



GEOMECHANICS FOR GEOPHYSICISTS

# Discrete Particle Modeling of Rock Behaviour

Rune M Holt (NTNU & SINTEF)

Idar Larsen (SINTEF)

Liming Li (SINTEF)

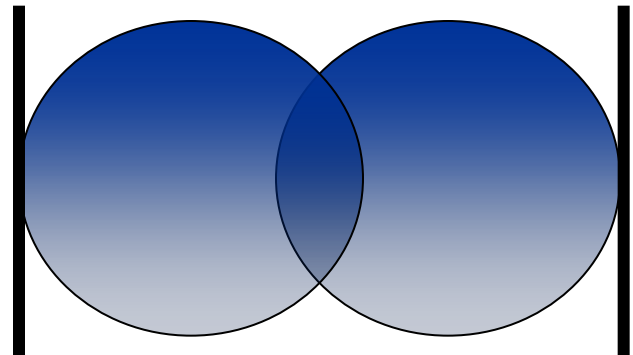
**Trondheim, 26 April 2012**

# Why?

- Main idea is to develop a Numerical Laboratory, where stress dependent rock properties can be measured from 3D (or 2D) microstructure images.
- Useful when no or insufficient amount or quality of core material is available.
- Useful for understanding of rock behaviour, enabling simpler models to be developed, incorporating the right physics.

# Discrete Particle Model

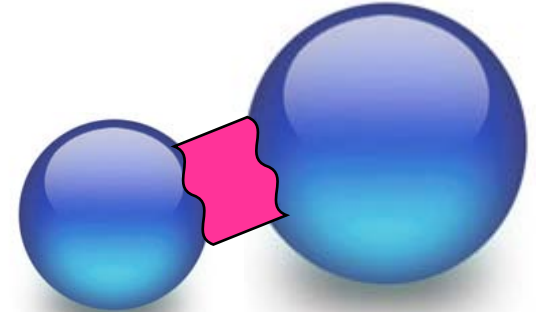
- ❑ Deformation is modeled using a Discrete Element Method (DEM)
- ❑ Key elements: Spherical particles (in 3D); Disks (in 2D)
- ❑ Overlap permitted ("soft contact")
- ❑ Use linear, Hertzian or user-defined contact laws to calculate elastic deformation between spheres



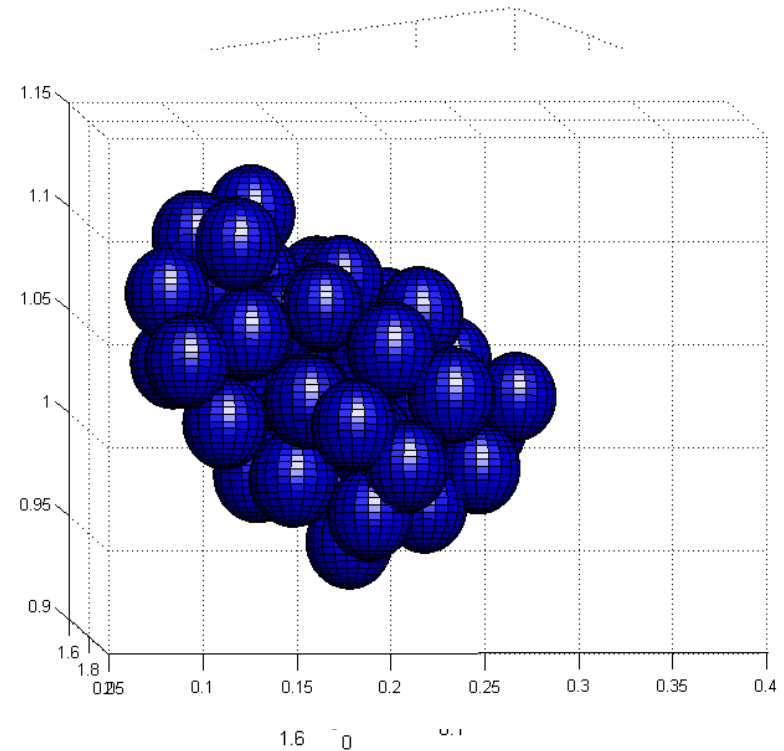
**In addition: Walls**

*We use PFC ("Particle Flow Code"); Potyondy & Cundall, Int. J. Rock Mechanics 2004*

# Discrete Particle Model

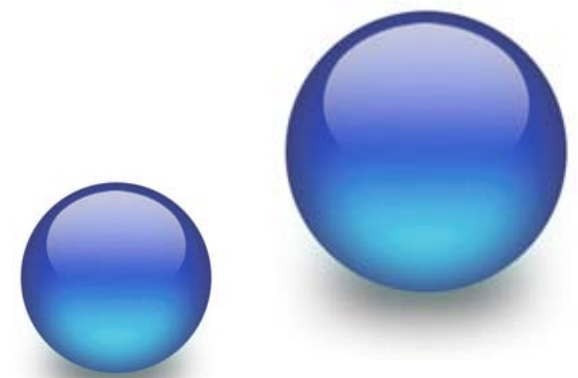


- ❑ Cement between particles is simulated through "parallel bonds"
- ❑ Bonds are defined through
  - ❖ shear & normal stiffness
  - ❖ shear & normal strength
  - ❖ Extent of contact (transfer of moment)
- ❑ Spheres are clustered to create grains



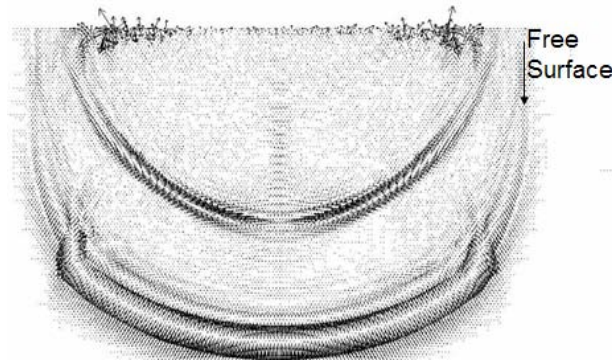


# Discrete Particle Model



- Force and moment equilibrium ensured for each contact in a cycling and time-stepping approach

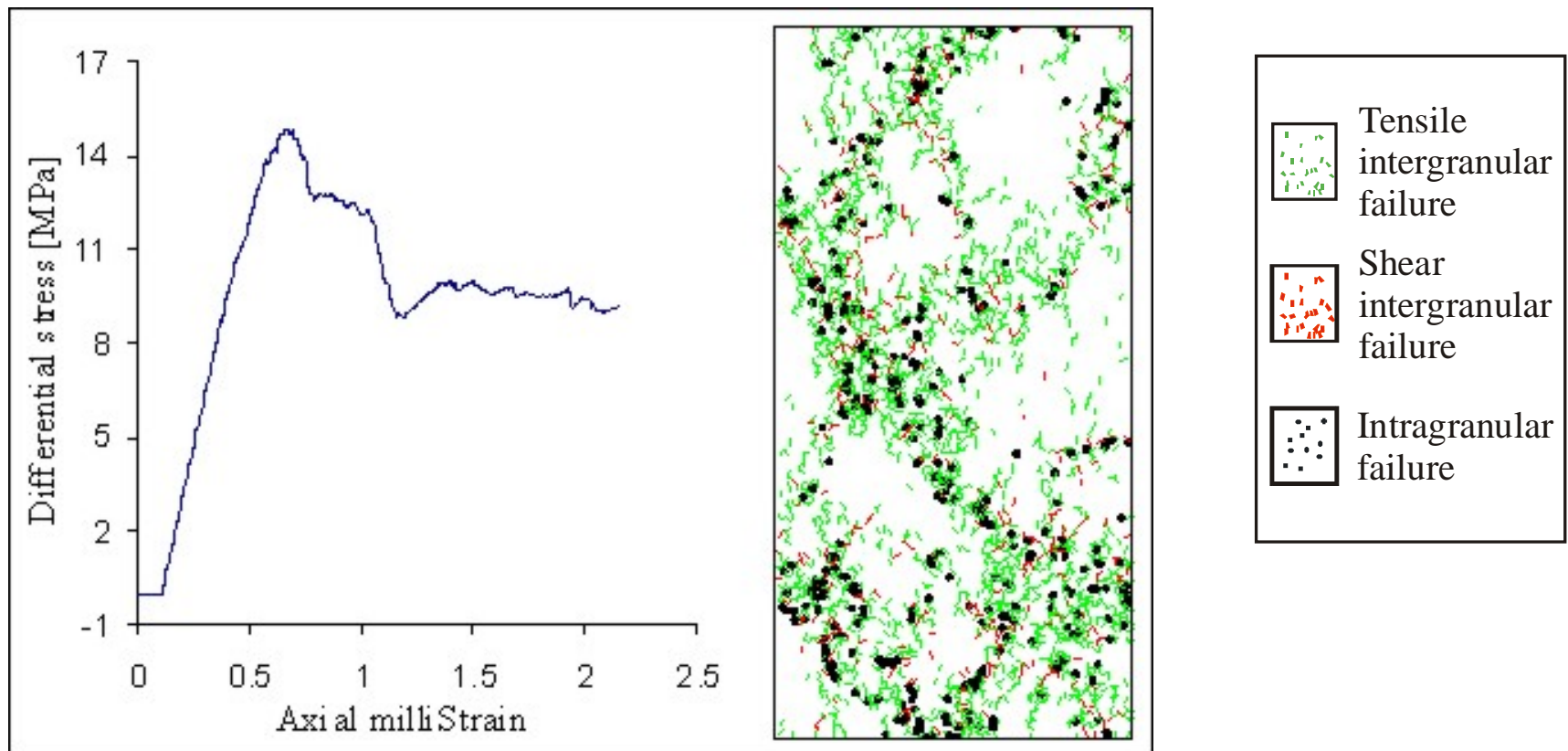
□ Discrete Particle Modelling represents a fully dynamic approach to computing complex behaviour of bonded rock based on contact law between individual particles



