

Recursive estimation of reflectivity by minimum-delay seismic trace decomposition

Milton J. Porsani

Centro de Pesquisa em Geofísica e Geologia (CPPG/UFBA) and National
Institute of Science and Technology of Petroleum Geophysics (INCT-GP/CNPQ).

Bjorn Ursin

The Norwegian University of Science and Technology, (NTNU)
Department of Petroleum Engineering and Applied Geophysics

Michelângelo G. Silva

Centro de Pesquisa em Geofísica e Geologia (CPPG/UFBA)

- By estimating a minimum-delay wavelet for each time-sample position of the seismic trace,
- Gives a decomposition of the seismic trace as a sum of minimum-delay wavelets.
- The data vector is equal to a wavelet matrix, which is lower triangular with elements 1 on the diagonal, multiplied by the seismic reflectivity vector.
- Recursive solution of this equation provides an estimate of reflectivity.

SEISMIC TRACE DECOMPOSITION

We consider a seismic trace $d(t), t = 0, 1, \dots, L$, and choose a data window $d(k + j), j = 0, 1, \dots, L_d$. The local auto-correlation function is

$$R_k(\tau) = \sum_j d(k + j)d(k + j + \tau), \quad \tau = 0, 1, \dots, L_d$$

From this we use the Levinson (1947) algorithm to compute a damped spiking filter (Robinson, 1967)

$$[R_k(\tau) + \lambda^2 \delta_\tau] * g_k(\tau) = \sigma^2 \delta_\tau$$

The inverse of the spiking filter is a minimum-delay wavelet computed directly from

$$g_k(t) * w_k(t) = \delta_t \quad w_k(t) = \begin{cases} 1 & t = 0 \\ 0 & t > L_w \end{cases}$$

This can be written in vector-matrix notation as

$$\begin{pmatrix} d(0) \\ \vdots \\ \vdots \\ \vdots \\ d(L) \end{pmatrix} = \begin{pmatrix} 1 & 0 & 0 & 0 & 0 \\ w_0(1) & 1 & 0 & 0 & 0 \\ \vdots & \ddots & \ddots & 0 & 0 \\ w_0(L_w) & \ddots & \ddots & 1 & 0 \\ 0 & \ddots & \ddots & w_{L-1}(1) & 1 \end{pmatrix} \begin{pmatrix} r_0 \\ \vdots \\ \vdots \\ \vdots \\ r_L \end{pmatrix}$$

$$\mathbf{d} = \mathbf{W}\mathbf{r} \quad (1)$$

TIME-VARYING DECONVOLUTION

In time-varying deconvolution we compute and apply a different filter for each time sample.

$$\hat{r}_k = \sum_{\tau} d(t - k - \tau)g_k(\tau)$$

This can be written

$$\begin{pmatrix} \hat{r}(0) \\ \vdots \\ \hat{r}(L) \end{pmatrix} = \begin{pmatrix} 1 & 0 & 0 & 0 & 0 \\ g_1(1) & 1 & 0 & 0 & 0 \\ \vdots & \ddots & \ddots & 0 & 0 \\ \ddots & \ddots & \ddots & 1 & 0 \\ 0 & g_L(L_f) & \ddots & g_L(1) & 1 \end{pmatrix} \begin{pmatrix} d_0 \\ \vdots \\ d_L \end{pmatrix}$$

$$\hat{\mathbf{r}} = \mathbf{G}\mathbf{d} \quad (2)$$

COMPARISON

Combining eq. (1) and (2) we obtain

$$\hat{\mathbf{r}} = \mathbf{G}\mathbf{W}\mathbf{r} \quad (3)$$

The matrix $\mathbf{F} = \mathbf{G}\mathbf{W}$ is also lower triangular with elements 1 on the diagonal. It is, however, different from the identity matrix, so that the two estimates of reflectivity are different.

From equation (1) we have

$$\mathbf{r} = \mathbf{W}^{-1}\mathbf{d}$$

The lines of inverse matrix can now be considered as time-varying filter impulse responses. They are, however, not necessarily minimum delay.

The new process is a decomposition of the seismic trace in minimum delay wavelets.

