

# 3D Elastic Time-lapse Full Waveform Inversion

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Norwegian University of  
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## Background

- During the last decade full waveform inversion (FWI) has proven to be a promising method for parameter model estimation
- Increase in computational power leads to an increase in problem size and type of wave phenomena included in the modeling
- Using FWI to reveal time-lapse effects directly in the parameter models is a rather new idea

## Objectives

- Apply elastic isotropic FWI on multi-component time-lapse data in 3D
- Invert for time-lapse changes in the P- and S-wave velocity models
- Investigate two data-difference based time-lapse FWI approaches

# Outline

1. Theory
2. From two to three dimensions
3. Examples
4. Conclusions

# A Quick Overview of Full Waveform Inversion

## Overall Goal

*Find a parameter model from which it is possible to create synthetic data that is close to some measured data*

Define  $S(\mathbf{m})$  as the measure between synthetic and measured data. The FWI is then the problem

$$\arg \min_{\mathbf{m}} S(\mathbf{m})$$

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Solved using an iterative method

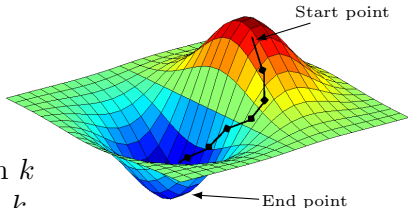
$$\mathbf{m}_{k+1} = \mathbf{m}_k - \alpha_k \mathbf{H}_k^{-1} \mathbf{g}_k,$$

$\mathbf{m}_k$  model at iteration  $k$

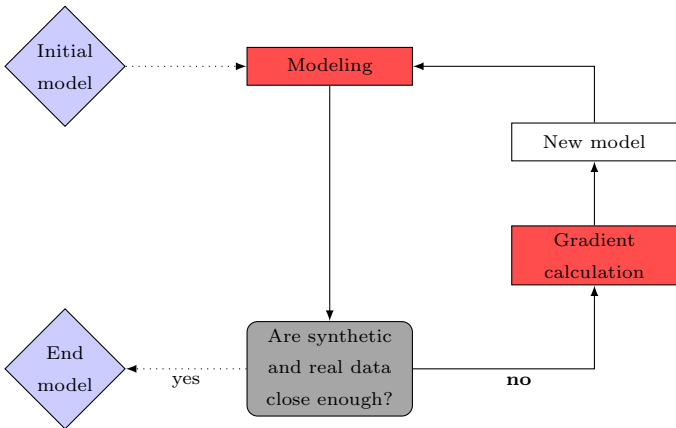
$\mathbf{g}_k$  gradient of  $S(\mathbf{m})$  at iteration  $k$

$\mathbf{H}_k$  Hessian of  $S(\mathbf{m})$  at iteration  $k$

$\alpha_k$  step length at iteration  $k$



# Schematic View of FWI



Synchronization

In parallel

# Time-lapse Full Waveform Inversion

## Goal

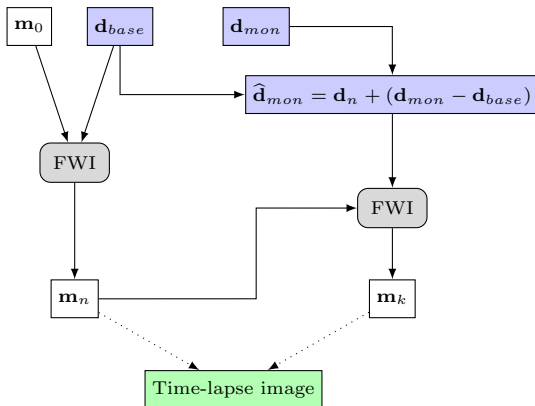
Use full waveform inversion to quantify changes in time for parameters affecting wave propagation.

