

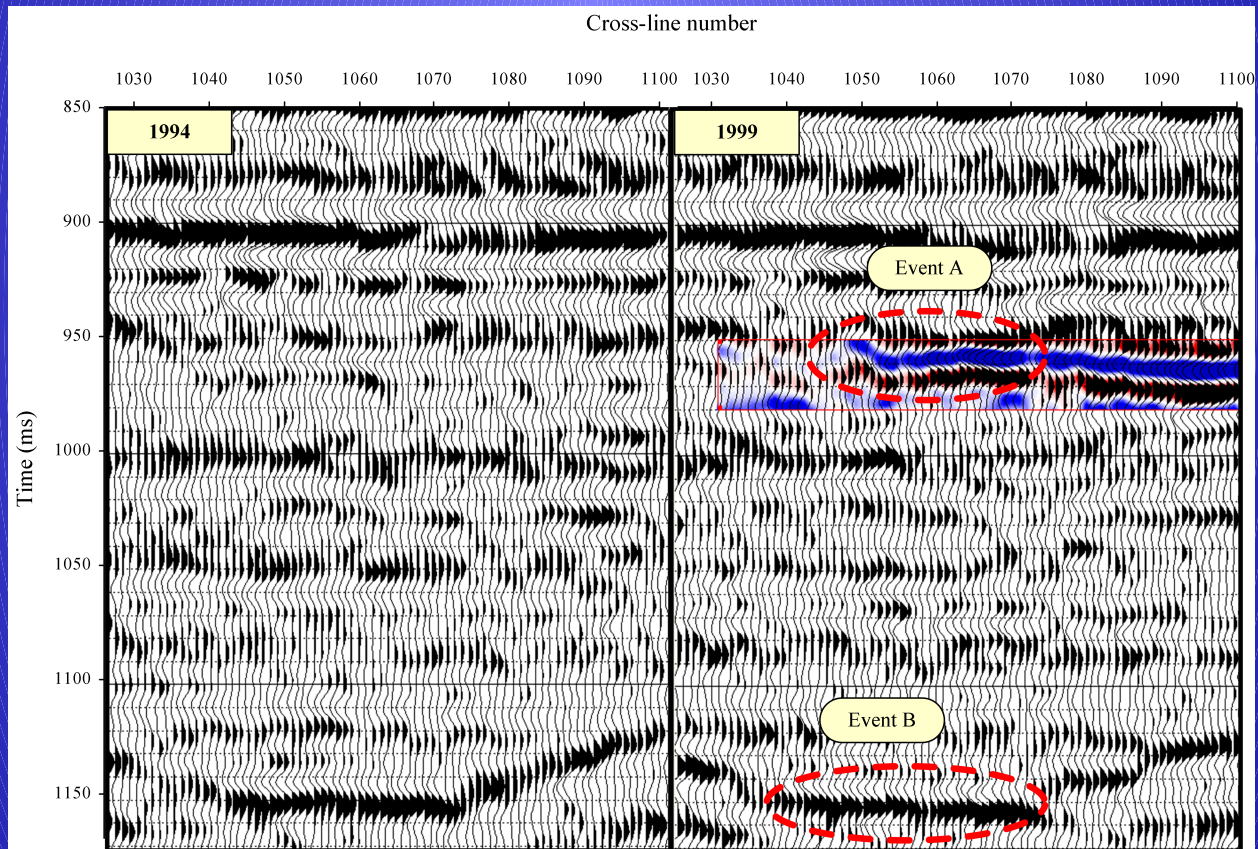
**Velocity and thickness estimation of
thin CO₂-layers
with uniform and patchy saturations**

Amir Ghaderi, Martin Landrø

Rose Meeting 2010

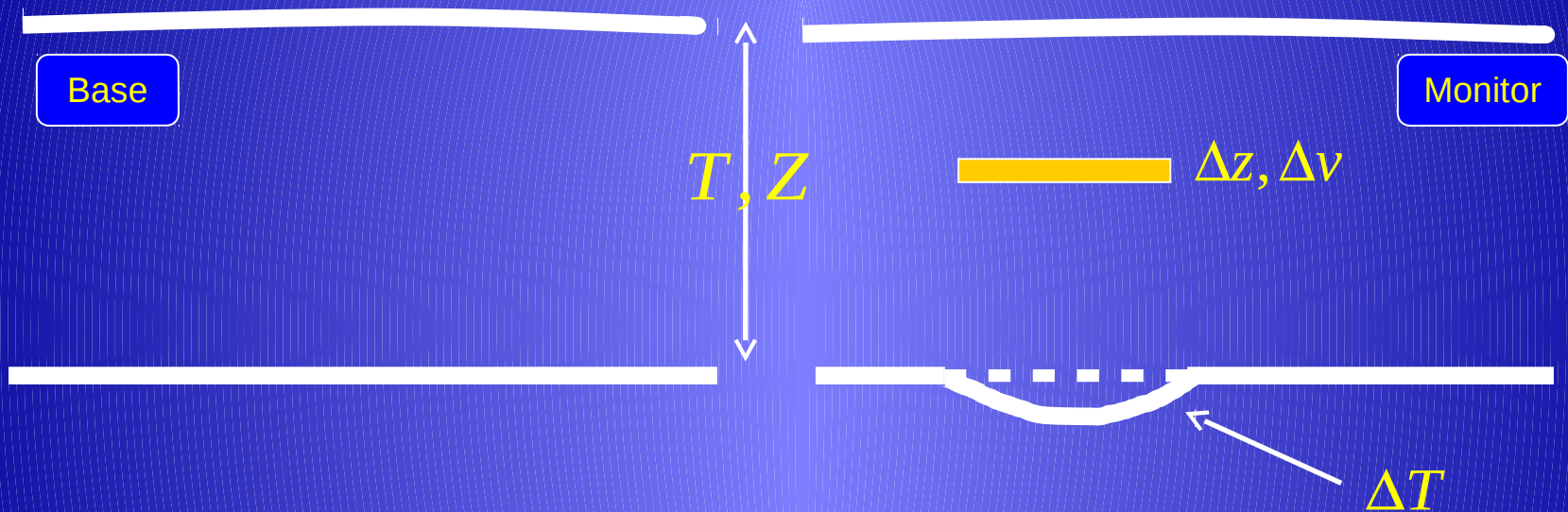
The Problem

Real seismic data anomaly



A section from Utsira formation
Ghaderi & Landrø, Geophysics 2009

The Problem



For the 4D seismic anomaly, we are interested in an estimate of

- thickness: Δz
- change in velocity : Δv
- a quantitative measure of saturation S_{anomaly}