# Deformation and failure

## A 2D model with multi-disk clusters under biaxial stress

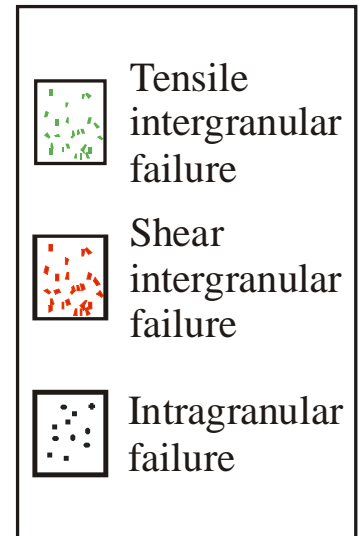
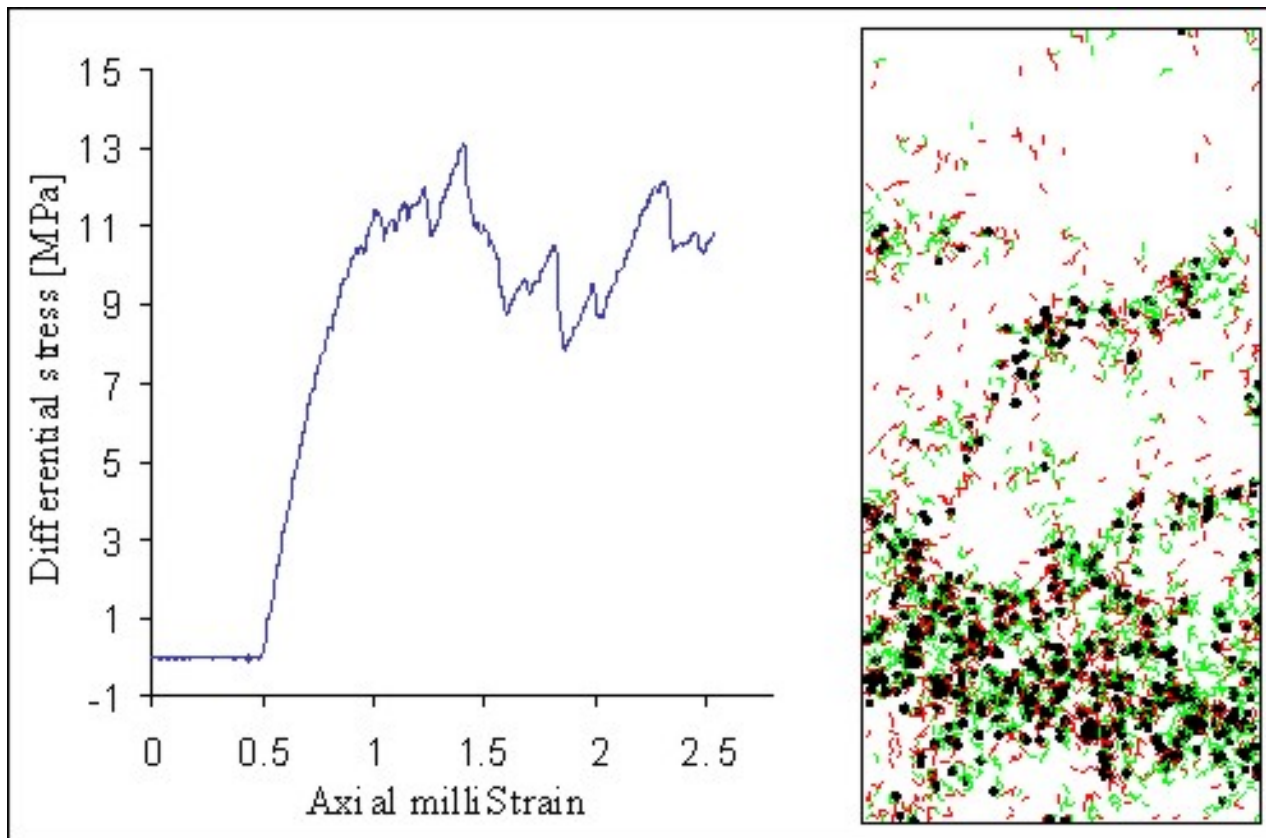
(Development of a shear band at low confinement 4 MPa)



# Deformation and failure

## A 2D model with multi-disk clusters under biaxial stress states

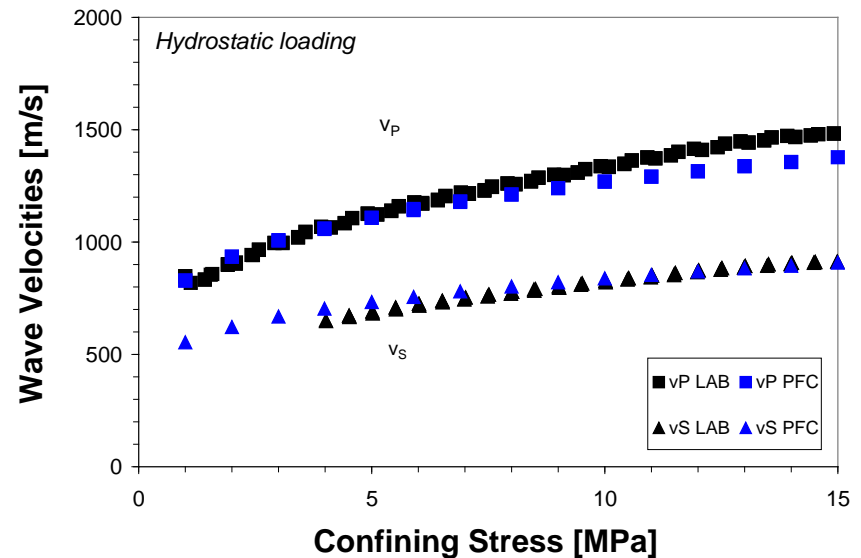
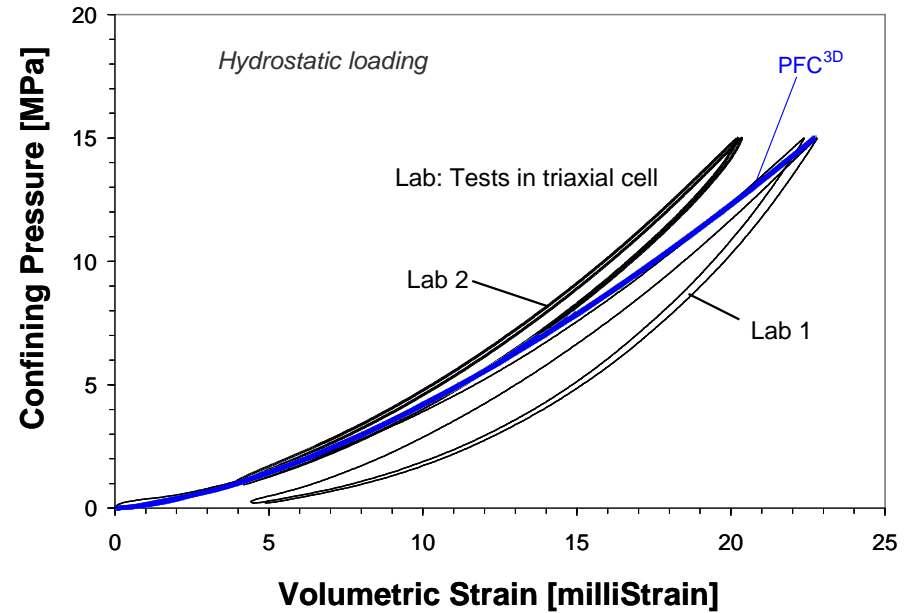
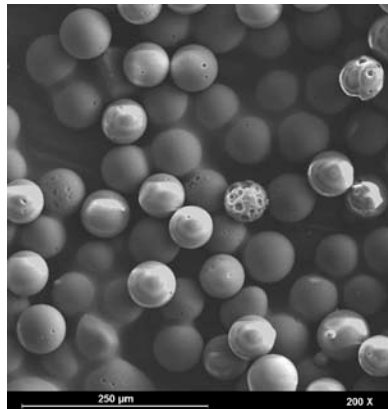
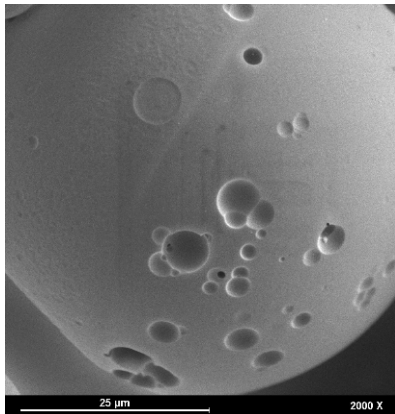
(Development of a compaction band at high confinement 18 MPa)