May be used

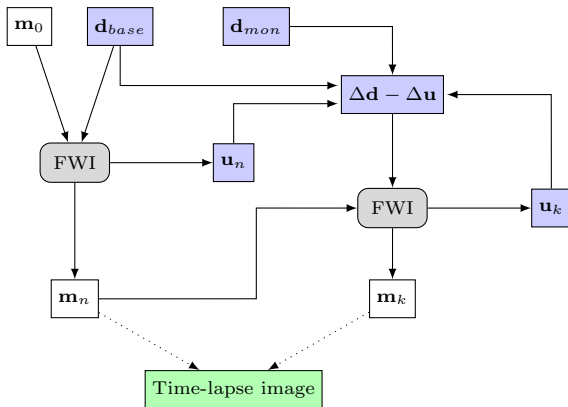
- as monitoring tool during the life-time of a reservoir
- to monitor injection of CO<sub>2</sub> in CCS experiments
- quantify amount of injected CO<sub>2</sub>



# Approach 1



## Approach 2



## TLFWI at a glance

- Need to perform at least two inversions  
→ Costly method

## TLFWI at a glance

- Need to perform at least two inversions
    - Costly method
  - The method may introduce artifacts in the time-lapse images due to for instance
    - non-linearity
    - ill-posedness
    - data differences
- Often called *time-lapse artifacts*

## From two to three dimensions

The real world is 3D, so we need to approximate it in 3D...

...but it is not easy

Some of the difficulties are

- More unknowns in the inverse problem, but not necessarily more data (i.e. more degrees of freedom, “more” ill-posed)
- Numerical methods scale extremely bad (i.e. long runtimes)
- Not everything can be done in memory

## The major problem: the gradient

$$g(\mathbf{x}) = \int_T \vec{\psi}(\mathbf{x}, t) \overleftarrow{\psi}(\mathbf{x}, t) dt, \quad (\mathbf{x}, t) \in (\mathbb{R}^3 \times T)$$

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- Large data transfer rates on the computer clusters are not possible

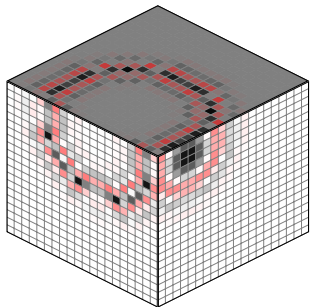


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- We need the wave fields at each time step to compute the cross correlation  
→ Impossible: Would require something like >1000TB of data storage for a small survey
- Large data transfer rates on the computer clusters are not possible
- **Solution:** Need to reconstruct the wave fields when they are needed, but how do we do that?

## Reconstruction of the wave fields

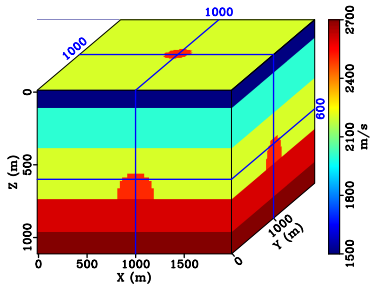
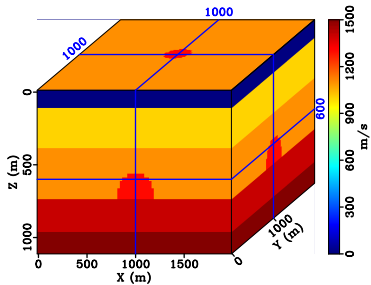


- Each boundary of the cube is stored to disc during the forward modeling
- To decrease data transfer, not all time-steps are saved
- In the backpropagation of the wave fields, we are reconstructing the forward field by feeding in each side of the cube, and use interpolation (to “reconstruct” the non-saved steps) where it is required

## Pros and cons

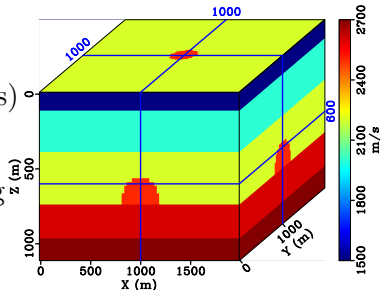
- We are keeping the need for storage at a minimum
- The necessary data transfer is “small”
- Back-propagation becomes (at least) twice as costly
- We are not able to reconstruct the field exactly, since we only have information on the boundaries

## Simple layered model

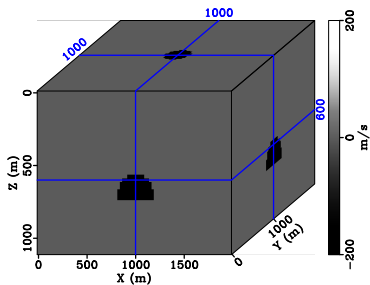
(a) True  $V_p$ (b) True  $V_s$

## Simple layered model

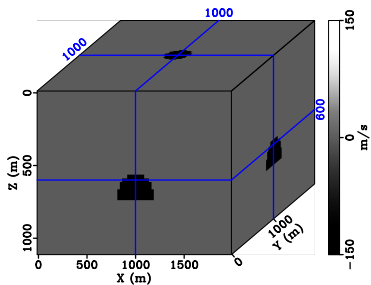
- Square receiver grid (4900 receivers)
- Receiver grid size:  $2 \times 2 \text{ km}^2$
- 324 shots with 100m shot sampling in x- and y-direction
- Grid sampling: 25m
- Source: Ricker wavelet with center frequency 6.0Hz