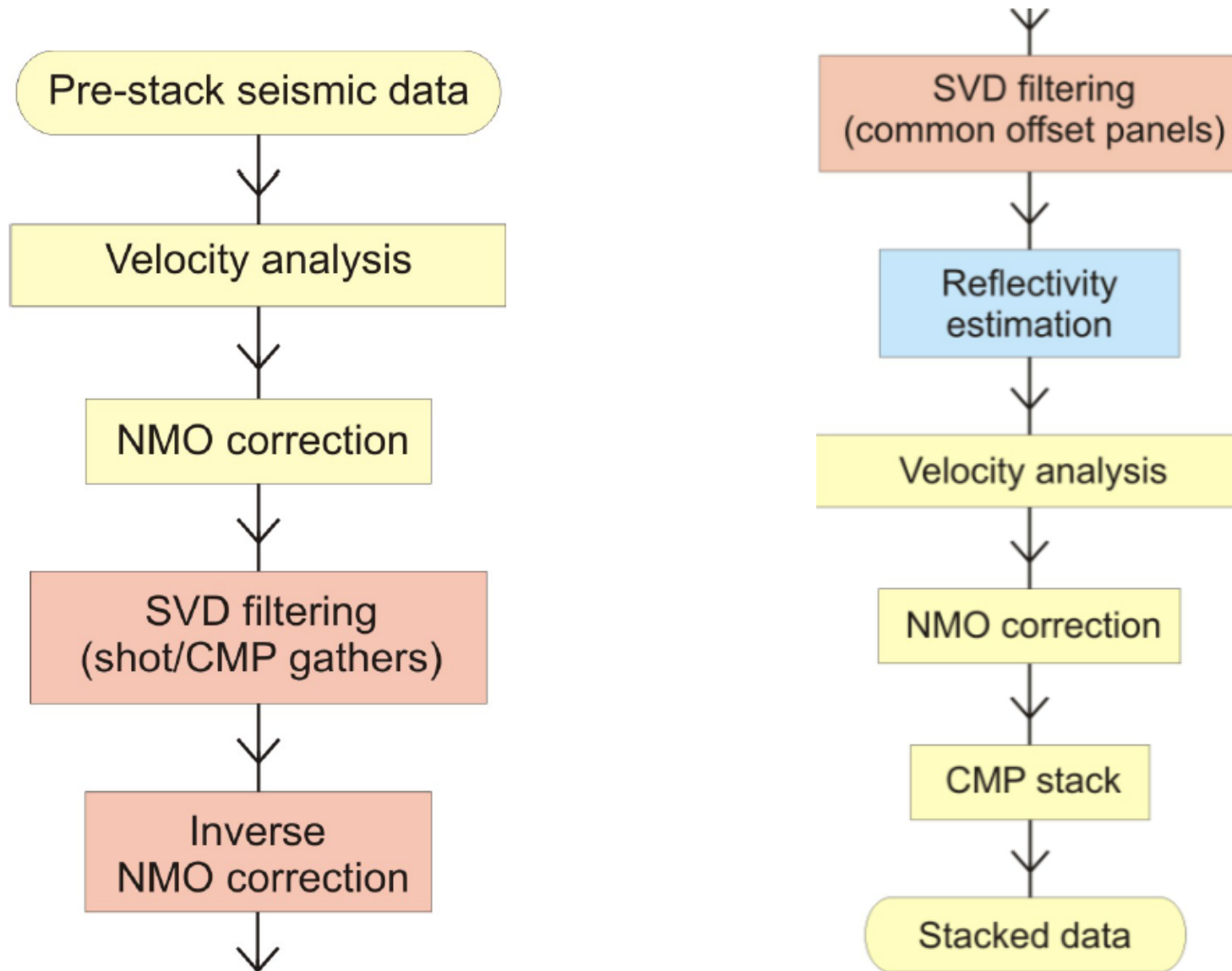
The recursive estimate of the reflectivity may also be considered to be the output of a mixed-delay time-varying filtering procedure.

LAND DATA PROCESSING EXAMPLE

Land seismic line from the Tacutu basin,
located in the North-east of Brazil

- 179 shots recorded at 4 ms sampling interval
- 96 channels per shot
- split-spread geometry with offsets from -2.500 m to -150 m and 150 m to 2.500 m and 200 m
- The distance between the shots is 200 m, giving a low CMP coverage of 12 fold

Flowchart of the seismic data processing:



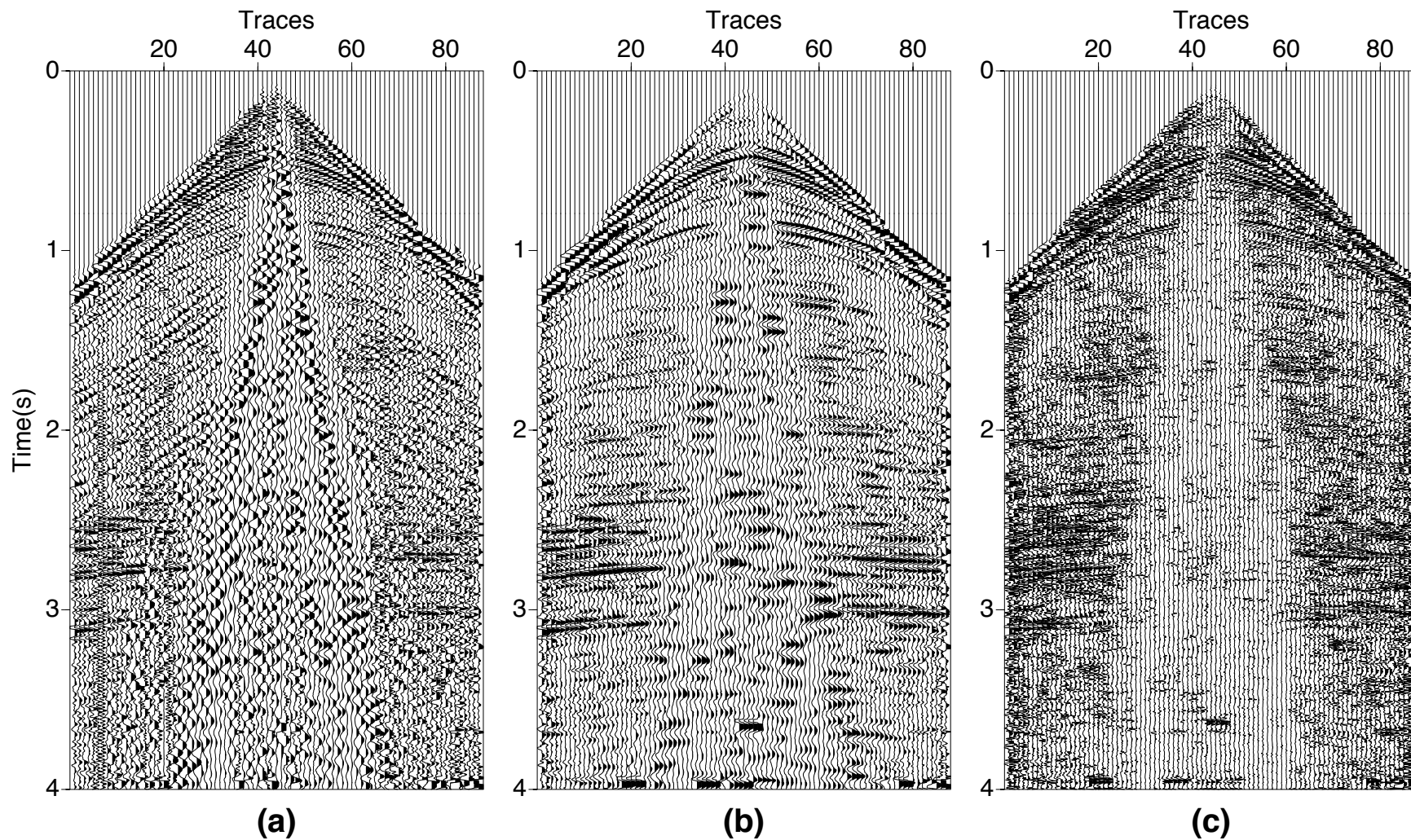
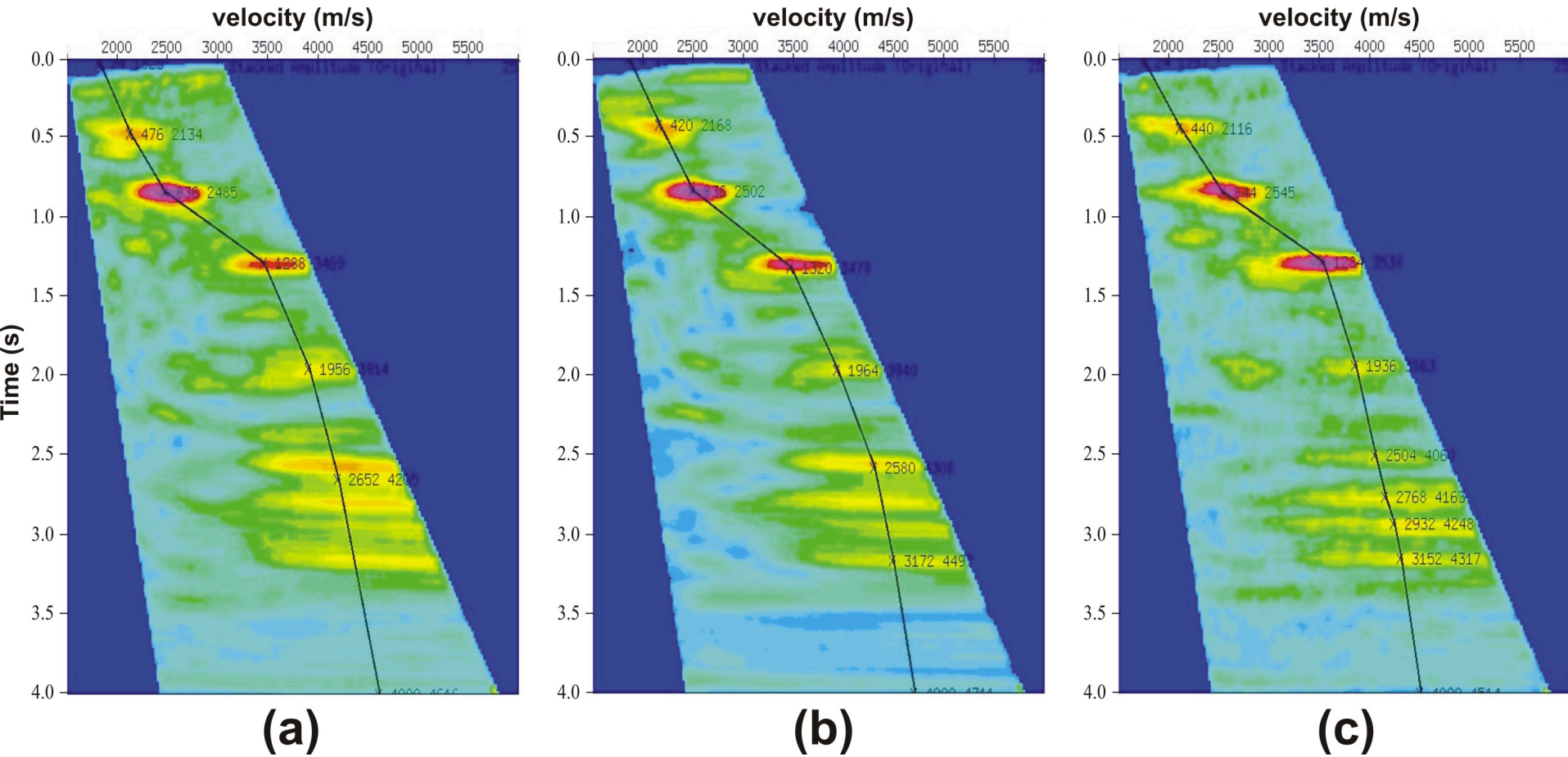