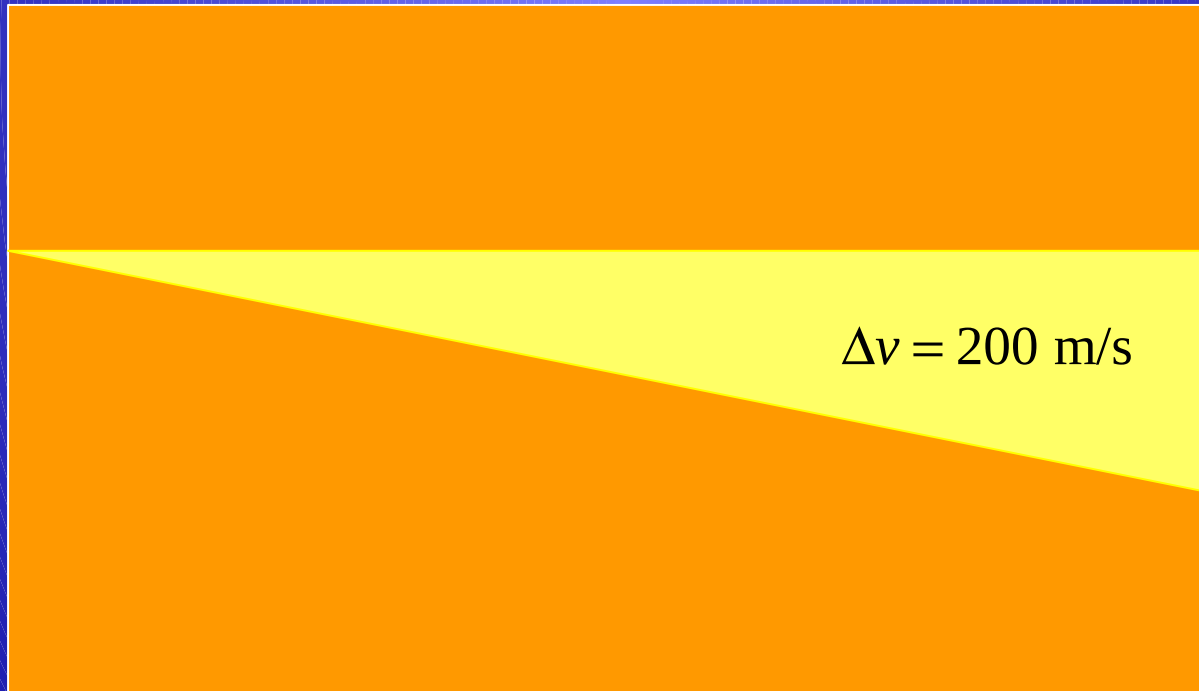
An estimate for solution

Assuming known Δv (some rock physics model, well log), Ghaderi & Landrø (geophysics 2009), propose to estimate Δz by