# Simple layered model

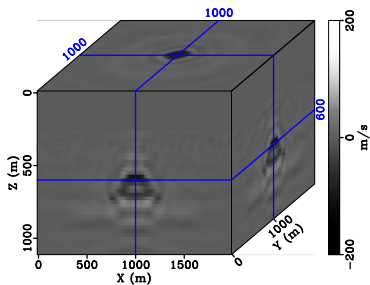


(a) Time-lapse  $V_p$

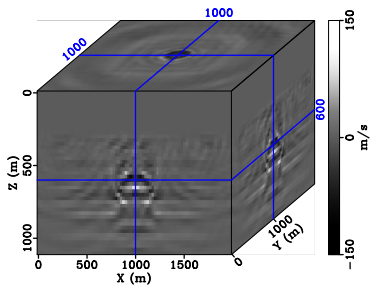


(b) Time-lapse  $V_s$

# Simple layered model: Approach 1

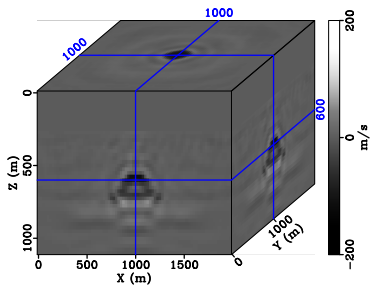


(a) Time-lapse  $V_p$

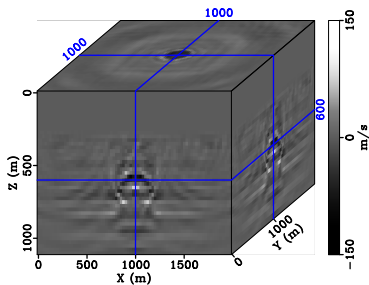


(b) Time-lapse  $V_s$

## Simple layered model: Approach 2



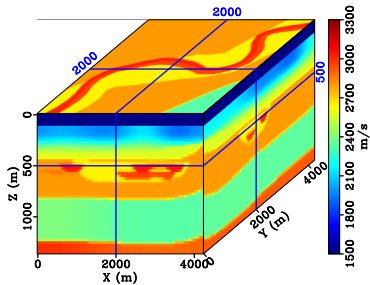
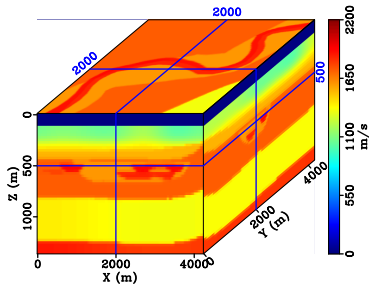
(a) Time-lapse  $V_p$



(b) Time-lapse  $V_s$

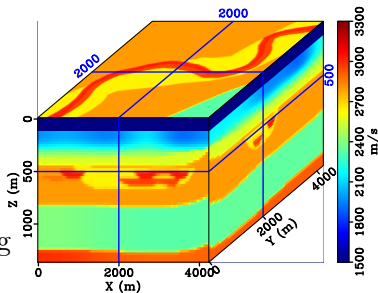


## Model with channel system

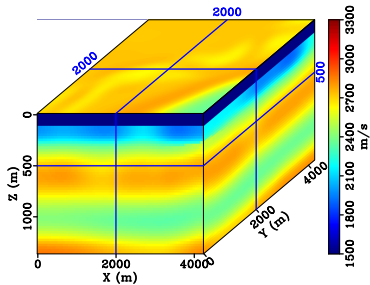
(a) True  $V_p$ (b) True  $V_s$

## Model with channel system

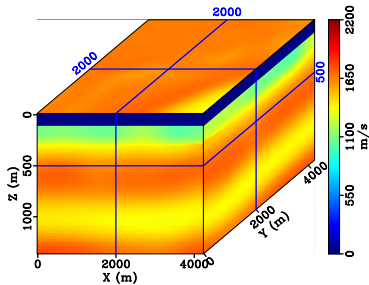
- 16 ocean-bottom cables
- Cable length: 4.0km
- Cable separation: 250m
- Total number of receivers: 2560
- 441 shots with 100m shot sampling in x- and y-direction
- Grid sampling: 25m
- Source: Ricker wavelet with center frequency 6.0Hz