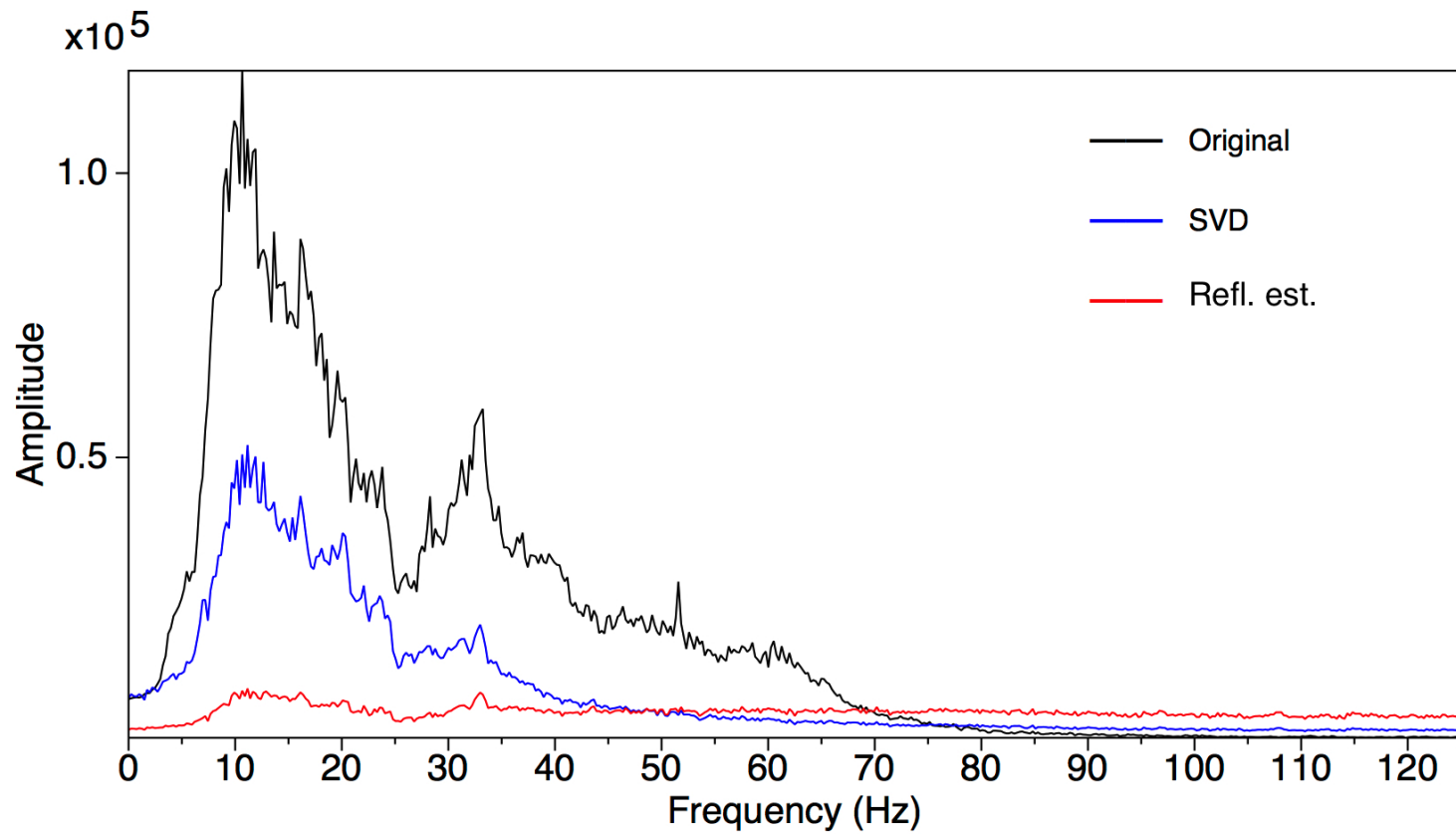