$$\frac{\Delta T}{T} = - \frac{\Delta v}{v} \frac{\Delta z}{z}$$

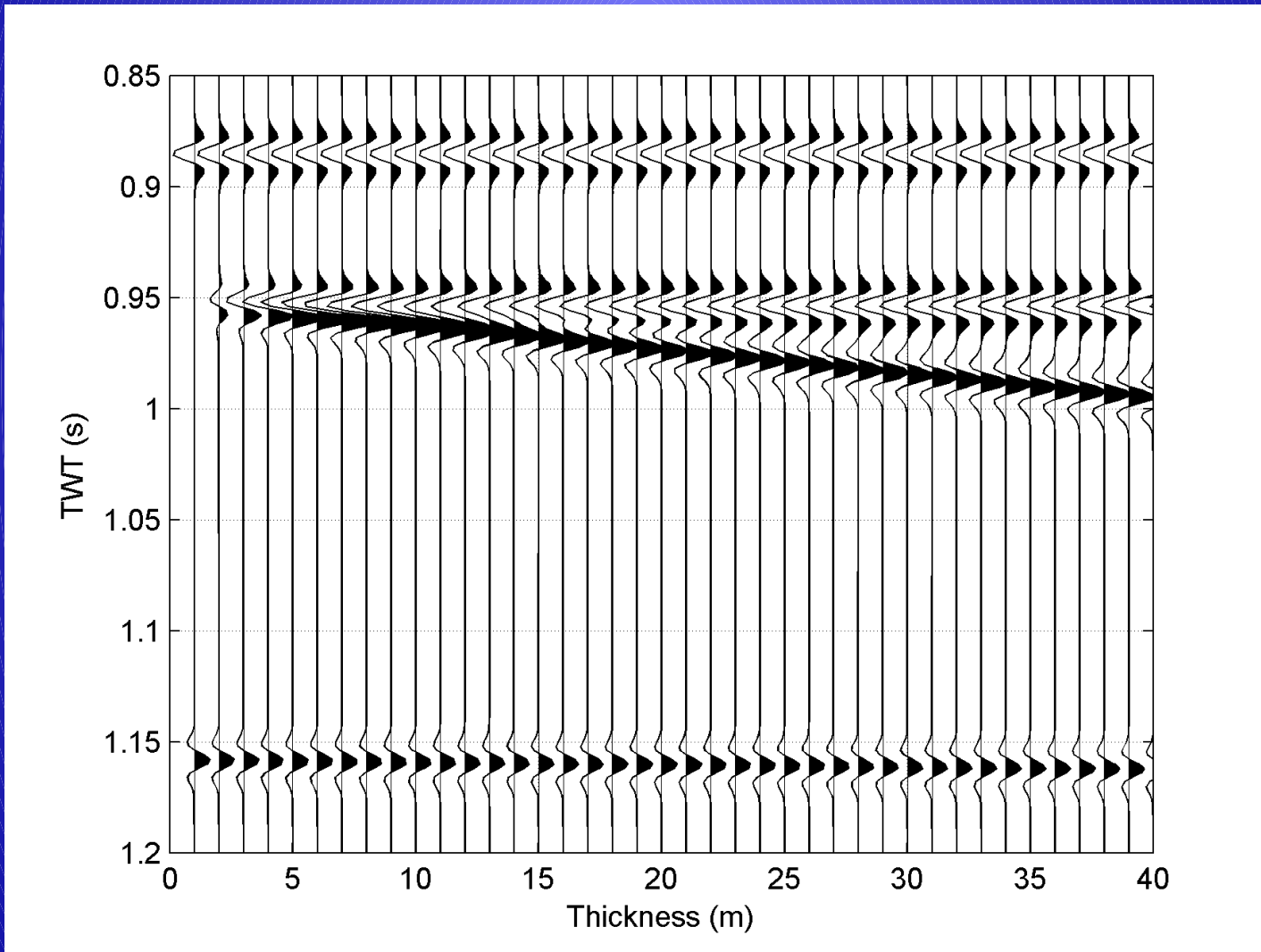
Synthetic test of the model

- Wedge model as a basis for testing the proposed estimate on synthetic data

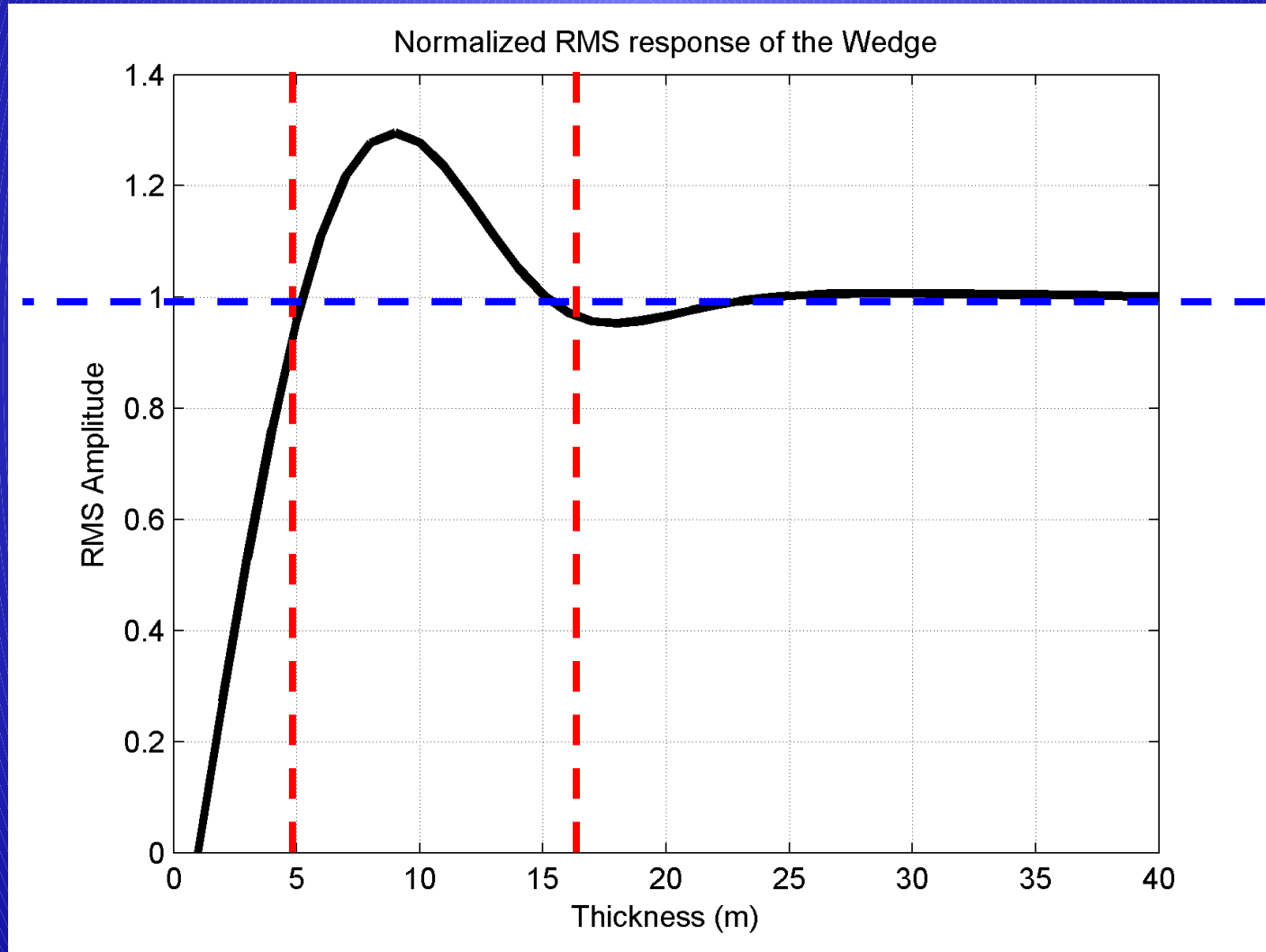


Convolution model (primaries only)

– homogenous saturation distribution

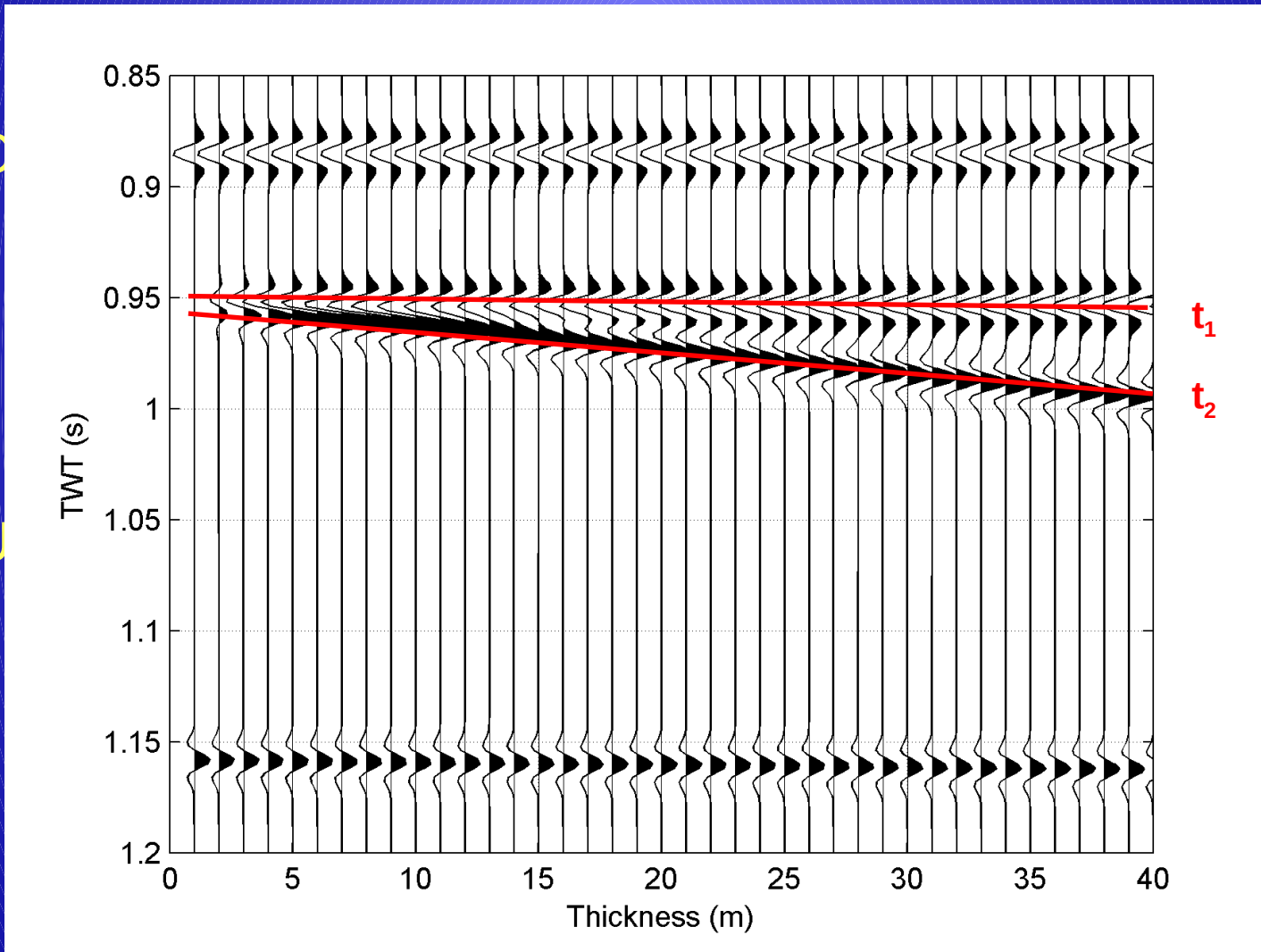


The Amplitude response of wedge model



Estimation of thickness Δz , given Δv

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Estimation of thickness Δz , given Δv

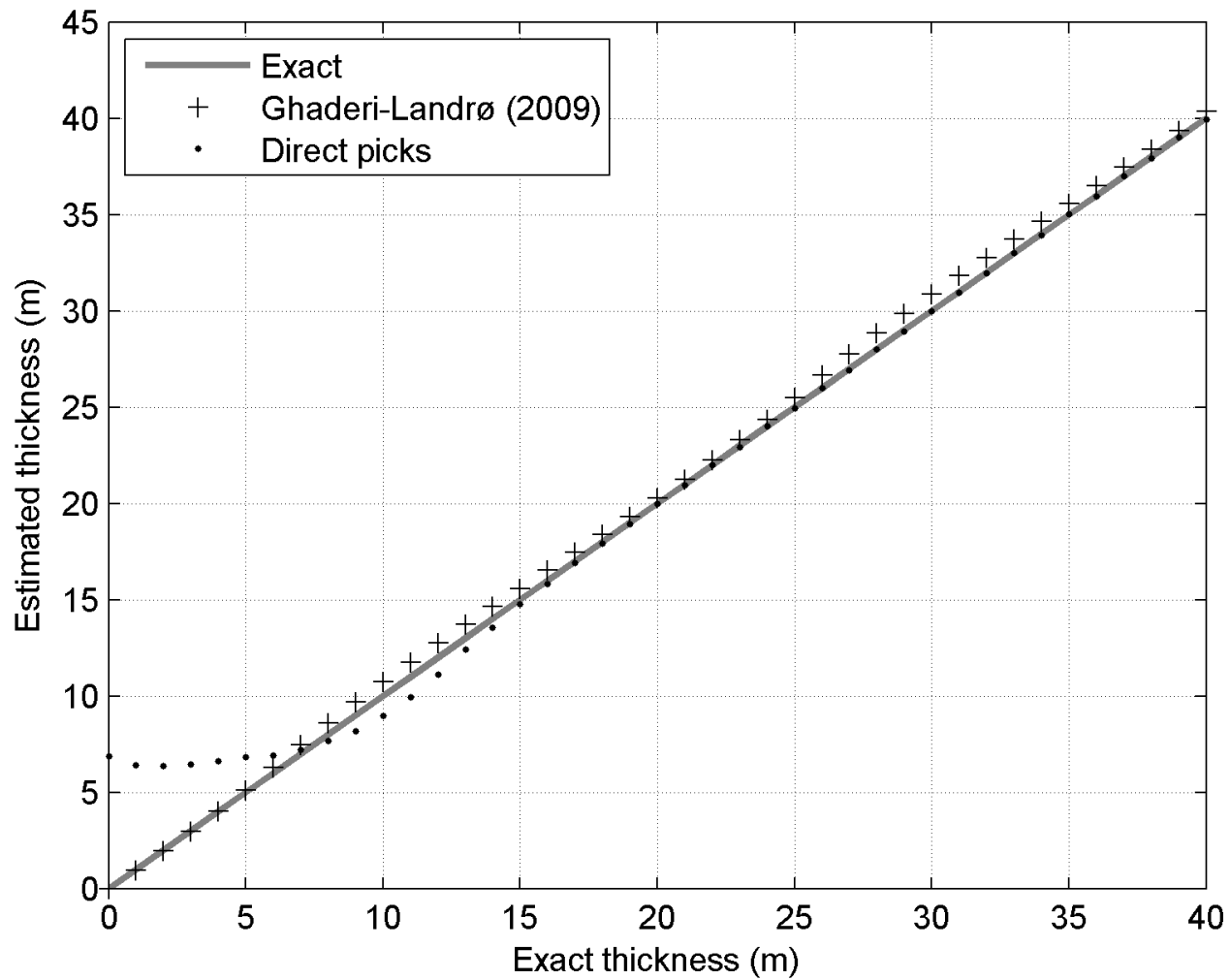
- One simple thickness estimate is based on direct picks and:

$$\Delta z = (t_2 - t_1) \Delta v$$

- Using Ghaderi & Landrø estimate:

$$\Delta z = -z \frac{v}{\Delta v} \frac{\Delta T}{T}$$

Estimation of thickness, given Δv



Observations

- Direct picking on the wedge leads to
 - an underestimate for a limited range of thicknesses above the tuning thickness
 - For thicknesses below the tuning thickness, it tend to a minimum as the Wedge gets thinner, leading to a gross overestimate.
- Ghaderi & Landrø method:
 - The result is better by picking traveltime below the event.
 - Knowing velocity change, measurements of travel time below the 4D seismic anomaly, can predict the thickness below tuning.

Simultaneous estimation of Δv and Δz

Ghaderi & Landrø, Geophysics (2009)

4D amplitude response of a thin layer :

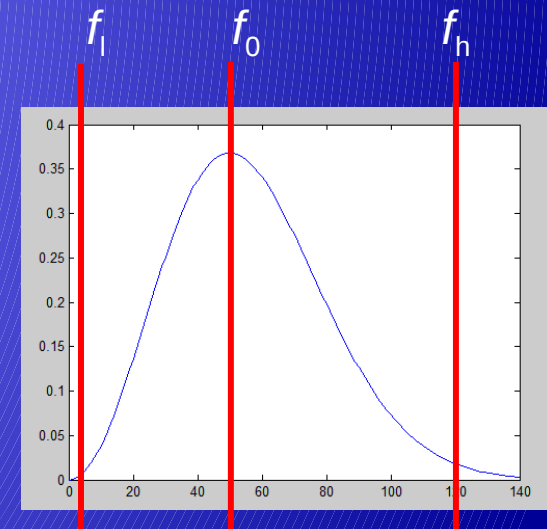
$$S_d(f_0) = -\frac{|P(f_0)|}{v_1 \cos^3 \theta} \frac{\Delta T}{T} \times \text{sinc}\left(\frac{\Delta T}{T} \frac{z_1 2\pi f_0}{\Delta v \cos \theta}\right)$$

Measure S_d and $\Delta T \Rightarrow \Delta v$

Propose to extend to all frequencies

$$S_d(f) = \left(\int_{f_l}^{f_h} S_d^2(f) df \right)^{\frac{1}{2}}$$

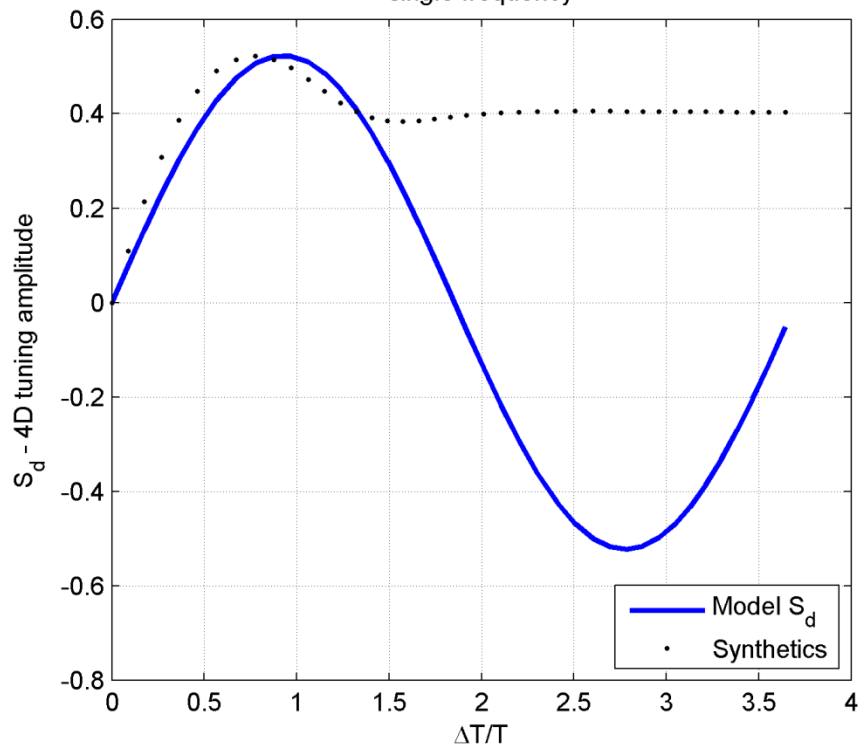
Modified expression from A.Barns, SEG Ext. Abs. 2004