As observed in Castlegate sst by Olsson & Holcomb (2000)!

# Comparison with experiments

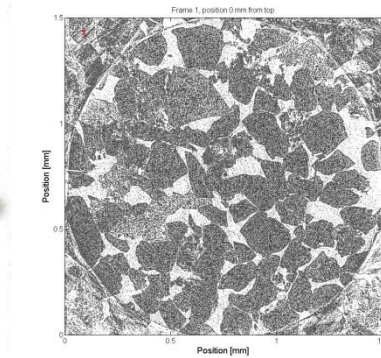
Experiments with uncemented glass beads give satisfactory [but not perfect] fit to data, [almost] without adjustable parameters



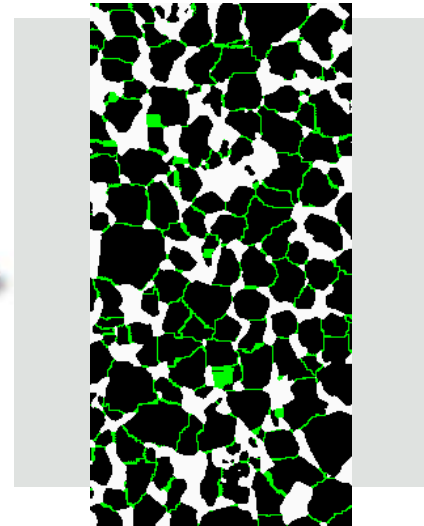
# Generation of a microstructure-based model for sandstone



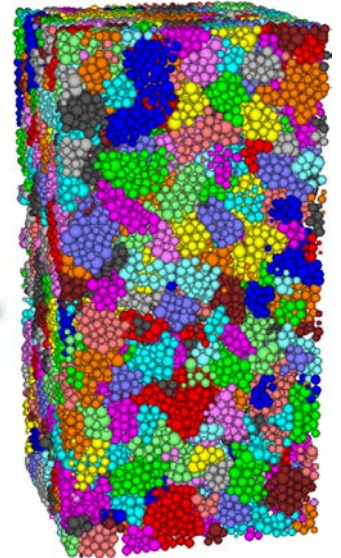
Sandstone specimen  
(may be from disintegrated core material or drill cuttings)



3D micro-CT image



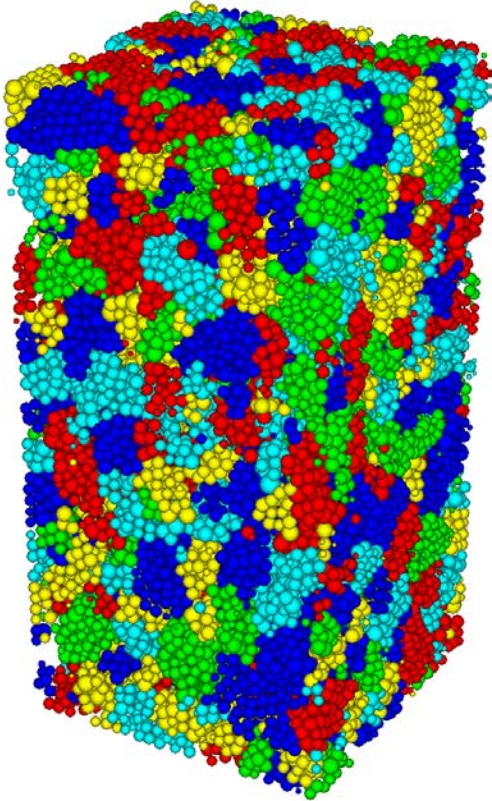
Segmented  
3D micro-CT  
data



Discrete element  
model of the  
sandstone (Each  
sand grain is  
represented by a  
cluster of elements  
of the same color)



# Using clusters of elements to represent grains



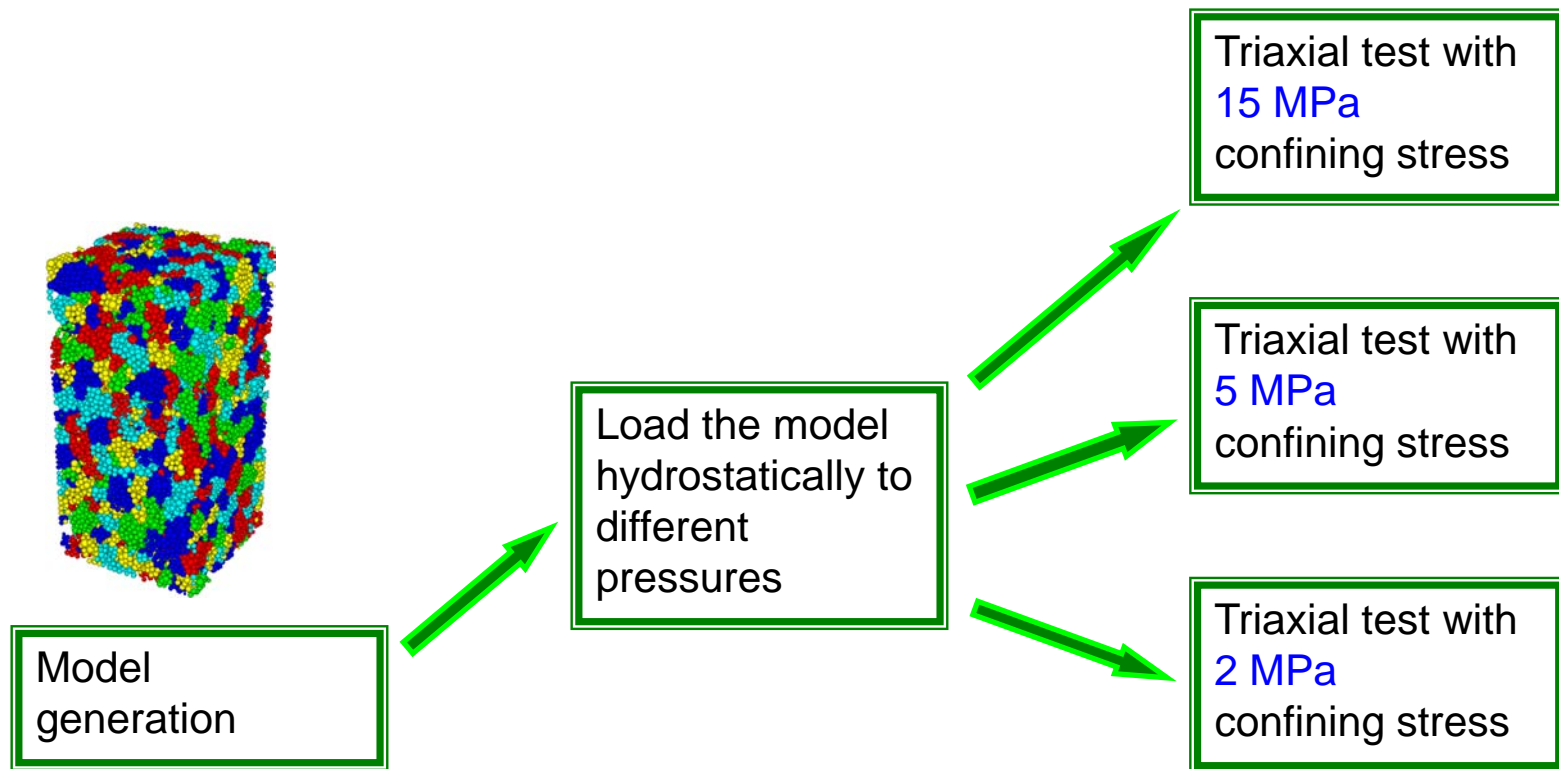
Two sets of bonding parameters:

**Intergranular bonds:** for a pair of elements which belong to two different grains.

**Intragranular bonds:** for a pair of elements which belong to the same grain.

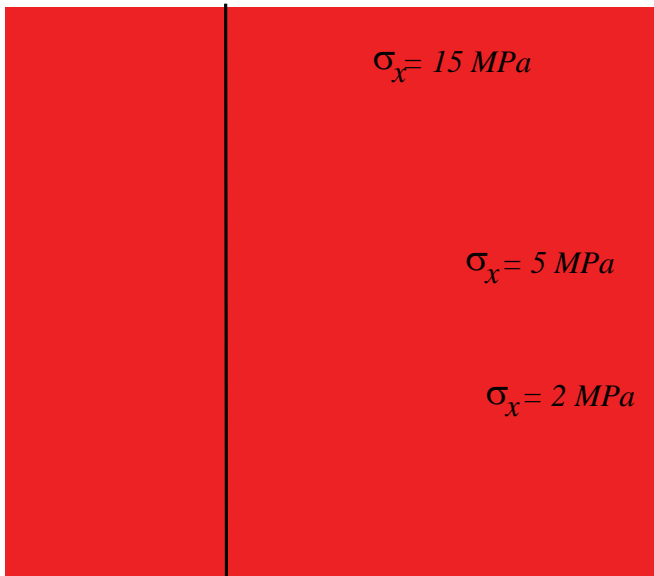
# Model calibration to determine input parameters

Fit the results of different lab tests with real rock specimens using the same model (same parameters).

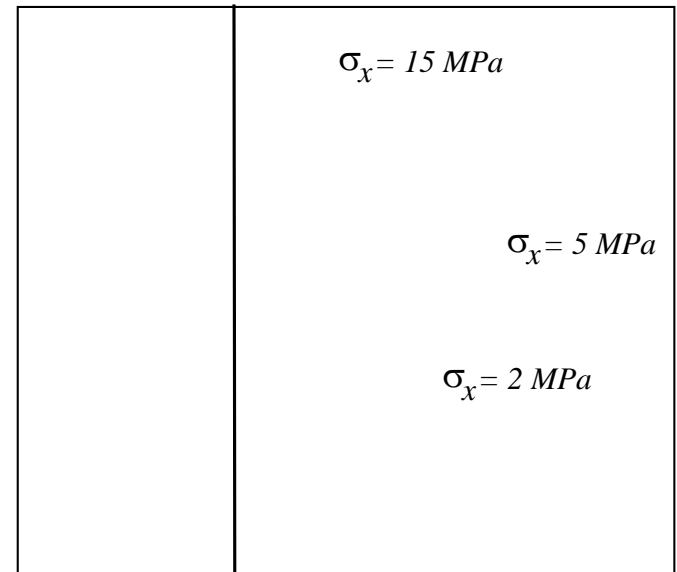


# Comparison of simulation results and data measured on Castlegate sst.

Stress vs. strain



Experiment

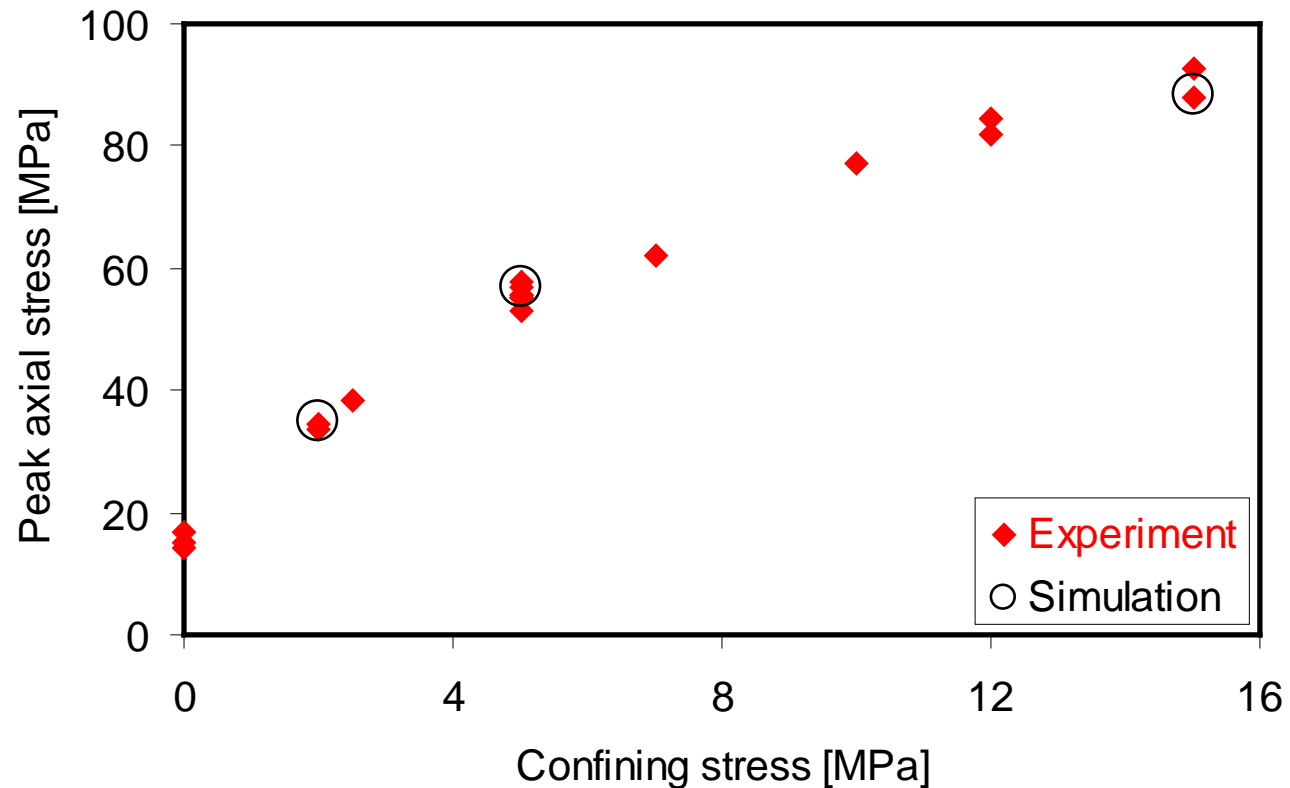


Simulation



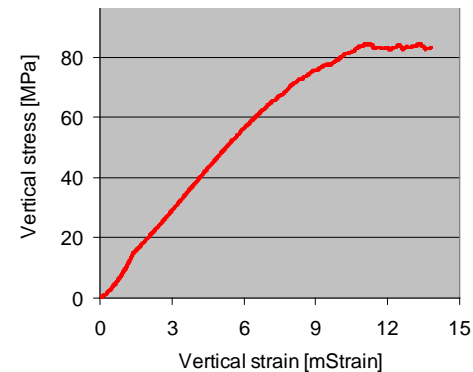
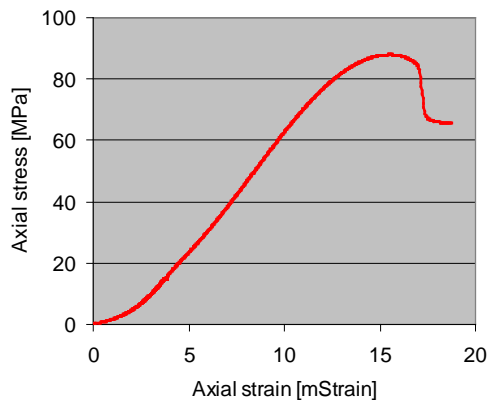
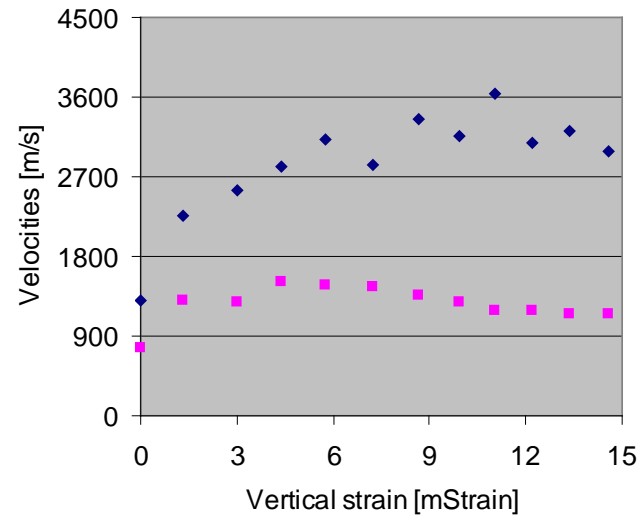
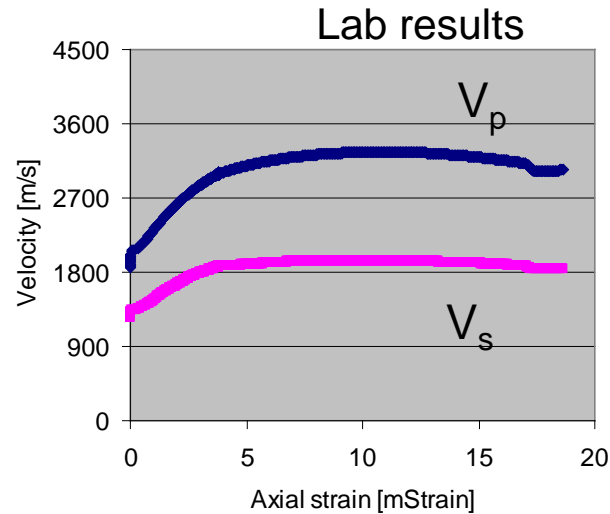
# Comparison of simulation results and data measured on Castlegate sst.