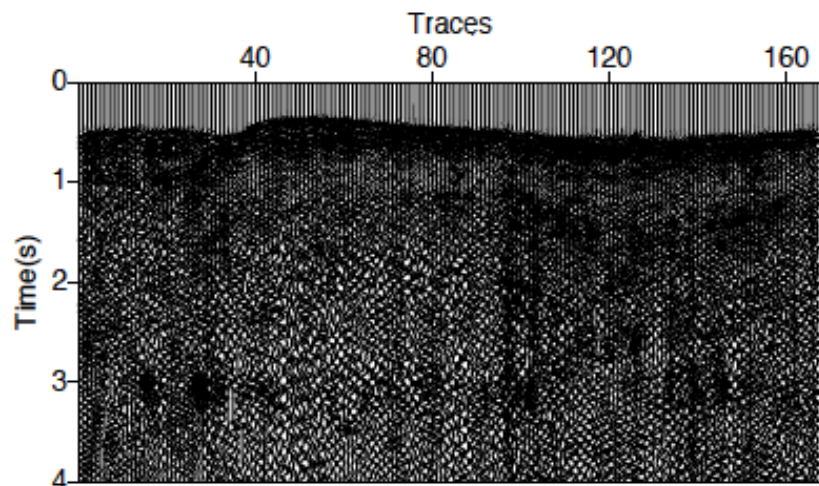
Figure 2: Comparison of SVD and reflectivity estimation filtering of a shot gather. Input data in (a), after SVD filtering (b) and after SVD filtering followed by recursive reflectivity estimation (c).



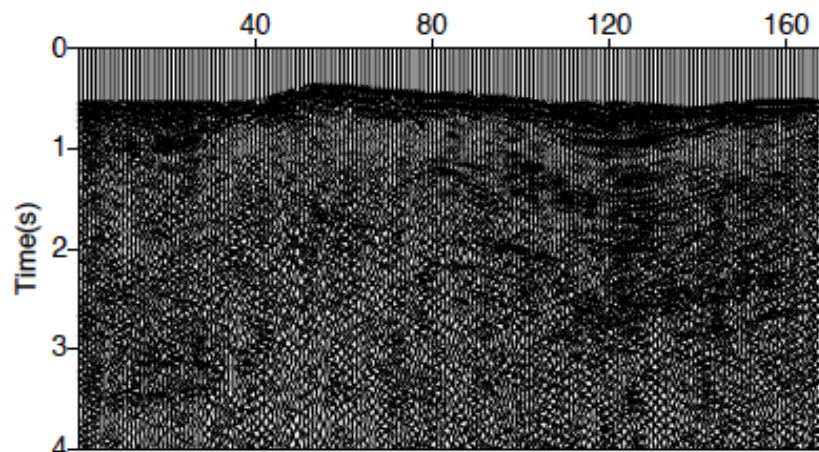
Velocity analysis plots corresponding to the three gathers in Fig. 2 with matching (a), (b), and (c).



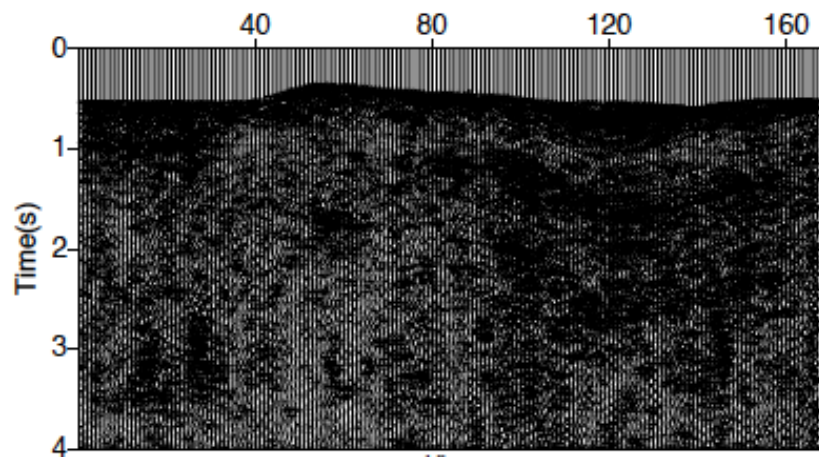
Average amplitude spectrum of the shot gathers in Fig. 2.