# Model with channel system

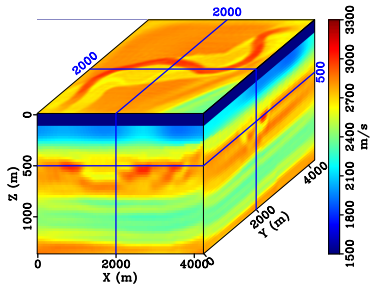


(a) Initial  $V_p$

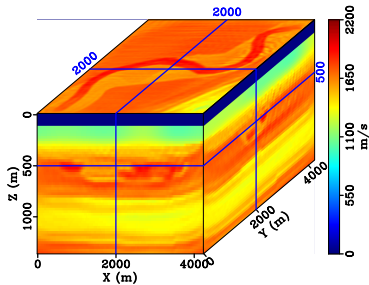


(b) Initial  $V_s$

# Model with channel system

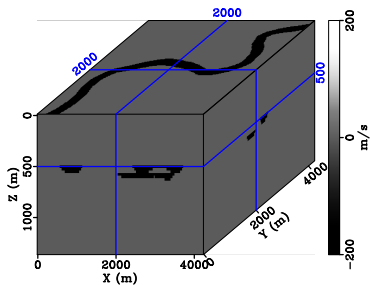


(a) Inverted  $V_p$

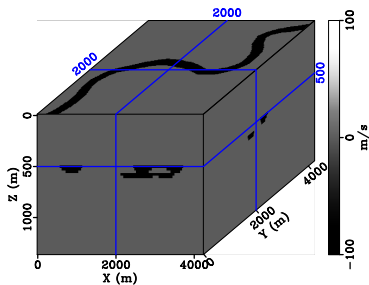


(b) Inverted  $V_s$

# Model with channel system

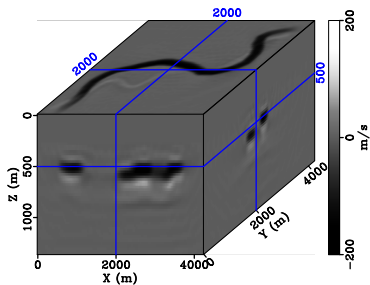


(a) Time-lapse  $V_p$

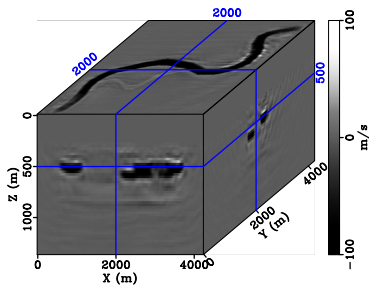


(b) Time-lapse  $V_s$

# Model with channel system: Approach 1

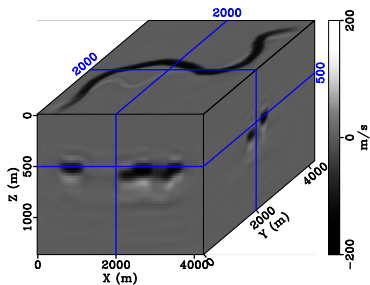


(a) Time-lapse  $V_p$

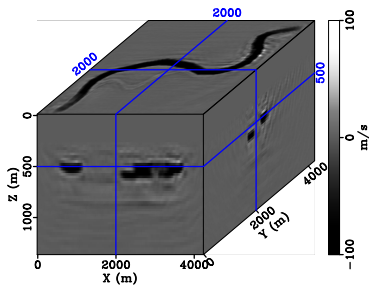


(b) Time-lapse  $V_s$

## Model with channel system: Approach 2



(a) Time-lapse  $V_p$



(b) Time-lapse  $V_s$

## Conclusions

- It is possible to do FWI in 3D within acceptable computing times
- FWI may be used to detect time-lapse effects in 3D
- Possible to invert for time-lapse changes in  $V_p$  and  $V_s$  using OBCs
- Small differences in the two time-lapse approaches



## Acknowledgements

We thank the Norwegian Research Council, BIGCCS, and the ROSE consortium for financing this research.