Peak axial stress vs. confining stress



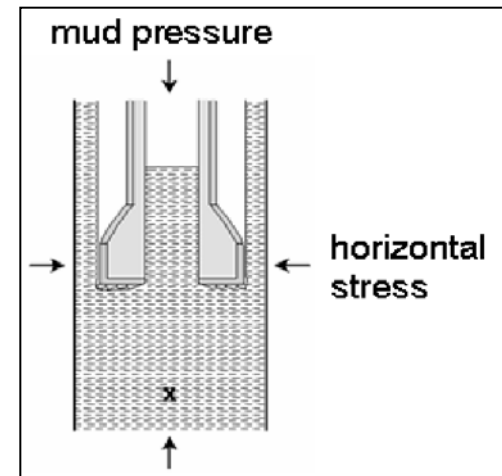
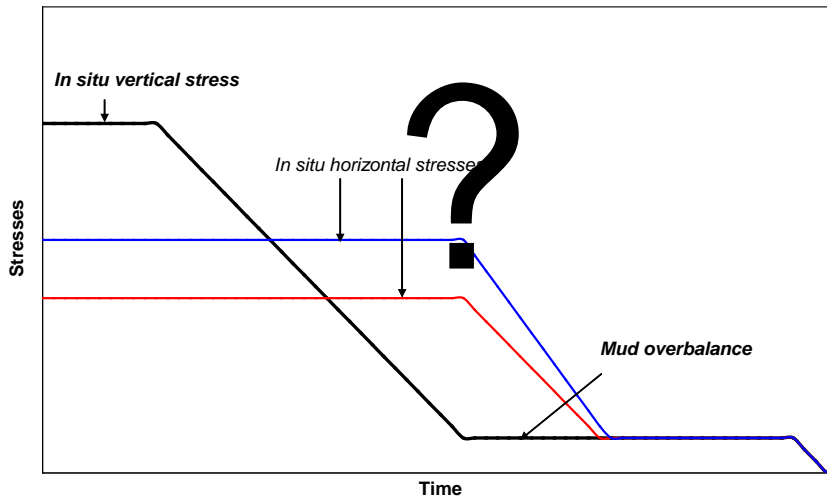
# Comparison of simulation results and data measured on Castlegate sst.

Velocities in a triaxial test (confining pressure 15 MPa)



# Stress Path during Coring

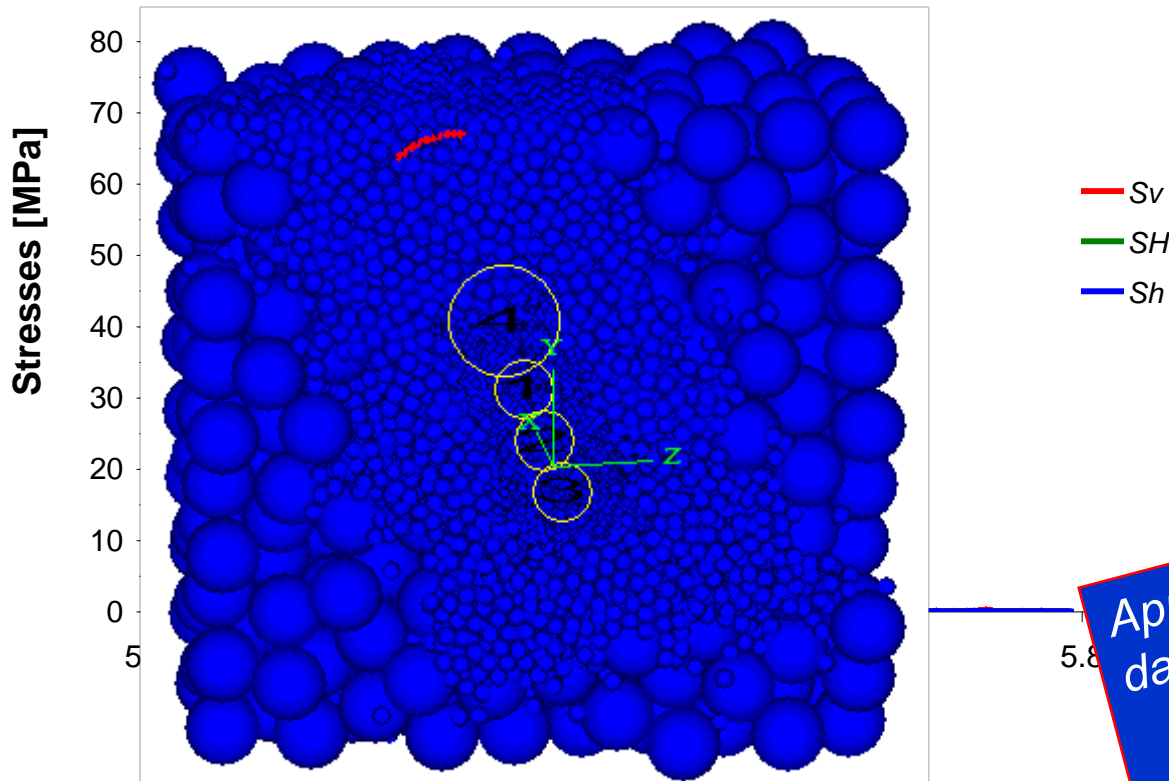
- ❑ Source of core alteration, affecting rock mechanical & wave velocity measurements
- ❑ Source of Stress Memory (Kaiser effect in AE), potential tool for stress determination



# Stress Path during Coring PFC<sup>3D</sup> Simulation

## Example of cube-shaped assembly

Well angle 20°, azimuth 10°, tor-shaped bit  
Visualization - rear ½, rotation x: 110°, y: 100°, z: 0°



Study effect of:

Rock properties

Hole angle

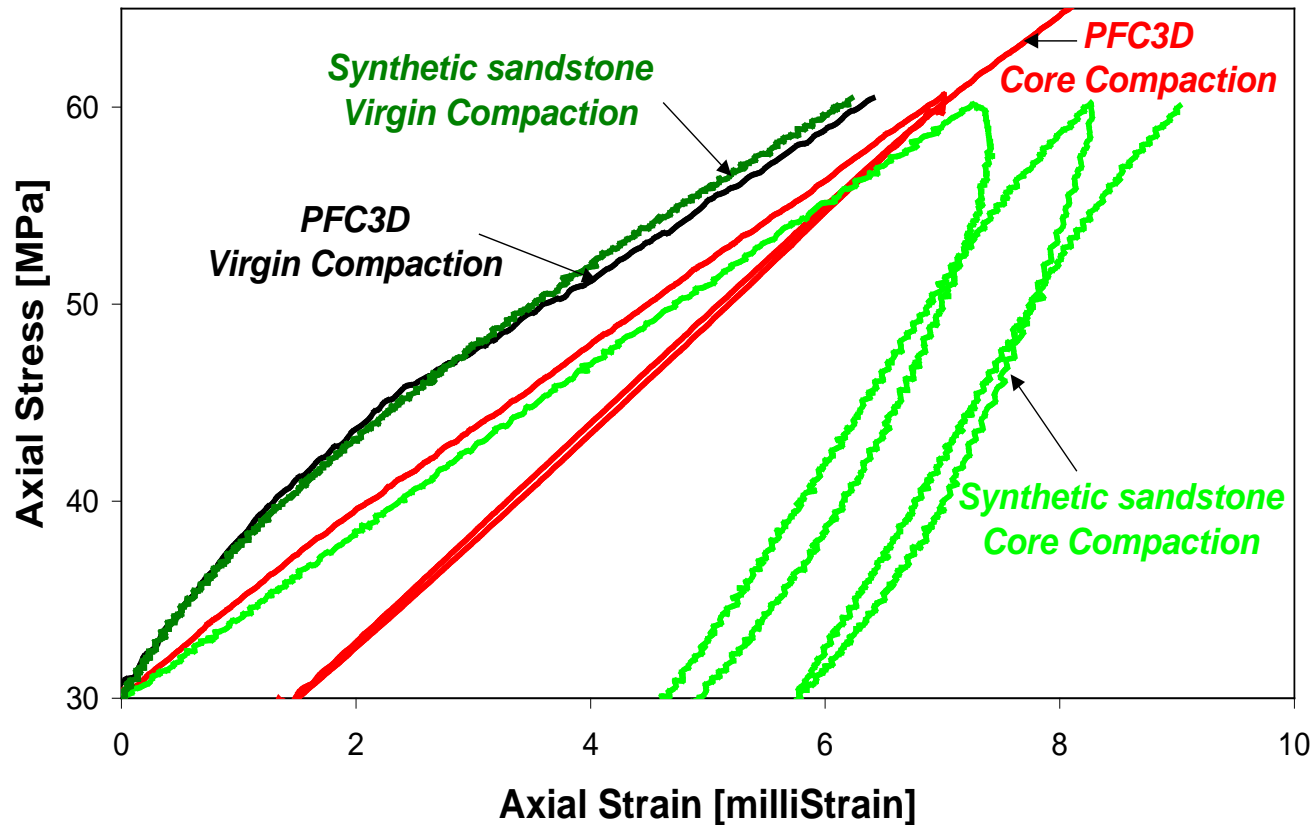
Bit shape

WOB

Apparent stress path is less  
damaging than anticipated

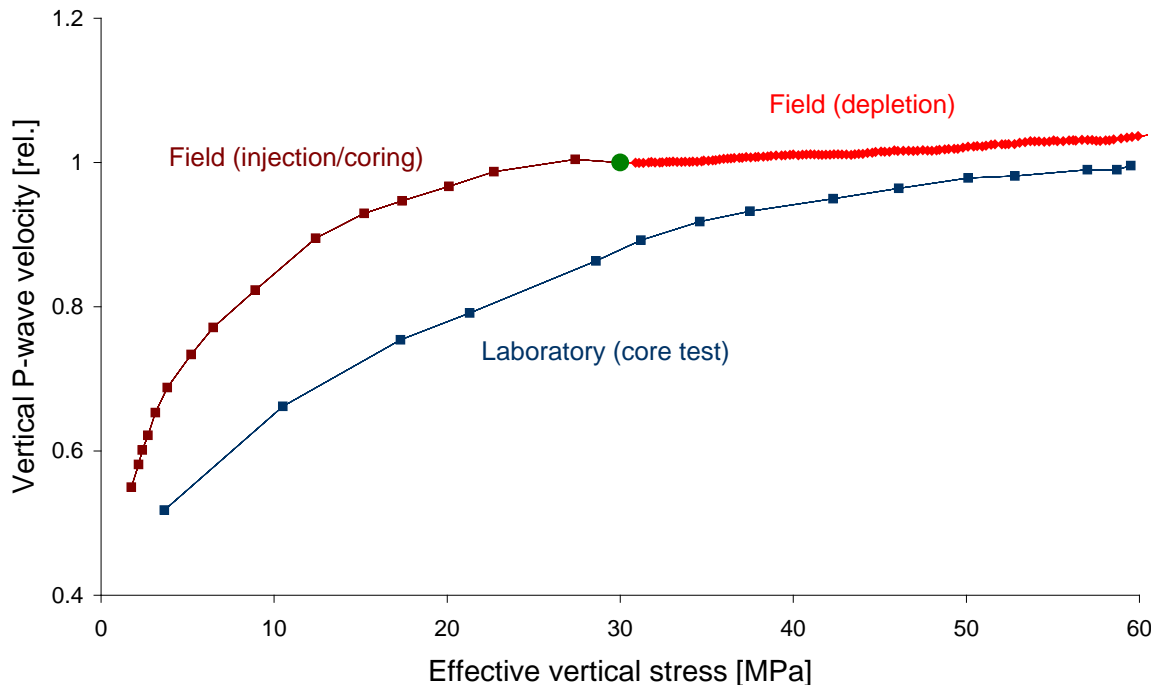
Gorodkov et al, Rock Stresses 2006

# Particle Modelling: PFC<sup>3D</sup> Virgin vs. Core Compaction



# Reservoir Rocks: Synthetic Sandstone

## Laboratory modelling of *In situ* vs. Core Behaviour



We observe:

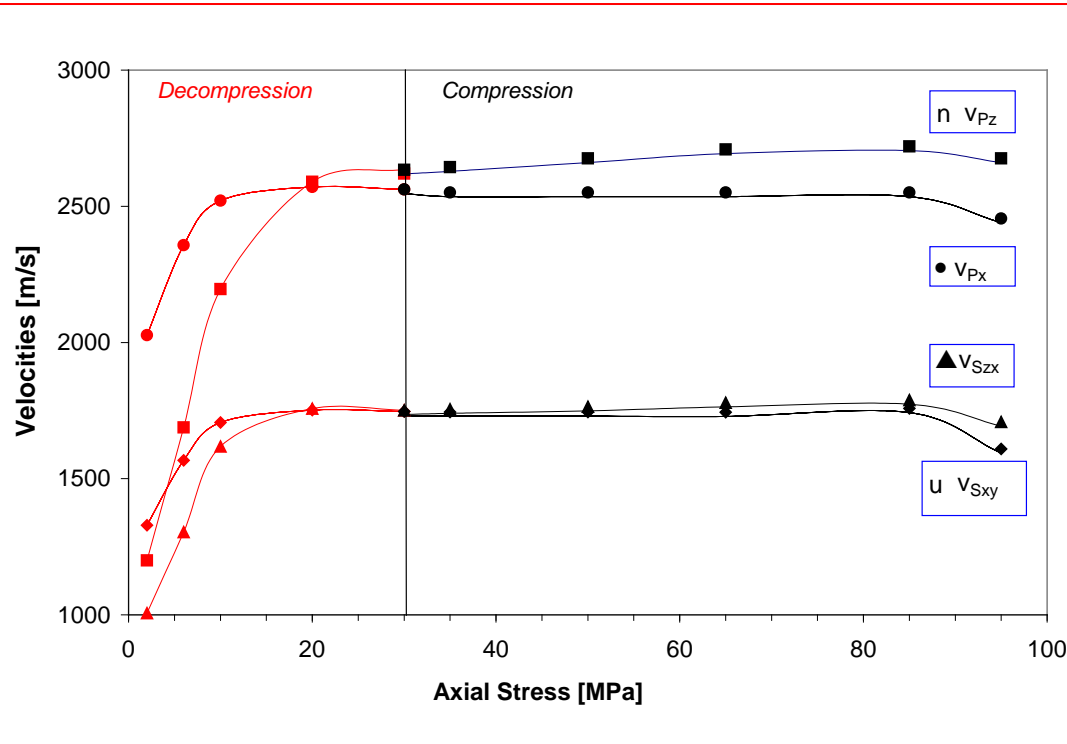
Low stress sensitivity during virgin loading (depletion) – effect of cementation

Significant stress sensitivity during unloading (inflation) and reloading (core measurement) – effect of cement bond breakage

Synthetic sandstone formed by cementation under simulated *in situ* stress conditions (here: 30 MPa vertical, 15 MPa horizontal)

# Reservoir Rocks: Synthetic sandstone

*In situ* Behaviour from numerical modelling



We observe:

Qualitatively the same response to loading & unloading as seen in the physical experiments