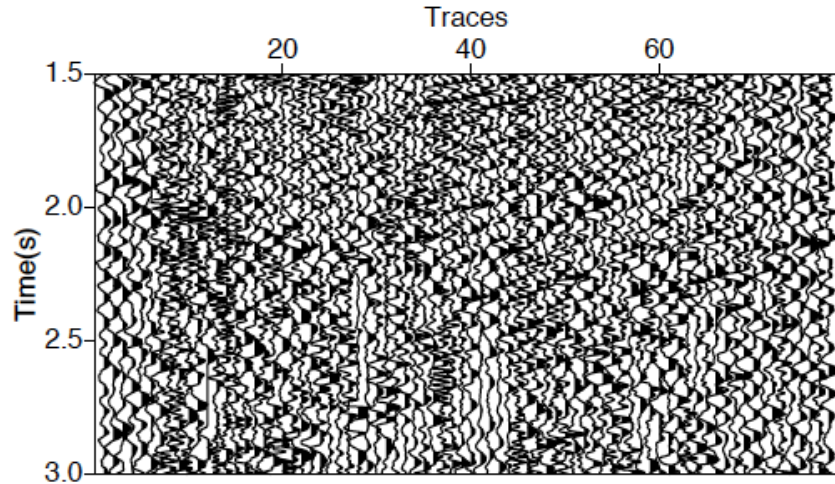
A common-offset panel
at 2050m



After SVD filtering

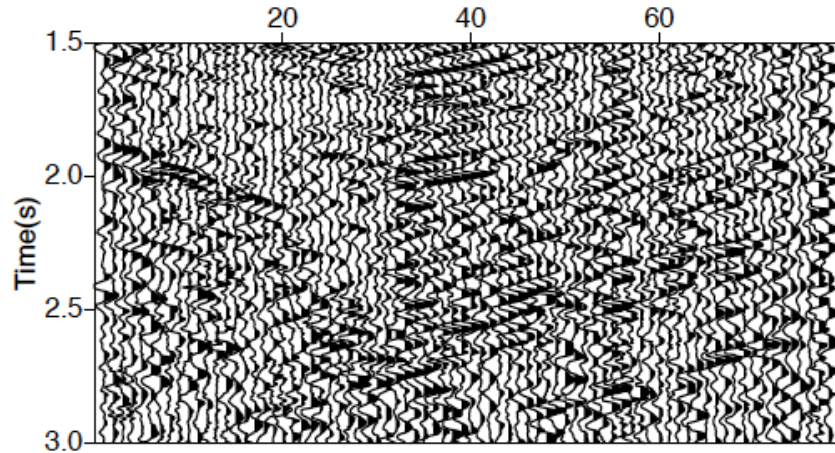


After SVD filtering followed
by reflectivity estimation

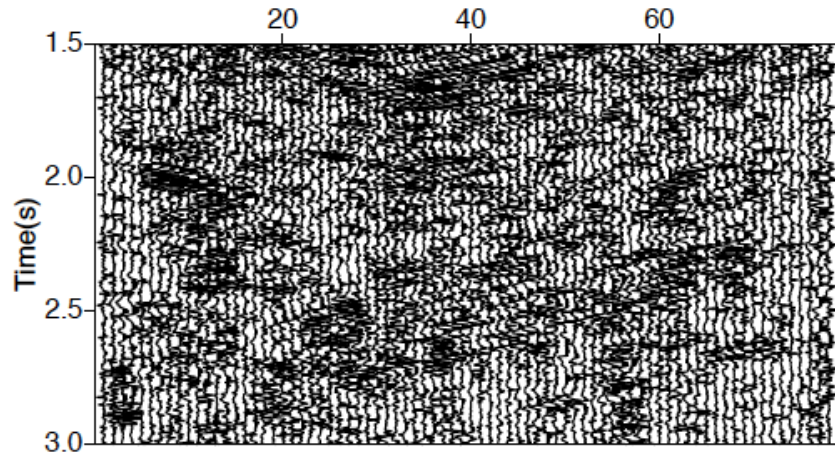


Detail of a common-offset panel

A common-offset panel at 2050m



After SVD filtering



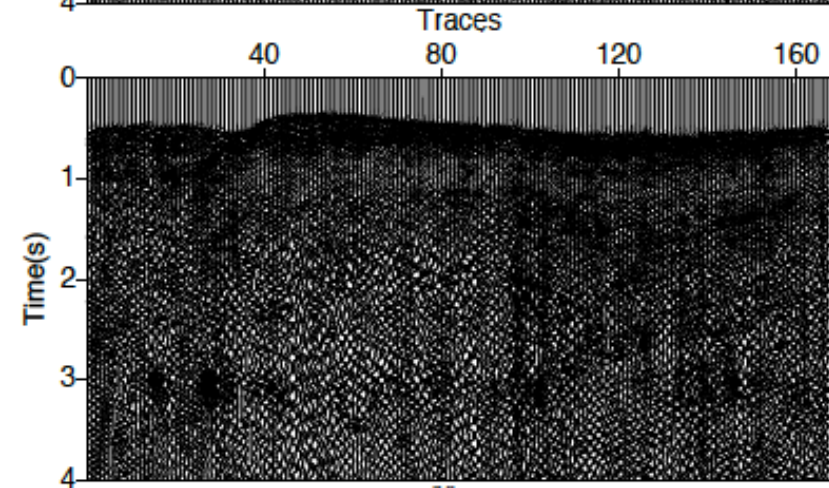
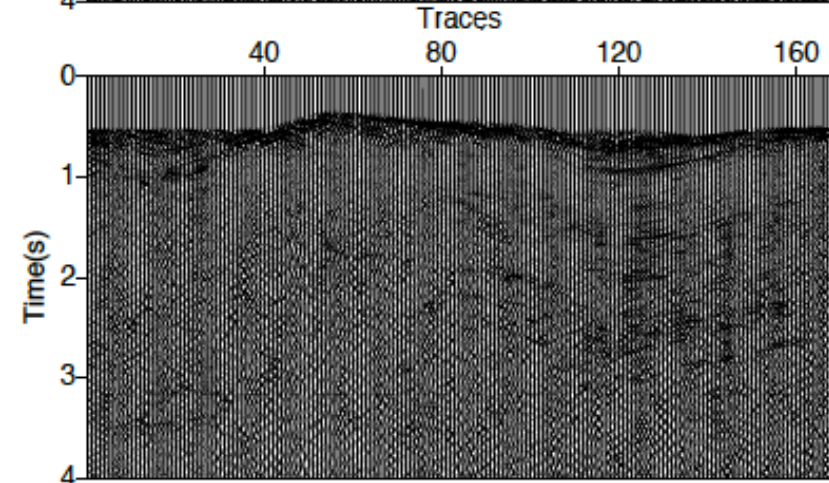
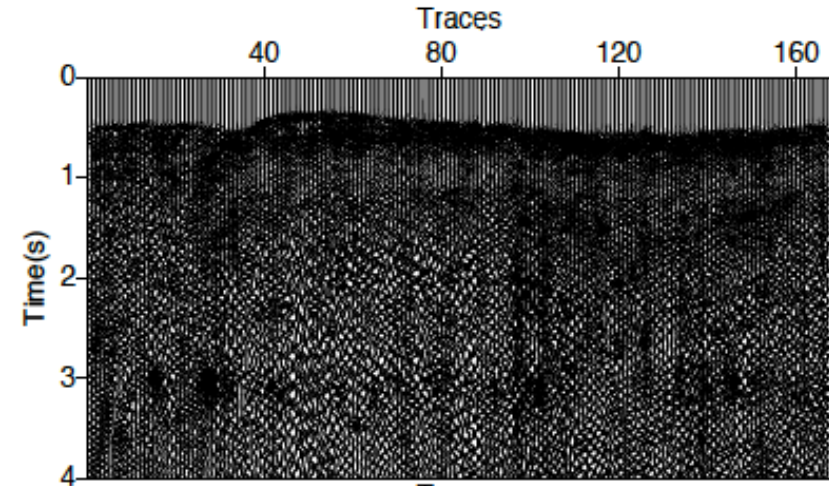
After SVD filtering followed by
reflectivity estimation

Removed noise in common offset panels

After SVD filtering

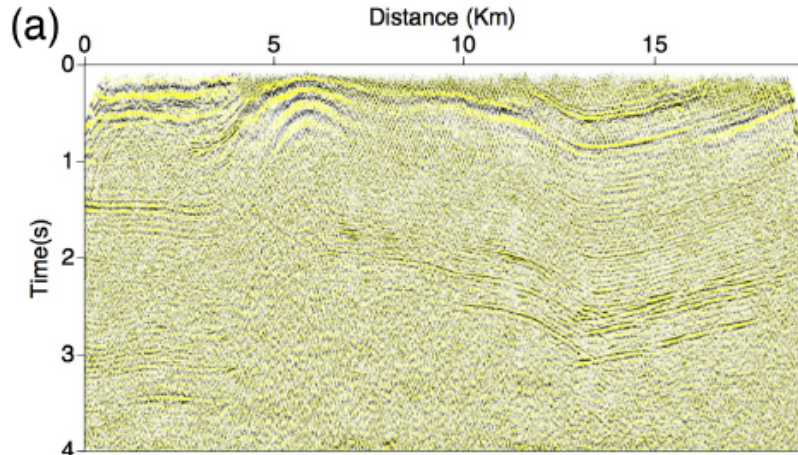
Additional noise removed by
reflectivity estimation