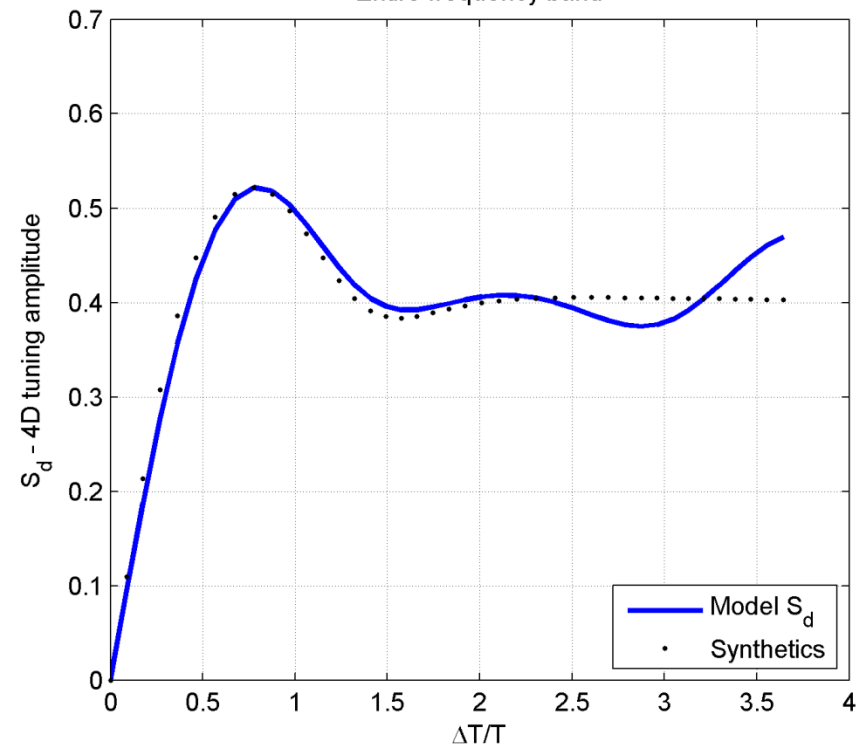
Frequency spectrum of Ricker, 50 Hz

Comparing S_d with synthetic modeling of the wedge

single frequency

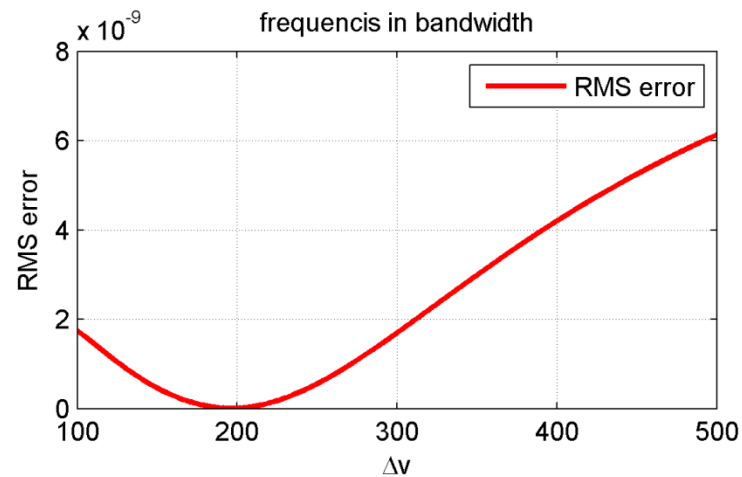
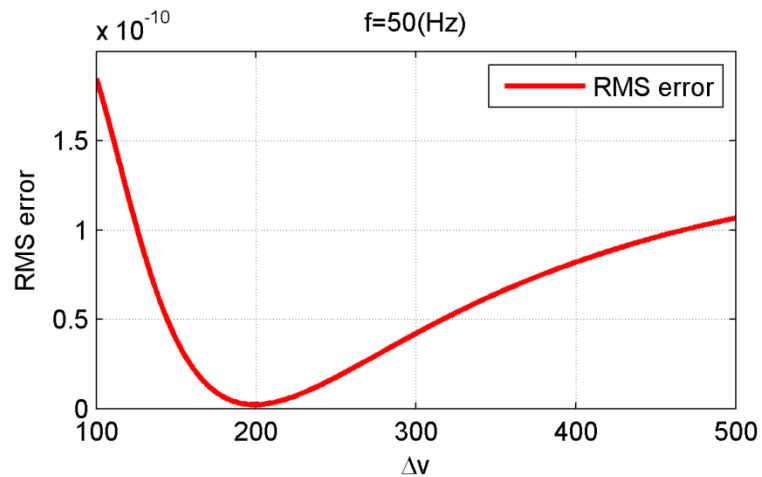
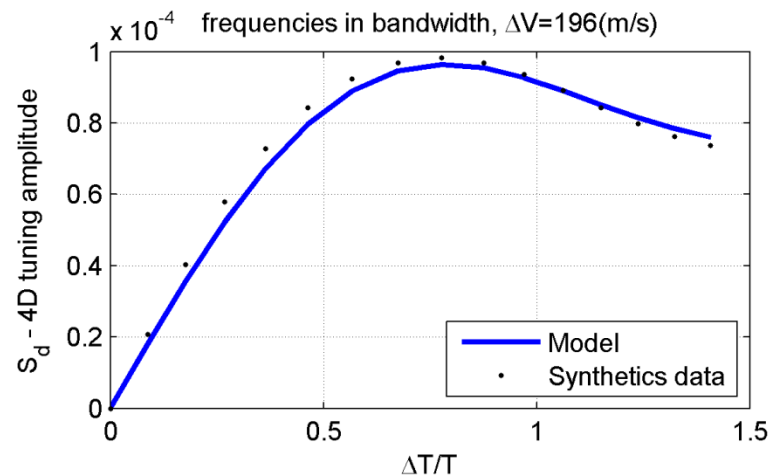
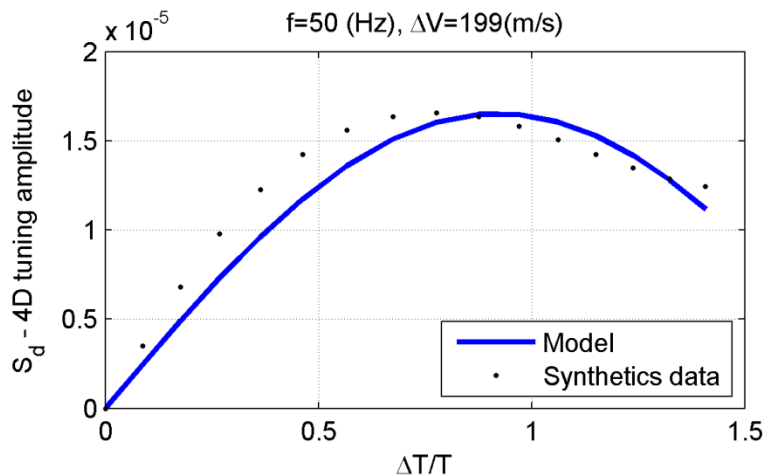


Entire frequency band

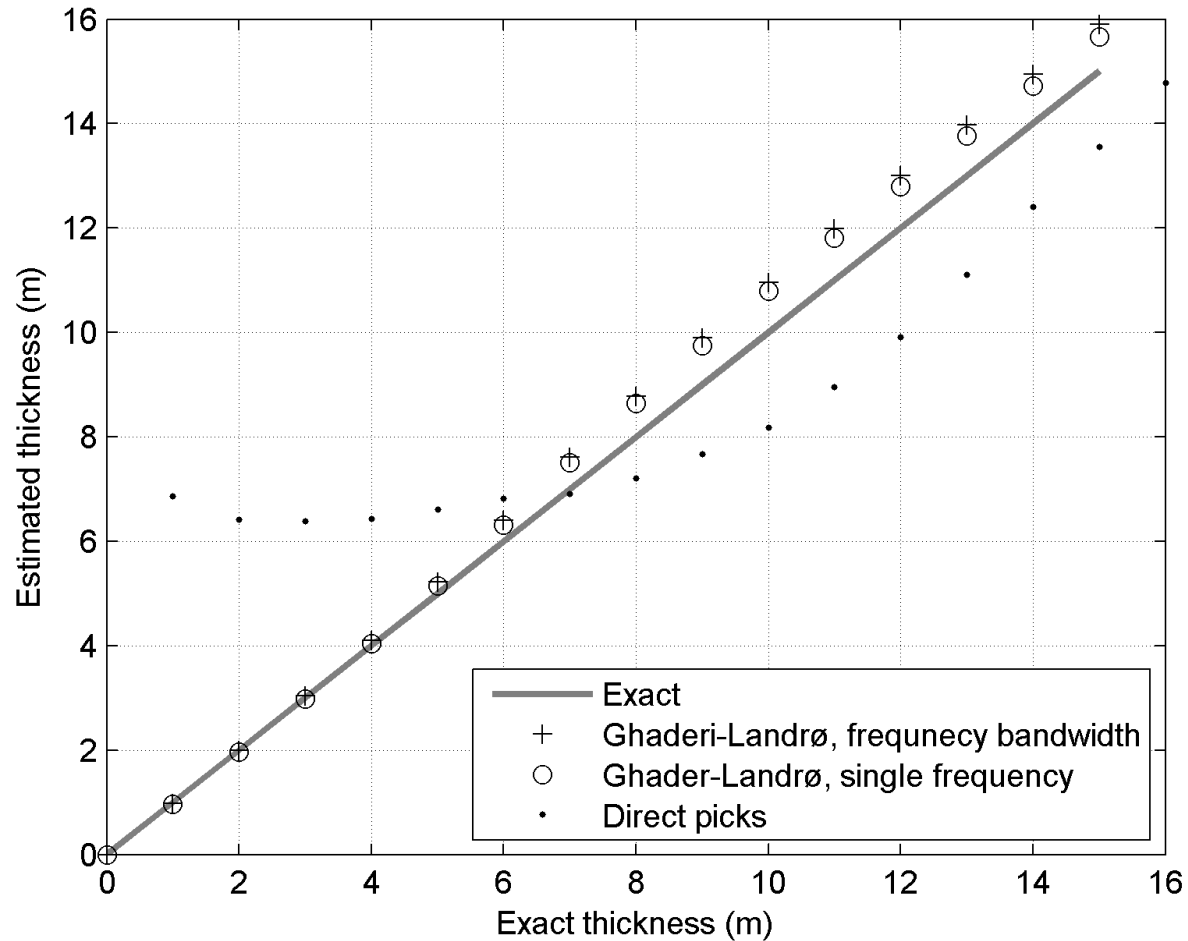


Inverting for Δv (exact answer: 200 m/s)