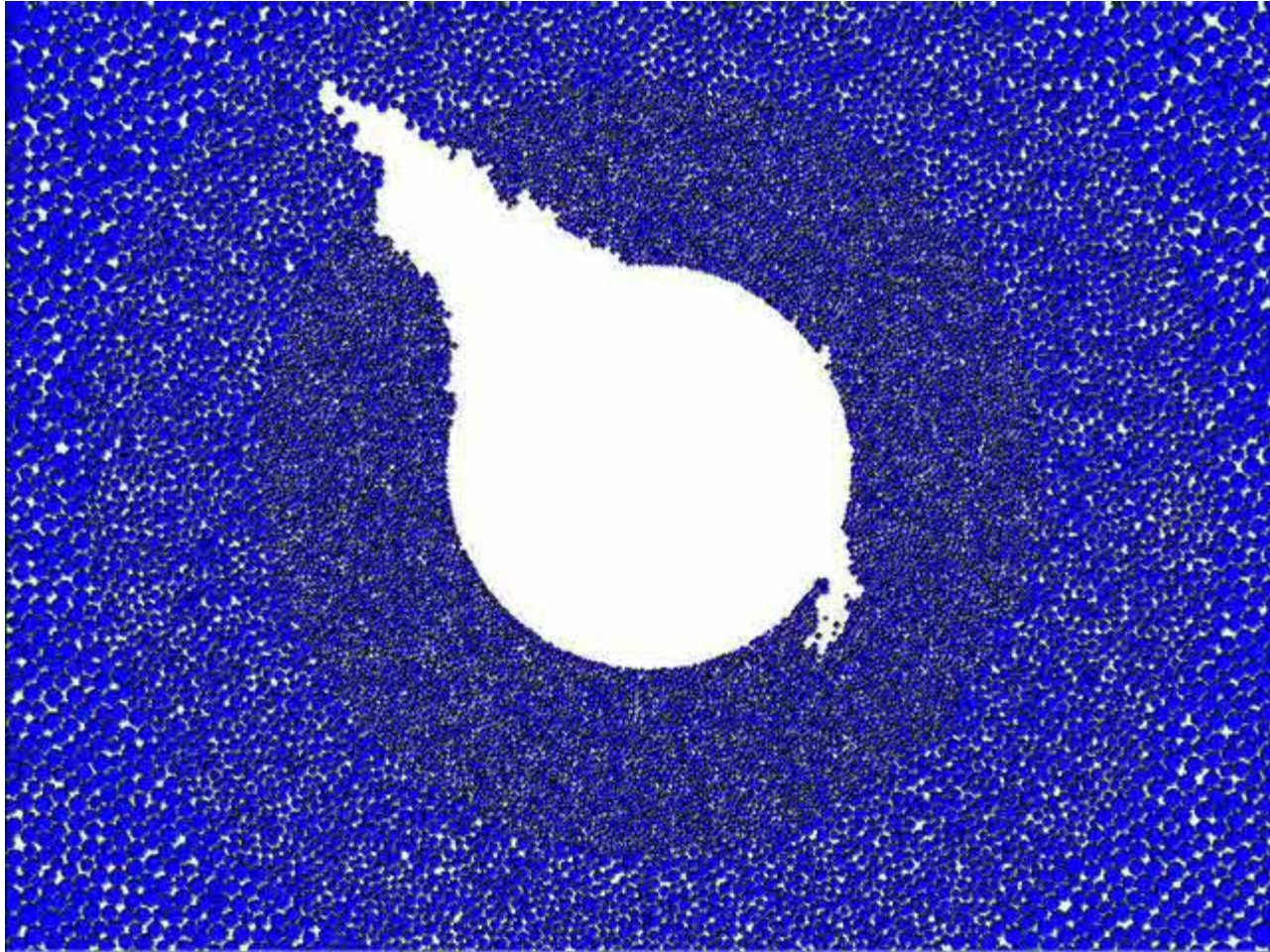
Notice Stress-Induced Anisotropy (also in lab!), and velocity decrease at high stress due to bond breakage

PFC<sup>3D</sup> simulation performed with spherical particles; bonds inserted under 30 MPa axial & 15 MPa lateral stress

*Courtesy of Lars M Moskvil*



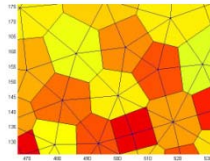
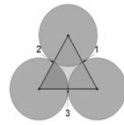
# Sand Production / Well Stability





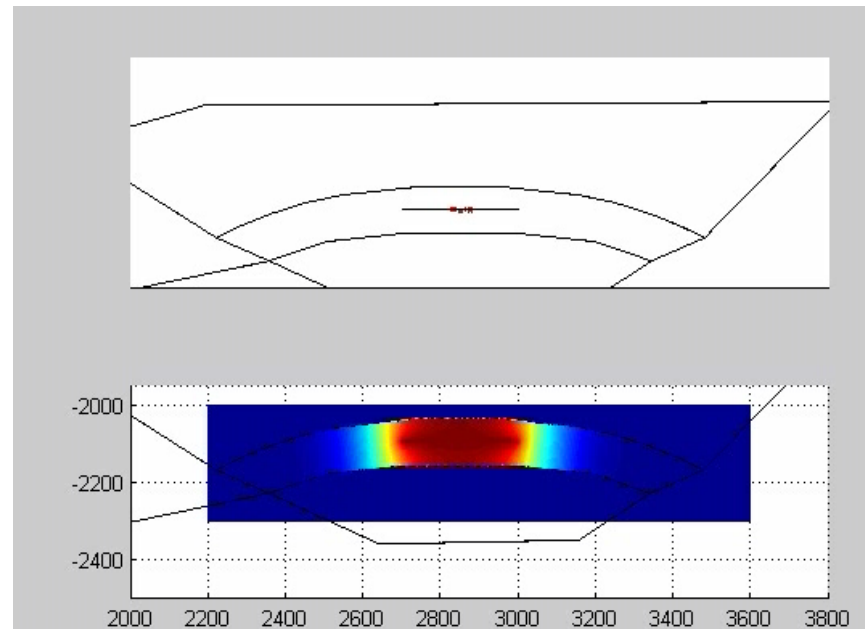
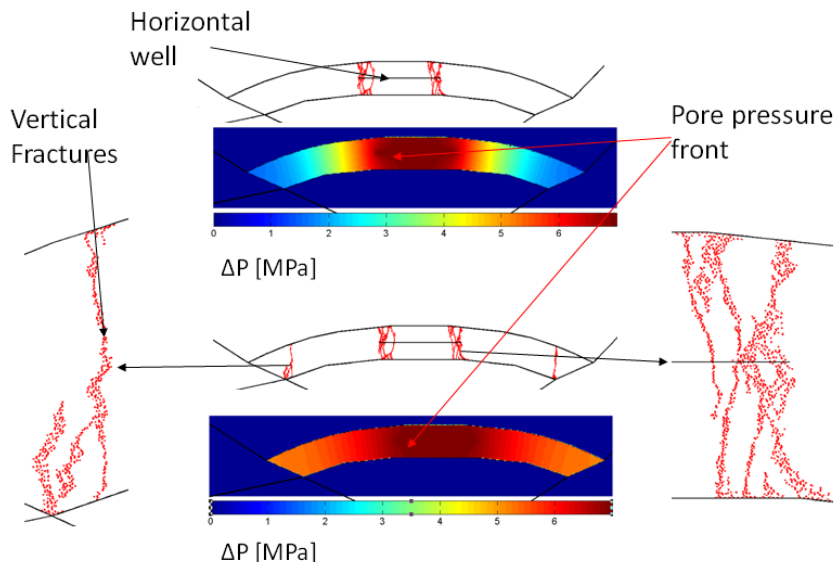
# DEM on larger scale

- Initial work with PFC on basin scale led to Modified DEM

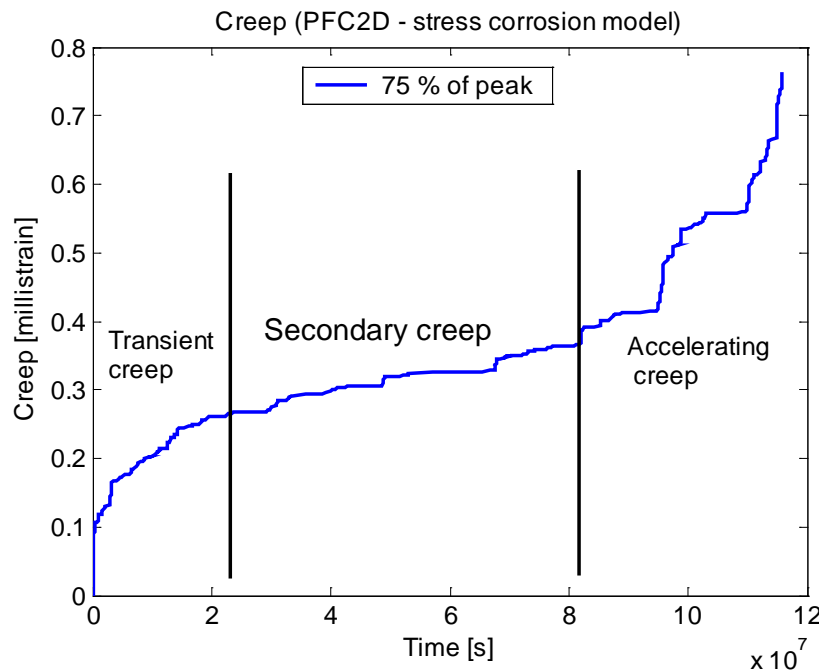


*PhD Study by  
Haitham Alassi*

- Permit realistic modelling of fracture development and fault (re-) activation during injection (or depletion) - Link to 4D seismics