Total removed noise after SVD filtering
followed by reflectivity estimation

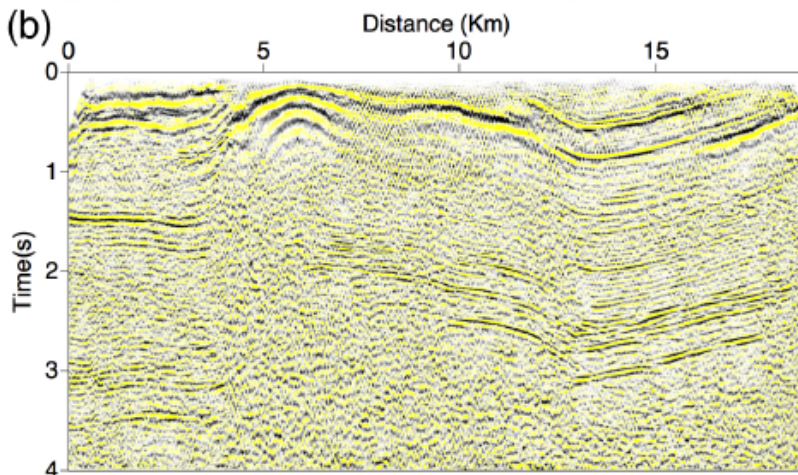


Stacked sections

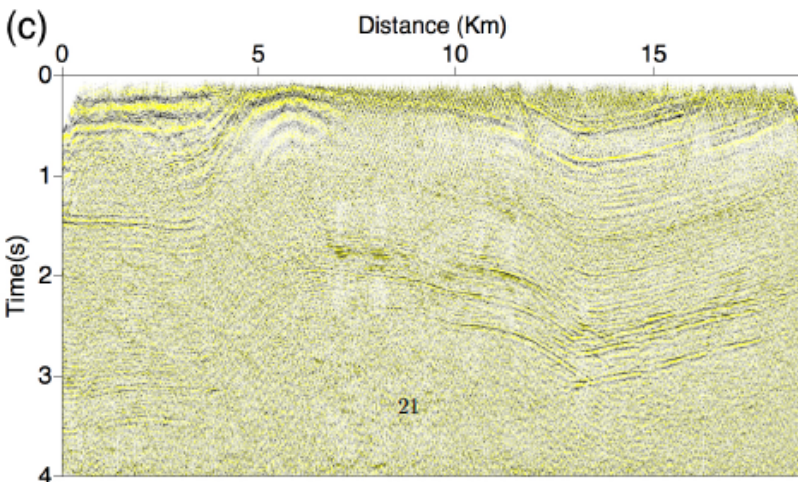
Original data



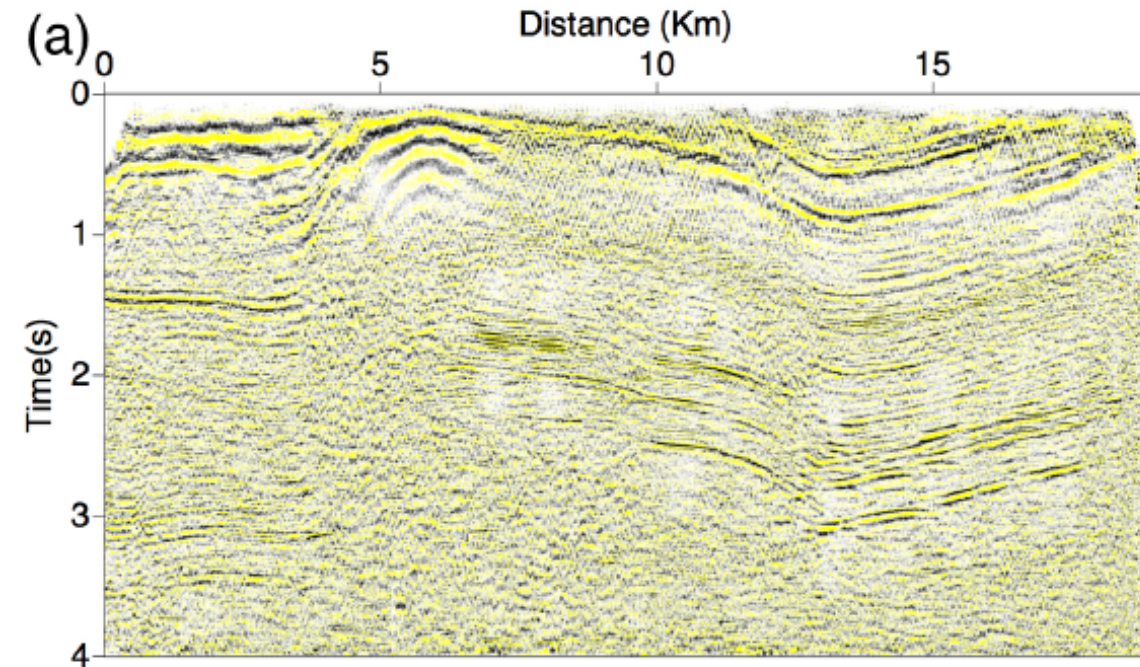
After adaptive SVD filtering



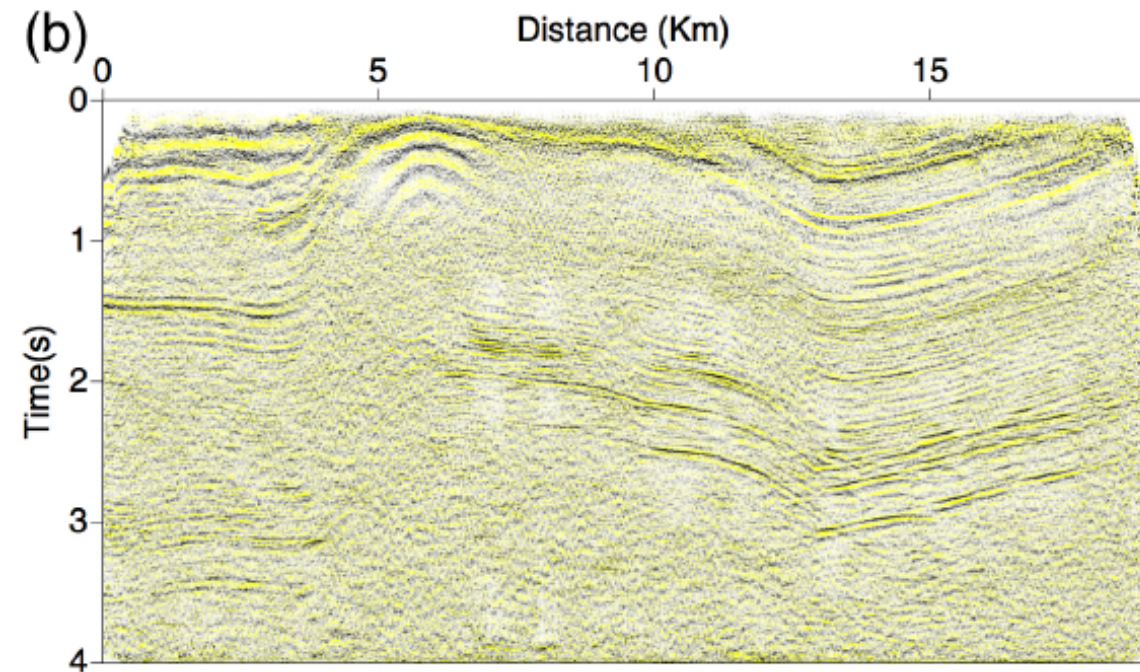
After recursive reflectivity estimation



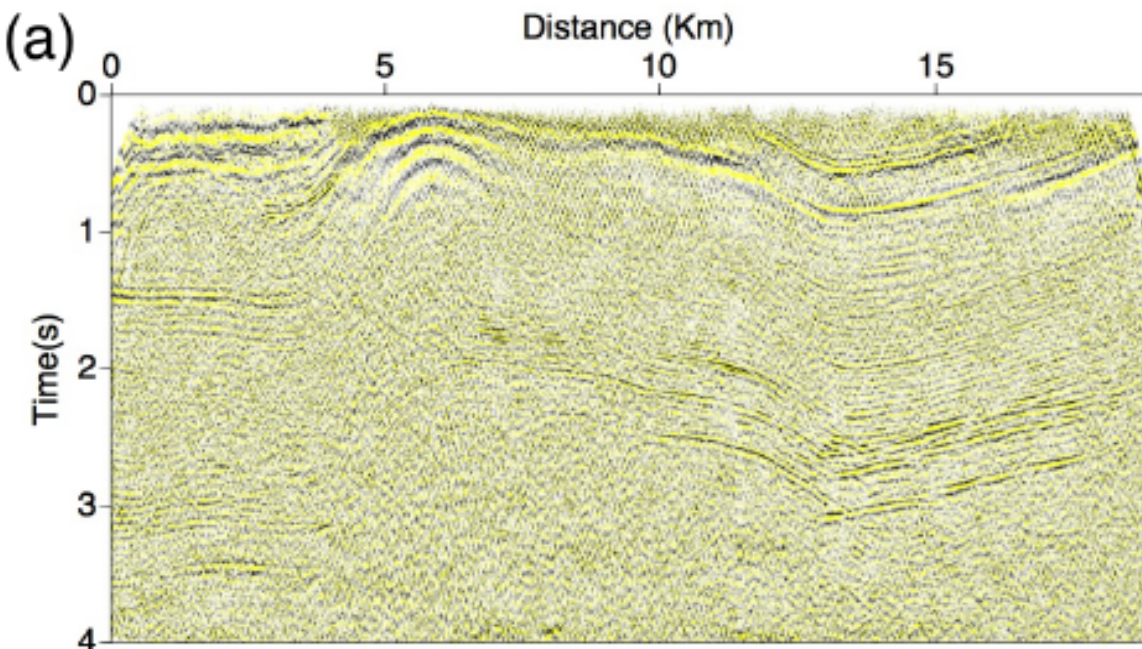
Stacked sections



After recursive reflectivity estimation followed by adaptive SVD filtering

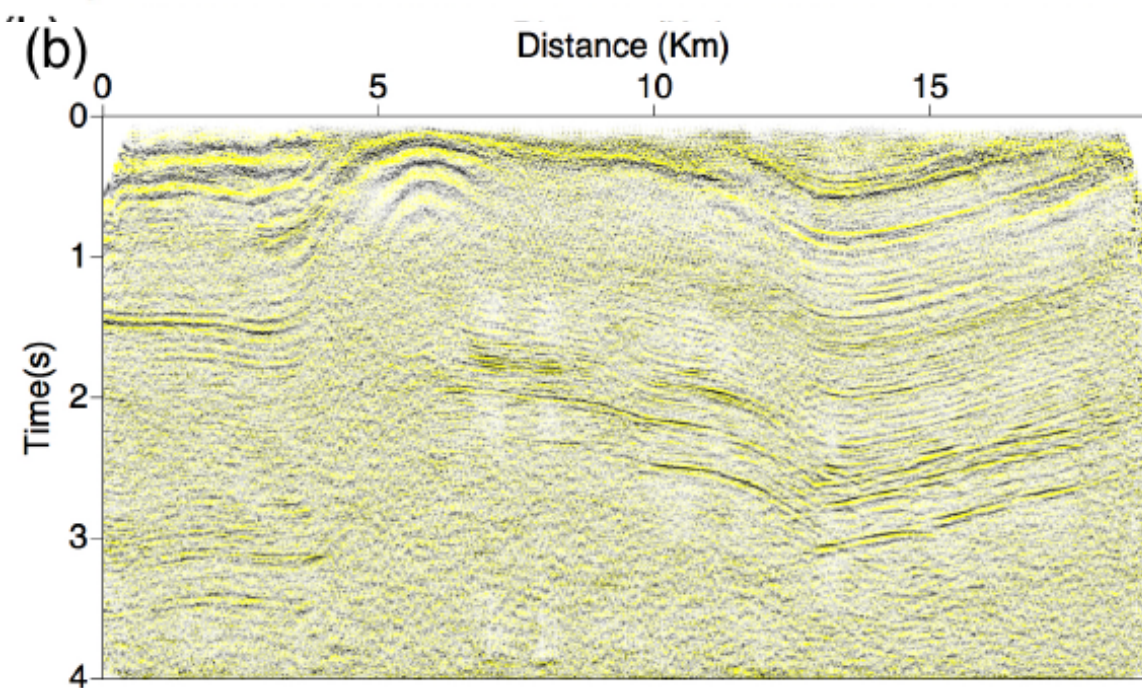


After adaptive SVD filtering followed by recursive reflectivity estimation



Stacked sections

Original data



After adaptive SVD filtering
followed by recursive
reflectivity estimation

CONCLUSION

- A new method for estimating seismic reflectivity by decomposition of a seismic trace in minimum-delay wavelets.
- The method improves vertical resolution for a source wavelet which is close to minimum delay.
- For a mixed-delay source wavelet one may apply an all-pass phase filter before or after the reflectivity estimation.
- We have also developed a data processing strategy for noise removal and signal enhancement by combining adaptive SVD filtering with reflectivity estimation.
- The SVD filtering removes noise and improves lateral continuity while the reflectivity estimation increases the high-frequency content in the data and improves vertical resolution.

ACKNOWLEDGEMENTS

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