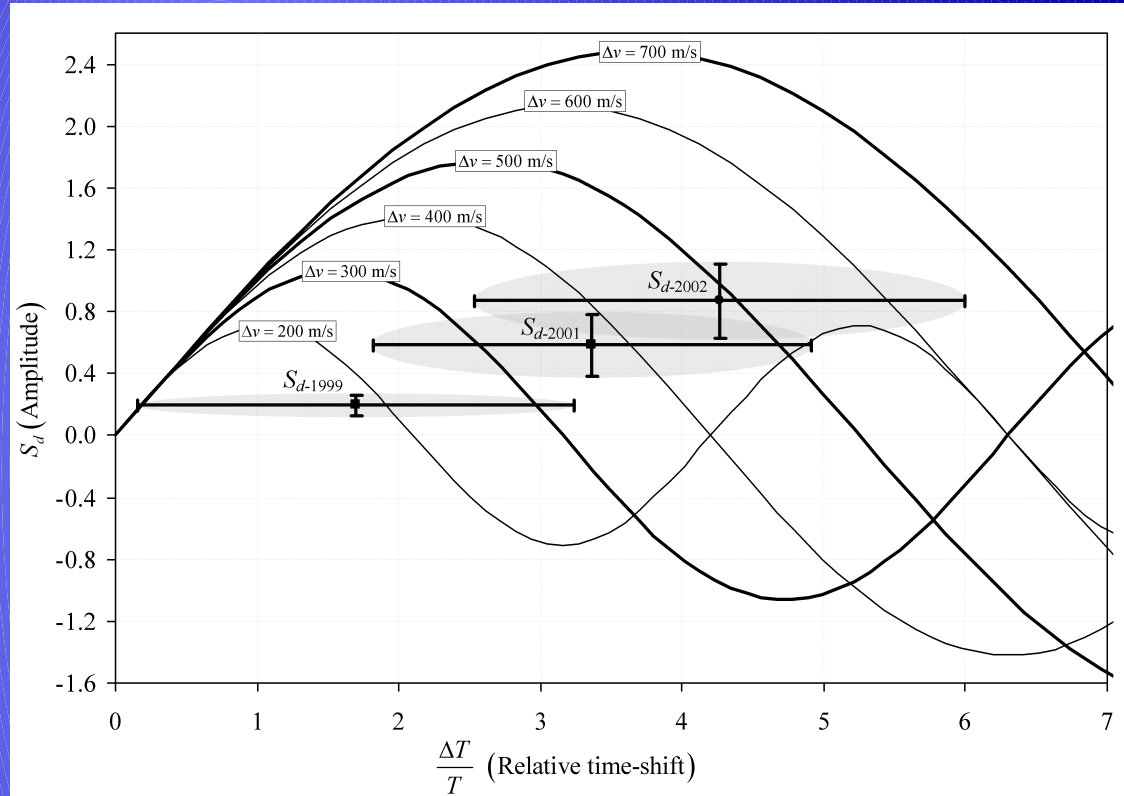
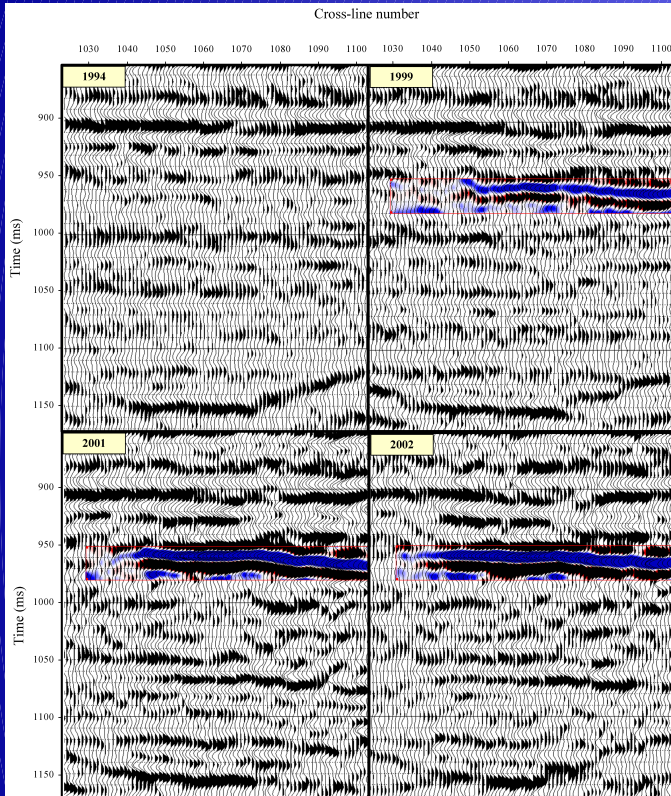
Least square method



Estimated thicknesses from inversion



Application to real data

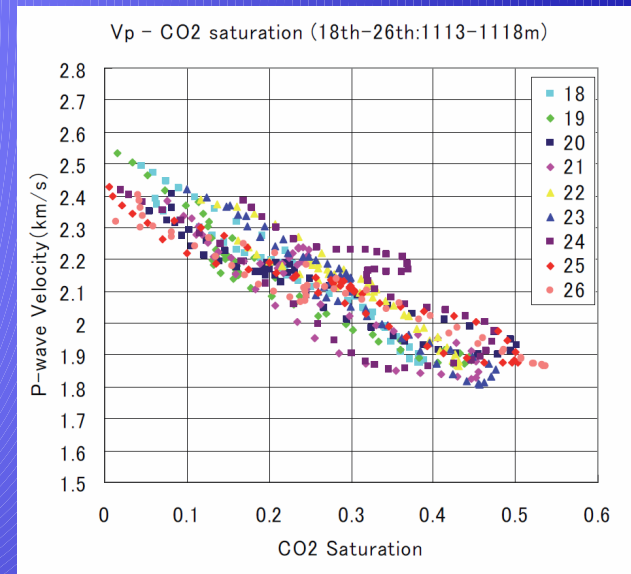
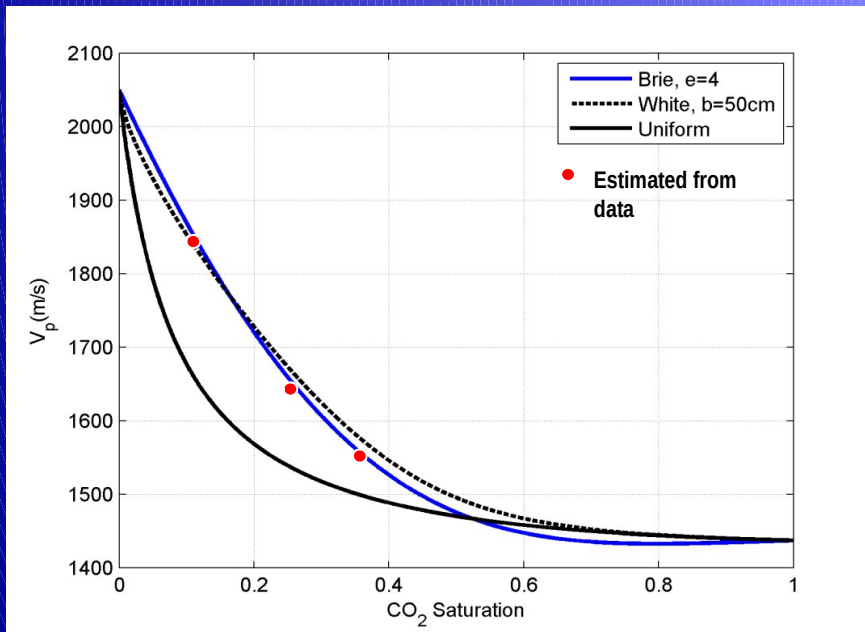


- Estimates of Δv and Δz
 - According to Ghaderi&Landrø
 - Values in parenthesis based on Gassmann and picked timeshifts

Monitor year	Δv (m/s)	Δz (m)
1999	200	15 (4)
2001	400	15 (8)
2002	500	15 (10)

So, what is happening?