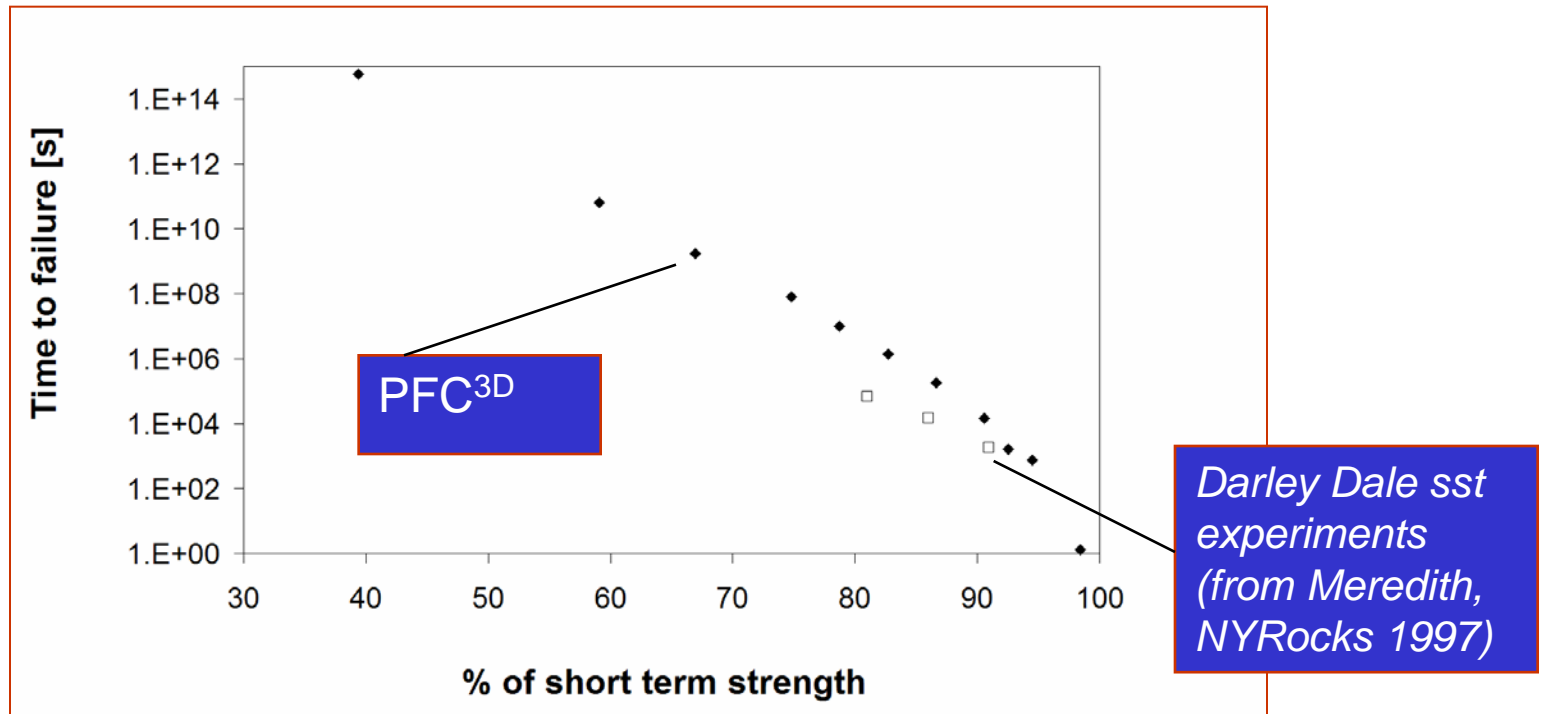
- ⌚ Creep is implemented to mimick stress-induced corrosion by reducing the parallel bond extent depending on the stress level relative to bond strength at each contact



The model captures the three commonly observed phases of transient, secondary and accelerating (tertiary) creep

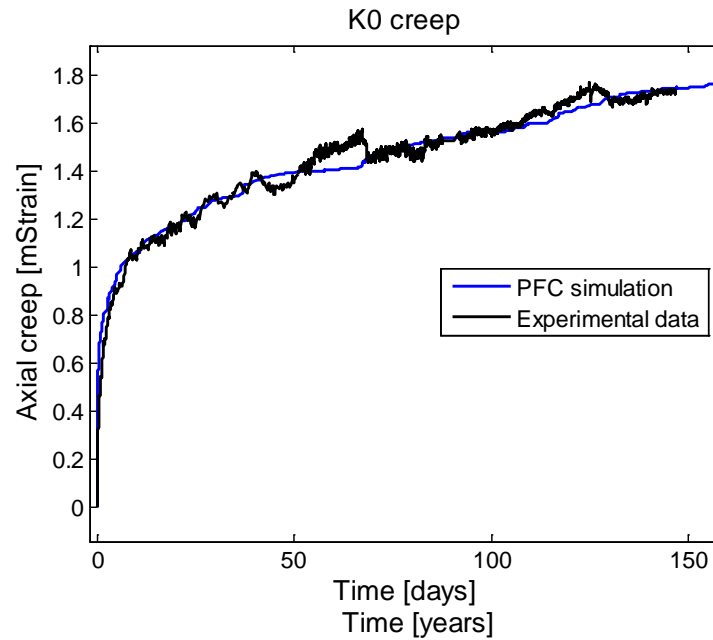
*A similar approach has been presented by Potyondy (2005)*

# Time dependent deformation



- ⌚ Long-term behaviour may be assessed from short-term simulations
- ⌚ Challenges: Appropriate calibration of microscopic creep parameters
- ⌚ Other physical mechanisms may play a vital role over long time scales

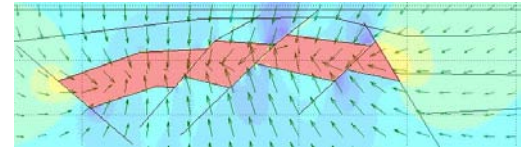
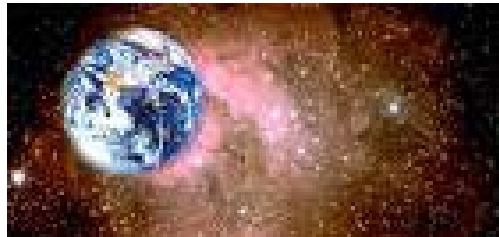
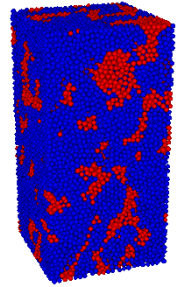
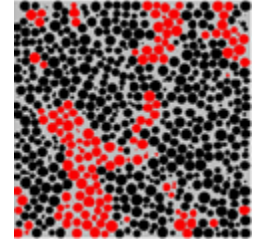
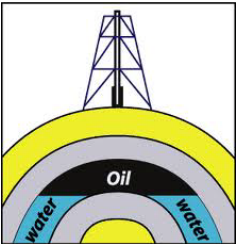
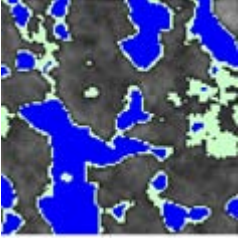
# □ *A Tool for the Future...*



# *Dance me through the end of the pore*

*Lyrics: Rune M. Holt*

*From the land of a lonely pore  
next to a solid grain  
We digest their contacts  
- squeezed by contracts -  
With courage and pain  
we compute the strain  
and derive the strength of a full sized core!  
It is not in vain  
- maybe it's insane -  
But one day we may capture the reservoirs -  
built by discrete balls,  
surrounded by walls,  
seismic waves moving in a silent waltz.  
Our dream is to model the Earth and the Stars!*



# Acknowledgements

Financial support to SINTEF's  
PETRUS & PETRUSCA projects:

Chevron  
ConocoPhillips  
Det norske  
RWE Dea  
Shell  
Statoil  
Petrobras (only PETRUS)



Cooperation:

Numerical Rocks

