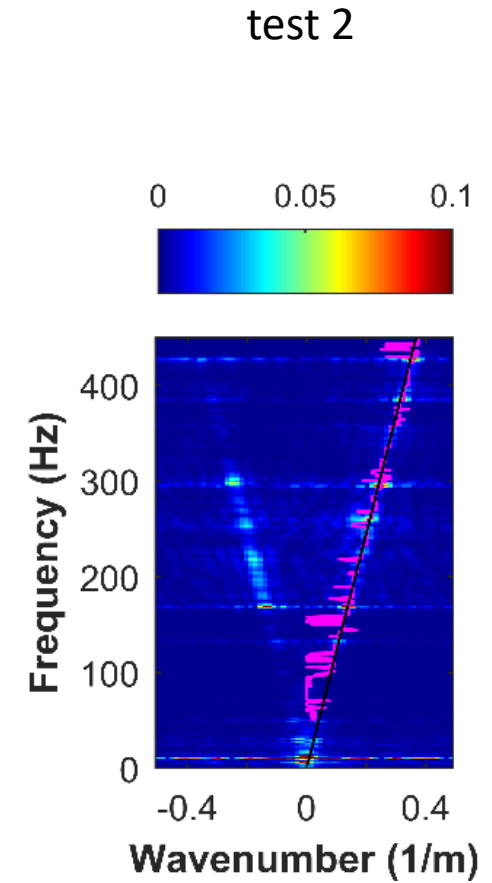
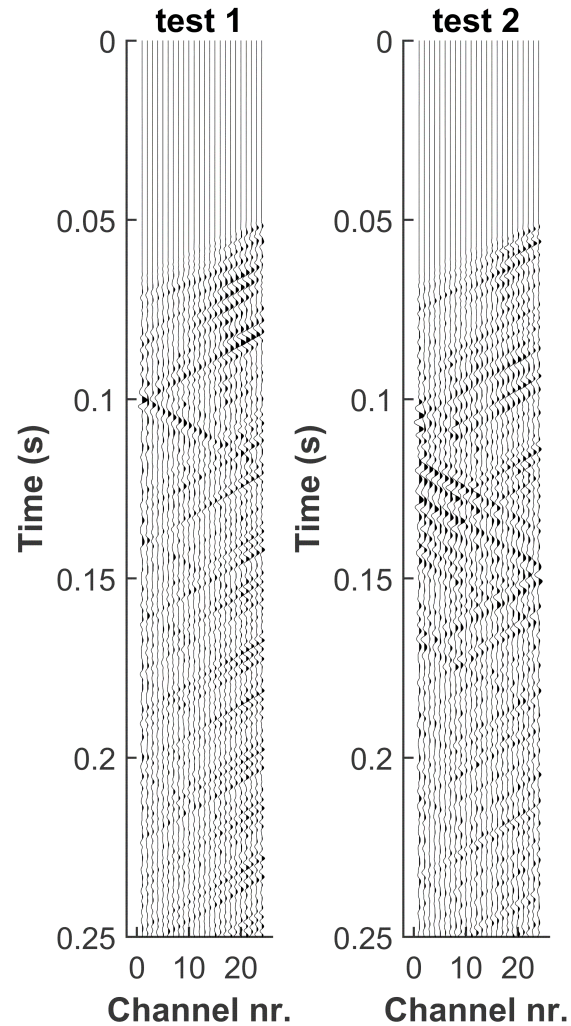
- hydrophones in deep well also show upgoing waves earlier than first bottom reflection
  - is recording in deep well impacted by shallow well and vice versa?

# 6. Interaction with second well

Frequencies between 50 – 450 Hz are used



$1224.5 \pm 3.3$  m/s



$1225.7 \pm 4.2$  m/s

# 7. Background noise (surface waves)