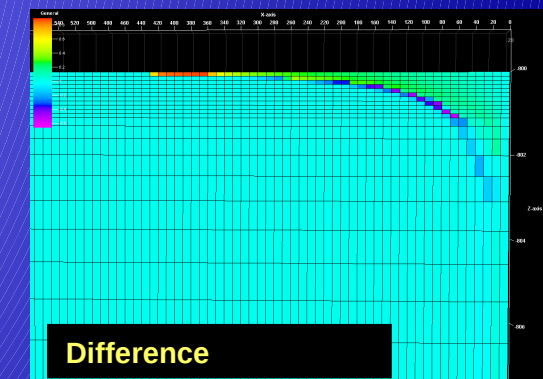
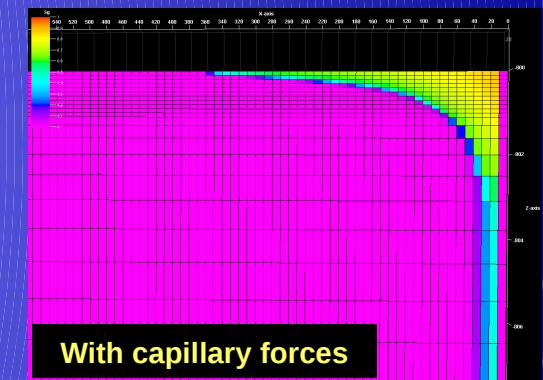
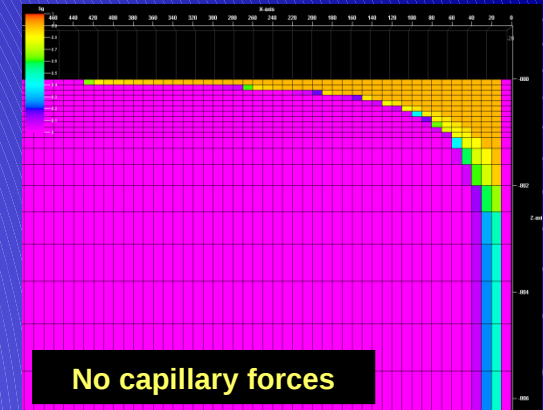
- Look at some rock physics models
 - Brie, describing the patchy saturation distribution
 - Gassmann-Wood, the uniform distribution
- Calibrating the patchy saturation with White's model



P-wave velocity and CO₂ saturation from Nagaoka field, Konishi et al, EAGE 2008

CO₂ distribution under thin shale layers

- Ongoing work
 - Ghaderi, Landrø and Lindeberg
- Mapping of the CO₂ 'finger' propagation, and variation of the thicknesses under shale
- Effect of capillary pressure on saturation distribution



Capillary pressure and transition zone

- Capillary pressure:
 - Difference between the two phase pressure

$$P_c = P_{fl_2} - P_{fl_1}$$

- Capillary transition zone:
 - The mixing zone that occurs between two phases (due to capillary pressure) when the fluids are immiscible

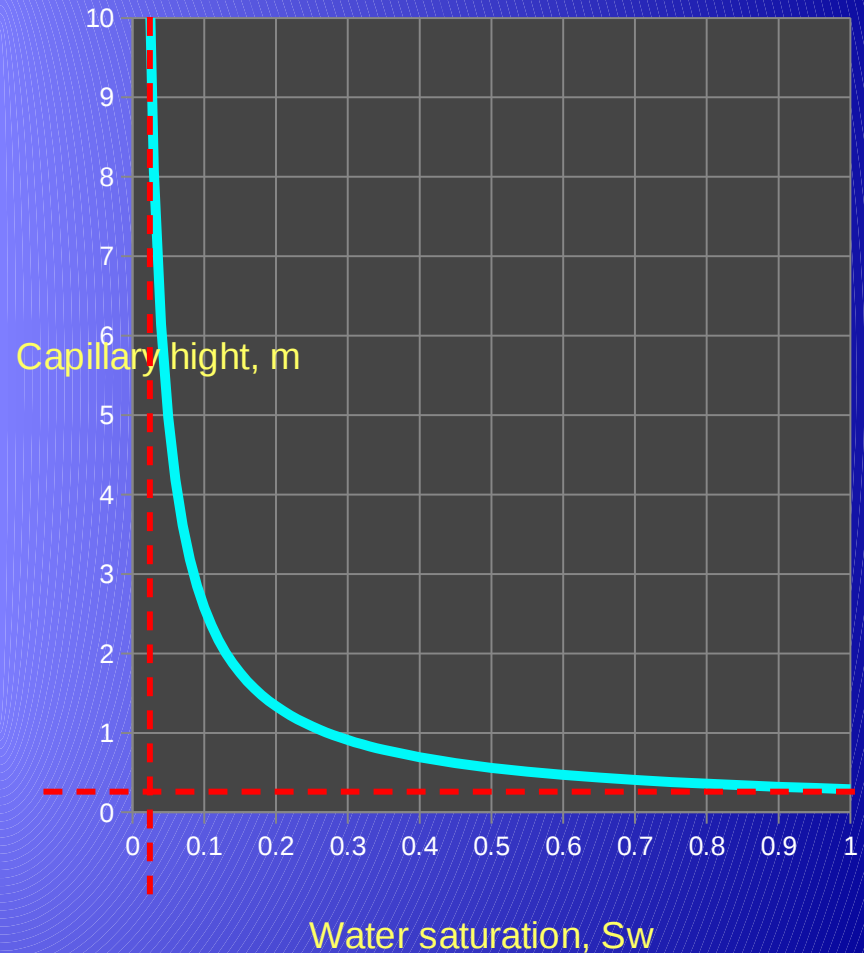
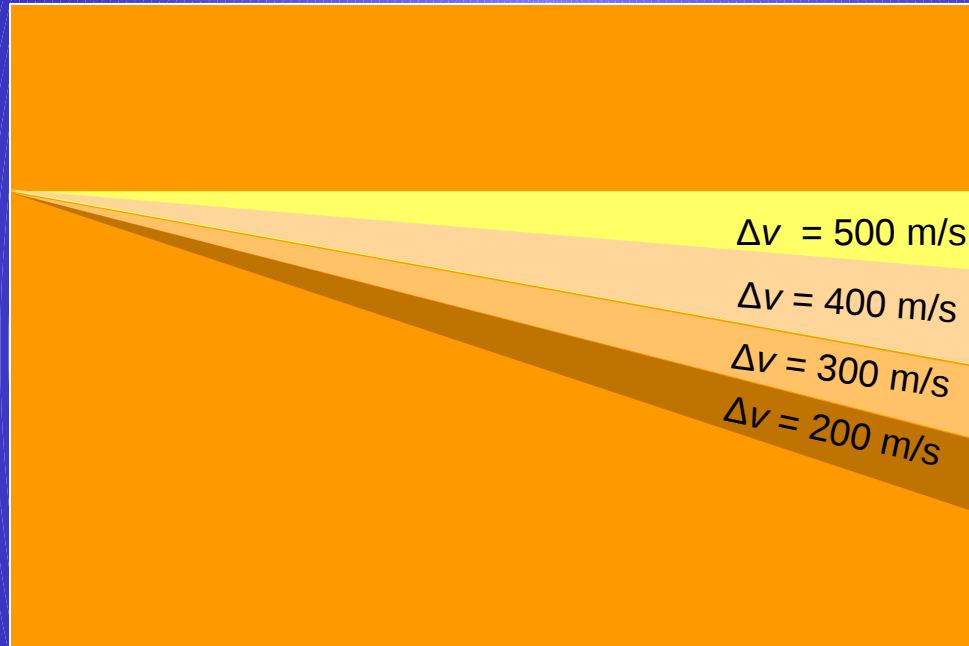


Figure: Erik Lindeberg, unpublished data Utsira

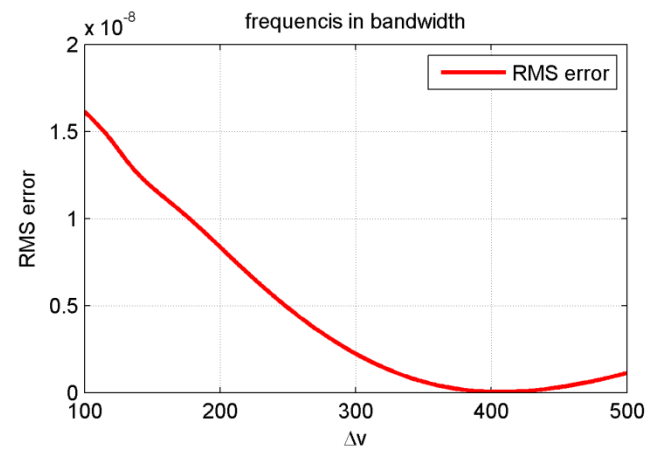
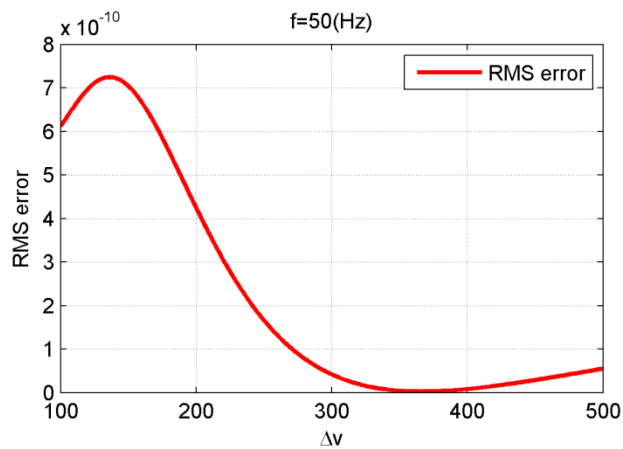
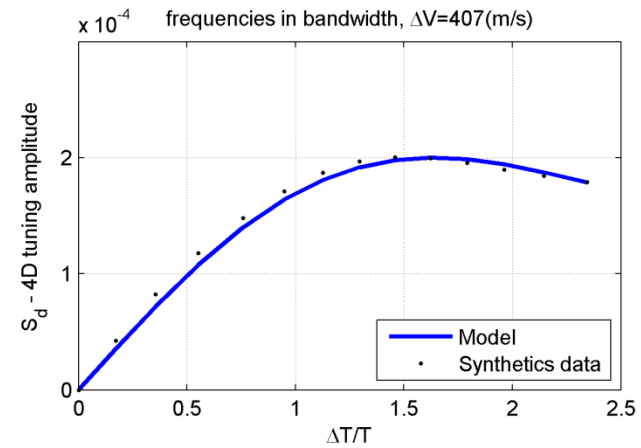
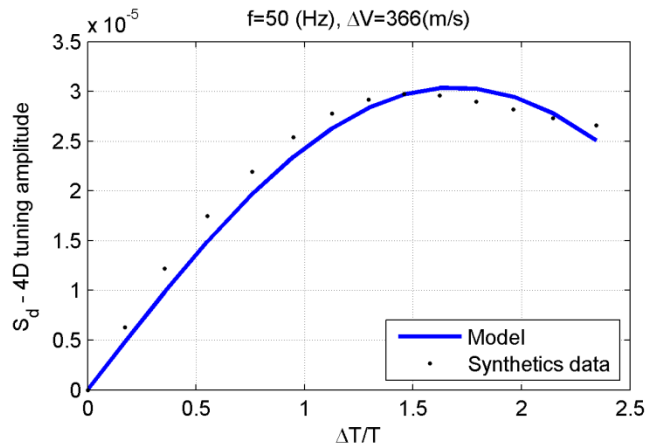
Modeling the transition zone



- 4 layer wedge model
- Progressively lower CO₂ saturations further down the model
- Average velocity change = 350 m/s

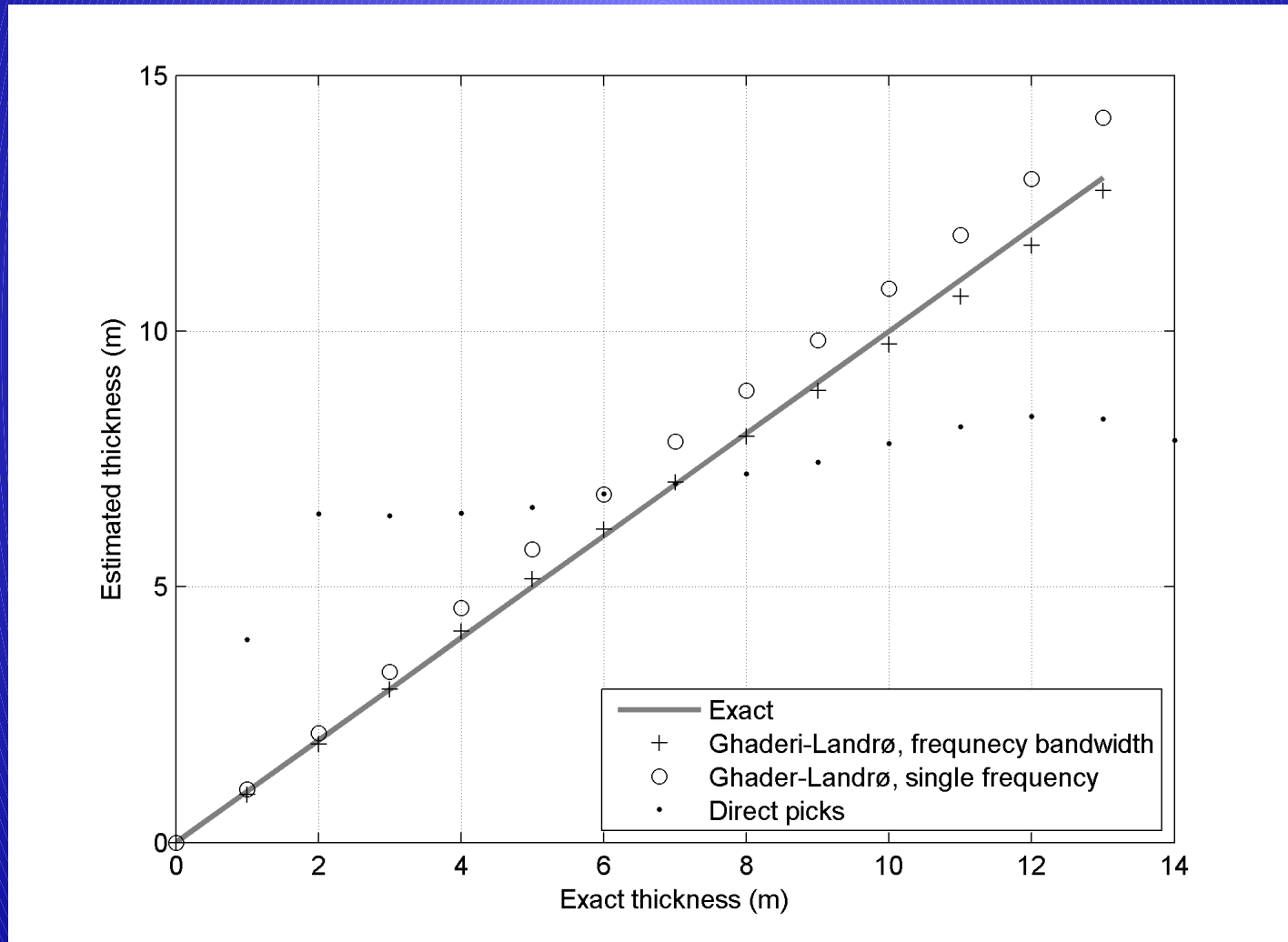
Inverting for Δv (average = 350 m/s)

Patchy saturation (4 layer model)



Estimated thicknesses from inversion

Patchy saturation (4 layer model)



Conclusion

- An efficient model is provided for estimating changes in velocity and thickness for CO₂ layers within and below the tuning thicknesses.
- A good match for homogenous saturation distribution
- A reasonable estimation with patchy saturation
- The scaling factor between the model and the data plays an important role in the RMS error estimation

Acknowledgement

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